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## Multi-Ant Colony Heuristic Approach To Solving The Traveling Salesman Problem

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### Abstract

In this paper, we propose a new approach to solving the Traveling Salesman Problem (TSP), for which no exact algorithm in literature is known to find a solution in polynomial time. The proposed approach is based on Ants Colony Optimization. It puts several colonies in competition to find improved solutions (in execution time and solution quality) to large TSP instances, and allows efficient exploration of the range of possible solutions. The results of experiments show that the approach leads to better results compared to other heuristics from the literature, especially in terms of quality of solutions obtained and execution time.

### Keywords

Ants; Colony; Heuristic; Multi-colony; Traveling Salesman Problem.

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## I INTRODUCTION

The Traveling Salesman Problem, *TSP for short*, is one of the most common combinatorial optimization problems. TSP is a classical problem which, has been studied in the field of operations research and computer science since the beginning of the years 1950. Its statement is simple, and yet it remains one of the most difficult problems in operations research because it is considered NP-difficult [1]. As a result, a large number of techniques were developed to solve this problem. Much of the work on TSP is only motivated not by practical applications, but rather by the fact that it provides a framework ideal for study platforms of general methods that can be applied to a wide range of combinatorial optimization problems. In the TSP, a number of cities are indicated and linked to others by arcs. A salesman starts his tour from any city and travelling only once to each city, and returns to the starting city once again. The idea of the problem is to find the shortest route for the salesman from a given city, visiting  $n$  cities once and then finally returning to the city of origin.

Despite the multitude of methods available to solve the fundamental or applied TSP, none of the methods to date have been successful in resolving large instances [1, 2]. Indeed one is generally confronted with a combinatorial explosion and a limitation of computers memory resources when the size of the instances increases. However, problems related to TSP are increasing frequent in our society and must be resolved. For most TSP large instances, the optimal solution is seldom achieved even by the most effective and up-to-date heuristics. In this work, we are interested in solving TSP using Ant Colony Optimization (ACO). We propose a new ACO-based heuristic solution to this problem, using several colonies of ants.

In the rest of this paper, we present in section 2, we present the TSP, a mathematical formulation and we give some applications. Section 3 is devoted to the problem statement. A review of litterature on solving TSP by heuristics is given in section 4, Our contribution is presented in section 5. Section 6 is dedicated to experimental results, elucidated from tests and discussions that are performed with TSP instances from the TSPLIB library. Section 7 concludes our work.

## II THE TRAVELING SALESMAN PROBLEM

The Traveling Salesman Problem (TSP) is defined as follows: given  $n$  points (cities) and the distances between each point, find a path of minimum total length that passes exactly once through each point and returns to the starting point[1, 10]. The distance can also be seen as the cost in general. This combinatorial optimization problem, therefore, consists in searching for the best solution among several possible choices. However, it is easy to state but difficult to solve. The problem is to determine a turn or Hamiltonian circuit, *i.e.* passing once and only once through the  $n$  cities, and that is of minimum cost. It is classified as a NP-difficult problem [1, 2], because there is no known method of resolution that provides exact solutions in reasonable time for large instances (large number of cities) of the problem.

### 2.1 Formulation

Mathematically, the Traveling Salesman Problem can be formulated as follows: Let  $n$  cities and  $C_{ij}$ , the cost or distance corresponding to the trip  $i \rightarrow j$ . Let the variable  $X_{ij}$ , which is 1 if the tour contains the trip  $i \rightarrow j$ , and 0 otherwise. The problem is written as [6]:

$$\left\{ \begin{array}{l} MinZ = \sum_{i=1}^n \sum_{j=1}^n C_{ij} X_{ij} \\ \sum_{j=1}^n X_{ij} = 1 \quad \forall i \\ \sum_{i=1}^n X_{ij} = 1 \quad \forall j \\ \sum_{i \in Q} \sum_{j \in Q} X_{ij} \geq 1 \quad \forall Q \\ X_{ij} \in \{0, 1\} \forall i, \forall j \end{array} \right. \quad (1)$$

where  $Q$  represents a subset of  $1, \dots, n$  and its complement. The constraints (c) express that the permutation of the  $n$  cities must be a trick, *i.e.* no subtower can exist.

### 2.2 TSP Applications

Globally, the TSP provides an example of a study of an NP-complete problem whose solution methods can be applied to other discrete mathematics problems. It has several real life

applications even in its purest formulation, such as planning, manufacture of microchips, transportation, networks, computer wiring, vehicle routing, job-shop scheduling and logistics. For example, to find the shortest route for school buses or, in industry, to find the shortest distance that the mechanical arm of a machine must travel to drill holes in a printed circuit board.

### III THE PROBLEM STATEMENT

Existing algorithms for solving the TSP are not efficient enough. As the number of cities increases, the time or space required to solve the problem increases exponentially. The ant colony system solves the problem in a reasonable time and produces optimal solutions [2]. But when the dimension of the problem increases, it takes a long time to produce the result which is often not optimal. Thus, a modification is needed to solve large instances of the traveling salesman problem. In this work, we propose an approach for solving the TSP based on an ant colony optimization heuristic (OCF) in which several colonies are put in competition to find competitive results and able to minimize the known execution times or to give optimal or near optimal solutions to the instances whose solution remains difficult to reach by current methods. This new approach would allow to explore more efficiently the ranges of possible solutions, and to determine the satisfactory iteration techniques to build as quickly as possible the path leading to the optimal solution among thousands of possible paths. We are particularly interested in the multi-colony approach for several reasons: First, we wish to offer a greater exploration in terms of the possibility First, we want to offer a greater exploration in terms of deployment possibilities of the ants, which was not the case with a single colony. Second, we want to obtain a multiplicity of potential solutions to the problem during the optimization during the optimization process. Third, we want to obtain good solutions more quickly, due to the good solutions, because of the competition at the colony level.

### IV REVIEW OF ART

Several approaches ranging from exact to approximate methods, have been used to address the TSP. The simplest approach is the exact methods approach, which consists of listing all possible solutions and taking the best solution. These exact approaches are effective only for small instances where the explicit enumeration of solutions is possible in reasonable time [2, 8]. For large instances, most of the work is based on heuristic and meta-heuristic methods. In literature, there are two types of heuristics: Those that build a tour from scratch and those that are effective at improving an existing tour called Tour Enhancement Heuristics. Research into heuristic methods for solving TSP has included Dorigo and al results [2, 6] who, inspired by the collective behaviour of ants and their similarities with TSP, proposed the first ant colony algorithm for TSP: "*the natural Ant System (AS)*". Unfortunately, the purely probabilistic choice of the AS makes it less efficient in terms of diversification, thus favoring the risks of premature convergence. To improve the performance of AS on large problems, Dorigo et al [2], modify the AS transition rule to provide a better balance between exploring new areas of the solution space and exploiting the accumulated knowledge of the problem to intensify the solution. To this end, they introduce a new rule that depends on a  $q_0$  ( $0 < q_0 < 1$ ) parameter.  $Q$  is a randomly generated number, evenly distributed between [0.1]. With this new version, the choice of the next cities is not only probabilistic but also according to a  $q$  parameter. The resulting algorithm is called ACO [3]. Only ACO has shown some weaknesses in terms of exploring new areas and intensify solutions.

Beside these so-called construction heuristics, we have improvement heuristics such as the K-opt Heuristic ( $K = 2, 3, \dots$ ) which improves solutions by testing whether permutations of  $k$  paths produce more optimal rounds [1] or the heuristic of Lin-Kernighan (LK) [3] which is an improvement of the K-opt heuristic with  $k$  variables, or the Lin-Kernighan heuristic modified by Helsgaun (LKH). These heuristics efficiently improve solutions starting from an already known solution. Another class of heuristics is hybrid heuristics, which has become increasingly popular in recent years. These hybrid heuristics can be divided into several groups. On one side we have the hybridization of construction heuristics. between them, which consists in replacing a mechanism of one heuristic by a mechanism of another heuristic, to make up for what is limited in one by what is seen as an advantage in the other. In this regard, we can quote hybridization (AG-ACO) done in the works [4, 10]. On the other hand, we have the hybridization of construction heuristics (AG, ACO ...) with the Local Search heuristics or Improvement heuristic(LK, LKH, RL). An example of this technique is the one produced in [10]. This work proposes two hybrid heuristics named "AG-LK" and "ACS-LK" for solving the TSP. The first results from the hybridization of a Genetic Algorithm (AG) and the heuristic (LK) while the second hybridizes the ant colony algorithm (ACS) and the heuristic(LK). However, the authors use only one colony. The results obtained from this experiment have sufficiently demonstrated the efficiency of these hybrid approaches on several instances of TSP [10]. Unfortunately, the resolution time resulting from this experiment remains enormous. To improve the efficiency of the hybrid heuristics, Soh and al proposed and implemented in [4], two hybrid heuristics for TSP. The first one between a Genetic Algorithm (GA) and the heuristic (LKH) which is an improvement of LK by Helsgaun [3] and the second one between the Ant Colony System algorithm (ACS) and the heuristic (LKH). The resulting heuristics were called respectively "AG-LKH" and "ACS-LKH".

As we can see, due to its real life applications, solving the TSP is a permanent quest in the field of computer science, especially in operations research. Several authors have already worked in this direction by approaching various approaches, as this art review clearly shows. None of these methods has been able to overcome TSP. In the following section, we propose a new hybrid heuristic for TSP.

## V MULTI-ANT COLONY OPTIMIZATION APPROACH

### 5.1 Basic idea

To achieve the above objectives, we present the basic ACO proposed by Dorigo et al in [2]. We then modify this algorithm using multiple colonies. This leads us to a new version that we call Multi Ant Colonies Optimization (MACO). MACO proposes a new way to iterate ants from different colonies by defining more or less one iteration step to optimize the decision of the artificial ants to take preferably the right paths while avoiding the pitfalls of the local optimum. Strategies exchanges or communication between ants during their movements will be done in real time in order to help ants detect failures or wrong paths as quickly as possible. The updating of pheromones by ants is done as in the ACO [2].

### 5.2 Description or Mechanism of ACO Approaches

For the study, we consider that our problem is modeled in the form of a graph. Each node of the graph represents a city or task to be performed,  $d_{ij}$  the distance between cities  $i$  and  $j$ , and the couple  $(i, j)$  the path between these two cities. We will also consider the following:

- The ant represents a solution to the problem at hand;
- Computer pheromones are values associated with found solutions. These values depend on the quality of the solutions.

### 5.2.1 Step 1: Build a path for each ant (Solution)

To move from one node (city) of the graph to another, the iteration and movement of the ants is as follows: Initially (at time  $t = 0$ ), the algorithm sets  $m$  ants to  $n$  cities and the intensity of the trace for all city pairs  $(i, j)$  is set to a small positive  $To$  value in the pheromone matrix. A taboo list is maintained to ensure that a city cannot be visited twice during the same tour. Each ant  $k$  will therefore have its own list of  $V_k$ -taboo cities that will keep in memory the cities already visited. During an iteration of the algorithm, several ants take turns visiting a sequence of cities. One cycle ( $NC$ ) is finished by the time the last of the  $m$  ants have finished building.

At  $t \neq 0$ , from a sequence of cities already visited, each ant  $k$  chooses the next city to add to its list  $V_k$ -taboo using a probabilistic rule whose formula is given in equation (2).

$$\eta_{ij} = \frac{1}{d_{ij}}$$

$$P_{ij}^k = \frac{[\eta_{ij}]^\beta [\tau_{ij}(t)]^\alpha}{\sum_{u \in v_k} [\eta_{iu}]^\beta [\tau_{iu}(t)]^\alpha} \quad (2)$$

$$\tau_{ij}(t+1) = \rho P_{ij}^k(t) + \Delta \tau_{ij} \quad (3)$$

It's based on a compromise between visibility ( $\eta_{ij}$ ) and the amount of pheromone ( $\tau_{ij}$ ) present between  $i$  and  $j$ . The parameters  $\alpha$  and  $\beta$  are used to determine the relative importance of track intensity and visibility, respectively in the construction of a solution. This mode of iteration allows to privilege the shortest paths since ants will need fewer iterations to get to the end.

### 5.2.2 Step 2: Pheromone deposition and solution evaluation

When an ant moves from city  $i$  to city  $j$ , it leaves a certain amount of pheromone (value) on the arc  $(i, j)$ . A so-called pheromone matrix records information about the use of the  $(i, j)$  arc. At each stage of the round, the matrix is updated so that the greater the use of the  $(i, j)$  arc in the past, the more pheromone it has been used, the higher the probability that these arcs will be used again in the future. In this version of ACO, it says, there is an overall update of the pheromone trace intensity after each transition based on the assessment solutions found. For example, an ant moving from node  $i$  to  $j$  will be able to signal the following ants that are arriving in  $i$  if the displacement in  $j$  is a justified displacement. Equation (4) allows the pheromones to be updated.

$$\tau_{ij}(t+1) = \rho \tau_{ij}(t) + \Delta \tau_{ij} \quad (4)$$

### 5.2.3 Ant Colony Optimization algorithm (ACO)

The Ant Colony Optimization procedure is stated in algorithm **V.1**

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**Algorithm V.1** Ant Colony Optimization algorithm

---

Inputs  $m$  : number of ants per colony  $n$  : number of cities

```
1  Nc:=0
2  Initialize  Taboolist
3  Initialize  the matrix t(i,j)
4  While (Nc< Nmax) and (convergence not reached)
5  For i from 1 to n}
6      For j from 1 to m
7          Select the city j to be added to the current tour with the
8          formula (2)of probabilistic rule
9
10         Update locally the trace according to cities (i,j)
11     For each ant k
12         Evaluate the solution k for each of steps
13         Insert the solution k in the TabooList
14         Update globally the trace according to the best solution of the cycle
15  NC:= NC + 1
```

---

### 5.3 Multi-Ant Colony ACO Approach (MACO)

#### 5.3.1 Description of Idea approach MACO

Our approach called MACO is based on ACO approaches with the difference that MACO uses several ant colonies to allow a better exploration of the paths and optimizes the solutions found by another LKH improvement heuristic. Indeed, one of the major flaws in single colony [2] ACO is the difficulty for the colony to be able to explore efficiently the solution ranges especially for large instances. With MACO, we intend to solve the problem using several colonies.

We put several colonies of artificial ants in competition with each other depending on the size of the problem to win in terms of exploring solutions. In this way, the different colonies build their tour independently and collaborate through a kind of shared memory (global pheromone matrix) by stimulating a pseudo-parallelism to reach the common goal. Indeed, each colony is placed in a departure city, a travel step is authorized for each colony in turn. If an ant belonging to a colony during its iteration finds a better solution than the one known by the other ants in the different colonies, it quickly informs the others by updating the solution through the global communication matrix. To optimize the solution time, information about the pheromone matrix is given in real time immediately after each transition and not delayed.

The different colonies of the MACO algorithm are independent and build their solutions independently. while working closely together to achieve the final goal through communication mechanisms made possible by a communication matrix and values called pheromone.

Each colony (the ants) represents a solution to the problem being treated. The pheromone matrix is common to all colonies. It is used as a shared memory to allow the ants to communicate with each other to guide each other's search. This matrix is dynamic and is used by the colonies to incrementally build solutions. Each ant has a simple behavior, but the exchanges between ants are made by the intermediary of of the pheromone matrix, allow the gradual production

of a solution that is close, if not optimal. Ants communicate indirectly via dynamic modifications of the pheromone tracks and thus build a solution to a problem, based on their collective experiences.

### 5.3.2 Description of the steps of the MACO algorithm

**Step 1: Initializing the algorithm:** Initially, there's no pheromone on the arcs. The global pheromone matrix is initialized with 0 values for each pair of nodes. To initialize this matrix for the first time, the ants move randomly and in parallel per colony and build their first round. Each colony has its own local communication matrix. Once all the points have been visited, the ants return to their starting point (city). At the end of this first stage, the ants modify the global communication matrix by updating its entries with the best colony found (the best solution at the end of a tour).

**Step 2: Construction of solutions:** After the initialization phase, from this sequence of cities already visited, within the different colonies, the ants move this time on the different nodes of the graph according to a probability and therefore the equation is that of formula (3). It allows the colonies to favour the shortest paths during the different iterations. During a tour, each ant  $k$  of a colony  $L$  records in its taboo list (memory) the list of cities already visited. The new probabilistic formula for selecting a node by the ant  $k$  of colony  $L$  is defined by the expression  $p_{ij}^{k,l}$  (5). This probability is modeled on the one used in the ACO heuristic [2] described above.

$$p_{ij}^{k,l}(t) = \begin{cases} \frac{[\eta_{ij}]^\beta [\tau_{ij}(t)]^\alpha}{\sum_{u \in v_{k_l}} [\eta_{iu}]^\beta [\tau_{iu}(t)]^\alpha} & \text{if } j \in v_{k_l} \\ 0 & \text{else} \end{cases} \quad (5)$$

where  $v_{k_l}$  is the set of nodes (cities) not visited by ants in colony  $L$ .

### 5.3.3 Description of the Pheromone Matrix:

It's an array of  $i$  rows and  $j$  columns. At  $t = 0$  each entry of the matrix is initialized with the value 0.  $\tau_{ij}(t)$  represents the intensity of the pheromones on the  $(i, j)$  edge at the  $t$  cycle. During the construction of a path, after each transition of an ant  $k$  belonging to a colony  $L$ , ants from different colonies use directly the global communication matrix to communicate and immediately update pheromones as they evolve. The pheromone matrix evolution equation is described in equation (6) by :

$$\tau_{ij}(t+1) = \rho\tau_{ij}(t) + \Delta\tau_{ij} \quad (6)$$

Equation (6) is the same as equation (3) in ACO [2]. The main purpose of updating after each transition is to simulate a kind of parallelism in order to save computing time by giving the information on the global communication matrix in real time and not in delayed time. As in ACO, to reduce failures, pheromones evaporate[2]. The pheromones have to be reduced (value) on each path depending on the quality of the solution. This allows the ants after a certain time to avoid taking certain paths that can lead to failure. This characteristic is modeled via the parameter  $\rho$  ( $0 < \rho < 1$ ). The evaporation equation of the pheromone matrix is described by the formula(7).

$$\tau_{ij}(t+1) = (1 - \rho)\tau_{ij}(t) \quad (7)$$



The inverse of the distance between cities  $\eta_{ij} = \frac{1}{C_{ij}}$  called visibility is a static information used to guide ants to nearby cities and avoid cities that are too far away. The parameters  $\alpha$  and  $\beta$  are used to determine the relative importance of the ant's presence in the area. the intensity of the trace and the visibility in the construction of a solution. This is based on a trade-off between visibility ( $\eta_{ij}$ ) and the amount of pheromone ( $t_{ij}$ ) present between i and j at cycle t. These parameters are the same as those used in ACO[2]. Each colony corresponds to a potential solution to the problem, i.e. a complete tour. When recovering a solution, each ant in the different colonies provides part of the solution to the problem. The assembly of the different sub-solutions provides the solution to the original problem. If at a given time t all the ants in a colony have the same solution, the iterations are stopped. The procedure finally obtained for optimization by multi-colony ants is the algorithm V.2

---

**Algorithm V.2** MACO Algorithm.

---

Inputs m: number of ants per colony, L: Number of colonies, n: number of cities

---

```

1 Nc:=0
2 Dij:=0      // Global matrix
3 dij:=t0     // local matrix of pheromones
4 Initialize t0 // with each ant's home city
5 Place each colony randomly in a starting point (city)
6 For K from 1 to m
7   Construction of a tour by each ant at random
8   Gradual deposition of pheromones in the dij matrix of each colony
9   Evaluation and selection of the best colony
10  Initialize the Dij matrix with the best colony
11  While(Nc<Nmax)
12    For i from 1 to n
13      For j from 1 to L
14        For K from 1 to m
15          Select the city Vi to be added to the current tour with formula(1)
16          Evaluate the solution of the ant K on route(i,j)
17          Update globally the trace according to city pair(i,j) if it's better than
18          the previous ants according to formula 5 and 6 (evaporation)
19          Insert as you go (i,j) in the taboo list so as to construct gradually solution K
20  S:= Best solution (Each colony provides a partial solution)

```

---

Complexity of MACO Algorithm The study of the complexity of our MACO algorithm is done by subdividing the algorithm into 4 sections to calculate the complexity.

**- Initialization:** Since we have assumed a total interconnection between cities, we have a complexity of  $O(n^2 + m \cdot L)$ .

**The Constructions of the path, and progressive deposition of pheromones plus evaluation of solutions:** Complexity  $O(n^2 \cdot m \cdot L)$ .

**Pheromone Evaporation:** in the Complexity is  $O(n^2)$ .

**- Evaluating paths after each transition:** Complexity  $O(n \cdot m \cdot L)$ . For the L colonies, we compare the towers of m ants in each colony. Each tower has a length of n elements.

In summary, we obtain the global complexity by adding the complexity of step 1, to the product of the total number of rounds (i.e. NCmax) by the global complexity of steps 2 to 4. This gives

$O(n^2 + m.L + NCmax.n^2 . m.L)$ .  
or finally  $O(NCmax . n^2 . m.L)$

## VI EXPERIMENTAL RESULTS - DISCUSSIONS AND INTERPRETATION

In order to demonstrate the performance of the approach we propose, we perform computer simulations on a machine with the following characteristics: Intel Dual core, 2Ghz processor, 2Gb RAM, Kali Lunix operating system.

In all the experiments in this section, we define as starting parameters in a first time  $m = 100$  and  $L = 10$ , then in a second time  $m = 100$  and  $L = 50$ . These experiments are carried out on the reference problems Lin105, Pr124, LIN318, att532, ALi535, rat783, std1655, Vm1748, pr2392, Usa13509 and pla33810 all from the TSPLIB library[5] with available TSP instances.

With the same conditions, we subjected them to our heuristics and compared the results obtained with the best current heuristics for TSP at the time of testing. Several simulations (100 in total) allowed us to assess the relevance and effectiveness of our approach. By making a comparative study between the MACO heuristic with the basic AS heuristic and ACS obtained by Dorigo [1] as well as ACS-LK one of the best heuristics for the TSP from the literature proposed in [10] or those obtained in [4] (AG -LKH, ACS -LKH) and under identical test conditions we obtain the results of Figures 1, 2, 3 and 4 respectively.

AS				
INSTANCES OF TSP	Size	best solution	Time	success/100
etl51	51	252,46	/	/
st70	70	675	/	/
LIN 105	105	ND	/	/
Pr124	124	ND	/	/
LIN318	318	ND	/	/
Attr532	532	ND	/	/
attr535	535	ND	/	/
Rat783	783	ND	/	/
std1655	1655	ND	/	/
Vm1748	1748	ND	/	/
pr2392	2392	ND	/	/
Usa13509	13509	ND	/	/
Pla33810	33810	ND	/	/

Figure 1: Results AS

In the results presented in figure 3, the green lines represent the cases where the gains observed with MACO are related to costs and turnaround times. The brown lines symbolize the cases where the observed gain is only at the level of execution time, the optimal solution having already been reached. We note a better execution time for MACO compared to those obtained so far with the best algorithms (ACS-LK, AG-LK, ACS-LKH, ACS) at the time of the tests. We also obtain a better and always optimal cost compared to the best solutions known so far with

INSTANCES OF TSP	TAILLE	ACS- départ		
		best solution	Temps	réussite/100
d198	198	585000	/	15
pcb442	442	595000	/	51
Attr532	532	830858	/	28
Rat783	783	991276	/	9
fl 1577	1577	942000	/	22

Figure 2: Results ACS-DORIGO [2]

MACO					ACS_LK				
Instances of TSP	Size	best solution	Time	success/100	Instances	Size	best solution	Time	success /100
LIN 105	105	14379	0,03	100	Lin 105	105	14379	0,03	100
Pr124	124	58537	0,03	100	Pr124	124	58537	0,92	100
LIN318	318	42029	0,34	100	Lin318	318	42029	0,8	100
Attr532	532	276787,7	5,3	100	Att532	532	276787,7	13,26	100
attr535	535	202339	1,94	100	All535	535	202339	30,94	100
Rat783	783	88060	0,28	100	Rat783	783	88060	0,28	100
std1655	1655	6218,6	72,18	100	std1655	1655	62128,6	73,28	100
Vm1748	1748	336557	41,86	100	Vm1748	1748	336557	71,86	100
pr2392	2392	378032,2	0,97	100	Pr2392	2392	378034,25	1,19	90
Usa13509	13509	19849706	21103,3	100	Usa13509	13509	19984330	1864,74	84
Pla33810	33810	ID	/	/	Pla33810	33810	ID	/	/

Figure 3: Comparison of MACO algorithm with ACS-LK hybrid algorithm

deviations ranging from 0.1 to nearly 1000 distance units on some reasonably sized instances (Usa13506, Pr2392...). The numbers in brackets represent the execution times.

Figures 5 and 6 present a comparison of the performance of our approach compared to the improved AG -LKH and ACS -LKH approaches, using the above-mentioned reference problems and terms of solution quality and runtime respectively.

The results of our experiments clearly show the superiority of our algorithm over others, especially in terms of solutions quality and in terms of time taken to reach this optimal solution. However, for some of the instances for which we do not yet know a solution, our approach could not give an optimal solution.

Instances of TSP	Size	ACS_LKH			AG_LKH			MACO		
		best solution	Time	success/100	best solution	Time	success/100	best solution	Time	success/100
LIN 105	105	14379	0,03	100	14379	0,03	100	14379	0,03	100
Pr124	124	58537	0,92	100	58537	0,46	100	58537	0,03	100
LIN318	318	42029	0,8	100	42097,4	1,6	100	42029	0,34	100
Attr532	532	276787,7	15,62	100	27691	13,74	100	276787,7	13,26	100
attr535	535	202339	30,94	100	202339	38,26	100	202339	1,94	100
Rat783	783	88060	0,28	100	88060	0,32	100	88060	0,28	100
std1655	1655	62128,6	73,28	100	63128	151,5	100	6218,6	72,18	100
Vm1748	1748	336557	71,86	100	336557	111,07	100	336557	41,86	100
pr2392	2392	378034,3	1,19	90	378034,8	1114,1	80	378032,2	0,97	100
Usa13509	13509	19984330	2113,3	100	ID	ID	ID	19849706	21103,3	100
Pla33810	33810	ID	/	/	ID	/	/	ID	/	/

Figure 4: Comparison MACO algorithm with ACS-LKH and AG-LKH algorithms

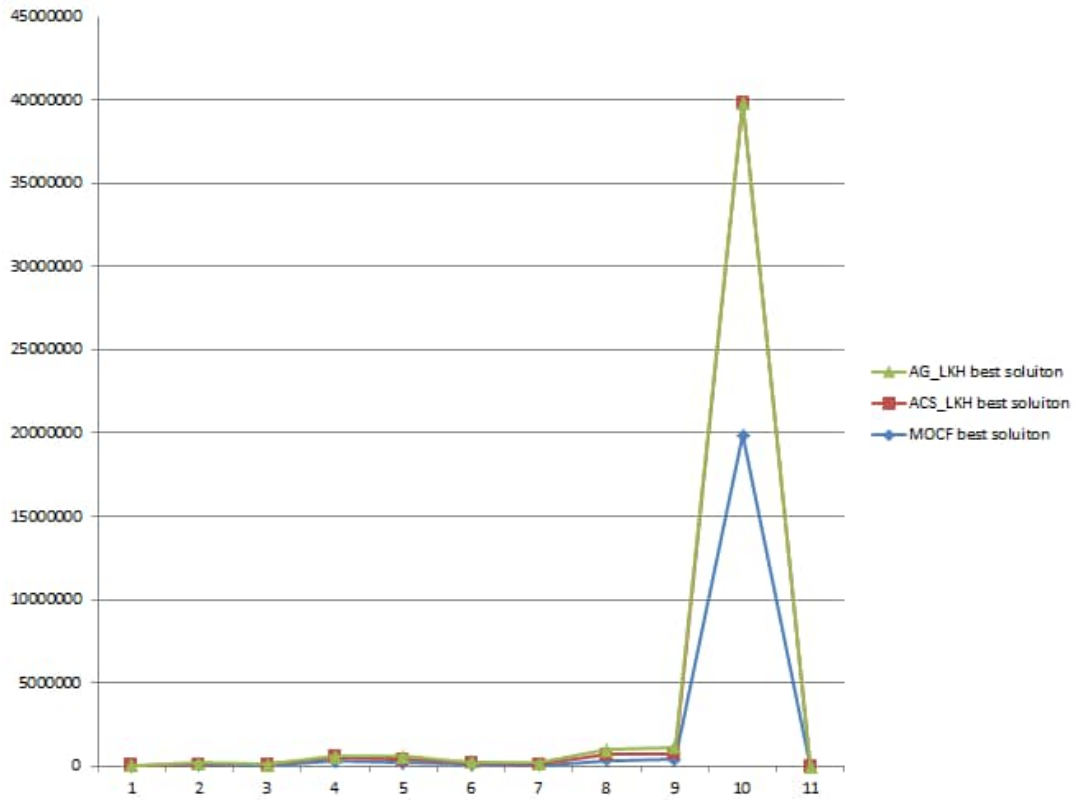


Figure 5: Comparison MACO, AG-LKH, ACS-LKH in terms of solution quality

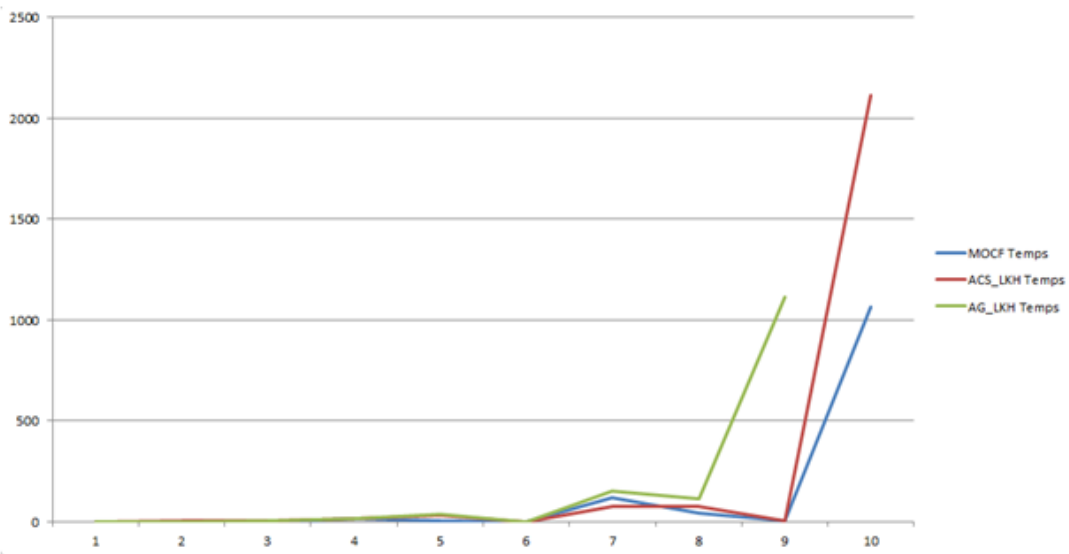


Figure 6: Comparison of MACO, ACS-LKH, AG-LKH running times

## VII CONCLUSION AND PERSPECTIVES

In this work, we proposed a new multi-colony ant heuristic (MACO) to improve the search for optimal solutions to TSP and in optimal time. The proposed MACO algorithm is based on the use of several ant colonies. It shows clear improvements in both cost and execution time, proving that it is much more competitive than the best time heuristics for TSP. A limitation related to our multi-colony approach will probably be the increase in execution time needed to find a solution in some cases, or the use of much more resources (memory and processor). We believe that parallelization of the ACS [2] or MACO algorithm would be a considerable contribution to metaheuristics to reduce TSP resolution times.

## VIII BIOGRAPHY

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