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Phonation threshold pressure at large asymmetries of the vocal folds*

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Abstract

The phonation threshold value of the lung pressure has been interpreted as a measure of ease of phonation and proposed as a diagnostic parameter for vocal health. Therefore, it is important to understand its behavior as a function of laryngeal parameters, particularly in abnormal configurations. This paper compares results from a theoretical model of the vocal folds with measures from a mechanical replica, in the presence of a natural frequency asymmetry. It shows that, at small asymmetry, the threshold pressure increases with the degree of asymmetry, whereas at large asymmetry, the threshold pressure reaches a plateau.

Keywords: phonation, vocal fold, oscillation, asymmetry

2010 MSC: 92C05, 74F10, 34C15

1. Introduction

During phonation, the right and left vocal folds act as a pair of coupled oscillators. In normal healthy conditions, they have a symmetrical configuration and oscillate in complete in-phase synchrony [1]. Abnormal conditions such as tissue lesions and neurological disorders introduce right-left asymmetries which may hamper the oscillation and cause phase differences, complex entrainment regimes and other nonlinear phenomena [2] [3] [4] [5].

An important parameter of the vocal fold oscillation is the so-called phonation threshold pressure, which is defined as the minimum lung pressure required

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10 to start phonation [6]. The threshold pressure appears as a relevant parameter
in equations of voice aerodynamics and has been interpreted as a measure of
“ease of phonation” [7]. A number of studies have shown that its value increases
with abnormal laryngeal conditions such as dehydration [8], fatigue [9], tissue
scarring [10] and others, favoring its application as an assessment tool for vocal
15 health.

In a recent theoretical study, the effect of a natural frequency asymmetry
on the threshold pressure was analyzed and different patterns at small vs. large
asymmetries were detected [11]. If the asymmetry is small, then the threshold
value pressure has a minimum at the symmetric configuration and increases
20 with the degree of asymmetry. On the other hand, if the asymmetry is large,
then the threshold pressure assumes a constant value. The existence of such a
region with constant threshold pressure would indicate caution in its proposed
application for clinical diagnosis, because an increase or decrease of asymmetry
(i.e., the abnormality) would not necessarily reflect in a respective increase or
25 decrease of threshold pressure, when the asymmetry is large. Thus, the present
study has the purpose of analyzing further this effect by comparing the theory
with data collected from a mechanical replica of the vocal folds.

2. Theoretical model

2.1. Equations of motion

Following [12], the right vocal fold is represented as a one-degree-of-freedom
oscillator of the form

$$M\ddot{x}_r + B(1 + \eta x_r^2)\dot{x}_r + Kx_r = P_g, \quad (1)$$

30 where x_r is the tissue displacement, M , B and K are the mass, damping and
stiffness, respectively, per unit area of the vocal fold medial surface, η is a
nonlinear coefficient to account for energy dissipation at large amplitudes, and
 P_g is the glottal air pressure averaged over the medial fold surface. A similar
equation in the variable x_ℓ is used for the left vocal fold. Both x_r and x_ℓ are
35 defined as positive in the direction of glottal opening.

The glottal airflow is assumed frictionless, stationary, and incompressible,
and any effects of the sub- and supraglottal systems are neglected. Then, the
subglottal pressure is equal to the lung pressure, and the pressure at the glottal
exit is atmospheric. Under such conditions, the glottal pressure P_g may be
approximated by

$$P_g = \frac{\tau P_s}{k_t x_0} (\dot{x}_r + \dot{x}_\ell), \quad (2)$$

where τ is the time delay for the superficial mucosal wave on the fold tissue to
travel half the glottal depth (in the direction of the air flow), P_s is the subglottal
pressure, k_t is a transglottal pressure loss coefficient, and x_0 is the glottal half-
width (in the lateral direction) at the prephonatory position (phonation neutral
40 position) [11].

The natural frequency of the right vocal fold is $\omega_r = \sqrt{K/M}$. Introducing a coefficient of asymmetry Q for the natural frequency of the left vocal fold, in the form $\omega_\ell = Q\omega_r$ [13], then the system of equations for the right and left folds may be written as

$$\ddot{x}_r + \beta(1 + \eta x_r^2)\dot{x}_r + \omega_r^2 x_r = \alpha(\dot{x}_r + \dot{x}_\ell), \quad (3)$$

$$\ddot{x}_\ell + \beta(1 + \eta x_\ell^2)\dot{x}_\ell + Q^2 \omega_r^2 x_\ell = \alpha(\dot{x}_r + \dot{x}_\ell), \quad (4)$$

where $\beta = B/M$, and

$$\alpha = \frac{SP_s}{k_t a_0 c M} \quad (5)$$

is the aerodynamic coupling, where $a_0 = 2Lx_0$ is the prephonatory glottal area, L is the glottal length (in the anterior-posterior direction), $c = T/(2\tau)$ is the mucosal wave velocity, T is the glottal depth, and $S = LT$ is the medial surface of the vocal folds.

45 2.2. Oscillation threshold

The equilibrium position of the vocal folds is obtained by setting all derivatives to zero in Eqs. (3) and (4), which yields $x_r = 0$, $x_\ell = 0$. A standard stability analysis for that position produces the characteristic equation

$$s^4 + 2(\beta - \alpha)s^3 + [\omega_r^2(Q^2 + 1) + \beta(\beta - 2\alpha)]s^2 + \omega_r^2(Q^2 + 1)(\beta - \alpha)s + Q^2\omega_r^4 = 0, \quad (6)$$

where s is a complex variable. When the subglottal pressure is $P_s = 0$, then $\alpha = 0$ and all roots of Eq. (6) have negative real parts [11]. In this case, the equilibrium position is stable. As P_s increases, the roots cross the imaginary axis and the equilibrium becomes unstable. The oscillation threshold is obtained by letting $s = \pm i\omega$ and separating real and imaginary parts, which yields

$$\omega^4 - [\omega_r^2(Q^2 + 1) + \beta(\beta - 2\alpha)]\omega^2 + Q^2\omega_r^4 = 0, \quad (7)$$

$$(\beta - \alpha)[2\omega^2 - \omega_r^2(Q^2 + 1)] = 0. \quad (8)$$

Solutions to Eq. (8) are

$$\omega = \omega_r \sqrt{\frac{Q^2 + 1}{2}}, \quad (9)$$

and

$$\alpha = \beta \quad (10)$$

Substituting Eq. (9) in Eq. (7) produces

$$\alpha = \frac{\beta}{2} + \frac{\omega_r^2}{4\beta} \frac{(Q^2 - 1)^2}{Q^2 + 1}. \quad (11)$$

Eq. (11) may be simplified by substituting ω_r from Eq. (9), and next defining

$$\Delta = \frac{Q^2 - 1}{Q^2 + 1}, \quad (12)$$

which is a normalized asymmetry coefficient that maps $Q \in [0, \infty)$ into $\Delta \in [-1, +1)$. Finally, substituting α from Eq. (5) and solving for the subglottal pressure, we obtain the oscillation threshold pressure

$$P_s = P_0 \left[1 + \left(\frac{\omega \Delta}{\beta} \right)^2 \right], \quad (13)$$

where

$$P_0 = \frac{k_t \beta a_0 c M}{2S} \quad (14)$$

is its value at the symmetric condition $\Delta = 0$.

Another solution to Eq. (8) is given by Eq. (10), which produces the threshold pressure

$$P_s = 2P_0. \quad (15)$$

In this case, the oscillation frequency at the threshold is obtained by substituting Eq. (10) into Eq. (7), which yields

$$\omega^4 - [\omega_r^2(Q^2 + 1) - \beta^2]\omega^2 + Q^2\omega_r^4 = 0, \quad (16)$$

and may have up to two real solutions.

Both Eqs. (13) and (15) coincide when

$$|\Delta| = \beta/\omega. \quad (17)$$

The above results are summarized and illustrated in Fig. 1. At small asymmetries ($|\Delta| \leq \beta/\omega$), the threshold pressure has a minimum at the symmetric configuration ($\Delta = 0$) and increases monotonically with the asymmetry following Eq. (13). The same pattern applies to the oscillation frequency. Both left and right vocal folds oscillate with the same frequency, given by Eq. (9). On the other hand, at large asymmetries ($|\Delta| \geq \beta/\omega$), the threshold pressure assumes a constant value in relation to the asymmetry, given by Eq. (15). Two different values of the oscillation frequency appear, given by Eq. (16); the lowest one corresponds to the lax vocal fold and the highest one to the stiff vocal fold. Thus, the vocal folds oscillate without synchronization, each one at its own oscillation frequency.

3. Data collection

Measures of oscillation threshold parameters were collected from a mechanical replica of the vocal folds. The replica and data collection method have been described in detail elsewhere [14, 15]. Briefly, the replica consists of two parallel latex tubes filled with water under pressure and supported by a metallic structure. The tubes represent the vocal folds in a 3:1 scale, and the internal water pressure of each tube can be set independently so that a stiffness asymmetry (and consequently, a natural frequency asymmetry) can be imposed in a controlled way. Air from a pressure reservoir is blown through a third latex tube,

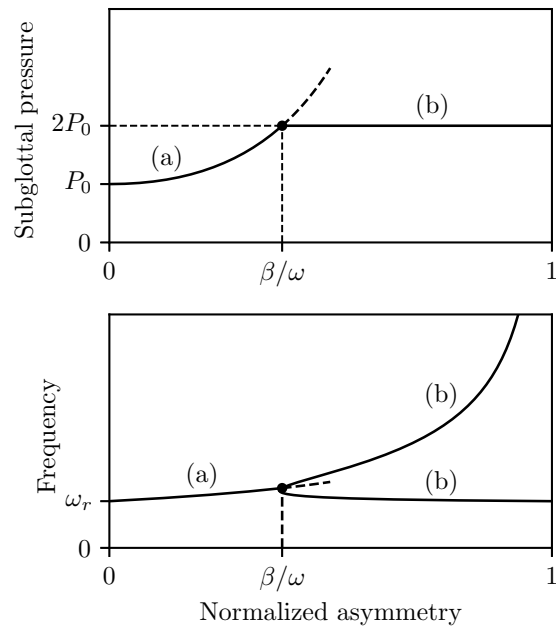


Figure 1: Oscillation threshold parameters. Top: subglottal pressure, (a) Eq. (13), (b) Eq. (15). Bottom: oscillation frequency, (a) Eq. (9), (b) Eq. (16).

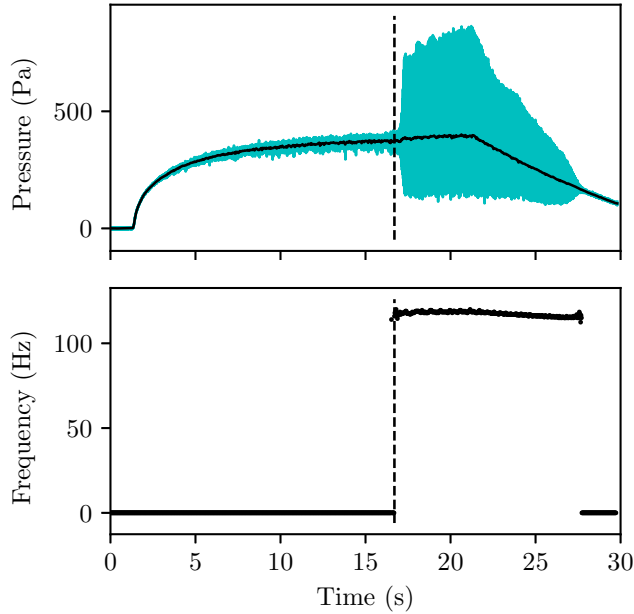


Figure 2: Example of the data collected from the replica when varying the upstream pressure. Top: subglottal pressure; the black curve is the mean pressure. Bottom: fundamental frequency. The broken line in each plot marks the oscillation threshold.

representing the glottal passage, situated in-between the two vocal fold tubes and perpendicular to them.

70 Values of oscillation threshold pressure and frequency were obtained by increasing the air pressure upstream of the replica from zero until an oscillation of the tubes was detected. The time instant of oscillation onset was determined by spectral analysis of the pressure signal measured immediately upstream the replica (subglottal pressure). Then, the mean subglottal pressure and oscillation frequency at that instant were computed (Fig. 2). The glottal area at rest was determined from pictures taken by a digital camera, calibrated with a benchmark grid.

75 Three experiments were performed, in which measures of the above parameters (pressure, frequency and area) were taken at various values of internal (water) pressures of the vocal fold tubes, in symmetrical and asymmetrical configurations. The theoretical model was next fitted to the collected data with the results shown in the next sections.

4. Experiment #1

In this experiment, the internal pressure of both vocal fold tubes was varied simultaneously between 4 kPa and 8.5 kPa, keeping a symmetrical configuration. In the symmetric case, the theoretical model produces a threshold pressure $P_s = P_0$ and an oscillation frequency $\omega = \omega_r$.

The natural frequencies ω_r of the tubes were approximated by their resonance frequencies, obtained from [15]. The first (lowest) resonance frequency is close to the oscillation frequency, and both are shown in the middle panel of Fig. 3 for comparison.

The threshold pressure was computed using Eq. (14). However, as the internal pressure of the tubes is increased, their volume also increases and all parameters in that equation vary. For the transglottal coefficient (k_t) we adopted an expression of the form

$$k_t = \frac{E}{a_0} + F, \quad (18)$$

where E and F are coefficients to be determined [16]. The prephonatory glottal area a_0 was directly measured from the replica, as explained in the previous section, and is shown in the bottom panel of Fig. 3. The other parameters in Eq. (14) are more difficult to model or measure, and were simply lumped into a single coefficient, as follows. Substituting Eq. (18) into Eq. (14), we obtain

$$P_0 = G(1 + F'a_0), \quad (19)$$

where $F' = F/E$ and $G = \beta cME/(2S)$.

The top panel in Fig. 3 shows measures of threshold pressure and the fit provided by the above Eq. (19), with $G = 626.5$ Pa and $F' = -0.052$ mm⁻². The theoretical model produces a good prediction of the data, and we note that the increase of threshold pressure with internal pressure is a direct consequence of the glottal area variation.

5. Experiment #2

In this experiment, the internal pressure of one fold was fixed at 6.0 kPa whereas the internal pressure of the other was varied between 4.1 kPa and 8.3 kPa. The intention was to obtain both negative and positive values of the asymmetry coefficient Δ , and the results are shown in Fig. 4.

The oscillation frequency is well approximated by Eq. (9) (Fig. 4 middle panel). In this case, ω_r was set equal to the second resonance frequency of the tubes, which was obtained from [15].

The threshold pressure was fitted using Eq. (13), and using the same approximation for P_0 as in Experiment #1, which produces

$$P_s = G(1 + F'a_0) \left[1 + \left(\frac{\omega\Delta}{\beta} \right)^2 \right]. \quad (20)$$

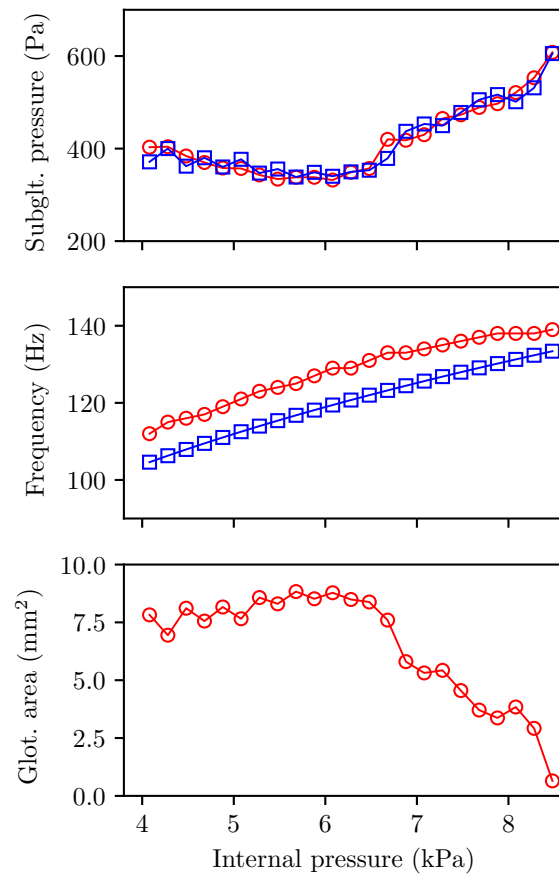


Figure 3: Results of Experiment #1. Top: oscillation threshold pressure, middle: oscillation frequency, bottom: glottal area at rest. Red circles: collected data, blue squares: theoretical results.

The top panel of Fig. 4 shows both the data and results from the above equation with $G = 640.1$ Pa, $F' = -0.039$ mm⁻², and $\beta = 12900$ s⁻¹. Again, we obtained a good match between theoretical results and data.

The values of $|\Delta|$ that separate the regions of small and large asymmetry, given by Eq. (17), fall between 0.106 and 0.116 (depending on the oscillation frequency ω). On the other hand, the range of values of Δ in this experiment is $[-0.116, 0.099]$. Thus, the results are contained within the small asymmetry region (except extreme points at most), which justifies the selection of Eqs. (9) and (13) to fit the data.

6. Experiment #3

In this experiment, the internal pressure of one fold was fixed at 2.5 kPa whereas the internal pressure of the other was varied between 2.5 kPa and 5.4 kPa. The intention was to obtain larger values of the asymmetry coefficient Δ , and the results are shown in Fig. 5

The top panel of Fig. 5 shows that the oscillation threshold pressure increases briefly for small values of Δ , next reaches a plateau followed by a decrease. This pattern matches approximately the pattern in the top panel of Fig. 1 except for the decrease of pressure at the right. The border between the regions of small and large asymmetry would be then located at the point when the pressure reaches a plateau (approximately third data point), and the parameters of the theoretical model were adjusted to obtain such result.

The oscillation frequency was approximated by Eqs. (9) and (16) (Fig. 4 middle panel). The value of ω_r was set equal to the first resonance frequency of the tubes, as in Experiment #1. Note that the theoretical model predicts two oscillation frequencies in the region of large asymmetry (one for each vocal fold oscillator, as explained in Section 2.2). On the other hand, the experimental setup produces a single value of the oscillation frequency, which is closer to the highest of the theoretical frequencies. A possible interpretation is that the stiffer vocal fold tube dominates the oscillation entraining the lax one, in a phenomenon similar to the broadband synchronization detected in [11]. However, such a phenomenon can not be captured by our present model owing to its simplicity.

The threshold pressure was fitted using Eqs. (13) and (15), and using the same approximation for P_0 as in Experiment #1. The top panel of Fig. 5 shows both the data and results with $G = 81.8$ Pa, $F' = 0.044$ mm⁻², and $\beta = 27.9$ s⁻¹. The fit is close for the small asymmetry and the plateau region, but it is not able to capture well the decrease of pressure in the right half of the plot. Note that the value of β is much smaller from the one obtained for Experiment #2. One possible explanation could be that the replica was set in a different configuration, as shown by the larger values of prephonatory glottal area in the bottom panel of Fig. 5

The values of Δ that separates the regions of small and large asymmetry, given by Eq. (17), fall between 0.0477 and 0.0460, approximately at the left of

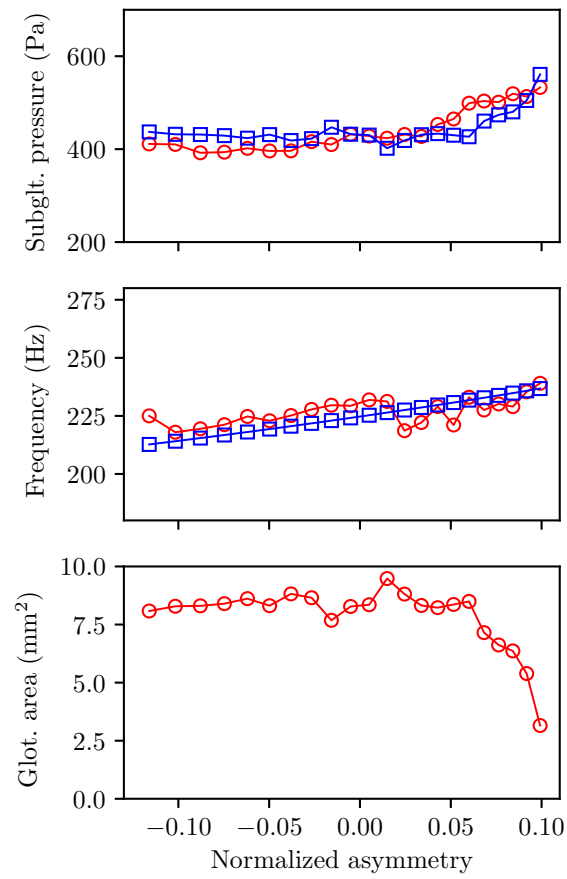


Figure 4: Results of Experiment #2. Top: oscillation threshold pressure, middle: oscillation frequency, bottom: glottal area at rest. Red circles: collected data, blue squares: theoretical results.

third data point (with $\Delta = 0.0496$). The difference with the value obtained for
150 Experiment #2 is caused by the smaller value of parameter β .

7. Conclusions

Our results show different patterns of variation for the phonation threshold
pressure in regions of low vs. high asymmetry of the vocal folds. At low asym-
metry, the threshold pressure increases with the asymmetry, whereas at large
155 asymmetry the threshold pressure assumes a constant value or even a decrease,
as shown by the measured data.

In general, the experimental models given by Eqs. (19) and (20) show good
agreement with the collected data, except for the decrease of threshold pressure
seen at large asymmetry, in Experiment #3. A difficulty when comparing the
160 models with the measured data is that variations of the internal pressure of the
latex tubes affect not only their natural frequency but also their volume, intro-
ducing variations in parameters such as oscillating mass and medial surface that
are not contemplated by the theory. Future research efforts will be dedicated to
solve such difficulties with improved theoretical models and new experimental
165 setups.

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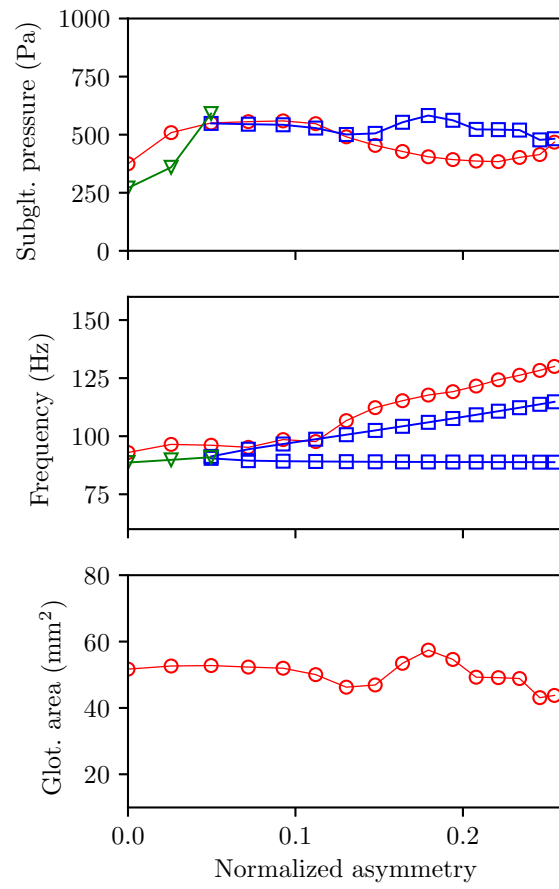


Figure 5: Results of Experiment #3. Top: oscillation threshold pressure, middle: oscillation frequency, bottom: glottal area at rest. Red circles: collected data, blue squares: theoretical results for the large asymmetry region, green triangles: theoretical results for the small asymmetry region.

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