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A discrete epidemic model and a zigzag strategy for curbing the Covid-19 outbreak and for lifting the lockdown

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Abstract. This study looks at the dynamics of a Covid-19 type epidemic with a dual purpose. The first objective is to propose a reliable temporal mathematical model, based on real data and integrating the course of illness. It is a daily discrete model with different delay times, and whose parameters are calibrated from the main indicators of the epidemic. The model can be broken down in two decoupled versions: a mortality-mortality version, which can be used with the data on the number of deaths, and an infection-infection version to be used when reliable estimates of infection rate are available. The model allows to describe realistically the evolution of the main markers of the epidemic. In addition, in terms of deaths and occupied ICU beds, the model is not very sensitive to the current uncertainties about IFR.

The second objective is to study several original scenarios for the epidemic's evolution, especially after the period of strict lockdown. A coherent strategy is therefore proposed to contain the outbreak and exit lockdown, without going into the risky herd immunity approach. This strategy, called *zigzag strategy*, is based on a classification of the interventions into four lanes, distinguished by a marker called the daily reproduction number. The model and strategy in question are flexible and easily adaptable to new developments such as mass screenings or infection surveys. They can also be used at different geographical scales (local, regional or national)

Keywords: *Covid-19 pandemic, lockdown, zigzag strategy, deconfinement, epidemic model, daily reproduction number.*

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1. Introduction

The Covid-19 epidemic we are witnessing today has spread at a phenomenal rate. Leaving Wuhan in mid-December 2019, it reached almost all the countries of the world within four months. The speed of circulation of the virus Sars-CoV-2 and the short development time of Covid-19 disease leave little time to react. In late April 2020, the epidemic has already absorbed, even saturated, the hospital capacities of many countries, causing more than 200,000 deaths worldwide and seriously affecting the health of at least a million people. The action time of the Sars-CoV-2 coronavirus appears to be much shorter than the different reaction times of human institutions.

Therefore, to understand the dynamics of a Covid-19 type epidemic, it is necessary to look at the action time of the virus and the disease it causes. Mathematical models that aim to predict these dynamics must take into account clinical times from infection to recovery or to death. More specifically, durations of incubation and of contagiousness period, time from illness onset to admission in ICU and time from illness onset to death or discharge, are all important parameters that must be estimated and integrated into the model.

However, in the face of urgency, scientists cannot rely solely on complex computational models, whose implementation, responsiveness, and needs in data require weeks of data collection and prohibitive calculation costs.

Paradoxically, the importance of chronological aspects in understanding the epidemic potential of this virus could lead to mathematical models that are less costly in terms of computing time and data collection. Indeed, space and age variables do not play a primary role in its spread: the virus is not spread by a wave that moves slowly from region to region, but by the multiplication of clusters. The introduction of one or a few infected cases may be enough to spread the infection rapidly, without waiting for waves arriving from neighbouring regions. Thus, models that rely on systems of partial differential equations where the space variable lives in a continuum may not be adequate for this epidemic. Similarly, the age of infected persons does not appear to play a major role in the spread of the virus (at least according to current knowledge). Only the development, severity and mortality of the disease are highly dependent on it. In summary, the rapidity of circulation that makes the pandemic force of this virus could give rise to simpler mathematical models, provided that they take into account its chronological characteristics.

Furthermore, one of the difficulties encountered in the study of this pandemic stems from the collected data, particularly those concerning the number of infected individuals. Many people are infected without developing severe clinical manifestations of the disease, while at the same time becoming contagious. In addition, the difficulty of performing virological tests in large numbers is leading to a refocusing of screening on cases who have severe illness symptoms. It is therefore unreasonable to base models solely on the number of cases detected or confirmed. Even the proportionality of this indicator to the total number of infected cases is not guaranteed, due to the continuous evolution of screening capacities and public policies. On the other hand, it could be accepted without difficulty that mortality (or in-hospital mortality), admission to intensive care units, or even hospitalizations, are markers that reflect the evolution of the pandemic in a much more specific way. Taking all these observations into account, we propose here a discrete deterministic model for forecasting the temporal evolution of the epidemic from day to day, taking into account the different medical parameters that characterize it. It is a decoupled model in which mortality is predicted from mortality data only, and which makes it possible to simulate the evolution of various other indicators such as the number of occupied ICU beds, the number of infected or recovered cases, and the number of active cases. The fact that these predictions are based primarily on mortality data makes the model less sensitive to the IFR, especially in realistic phases of the epidemic (the IFR will be used primarily to deduce the numbers of infected, recovered or active cases from the death numbers). This model makes it possible to monitor the impact of restrictive interventions and the behavior of individuals. It can also predict the short- and long-term dynamics of the epidemic, according to several scenarios. The state of the epidemic in France will be particularly examined.

The model has a number of parameters. These are mainly the daily reproduction number (to be distinguished from the basic reproduction number), transmission coefficients, and certain time delays. The transmission coefficients are calibrated from data using an inverse method (without making additional assumptions about the contagiousness profile). Time delays are inferred from clinical data. As for the daily reproduction number, introduced here, it is a dynamic marker that can be measured from the data and allows the impact of the public interventions to be assessed. It will play a fundamental role in predicting the course of the epidemic under different scenarios, and in designing a technique to control it without maintaining permanent drastic interventions. This technique, called **zigzag strategy**, consists of alternating periods of strict lockdown and moderate deconfinement according to precise rules.

Before closing this introduction, it should be recalled that there are several deterministic or stochastic mathematical models that describe the evolution of an epidemic. Deterministic models are often based on systems of ordinary differential equations, or partial differential equations integrating the space dimension and age of individuals. Probabilistic models, which are currently widely used, take into account the random nature of contacts between individuals as well as several other dimensions of the problem: age and gender, geographical location, etc. By adopting a global approach that takes into account the various dimensions of the problem, these models require important assumptions and data collection in order to set their structural parameters (probability laws of various random variables, contact matrices, etc.). However, they ultimately provide valuable information on the characteristics of the disease and its impact according to the ages of the individuals, the regions where they live, their health situation, etc.

The remaining of this paper is oraganized as follows:

In section 2, we expose the main features of the model. For reasons of readability, its formal justification has been moved to the Appendix A.

Section 3 is dedicated to the calibration of its various parameters (time delays, transmission coefficients, etc)

Section 4 deals with the study of the daily reproduction number in the case of several countries.

Section 5 includes the analysis of about ten scenarios for the lockdown exit, by choosing the exam-

ple of France. These scenarios are all replicable for other countries or for a specific region. The scenario of non-application of lockdown is also studied.

In 6, the zigzag strategy for exiting the lockdown is outlined in general terms while controlling the outbreak. This strategy is based on the results of various simulations and observation of the characteristics of the epidemic.

Section 7 is devoted to conclusions.

The reader not interested in the mathematical aspects of the model can simply read sections 5, 6, 7 and possibly 4.

Finally, it should be noted that the rigorous mathematical study of the model is postponed to another work. Here, the emphasis is deliberately placed on modelling and prediction in the context of realistic scenarios.

2. Model and its parameters

In severe epidemic situations such as the Covid-19 epidemic, many countries adopt daily reporting of infection, hospitalization and mortality indicators. Therefore, the **unit of time chosen here is the day**. Here \mathscr{E} designates an entity with a sufficiently large population. Such an entity can be a given region, a country or a set of countries. However, we can keep in mind, without losing generality, that the reference entity here is the country. We note P the initial size of its population.

In this model, we follow the evolution of the epidemic day by day, starting from a certain date J_0 . This date could depend on the country chosen for the study. We denote $(J_n)_{n \ge 1}$ the sequence of subsequent days. For all $n \ge 0$, we denote by

- S_n the number of susceptible individuals at the end of the *n*-day,
- I_n the number of infected individuals after the first n days (recovered or not),
- D_n the total number of deaths due to the epidemic that occurred in the first n days,
- R_n the number of individuals recovered after the first n days,
- A_n the number of individuals who were admitted in ICU the first n days (due to the epidemic)
- A_n^{\star} the number of occupied ICU beds at the end of the *n*-day (by patients affected by the epidemic).

Let us specify from now on that in the whole model the number of deaths D_n can be replaced by the number of deaths in hospital. The model will remain the same (provided that the mortality rate is adjusted, especially when the epidemic is amplified). It will be seen that it is not necessary to know all these indicators at the beginning of the epidemic. Recent data are sufficient to predict what will happen next.

For convenience, we set $S_k = P$, $D_k = A_k = R_k = 0$ for any integer $k \leq 0$ (no deaths,

hospitalizations or recoveries before the start of the epidemic). Thus, I_0 represents the number of individuals infected on day J_0 . We agree that $I_k = 0$ for k < 0. We set in the following

$$i_n = I_n - I_{n-1}, \ d_n = D_n - D_{n-1}, \ a_n = A_n - A_{n-1} \text{ for all } n.$$
 (2.1)

In other words, i_n and d_n represent the number of infections and deaths that occurred on day J_n , respectively, while a_n represents the balance sheet of ICU inflows and outflows recorded at the end of the day J_n . We have the obvious relationships for any $n \ge 0$

$$I_n = \sum_{k=0}^n i_k, \quad D_n = \sum_{k=0}^n d_k, \quad A_n = \sum_{k=0}^n a_k.$$
 (2.2)

Let us summarize the proposed model for studying the evolution of the epidemic. Its justification is postponed to appendix A. In the full version of the model, the dynamics of the number of deaths is governed by the decoupled law (mortality-mortality):

$$d_n = C_{n-r} (1 - \frac{D_{n-1}}{\alpha P}) \sum_{k=0}^{\ell-1} \lambda_k d_{n-m-k} \text{ pour } n \ge 0,$$
(2.3)

where D_{n-1} is calculated from d_k , $1 \le k \le n-1$, by the relation (2.2), and

- $\ell \ge 1$ refers to the observed average duration of contagiousness (days),
- $m \ge 1$ refers to the minimum time from infection to contagiousness (days),
- $r \ge 1$ is the average time from illness onset to death,
- α is the infection fatality ate (IFR) (or the infection in-hospital fatality rate if D_n denotes the number of deaths in hospital that occurred in the first *n* days),
- $\lambda_0, \dots, \lambda_{\ell-1}$ are nonnegative transmission coefficients independent of n satisfying

$$\sum_{k=0}^{\ell-1} \lambda_k = 1.$$

Qualitatively, the transmission coefficients $\lambda_0, \dots, \lambda_{\ell-1}$ describe the contagiousness of an infected individual (during the $m + \ell$ days following his infection). They depend in part on the evolution of his viral load. They are estimated from actual data using a least-squares technique explained in Appendix A.

In (2.3), for any integer $n \ge 1$, C_n designates a nonnegative coefficient that we will call *daily* reproduction number on day n. This factor depends on the interventions; it decreases when interventions are applied to curb the epidemic, and increases when these interventions are relaxed. We will remember that a sufficient condition to ensure a rapid decline in the epidemic is to keep the constant C_n below 1. An estimate of this factor will be given in the absence of interventions and in periods of strict lockdown, and its evolution in different countries will be compared.

We can observe that the parameter C_n intervenes in the model (2.3) with *a delay of r days*. This delay is justified by the time from the application of interventions to their impact on mortality figures. We also notice that the model (2.3) is a non-linear convolutional model. It is this model that we will adopt in the following and that we will complete with the identities to calculate the other indicators. However, it can be linearized if we look at the early stages of the epidemic, when the number of infections remains small compared to the population size. In the latter case we obtain the linearized convolutional model

$$d_n \approx \sum_{k=0}^{\ell-1} \lambda_k d_{n-m-k},\tag{2.4}$$

This last relationship does not involve mortality rate α . In other words, to predict the evolution of mortality in the early stages of the epidemic only a calibration of transmission coefficients $\lambda_0, \dots, \lambda_k$ and an estimation of daily reproduction numbers C_n are necessary. In addition, this linearized model does not require knowledge of the initial number of infections or deaths. After calibration of the coefficients, the prediction of mortality on day n can be made from the actual mortality data on the $(m + \ell)$ days preceding it.

We now show how we calculate the number of infected individuals and of occupied ICU beds. These two quantities are linked to D_n by the identities

$$D_n = \alpha I_{n-r}, \text{ for } n \ge 0, \tag{2.5}$$

$$A_n^{\star} = \gamma (D_{n+r-t} - D_{n+r-(t+p)}) \text{ for } n \ge 0,$$
(2.6)

where t is the average time from infection to admission to ICU and p is the average time spent in ICU. Here $\gamma = \frac{\beta}{\alpha}$, where β is the ICU admission rate by infection. The γ coefficient is easy to measure because it relates two quantities that are usually carefully monitored (number of deaths and number of occupied ICU beds). The relation (2.11) is therefore verifiable.

The relation (2.6) is easily extended to the number of occupied beds in hospital, replacing t by the time between infection and admission in hospital, p by the length of stay in hospital and replacing γ by a corresponding coefficient.

We will choose here to study the evolution of A_n^* rather than the evolution of A_n (although the latter is easy to deduct). Indeed, A_n^* is an important marker in practice.

The relations (2.5) and (2.6) can be used in (2.4) to infer similar decoupled models for the dynamics of I_n and A_n . In particular, the following infection-infection model is obtained

$$i_n = C_n (1 - \frac{I_{n-1}}{P}) \sum_{k=0}^{\ell-1} \lambda_k i_{n-m-k}.$$
(2.7)

This identity has two remarkable advantages. On the one hand, it does not involve the mortality rate. On the other hand, it focuses only on infection rate. Actually, by introducing the daily infection rate

$$i_n^{\star} = \frac{i_n}{P},$$

identity (2.7) becomes

$$i_n^{\star} = C_n (1 - \sum_{k=0}^{n-1} i_k^{\star}) \sum_{k=0}^{\ell-1} \lambda_k i_{n-m-k}^{\star}.$$
(2.8)

This *infection-infection* model is moreover independent of the overall size of the population studied. It can be used when we have a few successive surveys measuring the infection rate. We will come back to that point in the section 6.

It remains to estimate the number of recovered cases. It is calculated by the relation

$$R_n = (1 - \alpha)I_{n-s} = (\frac{1}{\alpha} - 1)D_{n+r-s},$$
(2.9)

where *s* is the average recovery time. The number of susceptible individuals can be easily deduced from the identity

$$P = S_n + I_n - D_n. (2.10)$$

Identities (2.3), (2.5), (2.6) et (2.9) are sufficient to describe the evolution of the quantities D_n , A_n^* , I_n and R_n , provided that they are completed with initial data I_0, \dots, I_{m-1} (which is equivalent to D_r, \dots, D_{r+m-1}). However, according to the formula (2.4) it is not necessary to go back to the initial conditions at the start of the epidemic, which are generally not well known. Mortality figures in the early stages of the epidemic can be used over a time interval of $m + \ell$ days. This provides a robustness of the model with respect to the initial conditions at the start of the epidemic.

Remark 2.1. The formula (2.6) can be used to predict mortality a few days before (8 days in France for example) from the number of occupied ICU beds (2.3). Actually, one can rewrite it in the form

$$D_{n+r-t} = \frac{1}{\gamma} A_n^* + D_{n+r-(t+p)} \text{ pour tout } n \ge 0, \qquad (2.11)$$

Remark 2.2. The above model can be completed by taking into account changes in overall population size. This is equivalent to considering population size as a sequence $(P_n)_{n \ge 0}$ governed by an equation of the form

$$P_{n+1} = (1+\tau)P_n - d_n, \tag{2.12}$$

where $\tau = \tau^+ - \tau^-$ is the difference between the daily fertility rate τ^+ and the non-epidemic all-cause mortality rate τ^- . In this case, the number of susceptible individuals can be calculated by a recurrence formula of the type

$$S_{n+1} = (1 - \tau^{-})S_n + \tau^{+}P_n - i_{n-1}.$$
(2.13)

Then we can readjust the model (2.3). This will be the subject of a forthcoming work.

3. Calibration of model parameters

The model described in the previous section is essentially based on two families of parameters which will be set by calibration from the data: the clinical times inherent to the illness and normalized coefficients of transmission $\lambda_0, \dots, \lambda_{\ell-1}$. There is also the coefficient γ linking the number of occupied ICU beds to mortality, as well as the infection fatality rate (we will see that its impact is limited on the mortality and occupancy of ICU predicted by this model and that it will mainly be used to estimate the number of infected people). We are going to calibrate these parameters (with the exception of α) using on the one hand, clinical data available in the literature, and on the other hand, mortality data published daily. The aim is to make the model as close as possible to reality and to be able to make forecasts for the weeks and months ahead. Note that the daily reproduction number C_n is a dynamic parameter which will be the focus of specific discussions thereafter.

Determining Clinical Delays.

Recent studies place the onset of Covid-19 between the 2nd and 14th day, with a median around 5 days (see, e. g., (voir [10], [12], [23], [14])). However, it is now known that infected individuals can be contagious in the pre-symptomatic phase up to two days after infection (see [22], [11]). This is supported by estimates of the mean serial interval (the time interval between the illness onset of a person already infected and of a person subsequently infected). In [5], it is estimated to be 4 days. It is estimated to be 5.1 days in [23]. These are two of the main causes of rapid circulation of the Sars CoV-2 virus. The value m should therefore be set at 2 (remember that m is the minimal time from infection to contagiouness period).

In addition, a viral load may remain in the nasopharynx for up to 17 days (very exceptionally up to 21 days) after illness onset (see [11], [24]), suggesting a period of contagiousness of up to 17 days. We choose $\ell = 17$.

The time from illness onset to hospital admission is usually 3 to 9 days (see [12], [23]). According to [24], arrival in ICU occurs on average within 12 days of onset. It is estimated to be 14.5 days in [14]. Again, taking into account the incubation period, we choose t = 19.

According to [12] et [14], the average time of death is 17 to 24 days after the illness onset. Adding the average length of the incubation period, we choose r = 25 (average time between time of infection and death). The average time from infection to recovery is estimated at 22 days: s = 22. Finally, the average length of stay in ICU (in France) will be chosen equal to 17 days (see [17]): p = 17.

Model transmission coefficients

In order to complete this set of parameters, the transmission coefficients $\lambda_0, \dots, \lambda_{\ell-1}$ still need to be fixed. We choose to set them by a least squares technique using mortality or in-hospital mortality data over a certain calibration period. It should be noted that the calibration period in question is chosen according to the country by meeting two criteria. The first criterion is that the mortality figures should be fairly significant (i.e. not at the very beginning of the epidemic where the death figures are still not very representative). The second criterion is that the interventions applied to contain the epidemic are not variable during a part of this period. For the sake of simplicity, the mathematical explanation of this least-squares technique is given in appendix A.

These coefficients have been estimated for several countries where the epidemic has advanced sufficiently or even strongly. For each country, a calibration period was chosen that met both of the above criteria. The resulting coefficients and calibration periods are detailed in Table 3 (in the appendix). The fact that these coefficients are close to each other reinforces the idea that they are a characteristic of the epidemic. In addition, similar values of these coefficients are found worldwide. However, in the case of South Korea, the coefficients are significantly different. It is concluded that the strategy used by South Korea has had a direct impact on the distribution of transmission probabilities during the period of contagiousness.

The infection fatality rate (IFR)

The difficulty in finding reliable estimates of the infection fatality rate (IFR) is a surprising fact about this epidemic. In the urgency of the crisis, screenings are often restricted to individuals with severe symptoms. This is a non-random sample of the population. However, a screening campaign based on the same principle as surveys could lead to an estimate of this rate after a certain waiting period (as well as the infection rate at a given time).

Today, the first estimates available in the literature are often based on data in China [19] or concerning passengers of the Diamond Princess cruise ship ([16]). In [16], it is estimated at 1.2% for Diamond Princess passengers and 0.6% for China. In the case of France, a similar estimate can be found in [17]. Nevertheless, these estimates are not the only ones, and it is not excluded that the rate is higher ([4], [21], [15]).

In the following, in order to be able to make predictions on the number of infected individuals, the number of recoveries and the number of active cases, simulations will be made based on the number of in-hospital deaths in France and for two values: $\alpha = 0.6\%$ and for $\alpha = 1.2\%$. It follows that α is the infection in-hospital fatality rate and is slightly lower than the IFR.

The rate γ

The coefficient γ links two important indicators through the identity (2.6): the number of deaths and the number of occupied ICU beds. Since reliable figures are available for these indicators (if we restrict ourselves to deaths in hospital), we would like to check first the validity of the proportionality identity (2.6) which has not been deduced from the observations. For this purpose, we choose hospital fatality data and the number of people in ntensive care in France. These two figures are communicated on a daily basis by Santé Publique France since March 17, 2020. In the Figure 1 we visualize the evolution of the ratio

$$\gamma_n = \frac{A_n^{\star}}{D_{n+r-t} - D_{n+r-(t+p)}}$$

from March 31 to April 13, 2020, according to in-hospital mortality data in France. The values of r and p chosen at the beginning of this section (r = 25, p = 17) have been adopted here. It can be observed that this ratio is almost constant, confirming the hypothesis of the model that led to this identity. In the following, we will choose the value $\gamma = 0.94$.

4. Evolution of the daily reproduction number

The daily reproduction number C_n plays a prominent role in this model (C_n will act as a dynamic basic reproduction number). By keeping C_n below 1, the epidemic decreases until it is extinguished. The rigorous proof of a threshold theorem for this model, not really difficult, will be done in a future work (here we give a numerical proof). As for the basic reproduction number, the formula (A.6) indicates that this number C_n is directly related to the average number of contacts of an infected person on day n, to the average transmission probabilities and to the duration of contagiousness.

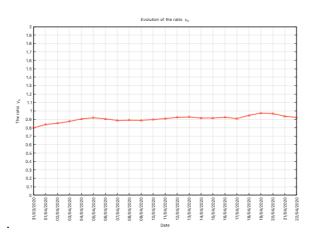


Figure 1: The ratio γ_n calculated from March 31 to April 24, 2020. It can be observed that this ratio is almost constant, confirming the assumed proportionality of the two quantities.

Its estimation from epidemic data allows to quantify the effectiveness of the interventions and to design realistic scenarios for the future.

For periods of time already passed, this parameter can be estimated by the formula (2.3) with a delay time of r days

$$C_{n-r} = \frac{d_n}{(1 - \frac{D_{n-1}}{\alpha P}) \sum_{k=0}^{\ell-1} \lambda_k d_{n-m-k}}$$
(4.1)

The time r reflects the fact that any change in the interventions (or in the behavior of the population) on day n will only have an impact on the number of deaths from day n+r. This delay in estimating this number can be overcome if accurate data are available on the rate of infection. Atually, one can use the formula *without delay*

$$C_n = \frac{i_n^{\star}}{(1 - \sum_{k=0}^{n-1} i_k^{\star}) \sum_{k=0}^{\ell-1} \lambda_k i_k^{\star}}.$$
(4.2)

The usefulness of this second formula and its advantages will be discussed in section 6. At the present stage, the delayed formula (4.1) is used to estimate C_n in the past.

The evolution of C_n has been reproduced for several countries and for the whole world. In the case of France, Italy and Spain, C_n is shown in Figure 2 until 5 April 2020 (data sources are given at the end of the paper). In view of (4.1), to measure the evolution of C_n beyond this date of April 5, 2020, we need mortality data beyond April 30, 2020, i.e. after the completion date of this study.

A closer look at the values obtained C_n for the total lockdown period in France, Spain or Italy shows that it is generally between a minimum value $C_- \approx 0.6$ and 1. The average for the strict lockdown period from March 17 to April 5, 2020 is 0.83 for France and Spain and 0.88 for Italy. It is not excluded that these averages slightly decrease if the strict lockdown lasts longer, especially because the individuals in contact remain the same.

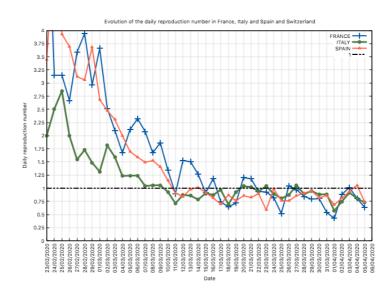


Figure 2: Evolution of the daily reproduction number for , France and Italy for the period from 23 February to 05 April 2020 during the Coronavirus Sars-Cov 2 pandemic. This number is calculated from mortality data.

The curve shows the different dates of entry into lockdown for the three countries.

Changes in C_n for a few other countries were calculated from public data (some public data sources are listed at the end of the paper). In figure 3 the evolution of this daily reproduction number is shown for Belgium, Germany and South Korea. In Figure 4, this rate is evaluated for the United States and the United Kingdom. The effectiveness of the public interventions in South Korea can be clearly seen, since the daily reproduction number in this country is, in average, the lowest of all the countries illustrated here.

A first remark should be made at this stage: drastic restrictions of the strict lockdown lead to values of C_n barely lower than the threshold value 1. It can indeed be observed that outside a regime of drastic restrictions, values of C_n are clearly higher than 1, even in periods with strong but not drastic interventions. This observation suggests that it will be difficult to control the epidemic in the long term without the application of drastic interventions. Thus, according to these estimates, deconfinement, even moderate, will systematically make the value of C_n greater tha 1. In the case of Covid-19, we are faced with a dilemma: to maintain a strict lockdown with numerous socioeconomic and systemic damages or to proceed to a deconfinement not totally under control risking a rebound of the epidemic.

5. Scenarios for the evolution of the epidemic

We are now able to use the calibrated model for studying some future scenarios of the epidemic. Although the model is independent of the choice of country, we will focus on the French situation as

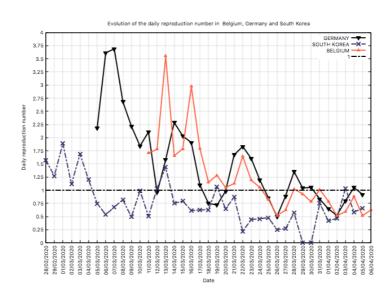


Figure 3: Evolution of the daily reproduction number for Belgium, Germany and South Korea from 28 February to 5 April 2020 (Covid-19 pandemic).

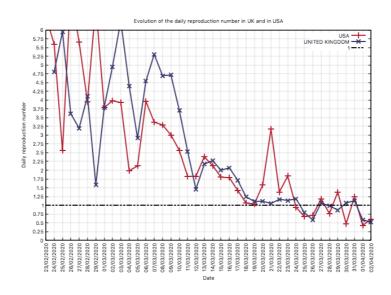


Figure 4: Evolution of the daily reproduction number for the period from the end of February to the beginning of April 2020 for the United States and the United Kingdom (Covid-19 pandemic).

an example of study. In general, the results obtained for other countries lead to similar conclusions, and can be easily replicated.

The study of these scenarios will be used in the design of a lockdown exit strategy.

Eleven scenarios, numbered from 0 to 10, are studied here. For all these scenarios, the focus will be on the evolution of five markers: the number of deaths in hospital, the number of occupied ICU

beds, the number of active cases, the number of recovered cases and the number of infected individuals. Again, it should be noted that the estimates of the first two markers provided by this model are little dependent on infection fatality rates, except when the epidemic is large¹.

Scenario 0 relates to the evolution of the epidemic in the case where strict lockdown had not been imposed and the epidemic was allowed to run its course while strong but less drastic interventions were applied. This scenario will give us an accurate idea of the severity of this crisis and what was avoided.

Scenario 1 consists of extending the strict lockdown beyond 11 may (the French government has set this date to relax the lockdown).

The 2nd and the 3rd scenarios describe a moderate deconfinement installed abruptly by May 12, 2020, or achieved gradually (over about a month).

Scenarios 4 and 5 involve a switch to a cyclic situation of alternating strict lockdown and deconfinement, with periods of equal durations.

Scenarios 6, 7, 8, 9 and 10 involve alternating lockdown and deconfinement based on an organized schedule (e.g., lockdown on some but not all days of the week).

5.1. Scenario 0: evolution of the epidemic without lockdown t

Prior to imposing lockdown on the population, almost all the nations have tried to block the introduction of the virus into the country, without any real success. They then tried to curb its circulation. If we look again at the curves of the daily reproduction number, we can see that interventions in the pre-lockdown period have contributed to a serious drop in this number, but rarely below 1. In France, in the ten days prior to entry into strict confinement, C_n had an average of 1.4. That is way lower than the values prior to this period, but this rate remains far enough away from the 1 threshold value.

In this scenario 0, we want to measure the impact of the strict lockdown, imagining that it had not been imposed, but keeping some strong interventions. *It is therefore not the scenario where nothing is done* (which will be much more catastrophic) but the scenario where the interventions **are not sufficient**. We will impose here a value of C_n equal to 1.3, and this will be effective from March 17, 2020, while keeping the actual data before that date. Note that in France, Italy and Spain, and in many other countries, this value of 1.3 is lower than the mean value measured the week before the lockdown (see Figure 2).

In Table 1, we indicate some figures from the simulations within the framework of this scenario. The evolution of the five markers chosen for these simulations is the subject of Figures 5 and 6. The results confirm that strict lockdown has prevented a much more severe health situation than

¹This fact may seem surprising, but the explanation is simple. Let us recall that in the model (2.3), the number of deaths is calculated from the deaths already recorded. It is not necessary to go through the number of infected individuals (all the more so as the number of infected individuals is generally imprecise or even unknown). On the other hand, estimating the number of infected cases will require setting a fatality rate per infection.

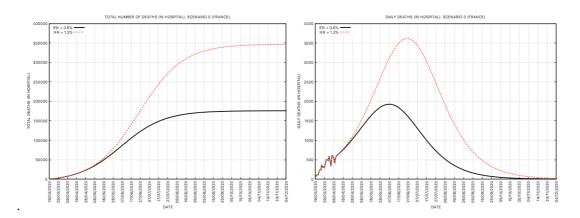


Figure 5: Scenario 0 in France. Left: total number of deaths in hospital. Right: daily deaths in hospital. Values up to 17 Marsh 2020 are actual (public data).

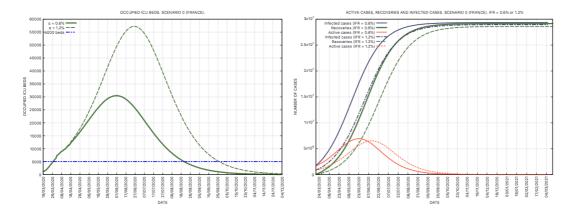


Figure 6: Scenario 0 in France. Left: : number of occupied ICU beds (estimated by the model). Right: : evolution of the number of active cases, the number of infected individuals and the number of recoveries until early December 2020 (estimated by the model). We observe that the peak of the epidemic occurs at the beginning or end of June 2020, depending on the value of the IFR. Values up to 17 March 2020 are actual (public data).

the one currently experienced. Indeed, under the conditions of rather strong interventions of this scenario, and with a fatality rate $\alpha = 0.6\%$, 100.000 deaths would have occurred in France in mid-June, and almost 170000 at the end of August. The need ICU beds would have exceeded 10000 places (per day) on 14 April 2020, and 28000 places at the end of May 2020. The epidemic would have continued to grow until it peaked in the last week of May 2020. On 31 August 2020, the number of infected people will reach, according to this scenario, a little over 29 million (43.2% of the French population).

An important conclusion which is necessary at this stage is not only to confirm the effectiveness of strict lockdown, but to note that the coronavirus Sars-Cov 2 leaves an extremely narrow margin of maneuver to control its circulation (let us recall indeed that this scenario 0 is that of the continuation since March 17 of strong but not drastic interventions). This observation will be reinforced when

Tahar Z. Boulmezaoud

			I	1	I	
		15/4/2020	11/5/2020	15/6/2020	31/7/2020	31/8/2020
	Total deaths at hospital	11829	39119	101717	159663	171190
	Daily deaths at hospital	689	1423	1868	636	195
$\alpha = 0.6\%$	ICU	10986	22694.	29563	10287	3181
(IFR)	Infected	6282628	13775511	23476048	28315221	29031306
		(9.36%)	(20.54%)	(35.00%)	(42.22%)	(43.28%)
	Recovered	2324174	7218145	17764407	26746052	28450238
	Active cases	3946624	6518245	5609923	1409505	409877
	Total deaths	11876	41637	133337	280397	325436
	Daily deaths	702	1663	3432	2249	846
$\alpha = 1.2\%$	ICU	11233	26737	54390	35984	13703
(IFR)	Infected	3331208	8394252	18468035	26656200	28244898
		(4.96%)	(12.51%)	(27.53%)	(39.74%)	(42.11%)
	Recovered	1163428	3863872	11839933	23613638	26988761
	Active cases	2155903	4488741	6494764	2762164	930701

Table 1: Scenario 0 (evolution of the epidemic in France without strict lockdown on 17 March 2020). Main indicators on the date of relaxing lockdown (11 May), 15 June, 31 July and 31 August 2020.

scenarios with even stronger interventions are analyzed.

It is nevertheless useful to indicate that according to this model, strict lockdown has saved France about 1233 hospital deaths as of 15 April 2020, and about 7496 hospital deaths as of 27 April 2020 (i.e. 12 days later). We will see thereafter (scenario 1) that this reduction in the number of deaths due to lockdown will be around 21720 cases on May 11, and around 80928 cases on June 15, 2020. It has also avoided an overflow of the hospital system that would have occurred as early as mid-April (see Table 1 and Figure 6).

5.2. Scenario 1: Continuation of strict lockdown

Here we would like to study the consequences of the eventuality (now ruled out) of an extension of the strict lockdown in France after May 11 2020, with the same interventions. To do so, by set $C_n = C_{\text{conf}}$ after this date, with $C_{\text{conf}} = 0.83$ (which is, it should be remembered, close to the average value observed in France, Spain and Italy during strict lockdown).

We ran simulations with two values of α : $\alpha = 0.6\%$ and $\alpha = 1.2\%$. We found that the predicted number of hospital deaths and ICU needs are almost the same. for both values, in accordance with the observations made previously (if the epidemic is not significant in terms of the number of infected people, the IFR has little influence on the model's predictions of mortality and ICU needs).

In the Table 2, some numbers predicted by the model have been given. The Figures 7 to 8 summarize the evolution of different indicators when strict lockdown is maintained.

		11/5/2020	15/6/2020	31/7/2020	31/8/2020	
	Total deaths at hospital	17399	20791	22009	22224	
	Daily deaths at hospital	165	53	12	5	
$\alpha = 0.6\%$	ICU	2668	68 851 184		66	
	Infected	3362987	3611423	3699615	3715156	
		(5.01%)	(5.38%)	(5.51%)	(5.53%)	
	Recovered	2959254	3468723	3651360	3683642	
	Active cases	386335	121910	26247	9290	
	Total deaths at hospital	17463	21184	22713	23027	
	Daily deaths at hospital	172	62	16	7	
$\alpha = 1.2\%$	ICU	2783	998	255	102	
	Infected	1706272	1854882	1915530	1927987	
		(2.54%)	(2.76%)	(2.85%)	(2.87%)	
	Recovered	1477887	1758469	1873640	1897345	
	Active cases	210924	75230	19178	7615	

Table 2: Scenario 1 (continuation of lockdown in France after 11 May 2020). Main indicators at the date of relaxing lockdown (11/5/2020), 15 June, 31 July and 31 August 2020.

In comparison with scenario 0, we observe that at May 11, 2020, the model predicts that lockdown will save approximately 21720 lifes. The number of deaths per day will be about 165 (compared to 175 on 17 March 2020). About 2,668 places in ICU will remain occupied. However, it should not be concluded that strict lockdown only postponed a situation by two months. It is indeed necessary to take into account delays between infection and admission to resuscitation or death.

On the other hand, the model predicts a number of active cases on 11/5/2017 equal to 386,335 cases. To find an equivalent number of active cases, the model indicates that it is necessary to go back to March 03, 2020 i.e. two weeks before lockdown (see Figure 8). At 17/3/2020 (start of strict lockdown), the number of active cases is estimated at 1,415,775 cases. In terms of the number of active cases, on 11/5/2020, when strict lockdown is due to end, the situation in France will be similar to that of 3 March 2020 (in almost two months, strict lockdown has reduced the number of active cases by a dozen days).

If strict lockdown is extended beyond 11 May, the simulation predicts that the number of deaths per day and the number of occupied ICU beds will drop significantly before the end of June (see Table 2). By the end of July, the total number of hospital deaths will be approximately 22,240 if $\alpha = 0.6\%$ and about 23,025 if $\alpha = 1.2\%$. It will only increase very slowly thereafter.

5.3. Scenarios 2 and 3: direct or progressive moderate deconfinement

The estimation of the daily reproduction number, discussed in section 4, revealed that a progressive deconfinement leading to values of C_n lower than 1 will be difficult to achieve, unless new drastic

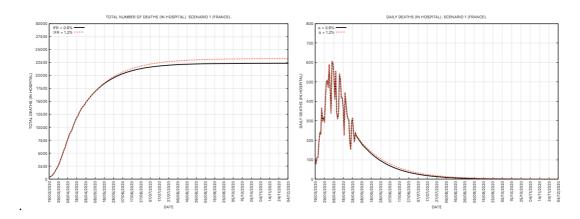


Figure 7: Scenario 1 in France. Left: total number of deaths in hospital. Right: daily deaths in hospital. Values up to 30 April 2020 are actual (public data).

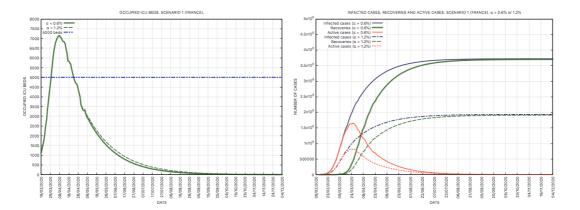


Figure 8: Scenario 1 in France. Left: number of occupied ICU beds (estimated by the model). Right: number of active cases, of the number of infected persons and of recovered persons until December 4, 2020 (estimated by the model). Values up to 30 April 2020 are real (public data).

interventions replace strict lockdown.

Scenarios 2 and 3 look at a lifting of strict lockdown in two ways. The first way (scenario 2) is to move directly to a soft deconfinement by lifting the lockdown abruptly on may 12, 2020. By "soft deconfinement" we mean a slightly relaxed lockdown or a partial lockdown (that is, a situation with strong interventions that are not totally drastic). The second way will be to reach the same deconfined regime in a "gradual" manner, i.e. after a transition phase of one month (from May 12 to June 15, 2020). On arrival (i. e. in deconfinement regime), a daily reproduction number slightly higher than 1 will be imposed.

In the results presented here, we choose $C_n = 1.2$ in deconfinement period (starting May 12 in scenario 2, and reached linearly on June 15 in scenario 3). This value is not very far from that obtained by lockdown. In particular, it is significantly lower than the mean value observed in France the week before the strict lockdown (it was around 1.40, when some interventions to curb the trans-

mission of the virus were already in place). In other words, these two scenarios 2 and 3 are almost minimalist (i.e. without exaggerating the consequences of deconfinement). In both the scenarios, we set $C_n = C_{\text{conf}} = 0.83$ between May 1 and May 11 (the deconfinement date). The data before April 30 are actual.

We impose an infection in-hospital fatality rate $\alpha = 0.6\%$.

The results of the simulations are described in Figures 9, 10 and 11. In both cases, the epidemic is again on the rise, with a time lag of one and a half months between the two scenarios. In both scenarios, the peak of the epidemic will be in the period mid-October 2020 to end November 2020, that is, next fall.

In addition, according to the model, the number of ICU beds required will exceed 5,000 by the end of August 2020 for Scenario 2, and by mid-October for Scenario 3. As of August 31, 2020, the infection rate of the population will be about 12.15% for scenario 2, and 8.67% for scenario 3. These two rates will reach 27.35% and 25.22% by 1 March 2021. In both scenarios, the total number of deaths exceeds 95,000 by the end of February 2021.

In conclusion, a scenario of measured deconfinement, whether sudden or gradual, will not be effective in the mid- or long-term even with strong interventions (i.e. slightly less stringent than those of strict lockdown). Such deconfinement will only push the peak of the epidemic into the last quarter of the year.

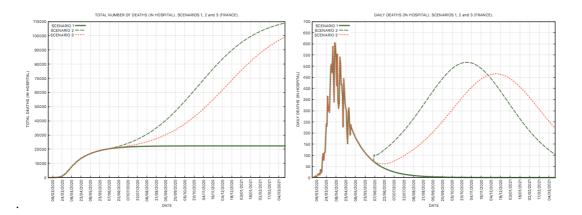


Figure 9: Deconfinement Scenarios 2 and 3 (France). Left: : total number of deaths in hospital. Right: : daily deaths in hospital. Scenario 1 of continuation of strict lockdown is shown for comparison. All Values up to 30 April 2020 are actual (public data).

5.4. Scenarios 4 and 5: periodic (or cyclic) deconfinement

We are now studying original scenarios consisting of alternating two phases: a phase 1 of strict

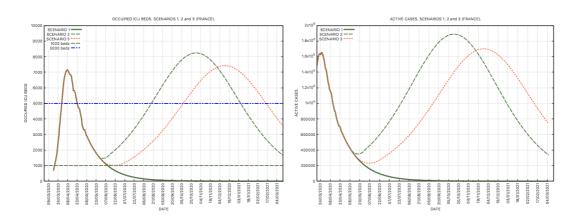


Figure 10: Deconfinement Scenarios 2 and 3 (France). Left: : number of occupied ICU beds (estimated by the model). Right: : number of active cases until 04 March 2021 (estimated by the model). Scenario 1 of continuation of lockdown is shown for comparison. All Values up to 30 April 2020 are actual (public data).

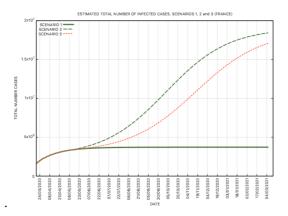


Figure 11: Deconfinement Scenarios 2 and 3 (France). Total number of infected individuals until early March 2021.

lockdown with drastic restrictions, and a phase 2 of moderate deconfinement with slightly less drastic restrictions. It will be assumed that the two phases have the same time duration T/2 (alternating with unequal durations will be discussed in the following scenarios). We impose a daily reproduction number $C_n = C_{\text{conf}}$ in the phase of strict lockdown with $C_{\text{conf}} = 0.83$. In the soft deconfinement phase, a value C_{deconf} is imposed, with $C_{\text{deconf}} = 1.1$ (4th scenario) or $C_{\text{deconf}} = 1.35$ (5th scenario). Qualitatively a value of C_{deconf} close to 1 means that the deconfinement practiced in phase 2 is accompanied by strong interventions to curb the circulation of the virus. A periodicity of T = 2 days is adopted (i.e. strict lockdown every other day). Note that this periodicity does not have much influence on the obtained results (we obtain practically the same results with alternating every other week). We chose to run simulations with a fatality rate $\alpha = 0.6\%$. The simulations with other values of α give qualitatively similar results, but with numbers that may differ.

We are mainly interested in the influence of the daily reproduction number practiced on the days of

deconfinement C_{deconf} .

In figures 12 and 13, the evolution of the main indicators of the evolution of the epidemic was visualized with a periodicity of one day. The curve of active cases 13 shows that scenario 4 leads to the extinction of the epidemic, a little slower than strict lockdown. The cumulative number of inhospital deaths will reach about 25074 on 31 August, and 27900 in early March 2021 (compared to 24600 with continuation of the strict lockdown). By the latter date, the percentage of the population having been infected will be 6.96%. It is therefore not a scenario of herd immunity.

As for scenario 5, the epidemic is curbed but not stabilized. The epidemic rises slowly and then falls back, over several months. The number of hospital deaths will fluctuate between 70 and 160 until February 2021. Similarly, between 1500 and 2300 ICU beds will remain occupied until February 2021. In the long term, the cumulative number of in-hospital deaths will reach around 29800 by the end of August and continue to rise to 50200 by the beginning of March 2021. By the latter date, 12.92% of the French population will have been infected. This scenario is not that of a herd immunity.

Naturally, if we choose a value of C_{deconf} greater than that adopted in this scenario 5 (where $C_{\text{deconf}} = 1.35$), the epidemic will become even more widespread. Unsurprisingly, an alternation of strict lockdown - total deconfinement is to be excluded.

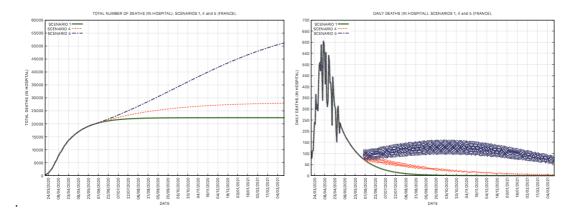


Figure 12: Scenarios 4 and 5 of periodic deconfinement (France). Left: : total number of deaths in hospital. Right: : daily deaths in hospital. Scenario 1 of continuation of strict lockdown is shown for comparison. All Values up to 30 April 2020 are actual (public data).

We conjecture at this point that the extinction condition of the epidemic in this scenario is written as follows

$$C_{mean} < 1, \tag{5.1}$$

where C_{mean} is a mean value of C_{conf} and C_{deconf} . The search for the exact expression of this mean value is a mathematical question that we do not address in this work. However, we can make the approximation that C_{mean} is close to the arithmetic mean of C_{conf} and C_{deconf} (the durations of the two phases being equal). This results in the following approximate criterion for a periodic-type

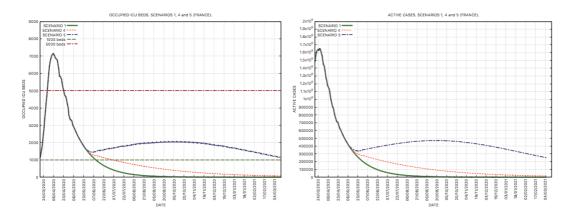
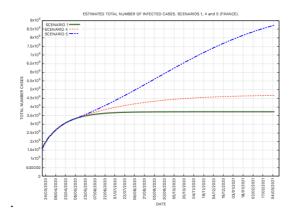


Figure 13: Scenarios 4 and 5 of periodic deconfinement (France). Left: : number of occupied ICU beds (estimated by the model). Right: : number of active cases until 04 March 2021 (estimated by the model). Scenario 1 of continuation of lockdown is shown for comparison. All Values up to 30 April 2020 are actual (public data).





scenario to stabilize or mitigate the epidemic without amplifying it:

$$\frac{C_{\text{conf}} + C_{\text{deconf}}}{2} \leq 1,$$

$$C_{\text{terref}} \leq 2 - C_{\text{conf}}$$
(5.2)

or

$$C_{\text{deconf}} \leqslant 2 - C_{\text{conf}}.$$
 (5.2)

We saw in paragraph 4 that in several countries (including France) the lockdown leads to values C_n in general around 0.80. If we use this value as a reference we deduce the following constraint on C_{deconf} :

$$C_{\text{deconf}} \leqslant C_+ \approx 1.2 \tag{5.3}$$

This approximate criterion is used here, although it is not exact. It defines the level of periodic deconfinement compatible with the control or extinction of the epidemic. We will come back to this point during the so-called zigzag strategy.

5.5. Scenarios 6 to 10: scheduled deconfinement

In this last series of simulations, we imagine epidemic control scenarios based on a precise schedule of strict lockdown on certain days of the week (or of the month) and soft deconfinement on the other days. We will call it a scenario of *weekly organized deconfinement*. One can also adopt a *monthly organized deconfinement*, choosing certain days of the month for strict lockdown.

More generally, such a scenario can be imagined by organizing a duration D (D = 7 when it is a weekly scenario), which will then be repeated identically.

Let $k, 0 \le k \le D$, the number of days of deconfinement over that period. The remaining D - k days are days of lockdown. One of the questions that occurs naturally is how many days per week at most can be relaxed (i. e. softly deconfined) without a resumption of the epidemic?

For simulations, we choose D = 7 (week). We impose on the days of strict lockdown $C_n = C_{conf} = 0.83$ (average value observed during strict lockdown in France). The days of deconfinement (or relaxed lockdown) we impose a rate $C_{deconf} = 1.35 > 1$. The same value of $\alpha = 0.6\%$ is maintained in these simulations (simulations carried out with other values give qualitatively similar results). The scenarios studied correspond to k = 5 deconfinement days per week and D - k = 2 lockdown days (scenario 6), k = 4 (scenario 7), k = 3 (scenario 8), k = 2 (scenario 9) and k = 1 (scenario 10). The evolution of the different indicators is illustrated in the figs 15, 16 and 17. It can be

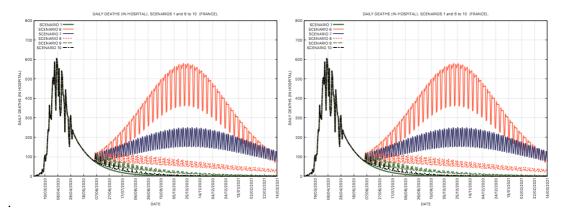


Figure 15: Scenarios 6 to 10: weekly organized deconfinement (France). Left: : total (cumulative) number of deaths in hospital. Right: : dialy deaths in hospital. Scenario 1 of continuation of lockdown is shown for comparison. All Values up to 30 April 2020 are actual (public data).

observed that for 1, 2 or 3 days of deconfinement per week (scenarios 8, 9 and 10 respectively), the epidemic continues to die down at various speeds. On the other hand, when deconfinement occurs 4 or more days per week, the epidemic starts to rise again with a peak reached on mid-October 2020. On March 5, 2021, with 5 days of deconfinement, the model predicts that at least 27.3% of the French population will be infected, compared to 16.75% for 4 days, 9.43% for 3 days of deconfinement, 6.74% for 2 days and 5.90% for one day. So these are not gregarious immunity scenarios.

Based on these simulations, it remains to be determined how many days of strict lockdown within a week are necessary to control the outbreak (we want to define a simple rule). Of course, this number

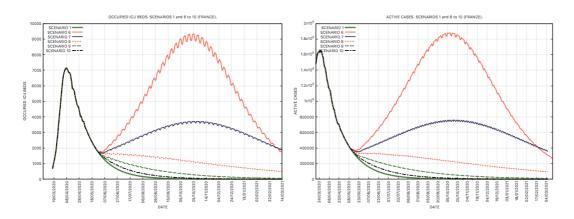


Figure 16: Scenarios 6 to 10: weekly organized deconfinement (France). Left: : number of occupied ICU beds (estimated by the model). Right: : number of active cases until 04 March 2021 (estimated by the model). Scenario 1 of continuation of lockdown is shown for comparison. All Values up to 30 April 2020 are actual (public data).

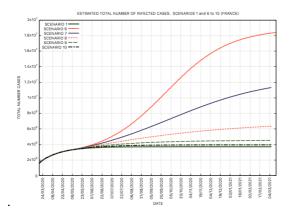


Figure 17: Scenarios 6 to 10: weekly organized deconfinement (France). Total number of infected individuals until early March 2021.

depends on the quality of the deconfinement, i.e. the level of restrictions applied on deconfinement days. As in the previous section, it is assumed that it boils down to a condition of form (5.1) with C_{mean} an average daily rate expressed as a function of C_{conf} and C_{deconf} . Here we will approximate it by th arithmetic mean of C_{conf} and C_{deconf} weighted by number of days in every regime. We get the approximate condition

$$\frac{(D-k)C_{\rm conf} + kC_{\rm deconf}}{D} \leqslant 1,$$

that is,

$$0 \leqslant k \leqslant D \frac{1 - C_{\text{conf}}}{C_{\text{deconf}} - C_{\text{conf}}}.$$
(5.4)

A deconfinement at least one day per week is possible if

$$D\frac{1 - C_{\rm conf}}{C_{\rm deconf} - C_{\rm conf}} \ge 1$$

This conditions means that

$$C_{\text{deconf}} \leqslant C_{\star} \text{ where } C_{\star} = D - (D - 1)C_{\text{conf}}.$$
 (5.5)

In the case of a weekly organized deconfinement the constraint (5.4) is written (with $C_{\text{deconf}} = 0.83$):

$$k \leqslant \frac{1.19}{C_{\text{deconf}} - 0.83},\tag{5.6}$$

where C_{deconf} indicates the level of interventions during deconfinement. In this case $C_{\star} = 7 - 6C_{\text{conf}} \approx 2.02$. Note that this limit is independent of the fatality rate by infection.

Thus, in conclusion, an organized weekly deconfinement makes it possible to stabilize the epidemic under two conditions

- (i) a deconfinement level not exceeding the C_{\star} bar,
- (ii) a number of deconfinement days per week checking the constraint (5.6).

As an example, if we want a deconfinement level comparable to that of the week preceding the decision of lockdown in France, the constraint (5.6) gives $k \leq 2.08$, where we used the value $C_{\text{deconf}} = 1.40$ (mean value observed the week preceding the decision of strict lockdown in France. See paragraph 4). In other words, a deconfinement of 3 days (or more than) per week with interventions comparable to those applied the week before lockdown in France does not guarantee an extinction or stabilisation of the epidemic.

6. A zigzag strategy to control the epidemic

6.1. Schemes and principles of the strategy

We propose here a non-pharmaceutical strategy to get out of the strict lockdown, while stabilizing or gradually reducing the outbreak. To explain this strategy, we need to classify the regime of restrictions into **four lanes**² defined as follows and represented in the Figure 18 below. Let us add that this classification and the resulting strategy are by no means a view of the mind. They stem directly from the detailed study in parts 4 and 5 (see, for example, Figure 19 where the daily reproduction number for France, Spain and Italy, is reproduced with the limits of the four lanes).

- The first lane is the **drastic lane**. This is the situation that results from a regime of drastic restrictions (at least equivalent to strict lockdown). Mathematically, this means that $C_n \leq 1$. In practice, strict lockdown in France, Italy and Spain indicate that this number is generally between $C_- = 0.6$ and 1 with an average of approximately 0.83. This is therefore a *narrow lane*.
- The second lane is the **semidrastic lane**. It is characterized by a slight relaxation of the drastic interventions or by a set of strong interventions not reaching in balance those of a drastic regime. Mathematically, it is characterized here by a daily reproduction number C_n satisfying between $1 < C_n \leq C_+ \approx 1.2$. It is also a very narrow lane. We will see that this lane will play an important role in the deconfinement strategy we are proposing.

²This terminology seemed to us to be adequate because it helps explain this strategy using the analogy of a four-lane highway

- The third lane is the intermediate lane (or cautionary lane). It is characterized by a situation in which the population is alerted of the presence of the virus and adopts precautionary measures and behaviors that are objectively insufficient to limit its circulation. At this stage, public interventions aim to curb the epidemic, without necessarily being restrictive (restaurants, cafés, schools, public establishments and public transport are still open). Mathematically, it is characterized by a daily reproduction number satisfying C₊ ≤ C_n ≤ C_{*}, with C_{*} ≈ 2.
- The fourth lane is the **relaxed lane** (or **carefree lane**). It is characterized by the total or almost total absence of restrictions. It corresponds to the situation of ordinary and unrestricted lifestyle, either because the virus is not present in the population, or because it is still in the introduction stage and that the population is reckless. Mathematically, this lane is characterized by the condition $C_n \ge C_{\star}$.

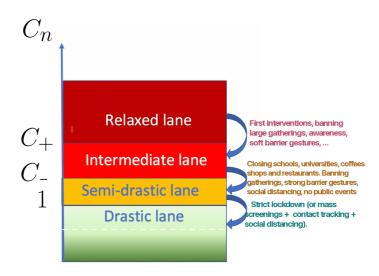


Figure 18: Simplified four-lanes diagram showing the levels of interventions to curb the epidemic.

Let us make some observations:

- Switching from one lane to another is done by adding or relaxing interventions. In view of actual the data, we conjecture here that these interventions are of the order of those indicated on the diagram 18,
- only the **drastic lane** leads to an extinction of the epidemic. The other three lanes are conducive to its spread, but at different rates. Thus, any strategy of deconfinement that excludes the drastic lane will lead to a rebound in the epidemic in the short to medium term,
- the **relaxed lane** is a lane to be excluded in any deconfinement strategy (in the absence of drug solutions). Indeed, it is a way without interventions and is very conductive to contagion. It should not be used in the presence of the virus (even for one day per week).

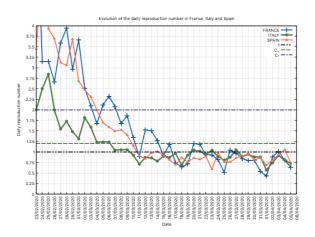


Figure 19: Superposition of the limits of the four lanes with the evolution of the daily reproduction number for France, Italy and Spain (for the period from 23 February to 02 April 2020 during the Coronavirus Sars-Cov 2 pandemic)

These observations explain the dilemma faced by almost every country in the world: in the absence of pharmaceutical solutions, the narrow and very expensive lane of drastic interventions must be taken.

As it stands, the reasonable time frame for quantifying the impact of any intervention is approximately 25 days to 1 month. This is due to the medical characteristics of Covid-19: incubation time, average time to hospitalization or death, length of hospital stay. It is also a delay that allows to measure retroactively the daily reproduction number and and to determine which lane has been taken. However, a practice of mass screening can considerably shorten this time frame and lead to a real-time conduct of the interventions. We will come back to this point later.

In light of the analysis of different exit scenarios studied in section 5, a gradual zigzag strategy for exiting lockdown while controlling the epidemic is proposed here. This strategy is based on a weekly organized deconfinement that can be adjusted over time (as a reminder, weekly organized deconfinement consists of imposing strict lockdown on certain days of the week, and moderate deconfinement on the other days).

This strategy, called **zigzag strategy**, has several phases

- The first phase consists of a weekly organized deconfinement with a maximum of 2 deconfinement days per week. Deconfinement on these two days must be accompanied by strong interventions limiting the circulation of the virus (the effect of which will be measured in the next step). If we take the classification below, this amounts to changing the lane two days a week, as illustrated in the diagram 20 and returning to the drastic lane on the other days (hence the name zigzag strategy). Such deconfinement can tolerate the use of part of the intermediate lane when the number of days of deconfinement is equal or less than 3 days. This lane becomes prohibited when the number of days of deconfinement is greater than 3.
- The transition from one phase to the next is made after measuring the impact of deconfine-

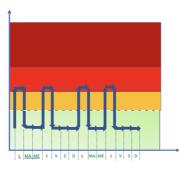


Figure 20: Simplified diagram of a zigzag strategy by a weekly organized deconfinement. Here we have chosen Monday and Thursday as days of deconfinement. The other days of the week are lockdown days. Schematically, deconfinement amounts to a change of lane, which can go up **to the intermediate lane** (because only two days per week are deconfined). The relaxed lane is excluded (or forbidden). When the number of days of deconfinement increases, the intermediate lane may become excluded as well.

ment by estimating the daily reproduction number from the main indicators using the formula (4.1), or possibly the formula (4.2). From this, we deduce C_{deconf} during the days of deconfinement. The number of deconfinement days is then decided in the next phase according to the simplified rule (see paragraph 5):

Number of days of deconfinement per week
$$\leq \frac{1.19}{C_{\text{deconf}} - 0.83}$$
.

The number of deconfinement days may increase, remain the same, or decrease. It decreases if it is found that deconfinement has has not been sufficiently moderate.

This strategy remains flexible. For example, we can adopt a deconfinement at scheduled months, with exactly the same phases, but by replacing the above rule by the rule (5.4) with D = 30.

Similarly, if C_{deconf} is below 1.2, we can also adopt a **periodic deconfinement**: we alternate periods of strict lockdown and deconfinement with equal durations (see diagram 21). Periodic deconfinement has been discussed in paragraph 5. It is illustrated in the diagram in figure 21.

Periodic deconfinement uses only two lanes: the drastic lane and the semi-drastic lane. It has the advantage of allowing a free choice of the length of the period, as it does not have much influence on the results obtained. One can thus opt for every other confined day, or every other confined week, etc. Qualitatively, a periodic deconfinement is equivalent to a weekly organized deconfinement with 3 and a half days of strict lockdown per week. Therefore, its success as a first phase of deconfinement cannot be guaranteed. Nor is it intended to be definitive (the goal being to deconfine completely). It is therefore a solution that can be adopted in the *intermediate stages* of the above zigzag strategy.

It should be noted that this zigzag strategy does not lead to herd immunity (on the horizon,

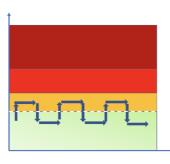


Figure 21: Simplified diagram of a zigzag strategy by periodic deconfinement. Strict lockdown and moderate deconfinement alternate over equal periods of time. Schematically, deconfinement amounts to a change of lane. The intermediate lane and the relaxed lane are prohibited in this strategy.

the rate of infection is less than 10%). It can be used on a local, regional or national scale (with possible variations from one region to another).

6.2. Usefulness of the generalization of screening tests

One of the greatest challenges in the fight against the Sars-CoV-2 Coronavirus pandemic is the estimation of the number of infected cases. The vast majority of these cases develop mild symptoms or are asymptomatic, requiring no hospitalization.

Today, the possibility of mass screening is becoming possible in many countries. In general, tests aim to detect the virus (virological tests) or to detect the presence of antibodies (serological tests). Many questions are raised regarding the use of these tests: privacy issues (in the case of mass tracking), respect for equality between individuals (if only immunized persons are allowed to go to work by issuing a so-called immunological passport), duration of immunity, etc. Moreover, the reliability and accuracy of these tests is itself subject to serious controversy.

Within the framework of the model proposed here and the zigzag strategy screening tests could have a decisive impact on how to manage the pandemics. Indeed, the adjustment of the zigzag strategy at the end of each of the above phases is based on the estimate of the daily reproduction number, which is considered here as the thermometer of the general situation. However, the estimation of this rate must be based on statistically reliable data. The use of fatality figures needs a period of 25 days, due to the delay between interventions and their effects on mortality. This could be slightly shortened by using ICU or hospitalization figures according to the same model.

However, screening tests performed daily on a fairly representative sample in the manner of a survey can be used to infer the percentage of infected individuals in the population. In this case, it becomes possible to switch to a formula for calculating the daily reproduction number based on the infection rate of the population, and not on the number of deaths. Recall that according to (4.2),

this formula is written as follows

$$C_n = \frac{i_n^{\star}}{(1 - \sum_{k=0}^{n-1} i_k^{\star}) \sum_{k=0}^{\ell-1} \lambda_k i_k^{\star}}.$$

Unlike (4.1), this formula does not include the r delay time.

Such a breakthrough would put the finishing touches to the strategy to make it a real-time decisionmaking tool. By measuring the daily reproduction number on a daily basis, we can determine exactly what lane we are on, and therefore adjust the driving of the epidemic, without waiting for hospitalization or death figures.

7. Conclusion

The deterministic model introduced in this study is used to predict the dynamics Covid-19 epidemic and its impact on deaths and ICU occupancy. By relying heavily on public data, the model reveals several characteristics of the epidemic and inspires **a plan to contain or stabilize it without resorting to herd immunity or strict long-term lockdown.**

In the light of this model, it has been shown that **moderate deconfinement with strong but non** drastic interventions, whether gradual or sudden, can lead to a rapid resumption of the epidemic, with saturation of intensive care units in the fall and a peak of the epidemic in winter.

It has also been shown through this model that scenarios alternating strict lockdown and moderate deconfinement can allow the epidemic to be brought under control without resorting to group immunity. The weekly organized deconfinement scenario with some days of strict lockdown and other days of moderate deconfinement allows to curb the epidemic. Similarly, alternating strict lockdown - deconfinement in equal periods of time allows the epidemic to be controlled, provided that deconfinement contains some strong interventions. In the latter scenario, the choice of the length of the alternating period remains free and does not affect this finding. Let us add that in both scenarios, the number of infected individuals remains far from that of herd immunity and does not exceed 10% of the population.

Another finding of this study is that drastic interventions (like strict lockdown) **are barely sufficient to control the epidemic**. There is very little room for manoeuvre to alleviate these drastic interventions while controlling the epidemic. .

In other words, **any lockdown exit strategy must include not only strong interventions but also a calculated dose of drastic interventions** (here, drastic interventions are defined as a set of interventions whose effectiveness when they are in effect is equal to or greater than that of strict lockdown).

Finally, the model and the simulations carried out made it possible to classify interventions into **four lanes**, one of which, the first, is **necessary** in any non-pharmaceutical deconfinement strategy (the drastic lane). The fourth lane is, on the contrary, to be **excluded** in any approach to controlling the epidemic. These lanes are schematized in Figure 18.

The result of all these elements is the gradual **zigzag strategy** that can control the epidemic by deconfinement, without exceeding 10% of infection in the population. **This strategy consists in alternating days of strict lockdown and days of deconfinement according to a precise schedule calculated in advance and dynamically readjustable**. This alternation can be organised by week, month or by any other period other period. In its intermediate stage, it can be periodic, with every other day of lockdown, or every other week, etc.

Schematically, this strategy consists in zigzagging between the different lanes mentioned above (see diagrams 20 and 21). It can be applied at local, regional, or national scales, without being invasive (as it does not require the use of personal data).

It should be noted that regular surveys to measure the infection rate could greatly enhance this strategy by giving it real-time flexibility.

Finally, it should be pointed out that in the case of France, this model reveals that when the strict lockdown is lifted, scheduled for 11 May 2020, the situation will be comparable in terms of the number of active cases to that of 3 March 2020. **By this date, strict lockdown will have saved France around 21,700 deaths**. The continuation of strict lockdown will lead to a significant drop in the number of deaths and the number of beds occupied in intensive care before the end of June At the end of the summer, if strict lockdown is maintained, the number of deaths in hospital will be between 22240 and 23025 (depending on the IFR value). The study also revealed that if average interventions had been applied instead of strict lockdown (after 17 March 2020), the number of ICU beds required would have been around 30,000 at the beginning of June. By mid-June, the number of deaths in hospital in this case would be around 100,000.

A. Appendices

A.1. Formal justification of the model

The purpose of this annex is to set out the main ideas that led to the above model. It can be based on two very simple observations. The first is that at the time of a Covid 19 type crisis, most epidemiological data are communicated on a daily basis. The second observation is that, in general, particular attention is paid to the mortality figures caused by the epidemic. This is a universal marker in all countries of the world, often measured accurately (unlike the number of infected people, which is more difficult to quantify). It is therefore natural to consider a discrete model with the unit of time as the day, and which takes into account the evolution of mortality (and not only the number of infected persons).

We use notations introduced in section 2.

Suppose an infected individual becomes contagious a few days after becoming infected and remains contagious for ℓ successive days. Thus, an individual infected on day J_k becomes contagious from day J_{k+m} and will remain so, at most, until day $J_{k+m+\ell-1}$. It will cease to be contagious from day $J_{k+m+\ell}$. If we now assume that this infected individual is in contact with N susceptible (or healthy) individuals during these days of contagiousness, we can assume that he will infect p_0N persons on the first day, p_1N on the second to $p_{\ell-1}N$ on the last day, where $p_0, \dots, p_{\ell-1}$ are probabilities of

transmission of the disease.

In the absence of isolation measures, these p_i parameters depend on the evolution of the viral load during the period of contagiousness; they are not necessarily equal. We will not fix these coefficients in advance. It is preferable to estimate them from actual data. Note, however, that they can be subject to additional constraints. We will come back to the profile of the parameters during their calculation, in paragraph A.

Note θ_{n-1} the proportion of susceptible (uninfected) individuals at the end of the (n-1)-day:

$$\theta_{n-1} = \frac{S_{n-1}}{P - D_{n-1}},\tag{A.1}$$

where $P - D_{n-1}$ is the population size after the (n-1)-day. Using the identity

$$S_{n-1} + (I_{n-1} - D_{n-1}) = P,$$

we can write

$$\theta_{n-1} = \frac{P + D_{n-1} - I_{n-1}}{P - D_{n-1}} \approx \frac{P - I_{n-1}}{P}.$$
(A.2)

Now, let us note the average number of people (susceptible or not) with whom an infected individual has contaminating contact during the successive days of his or her contagiousness. If we place ourselves at one day J_n , $n \ge 1$, of this period, only the $\theta_n \chi$ part is susceptible, and therefore can be infected by this individual.

We will now count the number i_n of individuals infected on day n. On that day, the contagious individual are those who are infected on days k where k satisfies

$$k + m \leqslant n < k + m + \ell,$$

that is $n - (m + \ell) < k \leq n - m$. Thus,

$$i_n = \sum_{k=n+1-(\ell+m)}^{n-m} p_{n-m-k} \theta_{n-1} \chi_n i_k$$

where χ_n is the average number of individuals encountered by an infected individual on the *n*th day. We can write

$$i_n = \chi_n \frac{P - I_{n-1}}{P} \sum_{k=n+1-(\ell+m)}^{n-m} p_{n-m-k} i_k \text{ pour } n \geqslant m.$$

Thus

$$i_n = \chi_n \frac{P - I_{n-1}}{P} \cdot \sum_{k=0}^{\ell-1} p_k i_{n-m-k} \text{ pour } n \ge m.$$
 (A.3)

We set

$$\bar{p} = \frac{1}{\ell} \sum_{k=0}^{\ell-1} p_k, \lambda_k = \frac{p_k}{\sum_{k=0}^{\ell-1} p_k} \text{ pour } 0 \leqslant k \leqslant \ell - 1.$$
(A.4)

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Hence,

$$\sum_{k=0}^{n-1} \lambda_k = 1. \tag{A.5}$$

We call the *daily reproduction number* on the *n*-th day the nonnegative parameter

$$C_n = \chi_n (\sum_{k=0}^{\ell-1} p_k) = \chi_n \ell \bar{p}.$$
 (A.6)

This parameter C_n is proportional to the average number of people who had contagious contact with an infected individual on the *n*th day, the duration of the contagiousness period and the average probability of transmission (this is similar to the law governing the basic reproduction rate R_0). This coefficient C_n is a marker of the interventions in effect.

If we now go back to the model of the evolution of the size of the infected population i_n we can rewrite the equation (A.3) as follows:

$$i_n = C_n (1 - \frac{I_{n-1}}{P}) \sum_{k=0}^{\ell-1} \lambda_k i_{n-m-k} \text{ pour } n \ge m+r,$$
 (A.7)

We now look at the evolution of the number of deaths. Here, we will assume that this number responds to a fundamental hypothesis for the following: the number of deaths caused by the epidemic before the *n*th day J_n is (uniformly) proportional to the number of individuals infected before (n - r)day, where *r* is *is the average life span* of an individual who died between the time of infection and death. This assumption will be considered true regardless of how this death figure is established (this number may represent in-hospital deaths). From a mathematical point of view, it means that there is a real $\alpha > 0$ factor such that

$$D_n = \alpha I_{n-r} \text{ pour tout } n \ge 0, \tag{A.8}$$

or, equivalently,

$$i_n = \alpha^{-1} d_{n+r}, \ \forall n \ge 0. \tag{A.9}$$

Combining with (A.10) we deduce the following model

$$d_n = C_{n-r} \left(1 - \frac{D_{n-1}}{\alpha P}\right) \sum_{k=0}^{\ell-1} \lambda_k d_{n-m-k} \text{ pour } n \ge m+r.$$
(A.10)

This model aims to describe the evolution of mortality due to the spread of a Covid-19 type epidemic, provided that the coefficients $\lambda_0, \dots, \lambda_k$ are available. In the relation (A.4), we see that these coefficients are related to the parameters (or probabilities) of contagiousness p_0, \dots, p_k that we could suppose to depend essentially on the viral load of the individual during his period of contagiousness.

We do not have a priori a measure of these data. Nevertheless, we choose here not to make any hypothesis to impose values of them, but to use an inverse least squares method to calibrate them with fatality data. The objective is obviously to make this model as close as possible to reality.

When the size of the population is large, it can be considered that in the early stages of the epidemic,

the number of infected individuals remains small with respect to the size of the population and one can write

 $I_n \ll P$,

or, equivalently,

$$D_n \ll \alpha P$$
.

One can thus approach at the beginning of the epidemic the model above by the simplified linearized mode

$$\begin{cases} d_n \approx C_{n-r} \sum_{k=0}^{\ell-1} \lambda_k d_{n-m-k} \text{ pour } n \ge m+r, \\ d_n = 0 \text{ pour } n < r. \end{cases}$$
(A.11)

This linear model can be used in the early stages of the epidemic, when the number of infected individuals is still small relative to the size of the population.

Let us now estime the number recoveries. Note s the average recovery time (for Covid 19, it is estimated at 22 days). Thus the number of individuals healed after the nth day is

$$R_n = I_{n-s} - D_{n-s+r} = (\frac{1}{\alpha} - 1)D_{n+r-s}$$

We are now looking at the number of people in intensive care units. The number of people admitted on *n*-day is $a_n = A_n - A_{n-1}$. If we consider that on average an individual having developed a severe form of Covid-19 stays *p* days in ICU, we can deduce that at the end of *n*-day, the number of individuals in ICU varied from $a_n - a_{n-p}$. Thus, at the end of the *n*-day the number of individuals in ICU is

$$A_n^{\star} = A_{n-1}^{\star} + (a_n - a_{n-p}).$$

Thus,

$$A_n^{\star} = \sum_{k=0}^n (a_n - a_{n-p}) = A_n - A_{n-p}.$$

Finally get the relation

$$A_n^{\star} = \frac{\beta}{\alpha} (D_{n+r-t} - D_{n+r-(t+p)})$$

A.2. Identification of transmission coefficients by a least squares method

Here we explain the least-squares technique used to identify the transmission coefficients $(\lambda_0, \dots, \lambda_{\ell-1})$.

So let us assume that we have the fatality figures within a time window of $K + (\ell + m) + 1$ days $\{J_{L+2-(\ell+m)}, \dots, J_{L+K}\}$, where $K \ge 1$ is fixed.

In practice, this window is chosen so that the mortality figures are significant, i.e. not in the days when the epidemic begins to claim the first victims. Furthermore, it will be assumed that over the sub-window of time $\{J_{L+1}, \dots, J_{L+K}\}$ the interventions to contain the epidemic have varied little, i.e. the daily reproduction number remains essentially constant over this small period equal to an unknown C value. In the Table 3 below in the appendix, the selected window was indicated for some countries. The coefficients $\lambda_0, \dots, \lambda_{\ell-1}$ are estimated so that the values predicted by the model $(d_j^*)_{L+2-(\ell+m) \leq j \leq L+K-m}$ are as close as possible to the figures actually observed $(d_j^*)_{L+1 \leq j \leq L+K}$. Specifically, we will look for $C, \lambda_0, \dots, \lambda_{\ell-1}$ in the form $C = \bar{\mu}$ and $(\lambda_0, \cdots, \lambda_{\ell-1}) = (\frac{\mu_0}{\bar{\mu}}, \frac{\mu_2}{\bar{\mu}}, \cdots, \frac{\mu_{\ell-1}}{\bar{\mu}})$ with $\bar{\mu} = \frac{1}{\ell} \sum_{k=0}^{\ell-1} \mu_k$ and $\mu_0, \cdots, \mu_{\ell-1}$ solutions to the constrained least squares minimizatio problem

$$\min_{\mu_0,\cdots,\mu_k} \sum_{n=L+1}^{L+K} (d_n^{\star} - \sum_{k=0}^{\ell-1} \mu_k d_{n-m-k}^{\star})^2, \quad \mu_0 \ge 0, \cdots, \mu_{\ell-1} \ge 0,$$
(A.12)

This problem can be written into the form

$$\min_{U} \frac{1}{2} U^{t} A^{t} A U - A^{T} B^{T} U, \text{ under the constraint } U \ge 0,$$
(A.13)

where $U = (\mu_0, \dots, \mu_{\ell-1})^T$ contains all the unknow coefficients, $A \in \mathbb{R}^{K \times \ell}$ is the rectangular matrix whose coefficients are

$$(A)_{i,j} = d^{\star}_{L+1+i-m-j} \text{ pour } 1 \leqslant i \leqslant K, \ 1 \leqslant j \leqslant \ell.$$

and $B = (d_{L+1}^{\star}, \dots, d_{L+K}^{\star})^T$. This is a quadratic programming problem whose matrix is $A^t A$ which is positive semidefinite, but not generally positive definite. It will be replaced by the slightly perturbed problem

$$\min_{U \in \mathbb{R}^{\ell}} \frac{1}{2} U^{t} Q_{\varepsilon} U - A^{T} B^{T} U, \text{ under the constraint } U \ge 0,$$
(A.14)

where

$$Q_{\varepsilon} = A^t A + \varepsilon I_{\ell},\tag{A.15}$$

where $\varepsilon > 0$ is a sufficiently small parameter and I_{ℓ} is the identity matrix of size $\ell \times \ell$ (we will choose $\varepsilon = 0.001$ in practice). The matrix Q_{ε} is clearly defined positive and the problem (A.14) admits a unique solution $U^{\varepsilon} = (\mu_0^{\varepsilon}, \dots, \mu_k^{\varepsilon})$. Other constraints to this quadratic programming problem may be added, such as if we want to take into account the evolution of an infected person's contagiousness. Indeed, contagiousness generally depends on the evolution of the viral load over the period of transmission. For example, it increases up to a maximum value and then decreases until the end of the contagiousness period. We choose to translate this into a constraint of the convexity type:

$$\mu_i \ge \frac{\mu_{i-1} + \mu_{i+1}}{2}$$
, pour $1 \le i \le \ell - 2$,

which we can rewrite as follows

$$\mu_{i-1} - 2\mu_i + \mu_{i+1} \leqslant 0$$
, pour $1 \leqslant i \leqslant \ell - 2$. (A.16)

In addition, in order to avoid profiles with increasing coefficients, it is possible, for example, to indicate that the person is, on average, more contagious over the entire period than at the end, that is,

$$\mu_{\ell-1} \leqslant \frac{1}{\ell} \sum_{k=0}^{\ell-1} \mu_k = \frac{1}{\ell}.$$
(A.17)

Simple software was used to solve this optimization problem. Since the number of unknowns is very low in practice ($\ell = 17$), the cost of the calculation is negligible. The values obtained for some countries are summarized in Table 3.

A.3. Appendix 3: Coefficients of transmission by country (calibrated). Pandemic Covid-19.

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						1			
	FR	IT	ESP	USA	UK	GER	KOR	BEL	WORLD
Period of	23/3/2020	27/3/2020	18/3/2020	17/3/2020	23/3/2020	8/4/2020	19/3/2020	22/3/2020	31/3/2020
calibration	- 2/4/2020	- 6/4/2020	- 28/3/2020	- 27/3/2020	- 2/4/2020	- 17/4/2020	- 29/3/2020	- 31/3/2020	- 9/4/2020
λ_1	0.1176	0.1176	0.1176	0.1176	0	0.1176	0	0.1176	0.1176
λ_2	0.1103	0.1103	0.1103	0.1103	0.0617	0.1103	0.0173	0.1103	0.1103
λ_3	0.1029	0.1029	0.1029	0.1029	0.1233	0.1029	0.0346	0.1029	0.1029
λ_4	0.0956	0.0956	0.0956	0.0956	0.1147	0.0956	0.0518	0.0956	0.0956
λ_5	0.0882	0.0882	0.0882	0.0882	0.106	0.0882	0.0691	0.0882	0.0882
λ_6	0.0809	0.0809	0.0809	0.0809	0.0973	0.0809	0.0864	0.0809	0.0809
λ_7	0.0735	0.0735	0.0735	0.0735	0.0887	0.0735	0.1037	0.0735	0.0735
λ_8	0.0662	0.0662	0.0662	0.0662	0.08	0.0662	0.1104	0.0662	0.0662
λ_9	0.0588	0.0588	0.0588	0.0588	0.0714	0.0588	0.1171	0.0588	0.0588
λ_{10}	0.0515	0.0515	0.0515	0.0515	0.0627	0.0515	0.1024	0.0515	0.0515
λ_{11}	0.0441	0.0441	0.0441	0.0441	0.054	0.0441	0.0878	0.0441	0.0441
λ_{12}	0.0368	0.0368	0.0368	0.0368	0.0454	0.0368	0.0732	0.0368	0.0368
λ_{13}	0.0294	0.0294	0.0294	0.0294	0.0367	0.0294	0.0585	0.0294	0.0294
λ_{14}	0.0221	0.0221	0.0221	0.0221	0.0281	0.0221	0.0439	0.0221	0.0221
λ_{15}	0.0147	0.0147	0.0147	0.0147	0.0194	0.0147	0.0293	0.0147	0.0147
λ_{16}	0.0074	0.0074	0.0074	0.0074	0.0107	0.0074	0.0146	0.0074	0.0074
λ_{17}	0	0	0	0	0	0	0	0	0

Table 3: Coefficients of coronavirus transmission Sars-2019 by country (calibrated) (FR: France, IT: Italy, ESP: Spain, USA: United States of America, UK: United Kingdom, GER: Germany, KOR: South Korea, BEL: Belgium, WR: World.

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