

# Cross-field electron diffusion due to the coupling of drift-driven microinstabilities

Kentaro Hara, Sedina Tsikata

## ► To cite this version:

Kentaro Hara, Sedina Tsikata. Cross-field electron diffusion due to the coupling of drift-driven microinstabilities. Physical Review E , 2020, 102 (2), pp.023202. 10.1103/PhysRevE.102.023202 . hal-02917882

## HAL Id: hal-02917882 https://hal.science/hal-02917882v1

Submitted on 7 Jan 2021

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

## Cross-field electron diffusion due to the coupling of drift-driven microinstabilities

Kentaro Hara<sup>®\*</sup>

Department of Aeronautics and Astronautics, 496 Lomita Mall, Stanford University, Stanford, California 94305, USA

Sedina Tsikata D<sup>†</sup>

ICARE UPR 3021, Centre National de la Recherche Scientifique (CNRS), Orléans, France

(Received 29 December 2019; revised 23 May 2020; accepted 10 July 2020; published xxxxxxxxx)

In this paper, the nonlinear interaction between kinetic instabilities driven by multiple ion beams and magnetized electrons is investigated. Electron diffusion across magnetic field lines is enhanced by the coupling of plasma instabilities. A two-dimensional collisionless particle-in-cell simulation is performed accounting for singly and doubly charged ions in a cross-field configuration. Consistent with prior linear kinetic theory analysis and observations from coherent Thomson scattering experiments, the present simulations identify an ion-ion two-stream instability due to multiply charged ions (flowing in the direction parallel to the applied electric field) which coexists with the electron cyclotron drift instability (propagating perpendicular to the applied electric field and parallel to the  $E \times B$  drift). Small-scale fluctuations due to the coupling of these naturally driven kinetic modes are found to be a mechanism that can enhance cross-field electron transport and contribute to the broadening of the ion velocity distribution functions.

DOI: 10.1103/PhysRevE.00.003200

g

10

11

12

13

14

15

16

17

18

19

20

## I. INTRODUCTION

Electron diffusion across magnetic field lines plays an 21 important role in a variety of contexts, including fusion, astro-22 physical, ionospheric, and cross-field plasma discharges. Par-23 tially magnetized plasmas, where ions are nonmagnetized and 24 electrons are magnetized, exhibit enhanced electron mobility, 25 i.e., reduced electron confinement, in the direction across the 26 magnetic field lines [1,2]. Plasma turbulence is of critical 27 importance for understanding transport of charged species [3]. 28 A number of key kinetic instabilities have been investigated in 29 the literature in the context of electron transport, including, 30 but not limited to, the electron cyclotron drift instability 31 (ECDI) [4-8], modified two-stream instability (MTSI) [9,10], 32 and ion acoustic instability (IAI) [11–13]. 33

Although electron diffusion across the magnetic field lines 34 can be caused by a plasma wave in the  $E \times B$  direction, 35 microturbulence may be driven not only by one type of linear 36 instability but by the nonlinear interaction of multiple linear 37 instabilities [14]. In a laboratory cross-field discharge, theoret-38 ical and numerical studies identified the plasma waves driven 39 by the ECDI [15–17] and these results were subsequently sup-40 ported by coherent Thomson scattering experiments [18–21]. 41 In recent years, an increasing number of numerical studies 42 have been undertaken by several groups revisiting this insta-43 bility [22–26] and its role in transport. 44

<sup>45</sup> One of the key experimental results in Ref. [20] was the de<sup>46</sup> tection of a plasma wave in the cross-field direction (parallel
<sup>47</sup> to the applied electric field), exhibiting a spatial scale similar

to that of the ECDI observed primarily in the  $E \times B$  direc-48 tion. Subsequent linear kinetic theory analyses revealed that 49 such cross-field oscillations observed in experiments can be 50 initiated by the ion-ion two-stream instability (IITSI) [27-31] 51 due to the presence of singly and doubly charged ion streams. 52 Generally, mode coupling of different instability mechanisms 53 plays an important role in plasma transport, particularly in 54 the nonlinear saturation phase of instabilities. However, it is 55 difficult to evaluate the effects of such mode coupling on 56 electron transport, e.g., current density, using diagnostic tools 57 or linear theories. The linear growth rate denotes how fast 58 an instability develops but does not account for how large its 59 amplitude ultimately becomes, i.e., at what level the nonlinear 60 saturation occurs. High-fidelity plasma simulations are there-61 fore of critical importance to investigate nonlinear dynamics 62 of coupled plasma instabilities and the corresponding electron 63 transport. 64

This paper analyzes the microturbulence that develops due to the mode coupling between the IITSI and ECDI in a lowtemperature magnetized plasma. Theory and simulation of the kinetic instability that results from the interaction of multiple ion streams interacting with electron cyclotron dynamics are reviewed in Secs. II and III, respectively. Section IV discusses the plasma properties, and in particular, the observation of enhanced cross-field electron transport and modification of the ion distribution function resulting from the mode coupling.

## **II. KINETIC INSTABILITIES**

65

66

67

68

69

70

71

72

73

74

Let us consider a partially magnetized plasma where an  $^{76}$  external electric field is applied in the *x* direction and a  $^{77}$  magnetic field is applied in the *z* direction, as shown in Fig. 1.  $^{78}$ 

<sup>75</sup> 

<sup>\*</sup>kenhara@stanford.edu †sedina.tsikata@cnrs-orleans.fr

soumansikata e ciii s-Offeans.II

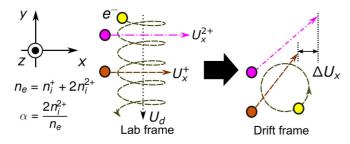


FIG. 1. A partially magnetized plasma where a DC electric field component and an external magnetic field are applied in the x and z directions, respectively. The difference between the singly charged ion velocity  $U_i^+$  and the doubly charged ion velocity  $U_i^{2+}$  in the x direction is denoted by  $\Delta U_x$ . Gyrating electrons move with an azimuthal drift,  $U_d$ , in the -y direction.

<sup>79</sup> Nonmagnetized ions are considered and are electrostatically <sup>80</sup> accelerated in the *x* direction while an electron drift,  $U_d$ , is <sup>81</sup> formed in the -y direction. Here, two cold ion streams are <sup>82</sup> considered in the *x* direction such that  $n_e = n_i^+ + 2n_i^{2+}$ , where <sup>83</sup>  $n_e$  is the electron density,  $n_i^+$  is the singly charged ion density, <sup>84</sup> and  $n_i^{2+}$  is the doubly charged ion density. Here,  $\alpha = 2n_i^{2+}/n_e$ <sup>85</sup> is introduced, i.e.,  $n_i^+/n_e = 1 - \alpha$ .

## A. Theory: Dispersion relation

86

Assuming for the purposes of this study that the dynamics along the magnetic field are negligible ( $k_z = k_{\parallel} = 0$ ), the twodimensional dispersion relation in the *x*-*y* plane, accounting for two cold ion species and magnetized electrons [7], can be written as

$$(k_{\perp}\lambda_{D})^{2} \left[ 1 - \frac{(1-\alpha)\omega_{pi}^{2}}{(\omega - \mathbf{k} \cdot \mathbf{U}_{i}^{+})^{2}} - \frac{\alpha\omega_{pi}^{2}}{(\omega - \mathbf{k} \cdot \mathbf{U}_{i}^{2+})^{2}} \right] + 1 - I_{0}(b)\exp(-b) + \sum_{n=1}^{\infty} \frac{2\omega^{2}I_{n}(b)\exp(-b)}{(n\omega_{B})^{2} - \omega^{2}} = 0, \quad (1)$$

where  $k_{\perp}^{2} = k_{x}^{2} + k_{y}^{2}$ ,  $\lambda_{D} = [\epsilon_{0}k_{B}T_{e}/(e^{2}n_{0})]^{1/2}$  is the Debye 92 length,  $\omega_{pi} = [e^2 n_0/(m_i \epsilon_0)]^{1/2}$  is the ion plasma frequency 93 (here,  $\epsilon_0$  is the vacuum permittivity,  $k_B$  is the Boltzmann 94 constant,  $T_e$  is the electron temperature, e is the elementary 95 charge,  $n_0$  is the plasma density, and  $m_i$  is the ion mass), 96  $\omega$  and **k** are the frequency and wave vector,  $\mathbf{U}_{i}^{s}$  is the ion 97 bulk velocity for species s = + and 2+ corresponding to 98 singly and doubly charged ions, respectively,  $b = (k_{\perp}r_L)^2$ , 99  $r_L = v_\perp / \omega_B$  is the Larmor radius [here,  $v_\perp$  is assumed to 100 be the electron thermal velocity  $v_{\text{th},e} = (k_B T_e/m_e)^{1/2}$ ,  $\omega_B =$ 101  $eB/m_e$  is the electron gyrofrequency, B is the magnetic field 102 amplitude, and  $m_e$  is the electron mass], and  $I_n$  is the modified 103 Bessel function of *n*th kind.  $I_n(b) \exp(-b)$  is also known as 104 the scaled modified Bessel function. 105

As shown in Fig. 1, the presence of an electron drift, e.g.,  $E \times B$  drift, can be accounted for by shifting the system to the frame of the electron drift. Here,  $\mathbf{k} \cdot \mathbf{U}_i^s = k_x U_x^s - k_y U_d$ , where  $U_x$  is the drift parallel to the applied electric field and  $U_d$  is the electron drift in the y direction. The wave frequency can be shifted by  $\omega - k_x U_x^+ + k_y U_y$  and Eq. (1) can be written

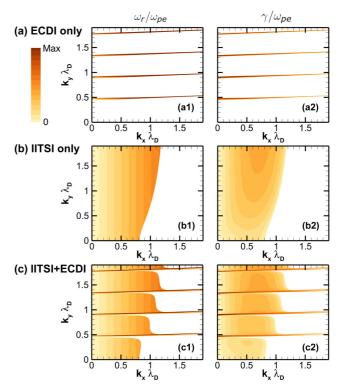


FIG. 2. Instabilities generated in a 2D partially magnetized plasma. (a) Electron cyclotron drift instability (ECDI) due to an electron drift in the *y* direction, where  $\tilde{U}_d = 0.239$ , assuming only singly charged ions, i.e.,  $\alpha = 0$ . (b) Ion-ion two-stream instability (IITSI) due to the mixture of singly and doubly charged ions, where  $\Delta \tilde{U}_x = 3.2 \times 10^{-3}$  and  $\tilde{U}_d = 0$ . (c) Coexisting ECDI and IITSI. Maximum value of color map is 0.002 for  $\omega_r/\omega_{pe}$  (left) and 0.001 for  $\gamma/\omega_{pe}$  (right). Xenon ions are considered. Here, B = 150 G,  $T_e = 25$  eV,  $n_0 = 2 \times 10^{17}$  m<sup>-3</sup>, and  $U_x^+ = 16$  km/s.

in a normalized form as

$$\tilde{k}_{\perp}^{2} \left[ 1 - \frac{\mu(1-\alpha)}{\tilde{\omega}^{2}} - \frac{\mu\alpha}{(\tilde{\omega} - \tilde{k}_{x}\Delta\tilde{U}_{x})^{2}} \right] + 1 - I_{0}(b) \exp(-b)$$
  
+ 
$$\sum_{n=1}^{\infty} \frac{2(\tilde{\omega} + \tilde{k}_{x}\tilde{U}_{x}^{+} - \tilde{k}_{y}\tilde{U}_{d})^{2}I_{n}(b)\exp(-b)}{(n\tilde{\omega}_{B})^{2} - (\tilde{\omega} + \tilde{k}_{x}\tilde{U}_{x}^{+} - \tilde{k}_{y}\tilde{U}_{d})^{2}} = 0, \qquad (2)$$

112

where  $\mu = m_e/m_i$  is the electron-to-ion mass ratio and  $\Delta U_x = U_x^{2+} - U_x^+$  is the difference between the doubly and singly that charged ion velocities in the cross-field direction. The tilde quantities denote normalized parameters. Time, space, and velocity are normalized with respect to the electron plasma frequency,  $\omega_{pe} = [e^2 n_0/(m_e \epsilon_0)]^{1/2}$ , Debye length,  $\lambda_D$ , and electron thermal speed,  $v_{th,e}$ , respectively.

The dispersion relation of the 2D ECDI when  $\alpha = 0$ 120 (singly charged ions only) and  $U_d \neq 0$  is shown in Fig. 2(a). 121 The maximum growth rate is located near  $k_x = 0$ . The ECDI 122 dispersion relation at  $k_x = 0$  is shown in Fig. 3 (cf. Ref. [7]). 123 The 2D dispersion relation yields a resonance condition for 124 the ECDI, namely,  $\tilde{k}_{v}\tilde{U}_{d} = n\tilde{\omega}_{B}$ , where n > 0. Note that the 125 current-carrying ion-acoustic instability can be derived in the 126 limit of zero magnetic field (i.e.,  $b \rightarrow \infty$ ) and singly charged 127 ions (i.e.,  $\alpha = 0$ ) [32]. 128

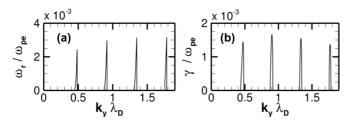


FIG. 3. ECDI dispersion relation at  $k_x \lambda_D = 0$  from Fig. 2: (a) real part of the frequency and (b) growth rate.

Figure 2(b) shows the case where the electron drift is 129 absent, i.e.,  $U_d = 0$ , and  $\alpha$  is set at 0.5 as an illustrative 130 case. The unstable roots (resonant condition) of the IITSI can 131 be found at  $\tilde{k}_x < \sqrt{\mu}/\Delta \tilde{U}_x = O(1)$ . The magnetized electron 132 contribution becomes small under this condition, reducing 133 Eq. (2) to a dispersion relation of a two-stream instability. 134 Since  $\tilde{U}_x^+$  is a few orders of magnitude smaller than  $\tilde{U}_d$ , the 135 ECDI-type resonance with the axial velocity is unlikely to be 136 observed. 137

Figure 2(c) illustrates the coexistence of the ECDI and 138 IITSI. The resonances of the ECDI in 2D (narrow lobes at 139 discrete  $k_v$  values and present for all  $k_x$ ) are apparent, along 140 with the IITSI solutions as shown in Fig. 2(b). It can be seen 141 that the ECDI growth rates are larger than the IITSI growth 142 rates in the present 2D configuration since the ECDI exhibits 143 discrete resonance-type solutions. In addition, the presence of 144 the ECDI lobes in Fig. 2(c), while not affecting the observed 145 IITSI mode frequencies, does reshape the unstable regions 146 corresponding to the IITSI. 147

#### 148

## **B.** Observations from experiments

The IITSI under study in this work is distinct from the ECDI, not only with regard to the instability mechanism, but also in terms of the spatial localization in laboratory cross-field discharges such as Hall effect thrusters and planar magnetrons.

In coherent Thomson scattering experiments [18,20], wave 154 identification is performed through the measurement of elec-155 tron density fluctuations. The diagnostic technique allows for 156 the measurement of such fluctuations not only at different 157 length scales but also along different directions, e.g., aligned 158 primarily with the  $E \times B$  drift in studies of the ECDI or 159 primarily along the applied electric field in studies of the 160 IITSI. 161

These experiments have provided evidence (i) that both 162 ECDI and IITSI modes, although different in their nature of 163 excitation, are associated with density fluctuations of similar 164 spatial scales, i.e., electron Larmor radius scales (on the order 165 of 1 mm), (ii) that the fluctuations driven by ECDI (i.e.,  $k_y \neq$ 166 0) are strongest in the region of maximum  $E \times B$  velocity and 167 detectable further downstream due to convection, and (iii) that 168 the fluctuations driven by IITSI (i.e.,  $k_x \neq 0$ ) are detectable 169 not only in a spatial region overlapping the largest-amplitude 170 ECDI fluctuations but also over a very large axial region 171 over which the ions are accelerated. While the plasma density 172 fluctuations are evident from measurements, it is difficult to 173 quantify the effects of such instability-driven plasma waves on 174 electron transport. As the following discussions will show, the 175

present numerical study captures such features and clarifies the dynamics of each mode.

## III. PARTICLE-IN-CELL SIMULATION OF THE PARTIALLY MAGNETIZED PLASMA

In the present paper, we focus on the physics of the 180 coupling between ECDI and IITSI modes within the same 181 computational framework in the literature. The computational 182 setup to study the  $E \times B$  discharge is identical to that orig-183 inally proposed by Boeuf and Garrigues [24] and used as a 184 benchmarking test case [33]. The 2D particle-in-cell (PIC) 185 simulation used in this paper (explicit PIC with particle and 186 domain decomposition) is described in Ref. [33] and has been 187 compared with other PIC codes. 188

Ionization occurs upstream where the electrons are trapped 189 by the magnetic fields. The crossed electric and magnetic 190 fields generate an  $E \times B$  drift for electrons (the source of the 191 ECDI) and ions are accelerated electrostatically (the source 192 of IISTI in the presence of singly and doubly charged ion 193 streams). The ionization rate is constant in time, leading to a 194 constant ion current density. In steady state,  $\nabla \cdot (\mathbf{j}_{i1} + \mathbf{j}_{i2}) =$ 195  $e(S_{i1}+2S_{i2})$ , where  $\mathbf{j}_{ik}$  is the ion current density and  $S_{ik}$ 196 is the ionization rate for singly (k = 1) and doubly (k =197 2) charged ions. Defining  $\alpha_0$  to be the fraction of doubly 198 charged ion current density, the individual source terms are 199 assigned as  $S_{i1}/S_i = 1 - \alpha_0$  and  $S_{i2}/S_i = \alpha_0/2$ , where  $S_i(x) =$ 200  $S_0 \cos[\pi (x - x_M)/(x_2 - x_1)]$  is the total ionization rate,  $x_1 =$ 20 0.25 cm,  $x_2 = 1$  cm,  $x_M = (x_1 + x_2)/2$ , and  $S_0$  is adjusted so 202 that the total ion current density is  $400 \text{ A/m}^2$ . Xenon ions are 203 considered. Note that  $\alpha_0$  is similar but not identical to  $\alpha$  in 204 Sec. II. 205

The domain size is  $L_x = 2.5$  cm and  $L_y = 1.28$  cm in the 206 x and y direction, respectively. The magnetic field is set to 207  $B(x, y) = B_{\text{max}} + B_0\xi(x)$ , where  $\xi(x) = 1 - \exp[-0.5\{(x - 1)^2 + (x - 1)^2\}$ 208  $(x_L)/\sigma_b\}^2$  and  $B_0 = (B_a - B_{\text{max}})/\xi(0)$  if  $x < x_L$  and  $B_0 = (B_a - B_{\text{max}})/\xi(0)$ 209  $(B_c - B_{\text{max}})/\xi(x_L)$  if  $x \ge x_L$ . Here,  $x_L = 0.75$  cm,  $\sigma_b = 0.625$ 210 cm,  $B_{\text{max}} = 100$  G,  $B_a = 60$  G, and  $B_c = 10$  G. Intermolecu-211 lar collisions, neutral atom dynamics, and transport in the z212 direction are neglected. The potential drop between x = 0 cm 213 and 2.4 cm is kept constant at 200 V [24,33]. The electrons are 214 reinjected randomly in the y direction at x = 2.4 cm to satisfy 215 charge neutrality in the system, i.e.,  $\Gamma_{ec} = \Gamma_{ea} - \Gamma_{i1a} - 2\Gamma_{i2a}$ , 216 where  $\Gamma_{ec}$  is the number of electrons reinjected from the cath-217 ode plane, and  $\Gamma_{ea}$ ,  $\Gamma_{i1a}$ , and  $\Gamma_{i2a}$  are the number of electrons, 218 singly charged ions, and doubly charged ions absorbed at the 219 anode plane, respectively. 220

The average number of particles per cell is 250 in the steady state, which shows satisfactory convergence based on the study in Ref. [33]. The grid size is 50  $\mu$ m in both directions; i.e., the number of cells is 500 and 256 in the *x* and *y* directions, respectively. The simulation utilizes a message passing interface (MPI) and the Poisson equation is solved using Hypre, a linear algebra library. 221

### IV. RESULTS

The effects of doubly charged ions are investigated by varying  $\alpha_0$  from 0% to 25%, which is the range of Xe<sup>2+</sup> 230 observed in  $E \times B$  discharges [34,35]. 231

3

228

178

179

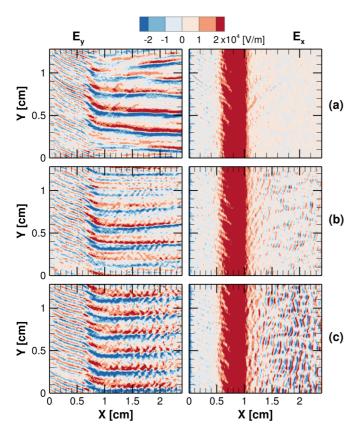


FIG. 4. Instantaneous  $E_y$  and  $E_x$  due to the cross-field plasma instabilities in the presence of singly and doubly charged ion streams. (a)  $\alpha_0 = 0$ , i.e., singly charged ions only, illustrating the ECDI in the azimuthal direction, (b)  $\alpha_0 = 10\%$  (moderate-amplitude IITSI), and (c)  $\alpha_0 = 20\%$  (large-amplitude IITSI). The axially modulated electric field develops as the fraction of doubly charged ions increases. The color bar is saturated, particularly for  $E_x$ , to allow for visualization of the plasma waves in the downstream region.

In this work, a fixed ionization rate is assumed to allow 232 the plasma instabilities to evolve naturally and reach steady 233 state without the need to run the simulation much longer, 234 i.e., to resolve the slow neutral dynamics. The plasma waves 235 driven by the instabilities achieve steady state after 10  $\mu$ s and 236 the simulations are run up to 30  $\mu$ s (or longer) to ensure 237 that the plasma state does not diverge. The same strategy 238 was validated in Ref. [33] in simulations of authors from 239 several groups. While oscillations on the order of 200 kHz 240 (also present in benchmarking simulations in Ref. [33]) are 241 observed in  $\alpha_0 \leq 15\%$ , such oscillations are not seen in the 242  $\alpha_0 = 20\%$  and 25% cases. Investigation of the low-frequency 243 oscillations requires simulations that self-consistently model 244 ionization and collisions, which is reserved for future work. 245

### A. Coexistence of IITSI and ECDI

Figure 4 shows the instantaneous electric fields,  $E_y$  and  $E_x$ , at  $t = 18 \ \mu$ s, in the steady state. The results with only Xe<sup>+</sup>, shown in Fig. 4(a), are consistent with Ref. [33]. The azimuthal plasma fluctuations, i.e.,  $E_y$ , driven by the ECDI are advected downstream. It can be seen from Figs. 4(b) and 4(c) that when Xe<sup>2+</sup> is added, a cross-field (axial) mode in

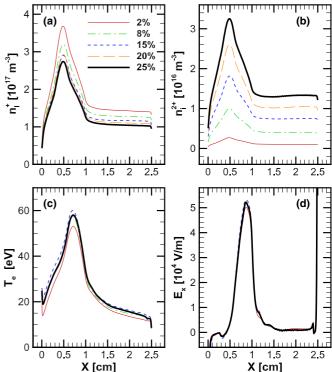


FIG. 5. Plasma properties from the simulation, averaged in the *y* direction and over 5  $\mu$ s. (a) Xe<sup>+</sup> density, (b) Xe<sup>2+</sup> density, (c) electron temperature, and (d) axial electric field. Ionization rate and magnetic field profiles were fixed while varying the ratio of doubly charged ionization to the total ionization rate,  $\alpha_0$ .

the x direction emerges at x > 1 cm, where the ions are accel-253 erated downstream. The amplitude of  $E_x$  in the downstream 254 region increases as the doubly charged ion contribution,  $\alpha_0$ , 255 increases. The axial fluctuation of  $E_{y}$  is also evident. The 256 dominant wavelength of the x fluctuation is approximately 257 1 mm, which corresponds to  $k_x = 6200$  rad/m. Using the 258 time-averaged, y-averaged plasma properties,  $\tilde{k}_x = k_x \lambda_D \approx$ 259 0.5–0.6, which is in good agreement with the theoretical 260 dispersion relation in Fig. 2. 261

The results of Fig. 4 shed light on aspects concerning the 262 two instabilities not previously accessible via experiments and 263 linear kinetic theory analysis [20,32]. Figure 4 shows that for 264 axial positions which coincide with those of the experimental 265 measurements (about  $x - x_L \ge 1$  cm), both the ECDI field 266 modulation (along y) and the IITSI field modulation (along 267 x) are present. Additionally, the present simulations elucidate 268 the regions in which different instabilities are created. The 269 ECDI is driven in the region of the fastest electron drift 270 (approximately where  $E_x/B_z$  is largest) as expected, while 271 the IITSI fully develops once the velocity difference  $\Delta U_x$ 272 between the singly and doubly charged ion streams becomes 273 large enough after acceleration. As previous experiments were 274 only performed outside the channel in the downstream region 275 due to restricted laser beam access, the present simulation 276 results provide information on how the instabilities evolve in 277 a multidimensional configuration. 278

The plasma properties averaged over 5  $\mu$ s and the y direction are shown in Fig. 5. The decrease of Xe<sup>+</sup> density and 280

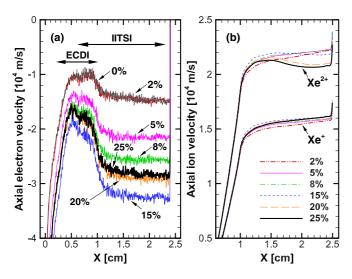


FIG. 6. Enhanced cross-field transport of electrons due to the kinetic instabilities driven by doubly charged ions. The plasma properties are averaged in the *y* direction and over 5  $\mu$ s, 200 sampling. (a) Electron velocity and (b) ion (Xe<sup>+</sup> and Xe<sup>2+</sup>) velocities for various values of  $\alpha_0$ . Note that x = 2.4 cm is where the electrons are injected in the simulation.

increase of  $Xe^{2+}$  density can be observed from Figs. 5(a) 281 and 5(b), as expected. It should be noted that there is a 282 slight increase in the Xe<sup>2+</sup> density in the downstream region, 283 which is due to the deceleration caused by ion trapping due 284 to the wave-particle interaction. This will be discussed in 285 more detail shortly. Figures 5(c) and 5(d) illustrate that doubly 286 charged ions do not significantly alter the electron temperature 28 and axial electric field. 288

#### 289

## B. Cross-field electron and ion transport

Figure 6(a) shows the enhancement of cross-field electron transport by the presence of doubly charged ions in addition to singly charged ions. Compared to cases where  $\alpha_0$  is small, e.g.,  $\alpha_0 \leq 2\%$ , the cross-field electron transport is enhanced by up to approximately 90% at larger  $\alpha_0$  cases. Considering a drift-diffusion approximation for the electron transport in the cross-field direction,

$$u_{e,\perp} = -\mu_{\perp} \left( E_{\perp} + \frac{1}{en_e} \nabla_{\perp} p_e \right), \tag{3}$$

where  $\mu_{\perp}$  is the cross-field mobility and  $p_e$  is the electron 297 pressure. Since the time-averaged plasma properties, such as 298  $E_{\perp}(=E_x)$ ,  $n_e$ , and  $T_e$  (see Fig. 5), are not modified signif-299 icantly by  $Xe^{2+}$ , a large  $|u_{e,\perp}|$  indicates that the effective 300 cross-field mobility has indeed increased. While anomalous 301 electron transport models have been proposed, such as the 302 Bohm diffusion  $\mu_{\perp} = (16B)^{-1}$ , the present PIC results sug-303 gest that  $\mu_{\perp}$  is dependent on the doubly charged ion fraction, 304  $\alpha_0$ . Figure 4(c) shows that the amplitude of the plasma wave 305 in the downstream region becomes approximately the same in 306 the x and y directions, despite the fact that the growth rate of 307 the ECDI is an order of magnitude larger than that of the IITSI 308 as illustrated in Sec. II. The electric field fluctuations in both 309 directions enhance the cross-field transport, but not merely by 310

randomizing the electron motions, which can be inferred from the fact that the electron temperature is not drastically changed as shown in Fig. 5(c). 313

The enhanced electron transport across the magnetic field 314 lines is correlated with the coexistence of the ECDI and IITSI. 315 These two instabilities are generated and interact as follows: 316 (i) The ECDI is created in the upstream region, i.e.,  $x \sim 0.5$ 317 cm. The plasma wave is generated due to the resonance at 318  $k_{\rm v}\lambda_D \approx 0.9$ , where the growth rate is at maximum. However, 319 there is a transition to a larger wavelength mode at x > 0.6 cm. 320 In this region, it is observed that  $k_y \lambda_D \approx 0.3$ , which is possibly 32 due to the physical phenomena not taken into account in the 322 theory. (ii) At 0.7 cm < x < 1 cm, the ECDI and IITSI can 323 coexist since an azimuthal electron drift exists and the velocity 324 difference between Xe<sup>+</sup> and Xe<sup>2+</sup>,  $\Delta U_x$ , increases, which can 325 be seen from Fig. 6(b). (iii) In the downstream region, i.e., 326  $x \ge 1$  cm, since the azimuthal drift is small, the ECDI is 327 unlikely to occur. Instead, the increasing nonzero  $\Delta U_x$  further 328 excites the IITSI. Since the plasma wave generated by the 329 ECDI upstream is advected downstream, the IITSI is first 330 initiated in the presence of the  $k_v$  component driven by the 331 ECDI. 332

It can be observed from Fig. 6(a) that the electron bulk 333 velocity is relatively constant between  $x \in [0.5 \text{ cm}, 1 \text{ cm}]$  for 334 the small  $\alpha_0$  cases (0 and 2%), while its magnitude increases 335 over the same spatial interval (seen in the sloping trend devel-336 oping over this region) in the presence of doubly charged ions 337 ( $\alpha_0$  exceeding 2%). This indicates that the electron mobility 338 is modified due to the presence of doubly charged ions. As 339 can be seen from Fig. 6(b), in this region, the difference 340 in the axial ion bulk velocities is nonzero, e.g.,  $\Delta U_x = 1-4$ 341 km/s, and the azimuthal electron drift is nonzero, e.g.,  $U_d \approx$ 342  $10^{6}$  m/s. With these features taken into account, it is expected 343 that both ECDI and IITSI modes will develop simultaneously 344 within this region, as discussed in Fig. 2(c). 345

The consequence of the cross-field IITSI due to the mul-346 tiple ion streams (here, singly and doubly charged ions) is 347 that the streaming ions with different velocities thermalize and 348 equilibrate. This is apparent in Fig. 6(b) where the cross-field 349 bulk velocity of the Xe<sup>2+</sup> decreases for the  $\alpha_0 = 20\%$  and 350 25% cases in the downstream region ( $x \ge 1.5$  cm). The cross-351 field plasma wave propagates with its own phase velocity and 352 traps, i.e., decelerates and heats, the doubly charged ions, 353 which is similar to the instabilities that occur within the 354 plasma sheath [31]. The nonlinear trapping of  $Xe^{2+}$  coincides 355 with the inverse tendency in the electron transport from  $\alpha_0 =$ 356 15% to  $\alpha_0 = 20\%$  and 25%, as can be seen from Fig. 6(a). 357 The ion velocity distribution functions (VDFs) will be shown 358 later. 359

The IITSI growth rate increases monotonically as  $\alpha_0$  in-360 creases for  $\alpha_0 \in [0, 0.25]$ . From an order of magnitude analy-361 sis,  $\gamma/\omega_{pe} \leq O(10^{-4})$  and the characteristic time for the IITSI 362 to grow,  $\tau \propto \gamma^{-1}$ , is larger than 0.1  $\mu$ s. It is to be noted that 363 the IITSI in the present simulation is a *convective* instability. 364 Since the ions are advected in the x direction with a speed, 365 v, on the order of 10 km/s, the characteristic distance for the 366 IITSI to grow is  $L = v\tau$ . When the growth rate of the IITSI is 367 small, i.e., for a small  $\alpha_0$ , L is large. As  $\alpha_0$  increases, the IITSI 368 growth rate becomes large; thus,  $L \propto \gamma^{-1}$  correspondingly 369 decreases. Simultaneously, the plasma wave amplitude in the 370

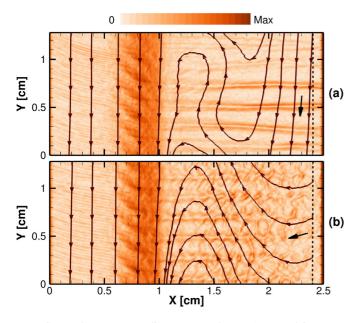


FIG. 7. Electron streamlines averaged over 1  $\mu$ s and instantaneous profile of the magnitude of electric fields,  $|\mathbf{E}| = \sqrt{E_x^2 + E_y^2}$ in Fig. 4, for the (a) ECDI and (b) ECDI and IITSI cases. Maximum value of  $|\mathbf{E}|$  is 80 kV/m. The vertical dashed line indicates the plane of electron injection. Arrows are shown to help the visualization of the electron streamline near the electron injection plane at x = 2.4 cm.

axial direction, or equivalently  $E_x$ , increases for a larger  $\alpha_0$ , as shown in Fig. 4. The characteristic length over which the IITSI grows becomes on the order of a few millimeters. This can be seen also from Fig. 6(b), where the deceleration of Xe<sup>2+</sup>, potentially due to the saturation of the axial wave, is apparent from x > 1.5 cm for  $\alpha_0 = 20\%$  and 25%.

## 377

## C. Electron turbulent transport

Figure 7 shows the effects of the multidimensional plasma wave structures on the electron streamline to investigate the enhanced cross-field electron transport. The streamline denotes the direction of the time-averaged electron current. The ECDI-only case in Fig. 7(a) corresponds to  $\alpha_0 = 2\%$  while Fig. 7(b), showing both ECDI and IITSI, corresponds to  $\alpha_0 =$ 20%.

One of the most notable observations from Fig. 7 is the dif-385 ferences in electron streamline, i.e., direction of the electron 386 flow, near the plane of electron injection at x = 2.4 cm (see 387 the arrows in Fig. 7), despite the similarity of the averaged  $E_x$ 388 profiles, as shown in Fig. 5(d). The temporally and spatially 389 averaged electron flux can be written as  $\langle \Gamma_{ex} \rangle = \langle n_e E_y \rangle / B_z$ 390 and  $\langle \Gamma_{ey} \rangle = -\langle n_e E_x \rangle / B_z$  [36,37]. Consider that plasma prop-391 erties can be written as  $Q = Q_0 + Q'$ , where  $Q_0$  and Q' denote 392 the steady-state value and fluctuation of  $Q = n_e, E_x, E_y$ . Here, 393 the electron flux in the cross-field (x) direction can be given 394 as 395

$$\langle \Gamma_{ex} \rangle = \frac{\langle n'_e E'_y \rangle}{B_z} \tag{4}$$

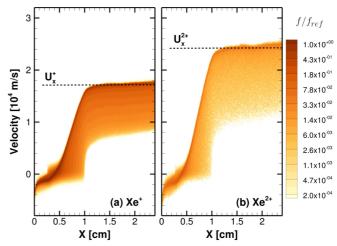


FIG. 8. The instantaneous ion velocity distribution function for  $\alpha_0 = 2\%$ , averaged over the y direction, for (a) Xe<sup>+</sup> and (b) Xe<sup>2+</sup>. The horizontal dashed lines indicate the corresponding ion velocity  $U_x^{Z+} = (ZeV_d/m_i)^{1/2}$ , where Z is the number of charges. The reference VDF value for Xe<sup>+</sup> is chosen to be approximately the maximum value of Xe<sup>+</sup>,  $f_{\text{ref}} = f_{\text{max}}^+$ . Additionally,  $f_{\text{ref}} = 0.1 f_{\text{max}}^+$  is used for the VDFs of Xe<sup>2+</sup>.

since  $E_{y0} = 0$  taking the average of  $E_y$  in the y direction (cf. periodic boundary condition). The electron flux in the y direction can be written as

$$\langle \Gamma_{ey} \rangle = -\frac{n_{e0}E_{x0}}{B_z} - \frac{\langle n'_e E'_x \rangle}{B_z}.$$
 (5)

The angle bracket quantities in Eqs. (4) and (5) denote the turbulent contribution, i.e., fluctuation-based transport.

Figure 7(a) shows that  $|\langle \Gamma_{ex} \rangle| < |\langle \Gamma_{ey} \rangle|$  within  $x \in [2 \text{ cm}, 401$ 2.4 cm] where the electrons are injected. The injected electrons primarily flow in the -y direction for the ECDI-only case, which is consistent with the  $-E_{x0} \times B_z$  drift. The finite  $|\langle \Gamma_{ex} \rangle|$  indicates that azimuthal  $E_y$  fluctuations  $(k_y \neq 0)$  induce the electron transport across the magnetic field in the absence of collisions, as discussed in Eq. (4).

In contrast, in the presence of the coupled ECDI and IITSI 408 as shown in Fig. 7(b), electrons adopt more axial trajectories 409 in the -x direction, indicating  $|\langle \Gamma_{ex} \rangle| > |\langle \Gamma_{ev} \rangle|$  within  $x \in [2]$ 410 cm, 2.4 cm]. The amplitude of  $E_x$  fluctuation increases and 411 the  $E_y$  fluctuations become multidimensional, i.e.,  $k_x \neq 0$  and 412  $k_v \neq 0$ , in the coupled ECDI and IITSI case, as shown in 413 Fig. 4(c). This is further evidence that the cross-field electron 414 transport is enhanced by small-scale plasma fluctuations due 415 to the presence of the axial plasma wave  $(k_x \neq 0)$  in addition 416 to the azimuthal fluctuations  $(k_v \neq 0)$ . Note that the electrons 417 are advected in the +y direction at  $x \in [1 \text{ cm}, 1.7 \text{ cm}]$  in 418 Fig. 7. While such trajectories can be influenced by various 419 drifts, including  $E \times B$ , diamagnetic, and gradient drifts [38], 420 the cross-field electron flux is enhanced in the presence of 421 singly and doubly charged ion streams, as shown in Fig. 6(a). 422

## D. Broadening of ion velocity distribution functions

423

Figure 8 shows instantaneous ion velocity distribution 424 functions (VDFs) averaged over the *y* direction for both 425 Xe<sup>+</sup> and Xe<sup>2+</sup>. Here,  $\alpha_0 = 2\%$ . The particles are sampled 426

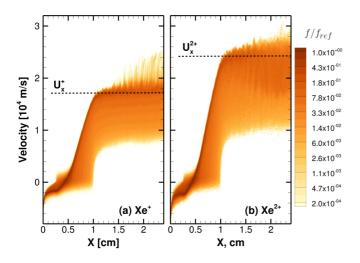


FIG. 9. Cross-field ion trapping observed in  $\alpha_0 = 20\%$  from the instantaneous ion velocity distribution function averaged over the *y* direction. Color map is identical to Fig. 8.

into the discretized phase space, here  $\Delta x = 5 \times 10^{-5}$  m and  $\Delta v = 100$  m/s. The ion bulk velocities obtained from the PIC simulation agree well with the values,  $U_i^+$  and  $U_i^{2+}$ , which assume a steady-state acceleration of ions across the discharge voltage,  $V_d$ . Here,  $U_x^+ \approx 1.7 \times 10^4$  m/s and  $U_x^{2+} \approx$  $2.4 \times 10^4$  m/s assuming a potential drop of  $V_d = 200$  V.

As shown in Fig. 8, the ion VDFs have some spread in the velocity space due to the spatial profile of the ionization rate. Such a velocity spread, i.e., nonzero ion temperature, can damp the two-stream instabilities. The electron transport at  $\alpha_0 \leq 2\%$  in our PIC simulation is indeed similar to that of the singly charged ion only case, i.e.,  $\alpha_0 = 0$ , which is illustrated in Fig. 6(a).

Figure 9 shows the ion VDFs for  $\alpha_0 = 20\%$ . While the ions 440 form a beamlike structure for cases with smaller  $\alpha_0$  (Fig. 8) 441 since the  $E_x$  fluctuation is small, by increasing the doubly 442 charged ion contribution, ion trapping features now appear in 443 both Xe<sup>+</sup> and Xe<sup>2+</sup>. The phase velocity of the plasma wave in 444 the x direction is between  $U_x^+$  and  $U_x^{2+}$ . Perturbation of Xe<sup>2+</sup> 445 by the axial plasma wave is observed in a wide range of  $\alpha_0$ 446 since some Xe<sup>2+</sup> particles are already populated in the range 447 of the wave velocity,  $v_{\phi}$ , which is between  $U_x^+$  and  $U_x^{2+}$ . The 448 phase velocity can be estimated as  $v_{\phi} = \hat{\omega}/k_x \approx \hat{U}_x^+ + c_s$ . 449 However, without the axial plasma wave, there are virtually 450 no Xe<sup>+</sup> ions in the range of  $v_{\phi} > U_{x}^{+}$ . Hence, the amplitude 451 of the plasma wave must be large enough to perturb and start 452 trapping Xe<sup>+</sup> ions. As can be seen from Fig. 9, the trapping 453 of both Xe<sup>+</sup> and Xe<sup>2+</sup> becomes visible at  $\alpha_0 \ge 20\%$ , which 454 is consistent with the deceleration of doubly charged ion bulk 455 velocity shown in Fig. 6(b). It can be considered that at this  $\alpha_0$ 456 value,  $E_x$  (hence, the potential amplitude,  $\phi_0$ ) becomes large 457 enough such that 458

$$\left|v_{\phi} - U_{x}^{Z+}\right| \geqslant \left(\frac{Ze\phi_{0}}{m_{i}}\right)^{1/2},\tag{6}$$

where  $v_{\phi}$  is the phase velocity of the wave and  $U_x^{Z+} = (ZeV_d/m_i)^{1/2}$  is the ion beam velocity for multiply charged ion states Z = 1 and 2. The right-hand side of Eq. (6) is 477

503

the trapping velocity of charged species. The results strongly indicate that the decrease in electron current from  $\alpha_0 = 15\%$  to 20%, as shown in Fig. 6(a), is correlated with the ion trapping.

These findings provide better insight into the significance 466 of some experimental results. Broadening of the Xe<sup>+</sup> ion 467 distribution has been observed in laser-induced fluorescence 468 measurements [39]. In the absence of any axial oscillations, 469 the maximum ion velocity is  $U_i^+$ , limited by the applied DC 470 voltage, as shown in Fig. 8. While some studies have at-471 tributed such high-energy ion formation to wave-riding effects 472 [22,40,41], where the discharge oscillation can generate ions 473 whose energy is larger than the applied DC voltage, the IITSI 474 due to the mixture of Xe<sup>+</sup> and Xe<sup>2+</sup> can broaden the ion VDFs 475 even in the absence of low-frequency discharge oscillations. 476

## **V. DISCUSSION**

As the results discussed in this paper attest, the presence of 478 the axially propagating IITSI, coupled to the azimuthal ECDI, 479 can influence the level of electron transport. The doubly 480 charged ion species concentration need only be low (2% and 481 above) for such effects to develop. The low threshold for the 482 appearance of the IITSI, and its demonstrated effects on trans-483 port, suggest the importance of accounting for doubly charged 484 ions in conventional low-temperature magnetized plasmas. 485 Although we have opted to consider interaction between the 486 two dominant ion streams in this study, triply charged xenon 487 ions have been measured in some  $E \times B$  discharges [42] and 488 the presence of such species may be worth accounting for as 489 well. The formation of axial plasma waves can also be critical 490 for ion beam spreading in the transverse (radial) direction 491 via ponderomotive forces [43,44] and would be expected to 492 influence macroscopic behavior in low-temperature magne-493 tized plasmas. Understanding how the small-scale turbulence 494 affects the large-scale self-organization, e.g., rotating spokes 495 [45], is reserved for future work. 496

While the simulations performed in this paper are in 2D, here the 3D dispersion relation is discussed. The electron component in Eqs. (1) and (2) utilizes the 2D approximation  $(k_{\parallel} = 0)$ , but can be updated to account for the 3D effects  $(k_{\parallel} \neq 0)$ . The 3D dispersion relation [19,46] using normalized quantities can be written as

$$\tilde{k}^{2} \left[ 1 - \frac{\mu(1-\alpha)}{\tilde{\omega}^{2}} - \frac{\mu\alpha}{(\tilde{\omega} - \tilde{k}_{x}\Delta\tilde{U}_{x})^{2}} \right] + \tilde{\xi} \left\{ Z(\bar{\xi})I_{0}(b)e^{-b} + \sum_{n=1}^{\infty} [Z(\xi^{+}) + Z(\xi^{-})]I_{n}(b)\exp(-b) \right\} + 1 = 0, \quad (7)$$

where  $k^2 = k_{\perp}^2 + k_x^2$ ,  $\bar{\xi} = (\xi^+ + \xi^-)/2$ ,

$$\xi^{\pm} = \frac{\tilde{\omega} + \tilde{k}_x \tilde{U}_x^+ - \tilde{k}_y \tilde{U}_d \pm n \tilde{\omega}_B}{\sqrt{2} \tilde{k}_z},\tag{8}$$

and  $Z(\sigma) = \sqrt{\pi} \int \exp(-\tau)(\tau - \sigma)^{-1} d\tau$  is the plasma dispersion relation assuming a Maxwellian distribution function for electrons. In the limit of  $k_z \rightarrow 0$ , the 3D dispersion relation reduces to its 2D version, i.e., Eqs. (1) and (2).

It is known that the resonance peaks of the cyclotron 508 motion, which are present in the 2D dispersion, become 509

## KENTARO HARA AND SEDINA TSIKATA

smoothed in the presence of a nonzero  $k_z \lambda_D$ , leading to 510 a broadband ion acoustic-like spectrum. It is important to 511 note that the 3D ECDI is different from an ion-acoustic 512 instability that is derived assuming nonmagnetized electrons. 513 As the 3D spectra result in a broadband (nonresonant) so-514 lution [19,32], the growth rates of the ECDI can become 515 comparable to those of the IITSI and the demarcation be-516 tween the different modes which is evident in Fig. 2(c)517 would be less clear. Comparison of a full 3D simulation 518 and the 3D linear kinetic theory is reserved for future 519 investigation. 520

521

## VI. CONCLUSIONS

This paper presents insights into the cross-field electron 522 transport in partially magnetized plasmas due to the pres-523 ence of multiply charged ions. Using a multidimensional 524 kinetic simulation accounting for both singly and doubly 525 charged ions, the nonlinear interaction between the ion-ion 526 two-stream instability (IITSI) and electron cyclotron drift 527 instability (ECDI) is investigated. The present study discusses 528 the effects of IITSI driven by the multiply charged ion streams 529 on electron and ion transport, while fixing the plasma charac-530 teristics, which sets up the ECDI. 531

While it has been considered that the azimuthal plasma 532 wave (in the direction of  $E \times B$  drift) may be the dominant 533 contributor to turbulent electron transport across the magnetic 534 field, the present paper illustrates that the plasma wave excited 535 in the axial direction (parallel to the applied electric field) 536 and its coupling with the azimuthal ECDI further enhances 537 cross-field diffusion. Numerical simulations presented in this 538 work reveal the presence of the IITSI driven by the relative 539 velocity between accelerated ions of different charge states 540  $(Xe^+ and Xe^{2+} in the present study)$ . This mode, coupled to 541 the ECDI via the  $E \times B$  drift of electrons, was first detected 542

using coherent Thomson scattering measurements and an ana-543 lytical basis for its appearance was proposed in Ref. [20]. The 544 simulation results presented in this paper capture the features 545 of the instability studied experimentally and analytically and it 546 is observed that the coupling of the ECDI and IITSI enhances 547 the cross-field electron transport by almost 90% of the contri-548 bution due to ECDI alone. Although the linear kinetic theory 549 predicts a growth rate for the IITSI which is smaller than 550 that of the ECDI, the nonlinear saturation (and, in particular, 551 the nonlinear coupling) of the various instabilities plays an 552 important role in the electron transport across the magnetic 553 field. 554

The plasma wave excited in the axial direction also leads 555 to the broadening of the ion velocity distribution functions. 556 Since the phase velocity of the plasma wave lies between 557 the velocities of the singly and doubly charged ion streams, 558 the trapping of doubly charged ions occurs even with small-559 amplitude plasma waves in the axial direction. As the doubly 560 charged ion fraction increases, the amplitude of the plasma 561 wave driven by the IITSI increases and both the singly and 562 doubly charged ions become trapped by the axial plasma 563 wave. This leads to decrease in the bulk velocity of  $Xe^{2+}$  and 564 broadening of the Xe<sup>+</sup> ion VDF. 565

## ACKNOWLEDGMENTS

566

This material is based on work supported by the Air Force 567 Office of Scientific Research under Award No. FA9550-18-568 1-0090 and by the US Department of Energy, Office of 569 Science, Office of Fusion Energy Sciences, under Award No. 570 DE-SC0020623. The authors acknowledge the Texas A&M 571 High Performance Research Computing Center. The authors 572 acknowledge D. Grésillon, C. Honoré, A. Héron, N. Lemoine, 573 and I. D. Kaganovich for prior discussions and the referees for 574 their valuable feedback on the manuscript. 575

- [1] J.-P. Boeuf, J. Appl. Phys. 121, 011101 (2017).
- [2] K. Hara, Plasma Sources Sci. Technol. 28, 044001 (2019).
- [3] S. Yoshikawa and D. J. Rose, Phys. Fluids 5, 334 (1962).
- [4] D. W. Forslund, R. L. Morse, and C. W. Nielson, Phys. Rev. Lett. 25, 1266 (1970).
- [5] D. W. Forslund, R. L. Morse, and C. W. Nielson, Phys. Rev. Lett. 27, 1424 (1971).
- [6] M. Lampe, W. M. Manheimer, J. B. McBride, J. H. Orens, R. Shanny, and R. N. Sudan, Phys. Rev. Lett. 26, 1221 (1971).
- [7] S. P. Gary and J. J. Sanderson, J. Plasma Phys. 4, 739 (1970).
- [8] L. Muschietti and B. Lembège, Adv. Space Res. 37, 483 (2006).
- [9] J. McBride, E. Ott, J. Boris, and J. Orens, Phys. Fluids 15, 2367 (1972).
- [10] S. Matsukiyo and M. Scholer, J. Geophys. Res. 108, 1459 (2003).
- [11] E. R. Priest and J. J. Sanderson, Plasma Phys. 14, 951 (1972).
- [12] C. T. Dum, Phys. Fluids 21, 945 (1978).
- [13] K. Hara and C. Treece, Plasma Sources Sci. Technol. 28, 055013 (2019).
- [14] L. Muschietti and B. Lembège, J. Geophys. Res. Space Phys. 118, 2267 (2013).

- [15] J.-C. Adam, A. Héron, and G. Laval, Phys. Plasmas 11, 295 (2004).
- [16] A. Ducrocq, J.-C. Adam, A. Héron, and G. Laval, Phys. Plasmas 13, 102111 (2006).
- [17] A. Héron and J.-C. Adam, Phys. Plasmas 20, 082313 (2013).
- [18] S. Tsikata, N. Lemoine, V. Pisarev, and D. Grésillon, Phys. Plasmas 16, 033506 (2009).
- [19] J. Cavalier, N. Lemoine, G. Bonhomme, S. Tsikata, C. Honoré, and D. Grésillon, Phys. Plasmas 20, 082107 (2013).
- [20] S. Tsikata, J. Cavalier, A. Héron, C. Honoré, N. Lemoine, D. Grésillon, and D. Coulette, Phys. Plasmas 21, 072116 (2014).
- [21] S. Tsikata and T. Minea, Phys. Rev. Lett. 114, 185001 (2015).
- [22] P. Coche and L. Garrigues, Phys. Plasmas 21, 023503 (2014).
- [23] T. Lafleur, S. D. Baalrud, and P. Chabert, Phys. Plasmas 23, 053503 (2016).
- [24] J.-P. Boeuf and L. Garrigues, Phys. Plasmas 25, 061204 (2018).
- [25] S. Janhunen, A. Smolyakov, D. Sydorenko, M. Jimenez, I. D. Kaganovich, and Y. Raitses, Phys. Plasmas 25, 082308 (2018).
- [26] F. Taccogna, P. Minelli, Z. Asadi, and G. Bogopolsky, Plasma Sources Sci. Technol. 28, 064002 (2019).
- [27] S. P. Gary and N. Omidi, J. Plasma Phys. 37, 45 (1987).

- [28] C. L. Grabbe, Geophys. Res. Lett. 12, 483 (1985).
- [29] J.-E. Wahlund, F. R. E. Forme, H. J. Opgenoorth, M. A. L. Persson, E. V. Mishin, and A. S. Volokitin, Geophys. Res. Lett. 19, 1919 (1992).
- [30] Y. Nakamura and Y. Saitou, Plasma Phys. Controlled Fusion 45, 759 (2003).
- [31] S. D. Baalrud, C. C. Hegna, and J. D. Callen, Phys. Rev. Lett. 103, 205002 (2009).
- [32] S. Tsikata, Ph.D. thesis, Ecole Polytechnique, 2009.
- [33] T. Charoy *et al.*, Plasma Sources Sci. Technol. 28, 105010 (2019).
- [34] L. Garrigues, I. D. Boyd, and J.-P. Boeuf, J. Propul. Power 17, 772 (2001).
- [35] F. S. Gulczinski, III and A. D. Gallimore, J. Propul. Power 17, 418 (2001).
- [36] R. E. Waltz, Phys. Fluids 25, 1269 (1982).
- [37] P. C. Liewer, Nucl. Fusion 25, 543 (1985).

- [38] O. Chapurin and A. Smolyakov, J. Appl. Phys. 119, 243306 (2016).
- [39] N. Dorval et al., J. Appl. Phys. 91, 4811 (2002).
- [40] J. Bareilles, G. J. M. Hagelaar, L. Garrigues, C. Boniface, J.-P. Boeuf, and N. Gascon, Phys. Plasmas 11, 3035 (2004).
- [41] K. Hara and K. M. Hanquist, Plasma Sources Sci. Technol. 27, 065004 (2018).
- [42] J. Bohlmark, M. Lattemann, J. T. Gudmundsson, A. P. Ehiasarian, Y. Aranda Gonzalvo, N. Brenning, and U. Helmersson, Thin Solid Films 515, 1522 (2006).
- [43] I. D. Kaganovich, G. Shvets, E. A. Startsev, and R. C. Davidson, Phys. Plasmas 8, 4180 (2001).
- [44] E. K. Tokluoglu, I. D. Kaganovich, J. A. Carlsson, K. Hara, and E. A. Startsev, Phys. Plasmas 25, 052122 (2018).
- [45] R. Kawashima, K. Hara, and K. Komurasaki, Plasma Sources Sci. Technol. 27, 035010 (2018).
- [46] A. Ducrocq, Ph.D. thesis, Ecole Polytechnique, 2006.