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Prognostics of Health Status of Multi-component Systems With Degradation Interactions

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Abstract—Many models and methodologies in order to predict the remaining useful life (RUL) of a critical component are investigated nowadays. However, estimating remaining useful life of multi-component systems is still an under explored area, especially when there are interdependencies among the components of these systems. Practically, prognostics can be quite complicated when there is absence of prior knowledge about these interactions. To optimize the availability and reliability of the system, it is required to embed a dependency model that implements component strength and the component's health status. In this paper, a novel approach is proposed in order to emphasize the importance of interactions between complex system's components in the RUL's calculating. The effectiveness of the approach is judged by applying it to numerical studies in order to estimate system's remaining useful life.

I. INTRODUCTION

Nowadays, the development of industrial systems is increasingly complex due to new technologies, and industrial manufacturing systems are becoming more complicated. Complex system may be defined as a coherent system composed of many interacting entities. Controlling, managing and keeping such a system in a good health status isn't an easy task. This topic has received more attention from academic researchers and manufactures in the past decade. In fact, many research works have been developed on reliability of complex systems and their maintenance [11], [10], [1]-[2]. Prognostics is considered as a key process in maintenance strategies in order to predict the RUL (remaining useful life) and the performance of multi-component and networked systems, like aircraft, cars and mechanical machinery. Prognostics and Health Management (PHM) is an emerging discipline which links studies of failure mechanisms and life cycle management [3]. According to ISO:13381-1, prognostics is defined as the "estimation of time to failure and risk for one or more existing and future failure modes" [4]. The use of prognostics methods in maintenance in order to predict the RUL is receiving more attention over the past years. Many experts expect that effective prognostics will result (i) in reduced numbers and severity of failures, especially failures in the field, (ii) optimizing operational performance, (iii) extending the time between needed maintenance activities and reducing life-cycle costs. However, the use of these techniques in maintenance decision making and optimization in multi-component systems is still an under explored area due to the complexity of these systems which introduces additional interdependencies between components. In fact, complex systems are handled differently from single-component systems

because we need a full understanding of interactions between components, and neglecting them leads to inefficient prognostics. Ancient approaches are reduced to consider the minimum of critical components RULs and to neglect interdependencies between components in order to avoid any possible system's shutdown. Nevertheless, many researches have reported that the assumption of independence is impractical. In fact, Sun et al. [7] notice that this assumption leads frequently to errors in estimating the system's RUL in real applications. Therefore, the decision making based on the resulting remaining useful life should be established in a predictive maintenance policy which highlights dependency between system components. Interdependencies between complex system components have been extensively studied in operations research literature for the past few decades. Murthy and Nguyen [5] indicate that the analysis of maintenance policies with failure interactions is an open problem. More recently, Nicolai and Dekker [6] have given a thorough overview of optimal maintenance policies for complex systems with dependency between components (i.e. stochastic, structural or economic dependence). However, no models that use prognostics or a prediction of Remaining Useful Life are mentioned. This paper focuses on stochastic dependence, where the degradation or the failure of one component influences the life time distribution of other components in the system, i.e. if a component degrades over time (due to wear, environmental variables or use conditions), it has an impact on the performance of other components by means of accelerating their degradation. In that context, Bian and Gebraeel focus on how degradation-based sensor signals associated with the components evolve over time, using stochastic models characterizing the natural degradation rates and the effects of interactions on the degradation rate [8]-[9]. Wu et al. [10] present a method to consider stochastic loading and strength degradation for computing the time-dependent reliability of a structural component. Besides, Van Horenbeek and Pintelon [11] present a dynamic predictive maintenance policy for complex systems that minimizes the long-term mean maintenance cost per unit time. This method is based on prognostics information while considering different component dependencies (i.e. economic, structural and stochastic). Moreover, Ribot [12]-[13] aims at improving classical approach to estimate the RUL of a complex system. Mainly, Ribot's approach has an advantage of better system modeling, when there is absence of components dependency. Our work differs from the papers mentioned above in two folds, as shown in Fig. 1: i) Presenting a stochastic dependency model for degradation rate

interactions, ii) Proposing a prognostics method to calculate the system's RUL considering the degradation rate interactions between system's components. The remainder of the paper is

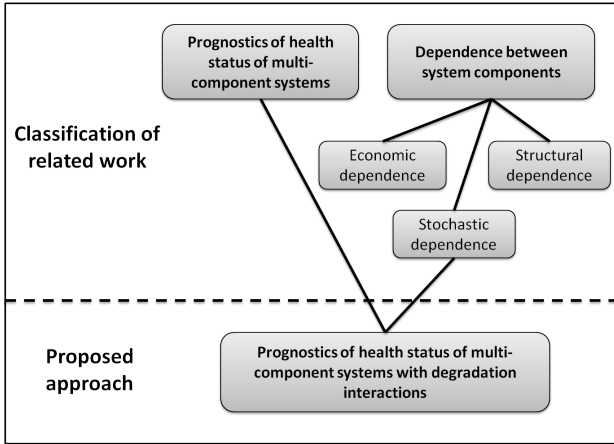


Fig. 1: Position of the proposed approach

organized as follows: In section 2, we describe the prognostics method. Sequentially, we present a stochastic dependency model in details with necessary assumptions. Under these assumptions, we prove in section 4 our approach by presenting a numerical studies. Conclusions are presented in section 5.

II. PROGNOSTICS METHOD

A. Introduction

Prognostics basically consists in estimating at time t_i the time t_{i+1} of the system failure. A prognostics function is defined to assess the probability associated with each possible future failure for the system. This probability is obtained from a set of aging models available in the current operational mode of the system. We assume that a set of aging models is available for each component in the system. These models represent the knowledge available about component's wear. They may indicate an average value of the next component's failure as the mean time to failure (MTTF) [12]-[13]. We consider as an example, a system of two interconnected components C_1 and C_2 with a set of failure probability density functions denoted by $f_{C_1}(t)$ and $f_{C_2}(t)$ respectively, as in Fig. 2, where the Weibull model represents the probability density function.

B. System's remaining useful life

We consider a system of n interconnected components C_1, C_2, \dots, C_n with a set of aging models denoted by $S_1(t), S_2(t), \dots, S_n(t)$ respectively. $S_i(t)$ is defined without taking into account interactions between components, in other word, it represents the component's own model. Failure probability is determined for each component from its aging model selected in the current operating mode. Let f_i denote the probability density function (pdf) representing the failure probability of a component i in its current operating mode, P_{max} be the maximal failure probability threshold acceptable for the component C_i . The *remaining useful life* of C_i consists in determining the time t_c for which the failure probability has reached the

threshold P_{max} , as in (1).

$$RUL(C_i) = t_c \text{ such that } \int_0^{t_c} f_c(t) dt = P_{max} \quad (1)$$

The date of the next system failure is then calculated by :

$$t_{i+1} = t_i + \min(RUL(C_i)) \text{ where } i \in [1, n] \quad (2)$$

C. Weibull model

The difficulty is to establish a common prognostics representation for each type of component. This representation should be as flexible as possible to represent the failure probability density functions of each component in the system.

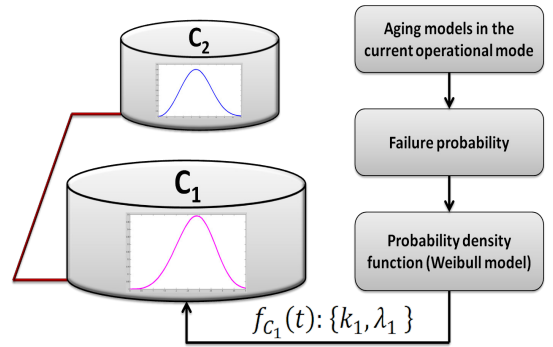


Fig. 2: Component's representation with the Weibull model

The probabilistic Weibull model is often used in the field of survival and failure analysis, reliability and systems life data analysis [14]-[12]. The Weibull probability density function is:

$$W(t, \kappa, \lambda, \theta) = \frac{\kappa}{\lambda} \left(\frac{t - \theta}{\lambda} \right)^{\kappa-1} e^{-\left(\frac{t-\theta}{\lambda}\right)^\kappa} \quad (3)$$

where $t \geq 0$, $\kappa \geq 0$, $\lambda \geq 0$, and $\theta \geq 0$. κ represents the shape parameter of the distribution, λ defines the scale parameter and θ determines its location on the time axis. These parameters define the probability distribution and model component aging signs. We assume that prognostics were done in the same time for all system's components, this translates into $\theta = 0$. For a given component C_i and a given probability threshold P_{max} , the remaining useful life is:

$$RUL(C_i) = t_c \text{ such that } \int_0^{t_c} \frac{\kappa}{\lambda} \left(\frac{t}{\lambda} \right)^{\kappa-1} e^{-\left(\frac{t}{\lambda}\right)^\kappa} dt = P_{max} \quad (4)$$

III. STOCHASTIC DEPENDENCY MODEL FOR DEGRADATION RATE INTERACTIONS

In this section, we present a stochastic methodology by modeling the degradation interactions effects of interdependent components C_1, C_2, \dots, C_n knowing its failure cumulative distribution functions $F_1(t, \kappa_1, \lambda_1), F_2(t, \kappa_2, \lambda_2), \dots, F_n(t, \kappa_n, \lambda_n)$ (6).

A. Cumulative distribution function CDF

To facilitate the analysis of degradation interactions between system components, each component will be represented by its cumulative distribution, as in Fig. 3. Moreover, CDF will allow us to fully note the degradation of the component's health state. In probability theory and statistics, the cumulative distribution function of a continuous random variable X can be expressed as the integral of its probability density function f_X as follows:

$$F_X(t) = \int_{-\infty}^t f_X(t) dt \quad (5)$$

The cumulative distribution function for the Weibull distribution is:

$$F(x; \kappa; \lambda) = 1 - e^{-\left(\frac{x}{\lambda}\right)^\kappa} \quad (6)$$

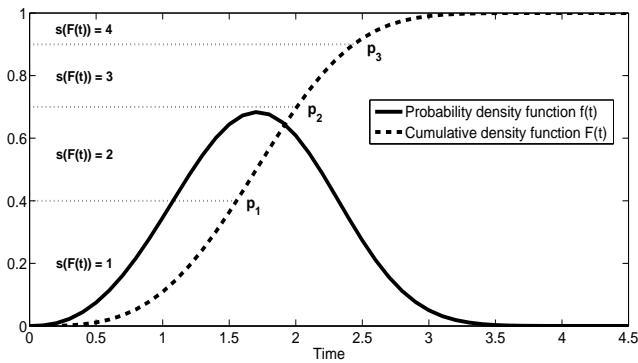


Fig. 3: CDF of the Weibull distribution with different degradation states

B. Component's degradation states

Interaction considers that the failure of one component induces failure of all other interdependent components. We refer to the former as the "influencing component" and the latter as the "affected component". The transition of an influencing component, say C_i to a more degraded state increases the degradation rate of the affected component, say C_a by an amount $\rho_{i \rightarrow a}$ which depend on the degradation states of the influencing component. We can take as an example "the gear train" which is a mechanical system formed by mounting gears on a frame so that the teeth of the gears engage. The degradation of a gear teeth may cause the degradation of the next one, which may increase the looseness of the smooth transmission of rotation from one gear to the next. In this example, the system is the rotation transmission system. Thus, based on the value of failure probability, a component C_i can be classified into different degradation states, e.g., "nominal", "degraded", "critical", "failed" (see Fig. 3). Let $s_i(t)$ denotes the degradation state of component C_i , whereby s_i is piecewise constant function, as in (7):

$$s(F_i(t)) = \begin{cases} 1 & F_i(t) < p_{i,1} \\ 2 & p_{i,1} \leq F_i(t) < p_{i,2} \\ 3 & p_{i,2} \leq F_i(t) < p_{i,3} \\ 4 & F_i(t) \geq p_{i,3} \end{cases} \quad (7)$$

where $p_{i,1}$, $p_{i,2}$, $p_{i,3}$ and $p_{i,4}$ represent the probability thresholds for different degradation states. $s(F(t))$ represents the degradation state of the influencing component.

C. Component's strength

Most components degrade as they age or deteriorate as a result of some factors that termed as covariates, i.e., degree of use, amount of load or extent of stress they experienced. To illustrate this idea, we can take the example of health concerns of old people. As people age, poor resistance and strength contribute to falls, health problems and, in some cases, fatal complications. Let $R_i(t)$ represents the strength of component C_i . $R_i(t)$ is a random variable that decreases over time and it can be described by gamma process which reduces the reliability and accelerate the risk of failure and shortens its life service [10]. Wu et al. [10] define the component strength which drops below the load as: $R_i(t) = R_0 - x(t)$, where R_0 represents the initial strength and $x(t)$ is the component strength's deterioration over time, as in Fig (4).

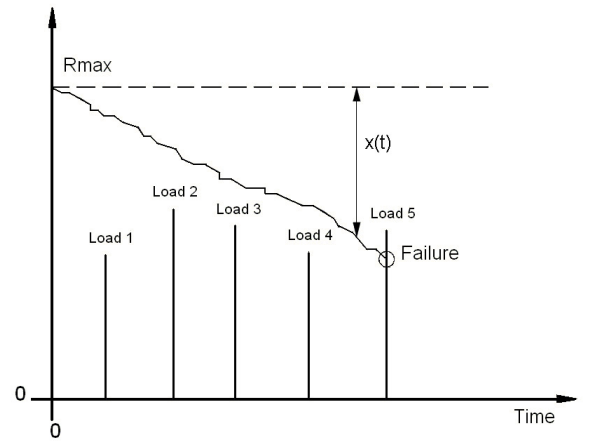


Fig. 4: Deterioration of component strength

D. Degradation rate of interactions

We denote the degradation rate of component C_i at time t by $r_i(t)$. We assume that $r_i(t)$ is composed of two parts: (i) Component's strength, (ii) component's degradation state. Thus, our proposed degradation rate of component C_i can be written in the following form: $r_i(t) = r_i[t; R_i(t), s(F(t))]$. To facilitate model development, we assume that the degradation rates of system components can be expressed as:

$$r(t) = \frac{\rho_{i \rightarrow a}}{R(t)} \quad (8)$$

Degradation occurs when the impact of influencing component degradation is higher than affected component's strength. Generally, the impact of influencing component's degradation tends to increase, while the component strength tends to decrease due to deterioration induced by higher than expected loads or fatigue damage.

E. Weibull model with degradation interactions

If the quantity t is a "time-to-failure", the Weibull distribution described in (3) gives a distribution for which the failure rate is proportional to a power of time. The shape parameter κ , is that power plus one [15], and so this parameter can be interpreted directly as follows :

- A value of $\kappa < 1$ indicates that the failure rate decreases over time.
- A value of $\kappa = 1$ indicates that the failure rate is constant over time.
- A value of $\kappa > 1$ indicates that the failure rate increases with time. This happens if there is an "aging process i.e., the degradation states of influencing components", or parts that are "more likely to fail i.e., component strength" as time goes on.

Moreover, the coefficient of variation depend only on the shape parameter. Thus, The degradation evolution of the cumulative distribution function $F_i(t)$ can be modeled as in (9):

$$F(t; \kappa'; \lambda) = 1 - e^{-\left(\frac{t}{\lambda}\right)^{\kappa \cdot r(t)}} \quad (9)$$

where $\kappa' = \kappa \cdot r(t)$. Equation (9) describes our stochastic dependency model which characterizes the effects of degradation interaction arising from other components. For the aim of this model, we consider the following assumptions:

1. κ represents the original degradation rate of the component C_a without taking into account the effect of dependency between system components, i.e., the strength of the "affected component" is maximal $R_a(t) = R_{aMax}$ and the degradation state of "the influencing component" is nominal $s(F_i(t)) = 1$.
2. The degradation rate of a component C_i is a linear function of its component strength and the degradation states of other influencing components, precisely $r(t) = \frac{P_{i,a}}{R(t)}$.
3. Degradation is triggered when the degradation of influencing component exceeds affected component's strength that is liable to deterioration, i.e., $r(t) > 0$.
4. The whole system is inspected simultaneously at a fixed time, and all inspection actions are perfect and instantaneous.

Figure 5 provides an example of the impact of component degradation interactions from a system that exhibit stochastic dependency.

IV. APPLICATION

A. System description

Our application is interested in ski lift. We illustrate our approach by studying the Lorry system which is a must for the good functioning of a ski lift, see Figure (6). Lorry is a tension system that enables to maintain cable tension almost constant on the driving pulley. In this case, an engine unit including the driving pulley is installed on a carriage which can move in the desired direction, forward or backward. In fact, the cable's length for a ski lift is made to change over

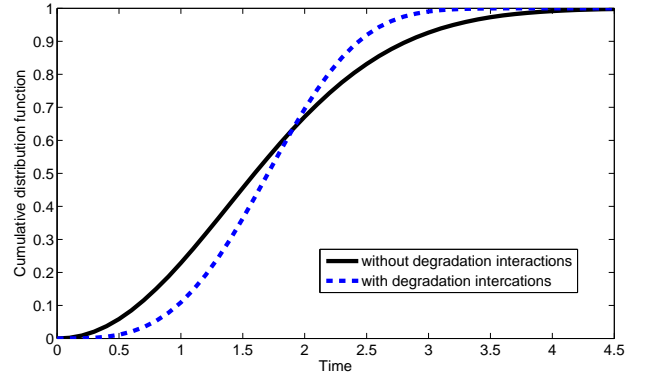


Fig. 5: Example of cumulative distribution function with degradation interactions

time, load and temperature. The cable's tension is mostly adjusted by one or two hydraulic jacks, which are powered by a hydraulic pump. We assume that engine of hydraulic pump and jacks present the most critical components of the system where engine is the influencing component and jacks represent the affected component. Thus, we consider a system

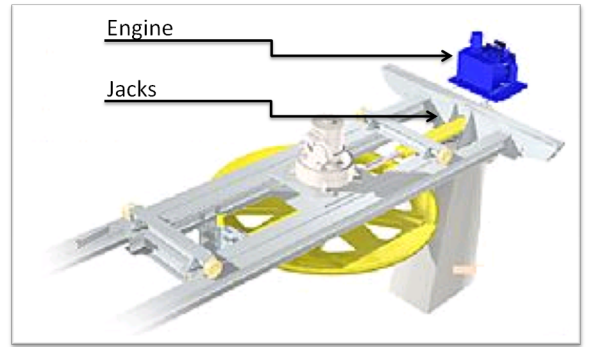


Fig. 6: Lorry system

of 2 interconnected components C_{engine} and C_{Jacks} with a set of failure probability density functions denoted by $f_{engine}(t)$ and $f_{Jacks}(t)$. λ and k represent respectively the scale and shape parameters, as in (10), and P_{Max} defines the probability threshold.

$$f_{engine} : \begin{cases} k_e = 2.6 \\ \lambda_e = 2 \\ P_{Max,e} = 0.9 \end{cases} \quad f_{Jacks} : \begin{cases} k_J = 2.1 \\ \lambda_J = 1.9 \\ P_{Max,J} = 0.9 \end{cases} \quad (10)$$

The system components are assumed to be interdependent and their degradation interactions are manifested in their cumulative distribution functions. For the purpose of this study, we simulate cumulative distribution functions for all two components using equation (6). To simulate degradation process for different scenarios, we consider two experimental settings: (i) In the first experiment, our model is equivalent to models that do not consider any interactions between components and assume components independence. (i) Next, for the second experiment, we study degradation interactions between system's components.

To facilitate our simulation, we start with a baseline setup. The initial strength of Jacks is $R_{Jmax} = 750MPa$, and it decreases over time as shown in Fig. 7. Next, we note that

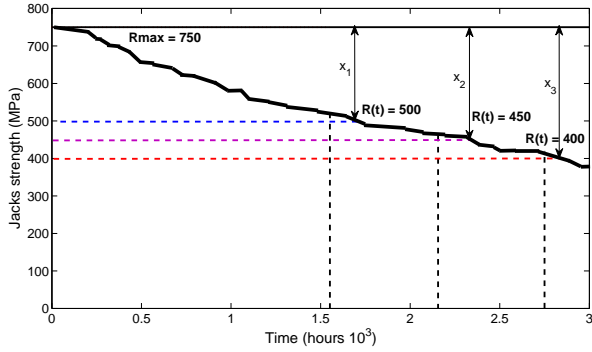


Fig. 7: Deterioration of Jacks strength

$\rho_{engine \rightarrow Jacks}$ represents the engine's degradation amplitude, i.e., the incremental change in the jacks degradation when engine switches to a more severe state. Engine degradation states are described in Fig. 8 where we notice four degradation states, nominal, degraded, critical and failed according to (11). For these degradation states, the values of probability thresholds $p_{engine,1}$, $p_{engine,2}$ and $p_{engine,3}$ are respectively 0.4, 0.7 and 0.9.

$$s(F_{engine}(t)) = \begin{cases} 1 & F_{engine}(t) < 0.4 \\ 2 & 0.4 \leq F_{engine}(t) < 0.7 \\ 3 & 0.7 \leq F_{engine}(t) < 0.9 \\ 4 & F_{engine}(t) \geq 0.9 \end{cases} \quad (11)$$

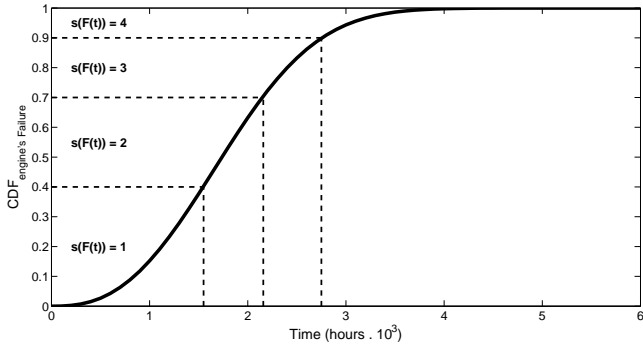


Fig. 8: engine's degradation states

To investigate the impact of different degradation magnitudes, we consider three levels of degradation interactions $r_J = (1.6; 2; 3)$, see table I. In other words, this allows us to study the impact of different amplitudes of degradation interactions.

B. Results

With the increase of degradation rate $r_J(t)$, the value of the RUL_{system} gradually decreases which can be shown in table II. In the first scenario where there are no interactions between system components, the system remaining useful life depends on the engine's RUL, i.e., engine represents the most

TABLE I: Degradation interactions rates

$\rho_{engine \rightarrow Jacks}(MPa)$	$R_{Jacks}(1000)(MPa)$	r_J
750	750	1 (No interaction)
800	500	1.6
900	450	2
1200	400	3

TABLE II: Simulation results

r_J	RUL_{Jacks}	RUL_{Engine}	RUL_{System}
1	1826.4	1750	1750
1.6	1435.3	1750	1435.3
2	1317.4	1750	1317.4
3	1168.9	1750	1168.9

critical component of the system. Taking into account the dependencies between the components changes the behavior of the system's RUL, and we clearly see that it becomes dependent of the value of the jacks RUL. Figures (9) and (10) illustrate the change in the jacks failure probabilities.

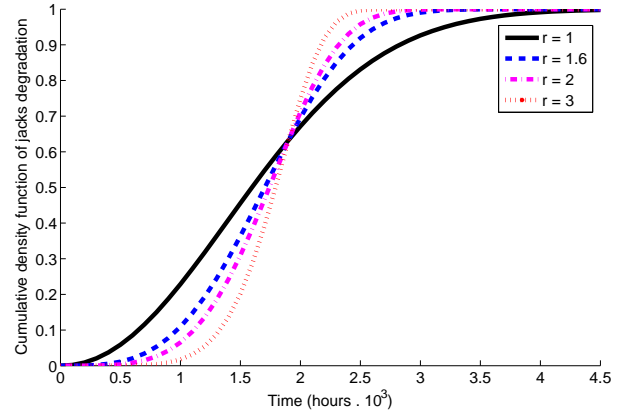


Fig. 9: CDF of jacks degradation interactions

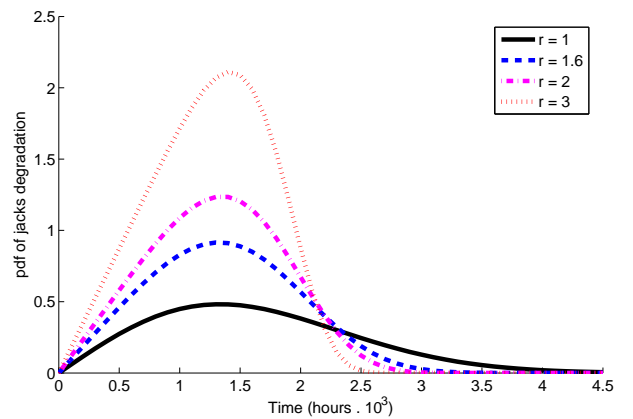


Fig. 10: Weibull model for jacks degradation interactions

Indeed, the high availability of systems such as aerospace, defense, petrochemical and automotive, is an important tar-

get of the new developments in systems design technology knowing that the failure is generally very expensive. To make maintenance strategies more effective and to take into account the system's changing status, the maintenance action has to be done at the right time according to the system remaining useful life given by the prognostics process. This allows us to increase the time of availability, performance and reliability of the system. The stochastic dependency is included in our approach to make it more accurate and realistic. In fact, a Weibull model is developed to highlight the link between prognostic method and dependencies between systems components. The decision making determined from the resulting RUL should be established, taking into account dependency between system components. These interactions require to be integrated in degradation models by considering these data as input data.

V. CONCLUSION

In this paper, we study prognostics approach for multi-component system which have failure interactions among them. The approach presented allows us in the first place to calculate the remaining useful life of system's components. Secondly, it permits to characterize the interactions among the degradation process of interdependent components where both the deteriorating component's strength and the health status of component are modeled as stochastic process. Hence, Our approach predicts the system's remaining useful life and demonstrates how the availability of a complex system is affected by its constituent components. Through numerical example, we demonstrate that failure interactions impacts prognostics results and these impacts will be intensified as the degradation interactions rate increases.

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