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R-miss-tastic: a unified platform for missing values methods and workflows

Imke Mayer* Aude Sportisse[†] Julie Josse[‡] Nicholas Tierney[§]
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Abstract

Missing values are unavoidable when working with data. Their occurrence is exacerbated as more data from different sources become available. However, most statistical models and visualization methods require complete data, and improper handling of missing data results in information loss or biased analyses. Since the seminal work of Rubin (1976), a burgeoning literature on missing values has arisen, with heterogeneous aims and motivations. This led to the development of various methods, formalizations, and tools. For practitioners, it remains nevertheless challenging to decide which method is most suited for their problem, partially due to a lack of systematic covering of this topic in statistics or data science curricula.

To help address this challenge, we have launched the “R-miss-tastic” platform, which aims to provide an overview of standard missing values problems, methods, and relevant implementations of methodologies. Beyond gathering and organizing a large majority of the material on missing data (bibliography, courses, tutorials, implementations), “R-miss-tastic” covers the development of standardized analysis workflows. Indeed, we have developed several pipelines in R and Python to allow for hands-on illustration of and recommendations on missing values handling in various

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statistical tasks such as matrix completion, estimation and prediction, while ensuring reproducibility of the analyses. Finally, the platform is dedicated to users who analyze incomplete data, researchers who want to compare their methods and search for an up-to-date bibliography, and also teachers who are looking for didactic materials (notebooks, video, slides).

Keywords: missing data; state of the art; bibliography; reproducibility; guided workflows; teaching material; statistical analysis community

1 Context and motivation

Missing data are unavoidable as soon as collecting or acquiring data is involved. They occur for many reasons including: individuals choose not to answer survey questions, measurement devices fail, or data have simply not been recorded. Their presence becomes even more important as data are now obtained at increasing velocity and volume, and from heterogeneous sources not originally designed to be analyzed together. As pointed out by Zhu et al. (2019), “one of the ironies of working with Big Data is that missing data play an ever more significant role, and often present serious difficulties for analysis”. Despite this, the approach most commonly implemented by default in software is to toss out cases with missing values. At best, this is inefficient because it wastes information from the partially observed cases. At worst, it results in biased estimates, particularly when the distributions of the missing values are systematically different from those of the observed values (e.g., Enders, 2010, Chap. 2).

However, handling missing data in a more efficient and relevant way (than limiting the analysis on solely the complete cases) has attracted a lot of attention in the literature in the last two decades. In particular, a number of reference books have been published (Schafer and Graham, 2002; van Buuren, 2012; Carpenter and Kenward, 2012; Little and Rubin, 2019) and the topic is an active field of research (Josse and Reiter, 2018). The diversity of the problems of missing data means there is great variety in the proposed and studied methods. They include model-based approaches, integrating likelihoods or posterior distributions over missing values, filling in missing values in a realistic way with single, or multiple imputations, or weighting of observations, appealing to ideas from the design-based literature in survey sampling. The multiplicity of the available solutions makes sense because there is no single solution or tool to manage missing data: the appropriate methodology to handle them depends on many features, such as the objective of the analysis, type of data, the type of missing data and their pattern. Some of these methods are available in various software solutions. As R (R Core Team, 2020) is one of the main software for statisticians and data scientists and as its development has started almost three decades ago (Ihaka, 1998), R is one of the language that offers the largest number of implemented approaches. This is also due to its ease to incorporate new methods and its modular packaging system. Currently, there are over 270 R packages on CRAN that mention missing data or imputation in their DESCRIPTION files. These packages serve many different applications, data types or types of analysis. More precisely, exploratory and visualization tools for missing data are available in packages like **naniar**, **VIM**, and **MissingDataGUI** (Tierney, Cook, McBain, and Fay, Tierney et al.; Tierney and Cook, 2018; Kowarik and

Templ, 2016; Cheng et al., 2015). Imputation methods are included in packages like **mice**, **Amelia**, and **mi** (van Buuren and Groothuis-Oudshoorn, 2011; Honaker et al., 2011; Gelman and Hill, 2011). Other packages focus on dealing with complex, heterogeneous (categorical, quantitative, ordinal variables) data or with large dimension multi-level data, such as **missMDA**, and **MixedDataImpute** (Josse et al., 2016; Murray and Reiter, 2015). Besides R, other languages such as **Python** (Van Rossum and Drake, 2009), which currently only have few publicly available implementations of methods that handle missing values in statistical tasks, offer more and more solutions. Two prominent examples are: 1) the **scikit-learn** library (Pedregosa et al., 2011) which has recently added a module for missing values imputation; and 2) the **DataWig** library (Biessmann et al., 2018) which provides a framework to learn to impute incomplete data tables.

Despite the large range of options, missing data are often not handled appropriately by practitioners. This may be for a few reasons. First, the plethora of options can be a double-edged sword, the sheer number of options making it challenging to navigate and find the best one. Second, the topic of missing data is often itself missing from many statistics and data science syllabuses, despite its omnipresence in data. So, when faced with missing data, practitioners are left powerless: quite possibly never having been taught about missing data, they do not have an idea of how to approach the problem, what are the dangers of mismanagement, navigate the methods, software, or choose the appropriate method or workflow for their problem.

To help promote better management and understanding of missing data, we have released “R-miss-tastic”, an open platform for missing values. The platform takes the form of a reference website¹, which collects, organizes and produces material on missing data. It has been conceived by an infrastructure steering committee (ISC; its members are authors of this article) working group, which first provided a CRAN Task View² on missing data³ that lists and organizes existing R packages on the topic. The “R-miss-tastic” platform extends and builds on the CRAN Task View by collecting, creating and organizing articles, tutorials, documentation, and workflows for analyses with missing data.

The intent of this platform is easily extendable and well documented, so it can seamlessly incorporate future works and research in missing values. The intent of the platform is to foster a welcoming community, within and beyond the R community. “R-miss-tastic” has been designed to be accessible for a wide audience with different levels of prior knowledge, needs, and questions. This includes, for instance, students looking for course material to

¹<https://rmissstastic.netlify.com/>

²<https://CRAN.R-project.org/package=ctv>

³<https://cran.r-project.org/web/views/MissingData.html>

complement their studies, teachers and professors who can use a reference website for their own classes or refer to students, statisticians or researchers in a different fields using statistics searching for solutions or existing work to help with analysis, researchers wishing to understand or contribute information for specific research questions, or find collaborators.

In this perspective, the platform provides new tutorials, examples and pipelines of analyses that we have developed with missing data that span the entirety of an analysis. The latter have been developed in R and in Python, implementing standard methods for generating missing values and for analyzing them under different perspectives. These pipelines cover the entirety of a data analysis: they contain exploratory analyses of the data, the establishment of statistical models, analysis diagnostics, the application of machine learning methods, and finally an interpretation of the results obtained from incomplete data. We hope that these pipelines also serve as guidance when it comes to choosing a method to handle missing values in a specific context. In addition, we reference publicly available datasets that are commonly used as benchmark for new missing values methodologies.

The remainder of the article is organized as follows: Section 2 describes the different components of the platform, the structure that has been chosen, and the targeted audience. The section is organized as the platform itself, starting by describing materials for less advanced users then materials for researchers and finally resources for practical implementation. Section 3 details the implementation and use-cases of the provided workflows, implemented both in R and in Python. Finally, in Section 4, we conclude with an overview of the planned future developments for the platform and of interesting areas in missing values research that we would like to bring to a broader audience.

2 Structure and content of the platform

The “R-miss-tastic” platform is released at <https://rmissstastic.netlify.com/>. It has been developed using the R package **blogdown** (Xie et al., 2017) which generates static websites using Hugo⁴. Live examples have been included using the tool <https://rdr.io/snippets/> provided by the website “R Package Documentation”. The source code and materials of the platform have been made publicly available on GitHub at <https://github.com/R-miss-tastic>, which provides a transparent record of the platform’s development, and facilitates contributions from the community.

We now discuss the structure of the “R-miss-tastic” platform, the aim and content of each subsection, and highlight key features of the platform.

⁴<https://gohugo.io/>

2.1 Workflows

An important contribution and novelty of this work is the proposal of several workflows that allow for a hands-on illustration of classical analyses with missing values, both on simulated data and on publicly available real-world data. These workflows are provided both in R and in Python code and cover the following topics:

- *How to generate missing values?* Generate missing values under different mechanisms, on complete or incomplete datasets. This is useful when performing simulations to compare methods that impute or handle missing data.
- *How to do statistical inference with missing values?* In particular, we focus on the different solutions (maximum likelihood or multiple imputation) that are available to estimate linear and logistic regression parameters with missing covariate values.
- *How to impute missing values?* We compare different single imputation/matrix completion methods (for instance using conditional models, low-rank models, etc.).
- *How to predict with missing values?* We consider building predictive models (for instance using random forests (Breiman, 2001)) on data with incomplete predictors. The workflows present different strategies to deal with missing values in the covariates both in the training set and in the test set.

The aim of these workflows is threefold: 1) they provide a practical implementation of concepts and methods discussed in the lectures and bibliography sections of the platform (see Sections 2.2 and 2.3 of the present article); 2) they are implemented in a generic way, allowing for simple re-use on other datasets, for integration of other estimation or imputation methods; 3) the distinction between inference, imputation, and prediction lets the user keep in mind that the solutions are not the same in these cases.

Furthermore, the workflows allow for a transparent and open discussion about the proposed implementations, which can be followed on the project GitHub repository, referencing proposals and discussions about practicable extensions of the workflows.

Additionally, a workflow on *How to do causal inference with incomplete covariates/attributes in R?* allows to use simple weighting and doubly robust estimators for treatment effect estimation using R language. This workflow is based on the R implementation of the methodology proposed by Mayer et al. (2020).

We provide a more detailed view on the proposed workflows in Section 3, with examples of tabular or graphical outputs that can be obtained as well as recommendations on how to interpret and leverage these outputs.

2.2 Lectures

For someone unfamiliar with missing data, it is a challenge to know where to begin the journey of understanding them, and the methods to handle them. This challenge is being addressed with “R-miss-tastic”, which makes the material to get started easily accessible.

Teaching and workshop material takes many forms – from slides, course notes, lab workshops, video tutorials and in-depth seminars. The material is of high quality, and has been generously contributed by numerous renowned researchers who investigate the problems of missing values, many of whom are professors having designed introductory and advanced classes for statistical analyses with missing data. This makes the material on the “R-miss-tastic” platform well suited for both beginners and more experienced users.

These teaching and workshop materials are described as “lectures”, and are organized into five sections:

1. General lectures: introduction to statistical analyses with missing values; the role of visualization and exploratory data analysis for understanding missingness and guiding its handling; theory and concepts are covered, such as missing values mechanism, likelihood methods, and imputation.
2. Multiple imputation: introduction to popular methods of multiple imputation (joint modeling and fully conditional), how to correctly perform multiple imputation and limits of imputation methods.
3. Principal component methods: introduction to methods exploiting low-rank type structures in the data for visualization, imputation and estimation.
4. Specific data or applications types: lectures covering in details various sub-problems such as missing values in *time series*, in *surveys*, or in treatment effect estimation (*causal inference*). Indeed, certain data types require adaptations of standard missing values methods (for instance handling the time dependence in time series (Moritz and Bartz-Beielstein, 2017)) or additional assumptions about the impact of missing values (such as the impact on confounded treatment effects in the causal inference context (Mayer et al., 2020)). But also more in-depth material, for instance video recordings from a virtual workshop on *Missing Data Challenges in Computation, Statistics and Applications*⁵ held in 2020.

⁵<https://www.ias.edu/math/mdccsa>

5. Implementations: a non-exhaustive list of detailed vignettes describing functionalities of R packages and of Python modules that implement some of the statistical analysis methods covered in the other lectures. For instance, the functionalities and possible applications of the **missMDA** R package are presented in a brief summary, allowing the reader to compare the main differences between this package and the **mice** package which is also summarized using the same summary format.

Figure 1 illustrates two views of the lectures page: Figure 1A shows a collapsed view presenting the different topics, Figure 1B shows an example of the expanded view of one topic (General tutorials), with a detailed description of one of the lecture (obtained by clicking on its title), “Analysis of missing values” by Jae-Kwang Kim. Each lecture can contain several documents (as is the case for this one) and is briefly described by a header presenting its purpose.

Lectures that we found very complete and thus highly recommend are:

- *Statistical Methods for Analysis with Missing Data* by Mauricio Sadinle (in “General tutorials”);
- *Missing Values in Clinical Research – Multiple Imputation* by Nicole Erler (in “Multiple imputation”);
- *Handling missing values in PCA and MCA* by François Husson. (in “Missing values and principal component methods”);
- *Modern use of Shared Parameter Models for Dropout (in longitudinal and time-to-event data)* by Dimitris Rizopoulos (in “Specific data or application types”).

The purpose of these lectures is to provide either an introduction or a deeper understanding of the statistical problems and proposed solutions in terms of their (mathematical) derivation and theoretical scope. The focus is thus less on a practical illustration on real data or a systematic comparison of all methods for a same statistical problem. This aspect is covered by the workflows as will be explained in more detail in Section 3.

2.3 Bibliography

Complementary to the *Lectures* section, this part of the platform serves as a broad overview on the scientific literature discussing missing values taxonomies and mechanisms and statistical, machine learning methods to handle them. This overview covers both classical

R-miss-tastic

A resource website on missing values - Methods and references for managing missing data

Below you will find a selection of high-quality lectures, tutorials and labs on different aspects of missing values.

If you wish to contribute some of your own material to this platform, please feel free to contact us via the [Contact form](#).

[General lectures](#)

[Multiple imputation](#)

[Missing values and principal component methods](#)

[Specific data or application types](#)

[Implementation in R](#)

Collapse All

+

+

+

+

+

Collapse All

[General tutorials](#)

+

Statistical Methods for Analysis With Missing Data
(Mark Deisen, course at NC State University, spring 2017)

Handling missing values

(Julie Jans, course at Ecole Polytechnique, fall 2018 and Julie Jans & Nick Tierney, tutorial at useR! 2018, 2016)

Analysis of missing values

(Jae-Kwang Kim, course at Iowa State University, fall 2015)

This course focuses on the theory and methods for missing data analysis. Topics include maximum likelihood estimation under missing data, EM algorithm, Monte Carlo computation techniques, imputation, Bayesian approach, propensity scores, semi-parametric approach, and non-ignorable missing data.

- [Introduction](#)
- [Unimproved-based approach](#)
- [Computation](#)
- [Introduction](#)
- [Multiple imputation](#)
- [Propensity Score approach](#)
- [Nonignorable missing data](#)

Statistical Methods for Analysis with Missing Data
(Mauricio Sudrià, course at University of Washington, winter 2016)

[Multiple imputation](#)

+

[Missing values and principal component methods](#)

+

[Specific data or application types](#)

+

[Implementation in R](#)

+

(a) Collapsed view

(b) Extract

Figure 1: Lecture overview.

references with books, articles, etc. such as Schafer and Graham (2002); van Buuren (2012); Carpenter and Kenward (2012); Little and Rubin (2019) and more recent developments such as Josse et al. (2019); Gondara and Wang (2018), which study the consistency of supervised learning with missing values. The entire (non-exhaustive) bibliography can be browsed in two ways: 1) a complete list, filtered by publication type and year, with a search option for the authors or, 2) as a contextualized version. For 2), we classified the references into several domains of research or application, briefly discussing important aspects of each domain. This dual representation is shown in Figure 2 and allows for an extensive search in the existing literature, while providing some guidance for those focused on a specific topic. All references are also collected in a unique BibTeX file made available in the GitHub repository⁶. This shared file allows external users to easily propose additions to the bibliography, which are then reviewed by the platform editorial and maintenance committee, composed of researchers with different focuses on the handling of missing values.

⁶in `resources/rmisstastic_biblio.bib`

R-miss-tastic

A resource website on missing values - Methods and references for managing missing data

On this platform we attempt to give you an overview of main references on missing values. We do not claim to gather all available references on the subject but rather to offer a peak into different fields of active research on handling missing values, allowing for an introductory reading as well as a starting point for further bibliographical research.

[See here for a full \(and uncommented\) list of references.](#)

Inspired by [CRAN Task View on Missing Data](#) and a [review](#) of Imbert & Villa-Vialaneix on handling missing values (2018, written in French) we organized our selection of relevant references on missing values by different topics.

[Short introduction to missing values](#)

[General references and reviews](#)

[Weighting methods](#)

[Hot-deck and kNN approaches](#)

[Likelihood-based approaches](#)

[Single imputation](#)

[Multiple imputation](#)

[Machine Learning](#)

[Missing values mechanisms](#)

(a) Contextualized version

R-miss-tastic

A resource website on missing values - Methods and references for managing missing data

[A commented version of this bibliography can be found here.](#)

| Publication type | Year | Author | | |
|------------------|------|---|------|----------------|
| All | All | Search by author name... | | |
| Citation | | | | |
| | | | Year | Publisher type |
| | | | 2008 | Article |
| | | Abayomi, K., A. Gelman, and M. Levy. <i>Diagnostics for multivariate imputations</i> . In: <i>Journal of the Royal Statistical Society, Series C (Applied Statistics)</i> 57.3 (2008), pp. 273-291. | | |
| | | | 2000 | Article |
| | | Albert, P. S. and D. A. Follmann. <i>Modeling repeated count data subject to informative dropout</i> . In: <i>Biometrics</i> 56.3 (2000), pp. 667-677. | | |
| | | | 2001 | Book |
| | | Allison, P. D. <i>Missing Data. Quantitative Applications in the Social Sciences</i> . Thousand Oaks, CA, USA: Sage Publications, 2001. ISBN: 9780761916727. | | |
| | | | 2010 | Article |
| | | Andridge, R. and R. J. A. Little. <i>A review of hot deck imputation for survey non-response</i> . In: <i>International Statistical Review</i> 78.1 (2010), pp. 40-64. | | |
| | | | 2016 | Article |
| | | Audigier, V., F. Husson, and J. Josse. <i>A principal component method to impute missing values for mixed data</i> . In: <i>Advances in Data Analysis and Classification</i> 10.1 (2016), pp. 5-26. | | |
| | | | 2016 | Article |
| | | Audigier, V., F. Husson, and J. Josse. <i>MIMCA: multiple imputation for categorical variables with multiple correspondence analysis</i> . In: <i>Statistics and Computing</i> 27.2 (2016), pp. 1-18. eprint: 1505.08116. | | |

(b) Unordered version

Figure 2: Bibliography overview.

2.4 Implementations

R packages As mentioned in the introduction, the platform development is based on the release of the *MissingData* CRAN Task View, which currently lists approximately 150 R packages. The CRAN Task View is continuously updated, adding new R packages, and removing obsolete ones. Packages are organized by topic: *exploration of missing data, likelihood based approaches, single imputation, multiple imputation, weighting methods, specific types of data, specific application fields*. We selected only those that were sufficiently mature and stable, and that were already published on CRAN or Bioconductor. This choice was made to ensure that all listed packages can easily be installed and used by practitioners.

Even though the Task View classifies packages into different sub-domains, it may still be a challenge for practitioners and researchers inexperienced with missing values to choose the most relevant package for their application. To address this challenge, we provide a partial and slightly more detailed overview of existing R packages, selecting the most popular and versatile ones. This overview is a blend of the Task View, and of the individual package description pages and vignettes as provided on CRAN or Bioconductor. For each selected package (7 at the date of writing of this article: **imputeTS**, **mice**, **missForest**, **missMDA**, **naniar**, **simputation** and **VIM**), we provided a category (in the style of the categorization in the Task View), a short description of use-cases, its description (as on CRAN), the usual CRAN statistics (number of monthly downloads, last update), the handled data formats (e.g., `data.frame`, `matrix`, `vector`), a list of implemented algorithms (e.g., k-means, PCA, decision tree), the list of available datasets, some references (such as articles and books), and a small chunk of code, ready for a direct execution on the platform via the *R package Documentation*⁷. Figure 3 shows the condensed view of the package page and the expanded description sheet of a given package (here **naniar**).

We believe shortlisting R packages is highly useful for practitioners new to the field, as it demonstrates data analysis that handles missing values in the data. We are aware that this selection is subjective, and we welcome external suggestions for other packages to add to this shortlist.

Python modules To the best of our knowledge, very few methods are already implemented for handling missing data in Python. However, one of the major libraries for machine learning and data analysis, **scikit-learn** (Pedregosa et al., 2011) has recently proposed a module for simple and multiple imputations, **sklearn.impute**. Also, as an alternative, the

⁷<https://rdr.io/snippets/>

R-miss-tastic

A resource website on missing values - Methods and references for managing missing data

R Packages

This page provides introductions to popular missing data packages with small examples on how to use them. Thus the page gives more extensive information than the [CRAN Task View on Missing Data](#), which is recommended to get a first overall overview about the CRAN missing data landscape.

You can also contribute on your own to this page and provide a short introduction to a missing data package. Take a look at [this short description](#) on how to do this. We are very happy about all contributions.

Search Sort by name Sort by Category

• missMDA

Category: Single and multiple Imputation, Multivariate Data Analysis
Imputation of incomplete continuous or categorical datasets; Missing values are imputed with a principal component analysis (PCA), a multiple correspondence analysis (MCA) model or a multiple factor analysis (MFA) model; Perform multiple imputation with and in PCA or MCA.

downloads 4000/month CRAN 2019-01-23
[more..](#)

• imputeTS

Category: Time-Series Imputation, Visualisations for Missing Data
Imputation (replacement) of missing values in univariate time series. Offers several imputation functions and missing data plots. Available imputation algorithms include: 'Mean', 'LOCF', 'Interpolation', 'Moving Average', 'Seasonal Decomposition', 'Kalman Smoothing on Structural Time Series models', 'Kalman Smoothing on ARIMA models'.

downloads 12K/month CRAN 2019-07-01
[more..](#)

• mice

Category: Multiple Imputation
Multiple imputation using Fully Conditional Specification (FCS) implemented by the MICE algorithm as described in Van Buuren and Groothuis-Oudshoorn (2011). Each variable has its own imputation model. Built-in imputation models are provided for continuous data (predictive mean matching, normal), binary data (logistic regression), unordered categorical data (polynomial logistic regression) and ordered categorical data (proportional odds). MICE can also impute continuous two-level data (normal model, pan, second-level variables). Passive imputation can be used to maintain consistency between variables. Various diagnostic plots are available to inspect the quality of the imputations.

downloads 41K/month CRAN 2019-07-10
[more..](#)

Package:

naniar

Category:

Data Structures, Summaries, and Visualisations for Missing Data

Use-Cases:

Visualization of missing values, descriptive statistics, ...

Popularity:

downloads 5305/month

Description:

Missing values are ubiquitous in data and need to be carefully explored and handled in the initial stages of analysis. In this vignette we describe the tools in the package naniar for exploring missing data structures with minimal deviation from the common workflows of ggplot and tidy data.

Last update:

CRAN 2019-02-15

Datasets:

- oceanbuoys
- pedestrian
- riskfactors

Further Information:

- Tierney, N. J., & Cook, D. H. (2018). Expanding tidy data principles to facilitate missing data exploration, visualization and assessment of imputations. arXiv preprint arXiv:1809.02264. [PDF \(on arXiv\)](#)
- [Vignettes](#)
- Related [visdat](#) R-package

Input:

data.frame, vector

Example:

```
library(naniar)
data(airquality)

print("print data set with NAs")
print(head(airquality))

## Replace "NA" values with values 10% lower
## than the minimum value in that variable.
## This is done by calling the geom_miss_point() function
ggplot2::ggplot(airquality,
  ggplot2::aes(x = Solar.R,
    y = Ozone)) +
  geom_miss_point()
```

Here you can have an interactive look at the example:

```
library(naniar)
data(airquality)

print("print data set with NAs")
print(head(airquality))

## Replace "NA" values with values 10% lower
## than the minimum value in that variable.
## This is done by calling the geom_miss_point() function
geom_miss_point(airquality)
```

Run (Ctrl-Enter)

(a) Extract of global view

(b) Description sheet

Figure 3: R packages overview.

statsmodels⁸ library also has an implementation module for multiple imputation in Python now. Additionally, the **missingno** toolset (Bilogur, 2018) allows to visualize missing values for exploratory data analyses. We regularly survey new Python implementations for handling missing values and, if pertinent from a theoretical and practical point of view, reference them on our platform. We expect this to promote their use but also additional assessment by practitioners and researchers from the missing values (statistics/machine learning) community.

2.5 Datasets

Especially in methodology research, an important aspect is the comparison of different methods to assess their respective strengths and weaknesses. Several datasets are recurrent in the missing values literature but have not been referenced together yet. We gathered publicly available datasets that have recurrently been used for comparison or illustration purposes in publications, R packages and tutorials. Most of these datasets are already included in R packages but some are available in other data collections. Figure 4 shows how the datasets are presented, with a detailed description shown for one of the dataset (“Ozone”, obtained by clicking on its name). The description follows the UCI Machine Learning Repository presentation (Dua and Graff, 2019), including a short description of the dataset, how to obtain it, external references describing the dataset in more details, and links to tutorials/lectures on our websites or to vignettes in R packages that use the dataset.

In addition, the *Datasets* section also references existing methods for generating missing data, given assumptions on their generation mechanisms (as in the R package **mice**).

Note, however, that the list of datasets gathered here is short compared to benchmark datasets for full data methods such as the UCI Machine Learning Repository. Therefore, our proposed list also serves as an invitation to tackle this lack of a wider variety of common benchmark datasets in the missing data community.

2.6 Additional content

This unified platform collects and edits the contributions of numerous individuals who have investigated missing values problems, and developed methods to handle them. To provide an overview of some of the main actors in this field, the list of all contributors who agreed

⁸<https://www.statsmodels.org/stable/about.html>

Incomplete data

The data sets listed below are either widely used in general in the missing data community or used for illustration of different methods handling missing values in the tutorials from the [Tutorials](#) and [R packages](#) sections. This presentation scheme is inspired by the [UCI Machine Learning Repository](#).

Click on a table entry to obtain further information about the data set.

| Name | Data Types | Attribute Types | # Instances | # Attributes | % Missing entries | Complete data available | Year |
|--|---------------------------|----------------------------|-------------|--------------|-------------------|-------------------------|------|
| Airquality | Multivariate, Time Series | Real | 154 | 6 | 7 | No | 1973 |
| chorizonDL | Multivariate | Integer, Real | 606 | 110 | 15 | Yes | 1998 |
| Health Nutrition And Population Statistics | Multivariate, Time Series | Integer, Real | 15,022 | 397 | 54 | No | 2017 |
| NHANES | Multivariate | Categorical, Integer, Real | 10,000 | 75 | 37 | No | 2012 |
| oceanbuoys | Multivariate, Time Series | Real | 736 | 8 | 3 | No | 1997 |
| Ozone | Multivariate | Categorical, Integer, Real | 366 | 13 | 6 | No | 1976 |
| <p>Los Angeles Ozone Pollution Data, 1976. This data set contains daily measurements of ozone concentration and meteorological quantities. It can be found in R in the mlbench package and is loaded by calling <code>data(Ozone)</code>.</p> <p>More information on the dataset.</p> <p>Tutorials illustrating methods on this data:</p> <ul style="list-style-type: none"> • Julie Josse's course on missing values imputation using PC methods. • Julie Josse's and Nick Tierney's tutorial on handling missing values. Download the data set from this tutorial: ozoneNA.csv • Nick Tierney's nan1ar vignette for missing data visualization. | | | | | | | |
| pedestrian | Multivariate, Time series | Categorical, Integer | 37,700 | 9 | 2 | No | 2016 |

Figure 4: Datasets overview.

to appear on this platform is given with links to their personal or to their research lab website.

We also provide links to other interesting websites or working groups, not necessarily working with R and Python (Van Rossum and Drake, 2009) but with other programming languages such as SAS/STAT[®] and STATA (StataCorp., 2019).

Two other features are finally provided to engage the community:

1. a regularly updated list of events such as conferences or summer schools with special focus on missing values problems, and
2. a list of recurring questions together with short answers and links for more details for every question (FAQ).

3 Workflows

After this general introduction to the “R-miss-tastic” project and platform and the overview of its structure, we now turn to a more detailed presentation of the various workflows that we have developed and proposed on this platform.

To allow for both hands-on tutorials illustrating current practices and state-of-the-art and ready-to-use pipelines, we propose the workflows under different formats such as HTML, PDF, R Markdown (for R code) and IPython Notebook (for Python code). . We encourage practitioners and researchers to use and adapt these workflows and propose modifications and improvements, in order to increase reproducibility and comparability of their work. Of course, we are aware that these workflows do not cover the entire spectrum of existing methods and data problems. The goal of the proposed workflows is rather to initiate a joint effort to create a larger spectrum of open-source workflows, and to encourage the use of standardized procedures to handle missing values.

With an incomplete dataset at hand, prior to embarking on an in-depth statistical analysis, two preliminary steps are essential: (i) a descriptive analysis leveraging visualization packages such as **VIM** (Kowarik and Templ, 2016) or **naniar** (Tierney, Cook, McBain, and Fay, Tierney et al.); (ii) a specific aim has to be defined in order to choose a specific method to use. An example of a method whose success crucially depends on the analyst’s goal is *mean imputation*: this approach is strongly counter-indicated if the aim is to estimate parameters, but it can be consistent if the aim is to predict as well as possible (Josse et al., 2019). Following this observation, our workflows are divided into different parts, defined by the objective of the statistical analysis. We aim to present and compare the main

implementations available both in R and Python for each objective. Currently there are seven workflows available on the platform and we briefly present their scope and use below. For details on the implementations we encourage the reader to open the corresponding workflows, all available on the “R-miss-tastic” platform.

3.1 How to generate missing values?

The goal of these workflows is to propose functions to generate missing values under different mechanisms. This code aims to unify classical solutions to do this. Indeed, a usual strategy to compare imputation or estimation strategies is to introduce (additional) missing values in the dataset, and use the ground truth for these missing values to evaluate the strategies (see Section 3.2).

Rubin (1976) classifies the cause for a lack of data into three missing data mechanisms. The missing data mechanism is said to be: (i) missing completely at random (MCAR) if the lack of data is totally independent of the data values, (ii) missing at random (MAR) if the process that causes the missing data only depends on the observed values and (iii) missing not at random (MNAR) if the unavailability of the data depends on the missing variables. The major (see Sportisse (2021) for a recent overview on the topic).

In R In the R workflow⁹, we have implemented the main function `produce_NA`¹⁰ which allows to generate missing values under the three missing data mechanisms outlined above. This function internally calls the `ampute` function of the `mice` package (van Buuren and Groothuis-Oudshoorn, 2011) but we chose to simplify its use while adding some additional options to specify the missing values generation. In addition, the original `ampute` function generates missing values only for a complete dataset with quantitative variables¹¹. In the main function of our workflow, the user can easily introduce (additional) missing values in a complete or incomplete dataset composed of quantitative, categorical or mixed variables, by choosing the mechanism and the percentage of missing values to be introduced. The function then returns the data matrix containing the new dataset with missing values, that also includes the missing values already present in the input data, and the indicator matrix

⁹<https://rmissstastic.netlify.app/how-to/generate/misssimul>

¹⁰<https://rmissstastic.netlify.app/how-to/generate/amputation.R>

¹¹If qualitative variables have previously been transformed by one-hot-encoding, they can also be handled by the `ampute` function of `mice`. The `produce_NA` function internally handles the transformation of qualitative variables prior to amputation.

(a binary matrix where an entry is equal to 1 if a new missing value has been generated at the same location in the data matrix and 0 otherwise).

For instance, if X contains three variables (fully observed) denoted as X_1 , X_2 , X_3 , two options are available to generate MAR values:

1. The first option consists in generating missing values in X_1 by using a logistic model depending on (X_2, X_3) , which are fully observed, i.e.,

$$\mathbb{P}(R_1 = 0|X; \phi) = 1/(1 + \exp(-(\phi_2 X_2 + \phi_3 X_3))), \quad (1)$$

where $\phi = (\phi_2, \phi_3)$ is the parameter of the missing data mechanism. In our function, ϕ is chosen such that the given percentage of missing values is achieved. This allows to obtain missing values in the first variable X_1^{NA} . Then, the same strategy is performed to introduce missing values in X_2 and X_3 , by using a logistic model depending on (X_1, X_3) (fully observed) and (X_1, X_2) (fully observed) respectively. To get the final matrix containing missing values, we concatenate X_1^{NA} , X_2^{NA} and X_3^{NA} by handling the rows containing only missing values.

2. The second option consists in generating the missing values *by pattern*, i.e., by rows. In this case, the combinations of which variables are observed and missing are specified in a pattern matrix. For the MAR mechanism, in each pattern, at least one variable must be observed. An example (the choice by default) of such a pattern matrix is

$$\begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix},$$

where 0 indicates that the variable should have missing values whereas 1 means that it should be observed. For example, the first pattern means that the process which causes the missingness of the first variable X_1 depends on the values of X_2 and X_3 that are observed.

We also propose several ways to generate missing values, under the MNAR mechanism. It includes the most general one when the missingness depends on both the missing variables and the observed variables, but also the self-masked mechanism, where the unavailability of the data only depends on their values themselves. For example, it is possible to introduce self-masked missing values using a quantile censorship for which the form is precised by the argument `self.mask`, e.g., if set to "lower", then the values are amputated based on a quantile from the lower tail of the empirical distribution such that the target proportion of missing values is achieved.

In Python To our knowledge, there is no specific module in **Python** to generate missing values. Consequently, we implemented such functions, in a **Python** workflow, which similarly to its **R** counterpart workflow¹²¹³ allows to generate missing values under by different mechanisms and different percentage of missing values. The key difference with the **R** workflow is that the data set must be complete and can currently only contain quantitative variables. Besides, for MAR and MNAR mechanisms, only the option *not by pattern* has been implemented. In this case, for a dataset X with three variables, a variable is chosen to be fully observed (say X_3), and the process which causes the missingness of two other variables (X_1 and X_2) depends on the values of the fully observed variable, for example with the logistic model given in (1).

3.2 How to impute missing values?

The aim of these workflows (in **R** and **Python**) is to compare the most classical imputation methods and to propose a reference pipeline for comparison on simulated and real datasets, which can be easily extended with other imputation methods. Here, the imputation methods are considered as such, i.e., the objective is not to estimate a parameter or to perform a statistical analysis on a completed dataset but to impute missing values to get a complete dataset in the best possible way. Therefore, we evaluate the methods in terms of imputation quality, by using the mean squared error (MSE). More precisely, the procedure is the following one: (i) we have access to a complete dataset X , (ii) missing values are introduced in X and we get an incomplete dataset X^{NA} , (iii) this incomplete dataset is imputed and we obtain an imputed dataset X^{imp} , (iv) the MSE, which measures the error committed by the imputation of the missing values, is computed: it is the ℓ_2 -norm of the difference of the imputed dataset and the complete one). Note that this procedure can also be performed on an incomplete dataset by introducing additional missing values. However, for now, both **R** and **Python** workflows only consider complete datasets.

Different types of imputation methods are included in this workflow:

1. imputation by the mean, which serves as a naive baseline.
2. conditional models, if the imputation relies on the conditional expectation or a draw from the conditional distribution of each variable given the others.

¹²https://rmissstastic.netlify.app/how-to/python/generate_html/how%20to%20generate%20missing%20values

¹³The code has been partially developed in collaboration with Boris Muzellec (post-doctoral reasearcher, Inria Paris).

- in R:
 - **mice** (van Buuren and Groothuis-Oudshoorn, 2011): it is a multiple imputations method by chained equations. Even if it returns several imputed data sets, they can be aggregated using the mean of the imputations to get a single imputation.
 - **missForest** (Stekhoven and Bühlmann, 2012): it imputes missing values iteratively by training random forests.
 - in Python:
 - **IterativeImputer** of scikit-learn library (Pedregosa et al., 2011): this function is inspired by mice, but it uses (iterative) regularized regression, imputes by the conditional expectation and provides a simple imputation. We also use the **ExtraTreesRegressor** estimator of **IterativeImputer**, which trains iterative random forests (it is similar to **missForest** in R).
3. low-rank based models, the data matrix to impute is assumed to be generated as a low rank structure plus a noise term.
- in R:
 - **softImpute** (Hastie et al., 2015): it minimizes the re-weighted least squares error penalized by the nuclear norm.
 - **missMDA** (Josse et al., 2016): it minimizes the re-weighted least squares error penalized by a mix between the ℓ_2 -norm and ℓ_0 -norm.
 - in Python: **softImpute** (coded for the purpose of this notebook and available here¹⁴), which minimizes the re-weighted least squares error penalized by the nuclear norm and with an internal cross-validation step to choose the regularization parameter.
4. machine learning methods (for the Python workflow only) using optimal transport or variational autoencoders.
- in Python:
 - **MIWAE** (Mattei and Frellsen, 2019): it imputes missing values with a deep latent variable model based on importance weighted variational inference.

¹⁴<https://github.com/R-miss-tastic/website/blob/master/static/how-to/python/softimpute.py>

- **Sinkhorn** (Muzellec et al., 2020): it randomly extracts several batches and consists in minimizing optimal transport distances between batches to impute missing values.

In R This workflow¹⁵ provides two main functions which compares the imputation methods: (i) on a simulated dataset for different mechanisms and percentage of missing values (`how_to_impute`) or (ii) on a list of real datasets and a given mechanism and percentage of missing values (`how_to_impute_real`).

The output of the first function `how_to_impute` is the mean of the methods’ MSEs for the different missing values settings by taking the average over several repetitions (the number of repetitions can be specified through the argument `nbsim`). Figure 5 shows the output of this function and its associated plot, when the simulated dataset is Gaussian with $n = 1000$ observations, $d = 10$ variables, a mean vector such that $\mu_i = 1, \forall i \in \{1, \dots, d\}$ and a covariance matrix such that $\Sigma_{ij} = 0.5$ if $i \neq j \in \{1, \dots, d\}$, and $\Sigma_{ij} = 1$ if $i = j$. In Appendix A, this function is illustrated for a particular dataset.

For the MCAR mechanism, the methods perform well, while for the MNAR mechanism, the results are close to those of the naive imputation by the mean. As expected, most methods give worse results for high percentages of missing values.

The second function `how_to_impute_real` can be particularly useful for practitioners who would like to have an indication of which method might be the most suited for a given or for several specific datasets. It returns a table containing the mean of the MSEs for the simulations performed and a table for the summary plot shown in Figure 6. Here, the real datasets are taken from the UCI repository¹⁶ (Dua and Graff, 2019).

An additional workflow¹⁷ is available and compare other deep-learning imputation strategies to most classical ones on data sets simulated either with linear relationships and nonlinear relationships. The conclusions points to better behavior of the low-rank based imputations methods even when deep-learning methods are tuned.

In Python The Python workflow is very similar to its R counterpart. The two same functions, `how_to_impute` and `how_to_impute_real`, have been implemented.

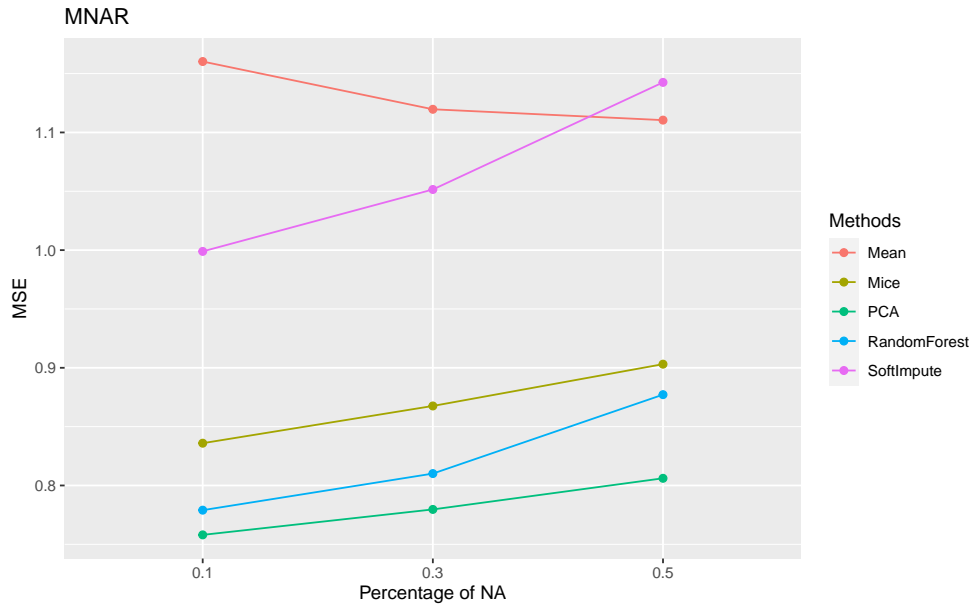
¹⁵<https://rmissstastic.netlify.app/how-to/impute/missimp>

¹⁶<http://archive.ics.uci.edu/ml/index.php>

¹⁷This workflow has been implemented by an external contributor, François Husson (Professor in Statistics, France).

| | 0.1 MCAR | 0.3 MCAR | 0.5 MCAR | 0.1 MAR | 0.3 MAR | 0.5 MAR | 0.1 MNAR | 0.3 MNAR | 0.5 MNAR |
|-----------------|----------|----------|----------|---------|---------|---------|----------|----------|----------|
| <i>X.pca</i> | 0.74 | 0.76 | 0.78 | 0.75 | 0.78 | 0.81 | 0.76 | 0.78 | 0.81 |
| <i>X.forest</i> | 0.77 | 0.8 | 0.86 | 0.78 | 0.81 | 0.87 | 0.78 | 0.81 | 0.88 |
| <i>X.mice</i> | 0.82 | 0.83 | 0.86 | 0.83 | 0.86 | 0.9 | 0.84 | 0.87 | 0.9 |
| <i>X.soft</i> | 0.93 | 0.86 | 0.87 | 0.97 | 1 | 1.1 | 1 | 1.1 | 1.1 |
| <i>X.mean</i> | 1 | 0.99 | 1 | 1.1 | 1.1 | 1.1 | 1.2 | 1.1 | 1.1 |

(a) Output of the function `how_to_impute` in R. The results are truncated to two digits. Note that the line `X.pca` is the result for **missMDA**. For all methods, the default parameter choices are used.



(b) Example of plot for the MNAR mechanism (one plot per mechanism).

Figure 5: Tabular and graphical outputs of the R function `how_to_impute`. The methods **mice**, **missForest**, **softImpute** and **missMDA** are compared with the naive imputation by the mean for several percentages of missing values (10%, 30%, 50%). The mean of the MSEs computed for several generations of missing values are given. In the tabular, the results are shown for several mechanisms (MCAR, MAR, MNAR) and the plot corresponds to the MNAR mechanism.

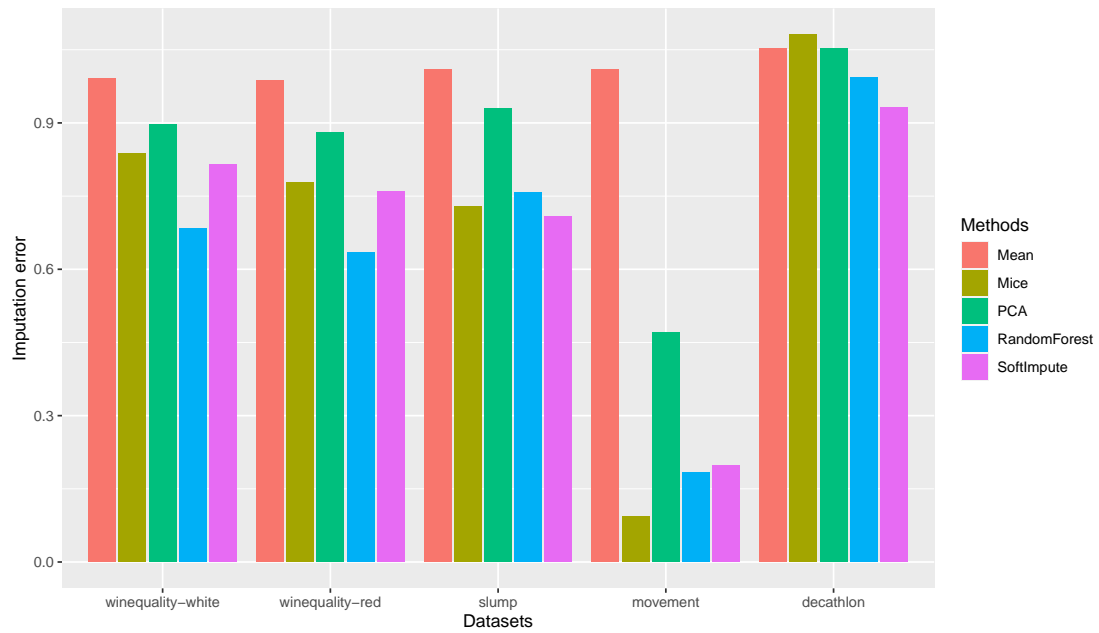


Figure 6: Graphical output of the R function `how_to_impute_real`. The methods **mice**, **missForest**, **softImpute** and **missMDA** for several real datasets in which 20% MCAR missing values have been introduced.

3.3 How to estimate parameters with missing values in R?

This R workflow¹⁸ is dedicated to a specific inferential framework when the aim is to estimate linear and logistic regression parameters for multivariate normal data. It is currently only available in R, as there are no analogous implementations available in Python to our knowledge.

There are two main methods to estimate parameters with missing values: maximum likelihood estimation adapted to missing values, using, e.g., EM-based algorithms or using multiple imputation. In this workflow, we compare two instances of these main methods, using available R implementations: the EM algorithm for logistic and linear regressions with the package **misaem** (Jiang et al., 2020) which uses the Stochastic Approximation of EM algorithm (SAEM Delyon et al., 1999) and multiple imputation with the package **mice**. Both strategies are valid under the MAR missing data mechanism. The workflow performs the estimation on a simulated dataset, but the dataset can be replaced with any custom dataset that the user believes satisfies the assumptions about the missing data mechanism and distribution of covariates.

The **misaem** package allows to estimate parameters of linear and logistic regression models from incomplete data, but it also provides valid estimates of these parameters' variances. The functions `miss.lm` `miss.glm` resemble the standard `lm` and `glm` functions both in terms of its signature and output.

The rationale behind the popular multiple imputation approach is to create $M > 1$ complete datasets by imputing the missing values with “plausible” values, and then to estimate a parameter of interest θ on each of the imputed datasets. The multiple estimations of θ and their variability allow to reflect uncertainty due to the unknown missing values. The parameter estimation is performed by applying the analytic method that we would have used had the data been complete. This provides an estimate of the parameter θ and an estimate of the corresponding variance, for each imputed dataset. These quantities are finally “pooled” by using specific rules named “Rubin’s rules” (Rubin, 2004), leading to a final point estimate with a corresponding estimation of its variance that takes into account the uncertainty due to the missing values.

In the corresponding workflow, we compare this method to the previous EM algorithm and provide the basic lines of code required to estimate parameters of linear or logistic regression models with incomplete covariate data.

For a additional example of how to estimate regression parameters we refer to the

¹⁸<https://rmissstastic.netlify.app/how-to/estimate/missestim>

tutorial¹⁹ on how to handle missing values in R by Julie Josse: it guides through a complete analysis, covering visualization of missing data patterns, data visualization, dimensionality reduction of incomplete data, and regression in the presence of missing data.

3.4 How to predict in the presence of missing values?

As mentioned in the introduction, methods to deal with missing values are not the same when the aim is to estimate parameters or to predict a target variable. Josse et al. (2019) study the problem of supervised learning with missing values, i.e., when the aim is to predict an outcome y , from incomplete covariates in X . Note that contrary to the estimation setting, supervised learning involves training and test sets and both may have missing values. Josse et al. (2019) recommend to impute the training set and the test set with a same constant, such as the mean, and then to apply a universally consistent learner, i.e., a very powerful learner, such as gradient boosting, able to learn or fit any function. When random forests are used to do prediction, another method is available, the Missing Incorporated in Attributes (MIA) method (Twala et al., 2008). Note that mean imputation or MIA are recommended asymptotically but when having limited data in the prediction setting, other imputation methods can outperform these asymptotically consistent methods (Josse et al., 2019). This is explored in the following workflows. The different methods are compared in terms of quality of the prediction of the outcome (AUC for a binary outcome and MSE for a continuous outcome).

In R The R workflow²⁰²¹ assesses a popular strategy (two-step strategy) which consists in imputing the training set and the test set independently with the same imputation method and in using usual learning algorithms to predict a target variable. Several imputation methods are compared, such as **mice**, **missForest**, **softImpute** and the mean imputation. Note that, until recently, using the popular **mice** package for learning predictive models on incomplete data in R was hindered by the fact that it did not allow to use the same imputation model for the training and for the test set. This has, however, been addressed and the details of this recent extension can be found on GitHub.²²

¹⁹https://rmisstastic.netlify.app/tutorials/josse_bookdown_dataanalysismissingr_2020

²⁰https://rmisstastic.netlify.app/how-to/external/how_to_predict_in_r

²¹It has been written by an external contributor of the website, Katarzyna Woźnica (PhD student at the Warsaw University of Technology, Poland).

²²<https://github.com/amices/mice/issues/32>

In Python The Python workflow²³ proposes to compare two strategies when the aim is to predict a target variable and the covariates may contain missing values:

1. The *two-step* strategy consists in imputing the missing values both in the training and in the test set with a method like mean imputation or `IterativeImputer` of the **scikit-learn** library, and to apply usual learning algorithms (random forests, gradient boosting, linear regression) on the imputed dataset. This learning algorithm can be applied to the imputed dataset \tilde{X} but also to a new variable made of the combination of the imputed covariates \tilde{X} with the response pattern R : $[\tilde{X}, R]$.
2. The *one-step* strategy aims at predicting with learning methods adapted to the missing data without necessarily imputing them, such as the MIA method (Twala et al., 2008), which we have implemented in our notebook.

We propose a function, `score_pred`, which compares these strategies in terms of prediction performances by introducing missing values in complete covariates under a specific missing data mechanism and a given percentage of missing values. The dataset is then split into a training set and a test set (75% in the training set, 25% in the test set) and the methods presented below are applied by considering a specific learning algorithm. The function then returns the prediction error on the test set, by comparing the ground truth (y) and the predicted outcome values on the test set for each simulation (i.e., each run for the generation of missing values). Figure 7 shows the graphical output of this function called for different learning algorithms (linear regression, random forests and gradient boosting) and for different missing data mechanisms (20% MCAR and MNAR, see Section 3.1).

When the learner is the linear regression, the two-step methods with added mask, both for the MCAR mechanism and the MNAR mechanism, perform well. Since the simulated dataset is generated considering a linear regression, the linear regression is expected to give better results than the other learners. In addition, for the MNAR mechanism, the one-step strategy *MIA* (especially when the gradient boosting is performed) appears to be a good choice.

Another function `plot_score_realdatasets` is specifically designed to handle datasets which already contain missing values. Appendix B shows a concrete example of this notebook on a real dataset.

This concludes the overview of the workflows which have been developed in this project and which we consider as an invitation to other practitioners and researchers to use and

²³https://rmissstastic.netlify.app/how-to/python/predict_html/how%20to%20predict

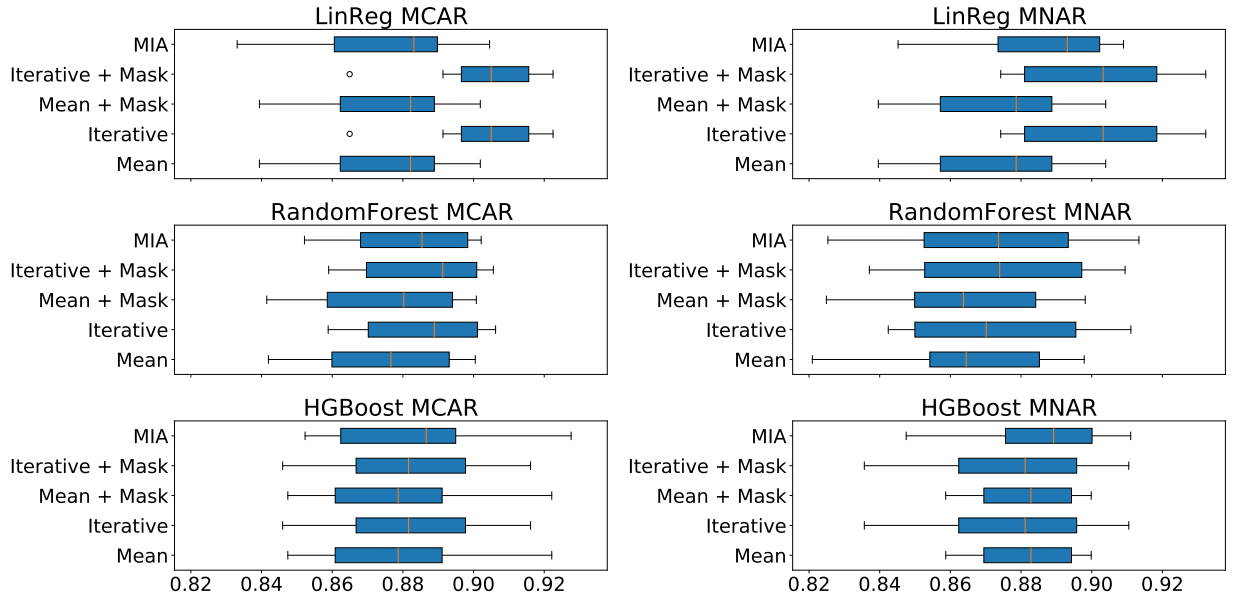


Figure 7: Plot of the function `score_pred` to compare different strategies when the aim is to predict in Python. 20% of missing values are introduced in a simulated dataset using the MCAR mechanism or the MNAR mechanism. The covariates $X \in \mathbb{R}^{1000 \times 3}$ are generated under a multivariate Gaussian distribution, the parameter of the regression $\beta \in \mathbb{R}^3$ follows a random uniform distribution. The outcome y is generated according to a linear model such that $y = X\beta + \epsilon$, with ϵ a Gaussian noise. The two-step strategies (**IterativeImputer** and the mean imputation) with or without adding a mask and the one-step strategy *MIA* are compared in terms of prediction error, and several learners are performed (linear regression, random forests, gradient boosting). The closer the result is to 1, the more accurate the prediction is (1 corresponds to perfect prediction, 0 to the worst prediction).

extend them for better comparability between methodologies when suggesting new methodologies in research articles.

4 Perspectives and future extensions

By providing a platform and community to discuss missing data, software, approaches and workflows, the sharing of expertise on missing data can hopefully improve and extend more easily.

4.1 Towards uniformization and reproducibility

One way to promote and encourage practitioners and researchers in their work with missing values is to provide community benchmarks and workflows centered around missing data. As has been demonstrated with data competitions, involving the community brings forth many creative solutions and discussions that advance the field, and challenge existing strategies. We will continue working on our workflows and the corresponding source code. In doing so, we hope to encourage users to continue benchmarking new methods and to present the results in a clear and reproducible way. In addition, we plan to propose two types of data challenges: 1) imputation and estimation, and 2) analysis workflows. For the first challenge, the objective is to find the best imputation or estimation strategy. The community would be given a dataset with missing values, for which there is actually a hidden copy of the real values. The community is then tasked with creating imputed values, which are assessed against the original dataset with complete values, to determine which imputation is best. This is similar in spirit to the Netflix prize (Bennett et al., 2007) and the M4 challenge in the time series domain (Makridakis et al., 2018). This benchmarking could be extended to other areas, such as parameter estimation, and predictive modeling with missing data. Analysis workflows could form another community challenge, assessed in a similar way to existing “datathon” events where entries are assessed by an expert panel. Here the challenge could be to develop workflows and data visualizations from complex data. The data could have challenging features, and be combined from various data with complex structure, such as data with several types of missingness, images, text, data, longitudinal data, and time series.

4.2 Future extensions

Potential extensions that could be added in future releases of the platform and for which we welcome suggestions and contributions are the following: a workflow with a focus on MNAR data and different solutions that can handle such data (as diversity of existing solutions is large, such a unified workflow will be a consequential contribution); for more applied users, a comparison of computation times of different methods, benchmarked on various types of data. In addition, a more and more often encountered problem concerns missing values in data integration. Indeed, questions such as *what do I do when I have clinical data from multiple centers with different mechanisms of missing values or with systematically missing values in certain data?* or *what do I do when I have time series and missing values in one of the groups of variables?* would be also worth addressing in a new workflow.

4.3 Participation and interaction

This platform is aimed to be a venue for the community, in the sense that we welcome every comment and question, encourage submissions of new work, theoretical or practical, either through the provided contact form or directly via the GitHub project repository. We have already received much useful feedback and contributions from outside, organized several remote calls and working sessions at statistics conferences. We are planning on regularly relaunching calls for new material for the platform, for instance through the R consortium blog²⁴, R-bloggers²⁵ and social media platforms. We also intend to use these channels to communicate more generally about the platform and the topic of missing values.

In order for the platform to be a reference to the community, it needs to provide regularly updated user friendly content. Proposing sustainable and accessible solutions for the maintenance of the “R-miss-tastic” platform is crucial to achieve this goal. We hope that the well documented code source of the platform invites contributions and community feedback on this project.

In conclusion, the aim of this platform is to go further than merely community participation, namely to seed meaningful community interactions, and make it a hub of communication among groups that rarely exchange, both within, and between academia and industry.

²⁴<https://www.r-consortium.org/news/blog>

²⁵<https://www.r-bloggers.com/>

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A Tutorial for imputing missing values in R

The goal of this tutorial is to give practical details on the R-workflow entitled *How to impute missing values?*²⁶. In this workflow, users can compare the most popular methods to impute missing values in R on simulated or real datasets.

We illustrate this workflow by considering a toy dataset called *airquality*, that contains athletes' performance during two sporting events (41 rows, 13 columns²⁷). It is available in the R-package **FactoMineR**.

```
1 library(FactoMineR)
2 data(decathlon)
3 head(decathlon[,1:4]) # four first columns of the dataset
4
5 ##           100m Long.jump Shot.put High.jump
6 ## SEBRLE  11.04      7.58    14.83    2.07
7 ## CLAY    10.76      7.40    14.26    1.86
8 ## KARPOV  11.02      7.30    14.77    2.04
9 ## BERNARD 11.02      7.23    14.25    1.92
10 ## YURKOV  11.34      7.09    15.19    2.10
11 ## WARNERS 11.11      7.60    14.31    1.98
```

If we have collected similar data, e.g., described by the same variables but for new athletes, that contain missing values, practitioners may want to know how to impute such a dataset. To address this question, we can introduce missing values under different mechanisms (MCAR, MAR or MNAR) and with different percentages of missing values (here we compare 20% and 50%) in the complete dataset and compare some imputation methods in terms of mean squared error (MSE), i.e., the error committed by the imputation of the missing values. The function `how_to_impute` can be used to compare the imputation methods described in Section 3.2 (**missMDA**, **mice**, **missForest**, **softImpute** and the imputation by the mean) using different percentages and types of missing values given in two lists by the users. More particularly, the arguments are the following ones:

²⁶This tutorial is only an example of use but more practical details are given in the original workflow.

²⁷We do not consider the last variable in this part, which is categorical. Some imputation methods do not handle mixed data.

- `X`: the complete dataset where the missing values will be introduced (matrix).
- `perc.list`: list containing the different percentage of missing values.
- `mecha.list`: list containing the different missing-data mechanisms ("MCAR", "MAR", "MNAR").
- `nbsim`: number of simulations performed.

Note that for **missMDA**, the number of components in the PCA used to predict the missing entries is estimated using a cross-validation with the function `estim_ncpPCA`. For **softImpute**, we use a cross-validation to choose the regularization parameter (coded for the purpose of this notebook). This function returns a table with the mean of the MSEs over the simulations for the different methods and for the different missing data settings (20% MCAR values, 50% MCAR values, 20% MAR values, 50% MAR values, 20% MNAR values, 50% MNAR values).

```

1 perc.list <- c(0.2,0.5)
2 mecha.list <- c("MCAR", "MAR", "MNAR")
3 how_to_impute(X=decat_sc, perc.list=c(0.2,0.5),
4               ... mecha.list=c("MCAR", "MAR", "MNAR"), nbsim=10)
5
6 ##           0.2 MCAR   0.5 MCAR   0.2 MAR   0.5 MAR   0.2 MNAR   0.5 MNAR
7 ## X.pca      0.8822782 1.0537611 0.9394561 1.0873315 0.9876867 1.1026891
8 ## X.forest  0.8820789 0.9577351 0.9403659 1.0526915 0.9940827 1.0809478
9 ## X.mice    0.8610320 1.0372518 0.9559042 1.0948981 0.9887239 1.1271581
10 ## X.soft   0.7935545 0.8865989 0.8721907 0.9556373 0.8951239 0.9692859
11 ## X.mean   1.0177192 1.0306089 1.0972080 1.0770715 1.1342289 1.1077467

```

With this result in hand, we can easily visualize some of the results (the corresponding code is provided in the R-workflow). For this dataset and these missing data settings, **softImpute** appears to be the best imputation method.

B Tutorial for predicting in presence of missing values in Python

The goal of this tutorial is to give practical details on the Python-workflow entitled *How to predict with missing values?*²⁸. In this workflow, users can compare methods in Python to predict a target variable when the covariates contain missing values.

²⁸This tutorial is only an example of use but more practical details are given in the original workflow.

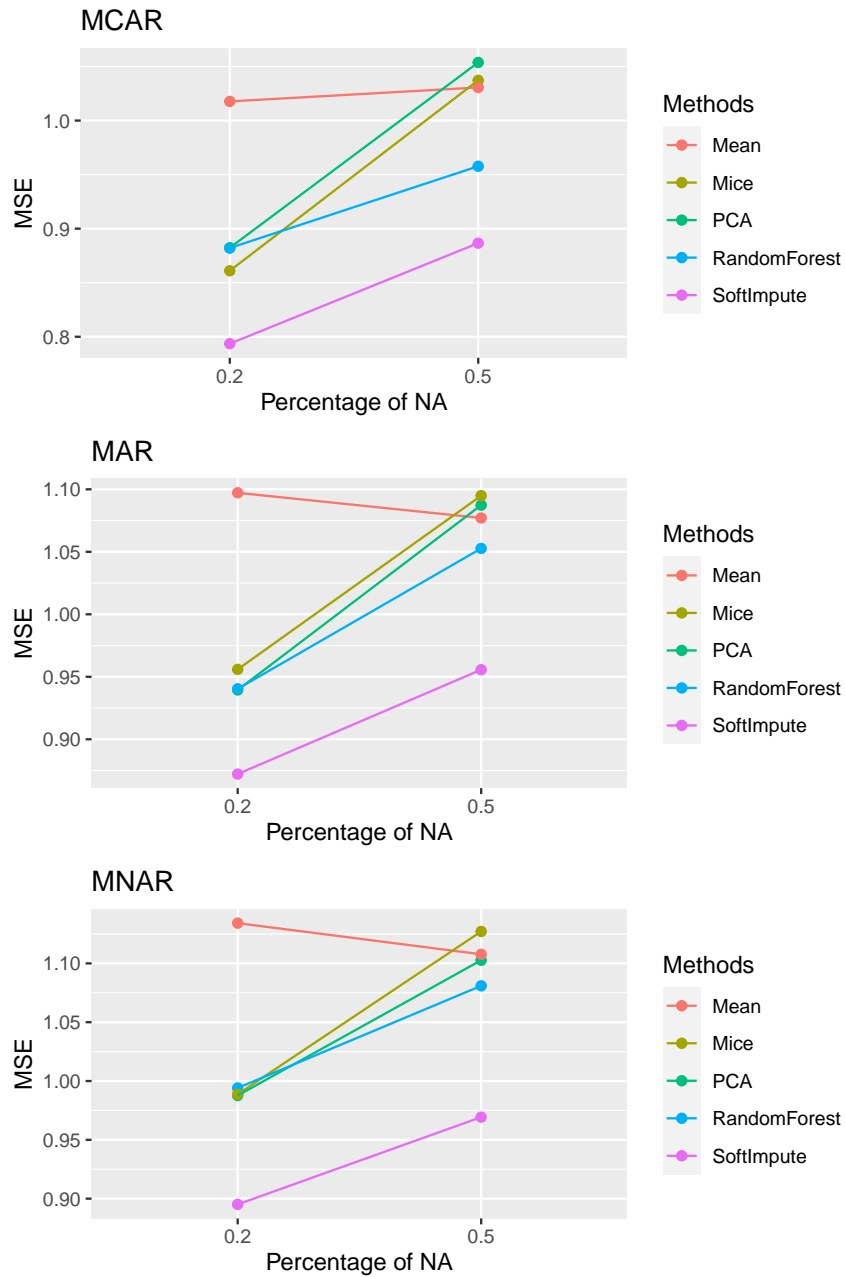


Figure 8: Graphical outputs of the R function `how_to_impute`. The methods **mice**, **missForest**, **softImpute** and **missMDA** are compared with the naive imputation by the mean for several percentages of missing values (20%, 50%). The mean of the MSEs computed for several generations of missing values are given. The results are shown for different mechanisms (MCAR, MAR, MNAR).

We consider the dataset called *california_housing* (20640 rows, 9 columns). The target variable is the median house value for California districts and the covariates provide information (latitude, longitude, number of people in the district...) on the different districts.

If we know that new observations will contain missing values, an interesting question is to know how to predict the target variable in presence of missing values in the covariates. To answer this, we can impute missing values in the covariates and compare methods which handle them and predict the target variable. To generate missing values in a complete dataset, the function `produce_NA` can be used. In the following example, we introduce 20% MCAR values.

```
1 XproduceNA_MCAR = produce_NA(x_comp, p_miss=0.2, mecha="MCAR")
2 x_MCAR = XproduceNA_MCAR['X_incomp'].numpy()
```

To predict, we consider two strategies presented in Section 3.4: (i) the *two-step* strategy which consists in imputing missing values and applying classical methods on the completed data sets to predict, and (ii) the *one-step* strategy which predicts using methods adapted to the missing values without necessarily imputing them. The code below allows to compare different prediction strategies nested in a two-step or a one-step strategy.

```
1 learners = {'LinReg': LinearRegression()
2             'RandomForest': RandomForestRegressor(),
3             'HGBost': HistGradientBoostingRegressor()}
4
5
6 for learner_name, learner in learners.items():
7     plt.figure(figsize=(10,10))
8     for ii, (X, X_name) in enumerate(zip([x_MCAR], ['MCAR'])):
9         plt.subplot(3, 2, ii+1)
10        plot_score_realdatasets(X, y, learner, learner_name
11                                + ' ' + X_name, x_comp)
```

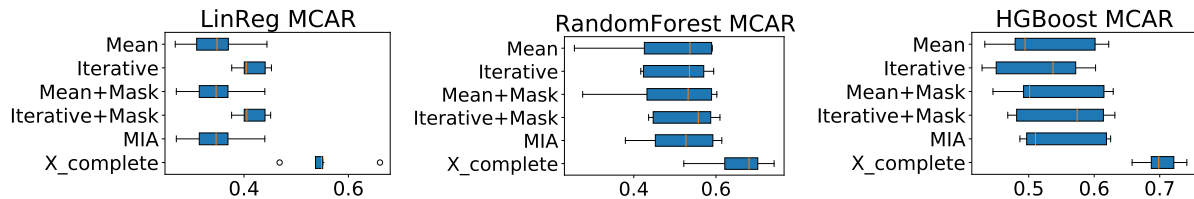


Figure 9: Graphical outputs of the Python function `plot_score_realdatasets`. The x-axis indicates the MSE. The two-steps methods considering the imputation by the mean (Mean), IterativeImputer (Iterative) with or without adding the mask and the one-step method MIA are compared with the case without missing values (X_complete). Note that the mask is the binary matrix which indicates where are the missing values. When we add the mask, we consider then an augmented matrix, with the initial matrix and the mask. The learner are the linear regression (left graphic), the random forests (middle graphic) and gradient boosting (right graphic).

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