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▶ To cite this version:

Yukiko Osawa, Abderrahmane Kheddar. Detection of Human Contact by Thermal Exchange Observer of Robot Skin. 2020. hal-02559722v1

HAL Id: hal-02559722 https://hal.science/hal-02559722v1

Preprint submitted on 4 May 2020 (v1), last revised 10 Dec 2020 (v2)

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Detection of Human Contact by Thermal Exchange Observer of Robot Skin

Yukiko Osawa¹, Member, IEEE, and Abderrahmane Kheddar², Senior Member, IEEE

Abstract-Physical human-robot interaction (pHRI) enables to achieve various assistive tasks for people by robots such as collaborative robotics or motion assistance. It pertains both planning-control and hardware considerations. We propose a new soft robot skin that can detect human contact through thermal features. An electrically conductive pipe is interposed between graphite sheet that has high heat conductivity and soft material for cover compliance. Then the temperature of the water pipe is controlled by a heat source and a small water pump. Besides, an observer for estimating heat flow is implemented; it can detect human interaction by measuring the temperature change of the water pipe. Hence, there is no need to attach sensors to the robot skin's surface, which can be kept soft and eventually textured with a desired pattern. We assessed the validity of the prototype in experiments of contact detection by human fingers.

I. INTRODUCTION

Physical interaction between human and robot enables to achieve various robot tasks: helping a frail person in daily life, programming a robot in manufacturing through touch guidance and demonstration, etc. In order to achieve such tasks like a human, robots need the physical features such as soft texture and warmth giving from human skin, which every human has, for providing pleasantness to touch and a kind of a secure feeling. Therefore, thermal exchanges and softness or touch material properties of the robot cover play an important role in embodiment, acceptability, and human friendliness. We claimed that soft material covering a robot –called robot skin, that has the thermal capabilities is one of the solutions for promoting pHRI.

Indeed, human-robot physical interaction has several positive effects, especially in caring for humans. For example, patients who are touched by a nurse before their surgical operation have a lower stress level [1]. The study in [2] shows that a gentle stroking touch lower blood pressure and increase transient sympathetic reflexes. The feeling of pleasantness generated from physical interaction has been analyzed in neuroscience and psychological fields. The study suggests the correlation between stimulus frequency and pleasantness [3]. Besides, contact force of a finger sliding has been analyzed in the spatial domain [4]. In particular, warmth in physical interactions gives us beneficial effects. The literatures [5], [6] show physical interactions with warm mediated touch devices generated in a stronger sense of trust



Fig. 1. Prototype of the robot skin.

and friendship. Therefore, texture, softness, and temperature on the contact surface affects human feeling. In this domain, we focus our investigations on combining a cover that gathers both thermal exchanges and softness. In [7] we propose a cover soft cover technology with thermal display capabilities. In this paper, we address the other aspect that is of prime importance in human-robot pHRI: the ability for the robot to detect human touch. The novelty of our approach w.r.t existing state of the art contact detection, is in using solely thermal exchange observers through the robot cover.

II. Related work

There are several existing methods for detecting human contact by using various sensors technology. In fact, all existing artificial robot skins are made exactly for that purpose! A large coverage of tactile sensing technologies is thoroughly reported in [8], [9]. This area of research is rich, with extensive different transduction technologies ranging depending on the robotic application requirements. There are also tactile sensing technologies based on printed electronics techniques [10], including deformable and even stretchable support and transduction. Such technologies allows more sophisticated tactile sensing that goes beyond touch, and not all of them embed also thermal exchange sensing as part of the skin.

There are also a class of different approaches for robot touch detection that do not require a dedicated skin and uses existing internal robot sensors that serve other purpose. The excellent survey by [11] summarized such methods of robotic contact sensing. Such method relay in principle on an observer that can reliably detect contact through expected versus actual state residuals. For example, [12] proposed the momentum observer, that has been extended even for lowcost personal robots, considering non-linear effects such as

^{*}This work was supported by JSPS Overseas Research Fellowships No.201960463.

¹CNRS-University of Montpellier, LIRMM, Interactive Digital Humans group, Montpellier, France yukiko.akiyama@lirmm.fr

²CNRS-University of Montpellier, LIRMM, Interactive Digital Humans group, Montpellier, France kheddar@lirmm.fr



Fig. 2. Proposed robot-skin system.

backlash and friction [13]. Such methods can perform even better when combined with existing (if any) robot terminal points force sensing [14], [15] in multi-contact. In [16] a contact detection method uses only joint encoders and learned robot motion dynamics.

Our aim is to achieve robot covers that are soft and capable of thermal display [7]. Our idea is to exploit the thermal cover duality in both displaying and detecting of human touch through monitoring the thermal exchange in the process of robot skin thermal regulation. To our best knowledge, this idea is totally new.

There are many kinds of thermal displays based on a Peltier pump heat source that can either heat or cool the surface based on the Peltier effect [17], see e.g. in haptics [18], [19], [20]. Our soft robot skin uses thermal transfer through water flow [7], and our idea builds on the structural design of our robot skin.

Our paper proposes a method to allow our robot skin to also detect human contact by estimating heat flow on its surface. Our main contributions are specifically as follows:

- with respect to [7] we considered a better thermally conductive outer layer and water-pipe to compose our soft robot skin;
- we control directly the water pipe temperature from the heat source (Peltier pump as in [7]) attached to a small water tank, and show that human contact can be detected through thermal features;
- there is no sensor on the robot outer skin; hence its surface can be kept soft, thermal conductive and can be patterned with different texture serving human touch requirements and eventually easthetics.

Figure 1 shows the developed prototype of the robot skin. An electrically conductive pipe, different from that of [7] is interposed between the graphite sheet (the new outerlayer) and the soft material. In this paper, the temperature of the water pipe is controlled directly by a heat source and a small water pump. Besides, an observer for estimating heat flow is implemented for detecting human interaction without using sensor on the surface of the prototype. We assessed the validity of our idea through a prototype of the robot skin in experiments of contact detection by human fingers.



Fig. 3. Modeling the prototype of the robot skin.

III. DESIGN STRUCTURE OF THE ROBOT SKIN

Figure 1 shows the developed prototype of the robot skin, which size for our study investigations is 30 mm \times 10 mm. This is because a free sample come at this dimension. This prototype is made to assess our proposed human touch detection method with a revisited version of our robot skin in [7]. For circulating water inside of the robot skin, we use another water pipe with an inner diameter of 1.9 mm. This pipe is made of nickel and copper, and was chosen for its high thermal conductivity. It is interposed between a graphite sheet and a foam material. The graphite material having a relatively high thermal conductivity, is used instead and in place of skin's upper layer composite material in [7]). Its role is to display a user-programmed or context-defined thermal behavior of the robot. The foam material composing the compliant part of the skin is similar to [7]. The thickness of the sheet and the foam layer is 0.5 mm and 5 mm, respectively. A silicone pipe with inner diameter of 3.0 mm is used for connecting the water pump and the water tank, and the value of the diameter is used for calculating the water-flow model as a characteristic diameter.

Our system is shown in Fig. 2. By varying the temperature T_p of the Peltier pump connected to the water tank, the temperature T_w of the water pipe is controlled to the desired temperature. At the same time, human contact is detected by monitoring the temperature change of T_w ; it means that any sensor on the surface of the prototype is not needed. In this paper, we refer to this system as "the robot-skin system". The proposed detection method is explained in the next section.

IV. PROPOSED DETECTION METHOD

A. Modeling of the robot-skin system

Thermal systems can be modeled based on a thermal network method where thermal properties are expressed as electric circuits analogies. The Fig. 3 shows the thermal model adopted for the prototype of robot skin, where T_w , T_g , C_w , C_g , R_g , q_p , q_i , q_{aw} , and q_{ag} stand for temperature of the water pipe, temperature of the graphite sheet, thermal capacitance of water pipe and graphite sheet, thermal resistance

between the pipe and the sheet, heat flow from the Peltier pump, heat flow from human finger, and heat dissipation of the air at the pipe and the sheet, respectively. To apply the model to the thermal network method, thermal resistance and thermal capacitance of the water pipe are defined as

$$R_w = \frac{1}{hA} \tag{1}$$

$$C_w = c_p \rho V, \tag{2}$$

where R_w , h, c_p , ρ , A, and V stand for thermal resistance of the water pipe, convection heat-transfer coefficient, specific heat and density of water, area and volume of the water tank, respectively. Here, q_{aw} and q_{aq} are derived as

$$q_{aw} = \frac{T_w - T_a}{R_{aw}} \tag{3}$$

$$q_{ag} = \frac{T_g - T_a}{R_{ag}},\tag{4}$$

where T_a , R_{aw} , and R_{ag} denote ambient temperature, thermal resistance of air at the water pipe and the graphite sheet, respectively.

The value of h switches depending on the case of water flowing or not; this is because the thermal phenomenon changes heat transfer to pure heat conduction through the water when water flow stops. Base on the empirical relationship for laminar flow [21], heat transfer coefficient is derived as

$$h = \begin{cases} \frac{k_c}{d} & (v = 0) \\ \frac{k_c}{d} \left(3.66 + \frac{0.0668 (d/L) \left(\frac{\rho v d}{\mu}\right) \Pr}{1 + 0.04 \left((d/L) \left(\frac{\rho v d}{\mu}\right) \Pr\right)^{2/3}} \right) & (v > 0), \end{cases}$$

where k_c , d, L, ρ , μv , and Pr stand for thermal conductivity, diameter of the pipe, length of the pipe and the tank, density, viscosity, velocity of water flow, and Prandtl number, respectively.

The block diagram of the robot-skin system is shown in Fig. 4. Based on this figure, the transfer function of the robotskin system is obtained as

$$\frac{T_w}{\left(q_p - q_{aw}\right)} = \frac{R_g C_g s + 1}{R_g C_w C_g s^2 + \left(C_w + C_g\right) s},\tag{5}$$

where *s* is the Laplace operator. This model includes two thermal capacitances and the structure is similar to two inertia system in a mechanical system too. An observer for estimating heat flow from human finger (our any external touch) q_i is calculated based on this thermal model.

B. Thermal exchange observer

To detect the thermal response of the robot's skin changed by human interaction, heat flow needs to be monitored. Heat flux sensor can obtain a heat flow response easily, but it biases heat conduction from a heat source and is difficult to design it soft on a surface. In this paper, heat flow from a human finger is estimated by temperature information obtained by the thermocouple attached to the electrically



Fig. 4. Block diagram of the robot-skin system.



Fig. 5. Block diagram of the thermal exchange observer.

conductive pipe. For sensing human interaction, an observer for estimating heat flow shall be implemented. The algorithm of this observer is based on a disturbance observer [22] that has a useful structure and can apply in many fields of control systems. Indeed, this observer can estimate heat flow in the load side of a control system and is suitable for this case. Therefore, the observer is applied to the prototype and called "thermal exchange observer" in this paper. From Fig. 4, the transfer function from q_i to T_w can be calculated as

$$\frac{T_w}{q_i} = \frac{\left(R_g C_w s + 1\right) \left(R_g C_g s + 1\right)}{R_g C_w C_g s^2 + \left(C_w + C_g\right) s}$$
(6)

Here, the transfer function was calculated except q_{ag} and the effect of q_{ag} adds to the estimated value derived from the observer at the end of the calculation. Therefore, T_w is expressed by using the thermal model as

$$T_{w} = \frac{R_{g}C_{g}s + 1}{R_{g}C_{w}C_{g}s^{2} + (C_{w} + C_{g})s} (q_{p} - q_{aw}) + \frac{(R_{g}C_{w}s + 1)(R_{g}C_{g}s + 1)}{R_{g}C_{w}C_{g}s^{2} + (C_{w} + C_{g})s} q_{i}.$$
(7)

Based on eq. (7), the observer for estimating q_i is derived as

$$\hat{q}_{i} = \frac{\left(R_{g}C_{w}C_{g}s^{2} + \left(C_{w} + C_{g}\right)s\right)T_{w} - \left(R_{g}C_{g}s + 1\right)\left(q_{p} - q_{aw}\right)}{\left(R_{g}C_{w}s + 1\right)\left(R_{g}C_{g}s + 1\right)}$$
(8)

Here, ^ denotes the estimated value. By using eq. (8), a structure of the observer is expressed as shown in Fig. 5.



Fig. 6. Control algorithm of the robot-skin system.

V. TEMPERATURE CONTROL SYSTEM

Figure 6 shows whole control system. The temperature of the flowing water is controlled by the Peltier pump attached to the water tank. Since the Peltier pump has a nonlinear behavior [7], a discrete-time autoregressive moving average (ARMA) model is used [23] for temperature controlling of the Peltier pump. As for the controller, a model preview controller (MPC) is also used to regulate the temperature of the robot-skin system. The cost function with the constraints are calculated as:

$$\min \sum_{i=1}^{H} \|\hat{T}_{w}(k+i|k) - T_{w}^{\text{cmd}}(k+i|k)\|_{W_{1}}^{2} + \sum_{i=0}^{H-1} \|\hat{T}_{p}(k+i|k)\|_{W_{2}}^{2}$$
(9)

subject to

$$T_w(k+1) = \left(1 - \frac{1}{R_w C_w} t_s\right) T_w(k) + \frac{1}{R_w C_w} t_s T_p(k) - \frac{q_{aw}(k)}{C_w} \quad (10)$$
$$T_{\min}^{\text{th}} \le T_p(k) \le T_{\max}^{\text{th}}, \quad (11)$$

where k, H,
$$W_1$$
, W_2 , t_s , T_w^{cmd} , T_{min}^{th} , and T_{max}^{th} stand for the discrete time, prediction horizon, weight values of the cost function, sampling time, temperature command of T_w , and minimum and maximum value of threshold of the calculated input, respectively. Here, temperature response of the Peltier pump T_p is the input of the MPC. The first term of (9) works for tracking the temperature of the water pipe T_w to its temperature command T_w^{cmd} , and the second one is for suppressing rapid change of the input T_p . In the case where the temperature response is larger than its temperature command, the velocity of water flow turns to 0 m/s for stopping heat transfer from the Peltier pump. It is possible to cool water by cooling the Peltier pump, but it takes time because the thermal capacitance of the water is too large. Therefore, water is cooled using natural heat loss after the response achieving the desired temperature.

As for contact detection, the thermal observer can be based only on the heat flow from the human finger, and the estimated value is not influenced by the temperature control.



Fig. 7. Experimental setup.



Fig. 8. Experimental results of temperature control.

It means the detection of human contact while controlling the temperature is possible using our proposed detection system.

VI. EXPERIMENTS

A. Outline

Fig. 7 shows the experimental setup. Two Peltier pumps $40\text{mm} \times 40\text{mm}$ were used for heating the water tank $40\text{mm} \times 80\text{mm}$, and the heat sink and the fan was attached to the



Fig. 15. Estimated heat flow of one finger contact. Fig. 16. Estimated heat flow of two fingers contact. Fig. 17. contact.

TABLE I Parameters for experiments.

Parameter	Description	Value
ts	sampling time	1.0 ms
k_c	Thermal conductivity of water	0.1 m W/mK
c_p	Specific heat of water	4.208 kJ·K/kg
ρ	Density of water	999.8 kg/m ³
μ	Viscosity of water	1.55 kg/ms
d	Diameter of the pipe	3.0×10^{-3} m
L	Length of the pipe	0.11 m
Α	Area of water tank	$3.2 \times 10^{-3} \text{ m}^2$
V	Volume of water tank	$3.2 \times 10^{-5} \text{ m}^3$
Pr	Prandtl number	11.35
C_w	Thermal capacitance of water pipe	0.134 J/K
C_q	Thermal capacitance of graphite sheet	0.0124 J/K
R_q	Thermal resistance of graphite sheet	10.0 K/W
R _{aw}	Thermal resistance of air at water pipe	2100 K/W
R_{ag}	Thermal resistance of air at graphite sheet	1.0 K/W
T_{min}^{th}	Minimum value of threshold of T_p^{cmd}	7 °C
T_{max}^{th}	Maximum value of threshold of T_p^{cmd}	37 °C
T_{w}^{cmd}	Desired temperature command	24–28 °C
\tilde{H}	Prediction horizon	100
W_1	Weight value of eq. (9)	1.0
W_2	Weight value of eq. (9)	0.03
K_p	Proportional gain	0.1
$\hat{K_i}$	Integral gain	0.03

Peltier pumps at back sides for heat radiation. To measure the temperature, the thermocouples were attached to the Peltier pumps and the electrically conductive pipe of the prototype. There are two kinds of experiments. First, the temperature controller was verified. The temperature command T_w^{cmd} was set to 24, 26, and 28 °C, and T_p was controlled based on its command T_p^{cmd} derived from the MPC. The velocity of the water pump keeps 0.141 m/s, except for the case where T_w is larger than its command. Second, the detection



Fig. 18. Estimated heat flow of three persons data.

method was verified. The temperature command T_w^{cmd} was set to 24°C, and heat flow from human fingers was estimated by the thermal exchange observer explained in Sec. IV-B. Since there is no sensor on the surface of the graphite sheet and T_g can not be obtained, q_{ag} was calculated using T_w instead of T_g in the experiments. For investigating the relationship between the heat flow and contact area/position, two cases of detection tests were compared in the case of contacting one/two/three fingers. The estimation results are compared to the data from three persons: age is 27–28 years old (man1, woman1, woman2). As for the second case, the values were compared in different contact positions; case1 (near the thermocouples), case2 (middle), and case3 (far from



Fig. 19. Estimated heat flow comparing finger positions.

the thermocouples). In these experiments, the human finger contacted the prototype every 3 seconds. The parameters for the experiments were summarized in Table I.

B. Experimental results

Experimental result of temperature control is shown in Fig. 8, the temperature dynamic change is known to be slow. It shows that the temperature of the water pipe tracked to its temperature command. The responses exhibits chattering sometimes around the desired temperature because the water pump repeatedly switch on and off when the response reaches its desired valued. Experimental results of detection for one/two/three fingers are shown in Figs. 9 to 17. In every cases, temperature of the pipe was controlled to 24 °C, other than the time that human contacted the prototype. From Figs. 15, 16, and 17, the estimated heat flows from human fingers tend to increase alongside the larger contact area (number of fingers). The three persons results were summarized in Fig. 18, and these results exhibits similar tendency although variations depending on persons can be observed. Figure 19 shows the estimated heat flow in the case 1, 2, and 3. The figure shows that heat flow from a finger is also changed depending on the contact positions. This is because thermal attenuation occurs depending on the distance between contact position and a thermocouples. The theoretical explanation about this is mentioned in [24], [25]. Therefore, the estimated heat flows were influenced by the contact area and positions. Since the prototype is small in size and it could be verified only contacting one to three fingers, other contact taxonomies such as grasping, holding, and stroking will be tested in future work with a integrated whole-scale system.

VII. CONCLUSION AND FUTURE WORK

This paper proposed a new soft robot skin that can at a time display thermal behavior of the robot, and still detect human contact through transient thermal exchange monitoring when touched by a human. For detecting human interaction, the thermal exchange observer was implemented in the control system; it works by estimating heat flow, which value changes depending on the temperature of the water pipe. Therefore, the detection method does not need to measure temperature on the robot skin, and its surface can be keep soft and patterned at will. The validity of the proposed system was confirmed by some experimental results. For future work, we aim to extend our algorithm to detect multi-point contact and identify the nature of touch beyond human through the signature of the heat flow dynamics and softness. Moreover, the value of the estimated heat flow will be utilized to detect precise human interaction, such as the grasping area, strength, and human body temperature. We will also improve a heating and cooling system to be more effective, and will cover important areas of the humanoid robot by the soft thermal robot skin.

Acknowledgment

This work was supported in part by JSPS Overseas Research Fellowships No. 201960463.

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