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Alicia Moya, Jordi Creus, Nuria Romero, José Alemán, Xavier Solans-Monfort, et al.. Organocatalytic vs. Ru-based electrochemical hydrogenation of nitrobenzene in competition with the hydrogen evolution reaction. Dalton Transactions, 2020, 49 (19), pp.6446-6456. 10.1039/D0DT01075H . hal-02612766

HAL Id: hal-02612766

<https://hal.science/hal-02612766>

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ARTICLE

Organocatalytic vs Ru-based Electrochemical Hydrogenation of Nitrobenzene in Competition with Hydrogen Evolution Reaction

Received 00th January 20xx,
Accepted 00th January 20xx

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DOI: 10.1039/x0xx00000x

Oxidized carbon fibres and ruthenium nanoparticles supported on unmodified carbon fibres have been studied for electrocatalytic PhNO₂ hydrogenation. While similar reaction outputs have been observed for both catalytic systems, DFT calculations revealed some significant differences on the reaction pathways related to distinct interactions of the catalytic materials with substrates or products. Furthermore, although PhNO₂ hydrogenation is the favoured reaction, HER competes in both systems under the catalytic conditions.

Introduction

Electrochemical reduction of organic substrates is not only an important synthetic method but also, an efficient way to remove persistent pollutants^{1–3} and to produce energy vectors based on reversible hydrogenation/dehydrogenation processes.^{4–6} Such processes, when carried out in the presence of proton sources, require electrocatalysts able to hydrogenate organic functionalities.⁷ Such electrocatalytic materials are intended to increase both the activity and selectivity of the reduction reaction. Regarding the selectivity, the occurrence of Hydrogen Evolution Reaction (HER) as a parasite process in competition with the hydrogenation of organic reagents is ubiquitously observed.⁸ The characteristics of the electrocatalytic materials are expected to determine the reaction output, tipping the balance in favour of one or another process. The rational design of materials able to electrocatalytically hydrogenate organic substrates or efficiently mediate HER requires a deep understanding of the mechanisms underlying both pathways. Regarding the mechanism of HER, it has been studied by using a wide range of materials due to the need of clean and renewable alternatives to the use of fossil fuels.^{9–11} Pt-based catalysts are known to be highly performant for HER, but due to economic concerns, its substitution by catalytic materials based on cheaper and earth-abundant elements is necessary.^{12–15} Metal-free catalysts, such

as carbon-based materials^{16,17} as well as Ru-based catalysts^{18–20} seem to be ideal alternatives for this purpose.

In a recent report, we applied carbon microfibres (CFs) prepared by the pyrolysis of polyacrylonitrile (PAN) as an alternative electro-organocatalytic material for HER (Fig. 1a, top).²¹ Carbon fibres have a graphene-like structure including pyridyl moieties. This carbon-based material can be easily oxidized to generate carboxylic acid groups at the surface, constituting nicotinic fragments in the carbon fibre structure. The resulting material that will be further referred as ox-CF presents HER electrocatalytic activity. Indeed, ox-CF can act as catalytic centres for the HER in way similar to those of NADPH in biological systems^{22,23} and Hantzsch esters in synthetic reduction procedures.^{24–26} In another work, we used pristine CFs as support for Ru-NPs in order to achieve stable and high surface area functionalized electrodes (Fig. 1a, bottom).²⁷ Our results demonstrated the viability of such hybrid materials composed by Ru-NPs onto CF as remarkable electrocatalysts for the HER (referred as Ru-CF). A common feature of both systems (ox-CF and Ru-CF) is the generation of hydride species that can be protonated to form molecular hydrogen. Also, they can hydrogenate a variety of substrates, widening the applicability of electrochemical systems usually employed for HER. Furthermore, electrocatalytic procedures are convenient strategies, avoiding the manipulation of H₂ gas or metal hydride derivatives (LiAlH₄ or NaBH₄), commonly used in chemical hydrogenation processes.

In this work, we compared the electrocatalytic HER and the hydrogenation of a model substrate, namely nitrobenzene (PhNO₂), using as electrocatalysts functionalized carbon fibres (ox-CF and Ru-CF) (see Fig. 1b). The reduction of PhNO₂ is of great interest since nitro aromatic compounds (such as explosives, dyes, agrochemicals or pesticides) are common water contaminants.^{28,29} Although many alternatives have been explored,^{30–35} electrochemical procedures are still the most convenient ways to reduce PhNO₂ and thus potentially degrade pollutants containing this fragment. However, in the presence

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† Electronic Supplementary Information (ESI) available. See

DOI: 10.1039/x0xx00000x

a) Previous work: Carbon Fiber-based Electrocatalyst for HER

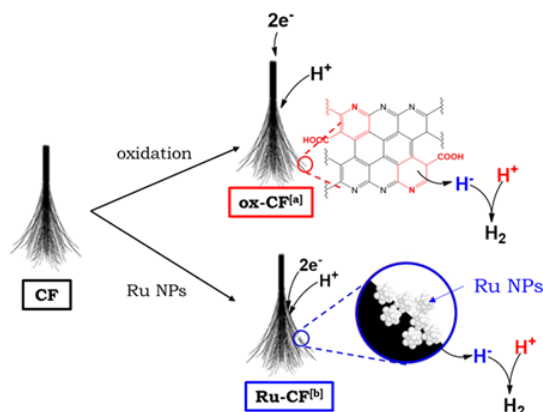
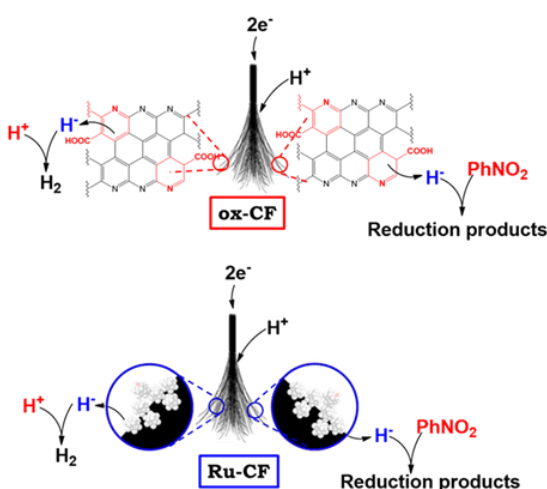
b) This work: Electrocatalytic HER vs PhNO₂ Reduction

Fig. 1 Schematic representation of a) Carbon Fibre-based electrocatalysts for HER (previous work)^{21,27} and b) HER vs hydrogenation of PhNO₂ using same electrocatalysts (this work).

of protic media this process would typically be in competition with HER. Indeed, electrochemical reduction of nitrobenzene is often performed using a platinum electrode which is also a typical electrocatalyst for HER.^{36–38} Currently, electrodes used for the electroreduction of aromatics are based on noble metals, which limit their applicability for large scale processes given their high cost and low abundance.³⁹ Thus, there is a need to find efficient, inexpensive, easy to make and recyclable electrocatalytic materials with no noble metals^{40,41} for the reduction of nitroaryl compounds. This reaction will be deeply presented in this manuscript, considering HER as a competitive process. We will determine the intrinsic properties of ox-CF and Ru-CF as electrocatalysts for both reactions (compare Fig. 1b top and bottom) by means of combination of experimental and theoretical results. This work will add fundamental understandings on the distinctive catalytic behaviour of metal-based and metal-free electrocatalysts. The obtained fundamental insights may allow the future design of active and selective electrocatalytic materials for HER or hydrogenation of organic substrates.

Results and discussion

Experimental Results

Details on synthesis and characterization of the electrocatalytic materials used in this comparative study are reported elsewhere.^{21,27} Previous mechanistic studies revealed that both, ox-CF and Ru-CF, generate hydrides, that after protonation, lead to HER. Then, the question is to determine if these systems are capable to transfer the hydride to nitrobenzene. Although the productivity typically formed from this process is simply aniline, several other species can be generated. Therefore, as previously reported, a more complex mechanism should be considered for hydrogenation of nitrobenzene (see Fig. 2).⁴²

The electrochemical behaviour of nitrobenzene has been analysed by cyclic voltammetry (Fig. S1). A reduction signal is observed at $E_{1/2} = -1.1$ V vs Ag/AgCl, which is associated to a reversible electron transfer process. According to this result, -1 V vs Ag/AgCl has been chosen as the limit potential for all electrochemical experiments in order to achieve electrocatalytic hydrogenation and avoid electrochemical electron transfer. The choice of an adequate proton source is determinant for the efficiency of the reaction. Also, in order to understand such effect, some factors have to be considered: 1) Electrocatalytic hydrogenation of nitrobenzene will compete with HER and 2) Hydride regeneration on the catalytic centres involves injection of two electrons into the electrocatalytic material and further protonation. Combination of both factors will determine the effect of the proton source in the output of the electrocatalytic PhNO₂ hydrogenation. In order to optimize the composition of our system we compared linear sweep voltammetry results of ox-CF and Ru-CF using water (1 M), trifluoroacetic acid (TFA, 20 mM) and a mixture of both as proton sources (Fig. S2) in acetonitrile. Maximized electrochemical response is observed for both catalytic systems when a mixture of water and TFA is used. Fig. 3 presents the linear sweep voltammeteries recorded in the absence (top) and in the presence (bottom) of nitrobenzene at a scan rate of 10 mV/s. Measurements were performed in acetonitrile using NaClO₄ (0.2 M) and TFA (20 mM) and water (1 M) mixture.

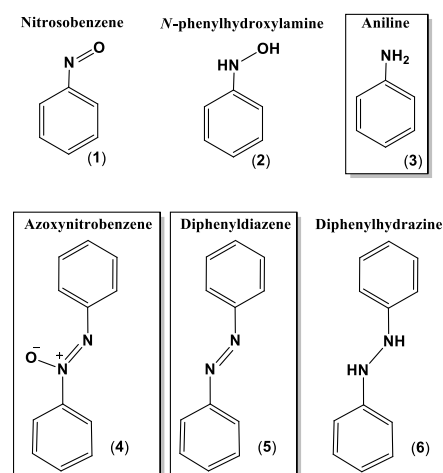


Fig. 2 Possible species that can be generated from hydrogenation of nitrobenzene with species detected in this work highlighted inside the frames.

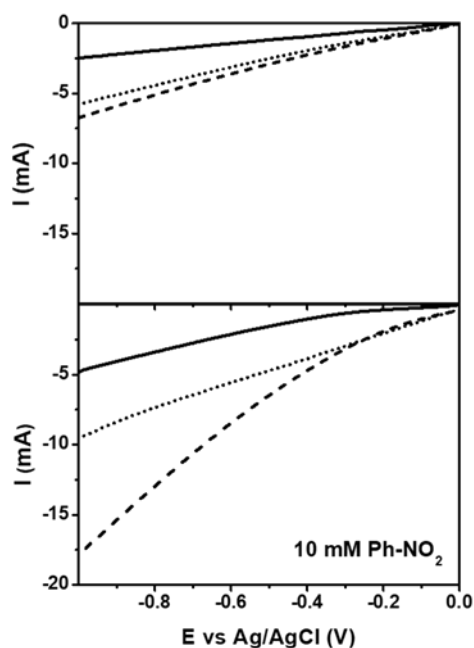


Fig. 3 Linear sweep voltammograms measured using pristine (solid line), oxidized (dashed line) and Ru-based (dotted line) carbon fibre electrodes in the absence (top) and in the presence (bottom) of 10 mM of nitrobenzene. In all cases, solvent is acetonitrile containing H₂O (1 M), TFA (20 mM) and NaClO₄ (0.2 M).

The current intensity values at -1 V vs Ag/AgCl are presented in Table 1 for comparison purpose. Electrochemical responses of the two materials studied (ox-CF and Ru-CF) are much higher than that of the pristine fibre (CF), which demonstrates their catalytic properties, either for the proton reduction or for the nitrobenzene hydrogenation (see -2.48 vs -6.76 and -5.77 mA; -4.85 vs -17.89 and -9.31 mA). Current intensity is greatly enhanced upon addition of PhNO₂ when using ox-CF (see -6.76 vs -17.89 mA). However, such an effect is less pronounced for the Ru-based electrocatalyst (see -5.77 vs -9.31 mA). PhNO₂ hydrogenation is clearly facilitated with the purely organic electrocatalyst while with the Ru-CF inorganic catalyst, HER seems to compete more with the nitrobenzene hydrogenation.

Then, a 5 h electrolysis has been performed at a constant potential of -1 V vs Ag/AgCl for the two electrocatalysts in the presence of water and TFA mixture (Fig. S3). The reaction outputs have been analysed by gas chromatography (GC). Interestingly, higher conversion was found for oxidized carbon fibres (Fig. 4a), as expected from the current observed in the LSV. It is important to note that the concentration of active sites is hard to determine. However, the activity observed cannot be uniquely related to the intrinsic properties of the active sites but also to their relative concentration on the electrode surface.

Table 1 Current intensities at -1 V vs Ag/AgCl in 1 M H₂O + 20 mM TGA corresponding to the linear sweep voltammograms of Fig. 3.

[PhNO ₂] (mM)	I of CF (mA)	I of ox-CF (mA)	I of Ru-CF (mA)
0	-2.48	-6.76	-5.77
10	-4.85	-17.89	-9.31

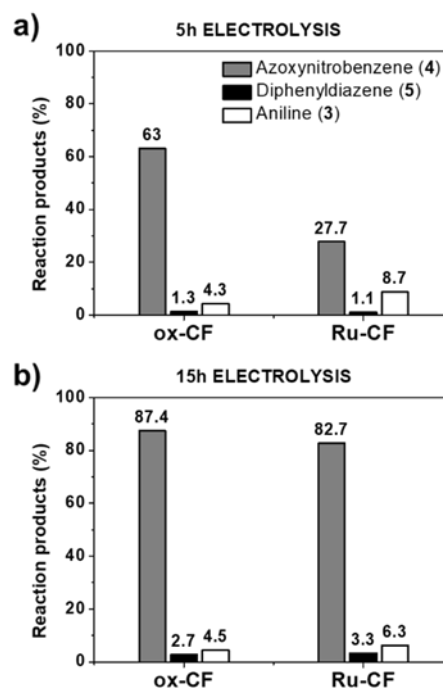


Fig. 4 Reaction products of the electrocatalytic reduction of nitrobenzene at -1 V vs Ag/AgCl after a) 5 h and b) 15 h of reaction using ox-CF and Ru-CF as electrodes in a mixed solution of 1 M of water and 20 mM of TFA in NaClO₄ (0.2 M, acetonitrile).

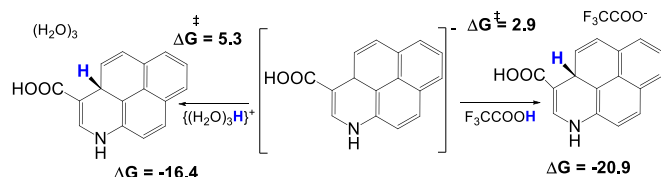
Furthermore, we investigated the reaction output after a longer reaction time (5 vs 15 h, Fig. 4a and 4b). After 15 h, the consumption of nitrobenzene is almost complete for both electrocatalytic materials. The pristine carbon fibre electrode was also tested for 5 h. In these conditions, no significant amounts of products were found, corroborating that the catalytic behaviour observed with the two other materials results from either the oxidation of carbon fibres or the presence of Ru-NPs (Fig. S3).

As shown on Fig. 4 and S4, the major product of the nitrobenzene reduction after bulk electrolysis at -1 V during 5 and 15 h, is in all cases azoxy nitrobenzene dimeric species (4). In addition, residual amounts of aniline (3) and diphenyldiazene (5) have been observed. Interestingly, amounts of aniline (3) at 15 h are equal or even lower than those detected at 5 h. In contrast, as observed for the major product (4), amounts of the minor product diphenyldiazene (5) are significantly superior at 15 h than at 5 h. These observations indicate that, a) the generation of aniline (3) corresponds to short reaction times, b) the formation of dimeric species (4 and 5) requires accumulation of monomeric intermediates that are produced over the electrochemical process, thus requiring longer reaction times. Remarkably, although the nature of the two catalytic systems studied is very distinct, similar product compositions are observed. However, faradaic yields after 15 h electrolysis are approximately 75% for ox-CF and 65% for Ru-CF, thus indicating that HER is a minor process but is more significant for Ru-CF, in agreement with voltammetry data (see Fig. 3).

Theoretical Calculations

Methodological Strategies. In order to get a deep understanding of the processes occurring in the electrocatalysis, we performed a computational DFT study. Two sets of calculations were carried out. The full catalytic process involving the organocatalytic system (ox-CF) was represented with a molecular model from a previous work.²¹ The hybrid M062X functional⁴³ was used and atoms were represented with the 6-311G** basis sets⁴⁴ including solvation effects of acetonitrile ($\epsilon = 37.5$) by means of solvation model density (SMD).⁴⁵ The protonation steps of the PhNO₂ hydrogenation were studied also at this level of theory without including any of the two catalysts in the calculations. The reactivity of Ru-NPs was studied with VASP.^{46,47} For saving computational time, the exploration was limited to the thermodynamics of all steps and the transition states that appeared to be key for the organocatalytic system. VASP includes periodic boundary conditions and defines the basis with plane wave. Thus, interaction with neighbour images was avoided by using a 25 Å edge cubic unit cell. These calculations were performed with the PBE GGA functional⁴⁸ and an energy cut-off of 500eV. Dispersion forces were taken into account with Grimme D2 empirical correction⁴⁹ (see Computational Details section for further information). Remarkably, values for the Ru-NPs do not include thermal corrections. However, since all steps are unimolecular, ΔE and ΔG values are expected to show little variations. In any case, it is worth to note that since the methodologies used for modelling the two catalytic processes differ significantly, comparison should be done with caution, particularly for the case of the energy barriers as it is well-known that PBE tends to underestimate them.⁵⁰

Initial Considerations. As reported previously,²¹ the electro-organocatalytic behaviour of oxidized carbon fibres is initiated by the injection of two electrons on the carbon material that contains randomly distributed nicotinic fragments. It is known that the value for the work function of highly orientated pyrolytic graphite (HOPG) in air is c.a. 4.8 eV,⁵¹ which is expected to be close to that of the carbon fibre material. Thus, it should allow stabilization of injected electrons through the graphitic π -electron density. However, considering the reduced size of the molecular model used in our calculations to simulate the graphenic region, the stabilization energy after injection of two electrons (3.13 eV) is underestimated. After injection of two electrons model, the negative charge increases the basicity of the pyridinic nitrogen atom resulting in its barrierless protonation. Thus, we considered as the starting point the negatively charged species shown in Scheme 1 (centre) that contains a protonated pyridinic nitrogen atom. Further



Scheme 1 Generation of the species able to transfer hydrides in the ox-CF organocatalytic system (energy values are given in kcal mol⁻¹).

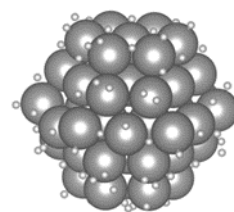


Fig. 5 Ru₅₇H₈₈ model used for representing the Ru-NPs.

evolution of this reduced species consists in its protonation in the *para*-position with respect to the nitrogen atom.

The corresponding species can transfer the hydride that is responsible for the observed reactivity. Taking into account the nature of the reaction medium, we considered two possible protonation agents: TFA molecule and hydrated proton [H₃O(H₂O)₃]⁺. Very similar results were found using both species, being slightly more favourable the protonation with TFA ($\Delta G = -20.9$ kcal mol⁻¹; $\Delta G^\ddagger = 2.9$ kcal mol⁻¹) than with [H₃O(H₂O)₃]⁺ ($\Delta G = -16.4$ kcal mol⁻¹; $\Delta G^\ddagger = 5.3$ kcal mol⁻¹).

In order to study the processes mediated by Ru-NPs, we used a model that includes 57 ruthenium (44 at the surface) and 88 hydrogen atoms (Ru₅₇H₈₈, Fig. 5). We considered this structure as a good representation of the active species generated under reductive potentials in acidic media, able to act as an efficient hydride transfer agent. The model choice and the number of hydrogen atoms is based on Comas-Vives *et al.* results.⁵² Their work showed that this model is a good compromise between accuracy and computational cost and that the number of hydrogen atoms per surface ruthenium is close to the double of surface ruthenium atoms in pristine nanoparticles.

Hydride Transfer to PhNO₂ vs Hydride Protonation. Once the active species able to perform hydride transfer processes are generated, two potential reactions can take place: hydride transfer to nitrobenzene and HER. Fig. 6 shows the comparison of the kinetics and thermodynamics of these processes in presence of model systems for a) ox-CF and b) Ru-CF. Fig. 7 shows some optimized structures.

Regarding the reactivity in presence of the ox-CF, calculations show that the hydride transfer to PhNO₂ is slightly endothermic ($\Delta G = +3.6$ kcal mol⁻¹) but this is clearly compensated by the subsequent protonation of PhNO₂H, which leads to PhNO (**1**) and a water molecule (origin of the exothermicity; $\Delta G = -108.9$ kcal mol⁻¹). The competitive H₂ formation is also thermodynamically favourable both from TFA and hydronium type molecule [H₃O(H₂O)₃]⁺, obtaining computed ΔG values of -11.6 and -6.2 kcal mol⁻¹, respectively. From a kinetic point of view, the hydride transfer to PhNO₂ is favoured with respect to HER by at least 9.2, kcal mol⁻¹. HER reaction is more favoured when TFA is used as proton source. These results are in accordance with the high faradaic yields found for nitrobenzene reduction (see above).

Nitrobenzene hydrogenation and H₂ formation on Ru-NPs start with the adsorption of the reacting substrates to the

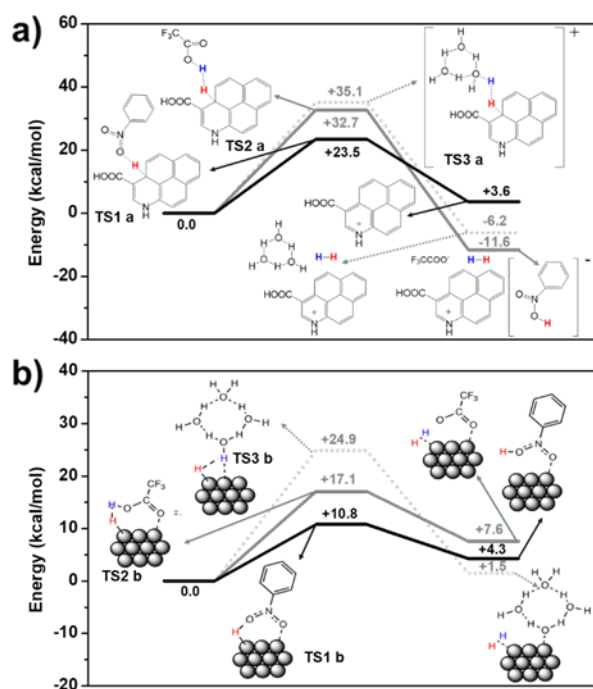


Fig. 6 Comparison of energetics for the hydride transfer to PhNO₂ (black line) and HER (grey lines) using a) ox-CF and b) Ru-CF electrocatalytic models. Hydride protonation can be carried out by TFA (solid grey line) or by [(H₃O)(H₂O)₃]³⁺ (dashed grey line). Energies are given in kcal mol⁻¹.

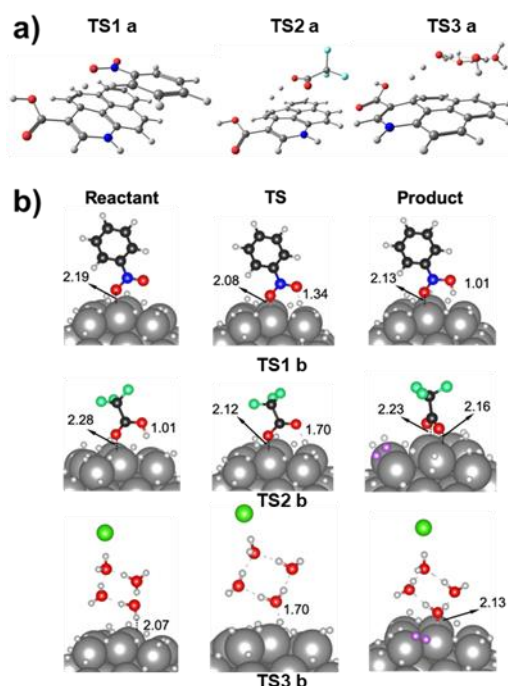
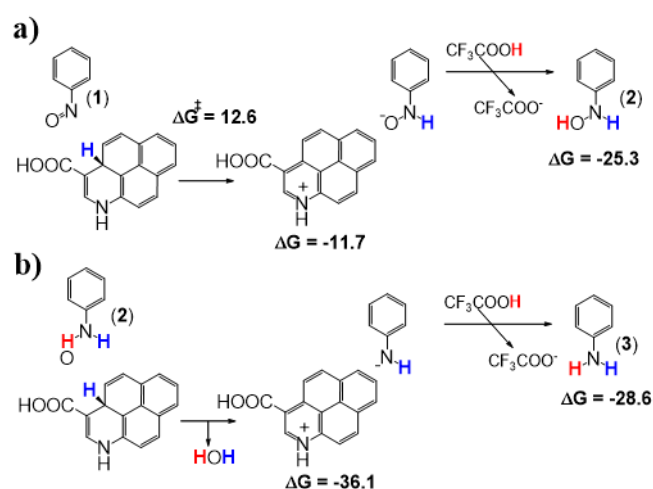


Fig. 7 Optimized structures found for PhNO₂ hydrogenation and HER using TFA and hydronium ion as source of protons: a) transition states shown in Figure 6a for ox-CF model system and b) the starting materials, transition states and final products using Ru-CF as catalytic model system as shown in Figure 6b. Distances are given in Å.

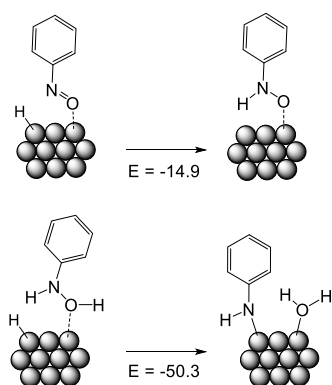
nanoparticle surface (Table S2). This adsorption is more favourable for nitrobenzene and TFA than for hydronium ion [H₃O(H₂O)₃]³⁺ due to the formation of Ru...O interactions (see S.I. for further details). As found for the carbon fibres, the hydride

transfer to the adsorbed nitrobenzene is slightly unfavourable ($\Delta E = 4.3$ kcal mol⁻¹), but the high exothermicity of the protonation step makes the formation of PhNO + H₂O largely favourable. The energy barrier for the hydride transfer to the adsorbed PhNO₂ species is computed to be 10.8 kcal mol⁻¹, thus suggesting it is kinetically easy. The hydride protonation in presence of Ru-NPs is easier when involving TFA than [(H₃O)(H₂O)₃]³⁺. The energy barrier is computed to be 17.1 kcal mol⁻¹ from adsorbed TFA. This value is higher than that computed for the PhNO₂ hydride transfer. The energy difference between the two processes is slightly smaller than for the oxidized fibres, indicating that HER (which is in both cases kinetically less favoured) could be a better competing reaction when using Ru-CF rather than when using ox-CF. These results agree with the experimentally measured faradaic yields for the two systems. A potential explanation of the large difference between the HER energy barriers when involving TFA and [(H₃O)(H₂O)₃]³⁺ could derive from the nature and the strength of the substrate-Ru-NP interaction. Indeed, the Ru...O interaction increases the acidity of TFA favouring the hydride protonation.

From PhNO (1) to PhNH₂ (3). Evolution of PhNO species formed from the first hydrogenation process (hydride transfer + protonation) to aniline consists of two consecutive hydrogenation steps (Scheme 2). Every hydrogenation step has been considered as an initial hydride transfer with a non-negligible energy barrier, followed by the protonation process, which is generally very exothermic, mainly barrier-less and does not involve the electrocatalyst. The hydride transfer to PhNO (1) results in deprotonated hydroxylaniline. This process is exothermic in presence of ox-CF by -11.7 kcal mol⁻¹. Moreover, the energy barrier is low ($\Delta G^\ddagger = 12.6$ kcal mol⁻¹) which indicates that the process is kinetically favourable (Scheme 2a). In addition, the protonation of deprotonated hydroxylaniline is also very favourable, suggesting that once PhNO (1) is formed, it easily evolves to PhNH₂ (2).



Scheme 2 Catalytic evolution of PhNO (1) consisting in two consecutive hydrogenation and protonation steps: a) forming hydroxylaniline (2) and b) aniline (3). Energy values are given in kcal mol⁻¹.



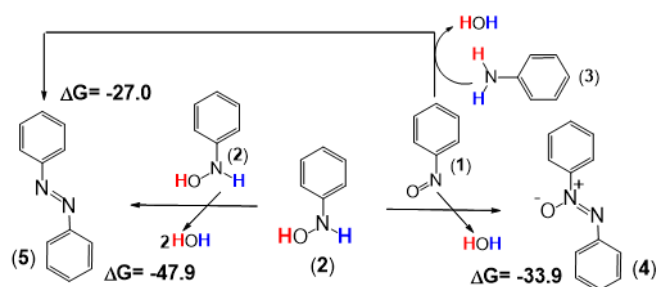
Scheme 3 Catalytic evolution of Ph-NO to aniline through two successive hydrogenation/protonation steps with Ru-NPs. Energies in kcal mol⁻¹

Calculations for the second hydrogenation step indicate that hydride transfer to the OH group of hydroxylaniline to generate a water molecule and deprotonated aniline is very exothermic (-36.1 kcal mol⁻¹, Scheme 2b). In this case, transition state has not been located, indicating that this reaction is barrierless or proceeds through a very shallow barrier. Further protonation of deprotonated aniline is very favourable. Consequently, nitrobenzene hydrogenation (Fig. 6) seems to be the rate-determining step. Once PhNO (**1**) is generated, its reduction to aniline (**3**) should consecutively occur.

With the aim of analysing if these two steps are also straightforward in presence of Ru-NPs, we computed the corresponding reaction energies. Results are reported in Scheme 3 and show that PhNO (**1**) hydrogenation is similar to that found for the ox-CF and it is favourable by -14.9 kcal mol⁻¹. On the other hand, the hydrogenation of PhNHOH shows larger differences. The resulting products are the same for the two catalytic systems. However, the strong Ru-NPs-H₂O interaction and the Ru-PhNH makes the reaction even more exothermic ($\Delta E = -50.3$ kcal mol⁻¹). The ability of Ru-NPs to coordinate the reacting substrates changes the thermodynamics in comparison with the ox-CF system. In any case, the initial PhNO₂ hydrogenation to PhNO (**1**) appears to be the more challenging step also when using Ru-NPs (Fig. 6b).

Overall, calculations suggest that aniline (**3**) should be easily formed with the two catalytic systems. However, according to the experimental data, aniline (**3**) is only a minor product detected in the reaction outcome. Justification of this observation is found in the next section.

Dimerization process. Since the major product observed in the electrolysis experiments (see Experimental Results section above) is the dimeric compound azoxynitrobenzene (**4**), we decided to evaluate the thermodynamics of its formation from the reaction of nitrosobenzene (**1**) and hydroxylaniline (**2**) intermediates. Effectively, condensation of such compounds is highly favoured, as it should be expected for the formation of a water molecule, which serves as an efficient driving force of the process (Scheme 4). Thus, while hydroxylaniline (**2**) is slowly being generated, it efficiently reacts with the excess of nitrosobenzene (**1**) to generate the main final product of this electrocatalytic system, azoxynitrobenzene (**4**).



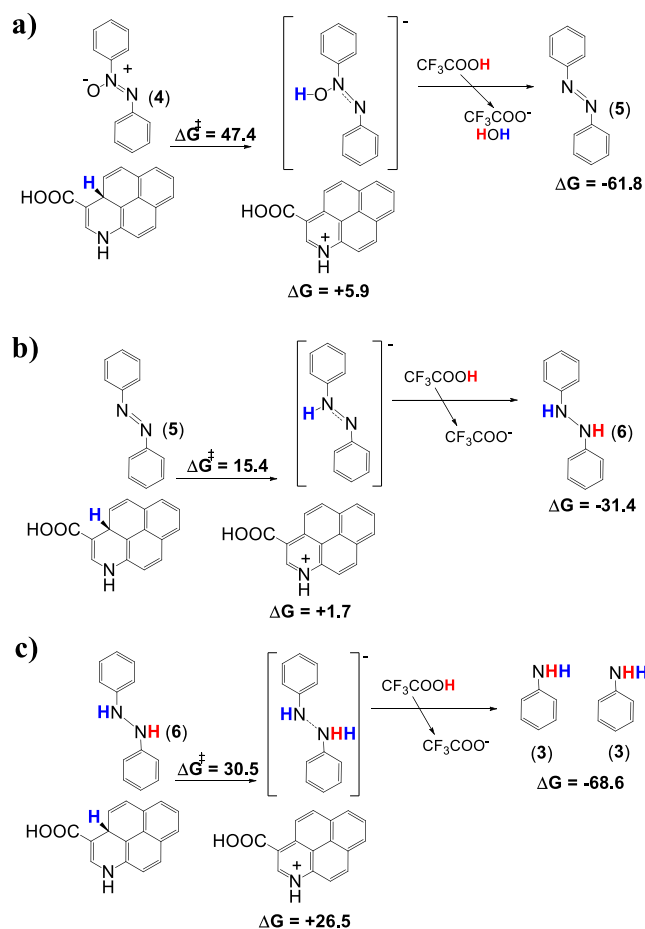
Scheme 4 Dimerization processes towards formation of azoxynitrobenzene (**4**) and azobenzene (**5**) (energy values are given in kcal mol⁻¹).

Furthermore, formation of the diazo compound (**5**) that has been detected in residual amounts can be explained by the dimerization of two hydroxylaniline (**2**) molecules (Scheme 4). Considering that during the reaction, hydroxylaniline (**2**) coexists with an excess on nitrosobenzene (**1**), this alternative process is less probable, which agrees with the residual amounts of such species experimentally detected. Finally, condensation of aniline and nitrosobenzene (**1**) could also account for the formation of the diazo compound (**5**), which could be responsible for the disappearance over time of aniline (**3**).

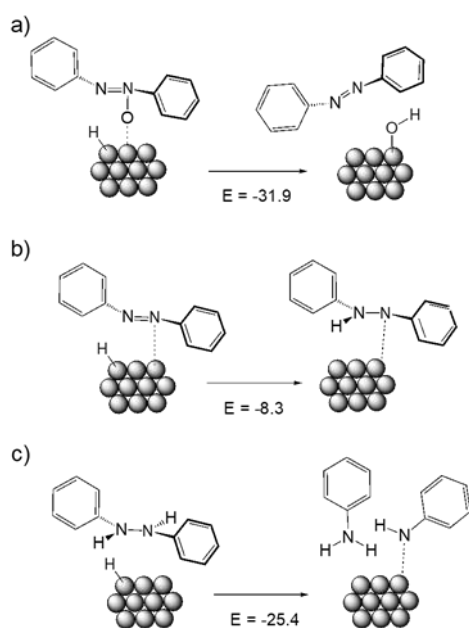
Dimerization processes require significant concentrations of monomer species. Therefore, at short reaction times, when concentration of products is still low, direct formation of aniline is plausible through the three consecutive hydrogenation steps presented above. However, after longer electrolysis, concentration of products increases, and dimeric structures can appear through exothermic condensations. Thus, aniline is expected to be formed at short reaction times as indeed experimentally observed (Fig. 4). It is also in good agreement with the experimental observation that both dimeric products are produced at longer reaction times. The fact that the major product found is the azoxynitrobenzene (**4**) species indicates that its hydrogenation is unfavourable as is demonstrated in the next section.

Evaluation of possible evaluation of azoxynitrobenzene (4**).** The hydride transfers to azoxynitrobenzene (**4**) and to the other dimeric species (diphenyldiazene (**5**) and diphenylhydrazine (**6**)) involving the two catalytic systems are summarized in Schemes 5 and 6. With ox-CF, the hydride transfer to azoxynitrobenzene (**4**) (Scheme 5a) is endothermic ($\Delta G = +5.9$ kcal mol⁻¹) and the computed Gibbs energy barrier ($\Delta G^\ddagger = 47.4$ kcal mol⁻¹) indicates that the process is highly kinetically hampered. This suggests that azoxynitrobenzene (**4**) would hardly be hydrogenated, even though protonation of the resulting product to form a water molecule and the diazo compound is highly exothermic. This agrees with azoxynitrobenzene (**4**) being the major product of nitrobenzene hydrogenation, the small portions of diazo compound observed experimentally being likely formed by the dimerization processes.

The potential formation of aniline from the diazo compound (**5**) in presence of ox-CF has also been considered (Scheme 5b and 5c). The obtained results indicate that under the reaction conditions, diphenyldiazene (**5**) would easily evolve to diphenylhydrazine (**6**). Finally, the hydride transfer to this hydrazine derivative (**6**) intermediate leading to aniline



Scheme 5 Catalytic evolution of hydrogenation of azoxynitrobenzene towards a) the diazo compound, b) the diphenyl hydrazine product and c) aniline (energy values are given in kcal mol⁻¹).



Scheme 6 Azoxynitrobenzene conversion to aniline through three successive hydrogenation/protonation steps with Ru-NPs. Energies in kcal mol⁻¹

formation is very endothermic ($\Delta G = +26.5$ kcal mol⁻¹) and kinetically hampered ($\Delta G^\ddagger = 30.5$ kcal mol⁻¹, Scheme 5c).

Therefore, although further protonation is calculated to be very exothermic, hydrogenation of diphenylhydrazine (6) does not seem to be the path for the formation of aniline (3). Indeed, the observed aniline is expected to be formed by successive hydrogenation of PhNO₂ without dimerization, while the major dimeric product is azoxynitrobenzene (4), which presents the highest hydride transfer Gibbs energy barrier. The reactivity of azoxynitrobenzene (4) with the Ru-CF has also been explored, considering the thermodynamics of the three potential hydrogenation steps (Scheme 6a to 6c) as well as the transition state for the hydride transfer to azoxynitrobenzene (4), which appeared to be a key step in the organocatalytic system. Fig. 8 shows the optimized structures of azoxynitrobenzene (4), diphenyldiazene (5) and the transition state connecting these two intermediates.

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The hydrogenation pathways found for azoxynitrobenzene (4) using Ru-CF are significantly different than those calculated for ox-CF. As observed for the hydrogenation of Ph-NHOH (2), the resulting products (PhNNPh + Ru-NPs-OH) using Ru-CF are the consequence of the formation of a Ru-OH bond at the nanoparticle surface. Remarkably, despite the large exothermicity of the reaction ($\Delta E = -31.9$ kcal mol⁻¹), the computed energy barrier is high (+24.9 kcal mol⁻¹) due to the large electronic reorganization to favour the concerted formation/cleavage of the Ru...O and N...O bonds. Moreover, the two subsequent hydrogenation steps are thermodynamically favourable (Scheme 6), indicating that aniline formation from azoxynitrobenzene (4) is thermodynamically feasible. However, as in the case of ox-CF, this is not expected to be the main route for aniline formation. This is due to the large energy barrier of the hydride transfer to azoxynitrobenzene (4), which should be the major dimeric species, as found experimentally.

Summarizing, calculations on the evolution of azoxynitrobenzene (4) suggest that this species could hardly be

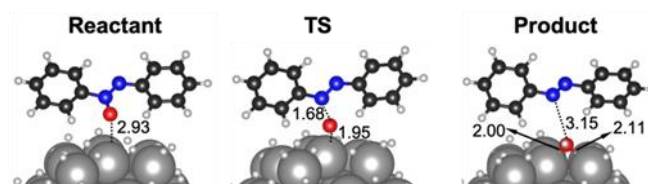
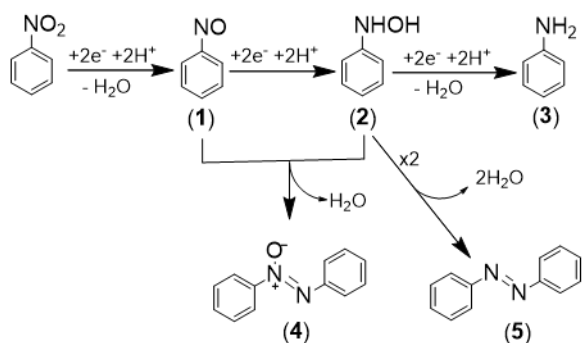


Fig. 8 Optimized structures for azoxynitrobenzene intermediate adsorbed on H₈₈Ru₅₇ nanoparticle, the diphenyldiazene resulting from its hydrogenation and the transition state connecting them. Distances in Å and energies in kcal mol⁻¹



Scheme 7 General scheme for the nitrobenzene reduction reaction proposed for the two electrocatalytic approaches studied.

reduced regardless the nature of the electrocatalyst. Thus, despite the different reactivity expected for ox-CF and Ru-CF, the chemical identity of the final products should not vary, being azoxynitrobenzene (**4**) the major product.

Overall, our calculations show a reaction mechanism for the nitrobenzene hydrogenation that is consistent with the experimental data. Despite the different reactivities observed for the two electrocatalysts for some particular steps, the mechanisms for the two systems share the main general issues, which are summarized in Scheme 7: nitrobenzene is hydrogenated following a first 2-electron and 2 proton transfer steps leading to the formation of nitrosobenzene (**1**), which is converted to hydroxylamine (**2**) following a further 2-electron and 2 protons reduction. While this species is being formed two processes can occur: a) further hydrogenation until aniline product (**3**) (which is detected in low amounts) or b) condensation with nitrosobenzene (**1**) to produce azoxynitrobenzene (**4**) (which is observed as main product). This dimeric species cannot be further reduced, appearing as the final product. In addition, residual amounts of diazo compound (**5**) found in the reaction outcome seems to be the result of dimerization of residual amounts of hydroxylamine (**2**) or the recombination of aniline (**3**) and nitrosobenzene (**1**). Controversially, according to our theoretical data, diazo species (**5**) should be easily reduced to hydrazine compound, which should accumulate because its further reduction is unfavourable. However, the known high reactivity of hydrazine compounds can account for its further evolution being impossible its detection under the working conditions.

Conclusions

The conclusions section should come in this section at the end of the article, before the acknowledgements. Two electrocatalytic systems of very different nature result on comparable outputs for PhNO₂ hydrogenation, which is kinetically favoured with respect to HER. Some subtle differences can be distinguished from our results. Combination of experimental results and DFT calculations indicates that HER is a more significant competitor when Ru-CF are used as catalyst. Theoretical calculations also show that Ru-CF is intrinsically more reactive than the organocatalytic system (ox-

CF). However, this trend is not necessarily observed experimentally as the concentration of active centres on the electrode surface may significantly vary.

The main product experimentally observed for nitrobenzene hydrogenation is the azoxynitrobenzene dimeric species, while aniline is formed in minor quantities during the first stages of the electrocatalytic process. However, according to DFT results, once the initial hydrogenation rate determining step occurs (from PhNO₂ to PhNO), successive hydrogenation steps to generate aniline (from PhNO to PhNH(OH) and from PhNH(OH) to PhNH₂) are highly favoured. In parallel to aniline formation, dimeric azoxynitrobenzene compound is generated as a consequence of the highly favourable condensation of PhNO and PhNH(OH).

Overall, this work presents an in-depth understanding of the catalytic behaviour of an organic- and a metal-based material that previously have been used as electrocatalysts for HER. In contrast, we have shown how hydrogenation of PhNO₂ efficiently competes with HER. Thus, the methodology reported herein can be applied to the electrochemical remediation of an important class of pollutants (nitro aryl compounds). In a more general perspective, these insights may contribute to the future designs of more efficient catalytic systems for hydrogen production, electrochemical waste-water treatments or use of hydrogenation/dehydrogenation based energetic vectors.

Experimental

Materials

All reagents, solvents and materials were purchased from commercial sources and used without further purification. Specifically, fabric of carbon fibre (Twill 2x2 3K weight 200 g/m² width 1200 mm, Model HA2301) was purchased from ClipCarbono.

Electrode Preparation

The commercial carbon fibre is prepared in a 6 cm long bunch of fibres. Then, it is joined to a copper wire and tight with a Teflon tape. The hand-made electrodes are modified using two different approaches, namely: 1) oxidative treatment of the carbon fibre and 2) ex-situ deposition of Ru-NPs. For the oxidized CF brushes, they are treated 30 minutes with sulfuric acid (98%) at room temperature with stirring and later they are immersed into a mixture 1:1 of H₂SO₄/H₂O₂. The mixture should be freshly prepared to obtain its stronger oxidative potential and thus, be able to oxidize the carbon fibre. Finally, the electrodes are washed and sonicated in distilled water to neutralize its surface, later washed in ethanol and dried with a heat gun. Characterization of this material was previously reported and confirms that the oxidation process changes the chemical features of the CF surface (generation of carboxylic groups, transforming pyridinic fragments into nicotinic ones) whereas keep its bulk properties and morphology.²¹ For the Ru-based CF, 2 cm of CF electrodes were soaked overnight in a THF (10 mL) crude dispersion of RuPP NPs^{27,53} inside a Fisher-Porter bottle under an Ar atmosphere. Then, the supernatant was

removed through cannula and the resulting CF materials were rinsed with pentane (3x10 mL) and dried under vacuum. RuPP@pCF. TEM: $\varnothing = 1.8 \pm 0.3$ nm. ICP(Ru%): 0.47%.

Electrochemistry

Electrochemical experiments were performed under an argon atmosphere at room temperature in CH_3CN . Sodium perchlorate (NaClO_4) was used as supporting electrolytes. Measurements were carried out using an Ivium CompagStat potentiostat interfaced with a computer. A standard three-electrode electrochemical cell was used with Ag/AgCl reference electrode. The working electrode was carbon fibre brush: pristine, oxidized and modified with inorganic nanoparticles. The counter electrode was a pristine carbon fibre brush.

Gas Chromatography

The evolution of the nitrobenzene during the electrocatalytic reaction was monitored by gas chromatography, by injecting samples of the intern atmosphere to an Agilent 7820A GC system equipped with a mass spectroscopy detector (5977B MSD). For gas chromatography quantification of nitrobenzene and its derivatives, the solvent of the working electrode solution is reduced at low pressure and then it is solved with 1 mL of CHCl_3 which is able to solve the nitrobenzene and its derivatives but not the inorganic salt of the electrolyte. An aliquot of 0.2 mL of the solution is mixed with 0.2 mL of methyl naphthalene as standard. A calibrate of nitrobenzene, nitrosobenzene, azoxynitrobenzene, diphenylazobenzene and aniline was carried out enabling the quantification of the products.

Computational Details

The main text of the article should appear here with headings. Quantum chemistry calculations were carried out using the density functional theory (DFT). For the organocatalytic system, geometry optimizations were performed using the M06-2X functional⁴³ in combination with the 6-311G(d,p) basis set.⁴⁴ Solvent effects were included with the solvation model density (SMD)⁴⁵ and considering acetonitrile ($\epsilon = 37.5$) as solvent. Graphitic surface was modelled using a fragment composed by 4 fused aromatic rings (1 pyridine + 3 benzenes) as a compromise between performance and computational cost. We introduced a carboxylic group in the meta position versus pyridine nitrogen. All optimizations were performed without any geometrical constraint and harmonic vibrational frequencies have been also evaluated at the same level of theory to characterize minima and transition states in the potential energy surface. Transition states have been connected to products by optimization of geometries slightly modified from the transition states. All the calculations were performed using the Gaussian09 program.⁵⁴ For modelling the reactivity with Ru-NPs, we use the PBE⁴⁸ functional as implemented in the VASP code.^{46,47} Grimme (D2) empirical correction was added to account for dispersion interactions.⁴⁹ The core electrons are described by ultrasoft

pseudopotential^{55,56} and the external ones by plane wave basis set, with a kinetic energy cutoff of 500 eV. With the aim of minimizing replica interactions, a cubic cell of 25 Å was employed. The k point grid includes the Γ point only, as a consequence of the discrete nature of the system. The energy convergence criteria were fixed to 10^{-5} and 10^{-4} eV for electronic and geometry relaxations, respectively. Solvent effects were included during the optimization with the implicit continuum model implemented in VASPsol⁵⁷ and using acetonitrile as solvent ($\epsilon = 37.5$). Transition states were located by using climbing image nudged elastic band (CI-NEB) method without including solvent effects.^{58,59} Six or eight images per NEB were used. The highest in energy image was used for locating the final transition state by performing a geometry optimization with the quasi-Newton algorithm implemented in VASP. Convergence was considered to be achieved when forces were smaller than 0.02 eV/Å. For the case of the hydronium ion, the transition state was located by performing restricted optimizations with solvation. The O-H distance was fixed to and the highest in energy point was used as starting point for localizing the transition state. The energies reported along the text are all given in kcal mol⁻¹.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This work was supported by Spanish Ministerio de Economía y Competitividad (MINECO) (CTQ2015-64261-R, CTQ2017-89132-P and RTI2018-095038-B-I00), and the Generalitat de Catalunya (2017SGR1323). We acknowledge the generous allocation of computer time at the Centro de Computación Científica at the Universidad Autónoma de Madrid (CCC-UAM) and the Consorci de Serveis Universitaris de Catalunya (CSUC). "Comunidad de Madrid" and European Structural Funds (S2018/NMT-4367) are also acknowledged. J.G.-A. acknowledges Serra Hùnter Program and KP CNRS.

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