

The progressive 6-year-old conserver: Numerical saliency and sensitivity as core mechanisms of numerical abstraction in a Piaget-like estimation task

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MECHANISMS OF NUMERICAL ABSTRACTION

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4	of numerical abstraction in a Piaget-like estimation task				
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The progressive 6-year-old conserver: numerical saliency and sensitivity as core mechanisms of numerical abstraction in a Piaget-like estimation task 3

4 Abstract

In Piaget's theory of number development, children do not possess a true concept of number 5 until they are able to reason on numerical quantity regardless of changes in other 6 nonnumerical magnitudes, such as length. Recent studies have echoed this result by arguing 7 that abstracting number from nonnumerical dimensions of magnitude is a developmental 8 milestone and a strong predictor of mathematics achievement. However, the mechanisms 9 supporting such abstraction remain largely underspecified. We aimed to study how 10 identification of the numerical equivalence in a Piaget-like estimation task by 6-year-old 11 children is affected by (a) the degree of interference between number and nonnumerical 12 13 magnitudes and (b) children's spontaneous orientation to numerosity. Six-year-old children first performed a card sorting task assessing their spontaneous orientation towards 14 15 numerosity, spacing, or item size in a set of dots. Then, they completed a Piaget-like 16 same/different numerical estimation task using two rows of dots in which the length ratio between the two rows varied systematically. Children were less likely to accept the numerical 17 equivalence in the Piaget-like estimation task (a) as the difference in spacing between the dots 18 increased and (b) as the children were more spontaneously oriented towards spacing over 19 number in the card sorting task. Our results suggest that abstracting number depends on its 20 saliency, which varies both as a function of the context (i.e., length ratio between the two 21 22 rows) and of individual differences in children's sensitivity to the numerical aspects of their environment. These factors could be at the root of the observed development of performance 23 in the seminal number-conservation task, which appears as a progressive abstraction of 24 number rather than a conceptual shift, as Piaget hypothesized. 25

26

- 27 Keywords
- 28 Numerical Estimation; Spontaneous Orientation to Magnitudes; Individual differences;
- 29 Heuristics

31 1. Introduction

In Piaget's theory of numerical development, children do not reach a proper understanding of 32 the concept of number until they are able to perceive the conservation of the numerical 33 properties of an array of objects despite visual transformations (Piaget, 1952). Indeed, in the 34 seminal number-conservation task, until approximately 6 or 7 years of age, children fail to 35 perceive the numerical equivalence between two rows of tokens after the length of one row is 36 37 transformed (i.e., by spreading the tokens apart), although they are able to do so when the two rows of tokens have the same length (i.e., before the transformation). Several studies provided 38 converging evidence that success in the number-conservation task in children and adults relies 39 in part on the executive ability to solve the interference between irrelevant nonnumerical 40 dimensions of magnitude (the length or density of the rows of tokens) and the pertinent 41 42 numerical dimension (Houdé & Guichart, 2001, Houdé et al., 2011). The authors suggest that the participants do so by inhibiting an automatic but misleading 'length equals number' 43 strategy. 44

45 Since Piaget's work, research in the field of numerical cognition has revealed the existence of numerical abilities long before children's success in Piaget's number-conservation task. 46 Children's development of the concept of number is thought to build, at least partly, upon 47 48 preverbal representations of quantities that are present very early in infancy (Dehaene, 2001; Izard, Sann, Spelke, & Streri, 2009). One of these numerical intuitions consists in the ability 49 to perceive the approximate quantity represented by a set of objects (e.g., an array of dots). 50 Echoing Piaget's work, many studies investigating these nonsymbolic numerical 51 representations have reported the impact of visuospatial cues on numerical estimation (Gebuis 52 & Reynvoet, 2012). For instance, congruency effects have been observed throughout 53 development in the context of numerical estimation tasks, showing that the participants' 54 performances are influenced by irrelevant spatial dimensions of the stimuli, such as the size of 55

the dots, or the extent of the space occupied by the array (i.e., field area, often measured by 56 the convex hull surrounding the dot array). In particular, field area has been shown to 57 influence numerosity judgments in preschool and school-aged children (e.g., Gilmore, Cragg, 58 Hogan, & Inglis, 2016). In numerical comparison tasks, number/field area incongruent trials 59 (i.e., where the most numerous array of dots is the one occupying less field area) are 60 performed less accurately and more slowly than congruent trials (i.e., where the most 61 numerous array is also the one occupying more field area). Recent studies have observed that 62 the developmental trajectories of these congruency effects can differ depending on the 63 interfering spatial dimension (Gilmore et al., 2016). In the case of field area, its impact on 64 65 numerical representation can be observed all the way into adulthood (Clayton, Gilmore, & Inglis, 2015; Gilmore et al., 2016). As in the number-conservation task (whereby field area is 66 equivalent to the length of the rows of tokens), inhibition seems to play a critical role in 67 68 blocking the influence of irrelevant spatial information to make judgments based on the numerical aspects of the stimuli in numerical estimation tasks (Leibovich, Katzin, Harel, & 69 70 Henik, 2017). These observations support the idea that, beyond children's precision of their numerical representations, their ability to abstract number from other nonnumerical 71 dimensions of magnitude is a strong predictor of math achievement (Gilmore et al., 2013; but 72 see Keller & Libertus, 2015). This is further supported by studies demonstrating that 73 conservation abilities in pre- and early-school years are related to children's mathematical 74 abilities such as math fluency (Cooper & Schleser, 2006; Ramos Christian, Schleser, & Varn, 75 2008). 76 Children's numerical estimation is not only related to their ability to inhibit irrelevant spatial 77

information. For instance, individual differences in children's spontaneous orientation to

number are predictive of math achievement (e.g., Hannula-Sormunen, Lehtinen, & Räsänen,

80 2015). Moreover, children's spontaneous orientation towards numerosity is related to their

ability to perform number/size incongruent trials in a nonsymbolic numerical comparison task 81 (Viarouge et al., 2018). In the study of Viarouge et al. (2018), the authors assessed children's 82 relative spontaneous orientation towards three dimensions of magnitude by asking them to 83 sort cards representing arrays of dots. No further instruction was provided on the sorting 84 criterion the children should use. The cards could be sorted on the basis of three dimensions 85 of magnitude: number, size, or spacing. Children who sorted the cards more frequently by 86 number in the card sorting task (hereafter referred to as the SOMAG task for "Spontaneous 87 Orientation to MAGnitudes") performed better on number/size incongruent trials in a 88 numerical comparison task. This indicated that children's spontaneous orientation towards 89 90 different dimensions of magnitude is related to their ability to solve interferences due to irrelevant visual cues in numerical estimation. Consistent with these results, a study 91 demonstrated that kindergarteners who succeed in the number-conservation task focus more 92 93 spontaneously on number than kindergarteners who fail the number-conservation task, and vice versa for length (Miller & Heller, 1976). 94

95 Taken together, these findings suggested that the development of children's numerical representations relies on a variety of mechanisms allowing them to abstract the numerical 96 aspects of their environment from other nonnumerical dimensions of magnitude. Hence, what 97 had been described by Piaget as a shift between two stages of numerical development, from a 98 nonconserving to a conserving response in contexts such as the number conservation task now 99 appears as a progressive ability to focus on the numerical aspects of one's environment. 100 However, so far, the mechanisms behind this progressive abstraction remain underspecified. 101 Our study is thus aimed to better characterize the mechanisms involved in numerical 102 abstraction, which is crucial to understand the predictive value of early numerical 103 representations for math achievement. 104

Both the ability to inhibit irrelevant dimensions and the spontaneous orientation to these 105 dimensions are likely to contribute to this development. From this perspective, children's 106 performance in the seminal number conservation task should depend both on the strength of 107 108 the interference between the numerical and nonnumerical dimensions and on children's sensitivity to the numerical dimension of the task. In classic nonsymbolic numerical 109 comparison tasks using arrays of dots, isolating nonnumerical dimensions of magnitude to 110 study their impact on performance is particularly tedious. Indeed, all the dimensions of 111 magnitude cannot be controlled for simultaneously. This is why we will use a Piaget-like 112 number conservation task, whereby a same-different numerical judgement is performed on 113 two horizontally arranged rows of tokens. This context allows investigating the impact of 114 length/field area on numerical representation, while keeping other dimensions of magnitude 115 such as size and total surface area constant. To date, no study has manipulated this level of 116 saliency in a systematic manner, while conjointly taking into account individual measures of 117 spontaneous orientation towards magnitudes. 118

119

120 In the current study, we asked 6-year-old children to perform the SOMAG task used in Viarouge et al. (2018) to assess their relative spontaneous orientation towards different 121 magnitudes (number, size, spacing). The participants were also asked to perform a 122 computerized "same/different" numerical estimation task with horizontally arranged dots (as 123 in Piaget's number-conservation task after the length of one row is transformed). The spacing 124 of the dots in one row (and thus the length ratio between the two rows) was systematically 125 varied. Using a Piaget-like same-different task will allow isolating for the first time the 126 selective impact of the field area dimension on numerical equivalence perception by 127 manipulating the strength of the interference between field area and number in a systematic 128 manner at a crucial age of numerical development in Piaget's theory. We investigated whether 129

children's ability to perceive the numerical equivalence between the two rows of dots (a) 130 varies systematically with the degree of interference between the nonnumerical and numerical 131 dimensions of magnitude and (b) is related to children's spontaneous orientation towards the 132 various dimensions of magnitude present in the tasks. We reasoned that, if succeeding in the 133 same-different numerical estimation task requires inhibition of irrelevant nonnumerical 134 dimensions, then children should make more errors as the difference in dot spacing increases. 135 Indeed, as the difference in dot spacing increases, the nonnumerical dimensions of magnitude 136 will interfere to a greater extent with numerical processing. Additionally, children who 137 spontaneously focus more on number over spacing in the SOMAG task should make less 138 139 errors in the same-different numerical estimation task, because spacing is less salient for these children and thus interferes to a lesser extent with their numerical processing. Note that, since 140 item size is maintained constant across the trials of the same-different task, children's 141 142 performances should only correlate with their spontaneous orientation towards number over spacing, but not with their orientation towards number over size. 143

144

145 2. Materials and Methods

146 2.1. Participants

We collected data on the SOMAG task and a numerical same-different task described below in ninety-three typically developing children (47 girls, mean age = 6.1 ± 0.62 years) from kindergarten and first grade classes at three public schools. Sensitivity analyses were performed using G*Power 3.1.9.2 (Faul, Erdfelder, Lang, & Buchner, 2007), revealing that, given our sample size, an alpha-level of .05 and a level of power of .80, minimum effect sizes that can be significantly detected were f = .12 for the repeated-measures ANOVA and r = .23 for the correlation analyses described below.

The same group of children also performed a nonsymbolic numerical comparison task, and 154 the results were reported in (Viarouge et al., 2018). Participation was voluntary after 155 obtaining signed informed consent from the children's parents. Since the SOMAG task 156 assesses children's spontaneous orientation towards either numerical or nonnumerical 157 dimensions of magnitude, this task was always administered first for all children. The 158 numerical same-different and comparison tasks were counterbalanced across the participants. 159 The results described below remained identical when controlling for the order of the two 160 tasks. Children were tested individually by groups of three or four in a quiet room. Apart from 161 encouraging comments, no feedback on accuracy in the numerical same-different task or on 162 the chosen sorting criteria in the SOMAG task was given. Each child received a certificate 163 with stickers for their participation in the study. The teachers and parents were instructed not 164 to talk with the children about the specific content and goals of the study. The study was 165 166 carried out in accordance with national and international norms that govern the use of human research participants. 167

168

169 2.2. Material and design

SOMAG task. In each trial of this computerized task, children were presented with three 170 images introduced to them as cards showing arrays of dots. Two cards (targets) were 171 horizontally aligned at the top of the screen, while the third card (reference) was centered at 172 the bottom of the screen. Children were asked to spontaneously pick one target card to go 173 with the reference card. The instructions were as follows: "Which card goes best with that one 174 (pointing at the bottom card)? This one (pointing at the card on the left) or that one (pointing 175 at the card on the right)? Give me your answer without thinking too much!" The 176 experimenters were instructed not to mention any of the dimensions of magnitude tested in 177 this task (number, size and spacing). Children responded using the same keys as in the 178

numerical same-different task. They were instructed to press the right key (green sticker)
when they wanted to pick the top right card and the left key (red sticker) when they wanted to
pick the top left card.

The collections of dots shown on the cards could be sorted according to the number of dots, 182 aspects of the dot size or of the spacing of the dots (the Size and Spacing dimensions were 183 defined following DeWind, Adams, Platt, & Brannon, 2015). The task included three 184 experimental conditions, depending on the two competing dimensions of magnitude matching 185 with the bottom card (see Figure 1): in one condition, the top cards matched with the bottom 186 card in either number or Size, while Spacing was maintained constant across the three sets of 187 dots (later referred to as the "NumSize" condition); in one condition, the top cards matched 188 the bottom one in Number or Spacing, while Size was maintained constant ("NumSpace" 189 condition); and in one condition, the top cards matched the bottom one in either Size or 190 191 Spacing, while the number of dots was maintained constant ("SizeSpace" condition).

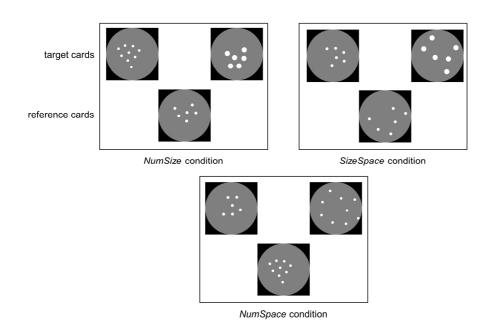
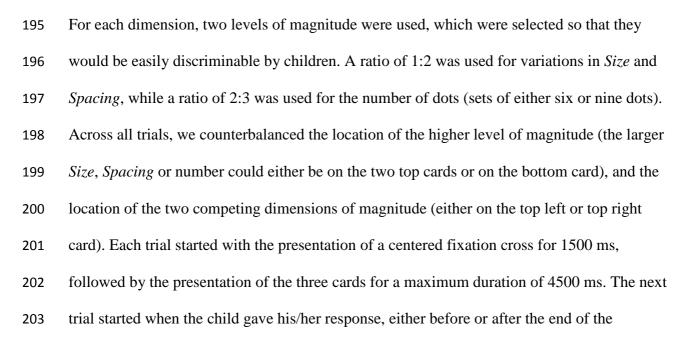


Figure 1: Examples of the stimuli used in the SOMAG task, for each of the three experimental conditions. In each condition, one dimension (Number, Size, or Spacing) is maintained constant. The bottom reference card can be sorted with one of the two top target cards according to one of the two remaining dimensions (e.g. NumSize condition pits the Number and Size dimensions against each other).

193



presentation of the cards. There were 16 trials per condition, resulting in 48 trials total, with a
randomized presentation, and for a total duration of the task of approximately 4 minutes.

206

207 Numerical same-different task. In each trial of the numerical same-different task, children were presented with two horizontal rows of evenly spaced blue dots on a white background 208 and were asked to perform a "same/different" numerical judgment. The two rows were left 209 aligned with each other and were located respectively on the top and bottom half of the screen 210 (at a 1.7° visual angle from the center). The spacing between the dots of each row was varied 211 so that the length of the two rows differed by one of four possible length ratios (1:2, 2:3, 6:7, 212 and 9:10). The location (top or bottom) of the longer row was counterbalanced across trials. In 213 24 test trials, both rows had an equal number of dots (6, 7 or 8). The length of the longest row 214 represented either 12.4°, 14.6°, or 16.7° of visual angle, depending on the number of dots 215 216 presented, and the length of the shortest row varied according to the length ratio tested. To prevent children from learning that the number of dots was the same in both rows while 217 218 maintaining a short duration of the experiment, 16 additional trials had a different number of 219 dots (6 vs. 7, or 7 vs. 8 dots), leading to a total of 40 trials. These numerical ratios were shown to be perceivable by 6-year-olds with an accuracy level of approximately 75% (Halberda & 220 Feigenson, 2008). The task started with four training trials to make sure that the children 221 understood the instructions correctly. All four training trials showed rows with a length ratio 222 of 1:2, two "equal number" trials (6 tokens in each row), and two "unequal number" trials (6 223 vs. 7 tokens), with counterbalanced location of the longest row. Each trial started with the 224 presentation of a centered fixation cross for a duration of 1500 ms, followed by the 225 presentation of the two rows of dots for a maximum duration of 1200 ms. This presentation 226 time was chosen to prevent the use of counting during the task. Children were asked the 227 following: "Do the two rows have the same number of dots, or a different number of dots?" 228

Children were instructed to respond using the K and D keys on an AZERTY keyboard. One 229 green and one red sticker were placed on each of the two keys, and children were instructed to 230 press the green key ("K" on the right) when they thought the number of dots was the same in 231 both rows and the red key ("D" on the left) when they thought the number of dots in each row 232 was different. Due to the tendency of some of the children to spontaneously give their 233 responses verbally or by pointing at the screen, the experimenters then pressed the 234 corresponding response key themselves. For this reason, reaction times were not included in 235 the analyses reported below. When children responded that the number of dots in each row 236 was different, the experimenter followed by asking, "Which row had more?" The child gave a 237 verbal response, which was coded by the experimenter by pressing the up or down arrow key, 238 depending on the location of the chosen row on the screen. The next trial started as soon as a 239 "same number" response or the location of the row judged as containing more dots was 240 241 provided. The 40 trials were presented in a different random order for each child, and the total duration of the task was approximately 5 minutes. 242

243

244 3. Results

245

Effect of the strength of the number/length interference

Three children systematically alternated the right and left responses throughout the task without following the instructions. Their data were removed from the analyses described below. One child's performance fell over the average ± 2.5 standard deviations on both accuracy levels for numerically equal and different trials and was not further analyzed, which led to a total of 89 children included in the analyses. All the results of the statistical analyses reported below were similar when adding the data from this child. For each child, we computed the average accuracy score on the 24 test trials (same number of dots in each row)

for each length ratio. Children judged the two rows as containing a different number of dots 254 89% of the time across all trials. However, a repeated-measures ANOVA using length ratio as 255 a within-subject factor showed a significant effect of the ratio on the children's performances, 256 $F(3, 264) = 24.36, p < .0001, \eta_p^2 = .22$, with accuracy scores increasing with the length ratio 257 (1:2 = 4.31%; 2:3 = 4.12%; 6:7 = 12.92%; 9:10 = 22.85%). Post hoc Bonferroni tests 258 confirmed a significant difference in performance between the 2:3 and 6:7 length ratio (p < 1259 .01) and between the 6:7 and 9:10 length ratio (p < .001) but not between the first two length 260 ratios (p = 1, Figure 2). 261

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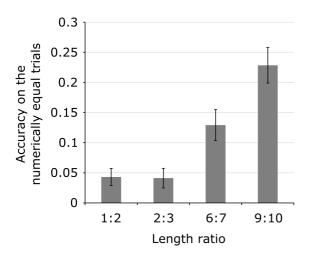
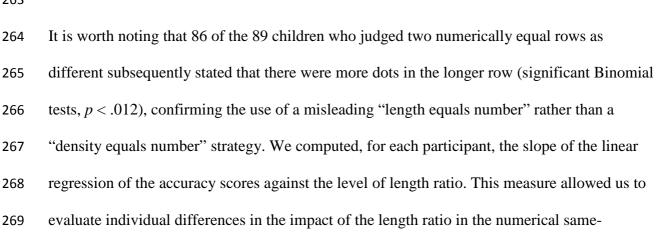


Figure 2: Performance on the numerically equal trials of the numerical estimation task, for each level of length ratios between the two rows of dots. Error bars represent \pm one standard error of the mean.

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270 different task. We observed a significant correlation between this slope and the slope obtained

from the accuracy scores on the 16 filler trials (numerically different rows), r(87) = -0.86, p < .001, showing that the ratio of length impacted the children's performances both on the

- numerically equal and different trials, and confirming the reliability of our measure.
- 274

275 Effect of the spontaneous orientation to numerical and nonnumerical dimensions of

276 magnitude

Despite the same instructions being repeated throughout the SOMAG task, some children had 277 a hard time choosing sorting criteria. Of the 89 children included in the analyses of the 278 numerical same-different task, 13 children did not follow the instructions of the SOMAG task 279 and systematically alternated between the left and right response keys. These children might 280 have been confused by the absence of a clear rule to follow and decided to follow a reassuring 281 strategy. Their data were removed from the following analyses, which were run on a total of 282 283 76 children. We verified that the effect of length ratio on the performance in the samedifferent task was still present in this sample ($F(3, 225) = 23.6, p < .001, \eta_p^2 = .22$), with 284 similar increasing accuracy scores (1:2 = 4.39%; 2:3 = 3.73%; 6:7 = 13.16%; 9:10 = 24.34%). 285 The SOMAG task provided individual scores corresponding to the total number of times each 286 dimension of magnitude (numerosity, Size, Spacing) was spontaneously chosen as a sorting 287 criterion by the child in the three experimental conditions (NumSize, NumSpace, and 288 SizeSpace). We ran correlational analyses between the SOMAG task scores and children's 289 average performances in the numerical same-different task (see Table 1 for a full description 290 of the correlations). The average performance in the test trials of the numerical same-different 291 292 task (i.e., trials in which there was a conflict between number and length/field area) was associated with the score in the NumSpace condition of the SOMAG task, r(74) = .30, p < .00293 .01, but not with the NumSize or the SizeSpace condition, p > .49. This correlation remained 294 significant after controlling for the exact age of the participants, r(74) = .35, p < .01. This 295

association showed that children who chose to sort the cards according to their numerosity
rather than the spacing of the dots in the SOMAG task were also more likely to make correct
numerical judgments regardless of the difference in the spacing of the dots between the two

rows in the numerical same-different task (Figure 3).

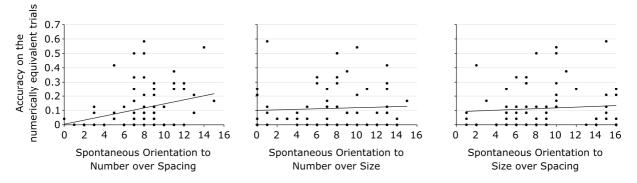


Figure 3: Correlation between the spontaneous orientation to Magnitudes in the three experimental conditions of the SOMAG task and the performance in the numerical estimation task.

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302 Note that, while there was a significant correlation between the two SOMAG conditions

involving Size (r(74) = .75, p < .001) we found no significant relation between the two

conditions of the SOMAG involving the Number dimension (r(74) = .03, p = .77, Table 1).

305 Thus, choosing Number as a sorting criterion over Spacing was not systematically related to a

306 general tendency of orienting towards numerical over nonnumerical dimensions of magnitude.

307 A multiple regression analysis confirmed that adding the NumSize and SizeSpace conditions

to the model did not significantly change the observed relation between NumSpace and our

309 same-different task (
$$\Delta R^2 = .01, F(2, 72) < 1$$
).

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- 311
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- 313

Measures	1	2	3	4
1. Same-Different Task	-	0.3 **	0.06	0.08
2. SOMAG NumSpace (Number)		-	0.03	0.14
3. SOMAG NumSize (Number)			-	- 0.75 ***

4. SOMAG SizeSpace (Size)

Table 1: Table of correlations between the performance on the test trials of the same-different task and the different SOMAG conditions. For each of the SOMAG conditions, the correlations were computed based on the dimension between parentheses.

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315

316 4. Discussion

By conjointly taking into account the impact of the strength of the interference between

numerical and nonnumerical dimensions of magnitude and individual differences in

spontaneous orientation to number, the current study shed new light on the mechanisms

underlying the development of children's ability to abstract number. We showed that both

321 factors significantly contribute to children's ability to handle the number/length interference

322 in a Piaget-like same-different numerical task.

323 First, we provided evidence that a systematic manipulation of the length ratio between the two

324 rows of dots in a Piaget-like same/different numerical estimation task affects children's

performance. Specifically, we found that children's ability to make a "same" judgment on two

rows containing an equal number of dots decreased progressively as the difference in the

327 lengths of the two rows increased. Thus, children's performance on this task decreased as the

- 328 interference between the nonnumerical and numerical magnitudes increased. This result adds
- 329 further support to the idea that the performance observed in numerical judgement tasks are

impacted by nonnumerical magnitudes, even in a same-different task thought to tap more

directly into magnitude representation (Van Opstal & Verguts, 2011).

One of the key advantages of the Piaget-like same/different numerical estimation task 332 designed in the present study is it allows systematic manipulation of the strength of the 333 interference between number and a nonnumerical dimension, with a fixed level of numerical 334 difficulty. Indeed, in our test trials (where the two rows contained the same number of 335 tokens), the evolution of the performance cannot be explained in terms of numerical difficulty 336 and can only be attributed to an influence of the nonnumerical aspects of the task. We argue 337 that manipulating the length ratio modified the strength of the interference between length and 338 number, and concurrently the probability to rely on the "length equals number" misleading 339 heuristic. In turn, this manipulation varied the level of inhibitory control required to block 340 such a misleading strategy in order to perceive the numerical equivalence in our same-341 342 different task. This is in line with previous findings showing that the inhibition of the 'length equals number' strategy is needed to overcome systematic errors in a Piaget-like number-343 344 conservation task (Houdé & Guichart, 2001, Houdé et al., 2011). Second, we found that children tended to make fewer errors in the numerical same-different 345 task when they sorted the cards in the SOMAG task more frequently by number than by 346 spacing. This correlation suggests that the prepotency to rely on the 'length equals number' 347 misleading strategy in the number conservation task is also dependent on individual 348 differences in children's spontaneous orientation towards relevant or irrelevant dimensions of 349 the stimuli. 350

Note that the children's performance in our numerical same-different task was not related to their spontaneous orientation towards number over size or towards size over spacing, as assessed by the SOMAG task. This is consistent with the material of our same-different task, whereby the size of the dots is maintained as a constant and only dimensions related to

density and field area vary. Thus, our results suggest a specificity of spontaneous orientation
towards magnitudes, with different predictive values of orientation towards number over size
v. over spacing, depending on the experimental context and/or possibly age. This hypothesis
is further supported by the lack of correlation between the NumSize and NumSpace
conditions in the SOMAG task.
This specificity is interesting to put in perspective with the results reported in the study of

Viarouge et al. (2018) based on data collected for the same group of children. These results showed that both the NumSize and the NumSpace SOMAG conditions explained significant and distinct parts of the variance in the performance on Size/Number incongruent trials of a nonsymbolic numerical comparison task.

The different patterns of correlation with the SOMAG reported in the current study might be 365 explained by differences between the numerical same-different and comparison tasks. As 366 367 mentioned above, one important aspect of the current study is that the same-different task allows separating the Size and Spacing dimensions more clearly than in the numerical 368 369 comparison tasks, such as the one used by Viarouge et al. (2018). Indeed, in the latter task, 370 given that the Spacing dimension is related both to field area and sparsity (DeWind et al., 2015), variations in these dimensions could have occurred, which in turn might explain why 371 the NumSpace condition was correlated with performance on Size/number incongruent trials. 372 Importantly, in the numerically equal trials of our same-different task, both the size and total 373 surface area of the two rows of dots are maintained as constant, and the impact of different 374 levels of dots spacing in the context of a fixed numerical difficulty is fully isolated. Another 375 potential explanation for this different pattern of correlations might have to do with what the 376 different conditions of the SOMAG are actually capturing. The correlation between the two 377 conditions involving *Size* suggests that children's choices were strongly influenced by this 378 dimension. Added to the lack of correlation between the NumSpace and the other two 379

conditions, this suggests that the NumSpace condition might be capturing children's
spontaneous orientation to Number more specifically. This could then explain why this
condition relates to both tasks involving interferences with number, regardless of the
competing nonnumerical dimension.

A limitation of our study is the lack of a separate measure of children's inhibitory control ability. This would have allowed us to determine the respective contribution of inhibitory control ability and spontaneous orientation towards number over spacing to the performance observed in our Piaget-like same-different task. Further studies are needed to better understand the relation between the ability to process number in contexts in which irrelevant non-numerical dimensions interfere with it, the spontaneous orientation towards relevant and irrelevant magnitudes, and the ability to inhibit these irrelevant dimensions.

Finally, our study provides new insights into the possible mediating factors of the relation 391 392 between early numerical abilities and formal mathematics. In particular, these findings help specify the mechanisms involved in the abstraction of number by suggesting to take into 393 394 account individual differences in spontaneous orientation to numerical and nonnumerical magnitudes. Indeed, recent studies have questioned the predictive value of numerical 395 intuitions for math achievement. In particular, some authors have suggested that inhibitory 396 control acts as a mediating factor of this relation, with mixed results. According to this view, 397 children's capacity to grasp the invariance of number with regard to other dimensions of 398 magnitude would be crucial for their true understanding of the concept of number, beyond the 399 precision of their early numerical representations. This capacity to abstract number from other 400 401 quantities might be particularly important in early school years, when the covariance of number with dimensions such as length might be unintentionally reinforced through 402 education. For instance, the use of nonsymbolic representations of integers via rows of evenly 403 spaced images might strengthen the misleading "number equals length" heuristic. 404

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406

407 5. Conclusion

Altogether, these results indicated that the development of numerical representations in 408 children relies on a variety of factors contributing to children's ability to abstract number 409 410 from other irrelevant, nonnumerical dimensions of magnitude. In particular, we showed that conserving responses in a Piaget-like numerical estimation task appear progressively 411 dependent on the saliency of the numerical dimension. This saliency depended both on the 412 degree of interference with nonnumerical magnitudes and on individual differences in 413 spontaneous orientation towards these dimensions. 414 Our results also provided additional evidence that cognitive development does not rely 415 416 exclusively on the acquisition of knowledge of increasing complexity (Piaget, 1952) but also on children's ability to inhibit misleading strategies and previously acquired knowledge 417 (Bjorklund & Harnishfeger, 1990; Houdé, 2000) and ability that can be expressed more or 418 less easily by the children depending on the context (i.e., the level of interference) and their 419 spontaneous orientation towards different dimensions of the context. 420 In light of current debates regarding the predictive value of numerical intuitions for math 421

422 achievement, our study helps specify the factors involved in numerical development and

423 provides new insights regarding the possible mediating factors of this relation.

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