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An atomistic study of the structural changes in a Zr-Cu-Ni-Al glass-forming liquid on vitrification monitored in-situ by X-ray diffraction and molecular dynamics simulation

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Abstract

Structural changes in the $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ liquid alloy on cooling from above the equilibrium liquidus temperature are studied by synchrotron radiation X-ray diffraction and compared with the results of first-principles molecular dynamics simulation. In-situ vitrification of the studied alloy is achieved using a containerless levitation technique. Subsequent analysis of the atomic and electronic structure of the alloy in liquid and glassy states reveals formation of medium-range order on cooling and its relationship with liquid fragility. The structural changes in this alloy are smaller in comparison with a more fragile one.

Keywords: metallic glass; liquid; fragility; X-ray diffraction; structure; synchrotron radiation

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1. Introduction

The high glass-forming ability (GFA) of some alloy compositions allowed production of bulk metallic glasses (BMGs) (also called glassy alloys) in the thickness range of 1-100 mm using various casting processes [1,2]. Zr-based BMGs are among the best metallic glass-formers known to date [1-3] which thermal stability is also good [4]. Formation of a glassy phase in both Zr–Cu and Zr–Ni alloys is strongly enhanced by the addition of Al thus forming ternary and quaternary bulk metallic glasses with good glass-forming ability [1-5]. The atomic structure of these BMGs at room temperature was studied in detail [6,7].

Liquids retain their volume as crystals but flow under the action of gravity [8,9]. They constantly undergo a restructuring of the atomic structure [10,11]. Above the equilibrium liquidus temperature (T_l) and slightly below it metallic melts show nearly Arrhenius-type temperature dependence of viscosity (η):

$$\eta = \eta_0 \exp(E_a / RT) \quad (1)$$

where η_0 is a pre-exponential factor, R is the gas constant and E_a is an activation energy [12]. However, on cooling below the liquidus temperature, starting from a crossover temperature [13], they exhibit a non-Arrhenius temperature dependence on viscosity which is known as *fragility* of liquids [14,15].

Here one should mention that anomalous variation in a liquid viscosity in the vicinity of T_l and above it was observed for Fe- [16,17] and Zr- based glass-forming alloys [18] as well as for Al-based crystalline alloys [19]. The authors stated that liquid metallic alloys can have various structural states and significant overheating is required to dissolve clusters inherited from the solid state and to reach equilibrium liquid structure. The existence of liquid-liquid transitions in deeply supercooled state found for water [20], molecular liquids [21,22] (confirmed by computer simulation [23]) and even metallic glasses [24] should also be taken into account when describing fragility.

The inverse temperature - logarithmic viscosity plot [25,26] with some limitations [27,28] is a very useful illustration of the difference between so-called “strong” and “fragile” liquids [29,30]. Fragility is also related to the glass-forming ability of BMGs [31,32] (with some argumentation [33])

partly because stronger liquids, in general, have a higher viscosity in the entire temperature range from T_l down to T_g . There are also experimental results which indicate correlation between liquid fragility and vibrational properties of the glass below T_g [34]. The fragility index (m) [35,36] of the supercooled liquid is calculated slightly above the glass-transition temperature (T_g) as a derivative:

$$m = d \log(\eta) / d(T_g/T) \quad (2).$$

Another way of representation of fragility is a famous Vogel-Fulcher-Tammann-Hesse equation [1]:

$$\eta = \eta_0 \exp[D^* T_0 / (T - T_0)] \quad (3)$$

where η_0 , D (as an indicator of the fragility) and T_0 are the fitting parameters. This equation is widely used but describes the temperature dependence of viscosity well only in an intermediate temperature region [37]. While some other equations make a better representation of the entire viscosity plot [38,39] they have a larger number of fitting parameters which physical meaning could be less clear.

On the other hand fragility can be expressed by the ratio of the activation energies for viscous flow in the equation (1) at low (E_L), (close to T_g) and high (E_H) temperature region (slightly above T_l) [40,41]:

$$R_D = E_L / E_H \quad (4).$$

Other methods are also used to describe and separate thermodynamic and kinetic fragility [42].

Metallic glasses exhibit structural changes in the supercooled liquid state and such changes are found to be responsible for the liquid fragility. A relatively fragile $\text{Pd}_{42.5}\text{Cu}_{30}\text{Ni}_{7.5}\text{P}_{20}$ melt (its fragility index m is close to 60 [43]) during cooling was studied by using the real-space pair distribution function (G) (which is a reduced radial distribution function (RDF)) [44] and compared to the results obtained by the first-principles calculations. As a result strong correlation between the structural changes and the variation of viscosity was observed in the supercooled liquid [45]. The rate of structural rearrangements on cooling was enhanced in the supercooled liquid close to T_g . It was also demonstrated for Ni–Nb–Ta [46] and other [47,48] liquid alloys.

Structural changes, thermal expansion and volume changes (structural relaxation) in Zr-based metallic glasses upon heating [49,50] and cooling [51] were studied by synchrotron X-ray radiation

diffraction and transmission electron microscopy [52,53]. Recently it was shown that even scanning tunneling microscopy allows achieving atomic scale resolution for metallic glasses [54].

Zr-Cu(Ni)-Al alloys are among the most studied bulk metallic glasses [55]. A detailed study on vitrification of a ternary $\text{Zr}_{60}\text{Cu}_{30}\text{Al}_{10}$ alloy was performed recently in-situ by high energy synchrotron radiation X-ray diffraction from above the liquidus T_l to room temperature [56]. Short (SRO) and medium range order (MRO) develop significantly during cooling the liquid phase to the glassy state. Significant glassy structure and volume changes are found during severe plastic deformation [57] and rolling [58]. Structural changes in Cu-Zr [59,60] and Cu-Zr-Al glasses [61] were also studied by MD computer simulation.

Here we study the atomic structure changes in a relatively *strong* $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ glass-forming liquid (one of the best glass-formers [62]) on vitrification and compare the results with those obtained for *fragile* metallic glasses. Its measured fragility parameter m for this liquid varies from about 45 [63,64] to 29 [65] but it is lower than that obtained for the Pd-Cu-Ni-P one studied earlier.

2. Experimental Procedure

An ingot of the $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ alloy (the composition is given in nominal atomic percentage) was prepared from pure metals of more than 99.9 mass% purity using the arc-melting method. Thermal stability of the samples was tested using a differential scanning calorimeter (DSC).

In-situ X-ray diffraction experiments were carried out at the European Synchrotron Radiation Facility (ESRF). The incident beam wavelength was 0.1245 Å (100 keV). Diffraction spectra were acquired in transmission mode by a 2D detector. An aerodynamic levitation setup [66] was used to heat up, melt and cool down the metallic glass spheres in situ under synchrotron radiation. Prior to experiments, the levitation chamber was first evacuated down to 10^{-5} mbar and then filled with the levitation gas. The spheres were levitating by high purity argon (containing less than 0.01 mass ppm O₂) flowing through an aluminum nozzle and melted using two CO₂ laser beams. Two pyrometers were used to record the temperature while temperature values below 620 K were calculated. Diffraction intensities were recorded during cooling with a time resolution of 100 ms. The radial

intensities were integrated over 90 degrees (1/4 of the entire halo) to obtain one-dimensional spectrum and enhance the signal to noise ratio. The accuracy of the temperature values is estimated at ± 10 K for the data above 900 K and better than ± 7 K below 900 K.

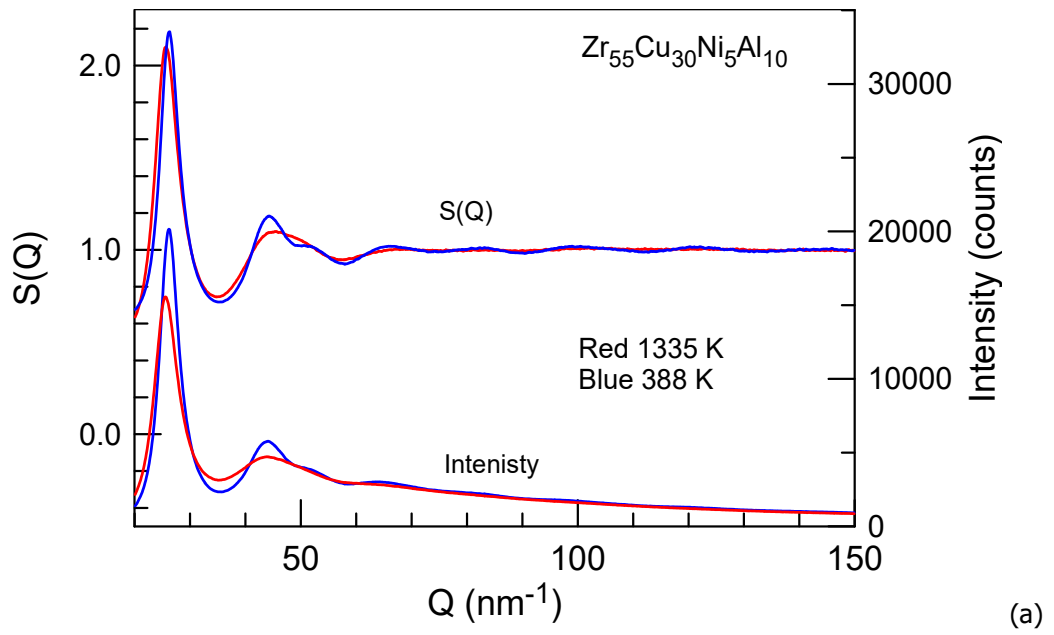
After necessary corrections the measured intensity was converted to electron units per atom with the generalized Krogh-Moe-Norman method [67]. The density value of 6800 kg/m^3 for the alloy was obtained from Ref. [68]. The total structure factor $S(Q)$ and the interference function $Qi(Q)$ ($Q = 4\pi \sin\theta/\lambda$, θ is the diffraction angle) were obtained from the coherent scattering intensity by using atomic scattering factors. The radial distribution $RDF(R)$ and pair distribution functions $PDF(R)$ and $G(R)$ were obtained by the Fourier transform of $Qi(Q)$ [67]. The maximum scattering vector (Q) value obtained was 250 nm^{-1} . However, as the noise level at high Q values was rather high the Fourier Transform was performed only until 150 nm^{-1} . Termination of the Fourier Transform at higher Q_{max} values was found to increase the noise of $G(r)$ without any positive effect on the curves.

The atomic structure of the $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ alloy in both liquid and glassy states was also modeled using the first-principles molecular dynamics simulation. The calculations were performed using density functional theory based pseudopotential plane-wave method as implemented in VASP code [69]. The atomic configuration was modeled within a cubic supercell consisting of 500 atoms. The spin polarized generalized gradient corrected Perdew-Burke-Ernzerhof exchange-correlation functional [70] and the projector augmented wave method [71] were used in order to accurately describe the interaction between the ion and electron. The Brillouin zone integrations were carried out using the Γ -point. At the first step, the random atomic structure was melted at 2000 K for a total of 10 ps. After that, the obtained system in liquid state was additionally equilibrated for 10 ps at 1400 K and 1000 K. The additional volume relaxations were performed for these structures using stress tensor calculation. In order to obtain the structures at lower temperatures owing to slower relaxation the cell obtained at 1000 K was cooled down to 800 K and then to 500 K with a cooling rate of $2 \times 10^{14} \text{ K/s}$. The volume optimization was done for structures at 800 K and 500 K. After cell optimizations, all structures were equilibrated again for 2.5 ps at the same temperatures, respectively. The calculation of

electron density of states were performed using enlarged Brillouin zone of $6 \times 6 \times 6$ in order to get denser electron coverage.

3. Results and discussion

The alloy sample was heated up, melted and then cooled down at about 85 K/s (average cooling rate) from 1335 K ($T_l \sim 1150$ K) to 388 K and the alloy vitrified [72]. The measured intensity and the structure factor profiles obtained at two temperatures are shown in Fig. 1a. The glass-transition temperature measured by DSC at the heating rate of 0.67 K/s was about 680 K. This value is close to those found in the earlier works [68,73].



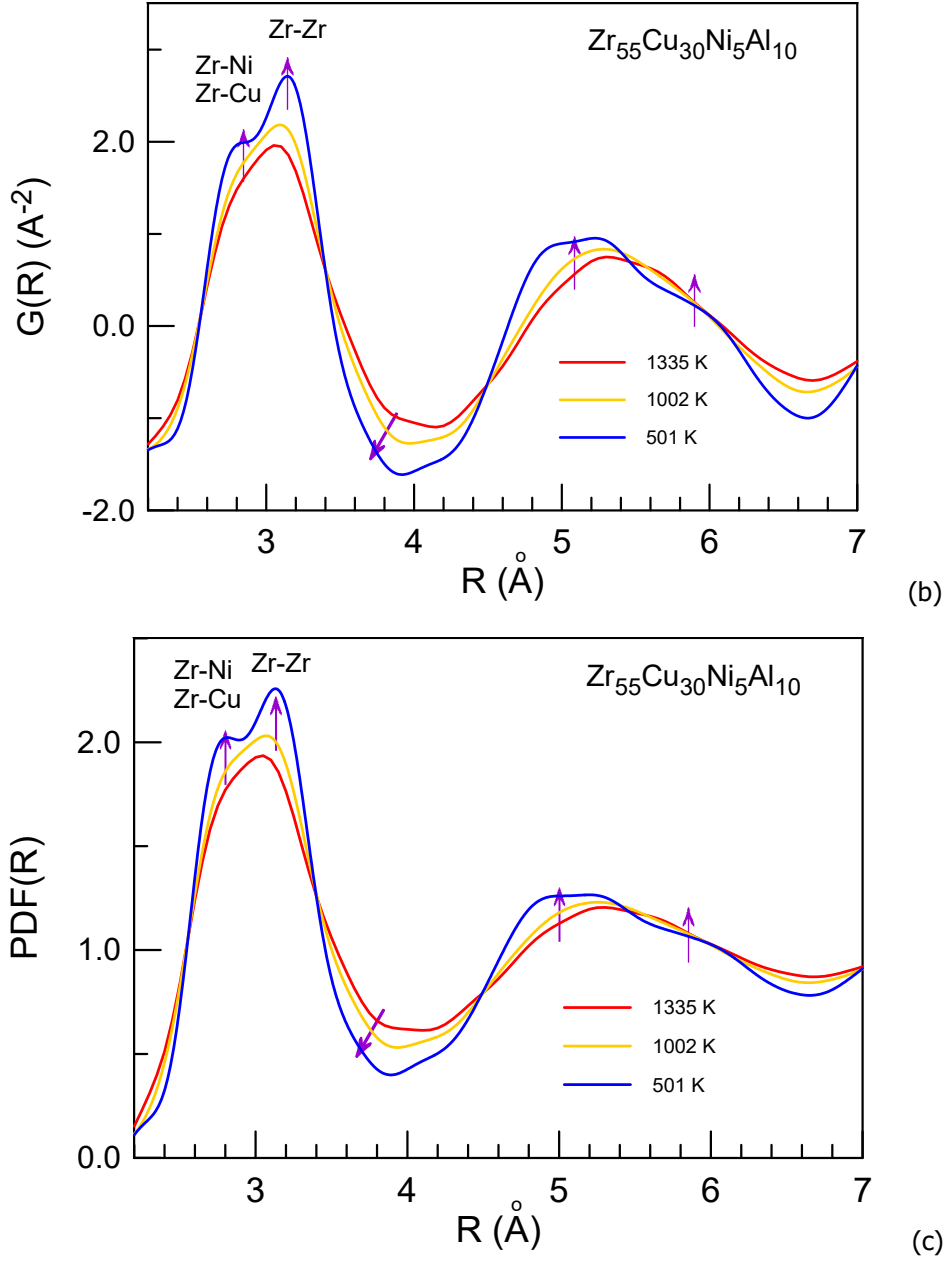
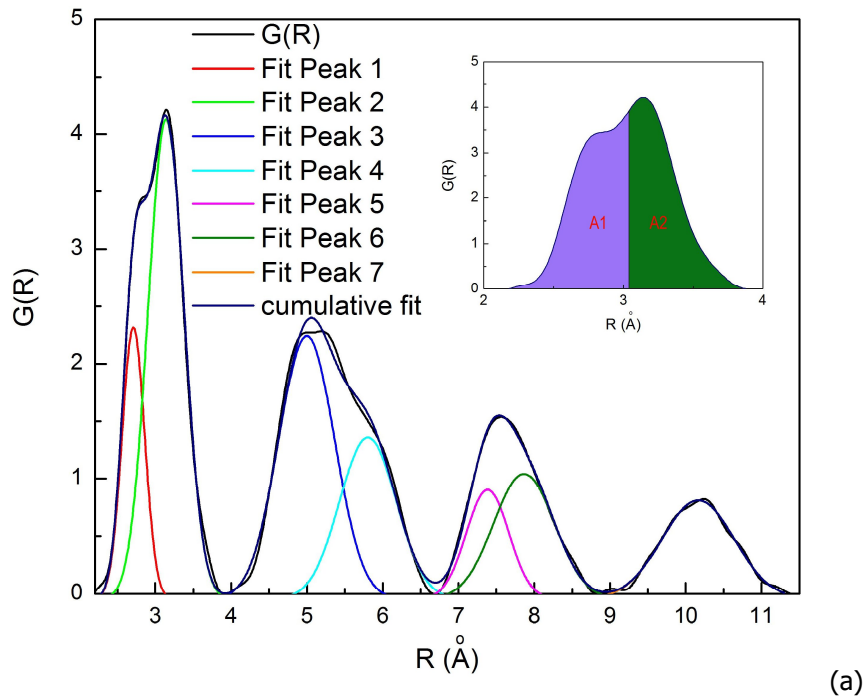


Fig. 1. (a) The experimental structure factor $S(Q)$ at 1335 and 388 K calculated from the corresponding XRD intensity profile after the necessary corrections. (b) three typical $G(R)$ functions and (c) three typical $PDF(R)$ functions. Violet arrows (upward) show intensification of two sub-peaks responsible for Zr-(Cu,Ni) and Zr-Zr atomic interactions in the first coordination shell and two sub-peaks at 0.5 and 0.58 nm in the second coordination shell. The arrow focusing downward-left indicates a decrease in the number of high R value interatomic distance on cooling.

Three typical $G(R)$ graphs are shown in Fig. 1b. Pair distribution function profiles ($PDF(R)$) calculated using the following equation:

$$PDF(R) = G(R) / (4\pi\rho_0 R) + 1, \quad (5)$$

where ρ_0 is the atomic number density, are also shown in Fig. 1c. In order to separate influence of different atomic pairs the $G(R)$ peaks were fitted with the several Gaussian functions. Fitting of four $G(R)$ maxima (the baseline was corrected to make both outermost points of each coordination shell maximum be equal to zero) using 7 Gaussian peak functions produced a reasonable correspondence with the original $G(R)$ plot (Fig. 2a). The temperature dependence of the center of mass positions of 5th and 6th peaks (3th coordination shell) indicates linear thermal contraction on cooling with a linear thermal expansion coefficient (α) of $2.8 \cdot 10^{-5} \text{ K}^{-1}$ in the liquid and of $1.1 \cdot 10^{-5} \text{ K}^{-1}$ in the glassy state (Fig. 2b). These values are quite close to those obtained by density measurements [68].



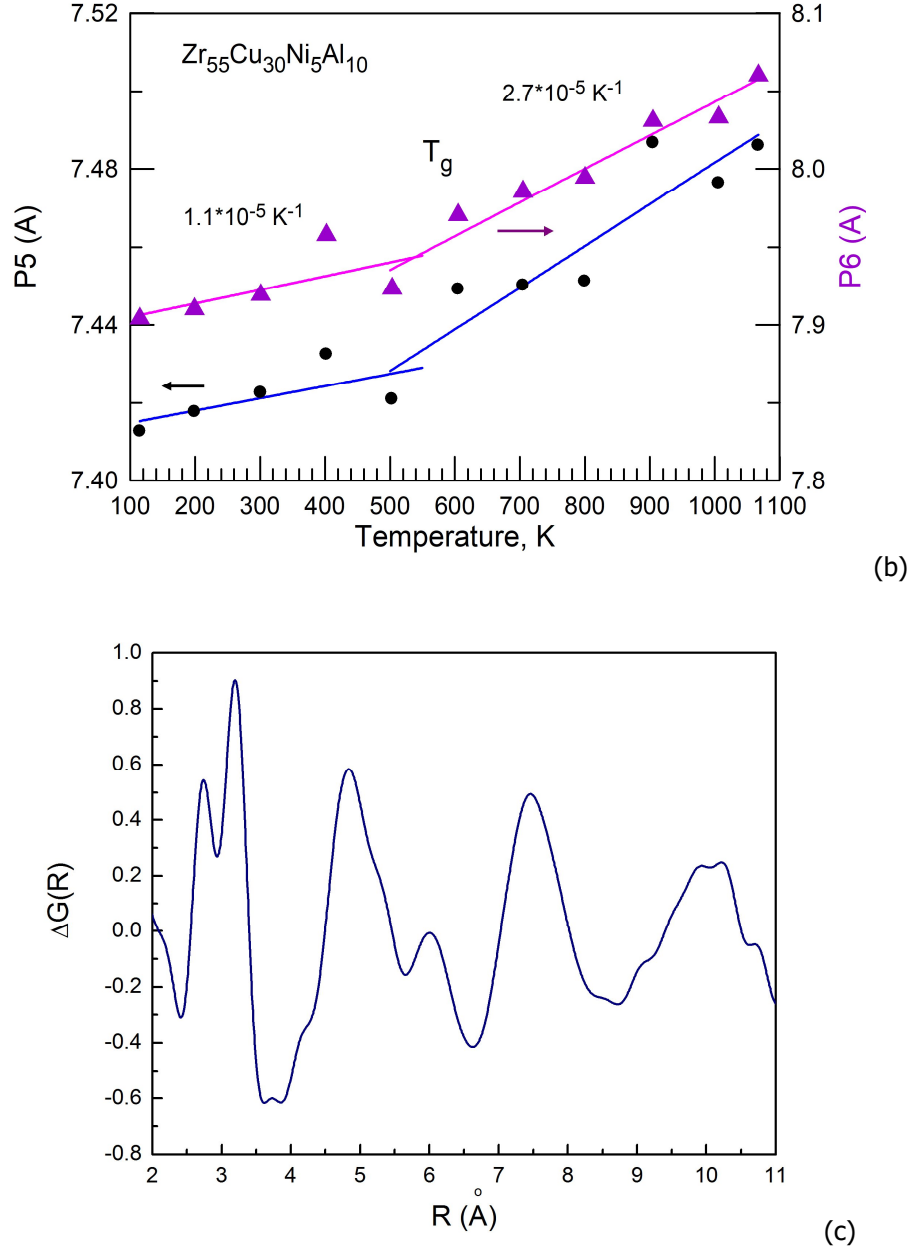
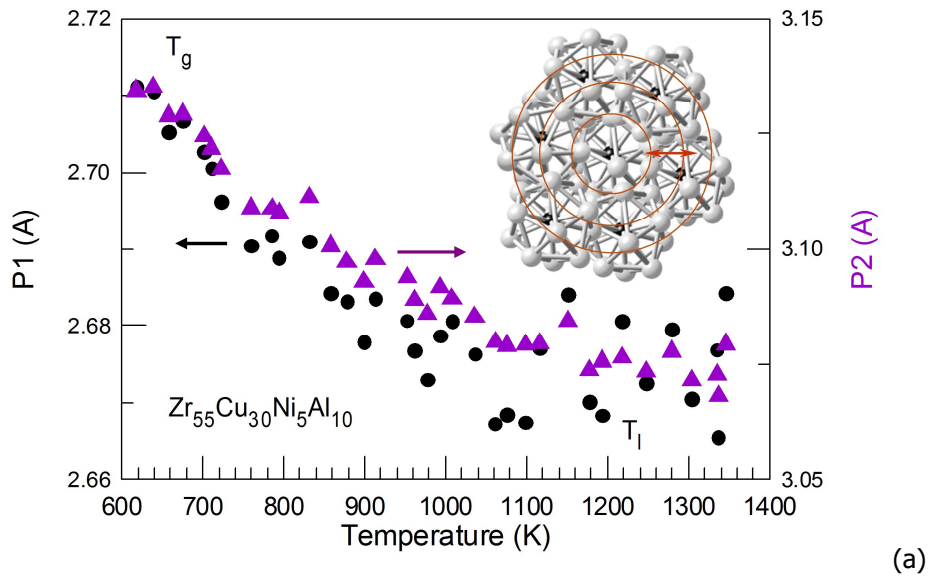


Fig. 2. Fitting of four $G(R)$ maxima (black curve) from 0.23 to 1.15 nm obtained at 501 K using seven Gaussian functions related to P1 – P7 (as indicated) (a). The baseline was subtracted prior to fitting according to the minima at about 2.2, 4, 6.7, 9 and 11.5 Å. The inset shows R_{50}^j value at which two areas A1 and A2 (purple and green) are equal. The positions of P5 and P6 as a function of temperature (b). The intensity difference between the $G(R)$ curves at 501 and 1335 K before the baseline correction (c).

As one can see the first and second $G(R)$ maxima clearly split in two sub-peaks (P1 and P2), especially at a low temperature. It is quite common for metallic glasses. A sub-peak at low R (P1) of about 0.271 nm is clearly visible on the first $G(R)$ nearest neighbor (NN) peak. The intensity difference between two $G(R)$ functions (Fig. 2c) indicates intensification of the sub-peaks at 0.272, 0.318 and 0.482 nm, etc... on cooling.

Opposite to the peaks related to other coordination shells (3^{rd} , 4^{th} , etc...) P1 and P2 of the first coordination shell shift to higher values on undercooling (Fig. 3a,b) as was found earlier for the Pd-Cu-Ni-P [74,75], Pd-Si [76], Cu-Zr [77], Zr-Cu-Ni-Al [78], Fe-B [79], many other alloys [80] as well as for pure metals [81]. On cooling the present Zr-Cu-Ni-Al liquid alloy exhibits contraction in 3^{rd} (P5 and P6) and 4^{th} (P7) coordination shells (Fig. 2b). The peak position in the 2^{nd} coordination shell, in general, did not change with temperature. Although P3 and P4 move in opposite directions (Fig. 3c) the average center of mass value of P3 and P4 is about 0.54 nm in the entire temperature range.



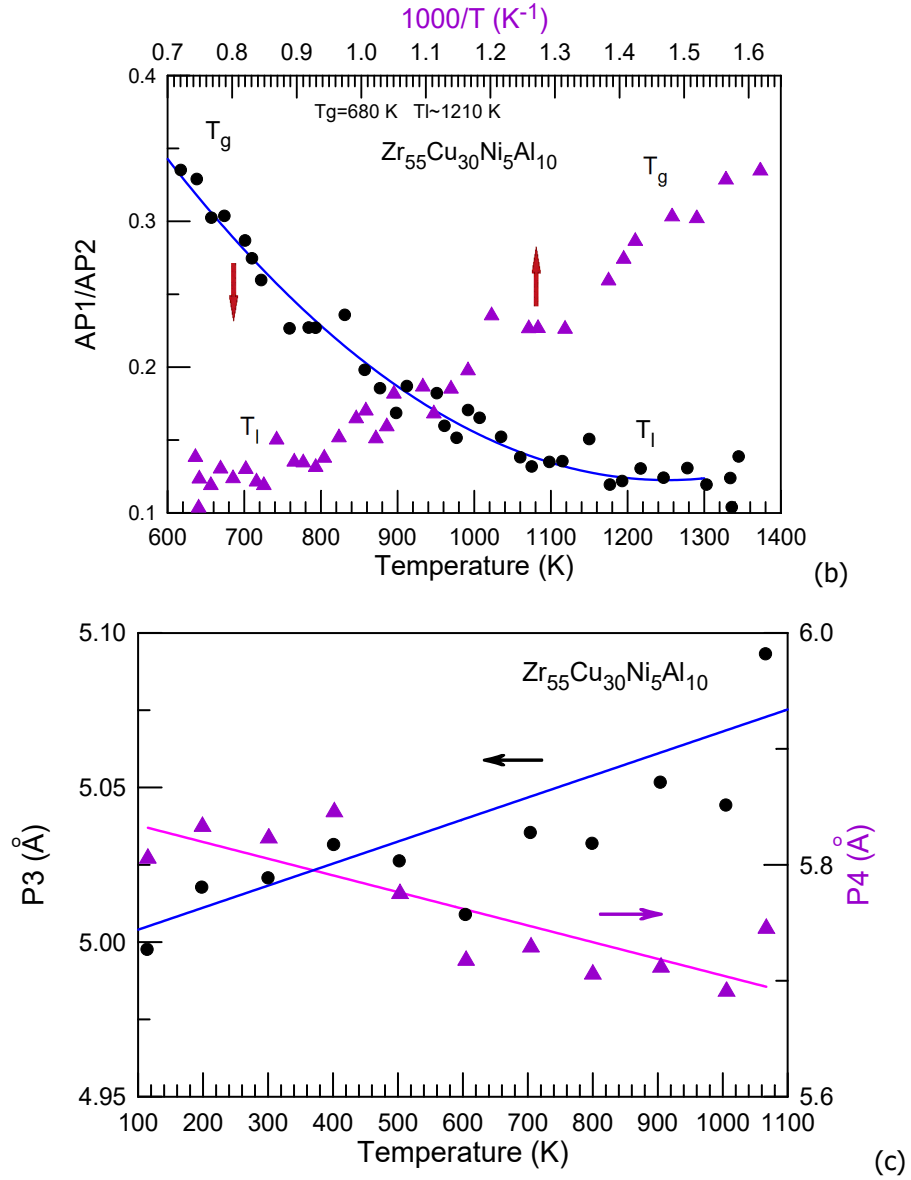


Fig. 3. Positions of P1 and P2 in the first coordination shell (a) and the ratio of the corresponding peak areas ($AP1/AP2$) (b) as a function of temperature (a,b) and inverse temperature in (b). The positions of P3 and P4 as a function of temperature (c). The arrows in (a and c) indicate Y-axes corresponding to the data while the arrows in (b) indicate the corresponding X-axes. The insert in (a) is schematic representation of atomic redistribution within and between the first and higher order coordination shells leading to continuous structure changes in metallic liquids on heating and cooling leading to redistribution of the atomic number density as indicated by the red double side arrow.

As it has been already mentioned before, seven Gaussian function peaks represent very well the entire shape of $G(R)$ (Fig. 2a). However, in the earlier works it was shown that owing to a complex asymmetrical shape of the first peak the maximum of $G(R)$ does not necessarily characterize all interatomic distances and the entire shape of the first peak should be taken into consideration [82,83]. As one can see in Fig. 1b, in addition to intensification of 4 sub-peaks marked with arrows, there is a decrease in the fraction of high R value atomic pairs in the first coordination shell (from 0.35 to 0.4 nm, see downward-left arrow) on cooling which is missed when the baseline is corrected. Nevertheless the Gaussian fitting peaks positions represent the most probable interatomic distances. Also, although the positions of the maxima in the first coordination shell are strongly influenced by the asymmetry of the interatomic potentials (steeper slope at lower R) no shift is observed in the average atomic position $((P3+P4)/2)$ in the 2nd coordination shell which is less affected by the potential.

Also, the area under the first maximum (see Fig. 2a) after the baseline correction was integrated and the point corresponding to 50 % of the integrated area (R'_{50}) (the areas of under the curve below (A1) and above this value (A2) are equal as shown in Fig. 2a,inset) was found in a wide temperature range below the liquidus temperature. As a result on cooling the R'_{50} position changes insignificantly from 0.303 to 0.304 nm. The change in R'_{50} is smaller than those obtained by the Gaussian fitting (Fig. 3a) but the tendency is same – larger R'_{50} values are found at lower temperatures. On the other hand integration of the total area under P1 and P2 in the first coordination shell of the radial distribution function (RDF) at 501 K indicates the coordination number (CN) of 13.3, a local RDF maximum (RDF_m) at 0.317 nm and $R'_{50}=0.312$ nm, while at 1335 K $CN=13.0$, $RDF_m = 0.313$ nm and $R'_{50}=0.315$ nm. Opposite variation in RDF_m and R'_{50} also indicate structural modification in the liquid phase on cooling.

Owing to chemical and size similarity between Cu and Ni this quaternary alloy can be considered as a pseudo ternary Zr-(Cu,Ni)-Al one. Then, there are 6 atomic pairs in the studied alloy with distinct interatomic distances. The interatomic distances in the first coordination shell correspond to the sums of the Goldschmidt atomic radii of $r_{Zr}=0.160$ nm, $r_{Cu}=0.128$ nm, $r_{Ni}=0.125$ nm and $r_{Al}=0.143$ nm [84]. The first sub-peak (P1) in the first coordination shell corresponds to the nearest Zr-

(Cu,Ni) distances ($r_{\text{Zr+Cu}}=0.288$ nm) while the second sub-peak (P2) mostly corresponds to that of Zr-Zr pair ($r_{\text{Zr+Zr}}=0.320$ nm) (Figs. 2a and 3a). The experimental peak position values are slightly lower than those predicted by the sum of the Goldschmidt atomic radii owing to formation of chemical bonds. Zr-Al interatomic distances are also closer to the value for the second peak and modify its position.

These findings imply the possible structural changes and atomic redistributions within and between the coordination shells as schematically shown in the inset of Fig. 3a. Several clusters are located around the central one. The atoms which are considered as the solute-centering are black while surrounding atoms are white. Red circles schematically illustrate the first, second and third atomic coordination shells. Red arrow indicates permanent atomic number density redistribution between the corresponding shells on cooling. One should keep in mind that such a planar representation of the atomic structure is oversimplification and can be redrawn by using any other atom as the central one because any atom in the structure is a center of its own atomic cluster with a unique atomic arrangement, interatomic distances and a certain number of nearest neighbors. $G(R)$ indicates statistically average atomic structure where maxima correspond to the most popular interatomic distances. Nevertheless this picture gives a visual representation of the structural processes occurring in a metallic fluid on cooling.

On subsequent heating of the glassy sample vitrified on cooling, the change of slope of temperature dependence of the first and second peaks (P1 and P2) takes place at about 500 K (see supplementary data, please) indicating densification of the glassy phase. This temperature corresponds well to the temperature of beginning of structural relaxation of the glassy phase on heating.

As in case of the Pd-Cu-Ni-P alloy studied earlier [45] $AP1/AP2$ (the area under P1 divided by the area under P2) ratio is nearly constant in the equilibrium liquid state. However, it changes on cooling in the supercooled liquid state (Fig. 3a). It indicates that the number of Zr-Cu and Zr-Ni atomic pairs increases on cooling below T_l owing to chemical ordering.

It is important to note that the changes in $AP1/AP2$ ratio (APR) for the $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ liquid alloy from T_l to T_g (the ratio in Fig. 3 is $0.30/0.12=2.5$) are smaller in the absolute values compared to

those found in the $\text{Pd}_{40}\text{Cu}_{30}\text{Ni}_{10}\text{P}_{20}$ liquid alloy ($0.09/0.02=4.5$) [45]. The $AP1/AP2$ ratio values normalized per Kelvin (APR^n) according to the supercooled liquid region on cooling ($T_l - T_g$) are 0.005 ($APR^n=2.5/530 \text{ K}^{-1}$) and 0.017 ($APR^n=4.5/270 \text{ K}^{-1}$), respectively. This fact is in line with a lower fragility of the $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ melt compared to that of the $\text{Pd}_{40}\text{Cu}_{30}\text{Ni}_{10}\text{P}_{20}$ one. Continuous structural changes in the supercooled liquid leading to the formation of atomic clusters likely change the activation energy for viscous flow, and thus, determine fragility of this glass-forming liquid through the equations (1 and 4).

Fragility of liquids also correlates with the difference in the specific heat capacity (C_p) at T_g between the liquid and glassy phases [85]. The $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ has C_p values for liquid (C_p^l) and glassy (C_p^g) phases at T_g of about 38 and 28 J/mol·K, respectively, [86] while these values for the $\text{Pd}_{42.5}\text{Cu}_{30}\text{Ni}_{7.5}\text{P}_{20}$ alloy are 45 and 28 J/mol·K, respectively [87]. Thus, ΔC_p^{l-g} values of 10 and 17 J/mol·K for $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ and $\text{Pd}_{42.5}\text{Cu}_{30}\text{Ni}_{7.5}\text{P}_{20}$ alloys, respectively, also correlate with a larger fragility of the latter alloy. As melting enthalpy of $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ is close to 7.5 kJ/mol and the liquidus temperature is about 1150 K [72,73], its melting entropy (ΔS_m) is about 6.5 J/K·mol. The resulted thermodynamic fragility m_t parameter calculated using the formula:

$$m_t = 37.5 \cdot \Delta C_p / \Delta S_m \quad (5)$$

[85] is 58. For an alloy close in composition to the $\text{Pd}_{42.5}\text{Cu}_{30}\text{Ni}_{7.5}\text{P}_{20}$ one melting enthalpy is close to 5 kJ/mol [88] which gives ΔS_m of 6.1 J/K·mol. The resulted m parameter is 104. If one uses ΔS_m of 8.03 J/K·mol [89] then $m=79$ which is still higher than $m=58$ found for the $\text{Zr}_{55}\text{Cu}_{30}\text{Ni}_5\text{Al}_{10}$ alloy.

$PDF(R)$ curves produced by MD simulation are shown in Fig. 4. Here the split of the peaks corresponding to first and second coordination shells is less visible owing to insufficient structure relaxation.

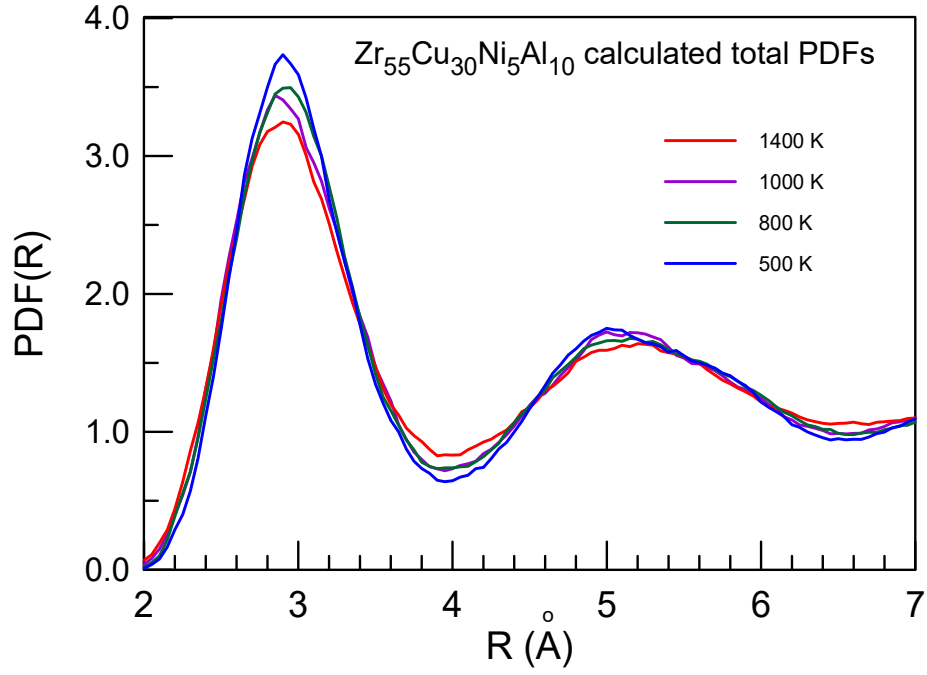


Fig. 4. $G(R)$ calculated by using ab-initio MD simulation. The curves were smoothed over 10 points.

The partial $PDF(R)$ functions shown in Fig. 5 indicate intensification of the Zr-Cu subpeak on cooling. The peak positions also correspond well to those obtained experimentally in Figs. 2a and 3a. On cooling there is a change in partial pair distribution functions position fitted by the Gaussian function, background subtracted. The results for two major atomic contributions are shown in Table 1. One can see the shift of Zr-Cu and Zr-Zr peaks to a higher R value on cooling. Intensification of both Zr-Zr and Zr-Cu peaks (area) is also observed.

Table 1. Position and area of two Zr-Zr and Zr-Cu peaks at two temperatures.

Temperature, K	Zr-Zr		Zr-Cu	
	R, nm	Area	R, nm	Area
1400 K	0.3185	0.788	0.2850	1.022
500 K	0.3225	0.850	0.2860	1.094

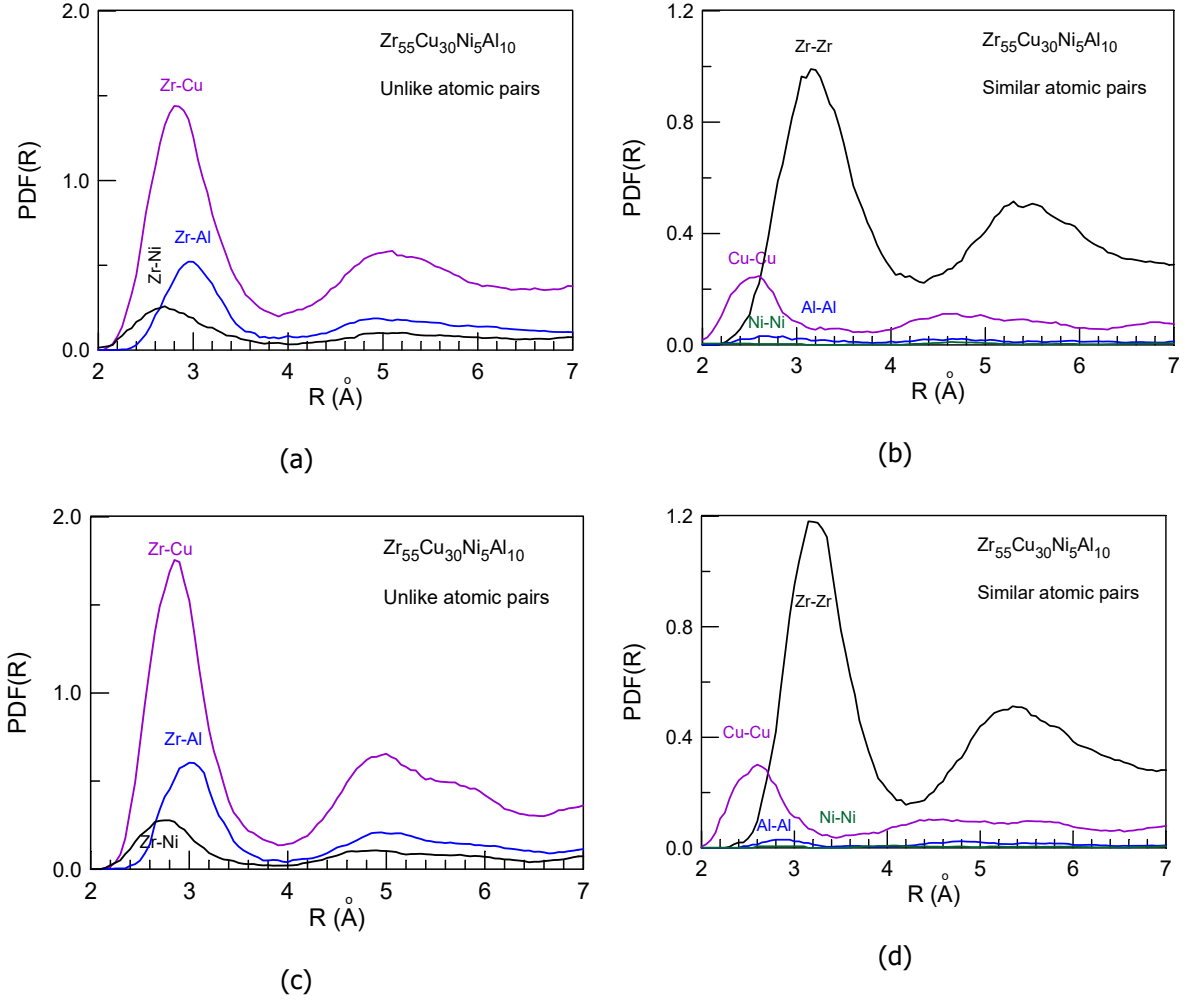
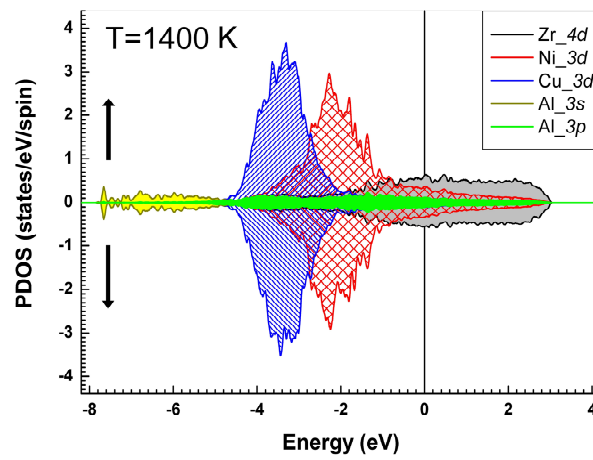


Fig. 5. Partial $PDF(R)$ functions obtained by computer simulation at 1400 K (liquid state) (a,b) and 500 K (glass state) (c,d).

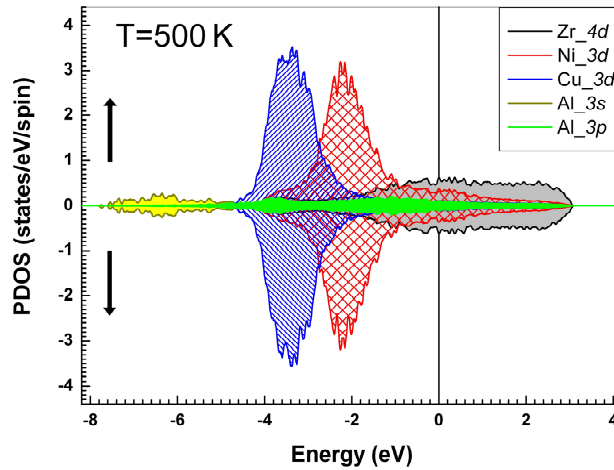
Moreover, as shown in Fig. 6, the calculated partial densities of states (PDOS) (corresponding to the 3s, 3p, 3d and 4d states of Al, Ni, Cu and Zr atoms), respectively, indicate some changes in the electronic structure towards a short range order formation in the glass. The redistribution of peak intensities for Ni and Cu is found on cooling. Broader peak distributions of electron density below the Fermi level corresponding to Cu and Ni atoms are observed in the liquid state. It is interesting that the most significant changes are found in the peak shape of Ni in the energy region from -3.0 to -1.0 eV. During the cooling process, the redistribution of peak intensities for Ni atoms occurred by shifting the

electron density to a narrower region between -3.0 and -2.0 eV. It indicates the formation of stronger bonds with Ni atoms.

The *s* and *p* electron orbitals of Al overlap with those of all other elements thus stabilizing the glassy structure. This fact may be related to a higher glass forming ability of ternary Zr-Cu-Al metallic alloys compared to binary Zr-Cu alloys. For example, PDOS of Zr and Cu are much less overlapped.



(a)



(b)

Fig. 6. PDOS for the spin-up (\uparrow) and spin-down (\downarrow) as shown, at $T=1400$ K (a) and at $T=500$ K (b) respectively. The Fermi level (vertical line) has been chosen as zero energy.

The Voronoi polyhedral analysis was also applied to the cells. However, owing to small cell sizes no systematic variation in coordination numbers of the polyhedral clusters is found with temperature except for Ni with $CN=12$. The number of Ni-centered clusters with $CN=12$ increased from 5 to 10 and to 12 on cooling from 1400 to 500 K. This is in line with intensification of the Ni PDOS peak in Fig. 6 indicating formation of Ni-centered clusters.

4. Conclusion

According to the results, strong chemical ordering forming Zr-Cu,Ni, Zr-Al and Zr-Zr atomic pairs takes place in the $Zr_{55}Cu_{30}Ni_5Al_{10}$ supercooled liquid alloy on cooling below the liquidus temperature. However, here the change in the Zr-Cu,Ni peak area to other peaks area ratio (APR and APRⁿ) is smaller than in case of the Pd-Cu-Ni-P alloy studied earlier (Cu,Ni-P to other peaks) in accordance with a lower fragility index of the $Zr_{55}Cu_{30}Ni_5Al_{10}$ melt. It is concluded that fragility is a sign of instability of short and medium range order in fragile liquids. MD simulation was found to support the observed structure variation as a function of temperature and indicated intensification of Zr-Cu, Zr-Al and Zr-Zr interactions on cooling.

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