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# An efficient end to end verifiable voting system

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**RÉSUMÉ.** Les systèmes de vote électronique sont devenus une technologie puissante pour améliorer la démocratie en réduisant le coût des élections, en augmentant la participation des électeurs et en permettant même aux électeurs de vérifier directement l'ensemble de la procédure électorale. Cependant, la vérification de bout en bout (E2E) a été largement identifiée comme une propriété critique pour l'adoption de tels systèmes de vote en réel pour des procédures électorales. Par ailleurs, l'un des piliers de tout scrutin, outre le secret du vote et l'intégrité du résultat, réside dans la transparence du processus, la possibilité pour les électeurs "de comprendre le système sous-jacent" sans avoir recours aux compétences techniques. Les systèmes de vote électronique vérifiables de bout en bout proposés dans la littérature ne le garantissent pas toujours car ils nécessitent des hypothèses de configuration supplémentaires par exemple l'existence d'un tiers de confiance comme source de hasard, l'existence d'une balise aléatoire. Ainsi, construire un système de vote vérifiable de bout en bout fiable offrant la confidentialité et l'intégrité reste un problème de recherche ouvert. Dans ce travail, nous présentons un nouveau système de vote électronique vérifiable de bout en bout nécessitant uniquement l'existence d'un babillard de vote cohérent, tolérant aux pannes, qui stocke toutes les informations relatives aux élections et permet à tout parti ainsi qu'aux électeurs de lire et vérifier le processus d'élection complet. La propriété de vérification de bout en bout de notre système est une information garantie compte tenu de l'existence du babillard, de l'implication des électeurs et des partis politique dans le processus. Cette implication ne compromet ni la confidentialité ni l'intégrité des élections et ne nécessite pas d'opérations cryptographiques pour le compte de l'électeur.

**ABSTRACT.** Electronic voting systems have become a powerful technology for the improvement of democracy by reducing the cost of elections, increasing voter turn-out and even allowing voters to directly check the entire electoral process. End-to-end (E2E) verifiability has been widely identified as a critical property for the adoption of such voting systems for electoral procedures. Moreover, one of the pillars of any vote, apart from the secret of the vote and the integrity of the result, lies in the transparency of the process, the possibility for the voters "to understand the underlying system" without resorting to the competences techniques. The end-to-end verifiable electronic voting systems proposed in the literature do not always guarantee it because they require additional configuration hypotheses, for example the existence of a trusted third party as a random source or the existence of a random beacon. Hence, building a reliable verifiable end-to-end voting system offering confidentiality and integrity remains an open research problem. In this work, we are presenting a new verifiable end-to-end electronic voting system requiring only the existence of a coherent voting board, fault-tolerant, which stores all election-related information and allows any party as well as voters to read and verify the entire election process. The property of our system is information guaranteed given the existence of the bulletin board, the involvement of the voters and the political parties in the process. This involvement does not compromise the confidentiality nor integrity of the elections and does not require cryptographic operations on the voters account.

**MOTS-CLÉS** : Vote électronique, Vérification de bout en bout, Confidentialité, Intégrité, Fonction de hachage

**KEYWORDS** : Electronic voting, End-to-End verifiability, Confidentiality, Integrity, Hash Function

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## 1. Introduction

In an end-to-end verifiable electronic system (E2E), voters have the ability to verify that their vote has been properly emitted, recorded and counted in the election result. Intuitively, the security property this system must provide is the ability of voters to detect fraud in the electoral process.

End-to-end verification requires the voter to be able to obtain a receipt at the end of the vote that will allow him to verify that his vote has been cast as expected, recorded as such and counted in the results. In addition, any external third party should be able to verify that the election procedure has been carried out correctly. Indeed, it is imperative that receipts from an end-to-end verifiable system be delegable, that is, that the voter can outsource the verification task to any interested third party, for example an independent, confident organization that performs a global check. This requirement, as well as the fact that it would be impossible for the voter to use his receipt as evidence of how he voted (to avoid buying votes) make the design of verifiable end to end a difficult problem.

The well-known e-voting systems that offers end-to-end verifiability generally ensure this only under certain configuration assumptions, such as the existence of a trusted third party for key generation and as a source of chance, a model or machine for generating random values. Indeed a limitation to the use of certain hypotheses to ensure end-to-end verifiability is the fact that one must have faith in that and therefore to the result of the elections. This causes a problem because it is not easy for electoral authorities to unequivocally convince voters that the election is correct. In addition, the ability of voters to easily understand the different components of the system gives rise to controversies. And so the results of the election can be the subject of several contestations.

Motivated by the foregoing, we are designing a new verifiable end-to-end electronic voting system that only requires the existence of a consistent voting bulletin board that provides a comprehensive and coherent view of the election. In addition, the proposed system does not require any cryptographic knowledge on the voter's side. End-to-end verification can be achieved through the use of transparent procedures, the voting bulletin board and the involvement of the different political parties concerned by the election.

In the rest of this work, section 2 presents a state of art of the verifiable end-to-end systems. Section 3 highlights the new end-to-end verifiable voting system. An evaluation of this system is proposed in section 4. Section 5 concludes our work and presents the prospects for improvement.

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## 2. Related work

The confidentiality, integrity and verifiability of elections are the main research objectives in the field of electronic voting, which has been in existence for some decades. The voting protocols resulting from this work are classified into three broad categories according to the technique used : mix-nets [1, 2], blind signatures [3, 4] and homomorphic voting systems [1, 5]. All of these protocols are based on heavy cryptographic components and require cryptographic skills for voters and political parties. As a result, in 2004, Chaum [6] and Neff [7] identified that the verifiability offered by voting systems relies too much on cryptography to be of practical use to voters. From these works emerges a new paradigm of research in electronic voting : E2E voting systems. The goal of end-to-end verifiable systems is to provide the opportunity for any voter to easily check his or her

vote and that all the results are verifiable universally. The system proposed by Chaum [6] was the base of many end-to-end verifiable systems such as : (Prêt à Voter [8], Punchscan [9], Scantegrity [10], Aperio [11], Eperio [12]). These systems are exposed to many problems : complexity, confidentiality, and usability. The verifiability is still argued but not assured.

Helios [13] was the first used verifiable end-to-end voting system. It targets the low risk elections by implementing existing ideas into a system. Helios uses a simplified version of the Benaloh challenge [14](considered acceptable for a low risk coercion environment) to achieve verifiability. However, it is exposed to several attacks related to privacy due to the malleability of the cryptographic scheme used [15]. As a result, other systems have emerged to truly achieve end-to-end verifiability.

This is the case for the Remoteegrity [16], based on a lock code that is provided to the voter on a scratchable surface to allow him to check his vote and detect unauthorized modification to their ballots made either by client software, either by an electoral authority. But, the software can be malicious and the corrupt authority. In addition, Remoteegrity is designed for a specific municipal election : Takoma Park, Maryland responds to a certain number of requirements and is an extension of the existing Scantegrity system [10], which constrains its conception. We realise that, the number of codes an elector must enter during the voting process is high. This number could be revised downward. For example, the serial numbers of the ballot and the authorization card can be harmonized to the same value.

At the same time, EVIV [17] has been developed with the objective of offering complete mobility to the voter and ensuring end-to-end verifiability while preserving confidentiality. In other to solve the problem of malicious software and authority, EVIV combines the voting code to the encryption technique MarkPledge. For the verification, the voter must match alphanumeric strings that detect and protect against voting manipulations on both the unstable voting client platform and the election server. In EVIV, each elector has a Voter Security Token (VST), which is responsible for encrypting the vote and to which the voter communicates his selection of candidates. With the help of VST, each elector generates the voting codes at home, which facilitates the logistics of the election and allows a complete voting process online and on mobile. However, the limited computing capabilities of VST limit the use of EVIV in elections with a small number of candidates. EVIV nonetheless requires the integration of coercion resistance mechanisms and improved usability and verifiability mechanism.

Rabin and Rivest [18] proposes an end-to-end verifiable voting system based on the distribution of vote count and the creation of a verifiable proof of the exactitude of server combined with a random representation of the integers used in the system. At the end of the count, a random permutation of the different recorded votes is published without revealing the identity of the voters. However, the system requires mechanisms of resistance to constraints and turns out to be complex.

Kiayias et Al. [19] finds that all known e-voting systems that offer end-to-end verifiability can only achieve this under configuration assumptions such as the existence of a trusting party that provides random values or of a machine as a random source. In fact, this verifiability can be argued, but not formally proven. For this purpose, the authors propose a verifiable end-to-end system without hypothesis except for the existence of a bulletin board. However, the system is based on the ElGamal cryptosystem with the Decisional Diffie-Hellman (DDH) basic hypothesis, which is a difficult cryptographic problem ; its commitment regime is homomorphic and uses entropy that is generated by the interaction between voters and the system.

In sum, the end-to-end verifiable voting systems proposed to this day allow voters to effectively check their votes. But however they remain based on a set of assumptions and cryptographic components that are sometimes heavy. What remains a problem in the process of verifiability of the voting system, namely : the ability for the political parties and voters concerned by the election to understand the voting system that is proposed to them and to be involved. This condition is necessary to increase verifiability and further enhance the reliability of the system. Hence the purpose of the protocol we propose.

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### 3. End-to-end verifiability protocol

In this section, we present different actors involved in the electoral process and the different phases of the voting process ranging from the enrollment of voters to the publication of the results.

Throughout the process, we will use the following notations :

$I_1, \dots, I_{N_2}$  the set consisting of all the authentication information of the registered voters such that  $\text{card}(E) = \text{card}(I) = q$ ,

$N_1$  the number of individuals able to vote,

$N_2$  individuals actually registered

$I_j$  : set of information about an individual  $j$ ,

$R$  the set of random values provided by the electors

$v$  all lock codes

$V$  all votes cast

$Id_{Office}$  : all the identifiers of the polling stations

$B$  : all the ballot papers

$Y = Y_1, Y_{N_2}$  : the vote database

#### 3.1. The entities of the system

The system comprises the following different entities :

**Enrollment service** : entity responsible for registering voters on electoral rolls, drawing voter registration cards, candidate databases and voter lists. These spots are done before polling day.

**Election authentication** : handles voter authentication on Election Day. This service is the responsibility of the Central Authority for Legitimation (**CAL**).

**Voting booth** : electronic entity used to store certain voting data.

**CAA (Central Accounting Authority)** : entity in charge of the counting of the ballot papers, the counting of votes by candidate and the publication of the results. The counting of votes is done centrally.

**Bulletin Board** : entity responsible for the publication of the public data of the vote and the results of the ballot.

**Voting service** : it includes a software unit for voting, a ballot validation unit and a voting data transfer unit in random order at the CAA.

**Verification service** : it is a entity responsible for the verification and validation of data and voting results. **Voters**, **Political parties**, and **Independent verification organizations** can run each instance of this service.

The architecture of the system is therefore the following.

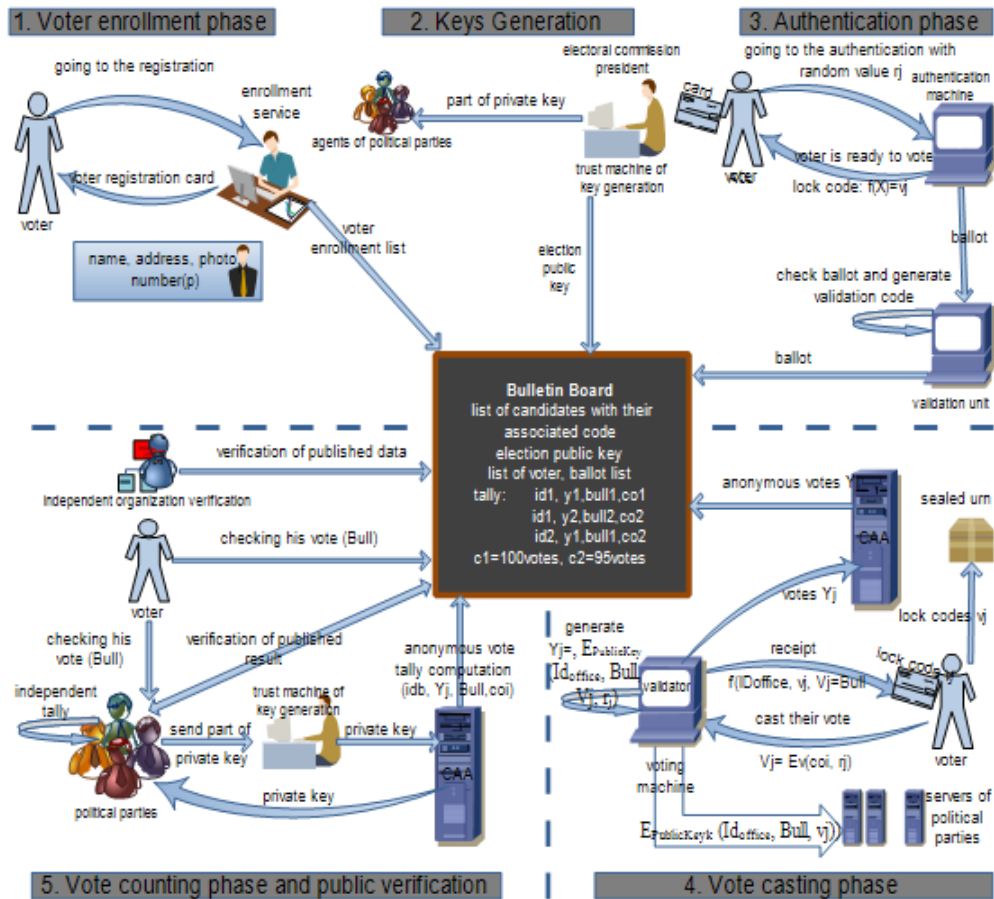


Figure 1. Architecture Example

### 3.2. Voter enrollment phase

Months before the poll, the organization responsible for managing the elections organizes the registration of voters on the electoral lists for a specific period. The entity in charge of registration (Enrolment service) is set up and any citizen of voting age can register. This phase is carried out through the following steps :

#### 3.2.1. Voter to Enrollment service

At this stage, the elector provides the registration service with all the information necessary for its identification with the aim of obtaining a voter’s card. For this purpose, he presents himself in a registration station equipped with a piece of civil status (national identity card or birth certificate) allowing identification. The following information, relating to the elector, is collected for the purpose of perfecting the electoral process : first and last names, date and place of birth, father’s name, mother’s name, CNI number. This information is unique for each voter, that is, there cannot be two individuals for whom all of this information is identical. Formally,

$$\forall j \in 1, \dots, N_2, I_j = i_j^1, i_j^2, \dots, i_j^k \text{ and } \forall l, j \in 1, \dots, N_2, \exists x \in 1, \dots, k, l \neq j, i_l^x \neq i_j^x$$

### 3.2.2. Enrollement service to Voter

The recording machine generates 4 disposable masks which will be used to encode the personal information of the voter that will be used for authentication before storage in the database. The choice of 4 masks is done in order to further reinforce the secrecy around the voter information and make the decoding task more difficult. After generating the masks, the information is coded with the masks as follows : Let be,

$n$  the number of bytes necessary to code all the information ( $I_j$ ) of a voter  $j$ ,  
 $I_{jy}$  is the part of the information  $I_j$  contained in the byte  $y$ , with  $0 \leq y \leq n - 1$ ,  $I_j = I_{j0}, \dots, I_{j(n-1)}$   
 $M_1, M_2, M_3, M_4$  the 4 generated masks, with  $M_q = m_q^0, m_q^1, \dots, m_q^{(n-1)}$ ,  $1 \leq q \leq 4$

We carry out an X-OR between  $I_j$  and  $M_1$  the result is carried out one X-OR with  $M_2$  and so on. The result obtained is  $I_j \oplus M_1 \oplus M_2 \oplus M_3 \oplus M_4$ .

Then, we perform permutations according to the permutation number chosen among the  $n!$  possibilities on the result  $I_j \oplus M_1 \oplus M_2 \oplus M_3 \oplus M_4$ . The number of the permutation is number (p).  $0 \leq y \leq n! - 1$ . In order to make the detection task of the disposable mask more complex, number  $p \geq 4$ . number (p) is associated with the elector's information and put on the elector's card. The masked information of the voter and the different masks are encrypted with the public key of the authentication machine (CAL).

At the end of the registration process, the enrollment service performs the redundancy check in order to eliminate duplicates. In the case of duplicates, that is to say that an elector has been registered twice, the most recent registration is retained.

### 3.3. Key generation

Throughout the process, several encryption / decryption keys are manipulated. The CAL and the ballot validation unit has each other a key pair to encrypt/decrypt the information from the record. Each political party  $k$  has a key pair ( $Publickey_k/Privatekey_k$ ) to encrypt/decrypt the voting data that will be transmitted to it. In order to achieve end-to-end verification, we involve the different political parties in the election process. Each party must have a function of the key (action) for decrypting the ballots and can perform the count independently. The election management organisation selects a brand and model of machines to use for keys generation. One month before the election, political parties and the media are invited to the key generation event. Each party sends an expert to attest the generation machines and an officer. Once the experts have certified the machines, the public key of the CAA is generated, signed and published. The corresponding private key is generated and then divided into pieces according to Shamir's secret-sharing technique as indicated by algorithm 1 below and according to the number of political parties involved in the election. Each party receives a function from the key. The threshold (k, n), k less than or equal to n which represents the number of political parties, is fixed for the reconstitution of the key. From k parts we can find the key.  $k = n$  implies that all parts are needed to find the key.

### 3.4. Authentication phase

Voter authentication on polling day is done by the CAL. The voter presents himself with his voter's card which he introduces into the authentication machine. The machine retrieves number (p) and calculates the inverse permutation to find the permutation performed on the hidden information. The CAL decrypts the registration information. Then



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**Algorithm 1** Generation & SharingKey

---

**Input:**  $c_1, c_2, \dots, c_n$ ;  $(k, n)$  the threshold chosen for sharing keys.

**Output:**  $p_1, p_2, \dots, p_n$

```
Pairkey  $\leftarrow$  generationPairkey ();
Publickey  $\leftarrow$  Pairkey.getPublickey ();
Privatekey  $\leftarrow$  Pairkey.getPrivatekey ();
// It takes k points to define a polynomial of degree k-1
Generate randomly k-1 coefficients  $r_1, r_2, \dots, r_{k-1}$ ;
Let  $r_0 = \text{Privatekey}$ ;
Build the polynomial  $f(x) = r_0 + r_1x + r_2x^2 + \dots + r_{k-1}x^{k-1}$ ;
for  $j \leftarrow 1$  to  $n$  do
    Build the share  $p_j = (x_j = j, y_j = f(j))$ , where  $p_j$  (a pair of antecedent and the
    corresponding image by the polynomial function) is the  $j^{\text{th}}$  part of the private key
    Privatekey;
    Give the share  $p_j$  to the agent of the  $j^{\text{th}}$  party.
end
```

Given a subset  $k$  of these pairs  $p_j$ , the polynomial interpolation makes it possible to find the coefficients of the polynomial whose constant term is the secret *Privatekey*; it verifies the voter's identity from the database and in case of compliance, a unique lock code is generated for the voter as proof that the authentication has succeeded. The voter information is unmasked once and gets  $X = I_j \oplus M_1 \oplus M_2 \oplus M_3$ .

Let  $f$  be the authentication function.  $f$  is a collision-resistant one-way hash function that provides for each voter its unique lock code,  $f(X) = v_j$ . The triplet  $(id_{office}, X, v_j)$  is sent to the electronic voting booth. The voting booth holds the function  $f$ . It retrieves  $X$  and calculates  $f(X)$  and verifies that  $f(X) = v_j$ . In case of equality, the machine checks in the set of stored triplets that it does not already exist this  $v_j$ . If this is the case the  $v_j$  is validated and the triple  $(id_{office}, X, v_j)$  is registered in the voting booth.  $v_j$  is given to the voter and posted on the voting bulletin board. In the case where  $v_j$  is already contained in the voting booth, access to the voting machine is refused to the voter because that supposes that he has already cast his vote.

### 3.5. Vote casting phase

This phase gathers all the steps of the actual voting from the creation of the ballot to the receipt marking the proof of registration of the vote of an voter.

#### 3.5.1. Creation of the ballot

Once the authentication is complete, the voter goes to the voting machine and accesses it via his code. Each candidate concerned by the election has a unique code to identify him and will be used at the polls by voters to make their choice. Formally, let  $C$  be the set of candidates and  $C_o$  be the set of candidate codes such that  $\text{card}(C) = \text{card}(C_o) = n$ . The bijection  $h$  that has each candidate associates a unique code is defined as follows :

$$h : C \rightarrow C_o$$

$$c_i \mapsto h(c_i) = c_{o_i}$$

The voter provides a random value  $r_j$ . This value is concatenated to each of the candidate codes and then encrypted with the public key of the ballot validation authority to produce a single ballot for that voter. Let  $E_v$  be the encryption function,  $E_v : C_0 \times \dots \times C_0 \times R \rightarrow \#C_o \times \dots \times \#C_o$

$$(c_{o_1}, \dots, c_{o_n}, r_j) \mapsto E_v(c_{o_1}, \dots, c_{o_n}, r_j) = (\#r_j c_{o_1}, \dots, \#r_j c_{o_n})$$

$E_v(c_{o_1}, r_j)$	$c_{o_1}$
$E_v(c_{o_2}, r_j)$	$c_{o_2}$
.....	.....
$E_v(c_{o_n}, r_j)$	$c_{o_n}$
Validation Code	

**Figure 2. Ballot Example**

The resulting ballot is of the form described in Figure1.

At this stage, the validation code is empty. He will be informed by the ballot validation unit of the ballot papers to certify that the ballot is correct. This built ballot is sent to the validation unit of the ballots for validation.

### 3.5.2. Validation of the ballot

Upon receipt of the ballot created, the ballot validation unit, decrypts with its private key, all the encrypted content in the bulletin and verifies that  $c_{oi}$  contained in each encrypted corresponds to that provided at the considered line and that it is a valid candidate code. In case of compliance, it validates the ballot by generating a unique validation code for it. The validated ballot is stored in the voting database (for verification) and sent to the voter.

### 3.5.3. Voting stage

To vote, the voter chooses the encryption corresponding to the code of the candidate for which he wishes to vote and builds his unique vote  $V_j = E_v(c_{oi}, r_j)$ .

$$\forall j \in 1, \dots, N_2, \exists! i \in 1, \dots, n | V_j = \#r_j c_{oi}$$

Let  $f^*$  be the voting function,  $f^*$  is an irreversible hash function which for a given voter recovers his choice and produces a single ballot corresponding to his vote and his Bull receipt,

$$f' : IdOffice \times v \times V \rightarrow B$$

$$(idOffice, v_j, V_j) \mapsto f'(idOffice, v_j, V_j) = Bull$$

Bull is given to the voter as proof of validation of his vote and will be used to verify his vote in the final count. After each vote, the voting unit builds a message consisting of Bull,  $v_j$  and  $idOffice$ , office identifier that is encrypted for each political party  $k$  with its public key ( $PublicKey_k$ ) and sent to the headquarters of said party. Let  $E_{PublicKey}$  this encryption function,

$$E_{PublicKey} : IdOffice \times B \times v \rightarrow \#B$$

$$(idOffice, Bull, v_j) \mapsto E_{PublicKey}(idOffice, Bull, v_j) = \#Bull$$

Each party also has the function  $f^*$ .

The voting unit also builds for each vote made by an voter a message consisting of Bull,  $V_j$ ,  $r_j$  and  $idOffice$  that it encrypts with the public key (PublicKey) of the CAA and gets the encrypted  $Y_j$ . Let  $E_{PublicKey}$  this encryption function,

$$E_{PublicKey} : IdOffice \times B \times V \times R \rightarrow Y$$

$$(idOffice, Bull, V_j, r_j) \mapsto E_{PublicKey}(idOffice, Bull, V_j, r_j) = Y_j$$

The  $Y_j$ s are transmitted by the voting data transfer unit to the CAA via a secure tunnel. The deciphering of the different  $Y_j$  will make it possible to count votes by candidates and obtain the results of the election.

### 3.6. Vote counting phase and public verification

At the end of the elections, the CAA has the  $Y_j$  vote database. However, the counting requires the use of the CAA private key *Privatekey*. This requires a step of reconstituting this key before the tally. In addition, each political party counts independently for the purpose of verifying the concordance of results published by the CAA.

#### 3.6.1. Key reconstitution

The election management organisation organizes the event to reconstitute the private key and summons all the actors, including the different political parties. Each party sends an officer with the function of the key held by the political party and an expert for possible controls. The different parts are recovered, introduced into the machine and reassembly performed according to the Shamir decoding principle described in algorithm 2 below. The reconstituted private key is given to the CAA and the different political parties (to perform the count).

---

**Algorithm 2** KeyReconstitution

---

**Input:**  $p_1, p_2, \dots, p_n$ ;  $(k, n)$  the threshold chosen for sharing keys.

**Output:** *Privatekey*

**for** each political party  $j \leftarrow 1$  **to**  $n$  **do**  
| recover  $p_j$  by the CAA via secure communication ;  
**end**

Use  $k$  sum of the parts  $(p_1, p_2, \dots, p_n)$ , interpolate with Lagrange contained in the Shamir scheme to generate the polynomial  $f(x)$  ;

The associated Lagrange polynomial is written :  $f(x) = \sum_{j=0}^{k-1} y_j l_j(x)$  where  $l_j$  are the basic polynomials of Lagrange and  $y_j$  the images by the polynomial function from  $p_j = (x_j, y_j)$ .

The  $l_j$  are defined as follows :  $\forall i \in \{0, \dots, k-1\} | i \neq j, l_j(x) = \prod \frac{(x-x_i)}{(x_j-x_i)}$  ;

The constant term in the polynomial  $f(x)$  is the private key *privateKey* ;

---

#### 3.6.2. Vote tally

The CAA decrypts the  $Y_j$  using *Privatekey* and extracts all the votes cast (*idOffice*, *Bull*,  $V_j$ ,  $r_j$ ). For each vote, using the voting code, he finds the corresponding ballot in the ballot database and verifies that the ballot actually contains  $V_j$ . It then retrieves the private key of the validation unit, decrypts all the entries of the ballot and from  $r_j$  extracts the different  $c_{oi}$ , checks that they are correct to ensure that the validation unit didn't fraud. It also verifies that the  $c_{oi}$  code in  $V_j$  corresponds to that of the line considered in the ballot. In case of compliance, he adds this vote in the list of counts that are in the form of tuples (*IdOffice*,  $Y_j$ , *Bull*,  $c_{oi}$ ). For each candidate  $c_i$ , the sum of the tuples containing  $c_{oi}$  give the number of votes he has obtained. The CAA publishes the list of results on the voting board and vote counts for each candidate. The CAA sends the  $Y_j$  database to the headquarters of each political party.

#### 3.6.3. Vote tally verification

Each party can also count independently and compare its results to those published by the CAA for verification and validation of results. Indeed each party has the following elements : the voting hash function  $f'$ , the database of encrypted messages ( $\#Bull$ ), the

database of  $Y_j$ , the private key *Privatekey*, the private key of the validation unit and his own private key *Privatekey<sub>k</sub>*.

To perform the count, he decrypts the  $Y_j$  with *Privatekey*, and extract the tuples  $(id\_office, Bull, V_j, r_j)$ . Then, using the private key of the validation unit and  $r_j$ , it decrypts the  $V_j$ , extract the  $c_{oi}$  and builds the database  $D1 = (id\_office, Bull, V_j, r_j, c_{oi})$  which is then sorted according to the key  $(id\_office, Bull)$ . Then, the encrypted messages  $E_{PublicKey}$   $(id\_office, Bull, v_j)$  are deciphered and extract the database  $D2 = (id\_office, Bull, v_j)$ . Similarly,  $D2$  is sorted according to the key  $(id\_office, Bull)$ . The join of  $D1$  and  $D2$  gives the database  $D$  whose each tuple is of the form  $(id\_office, Bull, v_j, V_j, r_j, c_{oi})$ . It calculates for each tuple,  $f(id\_office, v_j, V_j) = Bull$  and compare the value obtained with that of  $Bull$  of the considered tuple. It verifies that the  $c_{oi}$  corresponding to this  $Bull$  published by the CAA is the same as that contained in  $D$  and that it is a correct  $c_{oi}$ .

At the end, each party has the count of votes it has made and it can compare to the published one. In case of inconsistency the party may appeal for electoral fraud and a recount is organized to detect fraud. Each voter can go to the seat of his party to verify their vote or directly on the bulletin board or through an independent organization that he trusts by means of his receipt  $Bull$ . The verification consists of ensuring that he finds a tuple containing his  $Bull$  in all the published tuples and that the associated  $c_{oi}$  really corresponds to the code of their candidate. At the same time, any independent organization may also check the published voting data and track count using copies of the receipts from the voters. Anyone else can check the count because the check is based solely on the data posted on the bulletin board.

The voting sequence can be summarized as described in Figure 3.

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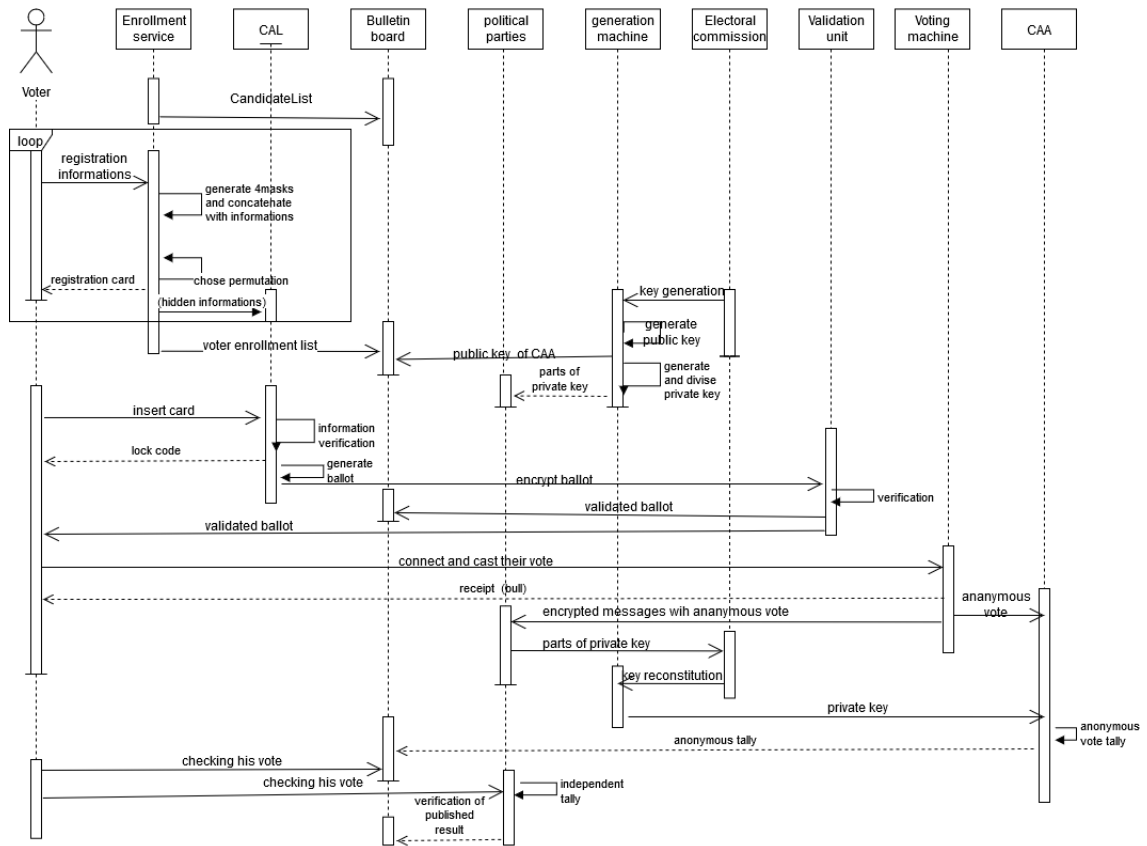
## 4. Evaluation

The published voting results are anonymous, encrypted and hashed and therefore do not reveal the voter's identity. In addition, the receipt provides to the voter is hashed with a one-way, collision-resistant hash function. It is impossible to know for whom an elector voted. Only the voter has this information and cannot reveal it to a third person.

The proposed protocol guarantees a set of properties required for a verifiable voting protocol. In the following we will be presenting these different properties.

- Precision : No vote can be added, deleted or modified without detection

Let's assume that an election authority is malicious and wants to vote for voters who abstained or voters who are absent. The authority is blocked at a first level because the personal information of the voters stored in the machine are locked using the disposable masks since the recording that only the voters hold. This information is required for authentication. It is therefore impossible for an authority to know exactly all the voters who did not vote. To obtain them, authority must be in agreement with the voters. Suppose an authority has skipped this step and generates a random lock code  $v_j$  as a result of authentication and will vote. However, the authority has no assurance that this  $v_j$  has not been used yet. The vote it will make will be easily detected as fraud because the lock codes  $v_j$  are deposited by each voter in a sealed urn in the voting booth immediately after his vote. The auditory trace of the  $v_j$  will show that the  $v_j$  used by the authority is not correct in case we do not find this  $v_j$  because it cannot have identical  $v_j$  especially as the function  $f$  to obtain them is a collision-resistant hash function. In addition, the malicious authority must provide a  $r_j$  that is necessary for the creation of a ballot. Thus, the addition of a vote requires the disposable mask, the values  $r_j$  and  $v_j$  correct. These elements are difficult to



**Figure 3. Voting interaction**

obtain without the voter because they depend on the voter and his personal information. Since the votes are published on the voting bulletin board, the voter can easily check that his vote has not been deleted. Also, the paper trace audit can detect any deletion.

Moreover, the false ballots are detectable because the ballots are validated by the validation unit. Indeed, the validation unit upon receipt of the ballots created decrypts all the encrypted  $E_v(c_{oi}, r_j)$  to ensure that the codes  $c_{oi}$  of candidates contained in these ciphered didn't modified when the ballot was created. Because the voters are called to make their choice from the encrypted in order to keep their vote secret. Because of this, any modification of the  $c_{oi}$  in the ciphered can cause a modification of the choice of the voter. The validation step of the ballot allows overcoming this type of fraud.

If the ballot validation unit is malicious and tries to rig the ballots with the false ciphered. For each vote, using the voting code, the CAA finds the corresponding ballot in the ballot database and verifies that the ballot actually contains  $V_j$  provided by the candidate. It then retrieves the private key of the validation unit, decrypts all the entries of the ballot and with  $r_j$  extracts the different  $c_{oi}$  and verifies that they are correct. It also verifies that the code  $c_{oi}$  in  $V_j$  corresponds to that of the line considered in the ballot. Thus, any modification made by the validation unit is detected by the CAA. In addition, the voting unit cannot modify a voter's vote because it is encrypted with the public key of the ballot validation unit. However, suppose that an external attacker intercepts the votes ( $Y_j$ ) when sent to the CAA by the transfer unit. It is impossible for this attacker to know the contents

of  $Y_j$  because he does not have the private key of the CAA . The functions of this key are held by the political parties and the key restored in the counting phase.

Suppose the CAA has changed, added or duplicated a vote. The  $Y_j$  database of votes is held by both the central counting authority and the different political parties. An equivalence test ensures that everyone has the same database. Each political party constructs the database of the tuples results  $D1 = (id_{office}, Bull, V_j, r_j, c_{oi})$  and the database of messages  $D2 = (id_{office}, Bull, v_j)$ . The join of D1 and D2 makes it possible to obtain the database D whose each tuple is of the form  $(id_{office}, Bull, v_j, V_j, r_j, c_{oi})$ . It calculates for each tuple,  $f'(id_{office}, v_j, V_j) = Bull$  and compares the value obtained with that of Bull of the tuple considered to ensure that the value of Bull has not been modified by the CAA. It also verifies that the  $c_{oi}$  corresponding to this Bull published by the CAA is the same as that contained in its database D and that it is a correct  $c_{oi}$ . Each party can verify the accuracy of the results published by the CAA. The CAA publishes the results on the voting bulletin board. Each voter can check with his Bull receipt that his vote has been taken into account. The verification consists in ensuring that he finds a tuple containing his Bull receipt in all the published tuples and that the associated  $c_{oi}$  actually corresponds to the code of the candidate of his choice. Any fraud of the CAA is detectable by the political parties. Similarly, any fraud by one of the political parties is detectable using the results of others or the CAA. One can easily check the concordance of the different results obtained at the end of the counts made by each of the parties.

Besides, it is difficult to add, delete, modify or duplicate an elector's vote in the proposed system. Indeed the voting process involves the different actors of an election and requires several key elements related to the voter. In addition, the protocol uses a public verification process.

- Democracy : Only authorized persons can vote once and only once. We have the population ie the number of people ( $N_2$ ) actually registered. Anyone wishing to vote must go through the registration phase and have at the end of which we have his disposable mask that is unique because there is a correspondence between his information and the mask provided.

- Confidentiality : Only the voter knows for which candidate he has voted The identifier and the personal information relating to a voter are locked using the disposable mask held solely by the voter. They cannot be known without the agreement of the voter. The ballot Bull, corresponding to the vote made by a voter and also used as a receipt for the voter, is the result of a collision-resistant and irreversible hash function. It is therefore impossible to make a correspondence between a voter and his vote. However, for each vote, the CAA knows the  $c_{oi}$  code of the chosen candidate and the random value  $r_j$  provided by the voter. The knowledge of these elements does not reveal to him the identity of the voter. As for the political parties, for each vote they are aware of the following elements :  $v_j, V_j, r_j, c_{oi}, f'$ . Each party has the elements that make it possible to reconstitute the vote (Bull) of a voter but in no case to reveal his identity. Although the lock code  $v_j$  is directly linked to the voter, it does not allow knowing his identity because  $v_j$  is obtained after authentication of the voter by an irreversible hash function of which the party is not aware. In addition, the elector cannot prove with his receipt to a third person for whom he has voted because the receipt is the result of a hash function. In sum, the use of the disposable mask and one-way hashing functions make it possible to ensure that it is difficult or impossible to match an elector and his vote and thereby guarantee confidentiality.

Verifiability is therefore ensured by the proposed protocol. Voters and political parties are involved in the voting process and are key elements of it, increasing confidence in the voting system. The system is based on simple processes that are understandable by all

actors, transparent and public, which makes it reliable. In addition, the system provides voters and political parties with the ability to check votes while ensuring confidentiality. This property limits the purchase of votes and ensures the integrity of elections.

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## 5. Conclusion and perspectives

The proposed system offers the possibility to check the vote. Voters, political parties have the opportunity to attest the published results as they are involved in the process. Voting procedures used are transparent ; do not require heavy cryptographic skills on the voters' side. The system is understandable by the different users. However, the proposed system, like any other network protocol, can be exposed to attacks related to the network infrastructure. Although the system can not specify any security measures to counter this type of security attack, it has properties that can simplify the design of these security measures.

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