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# model of interchange turbulent transport: on the correlation between scrape off layer width and core confinement in tokamaks

N. Fedorczak, Mathieu Peret, Philippe Ghendrih, Patrick Tamain, Hugo Bufferand

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- Spectral filament paradigm: self consistent prediction of turbulent spectra ( $n_e, \Phi$ ) of flux driven 2D isothermal interchange turbulence
- Predicts macroscopic transport properties (flux, fluctuations) in scrape-off layer ( $\rightarrow$  SOL width  $\lambda_q$ ) but also in the core ( $\rightarrow$  confinement time  $\tau_E$ )
- SOL transport: quantitative agreement with Tore Supra data (circular plasmas), recovers impact of divertor leg length on SOL width ( $\lambda_q$ ) in TCV, recovers multi-machine parametric sensitivity of  $\lambda_q$
- Core confinement: recovers multi-machine parametric sensitivity of  $\tau_E$  and correlation between core confinement and heat flux width
- Offers a flexible paradigm for addressing the optimization of power exhaust versus core confinement (key: impact of geometry in model)

## 2D isothermal interchange model (TOKAM2D)

Y. Sarazin et al. Phys. Plasmas 5 (12) (1998) 4214–4228

Flux driven (source  $S$ ), control parameters:  $g \approx \frac{\rho_S}{R}$ ,  $\sigma_{\parallel} \approx \frac{\rho_S}{q_{cyl} R}$

curvature // loss rate

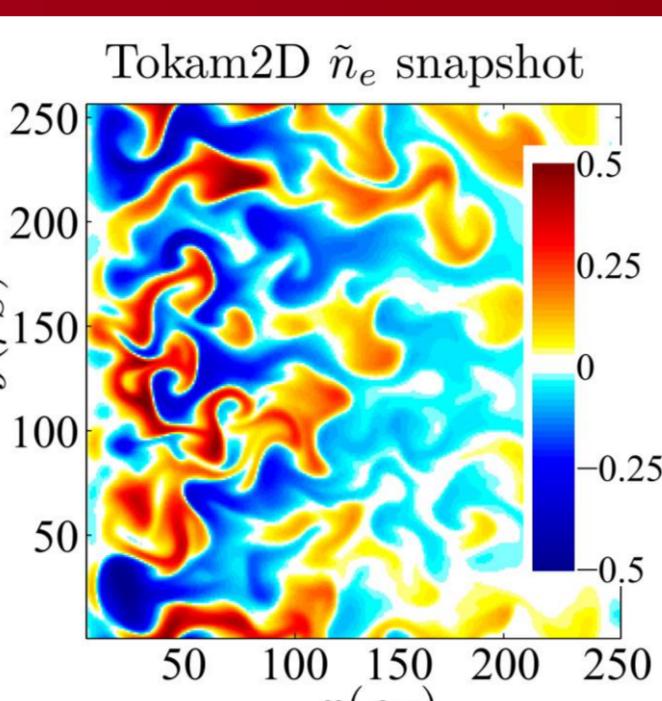
$$d_t n + D\nabla^2 n = S - \sigma_{\parallel} n e^{\Lambda-\Phi}$$

$$d_t = \partial_t + \{\Phi, \cdot\}$$

$$d_t \omega + \nu \nabla^2 \omega = g \frac{\partial_y n}{n} - \sigma_{\parallel} (1 - e^{\Lambda-\Phi})$$

$$\omega = \nabla_{\perp} \Phi$$

Intermittent filamentary transport, exponential SOL, etc



## Test isolated filament model

S. I. Krasheninnikov et al. J. Plasma Phys. 2008, 74, 679

Density filament: size  $\delta_f$  & normalized amplitude  $n_f$   
 $\rightarrow$  drift velocity ( $v_f$ ) predicted from vorticity balance

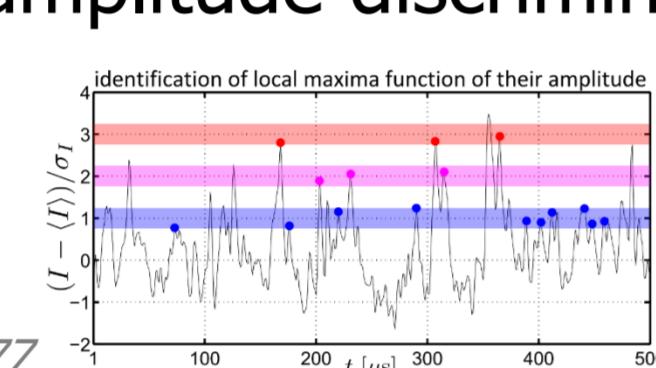
Hyp: well shaped filaments, not the case in simulations

Solution: construction of averaged filaments

$\rightarrow$  conditional average with event amplitude discrimination

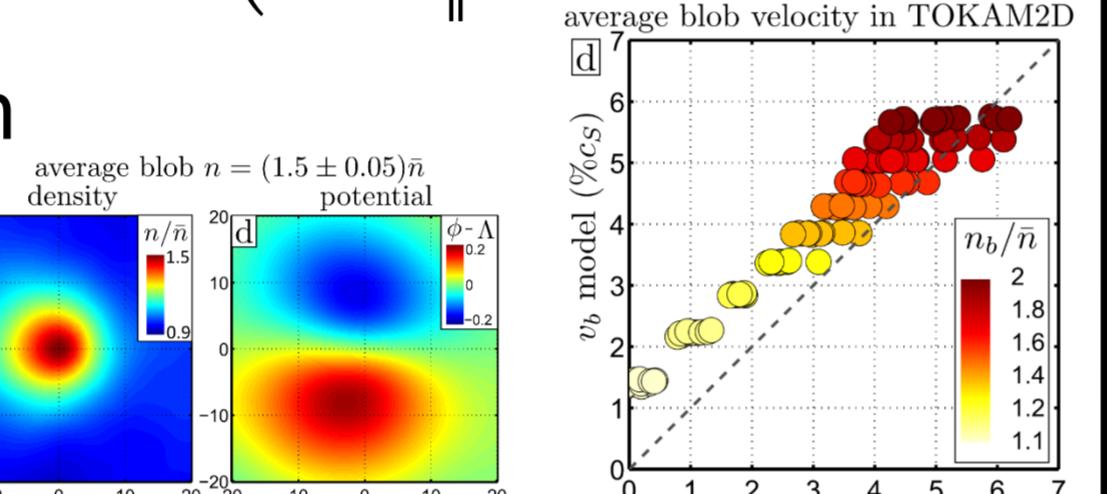
Isolated filament model works on  
TOKAM2D averaged filaments

N. Fedorczak et al. Contrib. Plasma Phys. 2018;58:471–477



$$v_f = \frac{1}{2} \sigma_{\parallel} \delta_b^3 \left[ \sqrt{1 + (\delta_0/\delta_b)^5} + 1 \right]$$

$$\delta_0 = \left( \frac{4g(n_b - 1)}{\sigma_{\parallel}^2} \right)^{\frac{1}{5}}$$



## Spectral filament (SF) model

N. Fedorczak et al. Nuc. Mater. & Energy 19 (2019) 433–439

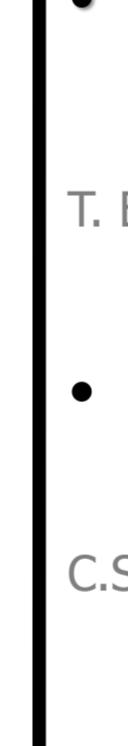
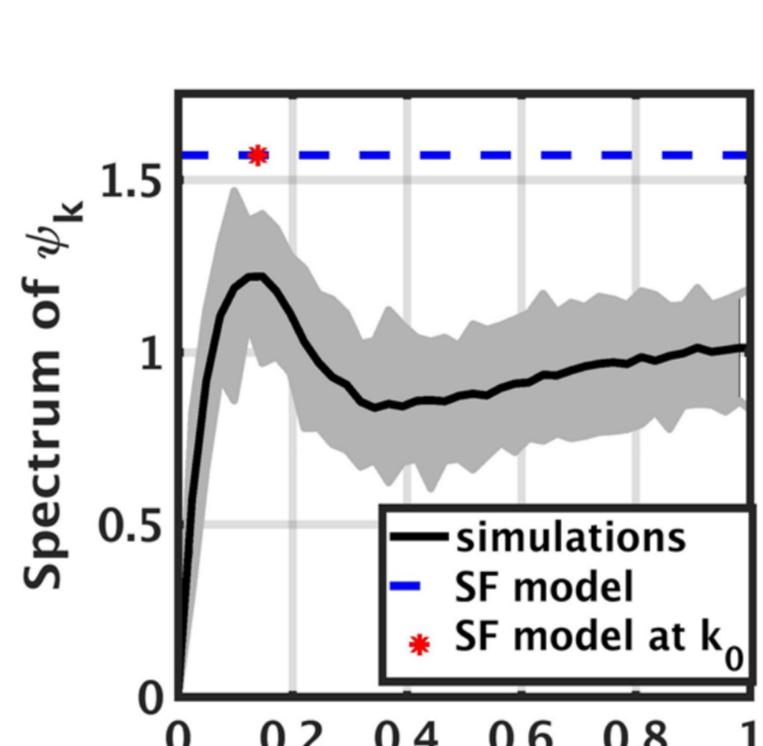
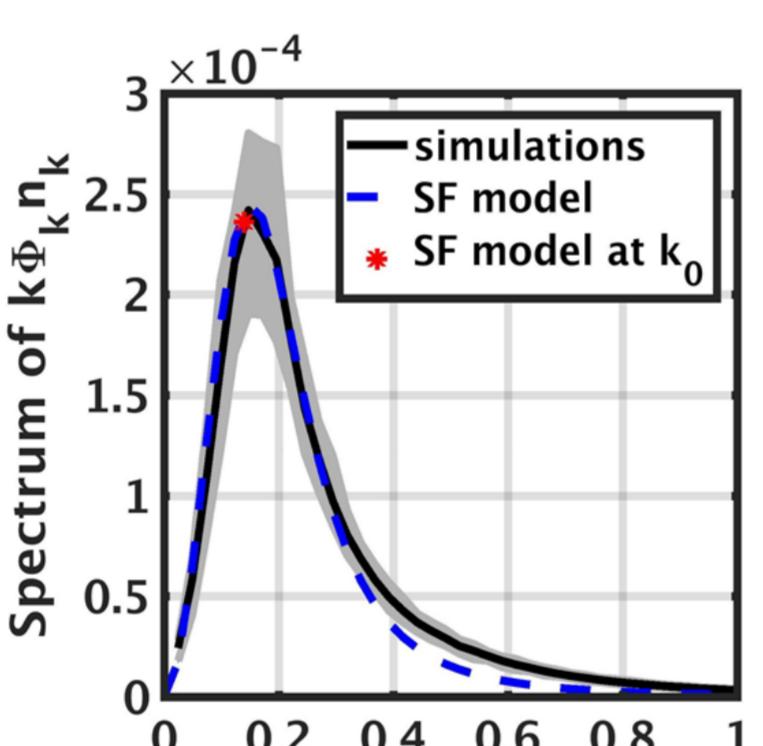
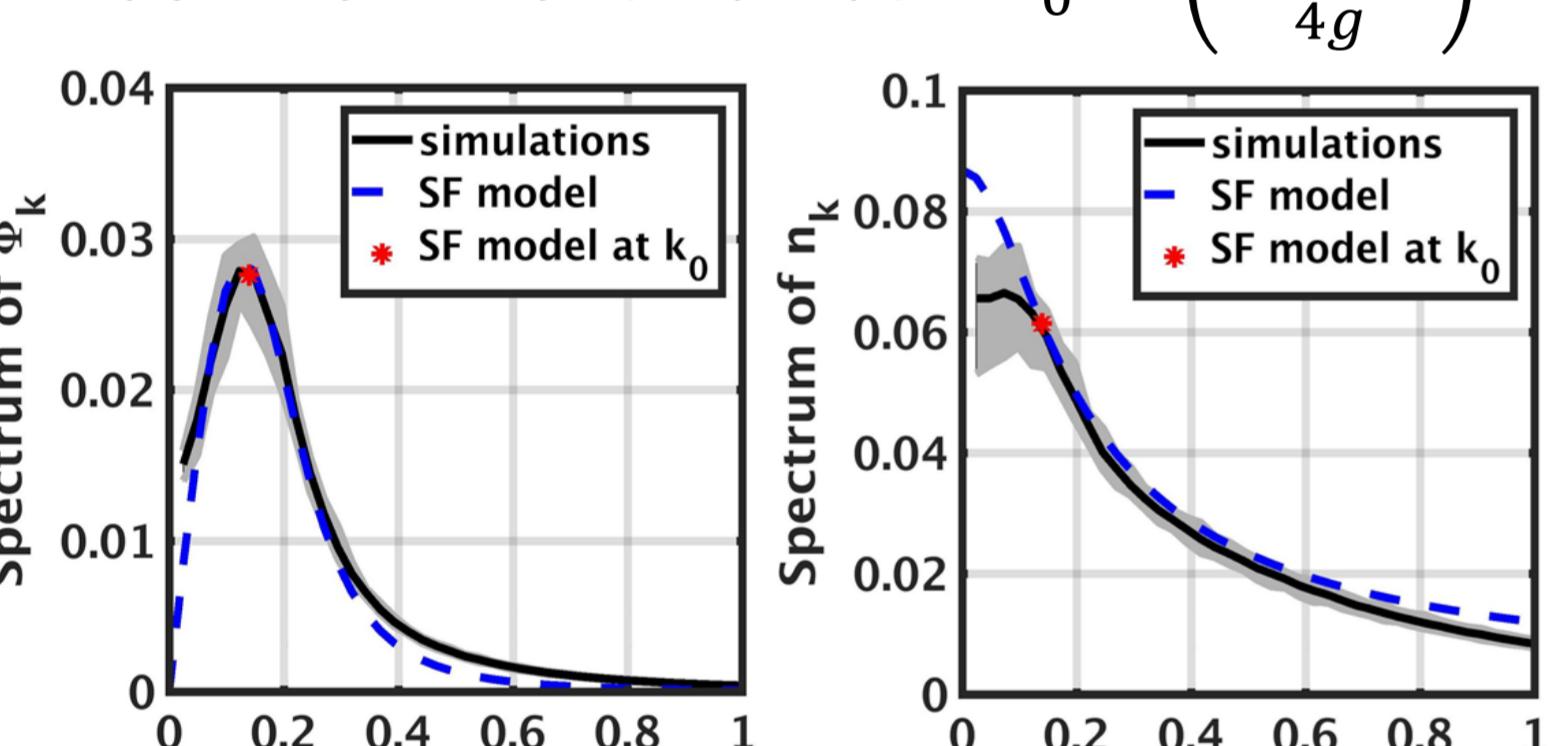
Principle: extend filament model to fluctuation spectra  $v_f(\delta_f) \rightarrow \Phi(k_{\theta})$  &  $n_b \rightarrow n(k_{\theta})$

Hyp: density & potential spectra in phase quadrature + time independent spectra (it is!)

- potential: include effective viscosity from dominant mode  $k^4 \Phi_{k_0} \Phi_k + \sigma_{\parallel} \Phi_k = g k n_k$

$$\text{density : mixing length + ad-hoc saturation at low } k \quad \sqrt{k^2 + k_0^2} n_k = \lambda_n^{-1}$$

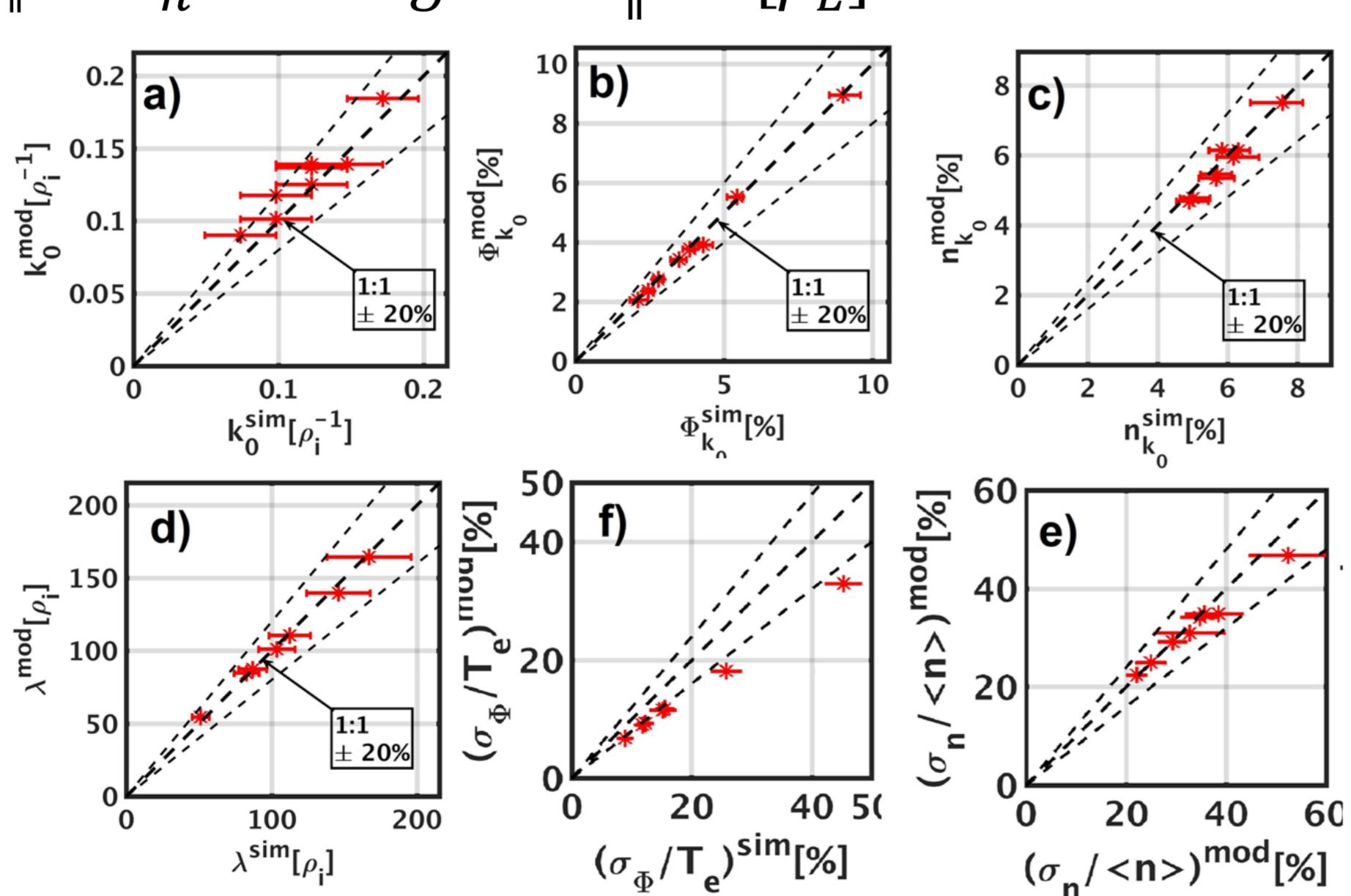
$$\text{dominant wave number } k_0 = \left( \frac{1.45 \lambda \sigma_{\parallel}^2}{4g} \right)^{1/4}$$



## Spectral integrals for macroscopic quantities:

- radial flux:  $\Gamma_r \equiv 8\pi^2 \int k \Phi_k n_k dk = 41 \lambda_n^{-\frac{7}{4}} g^{\frac{3}{4}} \sigma_{\parallel}^{-\frac{1}{2}} [\bar{n} c_s]$
- fluctuation levels  $\frac{\sigma_n}{\bar{n}} = 12.6 \lambda_n^{-\frac{9}{8}} g^{\frac{1}{8}} \sigma_{\parallel}^{-\frac{1}{4}}$  &  $\frac{\sigma_{\Phi}}{T_e} = 4.8 \lambda_n^{-\frac{7}{8}} g^{\frac{7}{8}} \sigma_{\parallel}^{-\frac{3}{4}}$
- scrape-off-layer width:  $\Gamma_r \equiv \lambda_n \sigma_{\parallel} \rightarrow \lambda_n = 3.9 g^{3/11} \sigma_{\parallel}^{-6/11} [\rho_L]$

$\rightarrow$  Quantitative agreement with TOKAM2D simulations (scan of  $g$  &  $\sigma_{\parallel}$ )



## SF model $\rightarrow$ prediction of heat flux width & confinement time

### Heat flux decay length

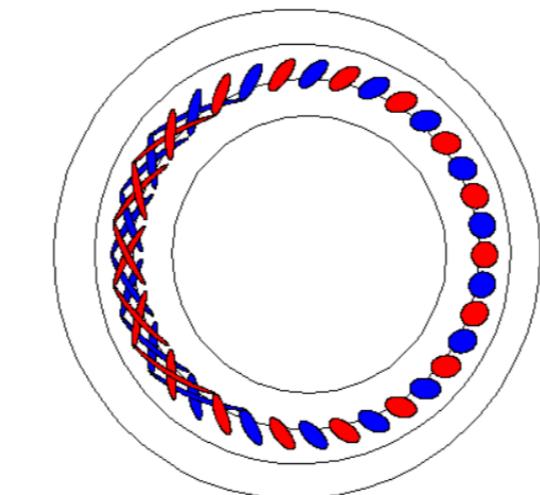
Hyp:  $\lambda_q = \alpha_q \lambda_n$ ,  $g = \rho_L/R$  &  $\sigma_{\parallel} = \frac{\rho_L}{L_{||}} = \rho_L/\pi q_{cyl} R$ , 2-point model for  $T_{sep}$

$$\lambda_q = 50 \alpha_q q_{cyl}^{0.63} B_{[T]}^{-0.65} R_{[m]}^{0.25} \left( \frac{A}{Z} \right)^{0.33} P_{sep}[MW] [mm]$$

### Confinement time:

Hyp: density  $\rightarrow$  pressure & particle flux  $\rightarrow$  heat flux  
vorticity // dissipation still valid (HFS decorrelation of LFS mode)  
gradient scale length  $\lambda \approx a$

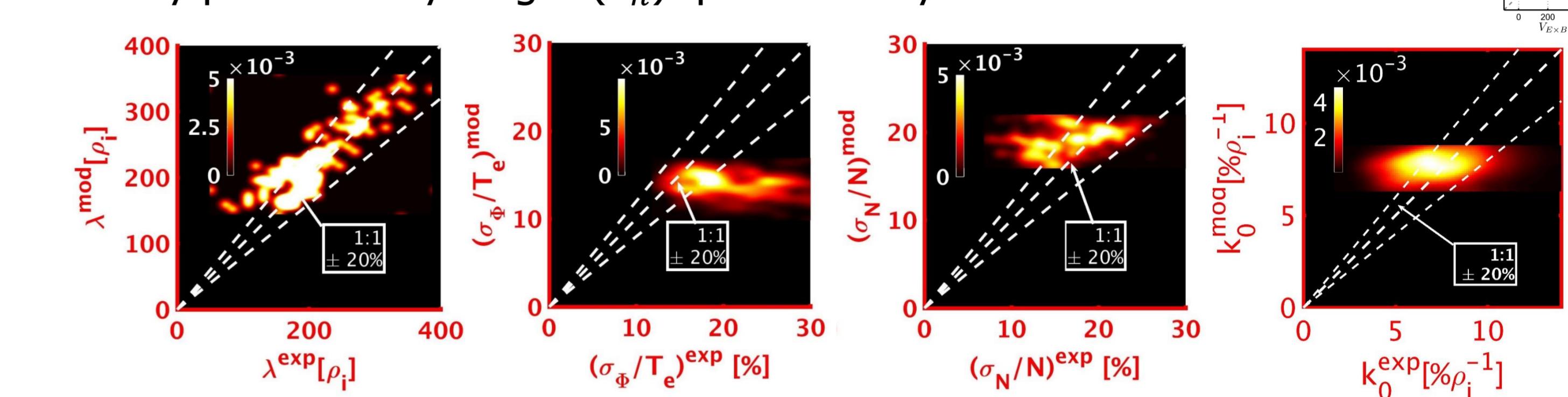
$$\tau_E = 0.007 \alpha_T I_P^{0.2} B_{[T]}^{0.6} P_{TOT[MW]}^{-0.6} n_e^{0.6} M^{0.2} R_{[m]}^{2.8} \left( \frac{a}{R} \right)^{1.9} [s]$$



## Model validated against broad SOL database from Tore Supra

>100 probe reciprocations with turbulence (1MHz  $\theta$ -rake) & profile (tunnel) collectors

- ExB velocities of averaged filaments match with isolated filament model
- fluctuation amplitudes ( $n_e$  &  $\Phi$ ) and main  $k_{\theta}$  well reproduced
- density profile decay length ( $\lambda_n$ ) quantitatively matched



## Recovering multi-machine scaling of ITER startup heat flux width

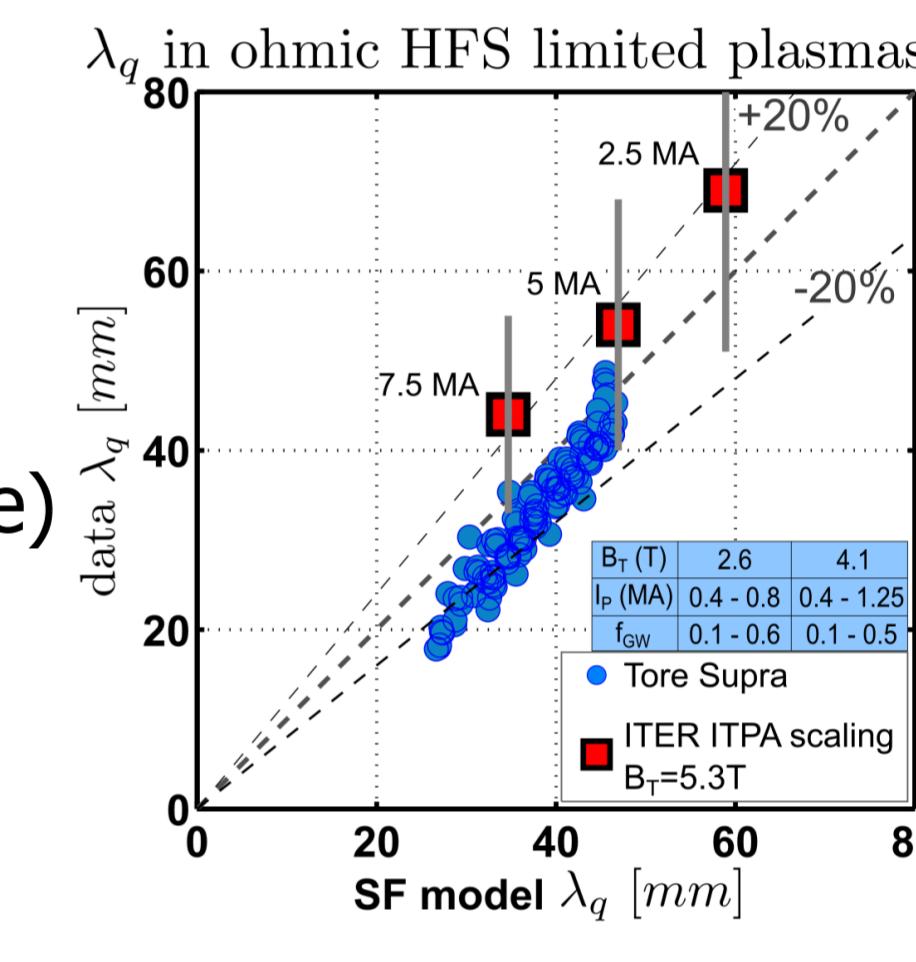
N. Fedorczak et al. Nuc. Mater. & Energy 19 (2019) 433–439

Hyp:  $\lambda_q = 0.5 \lambda_n$  (correlation from Tore Supra database)

$$\lambda_q = 25 q_{cyl}^{0.63} B^{-0.65} R^{0.25} \left( \frac{A}{Z} \right)^{0.33} P_{sep}[MW] [mm]$$

- quantitative agreement with Tore Supra  $\lambda_q$  (ITER database)
- quantitative agreement with multi-machine prediction of ITER startup SOL width

J. Gunn et al. J. Nucl. Mater. 438 (Suppl) (2013) S184–S188,



## Recovering multi-machine scaling sensitivity of $\lambda_q$ in H-mode

Model:  $\lambda_q \propto R^{0.25} \dots$

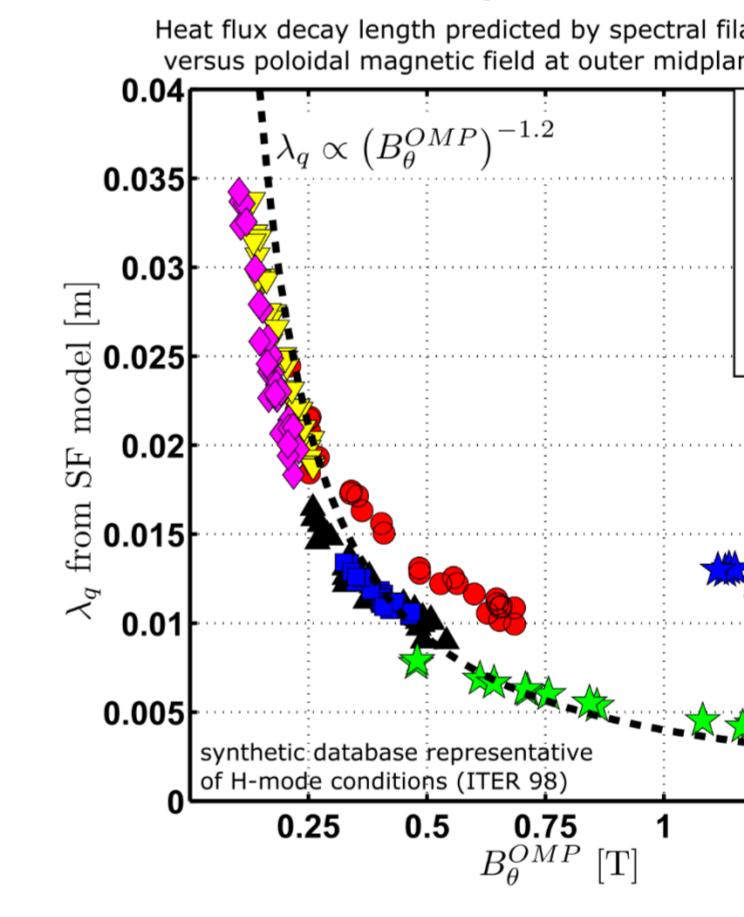
- $\lambda_q \propto R^{0.25}$  for ITER & DEMO compared to  $B_{\theta}$  scaling

T. Eich et al. Nucl. Fusion 53 (9) (2013) 093013

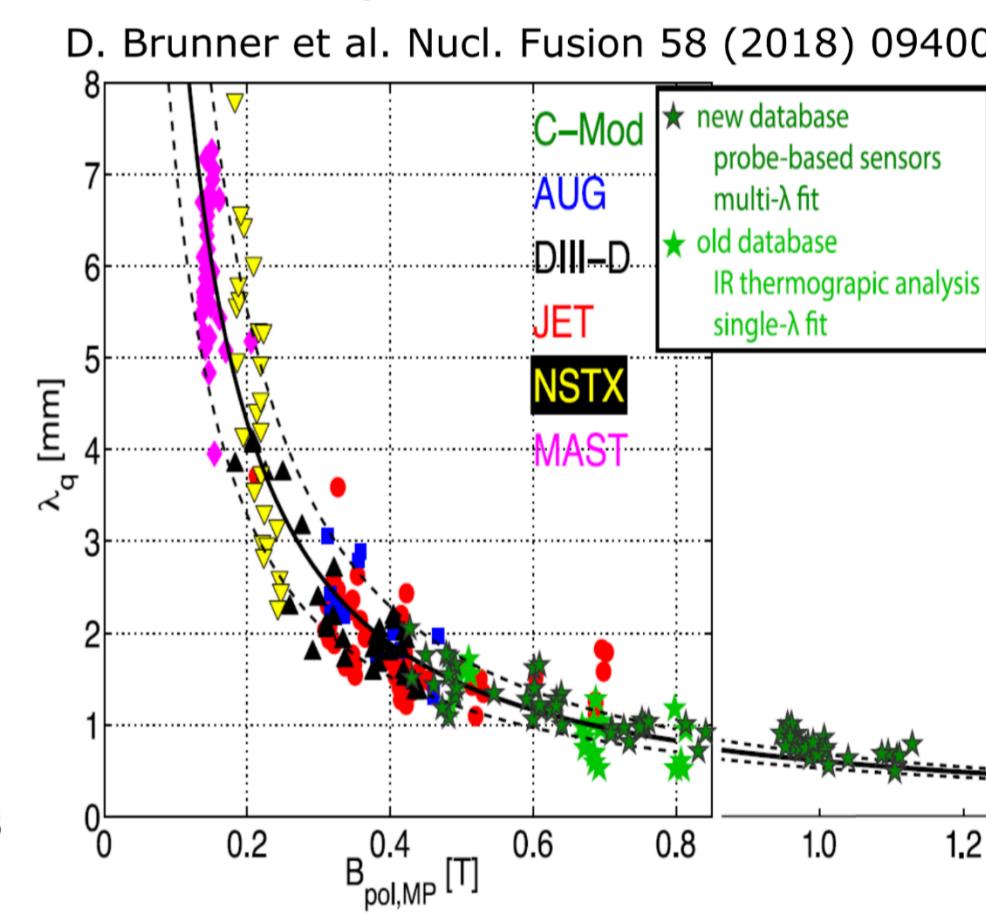
- sounds with XGC1 results (different interpretation)

C.S. Chang et al. 2017 Nucl. Fusion 57 116023

model prediction



experimental data



## Recovering impact of divertor leg length on $\lambda_q$ in TCV L-mode

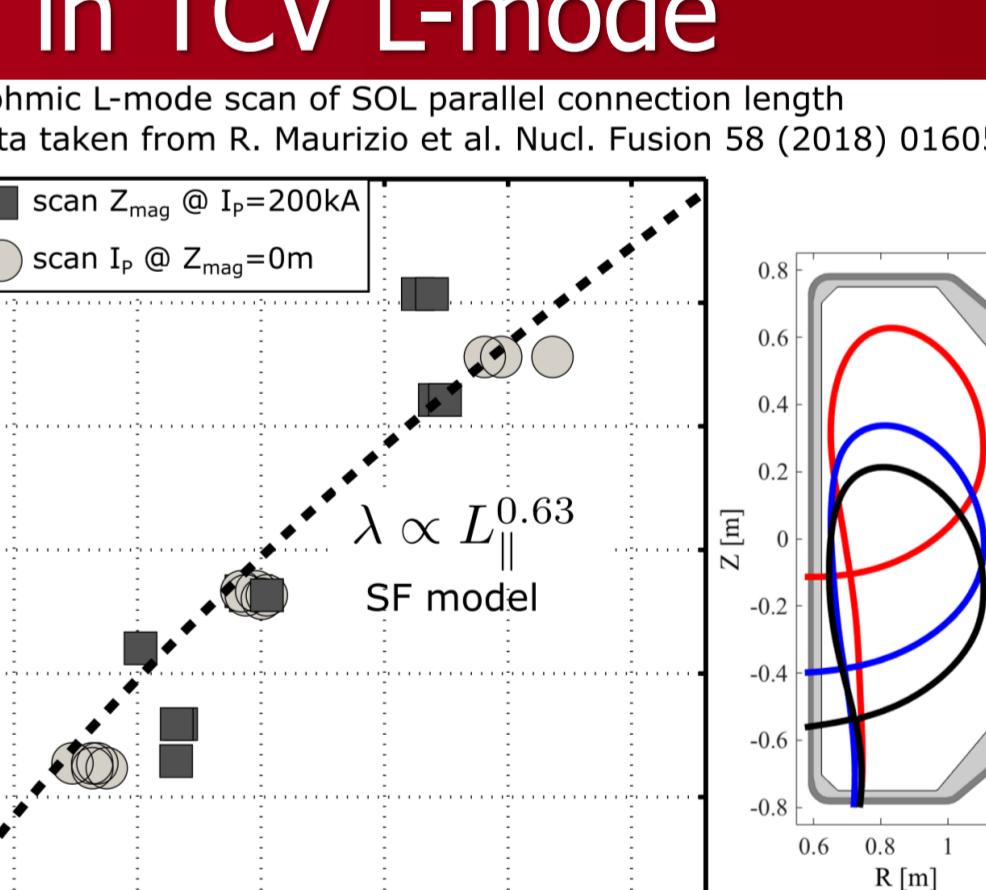
TCV ohmic pulses: scan of plasma current and divertor geometry gives same  $\lambda_q(L_{||})$

R. Maurizio et al. Nucl. Fusion 58 (2018) 016052

Model:  $\lambda_q \propto L_{||}^{0.63}$

- sensitivity recovered by the SF model
- 3D turbulent simulations show interchange along divertor leg, as the model considers

A. Gallo et al. Plasma Phys. Control. Fusion 60 (2018) 014007



## Recovering global multi-machine $\tau_E$ sensitivity & correlation with $\lambda_q$

Model :

$$\tau_E \propto I_P^{0.2} B^{0.6} P_{TOT}^{-0.6} n_e^{0.6} M^{0.2} R^{2.8} \left( \frac{a}{R} \right)^{1.9}$$

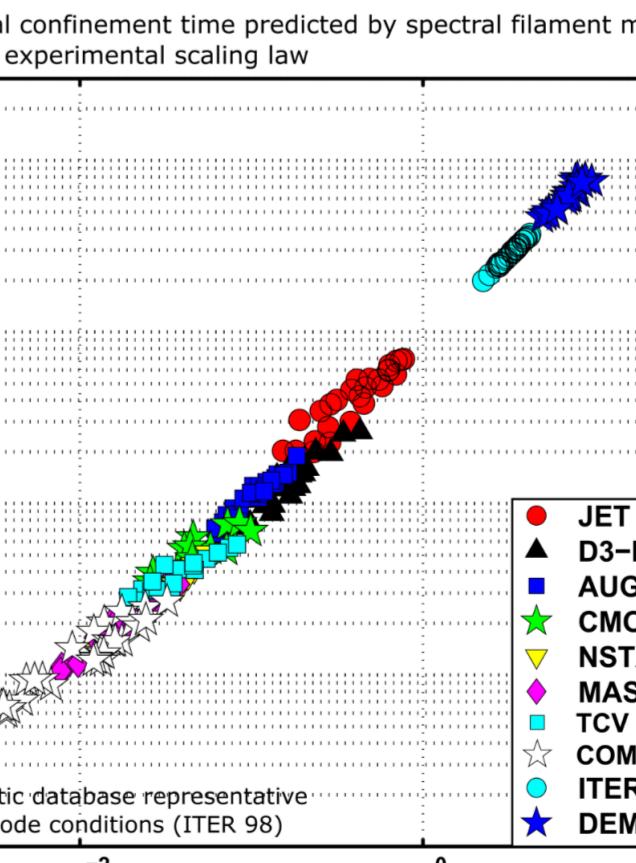
Scaling law ITER 98:

$$\tau_E \propto I_P^{1.0} B^{0.1} P_{TOT}^{-0.6} n_e^{0.4} M^{0.2} R^{1.9} \left( \frac{a}{R} \right)^{0.2}$$

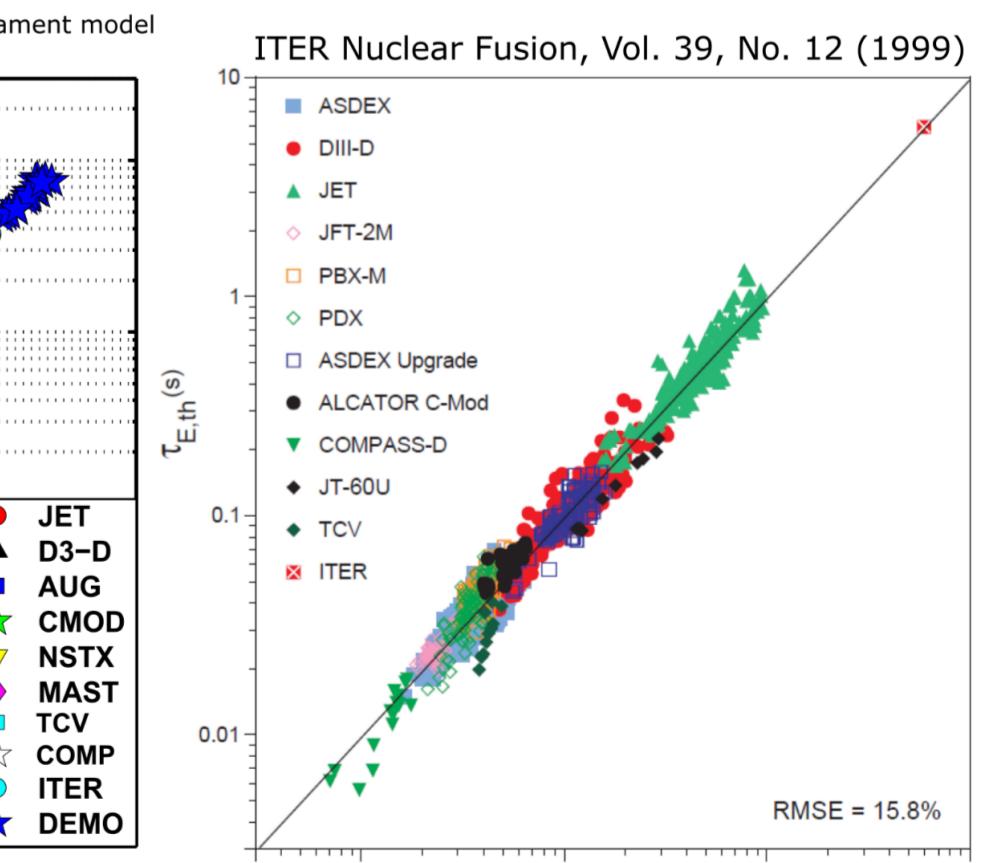
- significant difference in  $I_P$  &  $B$
- **global trend is well matched**

hints of correlations in exp. scaling

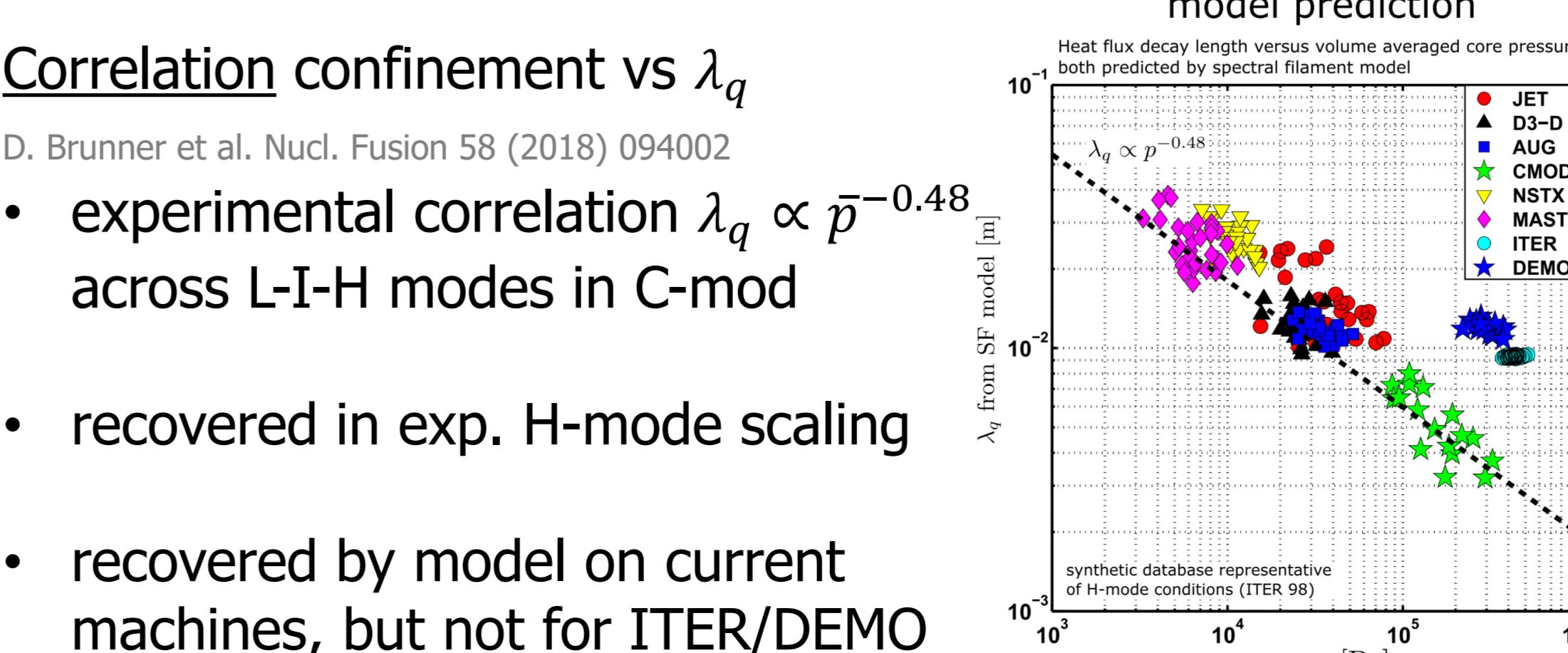
model prediction



experimental data



model prediction



experimental data

