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Shape evolution of neutron-rich ^{106,108,110}Mo isotopes in the triaxial degree of freedom

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The structure of 106 Mo, 108 Mo, and 110 Mo was investigated through β -delayed γ -ray spectroscopy at the RIKEN RI Beam Factory. New γ -ray transitions and levels are reported, including newly assigned 0_2^+ states in 108,110 Mo. The β -delayed neutron-emission probabilities of 108 Nb and 110 Nb were determined by examining the γ rays of their respective daughter decays. Quadrupole deformations were obtained for 106,108,110 Mo from their 2_1^+ energies and lifetimes. The even-odd energy staggering in the 2_2^+ band was compared with typical patterns of the γ -vibrational band, rigid triaxial rotor, and γ -soft rotor. The very small even-odd staggering of 106 Mo, 108 Mo, and 110 Mo favors a γ -vibrational band assignment. The kinematic moment of inertia for the 2_2^+ band showed a trend similar to the ground-state band, which is expected for the γ -vibrational band. Beyond-mean-field calculations employing the constrained Hartree-Fock-Bogoliubov (HFB) + local quasiparticle-random-phase approximation (QRPA) method using the SLy5+T interaction reproduced the ground and 2_2^+ bands in 2_2^+ bands as the 2_2^+ bands of the prolate shape. However, the staggering pattern observed in 2_2^+ band as the 2_2^+ band of the prolate shape. However, the staggering pattern observed in 2_2^+ band differs from the one suggested in the calculations which predict a 2_2^+ -soft rotor. There was no experimental indication of the oblate shape or the 2_2^+ -soft rotor predicted in heavier Mo isotopes.

I. INTRODUCTION

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The triaxial degree of freedom, γ , plays an important role in collective excitations of deformed even-even nuto clei. While the first $J^{\pi}=2^+$ state (2^+_1) is sensitive primarily to the quadrupole deformation parameter, β , the so-called γ band with a 2^+ band head is strongly related

43 to triaxial motion [1]. In the case of axially-symmetric 101 The staggering of the rigid triaxial rotor is opposite to 44 quadrupole deformation, a rotational band built on a γ - 102 that of the γ -soft rotor; for example, the 3^+_{γ} state is close 46 its band head is related to the softness of the vibrational $_{104}$ rotors, respectively, where the γ subscript indicates the 47 motion in the γ direction. When the potential energy 105 band member of the 2^+_2 state. On the other hand, the surface (PES) has a deep minimum between $\gamma = 0^{\circ}$ (pro- 106 γ -vibrational band with a small γ oscillation has a small 49 late) and 60° (oblate), the nucleus takes on a static tri- 107 or negligible staggering since the shape is close to being $_{50}$ axial shape and rotates about all three axes of the intrin- $_{108}$ axially symmetric. $_{51}$ sic body. The rigid triaxial rotor model by Davydov et $_{109}$ Another signature of γ vibration is the existence of a 52 al. [2] predicts that the 2^+_2 state lies below the 4^+_1 state 110 two-phonon γ -vibrational band based on the $K=4^+_1$ at the maximum triaxiality of $\gamma=30^\circ$. Another model 111 state. The $K=4^+$ band lying below the pairing gap $_{54}$ of the triaxial shape is the γ -unstable rotor by Wilets $_{112}$ was identified in the 104,106,108 Mo isotopes with an en-55 and Jean [3], where PES has a γ -independent valley at 113 ergy ratio $E_{K=4}/E_{K=2}=1.95, 2.02, \text{ and } 2.42 \text{ for } ^{104}\text{Mo},$ 56 a given β . The γ -unstable model predicts degenerate 114 $^{106}\text{Mo}, \text{ and } ^{108}\text{Mo}, \text{ respectively, which are close to the}$ 57 $^{2+}$ and $^{4+}$ states. A transitional rotor between the $^{7-}$ 115 harmonic-vibrator value of 2 [13, 14]. 58 vibrational band and the $^{7-}$ unstable rotor is the $^{7-}$ soft 116 The second $^{0+}$ state provides additional information $_{59}$ rotor, of which the PES has a moderate path between $_{117}$ on the nuclear shape, since its origin can derive from β prolate and oblate [4].

₆₂ investigate shape evolution in the γ degree of freedom. ₁₂₀ from β decay and (t,p) reaction studies [12, 18–20]. 69 Bogoliubov (HFB) calculations with the D1S-Gogny in- 127 ported in Ref. [22]. Reliable branching ratios of the 2^+_2 ₇₀ teraction [6] predict a gradual transition from γ -soft ro- ₁₂₈ states were determined. The 2_2^+ band in ¹¹⁰Mo was exto in ¹⁰²Mo to oblate in ¹¹²Mo. A calculation using the ¹²⁹ tended from 5⁺ to 7⁺. In ¹⁰⁸Mo and ¹¹⁰Mo, 0₂⁺ states ¹²⁹ global Skyrme energy density functional UNEDF0 pre- ¹³⁰ are newly assigned. It is observed that the previous ¹³⁰ dicts triaxial ground-state deformation in ^{106,108}Mo [7]. ¹³¹ 0₂⁺ assignment in ¹⁰⁶Mo [12] was incorrect. Values of neutron Fermi surfaces[8].

₇₈ band in ^{100–108}Mo [9], the quadrupole deformation was ¹³⁶ ing the constrained HFB (CHFB) + local quasiparticle-⁷⁹ indicated to reach a maximum at ¹⁰⁶Mo. More precise ¹³⁷ random-phase approximation (LQRPA) approach. 80 measurements are awaited to obtain a certain conclu-81 sion, since uncertainties of transitional quadrupole mo-82 ments are larger than a change among isotopes. The 138 measured 2^+_2 -state energy, $E(2^+_2)$, in the neutron-rich Mo $_{84}$ isotopes decreases as mass number, A, increases. It be- $_{139}$ so comes almost equal to $E(4_1^+)$ at A=108 and drops be- 140 (RIBF), operated by RIKEN Nishina Center and CNS, $_{88}$ terms of the rigid triaxial shape [12], γ vibration [13, 14], $_{143}$ impinging on a 3.0-mm thick beryllium target. The RI $_{99}$ and γ -soft rotor [15] based on the measured values of the $_{144}$ beam was separated by the BigRIPS fragment separa-90 energies of the 2_1^+ , 4_1^+ , and 2_2^+ states and the γ -decay 145 tor and transported through the ZeroDegree spectrome91 branching ratio from 2_2^+ state. The interpretation of the 146 ter [23, 24]. The particle identification (PID) was per- $_{92}$ 2_2^+ state attracts controversy due to its similarity be- $_{147}$ formed by determining the mass-to-charge ratio, A/Q, ₉₃ tween the three models, since the γ -vibrational state and ₁₄₈ and the atomic number, Z [25]. $\gamma\text{-soft}$ rotor have a finite root-mean-square value of γ as $_{_{149}}$ a result of a dynamic motion.

from the J(J+1) dependence of the rigid axial rotor. 155 y strips [27]. The implanted layer was determined by de-

vibrational state constitutes the γ band. The energy of $_{103}$ to the 2_{γ}^{+} and 4_{γ}^{+} states of the rigid triaxial and γ -soft

vibration or a coexisting shape. The 0_2^+ states in the The neutron-rich Mo isotopes are good candidates to $_{119}$ neutron-rich Mo isotopes are assigned up to A=106

Calculations using the liquid-drop or the finite-range $_{121}$ In the present study, the β -delayed γ rays of liquid-drop model using particle number projection or $_{122}$ 106,108,110 Mo were observed under lower background con-Bardeen-Cooper-Schrieffer methods predict the coexis- 123 ditions and/or with higher statistics than the previous tence of prolate and oblate shapes, a prolate-to-oblate 124 investigations [12, 15, 19, 21]. The lifetimes of the 2⁺₁ shape transition at N = 68 or 70, and triaxial ground 125 states were measured using a fast timing array of 18 states in ¹⁰⁴Mo, ¹⁰⁶Mo, and ¹⁰⁸Mo [5]. Hartree-Fock- ₁₂₆ LaBr₃(Ce) crystals, of which preliminary results are re-Calculations of two quasi-particle states are used to inves- 132 quadrupole deformation and evidence for triaxial motion tigate quasi-particle configurations near the proton and 133 have been extracted from these measurements. The re-134 sults are compared with beyond-mean-field calculations From the lifetime measurement of the ground-state 135 based on the five-dimensional collective Hamiltonian us-

II. EXPERIMENT

The experiment was performed at RI Beam Factory low $E(4_1^+)$ at $A \ge 110$ [10–16]. The low-lying 2_2^+ state $\frac{1}{14}$ University of Tokyo. The RI beam was produced by the in the neutron-rich Mo isotopes has been interpreted in 142 in-flight fission reaction of a 345 MeV/u ²³⁸U⁸⁶⁺ beam

The RI beam was implanted into the active stop-150 per WAS3ABi (Wide-range Active Silicon Strip Stop-The energy staggering of the 2^+_2 band is a good sig- 151 per Array for Beta and ion implantation), which comnature to distinguish among the three models which de- 152 prised five stacked Double-Sided Silicon Strip Detectors scribe axial asymmetry [1, 17]. The rigid-triaxial and 153 (DSSSDs) [26]. The RI hit position of one DSSSD was γ -soft rotors show an energy staggering which deviates 154 determined by selecting the fastest timing signal of x and

TABLE I. The number of $^{106,108,110}\mathrm{Zr}$ and $^{106,108,110}\mathrm{Nb}$ ions implanted in WAS3ABi and their implantation rate.

Isotope	The number of	Implantation rate
	implanted ions	(pps)
$^{106}\mathrm{Zr}$	1.9×10^{6}	3.5
$^{108}\mathrm{Zr}$	2.1×10^6	3.8
$^{110}{ m Zr}$	3.2×10^{4}	0.059
$^{106}\mathrm{Nb}$	7.1×10^{4}	16
$^{108}\mathrm{Nb}$	1.3×10^5	0.24
$^{110}\mathrm{Nb}$	1.9×10^{6}	3.5

156 tecting the cross-talk signal induced to the DSSSD downstream of the implanted one [28].

The β particles emitted by the decay of the RI were measured by WAS3ABi and two plastic scintillators with mm thickness, placed upstream and downstream of WAS3ABi. The timing signal of the plastic scintillator was used for the high-time resolution detection of β particles. The β -particle hit pattern and energy deposition in WAS3ABi and the plastic scintillators were used to restrict position candidates of the β emitter [29]. The β particle was associated with the implanted RI by using the position and time differences between the RI and β

WAS3ABi was surrounded by the EUroball-RIKEN The γ -ray detection efficiency was 3.0(5)% and 0.7(2)% ₂₄₂ evaluated value of 1.02(5) s [34]. at 250 keV and 1 MeV, respectively.

 $_{190}$ and to search for β -decaying isomeric states. The num- $_{247}$ decay chains, there was no evidence on the existence of a ber of implanted Nb and Zr isotopes are summarized in 248 second β -decaying state in ¹⁰⁶Nb. The absolute γ -ray inthrough the β decay of $^{102}\mathrm{Y}$ and the β -decay chain of 252 the $^{106}\mathrm{Nb}$ decay, which was determined from the decay-198 terms revealed that $^{102}{
m Y}$ has a β -decaying isomeric state 254 tion to the β -particle counts as a function of time. The

200 spin-parity of 0^+ can only populate the β -decaying low spin state in ¹⁰²Y. The same method was applied to the $Zr \rightarrow Nb \rightarrow Mo \beta$ -decay chain in this work. For each β decay chain, $Zr \rightarrow Nb \rightarrow Mo$ or $Nb \rightarrow Mo$, the β -ion time window was optimized to maximize the number of the 205 Nb-decay events and minimize the number of other de-206 Cays.

RESULTS

β decay to 106 Mo

The β -delayed γ -ray spectrum of ¹⁰⁶Mo obtained from ₂₁₀ the β -decay chain $^{106}\mathrm{Zr} \rightarrow ^{106}\mathrm{Nb} \rightarrow ^{106}\mathrm{Mo}$ is shown in Figs. 1 (a-b). The proposed level scheme of 106 Mo, illus-213 trated in Fig. 2, was constructed through the use of γ -ray 215 coincidences, for example Figs. 1 (c-d), energy sums and 216 intensity balances. Nine new levels were identified and 217 a new transition from the 2^+_2 to 4^+_1 states was observed. ₂₁₈ In the previous β - γ spectroscopic study [12], the ground 219 band was observed up to 6^+ , and the 2_2^+ and 4_3^+ bands 220 up to 4^+ . In the present study, γ rays from the 5^+ states $_{221}$ in the 2_2^+ and 4_3^+ bands were observed. These γ rays 222 are consistent with the results obtained from the spon-²²³ taneous fission of ²⁵²Cf [35–37]. The placement of the $_{224}$ 784.6-keV and 1106.7-keV γ rays were reassigned from 225 those of Ref. [12] based on the following arguments. The 0_2^+ state was previously assigned at 956.6 keV based on 170 Cluster Array (EURICA) [30] to detect γ rays emitted $_{227}$ the 784.6-keV transition feeding only the 171.4-keV level. $_{171}$ from excited states populated by the β decay of im- $_{228}$ However, the high statistics of the present study allowed $_{172}$ planted RIs. The systematic uncertainty of γ -ray en- $_{229}$ us to observe additional coincidences with the 784.6-keV ergy was evaluated to be 0.15 keV from the residuals of 230 transition, which are shown in Fig. 1 (d). Based on this the energy calibration with standard γ -ray sources. The $_{231}$ information, the assignment of the 784.6-keV γ ray as the γ -ray detection efficiency of EURICA was measured to $_{232}$ transition between the 5_1^+ and 4_1^+ states is preferred. The be 18.3% at 250 keV and 8.1% at 1 MeV. A system- 233 observation of the transition from 5₁⁺ to 3₁⁺ supports this atic uncertainty of 5% was determined for the absolute $_{234}$ assignment. The previous assignment of the 1106.7-keV value from the uncertainty of the radioactivity of the γ - γ - ray was the transition between a 1279.9-keV state to ray sources. A fast-timing LaBr₃(Ce) array consisting 236 the 2 the 2 that [12], but it was reassigned to a known transport of eighteen $\phi 1.5'' \times 2''$ crystals was coupled to the EU- 237 sition [34] from the 1816.9-keV state, since a coincidence RICA array to measure the lifetimes of low-lying excited 238 with 710.2 keV was observed. The half life of ¹⁰⁶Nb was 182 states in the nanosecond regime [31]. The Full-Width 239 determined to be 1.10(5) s from the decay curve of the ¹⁸³ Half Maximum (FWHM) of the time resolution of the ²⁴⁰ 171.4-keV γ ray for the ¹⁰⁶Nb \rightarrow ¹⁰⁶Mo decay as shown in ¹⁸⁴ LaBr₃(Ce) array was evaluated to be 0.61 ns at 200 keV. ²⁴¹ Fig. 3 (a). The obtained half life was consistent with the

at 250 keV and 1 MeV, respectively. 243 Table II summarizes the relative γ -ray intensity, I_{γ} , Excited states in 106,108,110 Mo populated in the beta 244 following the β decay from 106 Nb to 106 Mo from the two decay of 106,108,110 Nb were studied. The daughter decays 245 decay chains, 106 Nb \rightarrow 106Mo and 106 Zr \rightarrow 106Nb \rightarrow 106Mo. of Zr isotopes were also analyzed to increase statistics 246 Since I_{γ} of the major peaks was consistent between both Table I. Daughter-decay analysis provides evidence on 249 tensities per 100 β decays were determined from the data the existence of β -decaying isomeric states. For exam- 250 of the $^{106}\text{Nb}\rightarrow^{106}\text{Mo}$ decay for the first time. Here, we ple, in Ref. [32], the β - γ spectrum of $^{102}\mathrm{Zr}$ was observed $_{251}$ used the number of the detected β particles emitted from $^{102}\mathrm{Sr} \rightarrow ^{102}\mathrm{Y} \rightarrow ^{102}\mathrm{Zr}$. Two different γ -ray transition pat- 253 curve integral of the parent component in the fitting funcand the β decay of the even-even ^{102}Sr isotope with the 255 conversion factor from the relative to absolute γ -ray in-

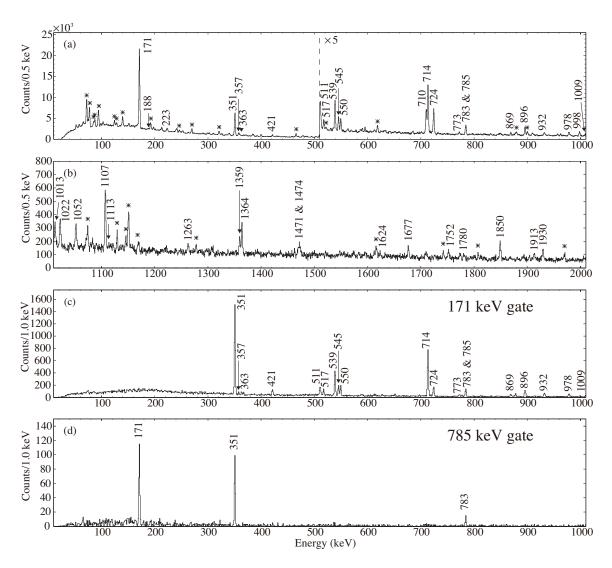


FIG. 1. (a-b) The β -delayed γ -ray spectrum of 106 Nb obtained from the β -decay chain 106 Zr \rightarrow 106 Nb \rightarrow 106 Mo. The range of the time window was set to be 180 ms $< t_{\rm ion} - t_{\beta} < 2200$ ms. The labeled peaks belong to ¹⁰⁶Mo. The identified background peaks are marked with asterisks. Other unknown peaks are mainly associated with parent ¹⁰⁶Zr decays. (c-d) The coincidence spectra gated on 171.4 keV and 784.6 keV.

tainty of the conversion factor as 0.696(38).

chains so as to take into account small β -decay branches. 279 < 8.4%. The decay schemes and I_{γ} values were obtained from 280 ₂₆₇ higher statistics. The total I_{β} of all γ -decaying excited ₂₈₂ atomic mass evaluation (AME2016) [33] and the calcula-268 states is given by summing the absolute transition in- 283 tion tool of Ref. [38]. The $\log ft$ of the 6_1^+ state, 6.6(1), 269 tensities of excited states decaying to the ground state.

256 tensities was obtained from the absolute intensity of the 270 Two relevant transitions, $2_1^+ \rightarrow 0_1^+$ and $2_2^+ \rightarrow 0_1^+$, were largest γ -ray peak at 171.4 keV in the $^{106}\text{Nb}\rightarrow^{106}\text{Mo de-}_{271}$ observed. The sum of the absolute intensities of these two cay. The relative systematic uncertainty of the absolute 272 transitions was 92.2(51)%, which included contributions γ -ray detection efficiency was adopted into the uncer- 273 of possible undetected transitions, due to low intensities, 274 through the 2_1^+ or 2_2^+ states. The remaining 7.8(51)%275 contribution is the sum of I_{eta} to the ground state, and The β -decay intensities, I_{β} , to excited states, given in 276 the β -delayed neutron emission probability, P_n . When a Table II, were determined by combining results obtained 277 previously measured P_n of 4.5(3)% [34] is subtracted, the from the $^{106}\mathrm{Zr} \rightarrow ^{106}\mathrm{Nb} \rightarrow ^{106}\mathrm{Mo}$ and $^{106}\mathrm{Nb} \rightarrow ^{106}\mathrm{Mo}$ decay 278 I_{β} value to the ground state is given as the upper limit

Table II summarizes the $\log ft$ value of each excited the $^{106}\text{Zr} \rightarrow ^{106}\text{Nb} \rightarrow ^{106}\text{Mo}$ decay chain, which provided 281 state calculated using $Q(\beta^-) = 9931(10)$ keV from the

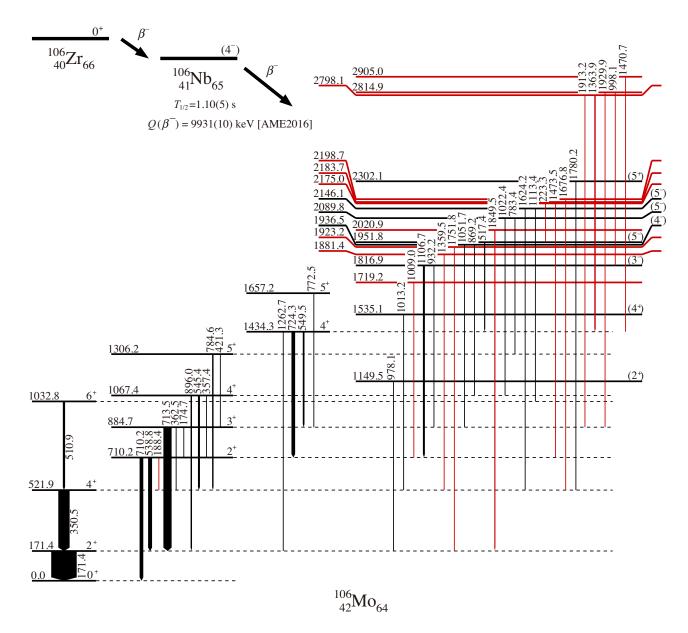


FIG. 2. The proposed level scheme of 106 Mo obtained from the β-decay chain 106 Zr \rightarrow 106 Mo. The Q(β⁻) of 106 Nb is taken from the atomic mass evaluation (AME2016: [33]). The arrow width is proportional to the relative intensity I_{γ} (Zr \rightarrow Mo, given in Table II). Red lines are the new levels and transitions. Spin-parities of the known states are taken from ENSDF [34].

TABLE II: The level energy, E_i , spin-parity, J^{π} , γ -ray energy, E_{γ} , relative γ -ray intensity, I_{γ} , β -decay intensity, I_{β} , and $\log ft$ of the excited states in 106 Mo. (Nb \rightarrow Mo) indicates the β decay from the implanted 106 Nb to 106 Mo. (Zr \rightarrow Mo) indicates the β decay to 106 Mo in the decay chain of the implanted 106 Zr, i.e. 106 Zr \rightarrow 106 Mb \rightarrow 106 Mo. (allowed/non-UF) indicates the calculation is for the allowed or non-unique forbidden transitions. (1UF) is for the first unique forbidden transition from 4^- to 2^+ or 6^+ states.

$E_i(\text{keV})$	J^{π}	$E_{\gamma}(\mathrm{keV})$	I_{γ}^{a} (Nb \rightarrow Mo)	I_{γ} (Zr \rightarrow Mo)	$I_eta(\%)^b$	$\frac{\log ft}{(\text{allowed/non-UF})}$	$\frac{\log ft}{(1\text{UF})}$
0.0	0^+				< 8.4		
171.4(2)	2^+	171.4(2)	100(2)	100.0(5)	7.3(8)	6.7(1)	9.1(1)
521.9(2)	4^+	350.5(2)	37.9(16)	43.8(5)	9.1(14)	6.5(1)	

TABLE II: (continued)

$E_i(\text{keV})$	J^{π}	$E_{\gamma}(\mathrm{keV})$	$I_{\gamma}{}^{a}$ (Nb \rightarrow Mo)	I_{γ} (Zr \rightarrow Mo)	$I_{eta}(\%)^b$	$\frac{\log ft}{(\text{allowed/non-UF})}$	$\frac{\log ft}{(1\text{UF})}$
710.2(1)	2+	188.4(4)	2.9(7)	0.3(2)	2.8(6)	7.0(1)	9.3(1)
		538.8(2)	16.6(12)	15.6(3)			
		710.2(2)	14.4(15)	15.2(3)			
884.7(2)	3^{+}	174.7(3)		1.0(4)	8.7(7)	6.5(1)	
		362.5(3)	1.7(7)	0.7(2)			
		713.5(2)	30.1(17)	31.9(4)			
1032.8(3)	6^+	510.9(2)	5.3(12)	8.2(15)	5.5(11)	6.6(1)	8.9(1)
1067.4(1)	4^+	357.4(2)	3.9(8)	2.1(2)	7.9(5)	6.5(1)	
		545.4(2)	5.3(10)	7.6(2)			
		896.0(2)	6.1(10)	6.1(2)			
1149.5(2)	(2^{+})	978.1(2)		2.3(2)	1.6(2)	7.1(1)	9.4(1)
1306.2(2)	5+	421.3(2)	3.1(7)	3.5(2)	5.4(8)	6.6(1)	
		784.6(2)	3.4(8)	5.5(7)			
1434.3(1)	4^+	549.5(2)	5.1(9)	6.9(2)	7.0(5)	6.4(1)	
,		724.3(2)	11.7(12)	14.0(3)	. ,	. ,	
		1262.7(3)	,	1.4(2)			
1535.1(3)	(4^{+})	1013.2(2)		1.5(3)	1.0(2)	7.2(1)	
1657.2(3)	5+	772.5(2)		1.4(2)	1.0(1)	7.2(1)	
1719.2(2)		1009.0(2)		1.3(2)	0.9(1)	7.2(1)	
1816.9(2)	(3^{-})	932.2(2)	1.3(7)	2.0(2)	4.9(4)	6.5(1)	
,	,	1106.7(2)	4.0(8)	7.4(3)	. ,	· ,	
1881.4(3)		1359.5(2)	,	2.9(2)	2.0(2)	6.9(1)	
1923.2(2)		1751.8(2)		1.6(2)	1.1(2)	7.1(1)	
1936.5(2)	(4^{-})	869.2(2)		2.0(2)	3.5(3)	6.6(1)	
		1051.7(2)	2.9(2)	3.1(2)			
1951.8(2)	(5^{-})	517.4(2)	6.2(9)	4.6(2)	2.3(2)	6.8(1)	
2020.9(2)		1849.5(2)	3.2(14)	4.1(3)	2.9(3)	6.7(1)	
2089.8(2)	(5^{-})	783.4(4)	2.6(11)	1.3(7)	2.7(5)	6.7(1)	
. ,	, ,	1022.4(2)	, ,	2.5(2)		. ,	
2146.1(4)	(5^{-})	1113.4(5)		0.3(2)	0.5(2)	7.4(2)	
,	,	1624.2(4)		0.4(2)	. ,	· ,	
2175.0(3)		223.3(2)		1.3(2)	0.9(1)	7.1(1)	
2183.7(4)		1473.5(3)		1.3(2)	0.9(1)	7.1(1)	
2198.7(3)		1676.8(2)		2.2(2)	1.5(2)	6.9(1)	
2302.1(3)	(5^+)	1780.2(3)		1.4(2)	1.0(1)	7.1(1)	
2798.1(2)		1363.9(2)	6.3(9)	5.9(2)	5.2(3)	6.2(1)	
• •		1913.2(3)		1.5(1)	• •		
2814.9(2)		998.1(2)		2.3(1)	3.5(2)	6.4(1)	
		1929.9(2)		2.7(2)			
2905.0(3)		1470.7(3)		1.7(2)	1.2(2)	6.8(1)	

^a The absolute intensity per 100 β -decays is $0.696(38)I_{\gamma}$.

 $[^]b$ Internal conversion coefficients, calculated using the BrIcc code [39], were adopted for three transitions with 171.4, 174.7, and 188.4 keV.

indicates an allowed transition with $\Delta J=0$ or 1 and 289 dicates allowed or first non-unique forbidden transitions. 286 $\Delta\pi=0$, or a first non-unique forbidden transition with 290 However, the transitions with $\Delta J\leq 1$ can not populate 287 $\Delta J=0$ or 1 and $\Delta\pi=1$ [40]. Three 2⁺ states have 291 both the 2⁺ and 6⁺ states. Therefore, transitions with 288 similar log ft values ranging from 6.7 to 7.1 which also in- 292 at least $\Delta J=2$ are required for these states. For the

293 unique forbidden transitions, the $\log ft$ values need to be calculated by taking into account the different energy 295 dependence of the shape factor from that of the allowed decay [38, 41]. The log ft of the 6_1^+ state becomes 8.9(1) for the first unique forbidden transition with $\Delta J = 2$ and $\Delta \pi = 1$. This value is consistent with the typical range from 8 to 11 [40]. This indicates that the spin-parity of ¹⁰⁶Nb is 4⁻. This assignment determines the transition 301 type to other states. Since the β decay to the 2⁺ states is $_{302}$ also a first unique forbidden transition, the log ft values of the 2^{+} states with 171.4, 710.2, and 1149.5 keV were recalculated as 9.1(1), 8.9(1), and 9.4(1), respectively. These values are consistent with the typical range of the first unique forbidden transition. The $\log ft$ values of the 3⁻, 4⁻, and 5⁻ states are consistent with the allowed transition with $\Delta J = 0$ or 1 and $\Delta \pi = 0$, and those of 309 3^+ , 4^+ , and 5^+ states are consistent with the first non-310 unique forbidden transition with $\Delta J = 0$ or 1 and $\Delta \pi =$ 311 1. Thus, providing further evidence that the spin-parity ₃₁₂ of ¹⁰⁶Nb is 4⁻. The quasi-particle state configuration of ¹⁰⁶Nb is discussed in Sec. IV F.

β decay to $^{108}{ m Mo}$

315

The β -delayed γ -ray spectrum of $^{108}\mathrm{Mo}$ obtained ₃₁₇ from the $^{108}\text{Zr} \rightarrow ^{108}\text{Nb} \rightarrow ^{108}\text{Mo}$ decay chain is shown in 310 Figs. 4 (a-b). The proposed level scheme illustrated in Fig. 5 was constructed through the use of γ -ray co-322 incidences, examples shown in Figs. 4 (c-d), energy 323 sums, and intensity balances. In the previous β -decay $_{324}$ study [21], the ground band was observed up to 4^{+} and the 2_2^+ band was up to 3^+ . In this work, the 2_2^+ band was $_{326}$ observed up to 4^+ , and the band head of the 4^{+} band was 327 observed at 1422.1 keV. Fifteen new levels were identi- $_{328}$ fied, of which the lowest at 893.4 keV was assigned to 0_2^+ from the typical γ decay pattern of a low-lying 0^+ state, 330 namely the observed 700.7-keV transition was measured ₃₃₁ to be in strong coincidence with the $2_1^+ \rightarrow 0_1^+$ transition, 332 as shown in Fig. 4 (c), and without an observed γ de- $_{333}$ cay to the 0_1^+ state. The spin-parity of the 1158.4-keV $_{334}$ state was assigned to be 2^+ , and those of the 1404.8-, 335 and 1727.6-keV states were to be 3 or 4⁺ by assuming the transition type from those states is E1 or M1/E2. The half life of the 108 Nb decay was determined to be 7 $T_{1/2}=186(8)$ ms from the decay curve of the 192.8-keV γ ray, as shown in Fig. 3 (b), and is consistent with the ³⁴⁰ evaluated value of 198(6) ms [34].

to absolute γ-ray intensities was determined from the absolute 192.8-keV intensity in the 108 Nb \rightarrow 108 Mo decay. 356 emission, was determined by using a new method design solute 192.8-keV intensity in the 108 Nb \rightarrow 108 Mo decay. 357 scribed in Sec. III C as, $P_{0n} = 82(11)\%$. The difference

 $_{349}$ sities and the decay scheme. As described in Sec. III A, $_{359}$ The I_{γ} values obtained in this work are inconsistent $_{350}$ the total I_{β} of the γ -decaying excited states in 108 Mo $_{360}$ with the previous results [21] with the exception of the

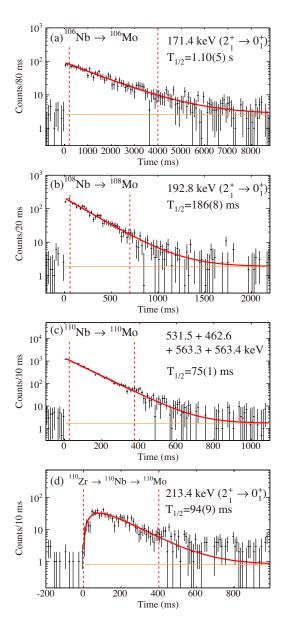


FIG. 3. The time spectra of β -delayed γ rays in the Mo isotopes. Dashed lines indicate the fitting region of the decay curve to determine the β -decay half life, $T_{1/2}$. Orange lines are the constant background, which was determined by fitting to the negative-time region. The β -delayed γ rays with 531.5, 462.6, 563.3, and 563.4 keV from the implanted $^{110}\mathrm{Nb}$ were selected as the β decays of the high-spin state in ¹¹⁰Nb.

The I_{γ} values were determined for the two decay 351 was determined to be 62.8(33)% from the sum of absochains, $^{108}{\rm Nb} \rightarrow ^{108}{\rm Mo}$ and $^{108}{\rm Zr} \rightarrow ^{108}{\rm Nb} \rightarrow ^{108}{\rm Mo}$, as 352 lute transition intensities of three transitions from the 2^+_1 , summarized in Table III. The consistent I_{γ} values be- 353 2_2^+ , and 2_3^+ states to the ground state. The zero-neutron tween two decay chains indicate no β -decaying isomeric 354 emission probability of the ¹⁰⁸Nb decay, P_{0n} , which is the state in ¹⁰⁸Nb. The conversion factor from the relative ³⁵⁵ probability decaying to ¹⁰⁸Mo without a delayed-neutron The I_{β} values were determined from the absolute inten- 358 of these two values gave the ground-state I_{β} of 19(12)%.

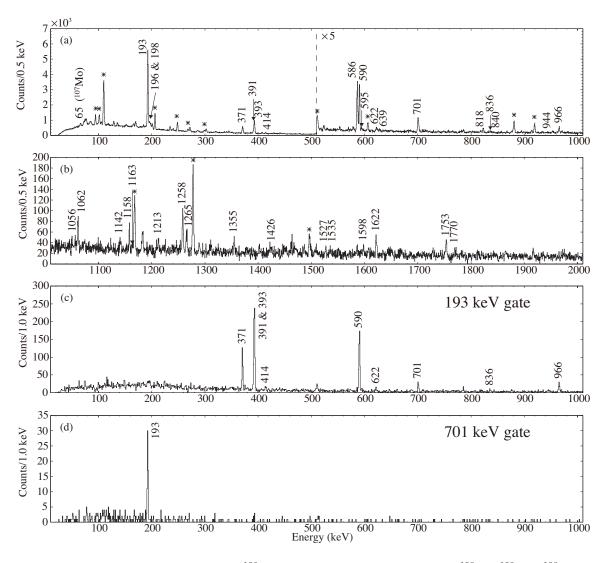


FIG. 4. (a-b) The β -delayed γ -ray spectrum of 108 Nb obtained from the β -decay chain 108 Zr \rightarrow 108 Nb \rightarrow 108 Mo. The range of the time window was set to be 80 ms $< t_{\rm ion} - t_{\beta} < 280$ ms. The labeled peaks belong to 108 Mo. The identified background peaks are marked with asterisks. Other unknown peaks are mainly associated with parent ¹⁰⁸Zr decays. (c-d) The coincidence spectra gated on 192.8 keV and 700.7 keV.

 $_{361}$ 371.1- and 393.1-keV γ rays. Notably the $I_{\gamma}(590.1 \text{ keV})$ $_{376}$ and 4_1^+ states were 5.8(3) and 6.4(1) and are too small $_{373}$ 3_{1}^{+} state.

390 $Q_{\beta} = 11210(12) \text{ keV } [33].$ The log ft values of the 0_1^+

of 26.1(6)\% was roughly half of that reported in Ref. [21], 377 for any transitions with $\Delta J > 2$ [40]. This is the same 53%. As mentioned in Ref. [21], a large background in 378 situation as for the ¹⁰⁶Nb decay. If the first unique fortheir γ -ray spectrum might be the cause of the inconsis- 379 bidden transition with $\Delta J=2$ and $\Delta \pi=1$ is considered tency. The absolute intensity of the $2_1^+ \rightarrow 0_1^+$ transition $_{380}$ for the transitions to these states, the spin-parity of the was also roughly half of that reported in Ref. [21]. This $_{381}$ 108 Nb ground state is 2^- . The $\log ft$ values of the 0^+ may be due to a 50% uncertainty of the ¹⁰⁸Nb yield ex- ₃₈₂ and 4⁺ states were recalculated as the first unique fortrapolated as a function of the atomic number [21]. Al- 383 bidden transition to be 8.2(3), 8.8(1), 8.7(1), 8.5(1), and though the uncertainty of the previous I_{β} was not eval- 384 9.2(1) for the ground state and the excited states at 563.8 uated, the present $I_{\beta}(3_1^+)$ of 5.1(6)% is 1/10 of the re- 385 keV, 893.4 keV, 978.3 keV, and 1422.1 keV, respectively. ported 53% [21] owing to yield uncertainties and the pre- 386 These are within the typical range from 8 to 11 [40]. The vious non-observation of the cascade transitions to the $_{387}$ log ft values of the 2^+ , 3^+ , and 3^- states indicate the 388 allowed transition or the first non-unique forbidden tran-The log ft values were determined from $T_{1/2}$, I_{β} , and $_{389}$ sition, and are consistent with the β decay from a $2^$ state. The β decay to the 5⁻ state at 2161.8 keV is the

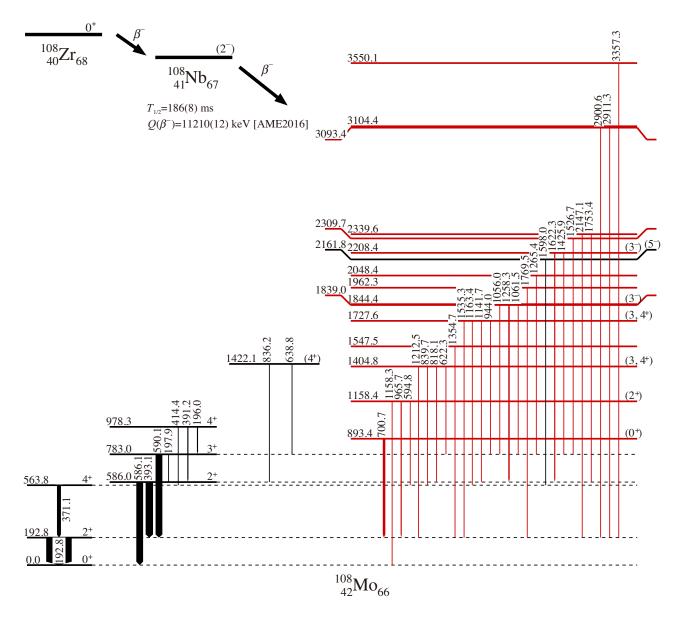


FIG. 5. The proposed level scheme of 108 Mo obtained from the β -decay chain 108 Zr \rightarrow 108 Nb \rightarrow 108 Mo. Red lines are the new levels and transitions.

TABLE III: Same as Table II, but for 108 Mo. (1UF) is for the first unique forbidden transition from 2^- to 0^+ or 4^+ states. (2UF) is for the second unique forbidden transition from 2^- to 5^- states.

$E_i(\text{keV})$	J^{π}	$E_{\gamma}(\text{keV})$	$I_{\gamma}{}^{a}$ (Nb \rightarrow Mo)	I_{γ} (Zr \rightarrow Mo)	$I_{eta}(\%)^b$	$\frac{\log ft}{(\text{allowed/non-UF})}$	$\frac{\log ft}{(1\text{UF})}$	$\frac{\log ft}{(2\mathrm{UF})}$
0.0	0^+				19(12)	5.8(3)	8.2(3)	
192.8(2)	2^+	192.8(2)	100(2)	100.0(9)	6.7(10)	6.2(1)		
563.8(2)	4^+	371.1(2)	18.2(10)	14.5(5)	3.7(6)	6.4(1)	8.8(1)	
586.0(1)	2^+	393.1(2)	28.3(13)	27.8(10)	13.2(12)	5.8(1)		
		586.1(2)	25.0(12)	26.4(7)				
783.0(2)	3^+	197.9(6)		3.4(1)	5.1(6)	6.2(1)		
		590.1(2)	27.4(12)	26.1(6)				
893.4(2)	(0^{+})	700.7(2)	4.7(16)	9.7(5)	4.3(3)	6.3(1)	8.7(1)	

TABLE III: (continued)

$E_i(\text{keV})$	J^{π}	$E_{\gamma}(\mathrm{keV})$	$I_{\gamma}{}^{a}$ (Nb \rightarrow Mo)	I_{γ} (Zr $ ightarrow$ Mo)	$I_{eta}(\%)^b$	$\log ft$ (allowed/non-UF)	$\frac{\log ft}{(1\text{UF})}$	$\frac{\log ft}{(2\mathrm{UF})}$
978.3(2)	4+	196.0(2)		5.0(1)	5.4(7)	6.1(1)	8.5(1)	
,		391.2(3)	7.0(9)	4.5(14)	. ,	,	. ,	
		414.4(3)	2.1(5)	2.3(6)				
1158.4(1)	(2^{+})	594.8(3)	1.2(5)	1.5(4)	3.8(4)	6.3(1)		
		965.7(2)	4.2(7)	4.4(4)				
		1158.3(2)	3.2(6)	2.5(4)				
1404.8(2)	$(3,4^+)$	622.3(3)		1.7(4)	2.1(3)	6.5(1)		
		818.1(4)		0.8(3)				
		839.7(3)		0.7(3)				
		1212.5(3)		1.4(4)				
1422.1(2)	(4^{+})	638.8(4)	0.6(1)	0.5(3)	0.9(2)	6.8(1)	9.2(1)	
		836.2(3)		1.4(3)				
1547.5(3)		1354.7(2)		2.1(4)	0.9(2)	6.8(1)		
1727.6(2)	$(3,4^+)$	944.0(5)		0.4(3)	1.5(3)	6.5(1)		
		1141.7(3)		1.4(3)				
		1163.4(6)		0.5(5)				
		1535.3(4)		1.1(3)				
1839.0(5)		1056.0(4)		0.8(3)	0.4(1)	7.1(1)		
1844.4(2)	(3^{-})	1061.5(2)	2.2(1)	3.6(4)	4.1(4)	6.1(1)		
		1258.3(2)	7.5(6)	5.6(5)				
1962.3(2)		1769.5(2)		0.8(1)	0.4(1)	7.1(1)		
2048.4(3)		1265.4(2)	3.3(5)	3.1(4)	1.4(2)	6.5(1)		
2161.8(4)	(5^{-})	1598.0(3)		1.2(5)	0.5(2)	6.9(2)		11.6(2)
2208.4(2)	(3^{-})	1425.9(7)		1.1(3)	2.4(3)	6.2(1)		
		1622.3(2)		4.2(4)				
2309.7(3)		1526.7(3)		1.8(3)	0.8(1)	6.7(1)		
2339.6(2)		1753.4(3)		3.3(5)	2.8(3)	6.1(1)		
		2147.1(3)		3.0(4)				
3093.4(5)		2900.6(4)		1.6(4)	0.7(2)	6.6(1)		
3104.1(4)		2911.3(3)		2.3(5)	1.0(2)	6.4(1)		
3550.1(5)		3357.3(4)		1.6(6)	0.7(3)	6.4(2)		

^a The absolute intensity per 100 β -decays is 0.448(23) I_{γ} .

 $_{392}$ $\Delta\pi=0$. The log ft value of the 5⁻ state was recal-403 tion, respectively. The neutron emission probability P_n 393 culated to be 11.6(2) and within the typical range from 404 is given by 10.6 to 18 for the second unique forbidden transition [40]. Therefore, the spin-parity of the ¹⁰⁸Nb was assigned to be 2⁻. The quasi-particle state configuration of ¹⁰⁸Nb is 397 described in Sec. IV F.

C. Neutron-emission probability in 108 Nb β decay

second unique forbidden transition with $\Delta J=3$ and 402 sured ¹⁰⁸Mo and ¹⁰⁸Nb decays after the ¹⁰⁸Nb implanta-

$$P_n = 1 - P_{0n} = \sum_{i \ge 1} P_{in},\tag{1}$$

 $_{405}$ where i is the number of the emitted neutrons. $N_{\beta}(^{108}{\rm Nb})$ was determined to be $5.20(13)\times 10^4$ from $_{407}$ a fit to the $\beta\text{-decay}$ time curve obtained following the 408 implantation of ¹⁰⁸Nb. The fit used the decay half-lives 409 and neutron-emission probabilities of the parent ¹⁰⁸Nb, The zero-neutron emission probability, P_{0n} , of the 410 daughters 107,108 Mo, granddaughters 106,107,108 Tc and 400 108 Nb decay is given by the ratio $N_{\beta}(^{108}$ Mo)/ $N_{\beta}(^{108}$ Nb), 411 great granddaughters 107,108 Ru from the literature [34] 401 where $N_{\beta}(^{108}$ Mo) and $N_{\beta}(^{108}$ Nb) are the integral of mea-412 except for 108 Nb where the half-life of 186(8) ms mea-

^b Internal conversion coefficients, calculated using the BrIcc code [39], were adopted for three transitions with 192.8, 196.0, and 197.9 keV.

413 sured in this work was used. It was assumed that the 464 414 probability of the emission of two or more neutrons is negligibly small so that $P_{1n} = 1 - P_{0n}$.

 $N_{\beta}(^{108}\text{Mo})$ can be derived from the number of counts of the 268.3-keV γ ray, $N_{\gamma}(268.3 \text{ keV})$, emitted from the $^{108}\text{Mo} \rightarrow ^{108}\text{Tc}$ decay using the relation,

$$N_{\gamma}(268.3 \text{ keV}) = N_{\beta}(^{108}\text{Mo})\varepsilon_{\gamma}(268.3 \text{ keV}) \times I_{\gamma,\text{abs}}(268.3 \text{ keV}),$$
 (2)

420 which is sensitive to the implantation position, and $I_{\gamma,abs}(268.3 \text{ keV})$ is the absolute intensity of 268.3 keV ⁴²² per one ¹⁰⁸Mo decay. In order to evaluate N_{β} (¹⁰⁸Mo), 423 we define the ratio,

$$R(268.3 \text{ keV}) = \frac{N_{\gamma}(268.3 \text{ keV})}{N_{\beta}(^{108}\text{Mo})},$$
 (3)

424 which should be the same for the $^{108}{\rm Nb}$ \rightarrow $^{108}{\rm Mo}$ \rightarrow $^{108}\mathrm{Tc}$ and $^{108}\mathrm{Mo} \rightarrow ^{108}\mathrm{Tc}$ decays, if the position of $_{\rm 426}$ the $^{\rm 108}{\rm Nb}$ and $^{\rm 108}{\rm Mo}$ parent in WAS3ABi is the same. 427 To satisfy this requirement, we consider only events 428 where the implanted ion is ¹⁰⁸Nb. To obtain a value of $_{429}$ R(268.3 keV) from the $^{108}\text{Mo} \rightarrow ^{108}\text{Tc}$ decay, we use the 430 detection time of the 192.8-keV γ ray emitted from the 431 2_1^+ state in 108 Mo as a time-zero of the decay of 108 Mo. N_{β} N_{β} N_{β} N_{β} N_{β} N_{β} N_{β} was then obtained from the β -decay time $_{433}$ curve using the same method as described for $^{108}\mathrm{Nb}$. The $_{^{434}}$ number of $^{^{\backprime}108}\mathrm{Tc}$ 268.3-keV γ rays was obtained from the $_{435}$ γ -ray peak integral to give R(268.3 keV) = 0.0558(65). To obtain a value of $N_{\gamma}(268.3 \text{ keV})$ for the ¹⁰⁸Nb \rightarrow $_{^{437}}$ $^{108}\mathrm{Mo}$ \rightarrow $^{108}\mathrm{Tc}$ decay, a time gate of 400–3000 ms af- $_{\rm 438}$ ter the $^{108}{\rm Nb}$ implantation in WAS3ABi was applied 439 to optimize the γ rays emitted from the $^{108}\mathrm{Mo}$ de-440 cay. This yielded a 268.3-keV peak containing 1695(43) 441 counts. The expected number of 268.3-keV γ rays ob-442 served without time restriction is evaluated as $N_{\gamma}(268.3)$ 443 keV) = 2380(140), which, using Eq. (3), equates to $N_{\beta}(^{108}\text{Mo}) = 42700(5600).$

By using the relation, $P_{0n} = \frac{N_{\beta}(^{108}\text{Mo})}{N_{\beta}(^{108}\text{Nb})}$, we obtain 504 reaction populates both states. 445 $P_{0n} = 82(11)\%$, giving $P_n = 18(11)\%$. Observation of 447 the known 65.4-keV γ ray [42] from the isomeric state 448 in ¹⁰⁷Mo in Fig. 4 (a) provides a direct evidence of the ⁵⁰⁵ ⁴⁴⁹ β-delayed neutron emission of ¹⁰⁸Nb. The absolute γ -ray $_{450}$ intensity of the 65.4-keV γ ray corresponds to a minimum 451 P_{1n} of 8.1(7)%, which includes the contribution of the in-452 ternal conversion for the E2 transition. It is reasonable 508 solute γ -ray intensities, I_{β} , and $\log ft$, need to be de-453 that this is less than $P_n = 18(11)\%$, given above, as there 509 termined separately for the low- and high-spin states in 454 exist unobserved one- or multi-neutron emission chan- 510 110 Nb. To evaluate $T_{1/2}$ for the high-spin state, the γ 455 nels. The minimum value reported here is larger than a 511 rays with 462.6, 531.5, 563.3, and 563.4 keV from the 456 previously reported P_n value of 6.2(5)% [43] and equal 512 5_1^+ , 6_1^+ , or 6_2^+ states were used as they are emitted only to 8(2)% of Ref. [44]. The previous P_n values were de- 513 in the β decay of the high-spin state. The half-life of the $_{458}$ rived from measurements of β-delayed neutrons with 3 He $_{514}$ high-spin state in 110 Nb was determined to be 75(1) ms ₄₅₉ ionization chamber tubes [43], or a combination of 3 He ₅₁₅ from the sum of the decay curves of these four γ rays 460 and B₃F proportional gas-counter tubes [44]. Neutron- 516 using the data of the $^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$ decay as shown in detection efficiencies of these configurations, which have 517 Fig. 3 (c). The 213.4-keV γ ray obtained in the $^{110}{\rm Zr}$ 462 a possible energy dependence, could have been affected $_{518} \rightarrow ^{110} \mathrm{Nb} \rightarrow ^{110} \mathrm{Mo}$ decay chain was used for the half-life 463 by unknown β -delayed neutron energy distributions.

D. β decay to 110 Mo

The β -delayed γ -ray spectrum of ¹¹⁰Mo obtained from 466 the β decay of ¹¹⁰Nb is shown in Figs. 6 (a-b), and 468 the coincidence spectrum of the $2_1^+ \rightarrow 0_1^+$ transition is 469 shown in Fig. 6 (c). The proposed level scheme is shown $_{470}$ in Fig. 7. In the previous works of the $^{110}{\rm Nb}~\beta$ decay and 472 the ²⁴⁸Cm spontaneous fission decay [15, 45], the ground band up to 10^+ and the 2_2^+ band up to 5^+ were reported. where $\varepsilon_{\gamma}(268.3 \text{ keV})$ is the γ -ray detection efficiency, 474 In the present work, thirty new levels are identified and 475 the 2^+_2 band is extended up to its 7^+ state. A new band $_{\rm 476}$ based on a 1243.8-keV state was observed and from its 477 interband transitions to the 2^+_2 band, a spin-parity of 4^+ 478 was assigned to its band head. The spin-parities of the $_{479}$ band members with 1520.1 keV and 1796.2 keV were as-(3) 480 signed as 5^+ and 6^+ , respectively. A state at 1042.2 keV 481 was measured based on the observation of a 828.8-keV γ 482 ray coincident only with the 213.4-keV γ ray, as shown in 483 Fig. 6 (d). Direct γ decay from the 1042.2-keV state to 484 the ground state was not observed. Based on this typical $_{485}$ γ -decay pattern of a low-lying 0⁺ state, the 1042.2-keV 486 state was assigned to 0^+ . The I_{γ} values are summarized

The β -delayed γ -ray spectrum of $^{110}\mathrm{Mo}$ obtained from 488 the $^{110}\mathrm{Zr} \rightarrow ^{110}\mathrm{Nb} \rightarrow ^{110}\mathrm{Mo}$ decay chain is shown in $_{\rm 490}$ Fig. 6 (e). Only five excited states were observed, which were the 2^+ and 4^+ states in the ground band, the 2^+ $_{492}$ and 3^{+} states in the 2_{2}^{+} band, and the 0_{2}^{+} state. This 493 β -decay feeding pattern and the I_{γ} values, given in Ta-⁴⁹⁴ ble V, are different from those of the $^{110}{
m Nb} \rightarrow {}^{110}{
m Mo}$ 495 decay. These differences indicate the existence of two β - $_{\rm 496}$ decaying states in $_{\rm ^{110}Nb}.$ Since the spin-parity of the 497 even-even nucleus $^{110}\mathrm{Zr}$ is 0^+ , it is expected that the 498 low-spin states in 110 Nb are populated by the β decay of ⁴⁹⁹ ¹¹⁰Zr. This expectation is consistent with the β -decay $_{500}$ feeding pattern to the lower-spin states in $^{110}\mathrm{Mo}$ by the 501 $^{110}\mathrm{Zr} \rightarrow ^{110}\mathrm{Nb} \rightarrow ^{110}\mathrm{Mo}$ decay chain. On the other hand, $_{502}$ the $^{110}{
m Nb}
ightarrow ^{110}{
m Mo}$ decay has contributions of the low-503 and high-spin states in ¹¹⁰Nb because the in-flight fission

\mathbf{E} . Extraction of β -decay properties for low- and high-spin states in ¹¹⁰Nb

Beta-decay properties, namely $T_{1/2}$, relative and abmeasurement of the low-spin state in ¹¹⁰Nb. The decay

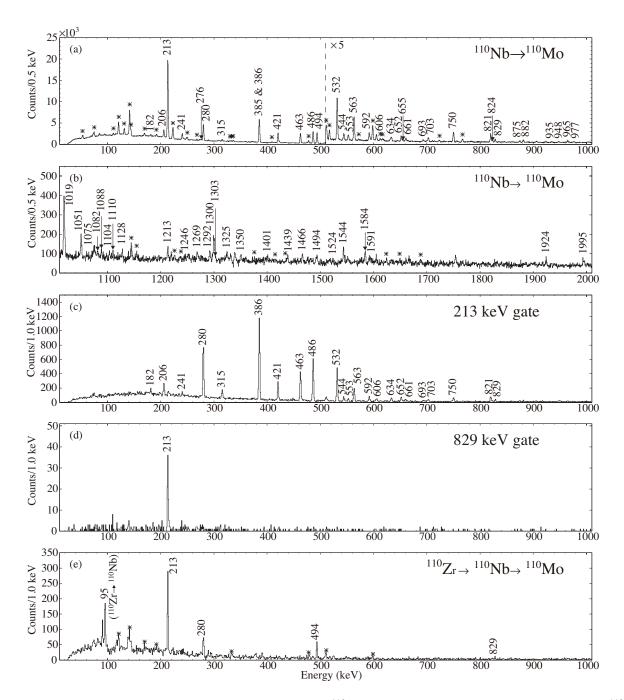


FIG. 6. (a–b) The β -delayed γ -ray spectrum of the implanted ¹¹⁰Nb. The time window after the implantation of ¹¹⁰Nb was set to be less than 400 ms. The labeled peaks belong to 110 Mo. The identified background peaks are marked with asterisks. (c-d) The coincidence spectra gated on 213.4 keV and 828.8 keV. (e) The β -delayed γ -ray spectrum obtained from the β -decay chain $^{110}\text{Zr} \rightarrow ^{110}\text{Nb} \rightarrow ^{110}\text{Mo}$, where $\Delta t_{\beta-\text{ion}}$ from 30 to 250 ms was selected.

₅₂₁ daughter populated by the decay of a parent. The half-₅₂₉ second β -decaying state in ¹¹⁰Nb. The previous values 522 life of the low-spin state in ¹¹⁰Nb was determined to be 530 of 82(4) ms [34] and 82(2) ms [46] appear to be a reason-523 94(9) ms by considering the daughter-decay component 531 able average of the presently reported low- and high-spin ₅₂₄ and the constant background. The half-life of ¹¹⁰Zr, used ₅₃₂ states. 525 in the fitting, was determined to be 37.7(31) ms from the 533 The absolute γ -ray intensities for the low-spin state in 526 decay curve of the 90.5- and 95-keV γ rays associated 534 110 Nb were determined as follows. The β decay of 110 Nb with the 110 Zr decay. The half life of previous measure—which followed the emission of a 95-keV γ ray from the

520 curve shown in Fig. 3 (d) shows the typical shape of a 528 ments was determined without any consideration of the

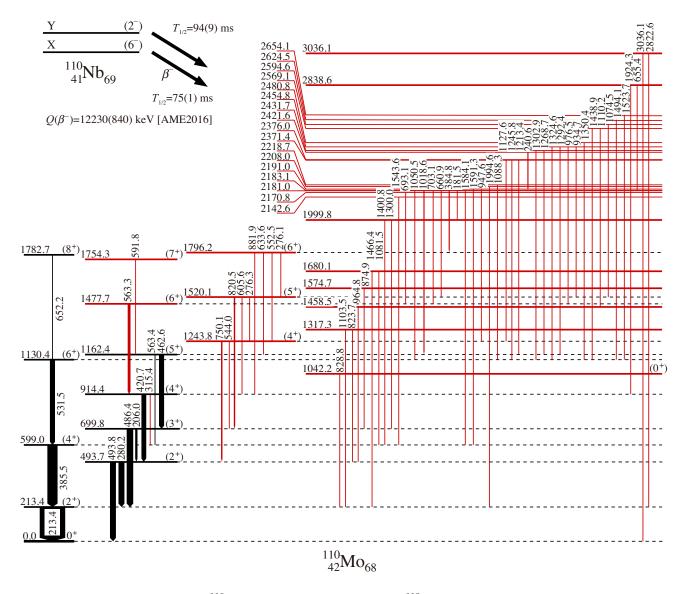


FIG. 7. The proposed level scheme of 110 Mo obtained from the β -decay of 110 Nb isotopes implanted into WAS3ABi. Red lines are the new levels and transitions.

TABLE IV: Same as Table II, but for the 110 Mo results obtained from the β decay of the implanted 110 Nb. (high) indicates the β decay of the high-spin state in 110 Nb. The low-spin contribution was subtracted by combining with the results in Table V and the assumption that the 0^+ states at 0 and 1042.2 keV are populated only from the low-spin β decay. (1UF) is for the first unique forbidden transition from 6^- to 4^+ or 8^+ states.

$E_i(\text{keV})$	J^{π}	$E_{\gamma}({\rm keV})$	$I_{\gamma}{}^{a}$ (Nb \rightarrow Mo)	$I_{\gamma}{}^{b} \ ext{(high)}$	$I_{eta}(\%)^c \ ext{(high)}$	$\log ft$ (high)	$\log ft$ (high)
			(110 /110)	(111811)	(8)	(allowed/non-UF)	(1UF)
0.0	0^+				0		
213.4(2)	(2^{+})	213.4(2)	100.0(5)	100(11)	< 1.5		
493.7(1)	(2^{+})	280.2(2)	23.5(4)	21.6(33)	-5.4(45)		
		493.8(2)	23.1(3)	18.9(38)			
599.0(2)	(4^{+})	385.5(2)	39.0(7)	52.7(14)	6.2(16)	5.9(2)	8.5(3)
699.8(1)	(3^{+})	206.0(2)	8.5(2)	$11.3(3)^e$	1.5(6)	6.5(2)	
		486.4(2)	26.2(3)	34.9(8)			

TABLE IV: (continued)

$E_i(\text{keV})$	J^{π}	$E_{\gamma}(\text{keV})$	$I_{\gamma}{}^{a}$ (Nb \rightarrow Mo)	$I_{\gamma}{}^{b}$ (high)	$I_{eta}(\%)^c$ (high)		$\log ft$ (high)
						(allowed/non-UF)	(1UF)
914.4(2)	(4^{+})	420.7(2)	18.8(3)	27.0(4)	4.8(15)	6.0(2)	8.5(3)
		315.4(2)	2.9(2)	4.2(3)			
1042.2(2)	(0^{+})	828.8(2)	1.8(1)	0	0		
1130.4(3)	(6^{+})	531.5(2)	19.7(3)	28.3(4)	8.2(20)	5.7(2)	
1162.4(2)	(5^{+})	462.6(2)	19.7(3)	28.3(4)	6.5(17)	5.8(2)	
		563.4(3)	1.8(4)	2.6(6)			
1243.8(1)	(4^{+})	544.0(2)	2.9(2)	4.2(3)	3.5(9)	6.1(2)	8.5(3)
		750.1(2)	5.9(2)	8.5(3)			
1317.3(2)		823.7(2)	1.3(1)	1.9(1)	1.4(3)	6.5(2)	
		1103.5(3)	0.5(1)	0.7(1)			
1458.5(2)		964.8(2)	1.1(1)	1.6(1)	0.5(2)	6.9(2)	
1477.7(2)	(6^{+})	563.3(2)	10.0(10)	14.4(14)	4.8(14)	5.9(2)	
1520.1(2)	(5^{+})	276.3(3)	0.3(4)	0.4(6)	3.8(11)	6.0(2)	
		605.6(2)	2.9(2)	4.2(3)			
		820.5(2)	4.9(2)	7.0(3)			
1574.7(3)		874.9(3)	0.9(1)	1.3(1)	0.7(2)	6.7(2)	
1680.1(2)		1081.5(3)	0.4(1)	0.6(1)	0.9(2)	6.6(2)	
		1466.4(3)	0.8(1)	1.2(1)			
1754.3(3)	(7^{+})	591.8(2)	3.3(3)	4.7(4)	2.5(7)	6.1(2)	
1782.7(3)	(8^{+})	652.2(2)	2.8(2)	4.0(3)	2.2(5)	6.2(2)	8.6(3)
1796.2(1)	(6^{+})	276.1(3)	0.8(4)	1.2(6)	1.7(7)	6.3(2)	
		552.5(2)	2.7(2)	3.9(3)			
		633.6(2)	2.1(2)	3.0(3)			
		881.9(2)	1.6(1)	2.3(1)			
1999.8(2)		1300.0(2)	2.3(2)	3.3(3)	0.5(3)	6.8(3)	
		1400.8(4)	0.3(1)	0.4(1)			
2142.6(3)		1543.6(2)	1.6(2)	2.3(3)	1.2(3)	6.4(2)	
2170.8(3)		693.1(2)	0.9(1)	1.3(1)	0.7(2)	6.6(2)	
2181.0(1)		181.5(2)	1.9(2)	2.7(3)	10.1(25)	5.4(2)	
		384.8(2)	5.0(6)	7.2(9)			
		660.9(2)	1.4(1)	2.0(1)			
		703.1(2)	2.4(1)	3.5(1)			
		1018.6(2)	5.0(2)	7.2(3)			
0109 1/9)		1050.5(2)	1.6(1)	2.3(1)	0.4(9)	C O(2)	
$2183.1(3) \\ 2191.0(3)$		$1584.1(2) \\ 947.6(3)$	1.4(2)	2.0(3)	0.4(2)	6.8(3) $6.4(2)$	
2191.0(3)		1591.3(4)	0.6(1) $0.7(2)$	0.9(1) $1.0(3)$	1.0(3)	0.4(2)	
2208.0(4)		1994.6(3)	0.7(2) $0.8(1)$	1.0(3) $1.2(1)$	0.6(2)	6.6(2)	
2208.0(4) $2218.7(4)$		1994.0(3) $1088.3(3)$	0.5(1) $0.5(1)$	0.7(1)	0.0(2) $0.4(1)$	6.8(2)	
2371.4(4)		1127.6(3)	0.6(1)	0.7(1) $0.9(1)$	0.4(1) $0.5(1)$	6.7(2)	
2376.0(3)		1213.4(3)	0.9(1)	1.3(1)	0.9(1)	6.4(2)	
		1245.8(3)	0.3(1)	0.5(1)	(-)	~·-(-)	
2421.6(2)		240.6(2)	4.2(7)	6.0(10)	3.2(9)	5.9(2)	
2431.7(3)		1268.7(3)	0.7(1)	1.0(1)	0.8(2)	6.5(2)	
· /		1302.9(6)	0.4(1)	0.6(1)	()	· /	
2454.8(2)		934.7(3)	0.5(1)	0.7(1)	2.0(5)	6.1(2)	

TABLE IV: (continued)

$E_i(\text{keV})$	J^{π}	$E_{\gamma}({ m keV})$	$I_{\gamma}{}^{a}$ (Nb $ ightarrow$ Mo)	$I_{\gamma}{}^{b} \\ (\text{high})$	$I_eta(\%)^c \ ext{(high)}$	$\begin{array}{c} {\rm log}ft\\ {\rm (high)}\\ {\rm (allowed/non-UF)} \end{array}$	
		976.5(3)	0.4(1)	0.6(1)			
		1292.4(2)	1.0(1)	1.4(1)			
		1324.6(3)	0.7(1)	1.0(1)			
2480.8(4)		1350.4(3)	0.7(1)	1.1(1)	0.5(2)	6.7(3)	
2569.1(3)		1110.2(3)	0.4(1)	0.6(1)	0.8(2)	6.5(2)	
		1438.9(3)	0.6(1)	0.9(1)			
2594.6(5)		1074.5(5)	0.4(1)	0.6(1)	0.3(1)	6.9(2)	
2624.5(4)		1494.1(3)	0.9(3)	1.3(4)	0.7(3)	6.5(3)	
2654.1(4)		1523.7(3)	0.6(1)	0.9(1)	0.5(1)	6.6(2)	
2838.6(2)		655.4(2)	0.9(1)	1.3(1)	1.4(4)	6.2(2)	
		1924.3(3)	0.9(2)	1.3(3)			
3036.1(2)		2822.6(3)	1.1(1)	1.6(1)	2.1(5)	5.9(2)	
		3036.1(3)	1.6(2)	2.3(3)			

- ^a The absolute intensity per 100 β -decays is $0.492(25)I_{\gamma}$.
- ^b The absolute intensity per 100 β-decays is $0.54(19)I_{\gamma}$.
- ^c Internal conversion coefficients [39] were adopted for two transitions with 213.4 and 206.0 keV.
- ^e Branching ratio of the 206.0- and 486.4-keV transitions and $I_{\gamma}(486.4 \text{ keV})$ in Table V were used to subtract the low-spin β decay contribution.

536 decay of ¹¹⁰Zr was analyzed using the observation of the 563 213.4 and 493.8 keV, which decay directly to the ground $_{557}$ 95-keV γ ray as time zero. The observation of the 213.4- $_{564}$ state. The conversion-electron coefficients were taken $_{538}$, 280.2-, and 493.8-keV γ rays shows that the low-spin $_{565}$ into account. This sum includes unobserved small I_{eta} state in 110 Nb is selected by the gate on the 95-keV γ ray. 566 contributions with cascade transitions through the 2_1^+ 540 The ratio of the number of the measured β decays and 567 and 2_2^+ states. The same method was applied to the β - $_{541}$ 213.4-keV γ rays was determined from this subsequent β - $_{568}$ decay results of the implanted 110 Nb. The contribution of

tion from the results given in Table V under the assump- 574 the low-spin state in the implanted 110Nb as, tion that the ground and second 0⁺ states are directly populated only by the low-spin β decay. The I_{β} values for low- and high-spin β decays were determined and are summarized in Tables IV and V.

The I_{β} value of the $^{110}{
m Mo}$ ground state corresponding $_{553}$ to the low-spin state and P_n values corresponding to the low- and high-spin states were determined by combining 555 the following five equations. First, the P_n value has a relation to $I_{\beta}(E_i)$ for the γ -decaying states at the energy 557 E_i and $I_{\beta}(0)$ for the ground state as,

$$\sum I_{\beta}^{L}(E_i) + I_{\beta}^{L}(0) + P_n^{L} = 100\%, \tag{4}$$

$$\sum I_{\beta}^{H}(E_i) + P_n^{H} = 100\%, \tag{5}$$

 $_{558}$ where \sum represents the sum over all excited states de- $_{559}$ caying to the ground state and the superscripts L and H ₅₆₀ represent the low- and high-spin states in ¹¹⁰Nb, respec- ₅₈₃ Here, only the differences from Sec. III C are de-561 tively. The $\sum I_{\beta}^{\rm L}(E_i)$ value was evaluated as 58(20)% 584 scribed. The 213.4-keV γ ray was used for the iden-562 by the sum of the two absolute transition intensities of 585 tification of the 110 Nb \rightarrow 110 Mo decay. The number

decay analysis. The conversion factor from I_{γ} to absolute the 3036.1-keV transition was also added. The obtained intensity was determined to be 0.41(14) using the 213.4- the V γ ray. The conversion factor from I_{γ} to absolute the 3036.1-keV transition was also added. The obtained the γ ray ray. The conversion factor from I_{γ} to absolute the 3036.1-keV transition was also added. The obtained to be 0.41(14) using the 213.4- to 3036.1-keV transition was also added. The obtained to be 0.41(14) using the 213.4- to 3036.1-keV transition was also added. The obtained to be 0.41(14) using the 213.4- to 3036.1-keV transition was also added. The obtained to be 0.41(14) using the 213.4- to 3036.1-keV transition was also added. The obtained to 500 the conversion factor from I_{γ} to absolute the 3036.1-keV transition was also added. The obtained 500 the 500 t The I_{γ} values corresponding to the high-spin state $_{572}$ L+H refers to the β decay of the implanted 110 Nb. The were determined by subtracting the low-spin contribu- $_{573} \sum I_{\beta}^{\rm H}(E_i)$ value was described by using the fraction r of

$$\sum I_{\beta}^{\text{L+H}}(E_i) = r \sum I_{\beta}^{\text{L}}(E_i) + (1-r) \sum I_{\beta}^{\text{H}}(E_i). (6)$$

₅₇₅ From the assumption that the 828.8-keV γ ray is emitted 576 only from the β decay of the low-spin state, r was given

$$r = \frac{I_{\gamma, \text{abs}}^{\text{L+H}}(828.8 \text{ keV})}{I_{\gamma, \text{abs}}^{\text{L}}(828.8 \text{ keV})} = 0.36(15), \tag{7}$$

where $I_{\gamma,abs}(828.8 \text{ keV})$ is the absolute intensity of the 579 828.8-keV γ ray.

(4) 580 From the data of the $^{110}{\rm Nb} \to ^{110}{\rm Mo} \to ^{110}{\rm Tc}$ decay (5) 581 chain, the $P_{0n}^{\rm L+H}$ value can be determined following the 582 procedure described in Sec. III C. It is given by

$$1 - P_{0n}^{L+H} = rP_n^L + (1 - r)P_n^H, \tag{8}$$

TABLE V. Same as Table II, but for the 110 Mo results obtained from the β -decay chain 110 Zr \rightarrow 110 Nb \rightarrow 110 Mo, where the low-spin state in ¹¹⁰Nb is populated by the β decay of the 0⁺ ground state in ¹¹⁰Zr. (1UF) is for the first unique forbidden transition from 2^- to 0^+ or 4^+ states.

$E_i \text{ (keV)}$	J^{π}	$E_{\gamma} \; (\text{keV})$	$I_{\gamma}{}^{\mathrm{a}}$	$I_eta(\%)$	$\log ft$	$\log ft$
		(low)	(low)	(low)	(low)	(low)
					(allowd/non-UF)	(UF)
0.0	0^{+}			47(26)	5.2(3)	7.8(4)
213.4	(2^{+})	213.4	100(4)	25.0(88)	5.5(2)	
493.7	(2^{+})	280.2	28.0(24)	25.0(87)	5.4(2)	
		493.8	33.0(27)			
599.0	(4^{+})	385.5	7.0(13)	2.9(11)	6.4(2)	8.9(3)
699.8	(3^{+})	486.4	6.0(4)	2.5(9)	6.4(2)	
1042.2	(0^{+})	828.8	6.0(15)	2.5(10)	6.3(2)	8.8(3)

^a The absolute intensity per 100 β decays is 0.41(14) I_{γ} .

 $_{590}$ 18(4)% were determined.

ing values were determined as $P_n^{\rm L} = -5(41)\%$, $P_n^{\rm H} =$ 593 31(15)%, $I_{\beta}^{L}(0) = 47(26)\%$, and $\Sigma I_{\beta}^{H}(E_{i}) = 69(15)\%$. Since the $P_n^{\rm L}$ value must be positive, an upper limit is given as $P_n^{\rm L} < 36\%$. The large uncertainties were prop-₅₉₆ agated mainly from the uncertainty of $I_{\gamma,abs}^{L}(828.8 \text{ keV})$. 597 The separate P_n determination of the low- and high-spin 598 states was made for the first time in the $^{110}{
m Nb}$ $\widetilde{\beta}$ decay. The previous P_n^{L+H} value of 40(8)% [43] is larger than the present result. In the previous work, ¹¹⁰Nb was produced by bombarding a U target with a 50 MeV H₂⁺ beam. The $_{602}$ low-spin fraction r may be different due to the different 603 production reaction and energy.

The $\log ft$ values were determined from the half-lives, 605 I_{β} and $Q_{\beta} = 12230(840)$ keV [33] for the low- and high-606 spin states, (as summarized in Tables IV and V), respec-607 tively. The excitation energy in ¹¹⁰Nb was not taken into 608 account, which would be negligible in comparison with its 609 Q_{β} .

 $_{611}$ is discussed. Positive-parity states with spins ranging $_{647}$ γ ray corresponding to the $2^+_1 \rightarrow 0^+_1$ transition in the $_{612}$ from 0 to 4 are populated by the β decay of the low- $_{648}$ LaBr₃(Ce) detector array. Figure 8 shows the time- $_{613}$ spin 110 Nb. Because this decay pattern and the $\log ft$ $_{649}$ difference distributions for the three nuclei and Fig. 9 values are similar to the 108 Nb decay, the spin-parity of $_{650}$ shows the corresponding γ -ray spectra with the regions the low-spin 110 Nb is assigned to be 2^- . The log ft values $_{651}$ used to make the time spectra highlighted in gray. The $_{616}$ of 0^+ and 4^+ states were recalculated as the first unique $_{652}$ time spectra show a clear single exponential decay on forbidden transition to be 7.8(4), 8.8(3), and 8.9(3) for $_{653}$ a very low background. The γ -ray spectra in Fig. 9 do $_{618}$ 0_1^+ , 0_2^+ , and 4_1^+ , respectively. These are consistent with $_{654}$ not show any evidence for delayed feeding of the 2_1^+ state the typical range from 8 to 11 [40].

 $_{621}$ sible to interpret the $\log ft$ values of both the 3^+ and $_{657}$ ps [9]. Its effect can be ignored, since the lifetime is 622 8⁺ states, even if the first unique forbidden transition 658 one order of magnitude smaller than the time resolution 623 is considered. Because the I_{β} to the 3⁺ state, 1.5(6), 659 of 0.61 ns at 200 keV. The lifetimes of the 2_1^+ states 624 is smaller than the other states, missing feedings from 660 were determined from fitting the slope with a single ex-

 $_{586}$ of the 110 Mo β decay was obtained using the 121.0- $_{625}$ higher excited states may cause a significant deviation 587 keV γ ray emitted from 110 Tc. From R(121.0 keV) = 626 from the actual log ft. On the other hand, it is reason- $_{588}$ 0.0375(16), N_{γ} (121.0 keV) = 2.279(44) × 10⁴, and $_{627}$ able that the 8⁺ state, which is the largest spin among $_{589}$ N_{β} ($_{10}^{10}$ Nb) = 7.39(7)×10⁵, P_{0n}^{L+H} = 82(4)% and P_{n}^{L+H} = $_{628}$ the measured states, is directly populated. Therefore, the 629 3⁺ state is considered to be mainly fed from the higher Based on the above values and Eqs. (4–8), the remain- 630 excited states. The logft values of the 4^+ , 5^+ , 6^+ , 7^+ , and 8⁺ states are in the range from 5.7 to 6.3. This case 632 is similar to the situation above. When the spin-parity of $_{633}$ the high-spin state in 110 Nb is 6^- , the transitions to 4^+ or 8⁺ states become the first unique forbidden transition. The recalculated $\log ft$ values, 8.5(3), 8.5(3), 8.5(3) and 636 8.6(3) for the 4_1^+ , 4_2^+ , 4_3^+ , and 8_1^+ states, respectively, are 637 consistent with the typical range. For the other positive $_{638}$ parity states, the $\log ft$ values are consistent with the first $_{639}$ non-unique forbidden transitions from the 6^- state. As 640 a result, the spin-parity of the high-spin state is assigned $_{641}$ to be 6^- .

F. Lifetime measurement of 2_1^+ states in 106,108,110 **Mo**

The mean lifetimes, τ , of the 2_1^+ states in 106,108,110 Mo 645 were measured from the time between the observation First, the spin-parity of the low-spin state in $^{110}{\rm Nb}$ $_{646}$ of a β particle in a plastic scintillation detector and a the typical range from 8 to 11 [40]. from higher-lying states and indeed, the lifetime of the 4^+_{55} from higher-lying states and indeed, the lifetime of the 4^+_{113} for the β decay from the high-spin state, it is impos- β state in β was recently measured as $\tau = 29.7^{+11.3}_{-9.1}$

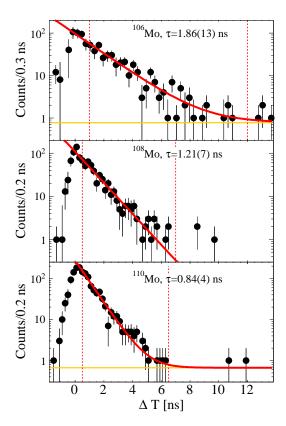


FIG. 8. The time spectra of $2_1^+ \rightarrow 0_1^+ \gamma$ -ray transition in 106 Mo, 108 Mo, and 110 Mo. ΔT is the time from β -particle detection by the plastic scintillator to γ -ray detection by the LaBr₃(Ce) array. The solid red lines are the best-fit curves using an exponential function and fixed constant background to the region indicated by the dashed red lines. The constant backgrounds, shown by the orange lines, were determined by fitting the region of 15 < ΔT < 25 ns, 10 < ΔT < 25 ns, and 8 < ΔT < 25 ns for 106 Mo, 108 Mo, and 110 Mo, respectively.

661 ponential function and a constant background, yielding $_{662} \tau = 1.86(13), 1.21(7), \text{ and } 0.84(4) \text{ ns for } ^{106}\text{Mo}, ^{108}\text{Mo},$ and ¹¹⁰Mo, respectively. The previously reported results 664 for ¹⁰⁶Mo are 0.54(8) [47, 48], 1.08(22) [49], 1.73(24) [50], and 1.93(14) ns [51]. The present lifetime ($\tau = 1.86(13)$ 666 ns) is consistent with the values in Refs. [50, 51]. The result of $\tau = 1.21(7)$ ns for ¹⁰⁸Mo is consistent with the 668 previously reported value of 0.72(43) ns [21] but pro-669 vides a smaller uncertainty. The measurement for ¹¹⁰Mo 670 was made for the first time. The systematic trend of $_{671}$ $B(E2;2_1^+ \rightarrow 0_1^+)$ values in the Mo isotopes is shown in 672 Fig. 10. The present results with small uncertainties show that the B(E2) value is nearly unchanged between 692 ₆₇₄ the neutron numbers N=62 and 66, and drops slightly ₆₉₃ against γ vibration, a γ -unstable rotor, or a rigid triaxial 675 at N = 68.

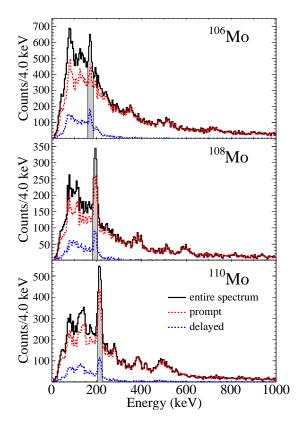


FIG. 9. The γ -ray energy spectra of the LaBr₃(Ce) array. The energy region used to make the time spectra of Fig. 8 are highlighted with gray. The prompt, $|\Delta T| < 1$ ns, and delayed, $\Delta T > 1$ ns, components are shown by the red and blue dotted lines, respectively.

DISCUSSION

Quadrupole deformation of ground state in $^{106,108,110}{\rm Mo}$

677 678

The ground-state band is described as the rotational 680 motion of a deformed nucleus. The quadrupole deformation parameter β was obtained from the $B(E2; 2_1^+ \to 0_1^+)$ 682 values using the formula given in the review paper [48] $_{683}$ as 0.349(13), 0.327(10), and 0.305(7) for ^{106}Mo , ^{108}Mo , and ¹¹⁰Mo, respectively. Figure 11 shows the neutron-686 number dependence of β for Mo and Zr isotopes. While the Zr isotopes have a clear peak structure at N=64and reach $\beta = 0.46(1)$, the Mo isotopes have almost constant $\beta \sim 0.32$ between N=60 and 68. A comparison 690 with microscopic calculations is described in Sec. IV E.

Triaxial motion in 2^+_2 band

The low-lying 2^+_2 state is a signature of a softness 694 rotor. The three models are distinguished by means of

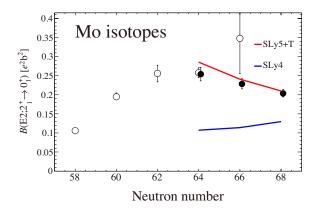


FIG. 10. Experimental and theoretical $B(E2; 2_1^+ \rightarrow 0_1^+)$ values of the even-even Mo isotopes. The experimental values were calculated by the use of the relation in Ref. [52]. The open circles are taken from Ref. [48]. The theoretical values were calculated using the five-dimensional collective Hamiltonian with the pairing-plus-quadrupole interaction parameters determined from the two kinds of the Skyrme-interaction parameters (SLy5+T and SLy4).

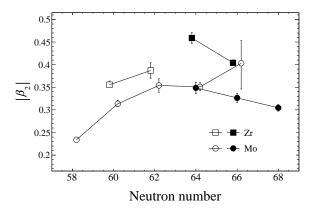


FIG. 11. Quadrupole deformation parameter β for Zr (square) and Mo (circle) isotopes. Filled circles are the present results for the Mo isotopes. Filled squares for the Zr isotopes are the results from the same data set [53], but the values were recalculated from $B(E2; 2_1^+ \to 0_1^+)$ by using the formula given in the review paper [48]. Open circles and squares are taken from the review paper [48] and a later work [54].

the energy staggering of the 2_2^+ band [1]:

$$\frac{E_s(J)}{E(2_1^+)} = \frac{\Delta E_J - \Delta E_{J-1}}{E(2_1^+)},\tag{9}$$

where $\Delta E_J = E_{\gamma}(J) - E_{\gamma}(J-1)$, and $E_{\gamma}(J)$ is the 736 a significant neutron contribution to make a shallow po-697 energy of the 2_2^+ band member with the spin J. The 737 tential minimum at a finite γ . $_{698}$ $E_s(4)/E(2_1^+)$ value of the γ -vibrational band is close to $_{738}$ For the γ -vibrational band, the kinematic moment of 700 rotational energies are described approximately as the 740 ground band. Figure 14 shows the kinematic MoI of the ₇₀₁ axially-symmetric rigid rotor. At maximum triaxiality ₇₄₂ ground and 2^+_2 bands up to J=10. The newly discovered $_{702}$ ($\gamma=30^{\circ}$) of a rigid-triaxial rotor in the Davydov model, $_{743}$ levels in the $\bar{K}=2$ band of 110 Mo extended the kinematic ₇₀₃ it becomes 5/3 [2]. Another extreme case of γ -unstable ₇₄₄ MoI up to J=7. The similar evolution of the kinematic ₇₀₄ nuclei in the Wilets-Jean model [3] yields -2. Figure ₇₄₅ MoI between these two bands supports the interpretation

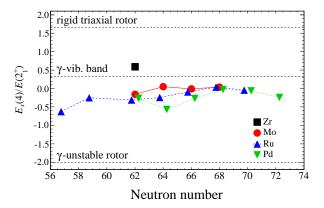


FIG. 12. The $E_s(4)/E(2_1^+)$ ratio around neutron-rich A=110. The black-dashed lines represent the ideal values of three models; rigid-triaxial rotor, γ -unstable rotor, and γ vibrational band. Filled square, circles, triangles and inverted triangles represent Zr, Mo, Ru, and Pd isotopes, respectively.

705 12 shows the $E_s(4)/E(2_1^+)$ ratio around the neutron-rich $_{707}$ A=110 region. The Mo, Ru, and Pd isotopes have simi- $_{708}$ lar values in the range from -0.5 to +0.1, which is below ₇₀₉ the 1/3 of the γ vibrational band. A larger value of $^{102}{\rm Zr}$ 710 than other isotopes suggests that ¹⁰²Zr has the steeper potential towards the γ direction.

Figure 13 shows the $E_s(J)/E(2_1^+)$ ratio as a function of J for the Mo, Ru, and Pd isotopes. The difference among the isotopes is more apparent than in Fig. 12. The J-dependence of $E_s(J)/E(2_1^+)$ is shown to have a relation to the triaxial motion from the calculation using the Bohr Hamiltonian with a γ -dependent potential [4]. While the γ -vibrational band shows a flat pattern, γ_{20} the γ -soft and the rigid triaxial rotors show a staggering pattern with low values at even and odd J, respectively. The flat pattern of the ^{106,108,110}Mo isotopes indicates $_{723}$ that the excitation energies are explained by the rota-724 tional bands built on a γ -vibrational 2_2^+ state with the 725 axially-symmetric deformed shape and quantum number $_{726}$ K=2. On the other hand, the staggering pattern of the 727 Pd isotopes with $N \leq 66$ indicates a γ -soft rotor. The 728 Ru isotopes show an intermediate behavior. The stag-729 gering pattern of the Pd isotopes suddenly disappears at $_{730}$ N = 68. Especially at J > 6, a slight staggering in the 731 opposite direction is observed. It is observed that the ₇₃₂ three isotopes with N = 68 show a similar staggering 733 pattern to each other. This staggering is enhanced for ₇₃₄ 112 Ru. The staggering pattern at N=68 might indicate 735 the onset of a very weak triaxial shape and might show

1/3, which is given by the $J(J+1)-K^2$ rule if the 739 inertia (MoI) is expected to be similar to that of the

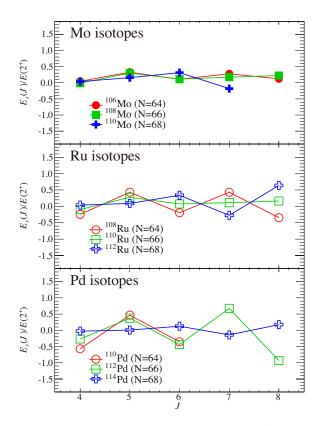


FIG. 13. The staggering pattern of $E_s(J)/E(2_1^+)$. The flat pattern indicates the γ -vibrational band, while the staggering pattern with low values at even and odd J indicates the γ -soft and rigid triaxial rotor, respectively, [4].

TABLE VI. The experimental and theoretical B(E2) ratios. The M1/E2 mixing ratio of $\delta = 6.2^{+1.0}_{-0.8}$ [56] was used for 106 Mo. A pure E2 transition was assumed for 108 Mo and 110 Mo. The theoretical calculation using the SLy5+T interaction is given.

	Alaga	$^{106}\mathrm{Mo}$	$^{108}\mathrm{Mo}$	$^{110}\mathrm{Mo}$
$\frac{B(\text{E2}; 2_2^+ \to 2_1^+)}{B(\text{E2}; 2_2^+ \to 0_1^+)_{\text{exp.}}}$		4.5(6)	8.3(6)	17.3(4)
$\frac{B(\text{E2}; 2_2^+ \to 2_1^+)}{B(\text{E2}; 2_2^+ \to 0_1^+)}_{\text{th.}}$	1.43	2.0	4.9	14.0

of a γ -vibrational band.

 749 B(E2) ratio is given as 1.43 by the Alaga rule [55], where 771 that the $K^{\pi}=4^{+}$ band head is a collective excitation $_{750}$ the rotational and vibrational motions for the axially- $_{772}$ rather than a two quasiparticle state. symmetric shape are well decoupled. The experimental $_{773}$ $_{752}$ B(E2) ratios shown in Table VI are clearly larger than the $_{774}$ the context of a two-phonon γ vibration [13]. The ra-754 Alaga value. For the γ -vibrational band, the enhance-775 tio of the lowest $K^{\pi}=4^+$ and 2^+ band-head energies 755 ment can be explained by the rotation-vibration coupling 776 is 2.02, which is close to the 2.0 value for a harmonic 756 model which introduces the Coriolis mixing between two 777 vibrator. The reduced transition probabilities of the inbands with $\Delta K = 2$ [1]. In Sec. IV E, the B(E2) ratio is 778 terband transition between $K^{\pi} = 2^{+}$ and 4^{+} bands were 758 compared with beyond-mean-field calculations.

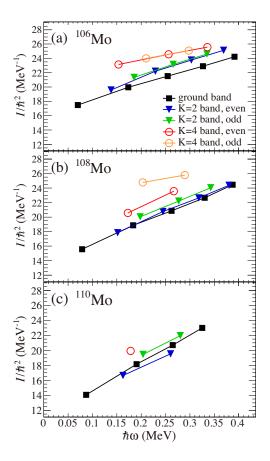


FIG. 14. The kinematic moment of inertia for the ground band (black line with filled squares), $K^{\pi} = 2^{+}$ band (blue line with filled triangles for even J and green line for odd J), and $K^{\pi} = 4^{+}$ band (red line with open circles for even J and orange line for odd J) in (a) 106 Mo, (b) 108 Mo, and (c) 110 Mo.

Candidate of two-phonon γ band

The $K^{\pi} = 4^{+}$ band in ¹¹⁰Mo has the lowest band-761 head energy of 1244 keV among the neutron-rich Mo iso-762 topes. A potential two-quasiparticle state with $K^{\pi}=4^{+}$ 763 would appear around or above the pairing gap. How-764 ever, the observed energy is well below $2\Delta_p \sim 3.4~{
m MeV}$ and $2\Delta_n \sim 2.5$ MeV for the proton and neutron pairs, 766 respectively, which are calculated from the atomic mass representation AME2016 [33]. A $K^{\pi} = 4^{+}$ band, decaying to $_{768}$ the γ band, is known in many neighboring nuclei, such $_{769}$ as $^{104,106,108}{\rm Mo},$ and $^{108,110,112,114,116}{\rm Ru}$ [34, 57]. The The ratio $B(E2; 2_2^+ \rightarrow 2_1^+)/B(E2; 2_2^+ \rightarrow 0_1^+)$ pro- ⁷⁶⁹ as ^{104,106,108}Mo, and ^{108,110,112,114,116}Ru [34, 57]. The vides additional information about the 2_2^+ band. The ⁷⁷⁰ systematical observations of the $K^{\pi} = 4^+$ state indicate

> The $K^{\pi}=4^{+}$ band in $^{106}\mathrm{Mo}$ has been discussed in 779 compared with those between $K^{\pi} = 0^{+}$ and 2^{+} bands,

₇₈₀ and were consistent with the relation of the one-phonon ₈₃₅ late shape with $\beta \sim 0.35$ and $\gamma = 0^{\circ}$, while the SLy4 $_{781}$ and two-phonon excitations. The ratio of the band-head $_{836}$ interaction predicts an oblate shape with $\beta\sim0.2$ and relation energies changes gradually as 1.95, 2.02, 2.43, and 2.52 surgest $\gamma = 60^{\circ}$. For the comparison with the experimental re-⁷⁸³ for ¹⁰⁴Mo, ¹⁰⁶Mo, ¹⁰⁸Mo, and ¹¹⁰Mo, respectively. The ⁸³⁸ sults, the $B(E2; 2_1^+ \rightarrow 0_1^+)$ value was used instead of β . ⁷⁸⁴ kinematic MoI of the $K^{\pi} = 4^+$ band shown in Fig. 14 has ⁸³⁹ The $B(E2; 2_1^+ \rightarrow 0_1^+)$ values were calculated by adopting 785 similar values to those of the ground-state and γ bands. 840 the effective charges, $e_{\pi}=1.5e,$ and $e_{\nu}=0.5e,$ for the ₇₈₆ Thus, the newly discovered $K^{\pi}=4^{+}$ band in ¹¹⁰Mo was ₈₄₁ two major-shell single-particle model space as shown in ₇₈₇ assigned as a candidate of the two-phonon γ vibrational ₈₄₂ Fig. 10. The theoretical values with SLy5+T are roughly 788 band.

D. Second 0⁺ state

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The energies of the 0_2^+ state, 893.4 and 1042.2 keV 790 791 for ¹⁰⁸Mo and ¹¹⁰Mo, respectively, are low enough to indicate a β -vibrational state or shape coexistence rather than two-quasiparticle states, since they are well below the pairing gaps, $2\Delta_p$ and $2\Delta_n$, given in Sec. IV C. The energies are similar to those of other Mo isotopes, which range from 695 keV to 886 keV between ⁹⁸Mo and ¹⁰⁴Mo, respectively [34].

The 1158.4-keV 2^+ state in 108 Mo has a similar decay pattern to the 2^+_3 state in 106,108,110 Ru isotopes [34]. The 2_3^+ state in the Ru isotopes decays also to the 0_2^+ state. 801 Although the corresponding γ -ray transition from 1158.4- $_{802}$ keV state to 0^{+}_{2} state in 108 Mo was not observed due to 803 the lack of the sensitivity for $I_{\gamma} < 0.5\%$, the energy dif-804 ference, $E(2_3^+)-E(0_2^+)=265$ keV, is similar to the cases 805 of 402, 273, and 260 keV for 106,108,110 Ru [34], respec-806 tively. Based on these systematic trends, the $1158.4\mbox{-keV}$ state in ¹⁰⁸Mo was tentatively assigned as the member of 865 vibration of the prolate shape. While the band-head en-

810 paring with predictions in Sec. IVE.

Comparison with 5D collective Hamiltonian calculation with microscopic approach

sign single-particle energies in the two-major harmonic oscil- mental results indicate γ vibration in the stiffer potential. ₈₂₀ lator shell model space and interaction strengths, were ₈₈₁ It is noticed that the calculated wave function of the $3\frac{1}{2}$ 821 fitted to the mean-field results obtained with two kinds 882 state is similar to those of the lighter Mo isotopes and in-822 of Skyrme interactions, SLy5+T or SLy4 (see Refs. [58– 883 dicates γ vibration. The characteristics of the wave func-823 60] for details). The Schrödinger equation in the collec-824 tive space was solved to obtain the energies and the col- 885 is even or odd. This is also noticed in the calculations say shown in Fig. 15 for SLy5+T and Fig. 16 for SLy4. The sss pend not only on the prolonged wave function toward the 830 two kinds of theoretical excitation energies are compared 889 γ direction, but also on the difference between the even 832 with the experimental ones in Fig. 17. The PESs show a 890 and odd spins. The odd-spin states cannot mix with the 833 strong dependence on the effective interaction used. The 891 $K^{\pi}=0^+$ component, since the odd-spin states are not

843 double those with SLv4 and agree well with the experimental ones. The energy of 2_1^+ state for the rotational band, which has a strong correlation to B(E2) [52], is an observable closely related to β . The energies of the 847 ground-state band are well reproduced by the calcula-848 tions with SLy5+T, as shown in Fig. 17. The good agree- $_{849}$ ment with the theoretical values using the SLy5+T in- $_{850}$ teraction indicates that the ground state in $^{106,108,110}\mathrm{Mo}$ has a prolate shape. The B(E2) values for SLy5+T shows $_{852}$ an increase at N=64, while the experimental ones are $_{853}$ rather constant. The PES of $^{106}\mathrm{Mo}$ has a gentle slope toward $\beta \sim 0.45$, which may increase β compared with $^{108}\mathrm{Mo.}\,$ Because the largest β was observed at N=64 $_{856}$ in the Zr isotopes [53] and the energy of the 2_1^+ state becomes minimum at N=64 for both isotopes [61], the 858 soft potential toward the large β might be consistent with 859 the experimental results. But a less-soft potential would 860 be necessary for a better agreement.

 861 $\,$ The energies of the 2_2^+ band in $^{106}{\rm Mo}$ are well reproduced by the calculation with SLy5+T. The wave func- $_{863}$ tions of 2^+_{γ} and 3^+_{γ} are localized on a finite γ value, reflect- $_{864}$ ing the dynamical triaxial deformation induced by the γ 866 ergy in ¹⁰⁸Mo is overestimated, the excitation energies The 0_2^+ states of 108,110 Mo will be discussed by com-868 duced and the wave functions show the γ vibration expected from the experimental odd-even staggering. Thus, $_{870}$ the calculations for $^{106}\mathrm{Mo}$ and $^{108}\mathrm{Mo}$ are consistent with 871 the interpretation in Sec. IVB, that is, the rotational $_{872}$ band of the γ vibrational state. On the other hand, the $_{873}$ calculated 2_2^+ band in 110 Mo shows considerable energy Five-dimensional collective Hamiltonian calculations ⁸⁷⁴ staggering. The 3_{γ}^{+} and 5_{γ}^{+} states converge toward the were performed for the low-lying states in ^{106,108,110}Mo. ⁸⁷⁵ 4_{γ}^{+} and 6_{γ}^{+} states, respectively. The degeneracy of these The PES and the kinetic terms (vibrational and rota- 876 states is predicted in the γ -unstable model. The wave tional masses) were microscopically calculated using the $_{877}$ function of 2^+_{γ} is prolonged in the γ direction as expected CHFB+LQRPA approach using pairing-plus-quadrupole 878 in the γ -unstable model. It is caused by the flatness of the (P+Q) interactions whose parameters, such as spherical 879 PES between $\gamma = 20^{\circ}$ and 60° . Conversely, the experilective wave functions of the ground and excited states. 886 with SLy4. It is suggested that the energy staggering The PESs and the collective wave functions squared are 887 with the close degeneracy of $E(3_{\gamma})$ and $E(4_{\gamma})$ might de-834 calculation with the SLy5+T interaction predicts a pro- 892 allowed in the $K^{\pi}=0^+$ band. This means that the ex-

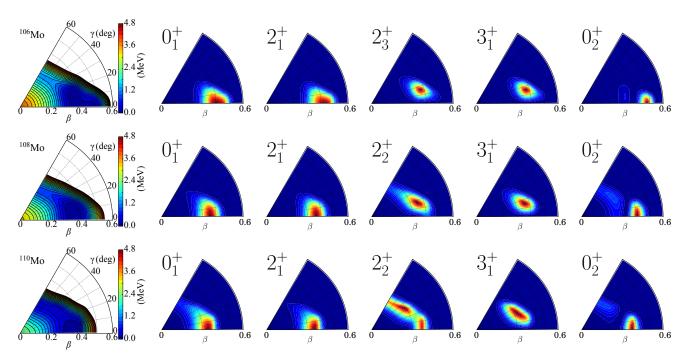


FIG. 15. The potential-energy surface and the collective-wave functions squared (with a factor of β^4) of low-lying states in 106 Mo, and 108 Mo, and 110 Mo. The pairing-plus-quadrupole interaction and spherical single-particle energies used in the CHFB+LQRPA calculations were fitted to the mean-field results obtained with the SLy5+T interaction.

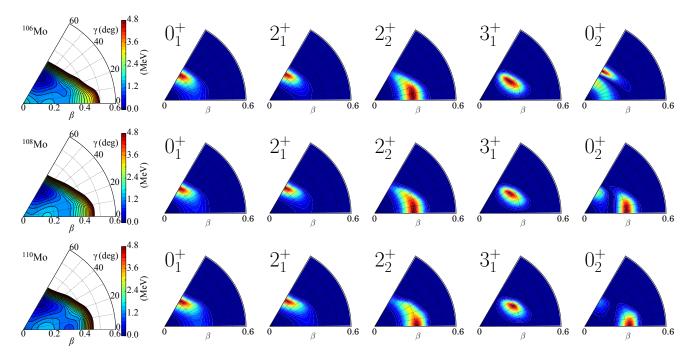


FIG. 16. Same as Fig. 15, but with the SLy4 interaction.

₈₉₄ the mixing with $K^{\pi}=0^+$ bands, which are built on the ₈₉₉ the even- and odd-spin states, and energy staggering that 895 ground state, shape coexistence, shape fluctuation in the 900 deviates from the ideal γ -band energy. 896 β direction around $\gamma = 0^{\circ}$, and any low-lying $K^{\pi} = 0^{+}$ 897 states. The odd-spin states are not very sensitive to them 901

893 cited even-spin states (e.g. 4_2^+) are more influenced by 898 at all. This will result in a qualitative difference between

The quadrupole collective Hamiltonian approach can 902 predict a two-phonon γ vibrational band with $K^{\pi} = 4^+$,

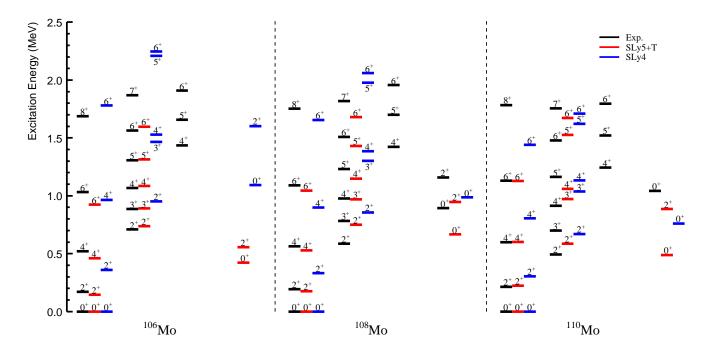


FIG. 17. The experimental and theoretical energies of the low-lying excited states in ¹⁰⁶Mo, ¹⁰⁸Mo, and ¹¹⁰Mo. Black lines present the experimental results, and red and blue lines present the results from the theoretical calculations using SLy5+T and SLy4, respectively.

903 but not two quasiparticle states because it does not in- 934 formation providing a favored origin for the 02 state in 904 clude the quasiparticle degrees of freedom explicitly. As 935 ¹¹⁰Mo. Additional experimental and theoretical works 905 discussed in Sec. IV C, the observed $K^{\pi}=4^{+}$ band is 936 are awaited for further discussions. 906 most likely built on a collective excitation. However, the g_{07} $K^{\pi}=4^{+}$ band was not predicted by the calculations. An 908 ideal two-phonon γ vibrational state has a wave function 937 localized around the prolate minimum. To have a local-910 ized two-phonon $K^{\pi} = 4^{+}$ vibrational state, which has 911 a larger vibrational energy than that of a one-phonon $_{912}$ state, generally the PES along the γ direction has to be 913 deep enough to prevent oblate admixtures. If this is not 914 satisfied, the corresponding two-phonon state will mix 915 with the oblate shape and lose its two-phonon charac-916 ter. The potential barriers in the γ direction from the 917 potential minimum, shown in Fig. 15, are shallow. By 918 increasing in energy by 1 MeV or so from the prolate 919 potential minimum, the other side of the axial symme- $_{920}$ try at $\gamma = 60^{\circ}$ (oblate) is reached. Further theoretical investigations are necessary to reproduce these collective 922 excitations. One of the important improvements for the 5D collective model is to use effective interactions such 924 as modern Skyrme energy density functionals instead of 925 the P+Q Hamiltonian [62].

₉₂₈ tion. On the other hand, the calculation with SLy4 indi- ₉₅₆ state was assigned to be a high-spin $K^{\pi}=4^{-}$ isomeric ₉₂₉ cates the possibility of shape coexistence of prolate and ₉₅₇ state of the GM partner in the $\pi 3/2^-[301] \otimes \nu 5/2^+[413]$ 930 oblate shapes. Since the energy difference between the 958 configuration. 931 0_2^+ and 2_3^+ states in 108 Mo is consistent with the predic- 959 Configuration of 108 Nb: The spin-parity of the 108 Nb 932 tion with SLy5+T, the 0_2^+ state in 108 Mo is suggested to 960 ground-state was assigned to be 2^- , and there was no ₉₃₃ be a β vibrational state. There is no experimental in-₉₆₁ evidence of a β -decaying isomeric state. The single-

Structure of parent nuclei 106,108,110 Nb

Configuration of ^{106}Nb : The spin-parity of the β -939 decaying state in ¹⁰⁶Nb was assigned to be 4⁻, and 940 there were no experimental indications of the existence $_{941}$ of a second $\beta\text{-decaying state}.$ From the prompt $\gamma\text{-}$ 942 ray spectroscopy of the ²⁵²Cf spontaneous fission [63], 943 the spin-parity of the ground state in ¹⁰⁶Nb was as-944 signed as 1⁻. Owing to the relatively strong popula-945 tion of high-spin states in ¹⁰⁶Mo and the fact that no $_{946}$ known γ rays of 106 Nb are observed following the de- 947 cay of $^{106}\mathrm{Zr}$, it is likely that the β -decaying state of 948 $^{106}{\rm Nb}$ is not the 1^- ground state. The configuration 949 of $\pi 3/2^-[301] \otimes \nu 5/2^+[413]$ with $K^\pi=1^-$ was pro-950 posed for the ground state [63]. In the Nilsson dia-951 gram [64], these quasiparticle states are predicted for ₉₅₂ the prolate shape with $\beta \sim +0.35$ measured in ¹⁰⁶Mo. 953 The Gallagher-Moszkowski (GM) rule [65] predicts that The squared wave functions of the 0_2^+ state in 954 the state with the antiparallel spin-coupling becomes a 106,108,110 Mo with SLy5+T indicate β vibrational mo- 955 higher-lying state. Therefore, the observed β -decaying

The spins of the assigned configurations for the low and high- $_{1011}$ figuration was assigned to the β -decaying 2^- state. spin states are written in bold text.

	$\pi 1/2^{+}[431]$	$\pi 5/2^{+}[422]$	$\pi 5/2^{-}[303]$	$\pi 3/2^{-}[301]$
$\nu 5/2^{+}[402]$	$2^{+}/3^{+}$	$5^{+}/0^{+}$	$0^{-}/5^{-}$	$4^{-}/1^{-}$
$\nu 1/2^{+}[411]$	$1^{+}/0^{+}$	$2^{+}/3^{+}$	$3^{-}/2^{-}$	$1^{-}/2^{-}$
$\nu 7/2^{-}[523]$	$3^{-}/4^{-}$	$6^-/1^-$	$1^{+}/6^{+}$	$5^{+}/2^{+}$
$\nu 1/2^-[541]$	$1^{-}/0^{-}$	$2^{-}/3^{-}$	$3^{+}/2^{+}$	$1^{+}/2^{+}$

962 proton and neutron levels in the deformed nucleus 963 were calculated according to the Nilsson diagram [64] 964 and by using the Woods-Saxon potential [66]. A ma-965 jor difference of the level orderings between these two 966 is the negative parity states of the protons. 967 didates of the valence proton and neutron configura1026 state in the Woods-Saxon potential may need to lower in 968 tions were selected based on these two predictions. 1027 energy so as to cross the $\pi 5/2^+[422]$ state at $\beta \sim 0.3$. ⁹⁶⁹ These are, $\pi 1/2^+[431]$, $\pi 5/2^+[422]$, $\pi 5/2^-[303]$, and ¹⁰²⁸ $_{970}$ $\pi 3/2^{-}[301]$ for the proton configuration, and $\nu 1/2^{+}[411]$, $_{971} \nu 5/2^{+}[413]$, and $\nu 1/2^{-}[541]$ for the neutron configura-₉₇₂ tion at around $\beta = +0.33$ for ¹⁰⁸Mo. The spin-parity ¹⁰²⁹ 973 of the $\pi 5/2^{-}[303] \otimes \nu 1/2^{+}[411]$ configuration is 2^{-} and $_{974}$ 3 $^-$ with the antiparallel- and parallel-spin couplings, re- $_{1030}$ 975 spectively. The lower-lying state is the 3⁻ state based 1031 106,108,110 Nb were observed to investigate the shape evo- $_{976}$ on the GM rule. The 2^- state would not form a β - $_{1032}$ lution of 106,108,110 Mo. The neutron-emission probabil-977 decaying isomeric state because of a fast M1 transi- 1033 ity, P_n , of 108 Nb and 110 Nb was determined from the β - $_{979}$ state is not the 2^- state, but the 3^- state. The $2^ _{1035}$ same mass number. The daughter decays of $^{106,108,110}{
m Zr}$ state of the $\pi 3/2^-[301] \otimes \nu 1/2^+[411]$ configuration is also 1036 were used to search for β -decaying isomeric states in the ₉₈₁ antiparallel-spin coupled, therefore the 1^- state with the ₁₀₃₇ Nb isotopes and to increase the statistics of the γ rays parallel-spin coupling would be the β -decaying state. The $_{1038}$ from 106 Mo and 108 Mo. Two β -decaying states with low ₉₈₃ $\pi 5/2^+$ [422] $\otimes \nu 1/2^-$ [541] configuration can generate a β -₁₀₃₉ and high spins were found in the ¹¹⁰Nb β decay. Althe 2⁻ state by a M1 transition. Therefore, the ground 1042 were separately determined for each state. state of 108 Nb was assigned to be the 2^- state with the $_{^{1043}}$ The lifetime of the 2^+_1 state in the Mo isotopes was $\pi 5/2^{+}[422] \otimes \nu 1/2^{-}[541]$ configuration.

observed. The spin-parities were assigned to be 2⁻ and 1046 the energy and lifetime of the 2⁺₁ state. The deforma-6⁻. The quasiparticle states are selected from the Nilsson 1047 tion is almost unchanged with $\beta \sim 0.33$ from the neutron diagram [64] at around $\beta = +0.305$ for ¹¹⁰Mo or the ₁₀₄₈ number N = 62 to 66 and slightly decreases to 0.305(7) single particle levels in the Woods-Saxon potential [66] $_{1049}$ at N=68. The even-odd energy staggering of the 2^{+}_{2} 994 as $\pi 1/2^+[431]$, $\pi 5/2^+[422]$, $\pi 5/2^-[303]$, and $\pi 3/2^-[301]$ 1050 band was evaluated using $E_s(J)/E(2_1^+)$ as a function of 995 for the proton, and $\nu 5/2^-[402]$, $\nu 1/2^+[411]$, $\nu 7/2^-[523]$, 1051 the spin J. The staggering of the ¹⁰⁶Mo, ¹⁰⁸Mo, and configuration coupled with these quasiparticle states are 1053 band. The comparison of kinematic moment of inertia summarized in Table VII.

pling of the $\pi 5/2^+$ [422] $\otimes \nu 7/2^-$ [523] configuration. The 1056 two-phonon γ vibrational band was found well below the 1002 anti-parallel spin coupled 1 state of this configuration, 1057 proton and neutron pairing gaps also in the ¹¹⁰Mo isowhich has a higher energy based on the GM rule, would 1058 tope.

TABLE VII. Candidates of the quasiparticle-state configurations of two β -decaying states in ¹¹⁰Nb. Four quasiparticle states are selected from the Nilsson diagram [64] and the 1006 2 state, there are three candidates as given in Table VII. quasiparticle level in the Woods-Saxon potential [66] for each 1007 Since the spin difference between the GM pair is 1 for all nucleon. The left and right values show the spin-parity of 1008 three candidates, the lower energy state with the parallel the parallel- and antiparallel-spin coupling, respectively. The 1009 spin becomes the β -decaying state. Thus, the parallel parallel-spin coupling state becomes lower-lying state [65]. 1010 spin-coupling state of the $\pi 5/2^+$ [422] $\otimes \nu 1/2^-$ [541] con-

> 1012 The difference between the assigned configurations of 1013 the two β -decaying states is the neutron quasiparticle $^{-}$ 1014 state. It is indicated that the $\nu7/2^{-}[523]$ and $\nu1/2^{-}[541]$ 1015 states are near the Fermi surface and close to each other. 1016 There was no experimental evidence to select the ground state from these two states.

Comparison between Nilsson diagram and single-1019 particle levels in Woods-Saxon potential: The assigned configurations of ¹⁰⁶Nb, ¹⁰⁸Nb, and ¹¹⁰Nb are consistent with the Nilsson diagram given in Ref. [64]. On the other hand, the $\pi 5/2^+$ [422] state in the Woods-Saxon potential 1023 is located below Z = 40 [66], even though it is used in the 1024 configuration of ¹⁰⁸Nb and ¹¹⁰Nb. From comparison with Can- 1025 the Nilsson diagram, it is suggested that the $\pi 3/2^-[301]$

SUMMARY

The delayed γ rays emitted from the β decays of tion to the 3⁻ state. Thus, the expected β -decaying 1034 delayed γ rays emitted from the daughter nuclei with the decaying 2⁻ state with the parallel-spin coupling. The 1040 though the ground state in ¹¹⁰Nb was not assigned from 3^- state with the antiparallel-spin coupling will decay to 1041 these two candidates, the decay properties, including P_n ,

1044 measured by using the fast timing LaBr₃(Ce) array. The Configuration of ^{110}Nb : Two β -decaying states were $_{^{1045}}$ quadrupole deformation parameter was obtained from and $\nu 1/2^{-}[541]$ for the neutron. The spin-parities of the $_{1052}$ 110 Mo isotopes shows the pattern of the γ -vibrational between the ground and 2^+_2 bands supports the inter-The 6^- state is only generated by the parallel-spin cou- 1055 pretation as the γ -vibrational band. A candidate of the

The ground, γ , and two-phonon γ bands were com- 1089 pared to beyond-mean-field calculations. The groundband energies and B(E2) of the 2_1^+ state were reproduced by the calculation with the SLy5+T interaction. The γ band of $^{106}\mathrm{Mo}$ was also reproduced very well. The comparison indicates that the shape is prolate with axial symmetry. However, the even-odd staggering of the γ band 1091 We would like to express our gratitude to the in 110 Mo was not reproduced. The predicted potential 1092 RIKEN Nishina Center accelerator staff for providmight be too shallow toward the triaxial deformation es- 1093 ing a stable and high intensity ²³⁸U primary beam. pecially for ¹¹⁰Mo. This may also be the reason why no ¹⁰⁹⁴ This work was supported by JSPS KAKENHI Grants two-phonon γ bands exist in the theoretical results.

were assigned as the second 0⁺ states, respectively. On 1097 Nos. ST/J000132/1, ST/J000051/1 and ST/K502431/1, the other hand, the transition from the second 0⁺ state 1098 DOE Grant No. previously reported in the β -decay to 106 Mo was shown $_{1099}$ ish Ministerio de Ciencia e Innovación under Contracts

when the first unique forbidden transition was intro-1104 toral Researcher Program. We acknowledge the EUduced. It gave the strong constraint for the spin-parity 1105 ROBALL Owners Committee for the loan of germaassignment of the parent nuclei. The quasiparticle con- 1106 nium detectors and the PreSpec Collaboration for the figurations of the parent nuclei were assigned by referring 1107 readout electronics of the cluster detectors. NH acthe Nilsson diagram for the prolate shape.

ment between the experiment and prediction for ¹¹⁰Mo ₁₁₁₀ ravelling mysteries of r-process." Numerical calculations is enhanced at heavier Mo isotopes or not. The low-lying 1111 were performed in part using the COMA (PACS-IX) and 1086 2_1^+ , 4_1^+ , and 2_2^+ states are known in ¹¹²Mo [16]. In order 1112 Oakforest-PACS provided by Multidisciplinary Coopera-1087 to study the triaxial motion, measurements of the higher 1113 tive Research Program in Center for Computational Scispin states in the 2^+_2 band are awaited.

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1095 Nos. 24740188, 25247045, 26800117, and 16K17680, The 893.4- and 1042.2-keV states in ¹⁰⁸Mo and ¹¹⁰Mo ₁₀₉₆ NRF Grant No. 2016K1A3A7A09005575, STFC Grant DE-FG02-91ER-40609, and Spanto be the known $5_1^+ \rightarrow 4_1^+$ transition. The compari- 1100 No. FPA2009-13377-C02 and No. FPA2011-29854-C04. son with the beyond-mean-field calculation indicates a 1101 P.H.R. acknowledges support from the UK National Mea- β -vibrational character for the 0_2^+ state in 108 Mo. 1102 surement Office (NMO). P.-A.S. was financed by JSPS The $\log ft$ values were reasonably understood only 1103 Grant No. 23 01752 and the RIKEN Foreign Postdoc-1108 knowledges the JSPS-NSFC Bilateral Program for the It is interesting to investigate whether the disagree- 1109 Joint Research Project on "Nuclear mass and life for un-1114 ences, University of Tsukuba.

- [1] R. F. Casten, Nuclear Structure from a Simple Perspec- 1142 tive (Oxford University Press, Oxford, 2000).
- [2] A. S. Davydov and G. F. Filippov, Nucl. Phys. 8, 237 1144
- [3] L. Wilets and M. Jean, Phys. Rev. 102, 788 (1956).
- [4] M. A. Caprio, Phys. Rev. C 83, 064309 (2011).

1115

1116

1117

1118

1119

1120

1121

1122

1123

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1129

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1136

1137

1138

1139

1140

1141

- [5] J. Skalski, S. Mizutori, and W. Nazarewicz, Nucl. Phys. 1148 A **617**, 282 (1997).
- S. Hilaire and M. Girod, AIP Conference Proceedings 1150 1012, 359 (2008). http://www-phynu.cea.fr/science_ 1151 en_ligne/carte_potentiels_microscopiques/carte_ 1152 potentiel_nucleaire_eng.htm.
- C. L. Zhang, G. H. Bhat, W. Nazarewicz, J. A. Sheikh, 1154 and Y. Shi, Phys. Rev. C 92, 034307 (2015).
- A.-C. Dai, F.-R. Xu, and W.-Y. Liang, Chinese Physics 1156 C **43**, 084101 (2019).
- D. Ralet, S. Pietri, T. Rodríguez, M. Alaquel, T. Alexan- 1158 der, N. Alkhomashi, F. Ameil, T. Arici, A. Ataç, 1159 R. Avigo, T. Bäck, D. Bazzacco, B. Birkenbach, 1160 P. Boutachkov, B. Bruyneel, A. M. Bruce, F. Cam- 1161 era, B. Cederwall, S. Ceruti, E. Clément, M. L. 1162 Cortés, D. Curien, G. De Angelis, P. Désesquelles, 1163 M. Dewald, F. Didierjean, C. Domingo-Pardo, M. Don- 1164 cel, G. Duchêne, J. Eberth, A. Gadea, J. Gerl, 1165 F. Ghazi Moradi, H. Geissel, T. Goigoux, N. Goel, P. Gol- 1166 ubev, V. González, M. Górska, A. Gottardo, E. Gregor, 1167 G. Guastalla, A. Givechev, T. Habermann, M. Hackstein,
- L. Harkness-Brennan, G. Henning, H. Hess, T. Hüyük, J. Jolie, D. S. Judson, A. Jungclaus, R. Knoebel, I. Kojouharov, A. Korichi, W. Korten, N. Kurz, M. Labiche, N. Lalović, C. Louchart-Henning, D. Mengoni, E. Merchán, B. Million, A. I. Morales, D. Napoli, F. Naqvi, J. Nyberg, N. Pietralla, Z. Podolyák, A. Pullia, A. Prochazka, B. Quintana, G. Rainovski, M. Reese, F. Recchia, P. Reiter, D. Rudolph, M. D. Salsac, E. Sanchis, L. G. Sarmiento, H. Schaffner, C. Scheidenberger, L. Sengele, B. S. N. Singh, P. P. Singh, C. Stahl, O. Stezowski, P. Thoele, J. J. Valiente Dobon, H. Weick, A. Wendt, O. Wieland, J. S. Winfield, H. J. Wollersheim, and M. Zielinska (for the PreSPEC and PreSPEC and AGATA Collaborations), Phys. Rev. C 95, 034320 (2017).
- H. Ahrens, N. Kaffrell, N. Trautmann, and G. Herrmann, Phys. Rev. C 14, 211 (1976).
- B. D. Kern, K. Sistemich, W.-D. Lauppe, and H. Lawin, Z. Phys. A 306, 161 (1982).
- K. Shizuma, H. Lawin, and K. Sistemich, Z. Phys. A 311, 71 (1983).
- A. Guessous, N. Schulz, W. R. Phillips, I. Ahmad, M. Bentaleb, J. L. Durell, M. A. Jones, M. Leddy, E. Lubkiewicz, L. R. Morss, R. Piepenbring, A. G. Smith, W. Urban, and B. J. Varley, Phys. Rev. Lett. 75, 2280

- 1168 [14] A. Guessous, N. Schulz, M. Bentaleb, E. Lubkiewicz, 1232
 1169 J. L. Durell, C. J. Pearson, W. R. Phillips, J. A. Shan- 1233
 1170 non, W. Urban, B. J. Varley, I. Ahmad, C. J. Lister, L. R. 1234
 1171 Morss, K. L. Nash, C. W. Williams, and S. Khazrouni, 1235
 1172 Phys. Rev. C 53, 1191 (1996).
- H. Watanabe, K. Yamaguchi, A. Odahara, T. Sumikama, 1237 1173 S. Nishimura, K. Yoshinaga, Z. Li, Y. Miyashita, K. Sato, 1238 1174 L. Próchniak, H. Baba, J. S. Berryman, N. Blasi, 1239 1175 A. Bracco, F. Camera, J. Chiba, P. Doornenbal, S. Go, 1240 1176 T. Hashimoto, S. Hayakawa, C. Hinke, N. Hinohara, 1241 1177 E. Ideguchi, T. Isobe, Y. Ito, D. G. Jenkins, Y. Kawada, 1242 1178 N. Kobayashi, Y. Kondo, R. Krücken, S. Kubono, 1243 1179 G. Lorusso, T. Nakano, T. Nakatsukasa, M. Kurata- 1244 1180 Nishimura, H. J. Ong, S. Ota, Z. Podolyák, H. Saku- 1245 1181 rai, H. Scheit, K. Steiger, D. Steppenbeck, K. Sugi- 1246 1182 moto, K. Tajiri, S. Takano, A. Takashima, T. Teranishi, 1247 1183 Y. Wakabayashi, P. M. Walker, O. Wieland, and H. Ya- 1248 [27] 1184 maguchi, Phys. Lett. B **704**, 270 (2011). 1185
- N. Paul, A. Corsi, A. Obertelli, P. Doornenbal, G. Au- 1250 1186 thelet, H. Baba, B. Bally, M. Bender, D. Calvet, 1251 1187 F. Château, S. Chen, J.-P. Delaroche, A. Delbart, J.-M. 1252 1188 Gheller, A. Giganon, A. Gillibert, M. Girod, P.-H. Hee- 1253 1189 nen, V. Lapoux, J. Libert, T. Motobayashi, M. Niikura, 1254 1190 T. Otsuka, T. R. Rodríguez, J.-Y. Roussé, H. Sakurai, 1255 1191 C. Santamaria, N. Shimizu, D. Steppenbeck, R. Taniuchi, 1256 1192 T. Togashi, Y. Tsunoda, T. Uesaka, T. Ando, T. Arici, 1257 1193 A. Blazhev, F. Browne, A. M. Bruce, R. Carroll, L. X. 1258 1194 Chung, M. L. Cortés, M. Dewald, B. Ding, F. Flav- 1259 1195 igny, S. Franchoo, M. Górska, A. Gottardo, A. Jung- 1260 1196 claus, J. Lee, M. Lettmann, B. D. Linh, J. Liu, Z. Liu, 1261 1197 C. Lizarazo, S. Momiyama, K. Moschner, S. Nagamine, 1262 1198 N. Nakatsuka, C. Nita, C. R. Nobs, L. Olivier, Z. Pa- 1263 [29] 1199 tel, Z. Podolyák, M. Rudigier, T. Saito, C. Shand, 1264 1200 P.-A. Söderström, I. Stefan, R. Orlandi, V. Vaguero, 1265 [30] 1201 V. Werner, K. Wimmer, and Z. Xu, Phys. Rev. Lett. 1266 1202 **118**, 032501 (2017). 1203 1267
- 1204 [17] N. V. Zamfir and R. F. Casten, Phys. Lett. B **260**, 265 1268 (1991).
- 1206 [18] R. Casten, E. Flynn, O. Hansen, and T. Mulligan, Nucl. 1270
 Phys. A 184, 357 (1972).
- 1208 [19] S. Takeda, S. Yamaji, K. Matsuda, I. Kohno, N. Nakan- 1272
 1209 ishi, Y. Awaya, and S. Kusuno, J. Phys. Soc. Jpn. 34, 1273
 1210 1115 (1973), https://doi.org/10.1143/JPSJ.34.1115.
- 1211 [20] K. Sistemich, W. D. Lauppe, H. Lawin, H. Seyfarth, and 1275
 1212 B. D. Kern, Z. Phys. A 289, 225 (1979).
- 1213 [21] H. Penttilä, P. Dendooven, A. Honkanen, M. Huhta, 1277
 1214 G. Lhersonneau, M. Oinonen, J.-M. Parmonen, 1278
 1215 K. Peräjärvi, J. Äystö, J. Kurpeta, and J. R. Persson, 1279
 1216 Phys. Rev. C **54**, 2760 (1996).
- F. Browne, A. M. Bruce, T. Sumikama, I. Nishizuka, 1281 [33] 1217 S. Nishimura, P. Doornenbal, G. Lorusso, Z. Patel, 1282 1218 S. Rice, L. Sinclair, P.-A. Söderström, H. Watanabe, 1283 1219 J. Wu, Z. Y. Xu, H. Baba, N. Chiga, R. Carroll, R. Daido, 1284 1220 F. Didierjean, Y. Fang, G. Gey, E. Ideguchi, N. In- 1285 1221 abe, T. Isobe, D. Kameda, I. Kojouharov, N. Kurz, 1286 1222 T. Kubo, S. Lalkovski, Z. Li, R. Lozeva, N. Naoki, 1287 1223 H. Nishibata, A. Odahara, Z. Podolyák, P. H. Regan, 1288 1224 O. J. Roberts, H. Sakurai, H. Schaffner, G. S. Simp- 1289 1225 son, H. Suzuki, H. Takeda, M. Tanaka, J. Taprogge, 1290 1226 V. Werner, O. Wieland, and A. Yagi, Acta Phys. Pol. 1291 1227 B **46**, 721 (2015). 1228
- 1229 [23] T. Kubo, Nucl. Instrum. Methods B **204**, 97 (2003).
- 1230 [24] T. Kubo, D. Kameda, H. Suzuki, N. Fukuda, H. Takeda, 1294
 Y. Yanagisawa, M. Ohtake, K. Kusaka, K. Yoshida, 1295

- N. Inabe, T. Ohnishi, A. Yoshida, K. Tanaka, and Y. Mizoi, Prog. Theor. Exp. Phys. **2012**, 03C003 (2012).
- [25] T. Sumikama, F. Browne, A. M. Bruce, I. Nishizuka, S. Nishimura, P. Doornenbal, G. Lorusso, Z. Patel, S. Rice, L. Sinclair, P.-A. Söderström, H. Watanabe, J. Wu, Z. Y. Xu, A. Yagi, H. Baba, N. Chiga, R. Carroll, R. Daido, F. Didierjean, Y. Fang, G. Gey, E. Ideguchi, N. Inabe, T. Isobe, D. Kameda, I. Kojouharov, N. Kurz, T. Kubo, S. Lalkovski, Z. Li, R. Lozeva, N. Fukuda, H. Nishibata, A. Odahara, Z. Podolyák, P. H. Regan, O. J. Roberts, H. Sakurai, H. Schaffner, G. S. Simpson, H. Suzuki, H. Takeda, M. Tanaka, J. Taprogge, V. Werner, and O. Wieland, RIKEN Accel. Prog. Rep. 47, 9 (2014).
- [26] S. Nishimura, Prog. Theor. Exp. Phys. 2012, 03C006 (2012).
- [27] S. Nishimura, G. Lorusso, Z. Xu, J. Wu, R. Gernhäuser, H. Jung, Y. Kwon, Z. Li, K. Steiger, and H. Sakurai, RIKEN Accel. Prog. Rep. 46, 182 (2013).
- [28] I. Nishizuka, T. Sumikama, F. Browne, A. M. Bruce, S. Nishimura, P. Doornenbal, G. Lorusso, Z. Patel, S. Rice, L. Sinclair, P.-A. Söderström, H. Watanabe, J. Wu, Z. Y. Xu, A. Yagi, H. Baba, N. Chiga, R. Carrol, R. Daido, F. Didierjean, Y. Fang, N. Fukuda, G. Gey, E. Ideguchi, N. Inabe, T. Isobe, D. Kameda, I. Kojouharov, N. Kurz, T. Kubo, S. Lalkovski, Z. Li, R. Lozeva, H. Nishibata, A. Odahara, Z. Podolyák, P. H. Regan, O. J. Roberts, H. Sakurai, H. Schaffner, G. S. Simpson, H. Suzuki, H. Takeda, M. Tanaka, J. Taprogge, V. Werner, and O. Wieland, JPS Conf. Proc. 6, 030062 (2015).
- [29] J. Ha, T. Sumikama, and S. Choi, Nucl. Instrum. Methods B 463, 216 (2020).
- [30] P.-A. Söderström, S. Nishimura, P. Doornenbal, G. Lorusso, T. Sumikama, H. Watanabe, Z. Y. Xu, H. Baba, F. Browne, S. Go, G. Gey, T. Isobe, H.-S. Jung, G. D. Kim, Y.-K. Kim, I. Kojouharov, N. Kurz, Y. K. Kwon, Z. Li, K. Moschner, T. Nakao, H. Nishibata, M. Nishimura, A. Odahara, H. Sakurai, H. Schaffner, T. Shimoda, J. Taprogge, Z. Vajta, V. Werner, J. Wu, A. Yagi, and K. Yoshinaga, Nucl. Instrum. Methods B 317, 649 (2013).
- [31] Z. Patel, F. Browne, A. M. Bruce, N. Chiga, R. Daido, S. Nishimura, Z. Podolyák, P. H. Regan, O. J. Roberts, H. Sakurai, P.-A. Söderström, T. Sumikama, and H. Watanabe, RIKEN Accel. Prog. Rep. 47, 13 (2014).
- [32] J. C. Hill, D. D. Schwellenbach, F. K. Wohn, J. A. Winger, R. L. Gill, H. Ohm, and K. Sistemich, Phys. Rev. C 43, 2591 (1991).
- [33] M. Wang, G. Audi, F. G. Kondev, W. J. Huang, S. Naimi, and X. Xu, Chin. Phys. C 41, 030003 (2017).
- [34] ENSDF database, http://www.nndc.bnl.gov/ensdf.
- [35] X. Rui-Qing, Z. Sheng-Jiang, J. H. Hamilton, A. V. Ramayya, J. K. Hwang, X. Q. Zhang, L. Ke, Y. Li-Ming, Z. Ling-Yan, G. Cui-Yun, Z. Zheng, J. Zhuo, X. Shu-Dong, W. C. Ma, J. Kormicki, E. F. Jones, J. D. Cole, R. Aryaeinejad, M. W. Drigert, I. Y. Lee, J. O. Rasmussen, M. A. Stoyer, G. M. Ter-Akopian, and A. V. Daniel, Chin. Phys. Lett. 19, 180 (2002).
- [6] S. J. Zhu, J. H. Hamilton, A. V. Ramayya, P. M. Gore, J. O. Rasmussen, V. Dimitrov, S. Frauendorf, R. Q. Xu, J. K. Hwang, D. Fong, L. M. Yang, K. Li, Y. J. Chen, X. Q. Zhang, E. F. Jones, Y. X. Luo, I. Y. Lee, W. C. Ma, J. D. Cole, M. W. Drigert, M. Stoyer, G. M. Ter-Akopian,

and A. V. Daniel, Eur. Phys. J. A 25, 459 (2005).

1296

- 1297 [37] E. F. Jones, P. M. Gore, S. J. Zhu, J. H. Hamilton, A. V. 1361
 1298 Ramayya, J. K. Hwang, R. Q. Xu, L. M. Yang, K. Li, 1362
 1299 Z. Jiang, Z. Zhang, S. D. Xiao, X. Q. Zhang, W. C. Ma, 1363
 1300 J. D. Cole, M. W. Drigert, I. Y. Lee, J. O. Rasmussen, 1364
 Y. X. Luo, and M. A. Stoyer, Phys. Atom. Nucl. 69, 1198 1365
 1302 (2006).
- 1303 [38] Calculation program of $\log ft$, http://www.nndc.bnl. 1367 gov/logft.
- 1305 [39] T. Kibédi, T. W. Burrows, M. B. Trzhaskovskaya, P. M. 1369
 Davidson, and C. W. Nestor Jr, Nucl. Instrum. Methods 1370
 A 589, 202 (2008).
- 1308 [40] B. Singh, J. L. Rodriguez, S. S. M. Wong, and J. K. Tuli, 1372
 Nucl. Data Sheets 84, 487 (1998).
- 1310 [41] H. Behrens and W. Bühring, Electron Radial Wave Func- 1374
 1311 tions and Nuclear Beta-decay (Oxford Science Publica- 1375
 1312 tions, 1982).
- 1313 [42] J. A. Pinston, W. Urban, C. Droste, T. Rzaça-Urban, 1377
 1314 J. Genevey, G. Simpson, J. L. Durell, A. G. Smith, B. J. 1378
 1315 Varley, and I. Ahmad, Phys. Rev. C 74, 064304 (2006). 1379
- 1316 [43] T. Mehren, B. Pfeiffer, S. Schoedder, K.-L. Kratz, 1380
 1317 M. Huhta, P. Dendooven, A. Honkanen, G. Lhersonneau, 1381
 1318 M. Oinonen, J.-M. Parmonen, H. Penttilä, A. Popov, 1382 [55]
 1319 V. Rubchenya, and J. Äystö, Phys. Rev. Lett. 77, 458 1383
 1320 (1996).
- 1321 [44] J. Pereira, S. Hennrich, A. Aprahamian, O. Arndt, A. Be- 1385
 1322 cerril, T. Elliot, A. Estrade, D. Galaviz, R. Kessler, K.-L. 1386
 1323 Kratz, G. Lorusso, P. F. Mantica, M. Matos, P. Möller, 1387
 1324 F. Montes, B. Pfeiffer, H. Schatz, F. Schertz, L. Schnor- 1388 [57]
 1325 renberger, E. Smith, A. Stolz, M. Quinn, W. B. Walters, 1389
 1326 and A. Wöhr, Phys. Rev. C 79, 035806 (2009).
- 1327 [45] W. Urban, T. Rzaça-Urban, J. L. Durell, W. R. Phillips, 1391
 1328 A. G. Smith, B. J. Varley, I. Ahmad, and N. Schulz, Eur. 1392
 1329 Phys. J. A 20, 381 (2004).
- G. Lorusso, S. Nishimura, Z. Y. Xu. A. Jungclaus, 1394 1330 Y. Shimizu, G. S. Simpson, P.-A. Söderström, H. Watan- 1395 1331 abe, F. Browne, P. Doornenbal, G. Gey, H. S. Jung, 1396 1332 B. Meyer, T. Sumikama, J. Taprogge, Z. Vajta, J. Wu, 1397 1333 H. Baba, G. Benzoni, K. Y. Chae, F. C. L. Crespi, 1398 1334 N. Fukuda, R. Gernhäuser, N. Inabe, T. Isobe, T. Ka- 1399 1335 jino, D. Kameda, G. D. Kim, Y.-K. Kim, I. Ko- 1400 1336 jouharov, F. G. Kondev, T. Kubo, N. Kurz, Y. K. 1401 1337 Kwon, G. J. Lane, Z. Li, A. Montaner-Pizá, K. Moschner, 1402 1338 F. Naqvi, M. Niikura, H. Nishibata, A. Odahara, R. Or- 1403 [59] 1339 landi, Z. Patel, Z. Podolyák, H. Sakurai, H. Schaffner, 1404 1340 P. Schury, S. Shibagaki, K. Steiger, H. Suzuki, H. Takeda, 1405 1341 A. Wendt, A. Yagi, and K. Yoshinaga, Phys. Rev. Lett. 1406 [60] 1342 **114**, 192501 (2015). 1343
- 1344 [47] G. Mamane, Ph.D. thesis, Weizmann Inst.Science, Re- 1408
 1345 hovot (1983).
- 1346 [48] B. Pritychenko, M. Birch, B. Singh, and M. Horoi, At. 1410
 1347 Data Nucl. Data Tables 107, 1 (2016).
- 1348 [49] E. Cheifetz, R. C. Jared, S. G. Thompson, and J. B. 1412
 Wilhelmy, Phys. Rev. Lett. 25, 38 (1970).
- 1350 [50] J. K. Hwang, A. V. Ramayya, J. H. Hamilton, Y. X. Luo, 1414
 1351 A. V. Daniel, G. M. Ter-Akopian, J. D. Cole, and S. J. 1415
 1352 Zhu, Phys. Rev. C 73, 044316 (2006).
- 1353 [51] E. Cheifetz, H. Selic, A. Wolf, R. Chechik, and J. Wil- 1417
 1354 helmy, in *Proc. Conf. Nucl. Spectr. Fission Products* 1418
 1355 (1980) p. 193.
- 1356 [52] S. Raman, C. W. Nestor Jr, and P. Tikkanen, At. Data 1420
 1357 Nucl. Data Tables 78, 1 (2001).
- 1358 [53] F. Browne, A. M. Bruce, T. Sumikama, I. Nishizuka, 1422
 1359 S. Nishimura, P. Doornenbal, G. Lorusso, P.-A.

- Söderström, H. Watanabe, R. Daido, Z. Patel, S. Rice, L. Sinclair, J. Wu, Z. Y. Xu, A. Yagi, H. Baba, N. Chiga, R. Carroll, F. Didierjean, Y. Fang, N. Fukuda, G. Gey, E. Ideguchi, N. Inabe, T. Isobe, D. Kameda, I. Kojouharov, N. Kurz, T. Kubo, S. Lalkovski, Z. Li, R. Lozeva, H. Nishibata, A. Odahara, Z. Podolyák, P. H. Regan, O. J. Roberts, H. Sakurai, H. Schaffner, G. S. Simpson, H. Suzuki, H. Takeda, M. Tanaka, J. Taprogge, V. Werner, and O. Wieland, Phys. Lett. B **750**, 448 (2015).
- [54] S. Ansari, J.-M. Régis, J. Jolie, N. Saed-Samii, N. Warr, W. Korten, M. Zielińska, M.-D. Salsac, A. Blanc, M. Jentschel, U. Köster, P. Mutti, T. Soldner, G. S. Simpson, F. Drouet, A. Vancraeyenest, G. de France, E. Clément, O. Stezowski, C. A. Ur, W. Urban, P. H. Regan, Z. Podolyák, C. Larijani, C. Townsley, R. Carroll, E. Wilson, H. Mach, L. M. Fraile, V. Paziy, B. Olaizola, V. Vedia, A. M. Bruce, O. J. Roberts, J. F. Smith, M. Scheck, T. Kröll, A.-L. Hartig, A. Ignatov, S. Ilieva, S. Lalkovski, N. Mărginean, T. Otsuka, N. Shimizu, T. Togashi, and Y. Tsunoda, Phys. Rev. C 96, 054323 (2017).
- [55] G. Alaga, K. Alder, A. Bohr, and B. R. Mottelson, Mat. Fys. Medd. K. Dan. Vidensk. Selsk. 29 (1955).
- 1384 [56] J. M. Eldridge, B. Fenker, J. H. Hamilton, C. Goodin,
 1385 C. J. Zachary, E. Wang, A. V. Ramayya, A. V. Daniel,
 1386 G. M. Ter-Akopian, Y. T. Oganessian, Y. X. Luo, J. O.
 1387 Rasmussen, and S. J. Zhu, Eur. Phys. J. A 54, 15 (2018).
 - P.-A. Söderström, G. Lorusso, H. Watanabe, S. Nishimura, P. Doornenbal, G. Thiamova, F. Browne, G. Gey, H. S. Jung, T. Sumikama, J. Taprogge, Z. Vajta, J. Wu, Z. Y. Xu, H. Baba, G. Benzoni, K. Y. Chae, F. C. L. Crespi, N. Fukuda, R. Gernhäuser, N. Inabe, T. Isobe, A. Jungclaus, D. Kameda, G. D. Kim, Y.-K. Kim, I. Kojouharov, F. G. Kondev, T. Kubo, N. Kurz, Y. K. Kwon, G. J. Lane, Z. Li, A. Montaner-Pizá, K. Moschner, F. Naqvi, M. Niikura, H. Nishibata, A. Odahara, R. Orlandi, Z. Patel, Z. Podolyák, H. Sakurai, H. Schaffner, G. S. Simpson, K. Steiger, H. Suzuki, H. Takeda, A. Wendt, A. Yagi, and K. Yoshinaga, Phys. Rev. C 88, 024301 (2013).
 - [58] N. Hinohara, K. Sato, T. Nakatsukasa, M. Matsuo, and K. Matsuyanagi, Phys. Rev. C 82, 064313 (2010).
 - [59] N. Hinohara, K. Sato, K. Yoshida, T. Nakatsukasa, M. Matsuo, and K. Matsuyanagi, Phys. Rev. C 84, 061302(R) (2011).
 - [60] K. Sato, N. Hinohara, K. Yoshida, T. Nakatsukasa, M. Matsuo, and K. Matsuyanagi, Phys. Rev. C 86, 024316 (2012).
 - 61] T. Sumikama, K. Yoshinaga, H. Watanabe, S. Nishimura, Y. Miyashita, K. Yamaguchi, K. Sugimoto, J. Chiba, Z. Li, H. Baba, J. S. Berryman, N. Blasi, A. Bracco, F. Camera, P. Doornenbal, S. Go, T. Hashimoto, S. Hayakawa, C. Hinke, E. Ideguchi, T. Isobe, Y. Ito, D. G. Jenkins, Y. Kawada, N. Kobayashi, Y. Kondo, R. Krücken, S. Kubono, G. Lorusso, T. Nakano, M. Kurata-Nishimura, A. Odahara, H. J. Ong, S. Ota, Z. Podolyák, H. Sakurai, H. Scheit, K. Steiger, D. Steppenbeck, S. Takano, A. Takashima, K. Tajiri, T. Teranishi, Y. Wakabayashi, P. M. Walker, O. Wieland, and H. Yamaguchi, Phys. Rev. Lett. 106, 202501 (2011).
 - [62] K. Washiyama and T. Nakatsukasa, Phys. Rev. C 96, 041304(R) (2017).

1423 [63] Y. X. Luo, J. O. Rasmussen, J. H. Hamilton, A. V. Ra- 1429 [64] Y.-X. Liu, Y. Sun, X.-H. Zhou, Y.-H. Zhang, S.-Y. Yu, mayya, E. Wang, Y. X. Liu, C. F. Jiao, W. Y. Liang, 1430 1424 1425 S. J. Zhu, N. T. Brewer, I. Y. Lee, G. M. Ter-Akopian, $_{1432}$ 1426

C 89, 044326 (2014).

1427

1428

- Y.-C. Yang, and H. Jin, Nucl. Phys. A 858, 11 (2011). F. R. Xu, Y. Sun, S. Frauendorf, J. K. Hwang, S. H. Liu, 1431 [65] C. J. Gallagher Jr and S. A. Moszkowski, Phys. Rev. 111, 1282 (1958).
- Y. Oganessian, R. Donangelo, and W. C. Ma, Phys. Rev. 1433 [66] F. R. Xu, P. M. Walker, and R. Wyss, Phys. Rev. C 65, 021303(R) (2002).