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Simulation of an Ondes Martenot Circuit

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Abstract—The ondes Martenot is a classic electronic musical instrument based on heterodyning processing. This paper proposes a power-balanced simulation of its circuit, in order to synthesize the sound it produces. To this end, the proposed approach consists in formulating the circuit as a Port-Hamiltonian System, for which power-balanced numerical methods are available. Observations on numerical experiments based upon this formulation allow simplifications of the circuit in order to achieve real-time computation in home-studio conditions.

Index Terms—Electronic music instrument, non-linear, power-balanced, simulation

I. INTRODUCTION

AS the audio industry is evolving from analog to digital, the preservation of analog machines and instruments—and with them, that of the craft of generations of engineers—is proving critical [1], [2]. The concern has been especially raised about the ondes Martenot; invented in 1928 by Maurice Martenot, this pioneer electronic musical instrument [3] is no longer produced in its original form and some of its components are now obsolete, such as specific triode vacuum tubes. A solution consists of modeling its circuit and building a real-time virtual instrument, so that the community of composers, musicians and musicologists may have access to virtual facsimiles.

Several techniques are available to build virtual analog instruments (for a review, see [4]–[6]). They include Modified Nodal Analysis [7], [8], the Nodal DK method [9] (for audio applications, see e.g. [10], [11]), Wave Digital Filters [12] (see e.g. [13]–[19]). Real-time simulations of circuits with vacuum tubes have been derived from such methods [20], [21] or from time-continuous state-space representations combined with numerical schemes [22]–[25]. The approach used in this paper is based on a state-space representation, which satisfies the power balance of the physical system structured into conservative, dissipative and external parts, known as Port-Hamiltonian Systems (referred to as PHS) [26], [27]. This formulation can be combined with numerical methods that preserve the power balance structure (and passivity) in the discrete-time domain for both linear and non-linear systems. This has proved to be relevant for simulations of audio (electronic or multi-physical) systems [28]–[31]. In a previous paper [32], the first stage of the ondes Martenot circuit (a variable oscillator) has been modeled and simulated using this method, with a special focus on electro-mechanical power balance. This paper addresses the full modeling and simulation of the circuit of the ondes Martenot No. 169, which is composed of 5 coupled stages. Moreover, analyzing numerical experiments allows some model simplifications, which in turn grant access to real-time.

This paper is organized as follows. Section II describes the history and the composition of the ondes Martenot as well as the way the instrument is played. In section III, the PHS formalism is briefly recalled and illustrated with a simple example. In section IV, each isolated stage is first separately modeled as a PHS and the coupling of the stages is then addressed. In section V, the physical parameters for simulation are examined and set. Section VI is devoted to off-line power-balanced simulations of the complete circuit. Finally, in section VII, simplifications are proposed based on the analysis of numerical experiments. They lead to a reduced order PHS from which a real-time audio plug-in is built for the sound synthesis.

II. HISTORY, ORGANOLGY, CIRCUIT AND PRINCIPLE

A. History

The advent of electrical engineering marked a disruption in many industrial domains, amongst them musical instrument making. Providing both new timbres and new playing modalities, it gave the 20th century instrument corpus its singularity. Nonetheless, instrument making is not immune to technological obsolescence, and only few of these innovative instruments are still played today. This is the case of the ondes Martenot; only 264 ondes were built, but around 1500 pieces were composed for it [33]. As they were handmade and subjected to successive enhancements, each ondes is unique and identified by a reference number. The considerable task of cataloguing and evaluating the condition of the remaining instruments has been achieved by the Musée de la Musique in Paris [34]. It appears that for some of the ondes, making them playable again would necessitate irreversible interventions. This poses a big deontological dilemma from the preservation point of view and argues in favor of building facsimiles.

B. Organology

This paper focuses on the ondes No. 169, manufactured in 1937, and kept in the Musée de la Musique in Paris. This specimen has a great heritage value, particularly because of its electronic circuit with vacuum triodes. Also, it is kept in playing conditions and is fully documented [35]. It is based on heterodyne processing, like the Theremin [36] and the Trautonium [37]. It generates a harmonic signal which feeds specific loudspeakers (called *diffuseurs*, Fig. 1a). The player controls the pitch with a sliding ribbon (continuous pitch change) or—in later versions of the instrument—with a mobile keyboard (discrete pitch change and vibratos, Fig. 1b). The loudness is controlled with an intensity key, by pressing a small bag containing a mixture of conductive and insulating

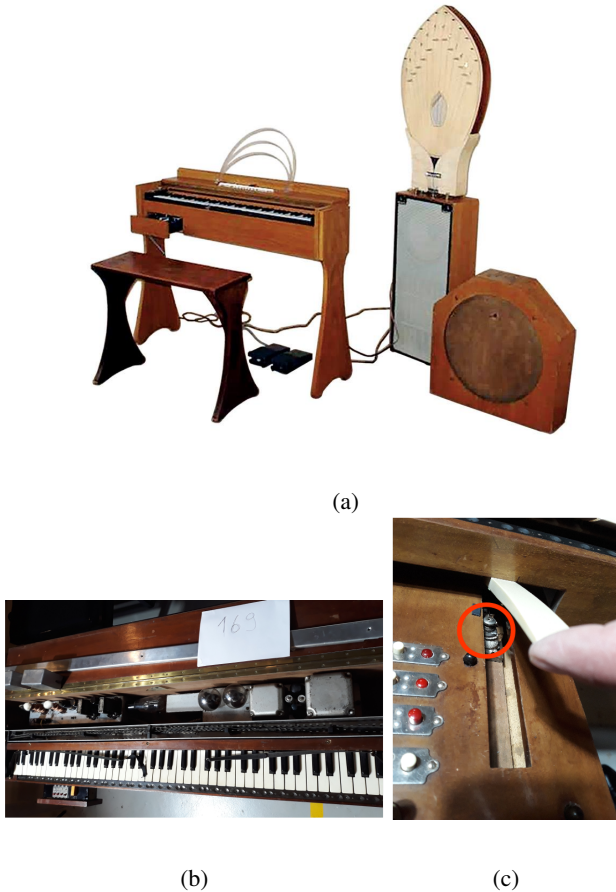


Fig. 1: Different parts of the ondes Martenot : diffuseurs (Fig. 1a on the right, from [33]), circuit, ribbon, keyboard (Fig. 1b), intensity key with the powder bag underneath circled in red (Fig. 1c).

powders. This key operates as a rheostat [38] (Fig. 1c). Thanks to this intensity key, the instrument's expressiveness has been praised since its creation. However, the lack of robustness of its circuit (subject to drifting, particularly in older models) is dreaded by musicians (called *ondists*) who are accustomed to perform repairs on the fly before concerts.

C. Circuit and operation

The technique of heterodyning was developed originally for wireless telegraphy [39], in order to shift high frequency signals into the audio domain. In the ondes Martenot specifically, two oscillators generate quasi-sinusoidal voltages at high frequency; one is set to 80 kHz and the other, variable below 80 kHz, is controlled by the player. Their sum is an amplitude-modulated signal, whose envelope is detected with a triode vacuum tube in series with an RC circuit. The envelope fundamental frequency, equal to the difference between the oscillators' frequencies, lies in the audible frequency range. The resulting voltage is amplified through two successive triode vacuum tubes, which increase the harmonic distortion present in the signal, due to their non-linear characteristics.

Finally, the *diffuseur*, selected by the player, converts the electrical waveform into sound and in turn modifies its spectral

content.

The complete circuit is structured into five stages devoted to specific functionalities (see Fig. 2a), namely : (1) fixed-frequency oscillator, (2) variable-frequency oscillator, (3) demodulator, (4) preamplifier, and (5) power amplifier. These stages are connected through transformers that introduce coupling: this will be naturally taken into account in the global PHS model (addressed in section IV-C). However, in first step, these stages are presented separately, ignoring coupling (no load on the secondary winding, 2b-2d). Qualitative specificities of these stages are stated below.

1) *Oscillators*: In both oscillators, a voltage noise V_{start} at the triode grid is amplified by the triode vacuum tube and filtered by a LC circuit, before feeding the grid through a transformer of ratio P . Each transformer has two windings on the secondary; the second secondaries (for oscillators 1 and 2) are connected in series to form the demodulator voltage input.

2) *Demodulator*: The voltage input, equal to the sum of the oscillators' outputs, can be assimilated to an amplitude-modulated sinewave: $\cos(\Phi) + \cos(\Phi - \phi_m) = 2 \cos(\Phi - \phi_m/2)\cos(\phi_m/2)$, where $F = \dot{\Phi}/2\pi = 80$ kHz is the fixed oscillator frequency, $f_m = \dot{\phi}_m/2\pi$ is the target frequency, and $F - f_m$ is the variable oscillator frequency. The demodulator is composed of a triode vacuum tube in series with an RC circuit (R_4 and C_{21} on Fig. 2c). As the triode grid polarization is close to zero, the qualitative behavior of the triode between the grid and the cathode is that of a diode: grid current only appears for positive grid voltages (Fig. 3). The triode vacuum tube is loaded with capacitors in parallel with a transformer. This load forms a resonant bandpass RLC filter (Fig. 2c): the resistance R_p models the transformer losses, L_p is the primary inductance, C_{dem} is the equivalent capacitor of C_9 and C_{10} in parallel. Its resonance frequency lies in the audible range. The stage amplification in a common cathode pattern increases with the triode load. As a consequence, the oscillators' frequencies and their intermodulation products are filtered out before amplification.

3) *Preamplifier and power amplifier*: Both stages rely on the triode vacuum tube amplification properties in a common cathode pattern [40].

III. POWER-BALANCED MODELING

A. Framework

Detailed presentations of PHS are available in [27]. Here we rely on a differential-algebraic formulation adapted to multi-physical systems [30], which allows the representation of a dynamical system as a network of

- 1) components storing energy E as a regular definite non-negative function of their state \mathbf{x} ($E = H(\mathbf{x}) \geq 0$),
- 2) instantaneous dissipative components for which efforts \mathbf{e}_w are related to flows \mathbf{w} through a constitutive law \mathbf{z} that dissipates power ($\mathbf{e}_w = \mathbf{z}(\mathbf{w})$, $P_{\text{diss}} = \mathbf{z}(\mathbf{w})^\top \mathbf{w} \geq 0$, $\forall \mathbf{w}$),
- 3) connection ports as control inputs \mathbf{u} and their associated outputs \mathbf{y} such as $\mathbf{u}^\top \mathbf{y}$ is the outgoing power P_{ext} .

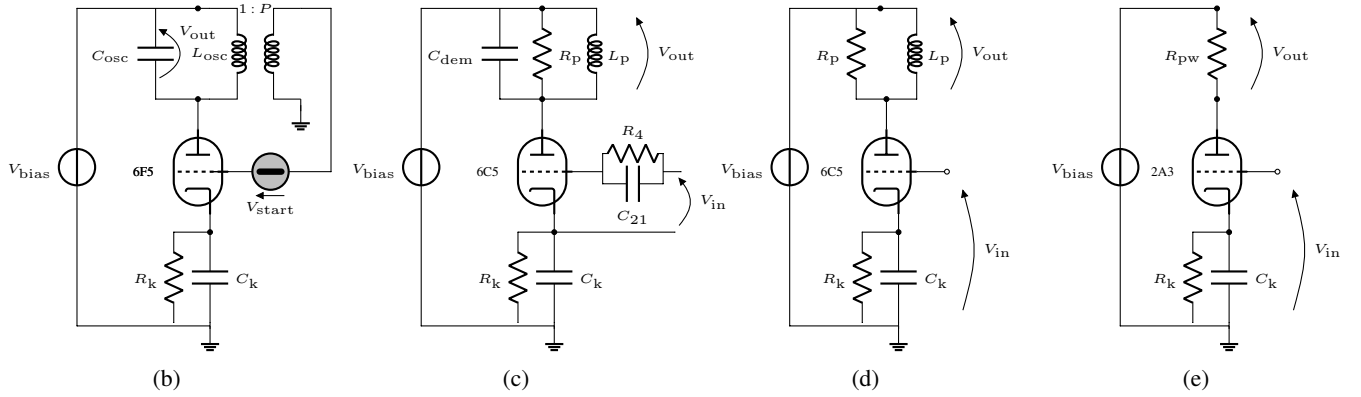
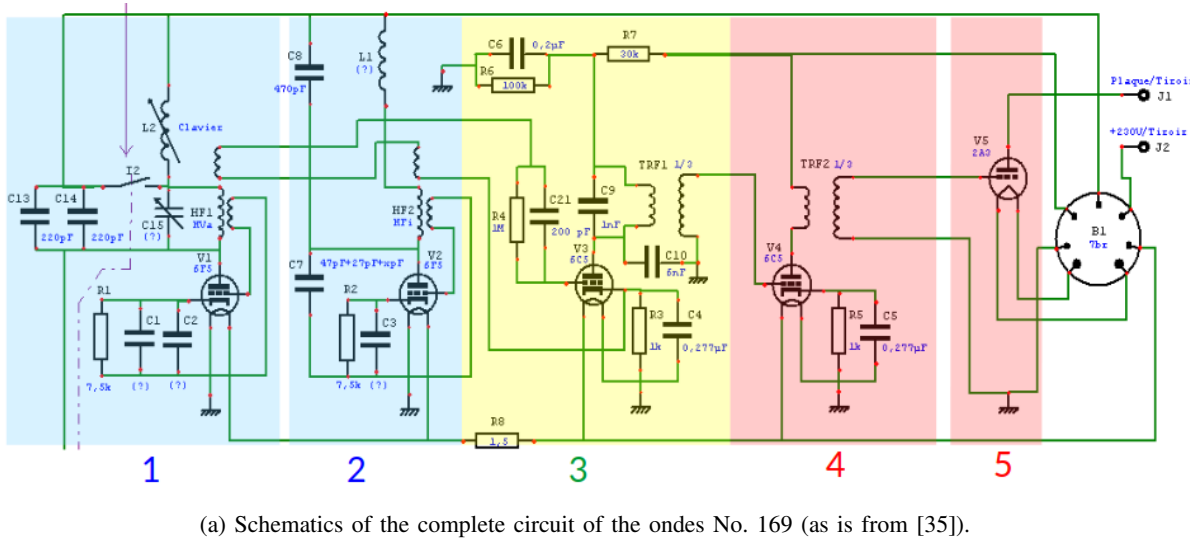


Fig. 2: Complete circuit (top) and isolated stages simplified for modeling (bottom): oscillators (stages 1 and 2, Fig. 2b), demodulator (stage 3, Fig. 2c), preamplifier (stage 4, Fig. 2d) and power amplifier (stage 5, Fig. 2e).

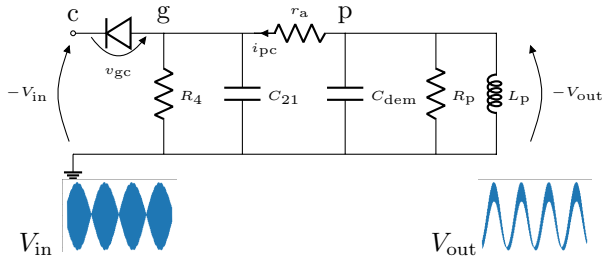


Fig. 3: Equivalent small signal schematic of the demodulator. The nodes c, g and p denote the triode cathode, grid and plate respectively; r_a is the triode plate resistor.

The variables are generally time-dependent. For each component, \dot{x} accounts for the incoming *state flow*. It is named “flow” in the following.¹ Jointly, $\nabla H(x)$ is named “effort” (w.r.t. the state) in the following, so that the power received by the energy-storing component $\dot{x}\nabla H(x)$ is the product of an effort and a flow. If such a system is realizable [41], [42], the exchanges of generalized flows and efforts between the

¹Note that, according to the component type, the “state flow” can be a current ($i = \dot{q} = \dot{x}$ for capacitors with charge q) or a voltage ($v = \dot{\phi} = \dot{x}$ for induction coils with magnetic flux ϕ). Thus, the flow is not systematically understood as the “charge flow” that is the electric current.

system components are coupled through a skew-symmetric interconnection matrix $S = -S^T$:

$$\begin{pmatrix} \dot{x} \\ \mathbf{w} \\ \mathbf{y} \end{pmatrix} = \mathbf{S} \begin{pmatrix} \nabla H(\mathbf{x}) \\ \mathbf{z}(\mathbf{w}) \\ \mathbf{u} \end{pmatrix}. \quad (1)$$

\mathcal{F} (flows) \mathcal{E} (efforts)

For convenience, to distinguish storage, dissipative, and connection ports exchanges, we introduce the following block-matrix notation:

$$\mathbf{S} = \begin{pmatrix} \mathbf{J}_x & -\mathbf{K} & -\mathbf{G}_x \\ \mathbf{K}^T & \mathbf{J}_w & -\mathbf{G}_w \\ \mathbf{G}_x^T & \mathbf{G}_w^T & \mathbf{J}_y \end{pmatrix}. \quad (2)$$

The skew-symmetry of \mathbf{S} guarantees the system power balance. Indeed,

$$\underbrace{\nabla H(\mathbf{x})^T \dot{\mathbf{x}}}_{\frac{dE}{dt}} + \underbrace{\mathbf{z}(\mathbf{w})^T \mathbf{w}}_{P_{\text{diss}} \geq 0} + \underbrace{\mathbf{u}^T \mathbf{y}}_{P_{\text{ext}}} = \mathcal{E}^T \mathcal{F}, \quad (3)$$

and

$$\mathcal{E}^T \mathcal{F} = \mathcal{E}^T \mathbf{S} \mathcal{E} = (\mathcal{E}^T \mathbf{S} \mathcal{E})^T = -\mathcal{E}^T \mathbf{S} \mathcal{E} = 0, \quad (4)$$

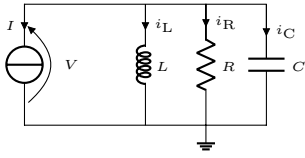


Fig. 4: Current-controlled parallel RLC circuit.

TABLE I: State variables and constitutive laws for a linear parallel RLC circuit.

	x	$\frac{dx}{dt}$	$H(x)$	$\nabla H(x)$
C	q	$\dot{q} = i_C$	$\frac{q^2}{2C}$	$\frac{q}{C} = v_C$
L	ϕ	$\dot{\phi} = v_L$	$\frac{\phi^2}{2L}$	$\frac{\phi}{L} = i_L$
	w			$z(w)$
R	v_R			$\frac{v_R}{R} = i_R$

so we have the following power balance:

$$\frac{dE}{dt} = -P_{\text{ext}} - P_{\text{diss}}. \quad (5)$$

Note that $-P_{\text{ext}}$ is the incoming power (since P_{ext} is the outgoing power). The passivity of the system stems from this power balance and the positivity of P_{diss} .

B. Example

Consider a linear parallel RLC circuit (Fig. 4). The capacitor C and the inductor L are storage components whose states are given by the variables q (charge) and ϕ (magnetic flux) respectively; the resistor R is a dissipative component described by Ohm's law. In order to represent it as a PHS, the system is chosen to be current controlled. Table I recaps the variables and the constitutive laws of the three components. Based on Kirchoff's laws, matrix \mathcal{S} relating efforts (\mathcal{E}) to flows (\mathcal{F}) in Eq. (1) is found to be

$$\begin{pmatrix} i_C \\ v_L \\ v_R \\ V \end{pmatrix} = \begin{pmatrix} 0 & -1 & -1 & -1 \\ 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} v_C \\ i_L \\ i_R \\ I \end{pmatrix}.$$

Flows which are currents (resp. voltages) have associated efforts which are voltages (resp. currents). Therefore their products are powers and Eq. (3) is naturally retrieved. Note that in this simple example, the matrix \mathcal{S} is sparse with constant coefficients, but the properties of the PHS formalism also hold for non-linear or coupled systems (state depending interconnection matrices, non-quadratic H , non-linear z).

IV. ONDES MARTENOT PHS MODELING

A. Ondes Martenot components

The ondes Martenot circuit contains resistors, capacitors, inductors, transformers, and triode vacuum tubes. Among those components, the ribbon-controlled capacitor and the triode need to be carefully modeled to satisfy a physical power balance and to admit a PHS formulation.

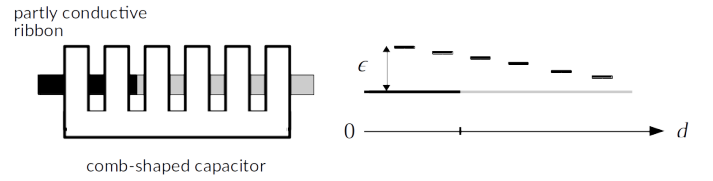


Fig. 5: Variable capacitor schematics where d denotes the ribbon position (up to 1.2 m for the highest note) and $\epsilon(d)$ the distance between the ribbon and the comb teeth (around 1 mm).

1) *Ribbon-controlled capacitor*: The variable capacitor C_{15} (Fig. 2a) is controlled by a partly conductive ribbon: as the player moves the ribbon along, it hides or "activates" the teeth of the comb-shaped electrical conductor, located at different distances from the ribbon (Fig. 5). Previous work [32] showed that the LTI capacitors C_{13} , C_{14} but also the *variable* capacitor C_{15} in parallel (Fig. 2a, stage 1) are equivalent to a single variable capacitor whose energy function is given by

$$H_{\text{cap}}(q, d) = \frac{q^2}{2C_{\text{osc}}(d)}, \quad (6)$$

$$C_{\text{osc}}(d) = \frac{1}{4\pi^2 \left(F - A_1 2^{\frac{d}{12d_0}} \right)^2 L_{\text{osc}}}, \quad (7)$$

where d is the ribbon displacement relative to the position corresponding to the lowest note A_1 , d_0 is the ribbon displacement for one semitone, F is the fixed oscillator frequency and L_{osc} is the inductance of the oscillator.

2) *Triode vacuum tubes*: Numerous models are available for triode vacuum tubes [43], [44]. For audio applications, the Norman Koren model [45] has proven to be accurate. Here we will rely on an enhanced Norman Koren model [46] which takes into account the triode grid current. Although this current is small compared to that of the plate, it must be considered to ensure the passivity of the component (since its power supply is external, the triode is indeed passive). As a result, the triode vacuum tube is a dissipative component with $w = (v_{\text{pc}}, v_{\text{gc}})^T$ and $z_{\theta}(w) = (i_{\text{pc}}, i_{\text{gc}})^T$, where p , g and c respectively refer to the triode plate, grid and cathode. The plate current i_{pc} and the grid current i_{gc} are given by

$$i_{\text{pc}} = \begin{cases} 2[E_1(v_{\text{pc}}, v_{\text{gc}})]^{E_x} / K_g & \text{if } E_1 \geq 0 \\ 0 & \text{else,} \end{cases} \quad (8)$$

$$i_{\text{gc}} = \begin{cases} 0 & \text{if } v_{\text{gc}} < V_a \\ \frac{v_{\text{gc}} - V_a}{R_{\text{gk}}} & \text{else,} \end{cases} \quad (9)$$

with

$$E_1(v_{\text{pc}}, v_{\text{gc}}) = \frac{v_{\text{pc}}}{K_p} \ln \left(1 + \exp \left(K_p \left(\frac{1}{\mu} + \frac{v_{\text{gc}} + V_{\text{ct}}}{\sqrt{K_{\text{vb}} + v_{\text{pc}}^2}} \right) \right) \right).$$

For each type of vacuum tubes used in the circuit of ondes Martenot No. 169, the set of constant parameters

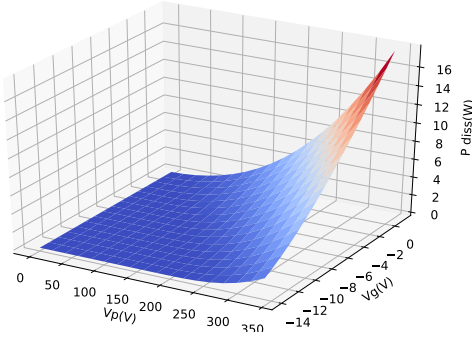


Fig. 6: Dissipated power for the triode 6C5.

$\theta = (\mu, E_x, K_g, K_p, K_{vb}, V_{ct}, V_a, R_{gk})$ is estimated by fitting the model to the datasheets [47, Fig. 1] [48, Fig. 1] [49, Fig. 1] through a least squares minimization. The results of that minimization fulfill the passivity criterion, i.e. $z_\theta(\mathbf{w})^\top \mathbf{w} \geq 0$ for all \mathbf{w} (Fig. 6). They are given in Table II, section VI.

3) *Other components*: Constitutive laws of R, L, C components are supposed to be linear, as shown in Table I. In the oscillators, the transformers are also supposed to be linear; their ratios P being unknown a priori, they are subjected to an estimation described in section V-A2.

B. PHS of isolated stages

For each stage, we denote R_k the regulation resistor between the triode cathode and the ground, C_k the bypass capacitor in parallel with R_k , V_{bias} the triode DC power supply, V_{in} the input voltage and V_{out} the observed output voltage. We denote L_p the transformer magnetizing reactance, R_p the transformer resistance modeling the core losses in the demodulator and the preamplifier and R_{pw} the input impedance of the diffuser. For each oscillator, we denote C_{osc} the capacitor equivalent to the parallel capacitors and L_{osc} the inductance equivalent to the coils in series (Figs. 2b-2e). Kirchhoff's laws yield the interconnection matrices for the oscillator (Fig. 7a), demodulator (Fig. 7b), preamplifier (Fig. 7c), and power amplifier (Fig. 7d).

C. Stages coupling

The connection of two PHS is still a PHS. The total state is the concatenation of the subsystems states, and the total Hamiltonian is the sum of the subsystems Hamiltonians. A conservative interconnection is then achieved by connecting each output port of one system to exactly one input port of the other. For two stages A and B connected through a transformer of ratio ρ , we have $V_{inB} = \rho V_{outA}$ and $I_{outA} = -\rho I_{inB}$, that is,

$$\begin{pmatrix} y_{outA} \\ y_{inB} \end{pmatrix} = \begin{pmatrix} 0 & 1/\rho \\ -1/\rho & 0 \end{pmatrix} \begin{pmatrix} u_{outA} \\ u_{inB} \end{pmatrix}.$$

The circuit A connected to the circuit B is then equivalent to a circuit C whose PHS is given by Eq. (1), with notations of Eq. (2): $\mathbf{x}_C = (\mathbf{x}_A, \mathbf{x}_B)^\top$ and $\nabla H_C, \mathbf{w}_C, \mathbf{z}_C$ are defined likewise,

$$\mathbf{J}_{\mathbf{x}_C} = \begin{pmatrix} \mathbf{J}_{\mathbf{x}_A} & \mathbf{0} \\ \mathbf{0} & \mathbf{J}_{\mathbf{x}_B} \end{pmatrix}$$

and $\mathbf{J}_{\mathbf{w}_C}, \mathbf{G}_{\mathbf{x}_C}, \mathbf{G}_{\mathbf{w}_C}, \mathbf{K}_C$ are defined likewise, $\mathbf{u}_C = (\mathbf{u}_{inA}, \mathbf{u}_{outA}, \mathbf{u}_{inB}, \mathbf{u}_{outB})^\top$ and \mathbf{y}_C is defined likewise, and

$$\mathbf{J}_{\mathbf{y}_C} = \begin{pmatrix} \mathbf{J}_{\mathbf{y}_A} & \begin{matrix} 0 & 0 \\ 1/\rho & 0 \end{matrix} \\ \begin{matrix} 0 & -1/\rho \\ 0 & 0 \end{matrix} & \mathbf{J}_{\mathbf{y}_B} \end{pmatrix}.$$

V. ESTIMATION OF THE INSTRUMENT PARAMETERS

Most parameters of the components are provided by the circuit specifications [35]. The others have to be determined, in particular the oscillator transformer re-injection ratio P and bypass capacitor C_k , as well as the characteristics of the transformers towards the amplification stages.

A. Oscillators (stages 1 and 2)

1) *Voltage noise source*: The oscillation arises from the voltage noise V_{start} at the grid of the triode at its operating point. This broadband noise mainly results from thermal agitation [50] and is modeled with a white noise source of peak voltage 1 mV^2 .

2) *Re-injection transformer ratio*: The voltage noise is amplified by the triode, filtered by a LC circuit at the plate and sent back to the grid through a transformer of ratio P (Fig. 2b). To estimate a range of possible values for P , the oscillator circuit is simplified: L_{osc} acts as the transformer primary and the cathode potential is considered constant. Moreover, the oscillator model is linearized around its operating point and it is assumed that the influence of the load on the second secondary is negligible. The oscillator can then be represented as a system of input V_{start} and output V_{out} . Under those assumptions, it can be shown [32], [53] that the system characteristic equation in Laplace domain is $s^2 + s(1 - \mu P)/(r_a C_{osc}) + \omega_0^2$ (μ being the triode amplification factor, r_a the triode plate resistor and $\omega_0^2 = 1/(L_{osc} C_{osc})$ the oscillation pulsation), and that the condition on P for the system to oscillate is

$$\frac{1}{\mu} \leq P < \frac{1}{\mu} + \frac{2\omega_0 C_{osc} r_a}{\mu}. \quad (10)$$

The closer to $1/\mu$ P is chosen, the more stationary the oscillation amplitude will be. Fig. 8 shows the range of P values for which an oscillation is possible.

3) *Inductance of the LC circuit*: For a parallel LC circuit of resonant frequency F , $L_{osc} = 1/(C_{osc}(2\pi F)^2)$. With F set to 80 kHz and $C_{osc} = 544 \text{ pF}$, this yields $L_{osc} = 7 \text{ mH}$.

4) *Cathode bypass capacitor*: The bypass capacitor C_k stabilizes the cathode potential, which otherwise would depend strongly on the plate current (through the regulation resistor R_k), itself depending on the input voltage. This stabilization ensures that the signal to be amplified v_{gc} is the biased input voltage and not a modulation of it. In parallel with

²The measured noise amplitude is around $1 \text{ } \mu\text{V RMS}$ [51] for a vacuum tube. However, as the noise is sufficiently filtered out by the oscillator, its amplitude mainly affects the transient duration [52].

	$\nabla H(\mathbf{x})$	$\mathbf{z}(\mathbf{w})$	\mathbf{u}
	$i_{L_{osc}}$ $v_{C_{osc}}$ v_{C_k}	i_{gc} i_{pc} i_{R_k}	V_{start} I_{out} V_{bias}
$\dot{\mathbf{x}}$	$\begin{pmatrix} v_{L_{osc}} \\ i_{C_{osc}} \\ i_{C_k} \end{pmatrix}$	$\begin{pmatrix} 1 \\ -P \\ 1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ -1 \\ \cdot \end{pmatrix}$
\mathbf{w}	$\begin{pmatrix} v_{gc} \\ v_{pc} \\ v_{R_k} \end{pmatrix}$	$\begin{pmatrix} P \\ -1 \\ 1 \end{pmatrix}$	$\begin{pmatrix} 1 \\ \cdot \\ \cdot \end{pmatrix}$
\mathbf{y}	$\begin{pmatrix} I_{start} \\ V_{out} \\ I_{bias} \end{pmatrix}$	$\begin{pmatrix} -1 \\ \cdot \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ \cdot \end{pmatrix}$

(a)

	$\nabla H(\mathbf{x})$	$\mathbf{z}(\mathbf{w})$	\mathbf{u}
	i_{L_p} $v_{C_{21}}$ v_{C_k} $v_{C_{dem}}$	i_{R_4} i_{R_p} i_{gc} i_{pc} i_{R_k}	V_{in} I_{out} V_{bias}
$\dot{\mathbf{x}}$	$\begin{pmatrix} v_{L_p} \\ i_{C_{21}} \\ i_{C_k} \\ i_{C_{dem}} \end{pmatrix}$	$\begin{pmatrix} \cdot \\ -1 \\ \cdot \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ \cdot \\ -1 \end{pmatrix}$
\mathbf{w}	$\begin{pmatrix} v_{R_4} \\ v_{R_p} \\ v_{gc} \\ v_{pc} \\ v_{R_k} \end{pmatrix}$	$\begin{pmatrix} 1 \\ \cdot \\ -1 \\ -1 \\ 1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ 1 \\ \cdot \\ \cdot \end{pmatrix}$
\mathbf{y}	$\begin{pmatrix} I_{in} \\ V_{out} \\ I_{bias} \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ -1 \\ \cdot \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{pmatrix}$

(b)

	$\nabla H(\mathbf{x})$	$\mathbf{z}(\mathbf{w})$	\mathbf{u}
	i_{L_p} v_{C_k}	v_{R_p} i_{gc} i_{pc} i_{R_k}	V_{in} I_{out} V_{bias}
$\dot{\mathbf{x}}$	$\begin{pmatrix} v_{L_p} \\ i_{C_k} \end{pmatrix}$	$\begin{pmatrix} 1 \\ \cdot \\ 1 \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ -1 \\ \cdot \end{pmatrix}$
\mathbf{w}	$\begin{pmatrix} i_{R_p} \\ v_{gc} \\ v_{pc} \\ v_{R_k} \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ -1 \\ \cdot \end{pmatrix}$	$\begin{pmatrix} 1 \\ \cdot \\ \cdot \\ \cdot \end{pmatrix}$
\mathbf{y}	$\begin{pmatrix} I_{in} \\ V_{out} \\ I_{bias} \end{pmatrix}$	$\begin{pmatrix} -1 \\ \cdot \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ \cdot \end{pmatrix}$

(c)

	$\nabla H(\mathbf{x})$	$\mathbf{z}(\mathbf{w})$	\mathbf{u}
	v_{C_k}	$v_{R_{pw}}$ i_{gc} i_{pc} i_{R_k}	V_{in} I_{out} V_{bias}
$\dot{\mathbf{x}}$	$\begin{pmatrix} i_{C_k} \end{pmatrix}$	$\begin{pmatrix} \cdot \\ 1 \\ 1 \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ -1 \\ \cdot \end{pmatrix}$
\mathbf{w}	$\begin{pmatrix} i_{R_{pw}} \\ v_{gc} \\ v_{pc} \\ v_{R_k} \end{pmatrix}$	$\begin{pmatrix} \cdot \\ -1 \\ -1 \\ 1 \end{pmatrix}$	$\begin{pmatrix} 1 \\ \cdot \\ \cdot \\ \cdot \end{pmatrix}$
\mathbf{y}	$\begin{pmatrix} I_{in} \\ V_{out} \\ I_{bias} \end{pmatrix}$	$\begin{pmatrix} -1 \\ \cdot \\ -1 \end{pmatrix}$	$\begin{pmatrix} \cdot \\ \cdot \\ \cdot \end{pmatrix}$

(d)

Fig. 7: PHS interconnection matrices of the isolated stages: oscillators (Fig. 7a), demodulator (Fig. 7b), preamplifier (Fig. 7c), power amplifier (Fig. 7d).

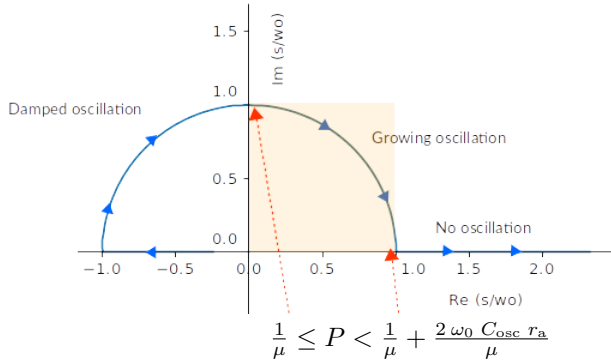


Fig. 8: Location of s and regimes of oscillation for P ranging between $1/\mu$ and $1/\mu + \beta$.

R_k , it constitutes a current-current high-pass filter whose cutoff frequency is $f_c = 1/(2\pi R_k C_k)$. For the oscillator amplification to be maximal at the frequency F , f_c must verify $F \geq 10f_c$. For the given value $R_k = 7.5 \text{ k}\Omega$, this yields $C_k \geq 3 \text{ nF}$. In the following, C_k is set to $0.22 \text{ }\mu\text{F}$, a typical capacitor value, for both oscillators.

B. Coupling transformer characteristics

Except for its ratio, the properties of the transformer between stage 3 (resp. 4) and 4 (resp. 5) are unknown and accessing a real circuit to perform measurements has proven to be delicate due to the instrument rarity and fragility. It is assumed that Maurice Martenot chose the transformers with audio applications in mind; the magnetizing reactance L_p and the resistance modeling the core losses R_p will be thus set as such in the following.

The capacitor C_{dem} in parallel with R_p and L_p (Fig. 2c) forms a current-current band-pass filter, whose high cutoff frequency is given by $f_{ch} = (r_a + R_p)/(2\pi r_a R_p C_{dem})$, with $C_{dem} = 7 \text{ nF}$ and $r_a = 10 \text{ k}\Omega$. The instrument ambitus is C1-B7 corresponding to a fundamental frequency ranging from 32 Hz to 3951 Hz in A440 tuning. Therefore, choosing $f_{ch} = 7.9 \text{ kHz}$ (the highest possible note second harmonic) yields $R_p \approx 4 \text{ k}\Omega$. Similarly, the low cutoff frequency is given by $f_{cl} = (r_a R_p)/(2\pi(r_a + R_p)L_p)$. Choosing $f_{cl} = 50 \text{ Hz}$ yields $L_p \approx 9 \text{ H}$. It is assumed that the transformer to the power amplifier has the same properties.

The values of the other circuit parameters are provided by the condition report of the ondes No. 169 [35].

VI. POWER-BALANCED SIMULATION

This section is devoted to the power-balanced simulation of the ondes Martenot No. 169 complete circuit, composed of the 5 coupled stages (the power amplifier being loaded by a basic resistor equivalent to that of a diffuseur—around 1.5 k Ω). Table II recaps all components parameters values used for simulation.

TABLE II: Component parameters values used for simulation.

Triode	μ	E_x	K_g	K_p	K_{vb}
6F5	98	1.6	2614	905	1.87
6C5	20	1.5	2837	138	89
2A3	4.3	1.5	1685	43	102
	V_{ct}	V_a	R_{gk}		
6F5	0.5	0.33	1300		
6C5	0.8	0.33	1300		
2A3	-1.2	0.33	1300		
Stage	V_{bias}	C_k	R_k		
osc	90 V	0.22 μ F	7.5 k Ω		
demod	100 V	0.277 μ F	1 k Ω		
preamp	180 V	0.277 μ F	1 k Ω		
poweramp	230 V	10 μ F	750 Ω		
L_{osc}	C_{osc}	C_{dem}	C_{21}	R_4	L_p
7 mH	544 pF	7 nF	200 pF	1 M Ω	9 H
R_p	R_{pw}	P	ρ	I_{out}	V_{start}
4 k Ω	1.5 k Ω	$1/\mu + \beta/35$	3	0 A	1 mV

A. Discrete-time system

The simulation is performed using the PyPHS library [30], [54]. It is based on the numerical method recalled below in the case of mono-variate storage components ($H(x) = \sum_{n=1}^N H_n(x_n)$ where N is the storage components number). Define $\mathbf{x}[k] = \mathbf{x}(k/F_s)$ where $F_s = 1/T_s$ denotes the sampling rate. Moreover, define the state increment $\delta\mathbf{x}[k] = \mathbf{x}[k+1] - \mathbf{x}[k]$ and the discrete gradient (see [30], [55]) $\bar{\nabla}H(\mathbf{x}[k], \delta\mathbf{x}[k])$, the n^{th} component of which is

$$\begin{aligned} & [\bar{\nabla}H(\mathbf{x}[k], \delta\mathbf{x}[k])]_n \\ &= \begin{cases} \frac{H_n(x_n[k] + \delta x_n[k]) - H_n(x_n[k])}{\delta x_n[k]} & \text{if } \delta x_n[k] \neq 0 \\ \frac{dH_n}{dx_n}(x_n[k]) & \text{otherwise.} \end{cases} \end{aligned} \quad (11)$$

The method consists of replacing $\dot{\mathbf{x}}$ with $\delta\mathbf{x}[k]/T_s$ and $\nabla H(\mathbf{x})$ with $\bar{\nabla}H(\mathbf{x}[k], \delta\mathbf{x}[k])$ in Eq. (1). As in Eqs. (3-5), due to the skew-symmetry of \mathcal{S} , the following discrete power balance is satisfied:

$$\underbrace{\bar{\nabla}H(\mathbf{x}[k], \delta\mathbf{x}[k])^\top \frac{\delta\mathbf{x}[k]}{T_s}}_{\delta E[k]/T_s} + \underbrace{z(\mathbf{w}[k])^\top \mathbf{w}[k]}_{P_{diss}[k]} + \underbrace{\mathbf{u}[k]^\top \mathbf{y}[k]}_{P_{ext}[k]} = 0.$$

Moreover, due to the positivity of $z(\mathbf{w}[k])^\top \mathbf{w}[k]$, the system is also still passive. Denoting $\boldsymbol{\nu} = (\delta\mathbf{x}[k]F_s, \mathbf{w}[k])^\top$, the discretization of Eq. (1) yields the implicit equation

$$F(\boldsymbol{\nu}) := \boldsymbol{\nu} - \bar{\mathcal{S}}\bar{\mathcal{E}}(\boldsymbol{\nu}, \mathbf{x}[k], \mathbf{u}[k]) = \mathbf{0}, \quad (12)$$

where

$$\bar{\mathcal{S}} = \begin{pmatrix} \mathbf{J}_x & -\mathbf{K} & -\mathbf{G}_x \\ \mathbf{K}^\top & \mathbf{J}_w & -\mathbf{G}_w \end{pmatrix}$$

and $\bar{\mathcal{E}}(\boldsymbol{\nu}, \mathbf{x}[k], \mathbf{u}[k]) = (\bar{\nabla}H(\mathbf{x}[k], \delta\mathbf{x}[k]), z(\mathbf{w}[k]), \mathbf{u}[k])^\top$. Denoting F' the Jacobian of F , Eq. (12) is solved using the Newton-Raphson iteration

$$\boldsymbol{\nu}_{k+1} = \boldsymbol{\nu}_k - F'(\boldsymbol{\nu}_k)^{-1}F(\boldsymbol{\nu}_k), \quad (13)$$

if F' is invertible. Conditions for convergence of the method can be found in [56], [57].

B. Numerical experiments

The circuit is simulated based on the concatenation of the stages PHS with component parameters values of Table II. The control law of the ribbon position d is built to generate a frequency sweep according to parameters in Table III and Eq. (7). Fig. 9a-9c show the output voltages of stages 3, 4 and 5 during the simulation, and the effect of the successive harmonic distortions. Fig. 9d shows the spectrogram of the complete circuit output during the whole sweep. Fig. 9e shows the stored power, outgoing power and dissipated power of the complete circuit during the whole sweep. As shown in Fig. 9f, the total power, sum of these three contributions, amounts to less than 10^{-13} W.

TABLE III: Simulation parameters.

sampling frequency F_s	768 kHz
fixed osc. frequency F	80 kHz
playing frequency f_m	55 Hz-3520 Hz
duration	1 s

VII. AUDIO PLUGIN

A. Circuit simplification

The voltage generated by the oscillators, even when connected to the other stages, is nearly sinusoidal: the harmonic distortion is about 0.03% for harmonic 2 (Fig. 10a-10b). For a real-time application, physically modeled oscillators may be thus replaced with a sinewave generator.

Additionally, although the simulated performances of the power amplifier are rather poor for a class A amplifier (almost 5% harmonic distortion for harmonic 2, Fig. 11), the stage contributions to the final sound are of much less importance compared to the demodulator and preamplifier. In practice, based on numerical experiments, this stage may also be removed for real-time application.

B. Oscillators frequency reduction

The original oscillator frequency F is around 80 kHz. This choice, alongside with heterodyning, can certainly be attributed to the cost and unreliability of high value capacitors in Maurice Martenot's time: an oscillator at an audible frequency, 3000 Hz for instance, would necessitate a capacitor of 4 μ F (the inductance being equal for both oscillators). But in a virtual instrument context, the components may take

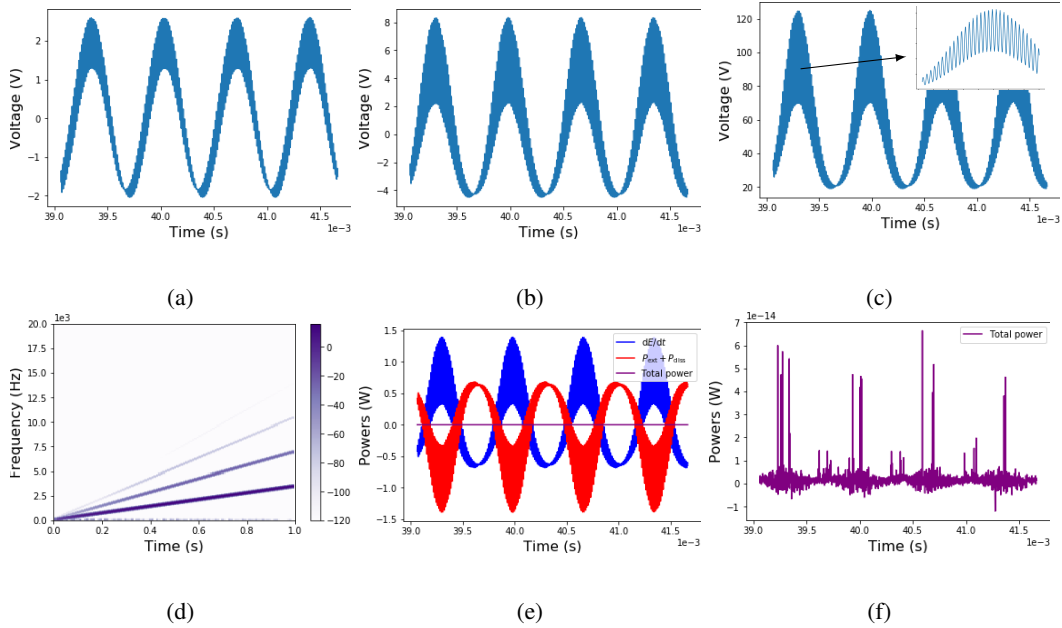


Fig. 9: From top left to bottom right: simulated output voltages at stages 3 (9a), 4 (9b) and 5 with carrier residual (9c), spectrogram of the simulated output voltage at stage 5 (9d), power balance of the circuit during the simulation (9e-9f).

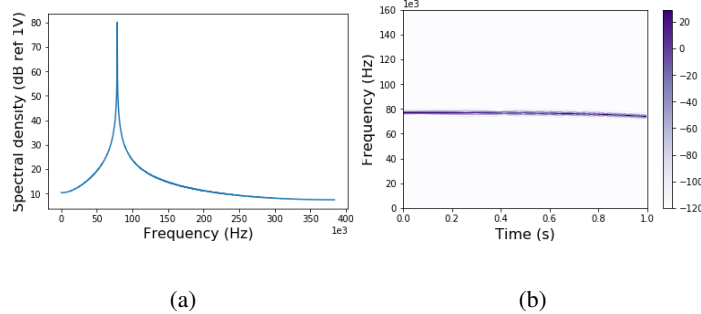


Fig. 10: Spectral density of the simulated fixed oscillator output voltage (10a) and spectrogram of the simulated variable oscillator output voltage during a sweep ($f_m = 55$ Hz to 3520 Hz, 10b).



Fig. 11: Spectral density of the simulated power amplifier output voltage for an input of 1 kHz, amplitude 20 V.

Fig. 12: Spectrogram of the simulated power amplifier output voltage for $F = 48$ kHz and $F_s = 192$ kHz, $f_m = 55$ Hz to 3520 Hz.

any value, provided that the oscillator frequency stays above 20 kHz. Knowing that the carrier and its first harmonics are not completely eliminated by the filtering, and that most commercial audio cards do not offer a sampling rate above 192 kHz, $F = 48$ kHz is arbitrarily chosen to reduce the sampling rate without introducing aliasing, for real-time application. Fig. 12 shows the spectrogram of the poweramp circuit output voltage for this new configuration. A small amount of

aliasing remains nonetheless. This can be improved either by increasing the value of C_{dem} , therefore lowering the lowpass frequency before amplification, or implementing methods such as the ones described in [58]. Note: the detection time constant $\tau = R_4 C_{21} = 0.0002$ is still valid as the relation $\tau \gg 1/F$ is still true.

C. GUI, real-time results and performances

The dimension of the complete PHS is defined as $n = \dim \mathcal{E} = \dim \mathcal{F}$. For each sample and each element, the matrix update computes n multiplications and $n - 1$ additions, and consequently $F_s \times n(2n - 1)$ floating operations per second (flops). Before the circuit simplification, the PHS contains 32 component variables, 5 voltage supply ports, 2 inputs ports and 1 observation port. Using $F_s = 768$ kHz and $n = 40$ requires 2.42 Gflops. After the circuit simplification and the frequency reduction, 17 component variables and 3 ports are removed leading to $n = 20$. For $F_s = 192$ kHz, this requires 149 Mflops (gain of about 16). The simplified PHS is implemented in the JUCE framework using the PyPHS library to generate C++ code [54]. The player controls the pitch and sound intensity either with sliders or with commercial midi interfaces. Additionally, the user has the possibility to adjust the quantity of harmonics by changing the demodulator input gain (a feature not present on the original instrument). While running, the plugin consumes 85% CPU (i7-2720QM CPU at 2.20 GHz) and 0.9% RAM (4Go), which is still quite heavy but allows real-time usage.

VIII. CONCLUSION AND PERSPECTIVES

In this paper, a refined simulation of the ondes Martenot circuit has been proposed, allowing a numerical investigation. It is based on a power-balanced modeling adapted to LTI (capacitors, resistor, inductor) and non-LTI (vacuum tubes and the multi-physical time-varying capacitor mechanically-driven by a ribbon) components. Due to the nature of the ondes Martenot instrument (rare, fragile and expensive), setting up extensive measurements to evaluate the accuracy of the circuit modeling is a complex operation which is still ongoing. However, numerical experiments on the modeled circuit lead to the following observations:

- 1) the combination of the triode vacuum tube amplification properties and the LC-resonator produces a quasi-sinusoidal oscillation with stable amplitude;
- 2) the contribution of the power amplifier is minor in terms of coloration compared to that of the preamplifier;
- 3) the overall result does not depend on the carrier frequency value, provided that this frequency stays outside the audio domain.

In consequence, the oscillators are replaced with sinewave generators, the power amplifier is replaced with a multiplying factor, and the sampling frequency is lowered by a factor of 4. These simplifications lead to the implementation of the circuit within a controllable audio plugin, functioning in real-time on a common computer.

Further work aims to model the *diffuseurs* and the control interfaces (ribbon and intensity key). Moreover, this work will rely on anti-aliasing methods [58] to handle the non-linear heterodyne process at lower sampling rates.

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