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Phase-locked laser-wakefield electron acceleration

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Subluminal and superluminal light pulses have attracted a considerable attention in the past decades¹⁻⁴ opening perspectives in telecommunications, optical storage, and fundamental physics⁵. Usually achieved in matter, superluminal propagation has also been demonstrated in vacuum with quasi-Bessel beams^{6,7} or Spatio-Temporal Couplings^{8,9} (STCs). While in the first case the propagation was diffraction-free, but with hardly controllable pulse velocities and limited to moderate intensities, in the second a high tunability was achieved, yet with significantly lengthened pulse durations. Here, we report on a new concept that extends these approaches to relativistic intensities and ultra-short pulses by mixing STCs and quasi-Bessel beams to control independently the light velocity and intensity. When used to drive a Laser-Plasma Accelerator¹⁰ (LPA), this concept leads to a new regime, dephasing-free, where the electron beam energy gain increases by more than one order of magnitude.

Electrical breakdown limits electric fields in radio frequency accelerators to about 100 MeV/m. LPAs commonly overcome this restriction by focusing ultra-short laser pulses in a gas to generate

a co-travelling plasma wave¹¹ with accelerating fields (the wakefield) typically 3 orders of magnitude higher. These extreme fields allow for a drastic decrease of accelerator sizes for scientific, medical and industrial applications¹², and makes of LPAs promising candidates for future high-energy colliders¹³. However, for reaching high energies, an electron bunch trapped in the plasma wave has also to experience acceleration on long distances, which remains challenging in LPAs because of 3 phenomena: diffraction, pump depletion and dephasing¹⁴. Pump depletion, i.e. the laser energy transfer to the plasma wave, and diffraction tend to decrease the laser intensity I during its propagation down to a level from which it can no more drive a steady plasma wave ($I \lesssim 10^{18} \text{ Wcm}^{-2}$). Dephasing originates from the difference between the electron bunch velocity and the laser velocity, which results in a progressive shift of the electrons towards a decelerating phase of the wakefield. Significant efforts have aimed at addressing these limitations¹⁵⁻¹⁷. Notably, a record energy of 8 GeV was obtained by guiding pulses in a capillary discharge¹⁸, dealing with the limitations, but not removing them.

Here we propose an acceleration concept which allows to tackle simultaneously these three phenomena, leading to new favorable energy scaling for LPAs. It associates high-intensity quasi-Bessel beams for generating the plasma wave and STCs (i.e. dependencies in the laser field requiring a non-separable time-space description) for controlling its velocity. The quasi-Bessel beam is generated by focusing an ultra-short laser pulse with an axiparabola¹⁹. This aspheric mirror produces a long focal line by reflecting rays towards different focal positions f according to their impinging coordinate on the mirror surface: $f(r) = f_0 + \delta(r)$, with f_0 the small radii focus and δ a function determining the intensity distribution. This optics is similar to axilenses²⁰, but contrary

to its refractive counterparts, axiparabola can focus laser with a high enough intensity for driving a steady plasma wave¹⁹, leading to a propagation regime unachieved with Bessel beams^{21,22}. Diffraction is naturally addressed since the focal line can be much larger than the Rayleigh length of a Gaussian beam of same numerical aperture. The accelerator is also free of pump depletion, because the plasma wave is excited by fresh rays originating from different r at each position along the focal line $z = f(r)$. In other words, the effective diffraction and depletion lengths equal the focal depth of the axiparabola by construction. Thus, dephasing remains the only limit to fix, which implies to control the laser velocity.

The velocity of the axial intensity peak in vacuum (also its phase velocity, in this case) is $v_z = df/dt$, with $t(r)$ the focusing time, giving in the ray optics approximation (see supplementary information):

$$\frac{v_z}{c} = 1 + \frac{r^2}{2f^2}. \quad (1)$$

Equation (1) shows that $v_z(z)$ is superluminal with variations along the optical axis imposed by the choice of $\delta(r)$. However, STCs bring additional degrees of freedom. In particular, a radially dependent pulse front delay $\Delta_t(r)$ leads to a modified focusing time $t + \Delta_t$ but unchanged focusing position, hence tailoring v_z . Within a plasma (of electron density n_e), the pulse velocity shifts in the paraxial approximation by $\Delta v_z = v_g - c$, with v_g the group velocity in the plasma. In the context of LPAs, the delay should be chosen in order to match the velocities of the pulse and of the electron beam ($\approx c$), hence suppressing dephasing. STCs have thus to compensate for both Δv_z

and the velocity change in Eq. (1), leading to:

$$c - \Delta v_z = \frac{\partial_r f}{\partial_r (t + \Delta t)}. \quad (2)$$

The principle of this phase-locked acceleration is illustrated in Fig. 1 (lower part). Appropriate STCs could be applied by using spatial light modulator and deformable mirrors²³, or chromatic optics²⁴, for instance. Figure 2 compares for a constant intensity focal line (see supplementary information) the maximum peak intensity and velocity evolution with and without STCs, stemming from linear spectral propagation simulations²⁵ in vacuum. As expected, a constant intensity line is actually obtained in both cases (Fig. 2a) while the application of the appropriate Δt for an homogeneous plasma (Fig. 2c) leads in vacuum to a constant superluminal ($c - \Delta v_z$) velocity (Fig. 2b).

Once diffraction, pump depletion and dephasing are overcome, the only limit to the electron beam energy gain ΔW is the achievable accelerating field E_z along the focal line. The maximum field amplitude in LPAs verifies $E_z \propto \sqrt{n_e}$, where the proportionality factor depends both on the laser pulse shape and normalized vector potential $a_0 = eA/(m_e c^2)$ ¹⁴. In regular LPAs¹⁰, maintaining high fields requires the plasma wave to be resonantly excited, which constrains the choice of the laser duration τ and spot size w_0 towards $c\tau \sim w_0 \sim \lambda_p$, with $\lambda_p \propto 1/\sqrt{n_e}$ the plasma wavelength. Here, thanks to diffraction-free focusing, the choice of w_0 does not affect the propagation length, thus the resonance condition mainly reduces to $c\tau \sim \lambda_p$. Moreover, the focal depth (so the acceleration length) can be set arbitrary long, but the longer the focal depth, the lower the intensity. For a top-hat beam and a constant intensity focal line of length δ_0 , the normalized

vector potential is (see supplementary information):

$$a_0 \approx 0.68 \sqrt{\lambda_0 [\mu\text{m}] P_0 [\text{TW}] / \delta_0 [\text{mm}]}, \quad (3)$$

with λ_0 the laser central wavelength and P_0 the incident power. The choice of a_0 determines the interaction regime; higher a_0 lead to stronger E_z , but also to stronger nonlinear propagation effects, altering the wakefield stability. In the following, we assumed $a_0 \approx 1.5$, which appeared to be a good trade-off. As setting a_0 fixes the ratio P_0/δ_0 in Eq. (3), the energy gain for a phase-locked acceleration with a resonant pulse duration is:

$$\Delta W = -e E_z \delta_0 \propto P_0 \sqrt{n_e} \quad (4)$$

$$\propto W_L / \tau^2, \quad (5)$$

with W_L the laser energy. To determine the relation between E_z and $\sqrt{n_e}$ involved in Eq. (5) Particle-In-Cell (PIC) simulations were carried out varying n_e , τ and axiparabola parameters (see methods and supplementary material). Figure 3 reports on the energy gain evolution stemming from Eq. (5) with the laser energy and duration. Two new trends emerge: first, a gain proportional to the laser energy and acceleration length, second, drastic increased gains towards shorter laser pulses and denser plasmas. Conversely, dephasing limitations push regular high-energy LPAs towards longer and more energetic pulses propagating in low density plasmas and over long acceleration lengths¹⁴. For example, Ref.¹⁰ estimated a gain $\Delta W = 120$ GeV from a 1120 J laser propagating in a 18 m plasma channel of minimum density $n_e = 1.0 \times 10^{16} \text{ cm}^{-3}$. For the same energy gain, Fig. 3a indicates that 71 J are required for a 15 fs laser, and only 20 J for a 8 fs duration, i.e. almost two orders of magnitude less. Importantly, the propagation is also drastically

shortened to a few tens of centimeters (Fig. 3b) and does not require any guiding. The flying focus technique^{8,9} relying on STCs and spectral chirp, allows for similar tailored velocities and extended Rayleigh lengths, but the large chromatic dispersion required to produce the extended Rayleigh lengths results in increased pulse duration. This prevents its application to phase-locked acceleration, which requires both short pulses and long acceleration distances.

To confirm these estimates, we performed PIC simulations (see methods). Due to its high phase velocity, trapping electrons in the wakefield requires external injection or controlled injection schemes, such as density transition²⁶ and/or colliding-pulse injection²⁷. For sake of simplicity we consider here only the case of a 200 MeV externally injected electron bunch. Figure 4a,b reports on the on-axis evolution of the wakefield in a c-traveling window (axial coordinate $\zeta = z - ct$). The initial settings of Fig. 2 were used for the simulation plotted in Fig. 4a,c. As expected from optimal phase-locking, the electron beam (located at $\zeta \approx -6 \mu\text{m}$) remains in an accelerating phase till the end of the focal line ($z \approx 12 \text{ mm}$) where fresh rays no longer arrive and the central part of the pulse self-focuses. For the same laser energy, Fig. 4b illustrates the standard acceleration from a Gaussian pulse with propagation parameters maximizing ΔW ¹⁰. Here, the electron beam progressively dephases ending the acceleration at $z \approx 6 \text{ mm}$. Bunch spectra show a respective gain of 1.4 GeV (Fig. 4c) and 0.65 GeV (Fig. 4d), in good agreement with predictions. As expected for $a_0 \approx 1.5$, deviations from theoretical modeling appear very limited in Fig. 4a, restraining nonlinear propagation effects to the axis vicinity. Indeed, before attaining $z = f(r)$ beamlets originating from on-mirror radius r travel at low intensities, enabling for an almost linear propagation. With gas targets, such low intensity beamlets may require a preexisting plasma to avoid experiencing

defocusing gradients from ionization fronts. Focusing the outer rays first ($\delta(r) < 0$) should limit this need, avoiding propagation of large aperture low intensity beamlets on many Rayleigh lengths, also minimizing the target volume to be ionized.

In conclusion, the proposed concept allows to get free of the three phenomena which limit the acceleration in LPAs. This phase-locked LPA, along with ongoing advances in laser technology opens unique opportunities. Coupled with high repetition-rate few-cycle lasers^{28,29}, it will boost the development of compact, flexible and bright particle and radiation sources for applications¹². For example, 1 GeV electron beams could be generated, at a 1 kHz repetition rate, from a 12 TW, 5 fs laser pulse. When used with multi-PW lasers³⁰, phase-locked LPAs offer the possibility to drastically reduce both the acceleration length and the required pulse energy (so setup complexity and facility cost), which could be decisive in the design of plasma-based colliders. For instance, a single acceleration stage of 6 m, driven by a 37 PW, 15 fs laser pulse could produce up to 1 TeV electron beams. Propagating a few-fs pulse over long lengths should however face dispersion-broadening. It could be mitigated by limiting the pulse front delay, for instance by using a discontinuous mirror surface to allow for quasi-phase-locking, or by designing a mirror that optimizes the radial delay and by jointly shaping the radial laser intensity profile to keep a constant a_0 along z . Propagation would also benefit from tailored plasma geometries aiming at reducing the crossed length of plasma, as well as from chirped pulse or advanced STCs. Finally, density variations along z could allow to balance the pulse lengthening by a better plasma wave coupling. In parallel, high energy positron beams could be produced with the same scheme by using laser pulses carrying orbital momentum to generate hollow focal lines³¹. The versatility of the proposed concept which

enables both laser diffraction and velocity control (with possibly complex evolution) should also benefit to other plasma-based particle and radiation sources such as: free-electron lasers, X-ray lasers³², Compton scattering³³ and betatron³⁴ sources, as well as to frequency converters³⁵. Similar to Bessel beams³⁶, it could also be used for high order harmonic generation, with the advantage that the pulse front delay uncouples the group velocity from the laser phase velocity.

Methods

PIC simulations. Particle-in-cell simulations were performed with the 3D PIC code CALDER-Circ³⁷, which relies on a cylindrical mesh (r, z) and a Fourier decomposition in the poloidal direction to take advantage of the laser symmetries and reduce the computational time. The simulation of Fig. 4a,c was performed with mesh sizes $dr = 0.8k^{-1}$ and $dz = 0.2k^{-1}$ (with k the wave number at 800 nm) and the two first Fourier modes. The plasma (of density $1.0 \times 10^{19} \text{ cm}^{-3}$) started with a $500 \mu\text{m}$ linear ramp and was initially neutral with a fixed ion background. The number of electrons per cell was 100 close to the optical axis and reduced to 10 for $r > 15 \mu\text{m}$. The beginning of the plasma ramp and of the focal line ($z = f_0 - \delta_0$) were matched. The profile of the on-axis injected electron bunch was assumed trapezoidal with $7k^{-1}$ axial and $6k^{-1}$ radial plateaus (at density $1.25 \times 10^{19} \text{ cm}^{-3}$, leading to 4.5 pC charge) and $1k^{-1}$ ramps in each direction, initial thermal effects were neglected. For finite mesh sizes, PIC calculations introduce numerical dispersion and thus a nonphysical offset in the laser pulse velocity Δv_{num} . With previous parameters, this effect would prevent phase-locked acceleration on the whole focal line. Finer meshes would reduce this deleterious contribution, but at the price of a significant increase in the simulation cost (evolution

as $1/dz^2 dr$), beyond our computational resources at the time of this study. Rather, we chose to fully precompensate for this velocity shift replacing $c - \Delta v_z$ by $c - \Delta v_z - \Delta v_{num}$ in Eq. (2). Fig. 4b mesh parameters were $dr = 1.2k^{-1}$ and $dz = 0.1k^{-1}$. The up ramp was $100 \mu\text{m}$ long and the 25 fs Gaussian pulse was focused to a $11 \mu\text{m}$ spot size at the end of the ramp, then propagated in a $3.2 \times 10^{18} \text{ cm}^{-3}$ density plasma. The externally injected bunch had the same spatial features as for the phase-locked simulation, with a 5 pC charge.

Estimation of the accelerating field. Several PIC simulations were carried out to determine the relation between the accelerating wakefield and the plasma density while using axiparabolas. Different top-hat pulses at 800 nm were focused by different axiparabolas (not necessary in a phase-locked configuration) and we averaged along the focal line the maximal accelerating field along the propagation. That led to the estimation $E_z[\text{GV/m}] \approx 76a_0^{1.5} \sqrt{n_e [10^{19} \text{ cm}^{-3}]}$ (see also supplementary information), i.e. $E_z[mc\omega_p/e] \approx 0.25a_0^{1.5}$, in normalized units.

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Author contributions

CC and CT jointly proposed the concept of phase-locked acceleration, using axiparabola and spatio-temporal couplings. The idea was then developed by CC with advices from VM and CT. CC and CT established the theoretical background, while CC and SS developed codes for optimizing

and simulating axiparabola focus. Simulations were carried out by CC. Finally, CC and CT wrote the manuscript with help from VM and SS.

Data availability

The data that support the plots and findings of this paper are available from CC upon reasonable request.

Competing interests

CT and SS filed a patent application (No EP18305810.6) on axiparabola. The authors declare no other competing financial interest.

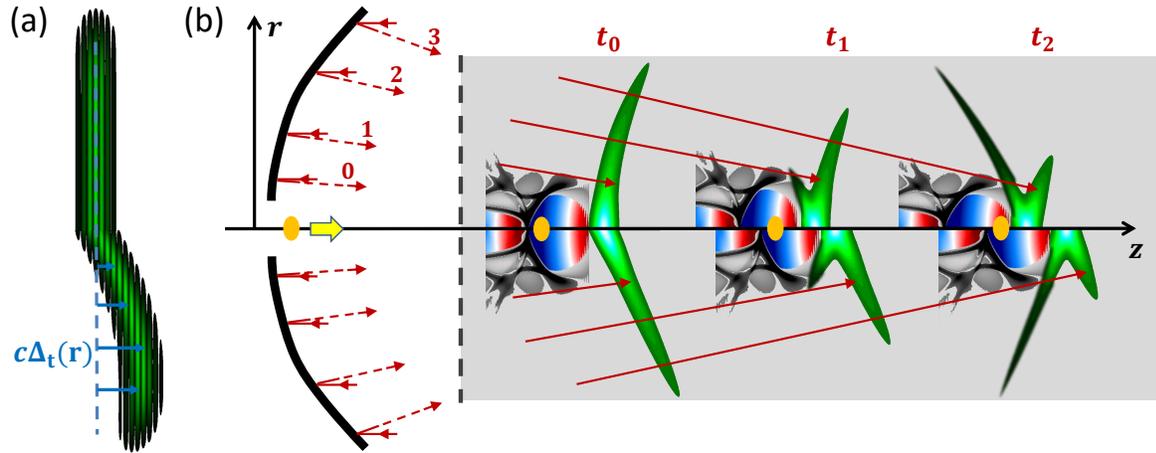


Figure 1: Schematic view of laser plasma acceleration with an axiparabola, without STCs (upper part), and with STCs added as a radially dependent pulse front delay $\Delta_t(r)$ to lead to phase-locked acceleration (lower part). (a) Laser pulse at the axiparabola. (b) Evolution along the focal line of the laser pulse (dark green to light blue color-scale) and of its co-travelling electron plasma wave (gray levels) sustaining strong wakefields (blue to red). Three propagation times are illustrated (ray i focuses at t_i). With STCs, an externally launched relativistic electron bunch (orange dot) remains in phase with the strongest accelerating wakefield (dark blue), whereas it slips towards a decelerating region (red) in the case without STCs.

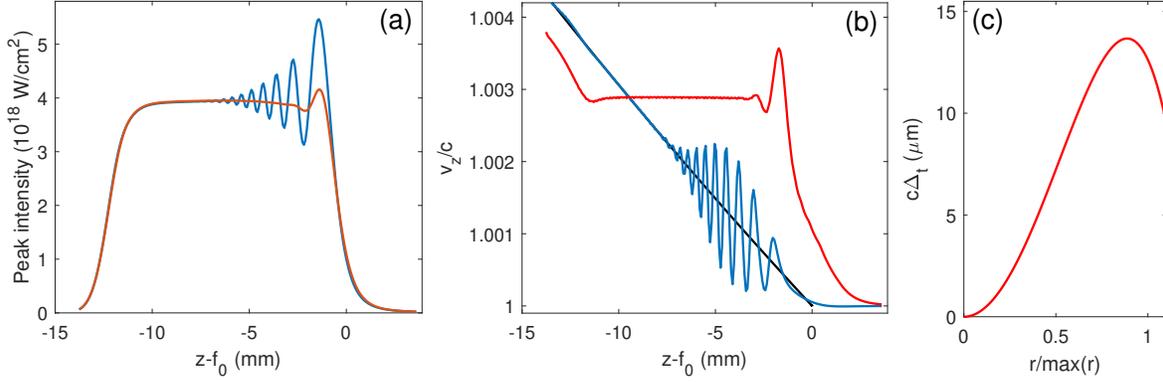


Figure 2: Maximum intensity (a) and peak velocity (b) along a 12 mm focal line obtained by focusing a 1 J, 15 fs top-hat laser pulse in vacuum with a $f/6$ axiparabola. Blue curves correspond to the case without STCs and red ones to the case with the pulse front delay displayed in (c). Black curve (b) gives the prediction from Eq. (1). A 800 nm central wavelength and a plasma density of 1.0×10^{19} cm $^{-3}$ were assumed for the calculation of the STCs which were applied at the axiparabola position (see supplementary information). Oscillations arise from interference effects, beyond the ray approximation description; STCs appear to smooth these effects.

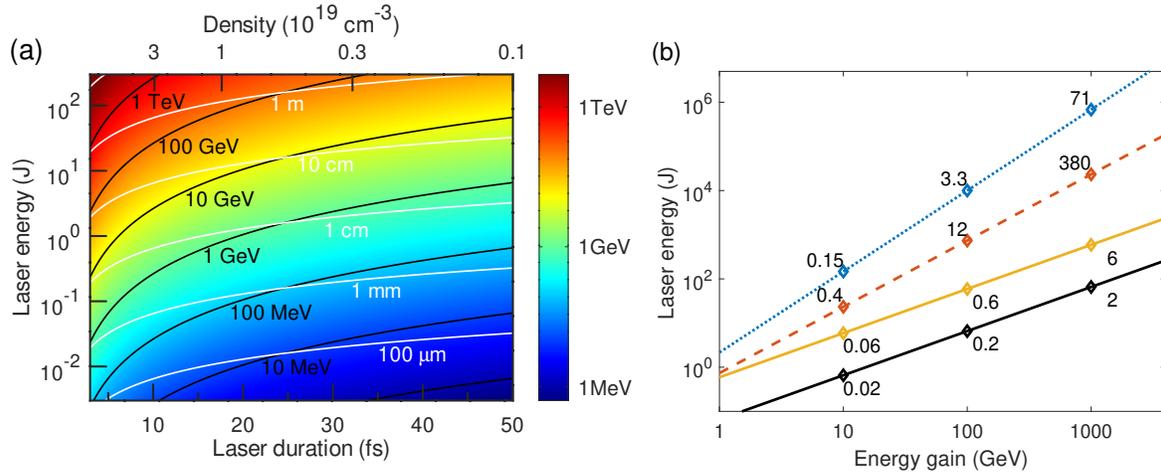


Figure 3: Evolution of the energy gain with accelerator, laser and plasma parameters. (a) Maximal energy gain from phase-locked LPAs (colormap), as a function of laser energy and duration. Lines indicate the evolution for a few energy gains (black) and a few acceleration lengths (white), upper x-axis specifies the corresponding electron density. (b) Laser energy scaling with energy gain, from standard self-guided LPAs (dotted blue), externally guided LPAs (dash red), and from phase-locked LPAs (solid curves) respectively with 15 fs (yellow) and 5 fs (black) laser duration. Diamonds indicate some corresponding acceleration lengths in meters. Condition $c\tau = \lambda_p/2$ was assumed for phase-locked acceleration.

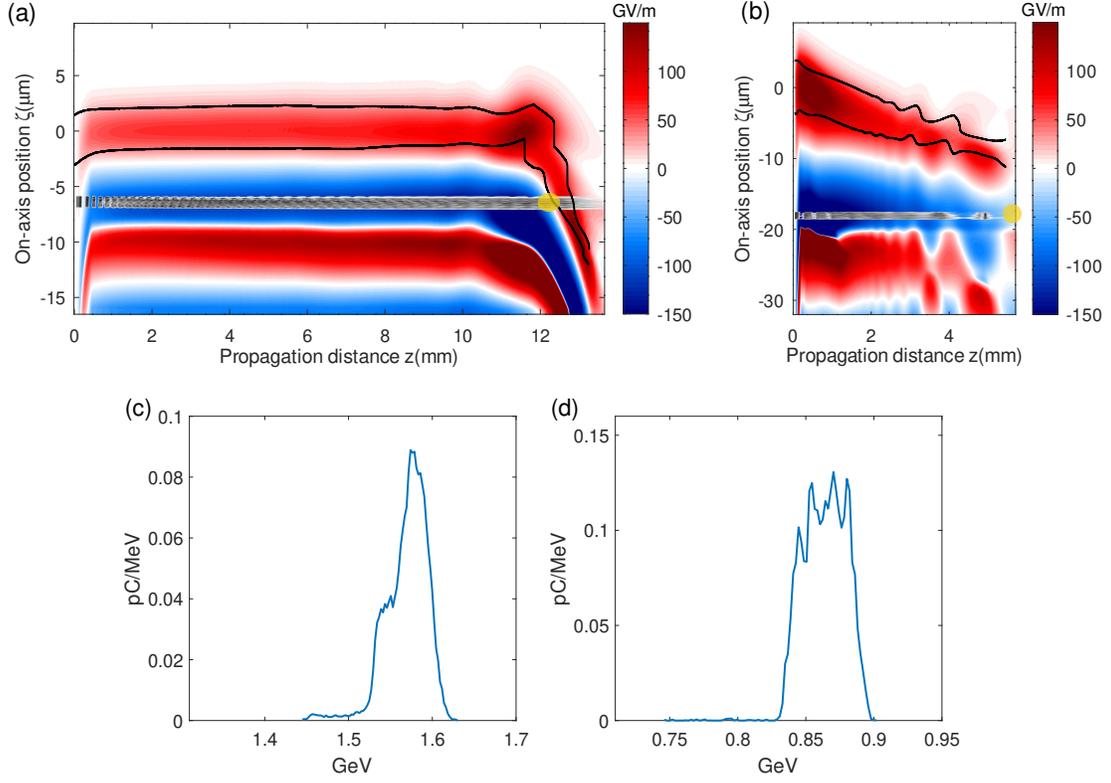


Figure 4: PIC simulations of phase-locked acceleration (a,c) and standard LPA (b,d), with an externally injected electron bunch and the same laser energy (see methods). In a c -traveling window, (a) and (b) show the evolution of the on-axis accelerating field E_z (blue to red colormap), of the electron bunch density (gray arbitrary unit) and of the laser half-maxima (black lines) along propagation. The pulse maximum at its entrance in the plasma is located at $\zeta = 0 \mu\text{m}$. Yellow dots mark the end of the acceleration. Electron energy spectrum at the acceleration end from phase-locked acceleration (c) and standard LPA (d).