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Science of the Total Environment, 2019

## Numerical modelling of the suspended particulate matter dynamics in a regulated river network

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#### Abstract

Understanding and predicting the propagation, deposition and re-suspension of suspended particulate matter (SPM) in river networks is important for managing water resources, ecological habitat, pollution, navigation, hydropower generation, reservoir sedimentation, etc. Observational data are scarce and costly, and there is little feedback on the efficiency of numerical simulation tools for compensating the lack of data on a river scale of several hundreds of kilometres. This paper aims at exploring the use of a one-dimensional (1-D) hydrodynamical model for understanding the source and fate of SPM during complex events. The numerical model was applied to the May-June 2008 flood in the Lower Rhône River, France. This event was a combination of floods of the Isère (including dam flushing operations in the Lower Isère River) and Durance tributaries over a two-week period. The simulation code was used to model the SPM fluxes at a high spatial and temporal resolution using a multi-class approach. Approximately half of the 4.9 Mt of SPM measured at the outlet at Beaucaire were found to come from the Isère River and the other half from the Durance River, whereas previous studies estimated that most of the SPM flux at the outlet came from the Durance River. The amount of SPM trapped within the river network, mainly behind the first hydropower structure downstream of the Isère confluence, was estimated to be 3.7 Mt due to the deposition of the coarsest

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particles. Such a model proved to be able to compute the interaction of various grain size classes with dams and other structures. In turn, the quality of the results of SPM fluxes and deposition is highly sensitive to particle parameters, especially grain size distribution, and to the operational rules of reservoirs.

Keywords: suspended sediment, suspended solids, 1-D hydrodynamical model, numerical simulation, Rhône River, flood

#### 1. Introduction

- Monitoring the suspended particulate matter (SPM) dynamics in river sys-
- 3 tems is crucial for multiple environmental management issues, such as the eco-
- 4 logical restoration of aquatic habitats, the sustainable operation of reservoirs,
- or the management of particle-bound contaminant fluxes (Walling et al., 2003).
- 6 These questions are generally facing a lack of data available at the watershed
- scale and at time scales from flood events to several years (*Horowitz et al.*, 2015).
- 8 The presence of dams significantly affects the SPM dynamics with large deposi-
- <sub>9</sub> tion in the reservoirs and possible resuspension during specific events when dam
- gates are opened. Sediment management in dam reservoirs and regulated rivers
- is indeed one important issue of the 21st century (Kondolf et al., 2014).
- The development of station networks measuring SPM and particulate con-
- taminants at large catchment scales remains limited due to the water sampling
- constraints and the cost of analyses (Horowitz, 2008). Data on SPM concentra-
- tion  $(C_{SPM})$  are mostly derived from discrete water sampling carried out as part
- of water quality monitoring programs (Walling and Webb, 1985; Phillips et al.,
- 17 1999; Horowitz et al., 2001). The frequency of these measurements, generally
- performed with a fixed periodicity, is almost never high enough to measure the
- <sub>19</sub> fine temporal variations in  $C_{\rm SPM}$ , leading to large uncertainties in flux budget
- estimation (Moatar et al., 2008). In recent decades, the development of surro-
- 21 gate techniques (Gray and Gartner, 2010) such as Optical Backscatter Systems
- 22 (OBS, also known as turbidity meters) has allowed the continuous measurement
- of the SPM concentration, provided that sufficient calibration data are available

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(Foster et al., 1992; Gippel, 1995; Clifford et al., 1995; Thollet et al., 2013; Dru-
   ine et al., 2018). Hydro-sedimentary stations based on water sampling and/or
   turbidity measurements at one point of the cross-section rely on the assumption
   of homogeneous SPM concentration (Horowitz, 2008). Nevertheless, the direct
   measurement of C_{\text{SPM}} at the river basin scale remains very expensive, time con-
   suming and in many instances problematic, especially in inaccessible sections
29
   and during floods (Ulke et al., 2017). Most of the time, field data are available
   only for a particular event or over a limited period of time (Mano et al., 2008;
   Navratil et al., 2012).
32
      Together with the deployment of denser measuring networks, hydro-sedimen-
   tary modelling allows the development of operational tools to improve the knowl-
34
   edge of the fate of suspended sediment in the river network (Wu et al., 2004).
   Moreover, it allows testing alternative management scenarios and several hy-
   potheses on the water and SPM inputs. The use of numerical hydro-sedimentary
   models has increased considerably in the last decades in conjunction with the
   advances in computational techniques. One-dimensional (1-D) codes are admit-
39
   ted to be suitable for simulation over large temporal and spatial scales as they
   require less field data and computational resources than 2-D and 3-D codes do.
   The limited ability of 1-D codes to reproduce fine physical processes is compen-
42
   sated by the stability of their numerical schemes and their fast calculation speed
   (Papanicolaou et al., 2008; El Kadi Abderrezzak and Paquier, 2009). Numerous
   1-D codes have been developed and are frequently used for engineering pur-
   poses. Amongst others, Wu et al. (2004) and Papanicolaou et al. (2008) listed
   several 1-D codes and their applications to rivers and dam reservoirs. These
47
   codes can be classified according to their range of application or their formu-
   lations: steady/unsteady flow, fully coupled/semi-coupled/decoupled flow and
49
   suspended sediment modelling, uniform/non-uniform grain size, equilibrium/non-
   equilibrium suspended sediment transport model. 1-D modelling is particularly
   suitable for calculating SPM dynamics since SPM concentrations are generally
52
   assumed to be homogeneously distributed throughout a river cross-section and
   modelling transverse mixing is not necessary (Garneau et al., 2015). Modelling
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a flood event at the river basin scale requires i) calibrating the hydraulic and suspended sediment transport parameters, ii) specifying the water and SPM inputs (upstream boundary conditions) and iii) validating the results along the river system, including at the outlet. The objective of this paper is to explore the use of a 1-D numerical model to better understand the spatial and temporal dynamics of SPM during floods 60 throughout complex river networks. In particular, we test the application of a 1-D numerical model in simulating the SPM dynamics in a river regulated by a series of run-of-the-river dams and other infrastructure. There is indeed very limited feedback in the literature on the following questions. What kind of results is a 1-D model able to provide and what is the added value compared to 65 observational data? What are the most sensitive parameters, hence the main sources of error? What are the most restrictive assumptions and the main perspectives for improvement? The first part of the paper describes the May-June 2008 flood event in the Lower Rhône River. This hydro-sedimentary event was selected for testing the model as it was a typical combination of floods and dam flushing operations and it comes with a complete set of high temporal resolution measurements on the main tributaries and at the outlet. The second part of the paper presents the 73 hydro-sedimentary numerical tools and the Rhône 1-D model used to simulate the May-June 2008 event. The Rhône 1-D model was developed as part of the 75 Rhône Sediment Observatory (OSR) to become an efficient tool for managing SPM at the scale of the river basin. The third part details the results of the modelling and highlights the impacts of grain size distribution and hydropower structures on the simulated SPM concentrations and deposits. The main lessons learnt from the modelling exercise are briefly discussed and summarised in con-

clusive comments.

#### 2. Case study

#### 83 2.1. The Rhône River

The Rhône River flows 810 km from its source in the Swiss Alps to its out-84 let to the Mediterranean Sea in the South of France (Fig. 1). It is the largest single source of freshwater to the Mediterranean Sea (Ludwig et al., 2009). Its 86 hydrological regime is influenced by snow melting in headwater catchments, 87 and by oceanic and Mediterranean rain events (Pardé, 1925). The three tributaries with the largest mean discharges are the Saône, Isère and Durance Rivers 89 (Tab. 1). The Rhône River basin is characterized by a large geological and climatic heterogeneity, and by a dense network of hydropower schemes. From 91 Lake Geneva to the Mediterranean Sea, the Rhône River is equipped with 21 hydropower schemes, all of which are run-of-the-river schemes except Génissiat Dam in the Upper French Rhône River (Fig. 1). 94 The Bourg-lès-Valence scheme detailed in Fig. 1 is typical of the other run-ofthe-river, by-passing hydropower plants (cf. Camenen et al. (2019) for a detailed description and analysis of sand fluxes). The Roche-de-Glun dam controls the discharge distribution between the Old Rhône and the power canal containing the Bourg-lès-Valence hydropower plant. A minimum compensation discharge 99 is maintained in the Old Rhône at any time. During floods, when discharge 100 exceeds the canal capacity, the excess flow is released in the Old Rhône. The 10: particularity of this scheme lies in the confluence between the Isère River and 102 the canal. In case of flood of the Isère River, the so-called Isère dam located 103 between the headrace canal and the Old Rhône (cf. Fig. 1) can derive the excess 104 discharge into the Old Rhône. 105 The Rhône River delivers substantial amounts of SPM to the Mediterranean 106 Sea (Radakovitch et al., 2008; Launay, 2014) with a mean inter-annual SPM 107 flux varying between 4.7 and 7.4 Mt/yr (Pont et al., 2002; Eyrolle et al., 2012; 108 Ollivier et al., 2010; Launay, 2014; Copard et al., 2018; Poulier et al., 2019) 109 but with huge variations of the annual SPM flux from one year to another. For

example, annual SPM flux ranged from 1.2 to 22.7 Mt/yr between 1992 and

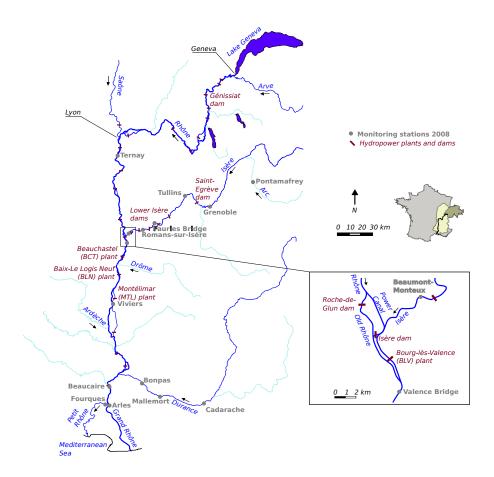


Figure 1: River network and hydroelectric schemes of the Rhône River from Lake Geneva to the Mediterranean Sea with a close-up view of the Bourg-lès-Valence hydroelectric scheme at the Rhône-Isère confluence. Monitoring stations of the May-June 2008 flood event in the Rhône, Arc, Isère and Durance Rivers are displayed.

112 1995 (Pont, 1997). Based on the long-term monitoring of  $C_{\rm SPM}$  at Arles near 113 the delta of the Rhône River,  $Eyrolle\ et\ al.\ (2012)$  showed that singular events 114 (flood or dam flushing) can represent up to 95 % of the annual SPM budget. The 115 need for a better monitoring of SPM fluxes through the Rhône River motivated 116 the creation of the Rhône Sediment Observatory (OSR) in 2009. As part of the 117 OSR, an SPM monitoring network in the Rhône River and its tributaries from 118 Lake Geneva to the Mediterranean Sea was developed mostly based on turbidity 119 measurements calibrated with frequent SPM samples.

Table 1: General information on the catchments and hydrological regimes of the Rhône River and its main tributaries.

-						
	A	$Q_a$	$F_a$	$Q_{max,2003}$	$Q_{max,2008}$	$C_{max,2008}$
Station	$[\mathrm{km}^2]$	$[\mathrm{m}^3/\mathrm{s}]$	$[\mathrm{Mt/yr}]$	$[\mathrm{m}^3/\mathrm{s}]$	$[\mathrm{m}^3/\mathrm{s}]$	[g/L]
Rhône at Lyon	20 300	600	0.6	813	1 206	-
Saône at Lyon	29 908	475	0.4	1 262	568	-
Isère at Beaumont	11 890	333	2.3	1 513	1 458	25.2
Durance at Bonpas	$14\ 225$	190	1.7	1 496	1 495	11.1
Rhône at Beaucaire	95 590	1 690	4.7 - 6.7	11 500	5 126	5.0

A= catchment area,  $Q_a=$  mean annual discharge,  $F_a=$  mean annual SPM flux according to Launay (2014),  $Q_{max,2003}$  and  $Q_{max,2008}=$  maximum discharges for the events of December 2003 and May-June 2008,  $C_{max,2008}=$  maximum  $C_{\rm SPM}$  for the May-June 2008 flood event.

According to Launay (2014) and Poulier et al. (2019), the main four tribu-120 taries in terms of SPM contribution to the Rhône River are the Arve River, the 121 Saône River, the Isère River and the Durance River (Fig. 1 and Tab. 1). The 122 SPM output of Lake Geneva is assumed to be negligible due to the large trap-123 ping capacity of the lake. The Isère and Durance Rivers are left bank alpine 124 tributaries of the Rhône River with fast and violent floods. The main SPM contributor of the Isère River is the Arc River, a mountainous river producing fine SPM (Camenen et al., 2016). The six Lower Isère dams located between 127 Grenoble and the Rhône confluence near Valence (Fig. 1) are run-of-the-river 128 dams. Only the lowest Isère dam, Beaumont-Monteux, by-passes the Isère River 129 with a derivation canal. 130

#### 2.2. The 2008 hydro-sedimentary flood event

In May-June 2008, a major hydro-sedimentary event occurred in the Lower Rhône River, combining natural floods in its two main tributaries, the Isère

and Durance Rivers, and flushing operations of the Lower Isère dams. All the 134 reservoirs of the Lower Isère and the Lower Rhône are run-of-river dams with 135 very limited storage capacity. They can be partially drained and sediment flushing operations must meet precise regulation requirements. Isère dams can 137 be flushed during flood falling phases in order to evacuate excess deposited 138 sediment. Rhône dams are not expected to be flushed but their operation can 139 be adapted to avoid deposition in critical areas such as around navigation locks or dam gates. This could not be done during the 2008 event presented here due to a lack of understanding and forecasting of the hydro-sedimentary processes, 142 and a lack of real-time coordination between the two distinct companies that 143 operate the Isère dams and the Rhône dams, respectively. 144 The peak discharge recorded at the Beaucaire station during this event was 145

The peak discharge recorded at the Beaucaire station during this event was 5 125 m<sup>3</sup>/s, corresponding to a 2-year return period flood. Between May 26th and June 8th 2008, the Arles station recorded a total SPM flux of 4.2 Mt at the Rhône outlet (*Eyrolle et al.*, 2012), equivalent to the SPM output of the 100-year flood in 2003 which had a twice larger peak discharge (Tab. 1). The May-June 2008 flood event in the Lower Rhône River was also remarkable because it produced an SPM flux almost equal to the mean annual SPM export of the Rhône River to the Mediterranean Sea recorded since 2005 (*Launay*, 2014).

During the 2008 flood event, SPM concentrations were measured at the 153 monitoring stations presented in Fig. 1, either continuously using OBS or the 154 acoustic attenuation method presented by Moore et al. (2012), or by sampling-155 filtration method (AFNOR, 2005). All the SPM samples were taken near the free-surface using buckets or automatic samplers. They include the homoge-157 neously distributed suspension ("washload"), not the graded sand suspension. 158 Well mixed cross-sections were chosen for the monitoring of  $C_{\text{SPM}}$  except for 159 the Rhône station at Valence Bridge, where the Isère and Rhône waters were 160 not fully mixed. Available SPM data cover the Arc-Isère-Rhône river network, the Rhône-Isère confluence with numerous samples, the Durance River network, 162 and some stations along the Rhône River. 163

Fig. 2 presents the water discharge times series and  $C_{\mathrm{SPM}}$  data collected

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during the event at the outlet of the Arc, Isère and Durance Rivers, and at four stations of the Rhône River. The Rhône at Ternay station is located upstream of 166 the Isère confluence and monitors the discharge and SPM inputs from the Upper Rhône River. The Rhône at Viviers station provides an intermediate checkpoint to study the Isère River input independently from the Durance input. This is 169 the first monitoring station downstream of the Isère confluence with a complete 170  $C_{\mathrm{SPM}}$  time series for the May-June 2008 flood event, while the Rhône at Valence 171 station recorded  $C_{\rm SPM}$  only during the third period of the event. The Beaucaire station located near the outlet of the Rhône River gives indication on the SPM 173 fluxes delivered to the Mediterranean Sea. The Beaucaire station is the last 174 discharge monitoring station for the Rhône River before the separation of the 175 two branches of the Rhône Delta. The measurement of  $C_{\text{SPM}}$  is performed at 176 the Arles station located about 13 km downstream on the Grand Rhône branch. The SPM concentrations are considered to be the same at Beaucaire and Arles 178 for the SPM flux calculation. 179

The measured SPM fluxes were determined by multiplying the instantaneous water discharges and the instantaneous  $C_{\rm SPM}$ . For monitoring stations with occasional  $C_{\rm SPM}$  measurements (samples), the SPM fluxes were estimated by establishing a power relation between discharge and  $C_{\rm SPM}$  to reconstruct a continuous  $C_{\rm SPM}$  time series.

The event can be divided into three SPM-producing periods (Fig. 2). The 185 first period covers the dam flushing of the Saint-Egrève dam occurring between 26/05/2008 and 29/05/2008 in the Isère River. This dam flushing was triggered concomitantly with a 1-year return period flood of the Isère River, with 188 discharges up to 1 000 m<sup>3</sup>/s at the Beaumont-Monteux station. During this pe-189 riod, the Lower Isère dams were operated with high water levels in the reservoirs, 190 and the water overflowing the gates. Meanwhile, a substantial flood occurred 191 in the Durance River, with  $C_{\rm SPM}$  greater than 10 g/L on the 27/05/2008. The management of the hydropower schemes of the Durance River during this pe-193 riod led to mitigate the discharge (around 800 m<sup>3</sup>/s) while releasing a large 194 amount of SPM. To account for the flood wave time lag between the upstream

part of the catchment and its downstream part, the ending date of the first 196 period was postponed to the 30/05/2008 for the downstream part. During the 197 second period, from 29/05/2008 to 02/06/2008, a large flood of the Arc River was recorded with  $C_{\text{SPM}}$  greater than 30 g/L, causing a  $C_{\text{SPM}}$  peak greater 199 than 20 g/L in the Isère at Beaumont-Monteux on the 30/05/2008. This peak 200 propagated in the Rhône River and about 8 g/L were recorded at Viviers on 201 the 31/05/2008. During this period, the Lower Isère dams were not flushed, 202 but the bottom gates were opened. The second period runs from 30/05/2008to 03/06/2008 to account for flood propagation delay. During this period, a 204 major flood occurred in the Durance River with discharge up to 1 500 m<sup>3</sup>/s and 205  $C_{\rm SPM}$  up to 6 g/L. The third period lasted from 02/06/2008 to 10/06/2008, for 206 which the Lower Isère dams were flushed, with low water level in the reservoirs 207 to evacuate the deposited sediments. The cloud of SPM was recorded around 04/06/2008 in the Isère at Beaumont-Monteux with maximum  $C_{\rm SPM}$  around 209 20 g/L. It was recorded in the Rhône at Viviers with a propagation delay of one 210 day and the peak  $C_{\text{SPM}}$  was about 2 g/L.

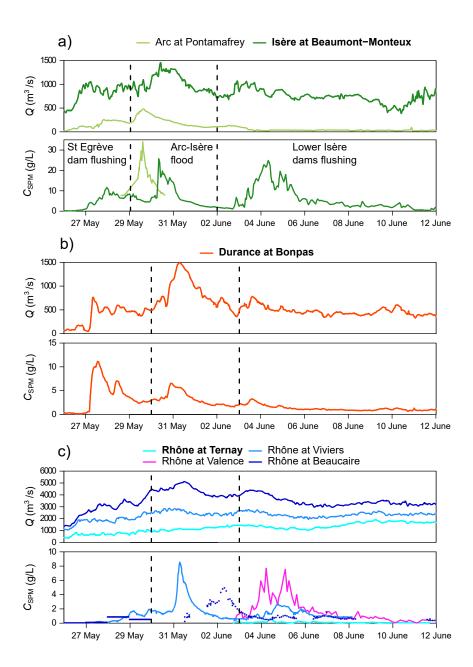


Figure 2: Discharges and SPM concentration ( $C_{\rm SPM}$ ) in (a) the Arc and Isère Rivers, (b) the Durance River and (c) the Rhône River during the May-June 2008 flood event. The limits of the three periods are shown with vertical dashed lines: on the 29/05/2008 and 02/06/2008 for the Isère River, on the 30/05/2008 and 03/06/2008 for the Durance River and the Lower Rhône River. Monitoring stations indicated in bold are the upstream boundary conditions of the model.

#### 2.3. SPM inputs from the Isère River

A  $C_{\text{SPM}}$  time series was reconstructed at the outlet of the Isère River since 213 a continuous  $C_{\rm SPM}$  time series was not available at the Isère at Beaumont-214 Monteux for the entire event (Fig. 3). The measurements used for the reconstruction were taken at Tullins (turbidimeter, Rieux, 2008), Romans-sur-216 Isère (side-looking hydroacoustic profiler, Moore et al., 2012), Beaumont-Mon-217 teux (manual water samples, Rieux, 2008) and the Rhône at Viviers. Between 218 26/05/08 and 30/05/08, the reconstructed  $C_{\text{SPM}}$  time series followed the measurements at Romans-sur-Isère, the closest station upstream of Beaumont-Mon-220 teux, with an estimated time lag of 1 h. Time lag between stations was cal-22: culated based on  $C_{\text{SPM}}$  peaks. Similarly, between 01/06/08 and 02/06/08, the 222 reconstructed  $C_{\rm SPM}$  time series followed the measurements at Tullins with an 223 estimated time lag of 10 h. However data based on Tullins station may be un-224 derestimated if erosion occurs in the Lower Isère reservoirs. Between 30/05/08 and 01/06/08, those reservoirs were flushed; as no representative measurements 226 were available, the SPM concentration at Beaumont-Monteux was evaluated as 227 the SPM flux in the Rhône at Viviers divided by the water discharge of the Isère 228 at Beaumont-Monteux. The rationale behind this computation is that during 229 that period the SPM flux coming from the Rhône upstream of the Isère junction 230 was negligible with respect to the SPM flux coming from the Isère. This ap-231 proximation is reasonable as discharges and SPM concentrations remained very 232 low in the Rhône upstream of the Isère junction during that period of time. 233 Finally, from 03/06/2008 on, SPM concentrations were measured at Beaumont-Monteux. 235

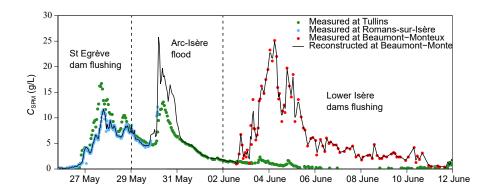


Figure 3: Reconstruction of the SPM concentration ( $C_{\rm SPM}$ ) time series of the Isère River at Beaumont-Monteux station from SPM measurements at Tullins and Romans-sur-Isère stations from 26/05/2008 to 12/06/2008.

#### 3. 1-D modelling of the May-June 2008 flood event

3.1. Numerical codes

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The 1-D hydro-sedimentary numerical tool used in this study was developed by Irstea. It couples the Mage and AdisTS hydro-sedimentary numerical codes.

Mage (Souhar and Faure, 2009) is a 1-D hydrodynamic code which simulates transient open-channel flows by solving the 1-D Barré de Saint-Venant equations (shallow water equations):

$$\frac{\partial A_w}{\partial t} + \frac{\partial Q}{\partial x} = q_{lat} \tag{1}$$

$$\frac{\partial Q}{\partial t} + \frac{\partial}{\partial x} \left( \beta \frac{Q^2}{A_w} \right) + g A_w \frac{\partial z}{\partial x} = -g S(J + J_s) + k q_{lat} V \tag{2}$$

where  $A_w$  is the wetted area, Q the water discharge, t the time, x the longitudinal coordinate,  $q_{lat}$  a lateral input/output discharge,  $\beta$  the momentum coefficient, z the water surface elevation, J the energy slope computed using the Manning-Strickler equation,  $J_s$  the local energy losses due to sharp variation of the cross-section, k a coefficient depending on the sign of  $q_{lat}$  (k=1 if  $q_{lat} < 0$ , k=0 if  $q_{lat} \ge 0$ ), and  $V=Q/A_w$  the cross-section-averaged velocity.

Mage describes the real geometry of the river bed as a series of cross-sections, and accounts for compound channel effects using the Debord equations (Nicollet

252 and Uan, 1979). Storage nodes can be defined to model floodplain areas where
253 the water velocity may be assumed to be negligible. No storage nodes were used
254 in the presented simulations. The river network topology may be looped (bi255 furcations, confluences), with multiple downstream boundary conditions. The
256 1-D Barré de Saint-Venant equations are solved using a four point semi-implicit
257 finite-difference scheme (Preissmann scheme).
258 AdisTS (Guertault et al., 2016) is a 1-D code solving mass conservation
259 equations for SPM transport in parallel. The code includes advection-dispersion

AdisTS (Guertault et al., 2016) is a 1-D code solving mass conservation
equations for SPM transport in parallel. The code includes advection-dispersion
equations in conservative formulation (Eq. 3) for several SPM classes. SPM
grain size distribution (GSD) is reproduced by mixing a fixed number of classes
of different proportion. The equations are coupled using source terms that allow
modelling erosion and deposition terms:

$$\frac{\partial A_w C_i}{\partial t} + \frac{\partial Q C_i}{\partial x} - \frac{\partial}{\partial x} \left( D_f A_w \frac{\partial C_i}{\partial x} \right) = (E_i - D_i) W_z \tag{3}$$

where  $C_i$  is the concentration in SPM class i,  $E_i$  and  $D_i$  are erosion and deposition fluxes of SPM class i,  $D_f$  is the longitudinal diffusion coefficient, and  $W_z$  is the river width. The source term combines the *Partheniades* (1965) formula for erosion and the *Krone* (1962) formula for deposition:

$$E_i - D_i = a_{\text{PD},i} (C_{\text{eq},i} - C_i) w_{s,i} \tag{4}$$

where  $C_{\text{eq},i}$  is the equilibrium concentration for the SPM class i,  $a_{\text{PD},i}$  is a recovery coefficient, reflecting non equilibrium sediment transport (Han, 1980;  $Armanini\ and\ Di\ Silvio$ , 1988), and  $w_{s,i}$  is the settling velocity of the SPM class i. The equilibrium concentration depends on the effective bed shear stress,  $\tau_{\text{eff}}$  as:

$$C_{\text{eq},i} = \begin{cases} C_{0,i} \left( \frac{\tau_{\text{eff}}}{\tau_{\text{cr},i}} - 1 \right) & \text{if } \frac{\tau_{\text{eff}}}{\tau_{\text{cr},i}} > 1 \\ 0 & \text{otherwise} \end{cases}$$
 (5)

where  $C_{0,i}$  is a calibration concentration specific to SPM class i,  $\tau_{\text{cr},i}$  is the critical shear stress for initiation of movement of SPM class i, estimated using the Shields diagram. For fine sediments ( $d < 70 \mu \text{m}$ ), since consolidation can be neglected when simulation is performed at event scale, the critical bed shear

```
stress is assumed independent of the grain size for fine sediments (\tau_{\rm cr} = 0.15 \, {\rm Pa}).
    The effective bed shear stress is computed as \tau_{\text{eff}} = (K_S/K_S')\tau, with K_S the
    total Strickler coefficient, K_S'=24/d_{90}^{1/6} the skin-friction Strickler coefficient.
    The total bed shear stress \tau = \rho g R_h J is computed using the 1-D hydraulic
    model (\rho water density and R_h hydraulic radius). The calibration of the two
281
    AdisTS parameters, a_{PD,i} and C_{0,i}, was performed as functions of the grain size
282
    by Guertault et al. (2016) on Génissiat hydropower scheme in the Rhône River.
       The longitudinal diffusion coefficient D_f was calculated using the formula of
284
    Iwasa and Aya (1991) as Launay et al. (2015) concluded it was the best suited
285
    based on their analysis of tracing experiments and hydro-acoustic measurements
    in the Rhône River near Lyon.
287
       AdisTS is loosely coupled with Mage software. The bed geometry remains
    fixed over time but the model simulates a potential stock of sediments available
    over each channel (main channel and floodway) in each cross-section. This stock
290
    is spatially distributed using a mean thickness and assuming a constant porosity
291
    p = 0.45; it can vary in mass and GSD over time due to erosion and deposition.
292
    Indeed, the advection-dispersion equation is solved for each sediment class and
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    the GSD of bed sediment stocks depend on the erosion or deposition simulated
    along the system for each class independently. It is possible to specify initial
29
    sediment stocks along the river system but for the presented simulations no ini-
296
    tial stock was assumed. Over long timescales, there may be geometric feedbacks
297
    that change channel capacity when erosion and sedimentation do not balance.
    However, the fixed-bed assumption has limited consequences over the timescale
    of an individual event. It allows a faster calculation which is of particular inter-
300
    est when dealing with long river reaches and long-term scenarios with limited
301
    bed evolution.
302
       The 1-D numerical tool can be used to identify the origin of the water flowing
303
    at a downstream monitoring station. This identification is done by injecting a
    numerical tracer in each tributary j with concentration C_{j,ref} = 1 g/L. At a
305
    downstream monitoring station where the total water discharge Q is calculated,
306
    the proportion of water Q_j/Q coming from the tributary j can be determined
```

based on the tracer mass continuity equation:  $Q_j/Q = C_j/C_{j,ref}$ , where  $C_j$  is the concentration of tracer coming from the tributary j calculated at the station. Similarly, each SPM class i from each tributary j can be traced so that concentration  $C_{SPM,i,j}$  is computed at each node and at each time of the simulation.

#### 3.2. 1-D model of the Rhône River

The Rhône 1-D model, developed by Irstea as part of the OSR program, rep-314 resents the Rhône River from Lake Geneva to the Mediterranean Sea (Fig. 1). 315 Bathymetry surveys of the river cross-sections are available every 500 m stream-316 wise. Lidar data were used to complete some profiles in the main channel and 317 to estimate the extent of the floodway. Additional profiles were included to represent dams and hydroelectric plants. In the model, cross-sectional profiles were 319 interpolated every 100 m. Cross-sections of the major tributaries (Arve, Ain, 320 Saône, Isère and Durance Rivers) were also included to represent their lowest 32 sections up to their confluences with the Rhône River. Other tributaries are 322 only represented as local inputs. 323

Flow resistance coefficients of the main channel (30  $\leq K_S \leq$  42 m<sup>1/3</sup>/s) 324 were calibrated and validated over each reach using longitudinal water profiles 325 measured over a wide range of discharges from low water to flood conditions 326  $(1500 \le Q \le 4500 \text{ m}^3/\text{s})$ . It was not necessary to vary the flow resistance 327 coefficients with discharge to achieve an acceptable calibration, i.e. stage errors lower than 0.1 m, typically. Flow resistance coefficients of the floodways (over 329 bars, islands, etc.) were assumed to be equal to  $20 \text{ m}^{1/3}/\text{s}$  everywhere. The 330 floodways of the Rhône River are narrow due to the presence of dykes and 331 overbank flows are limited. Therefore, the results are not much sensitive to the 332 values of the flow resistance coefficient defined for the floodways. The model does not include floodplains and cannot be used to simulate flooding over dikes. 334 The model includes the operation rules of the 21 run-of-the-river hydropower 335 schemes (Dugué et al., 2015). All the Rhône dams included in the model have 336 a bypass channel (remember that no Isère dams are included in the computational domain). The operation rules of the run-of-the-river hydropower schemes impose a minimum compensation discharge in the bypassed channel and a maximum discharge in the power canal as allowed by the hydropower plant (*Dugué et al.*, 2015). Also, the maximum water level at a regulation point in each reservoir is prescribed through legal dam operation rules which the operator has to follow, especially during floods, whatever the initial storage is. Such run-of-river dams actually have a limited storage capacity and the water level in the reservoir can be regulated by opening the dam gates, typically. The legal dam operation rules are specific to each dam and relate the maximum allowed water level as a function of inflow, usually.

For the specific study of the May-June 2008 flood event, the 1-D numerical 348 model was restricted to the Lower Rhône River, starting from Ternay station. Eleven hydropower schemes are present in the study area. In this configuration, the model has three main upstream boundary conditions: the Rhône at Ternay, 35 the Isère at Beaumont-Monteux (i.e. just downstream of the last dam of the 352 Lower-Isère chain of dams) and the Durance at Bonpas (see Fig. 1). The smaller 353 tributaries located between Ternay and the Mediterranean Sea are considered 354 as local water inputs. Both discharge and  $C_{\text{SPM}}$  time series for the three main 355 upstream boundaries are indicated as thick lines in Fig. 2. The discharge of the 356 smaller tributaries were also simulated. The downstream boundary conditions 357 on the Rhône Delta are the water levels measured in the Grand Rhône branch 358 and in the Petit Rhône branch (cf. Fig. 1).

Upstream of the Isère confluence, the SPM concentration in the Rhône River at Ternay was lower than 0.2 g/L typically (cf. Fig. 2c), which is much lower than the SPM concentration of the Isère and Durance tributaries during the flood event. As the discharge time series at Ternay does not indicate any flood, the SPM input at Ternay was set to zero for the simulations. The  $C_{\text{SPM}}$  time series used as input for the Isère River at Beaumont-Monteux was reconstructed as discussed in section 2.3. For the Durance River, SPM time series was recorded at Bonpas turbidity station (Fig. 2b). SPM inputs from smaller tributaries were considered to be negligible during the May-June 2008 flood event compared to

the inputs of the Isère and Durance Rivers.

#### 3.70 3.3. Grain size distributions

The 1-D numerical model requires information on the grain size distribution (GSD) of the SPM. Numerical simulations on the Rhône River were performed using six SPM classes with variable grain sizes from clay to medium sand, and assuming grain size distribution of each class to be log-normal of parameters  $d_{50,i}$  and  $\sigma_i$  (see Tab 2).  $d_{50,i}$  and  $\sigma_i$  are assumed constant in time; only the relative proportion of the class i (in the total SPM concentrations and stocks) may vary in time.

The three classes with the finest SPM were determined based on grain size 378 analysis of Rhône SPM samples (Launay, 2014) and the three classes with the coarsest SPM were defined by Guertault (2015). These classes were defined 380 so as to best represent main groups of particles that systematically show up 381 in the measured grain size distributions. Eventually, only the first four finest 382 classes will be used for this study, the two coarsest sand classes being easily 383 trapped by dam reservoirs (Camenen et al., 2019). The representative settling velocity  $w_{s,i}$  for each class of sediment i was calculated using Camenen (2007) 381 formula and assuming the grain size distribution of each class to be log-normal 386 (cf. Tab. 2). Cohesion is neglected since organic content is very low (< 5\%, 387 typically) as well as cohesiveness (Legout et al., 2018). The impact on settling velocity (flocculation) is thus relatively low, and there is actually no possible validation of any flocculation model for this specific case. 390

No GSD was measured in the Isère or Durance Rivers during the May-June 2008 flood event. Grain size analysis of the SPM of the Isère River in 2008 and during a similar hydrological event in 2015 showed that the particles of the Isère River and the SPM collected in the Rhône River during the 2012 dam flushes have similar grain size distributions. Therefore, the parameters calibrated by Guertault et al. (2016) were kept to simulate the 2008 flood event. The same assumption was made on Durance SPM although no grain size analysis was performed on SPM samples of the Durance River.

Table 2: Physical properties of the elementary SPM classes and AdisTS coefficients  $a_{PD,i}$  and  $C_{0,i}$ , as proposed by *Guertault* (2015). Proportions of the SPM classes in the three SPM mixtures tested with the numerical model for the Isère input.

Name	Class 1	Class 2	Class 3	Class 4	Class 5	Class 6
Median diameter: $d_{50,i}$ ( $\mu$ m)	4	15	45	90	200	400
Standard deviation of $\ln(d_i)$ : $\sigma_i$ (-)	0.32	0.24	0.17	0.17	0.20	0.20
Settling velocity: $w_{s,i}$ (m/s)	$2.8 \ 10^{-5}$	$2.3 \ 10^{-4}$	$1.4 \ 10^{-3}$	$7.5 \ 10^{-3}$	$2.6 \ 10^{-2}$	$5.8 \ 10^{-2}$
Critical shear stress: $\tau_{{\rm cr},i}$ (Pa)	0.153	0.154	0.155	0.158	0.174	0.232
Recovery coefficient: $a_{\text{PD},i}$	1	1	1	1	1	1
Calibration concentration: $C_{0,i}$ (g/L)	1	1	0.5	0.2	0.2	0.2
% in Mixture A - Fine	31	44	25	0	0	0
% in Mixture B - Medium	23	28	31	18	0	0
% in Mixture C - Coarse	12	18	40	30	0	0

determine three possible GSD for the SPM transported by the Isère River in 400 May-June 2008, named Mixtures A, B and C (see Fig. 4 and Tab. 2). The 401 measured GSD were approximated using a mixture of log-normal distributions, 402 as explained by Masson et al. (2018). 403 Two surface water samples were collected during floods of the Arc River 404 (June 2015, documented by Camenen et al. (2016)) and the Isère River (May 405 2015). The Arc River is the main natural SPM input to the Isère River. The 406 SPM usually transported by the Arc River represent the finest SPM transported during a flood in the Arc-Isère river network (classes 1 and 2 composed of clay and fine silt). They were averaged to give Mixture A - Fine GSD (Fig. 4). 409 Two samples of riverbed sediment were collected in the Rhône River after the 410 May-June 2008 flood event. One sample was collected downstream of the Bourg-411 lès-Valence (BLV) plant (06/08/2008), and the other sample was collected in 412 the garage of the BLV lock (23/06/2008). Additionally, one sample was taken 413 after the flood of May 2015 from a deposit near the right bank of the Isère 414 River downstream of Beaumont-Monteux. Bank deposit and riverbed sediment

Samples collected in other occasions in the Arc-Isère network were used to

399

samples correspond to the coarsest SPM transported during a flood. They were averaged to compose Mixture C - Coarse GSD, which is considered as an extreme scenario for which most of the SPM would be made of that coarsest fraction. Finally, one sample taken in the water column close to the bottom at the Rhône and Isère confluence during the May 2015 flood contained particles from clay to coarse silt in equal proportions. This intermediate sample constitutes Mixture B - Medium GSD.

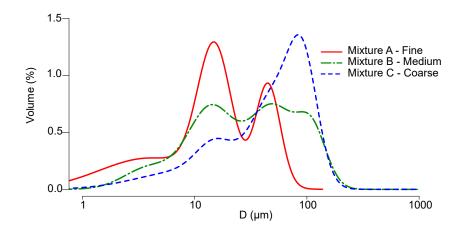


Figure 4: Three possible grain size distributions for the SPM transported by the Isère River during the May-June 2008 flood event.

The SPM of the Durance River was assumed to be composed of clay only (class 1), with a median diameter  $d_{50}$  of 4  $\mu$ m. This hypothesis relies only on field observation of the very fine aspect of the washload transported by the Durance River.

#### 7 4. Results

4.1. Origin of water discharge during the May-June 2008 flood event

The contributions of the Isère and Durance Rivers to the Rhône River water discharge during the May-June 2008 event were evaluated using the 1-D model. The hydrograph decomposition results are presented for the Rhône at Valence Bridge, Viviers and Beaucaire stations (Fig. 5). Overall, the simulated discharge is within 10% of the measured discharge, except for short transient phases. This is less than the expected level of uncertainty of hourly discharge measurements (*Horner et al.*, 2018), which suggests that the main sources of water and their propagation through the river network are correctly simulated by the model.

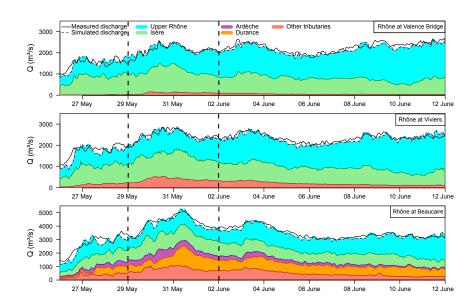


Figure 5: Decomposition of the flow hydrographs of the May-June 2008 flood event at the hydrometric stations of the Rhône at Valence, Viviers and Beaucaire using the 1-D hydrodynamic model. The three periods (see section 2.2) are separated by the vertical dashed lines.

At Valence Bridge station (Fig. 5a), two water sources can be distinguished:
the Upper Rhône River (upstream of Ternay) and the Isère River. The contribution of the tributaries between Ternay and Valence was very small during the
event. The Upper Rhône River was not in flood during the period of the MayJune 2008 flood event, so the shape of the hydrograph at Valence Bridge was
mainly influenced by the Isère River contribution. At Viviers station (Fig. 5b),
the contribution of the tributaries other than the Isère is increased by water
inputs from the Eyrieux, Drôme, Right-bank Ouvèze and Roubion Rivers. The

discharge contribution of these tributaries is higher than that of previous tributaries between Ternay and Valence but remains small. At Beaucaire (Fig. 5c),
most of the water came from the Upper Rhône (from 20 to 40 %), the Isère
(around 25 %) and the Durance (around 25 %) Rivers, with smaller inputs from
the Ardèche and other tributaries.

#### 4.2. Impact of grain size distribution on simulated SPM concentrations

During the May-June 2008 flood event, one can expect different sources of SPM for the three distinct periods described in section 2.2, with dam flushing operation during the 1st and the 3rd periods and natural floods during the 2nd period. As a consequence, one can expect different GSD for each of these periods. As the GSD of SPM transported by the Isère River were not measured in 2008, simulation tests were run using the three hypothetical mixtures defined in Tab. 2 from samples collected in the Isère River during other events (Section 3.3). Results from these three simulations are presented in Fig. 6.

Simulated concentrations  $C_{\rm SPM}$  obtained at Viviers station are compared with measured concentrations in Fig. 6. Simulated SPM concentrations are sensitive to grain size due to erosion/deposition and transport processes. Concentrations  $C_{\rm SPM}$  at Viviers using the coarse GSD (Mixture C) are half the  $C_{\rm SPM}$  simulated using the fine GSD (Mixture A). This is explained by the more intense deposition of the coarsest particles within the four hydropower schemes between the lowest Isère dam and Viviers.

For the flood period, although concentrations at Beaumont-Monteux were 466 evaluated based on Viviers concentrations, the model yields an underestimation 467 of the peak concentrations whatever the choice of GSD. This results from dis-468 persion processes. The concentration peak at Beaumont-Monteux should thus 469 have been higher and narrower to take into account this effect. The difference between measured and simulated  $C_{\text{SPM}}$  could also be partly due to an overes-47 timation of the  $C_{\text{SPM}}$  measured at Viviers by the acoustic attenuation method, 472 particularly when fine particles are highly concentrated, which increases the 473 acoustic attenuation (Moore et al., 2013).

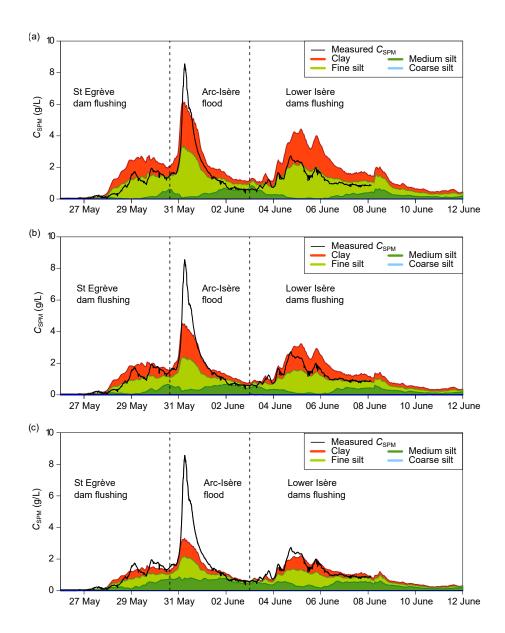


Figure 6: Simulated and measured SPM concentration ( $C_{\rm SPM}$ ) at Viviers station for the three hypothetical GSD defined in Tab. 2: (a) Mixture A - Fine, (b) Mixture B - Medium and (c) Mixture C - Coarse.

Simulation tests also confirm that the GSD of the SPM transported was different during the three periods of the May-June 2008 flood event. During the

St Egrève Dam flushing period, the model using medium or coarse GSD (Mixtures B or C) yields  $C_{\rm SPM}$ -values in relatively good agreement with measured data. Mixture B was eventually preferred since it corresponds to measured data during the flood period of a similar event (in 2015). Also, it yields a better estimation of peak concentrations. Flushing operation evacuated the coarse SPM from the St Egrève reservoir, but they were partially stored into the Lower Isère reservoirs, as the Lower Isère dams were operated with high water levels during this period. This could explain why the medium GSD is consistent with this situation.

During the Arc-Isère flood period, the  $C_{\text{SPM}}$  peak measured at Viviers 486 reached about 9 g/L. Mixture A yielded the best agreement between simu-487 lated and measured  $C_{\text{SPM}}$  time series. Such very fine washload material, poorly 488 represented in the bed, is brought from the Isère basin by the flood wave. Nevertheless, the simulated  $C_{\text{SPM}}$  peak reached only 6 g/L. As discussed above, 490 the concentration peak at Beaumont-Monteux should have been higher and 491 narrower. Using a finer GSD could also increase the simulated  $C_{\text{SPM}}$  peak. 492 However, as discussed in section 3.3, a finer GSD would no longer correspond 493 to the samples measured in the Isère River during floods of the Arc River. 494

For the third period of the event, corresponding to the Lower Isère dams flushing, Mixture C yields  $C_{\rm SPM}$  at Viviers station that are in best agreement with measurements. This is consistent with the opening of the dam gates and the resuspension of coarser particles previously settled in the reservoir.

According to these observations, the GSD was parametrized as follows for the simulation of the May-June 2008 flood event: the medium GSD of Mixture B for the first period, the fine GSD of Mixture A for the second period and the coarse GSD of Mixture C for the third period.

#### 503 4.3. Interaction of SPM with hydropower schemes

The objective of this section is to study the SPM dynamics in interaction of SPM with hydropower schemes between the lowest Isère dam and Viviers station (Fig. 1). Five additional simulations were carried out to study the de-

position/erosion processes occurring in each hydropower scheme of the reach. The first simulation was run without activating deposition/erosion within the 508 entire river system. In the other four simulations, deposition/erosion was successively activated in the four hydropower schemes of the system, which led to 510 the decrease of the  $C_{\text{SPM}}$  simulated at Viviers (Fig. 7). Simulation of deposition 511 is necessary to reproduce the  $C_{\rm SPM}$  measured at Viviers. The simulated  $C_{\rm SPM}$ 512 peak decreased from 4 to 2 g/L, 9 to 6 g/L, and 8 to 2 g/L in the first, second, 513 and third period, respectively. This confirms that hydropower schemes are an 514 obstacle to SPM transport due to the decreased flow velocity in dam reservoirs, 515 which enhances deposition particularly for coarse SPM. Deposition is particu-516 larly intense during the dam flushing periods (first and third periods), as coarser 517 GSD was parameterized for these periods (see section 4.2). These simulations 518 also suggest that the largest decrease of  $C_{\mathrm{SPM}}$  occurred in the Bourg-lès-Valence (BLV) scheme, between the lowest Isère dam and BLV dam. SPM also settled 520 down within the next three hydro-electric schemes, but to a lesser extent since 521 most of the coarsest particles settled down in the first scheme.

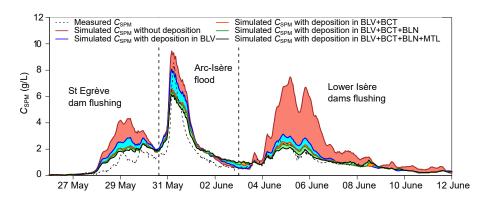


Figure 7: Measured and simulated SPM concentration ( $C_{\rm SPM}$ ) at Viviers station during the May-June 2008 flood event, with deposition/erosion processes successively activated in the four hydropower schemes located between the lowest Isère dam and Viviers. BLV = Bourglès-Valence, BCT = Beauchastel, BLN = Baix-Le Logis Neuf, MTL = Montélimar. Coloured areas represent the cumulative SPM trapped in successive reservoirs.

The numerical model provides detailed information on the quantity and grain

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size distribution of the SPM present in each branch of the river system at any time of the simulation. In order to better understand the deposition processes 525 between the lowest Isère dam and the BLV dam observed in Fig. 7, the cumulative amounts of SPM settled in the area are presented in Fig. 8. At the scale 527 of the entire event, the Isère River produced a total amount of 7.7 Mt of SPM, 528 of which 2.8 Mt deposited at the Isère-Rhône confluence (Fig. 8d). The SPM 529 deposition occurred mainly within three branches of the network: 60% in the 530 lowest Isère branch, and 30% in the BLV and Beauchastel (BCT) power canals. Deposition mainly occurred during the second and third periods with a segre-532 gation in the grain size of the particle deposited, as also observed by Camenen 533 et al. (2019). The Isère River produced 2.8 Mt during the second period, and 534 80 % of this input, mainly composed of fine SPM, travelled through the BLV 535 and BCT schemes. The remaining 20%, mainly composed of class 3 particles, were trapped in the BCT and BLV power canals, and not in the lowest Isère 537 branch. But most of the deposition occurred during the third period when the 538 Lower Isère dams were flushed. The SPM flux during this period was 3.8 Mt, i.e. 539 half of the total input of the Isère during the event. SPM of class 4 represented 540 30 % of the Isère River input, and these particles massively deposited within the Isère branch, and to a lesser extent within the BLV and BCT power canals. 542 The deposits simulated in the downstream Isère reach are mainly composed of 543 classes 3 and 4, which is consistent with available observations and with the 544 choice of Mixture C as a coarse GSD representative of a deposit collected after the May 2015 flood.

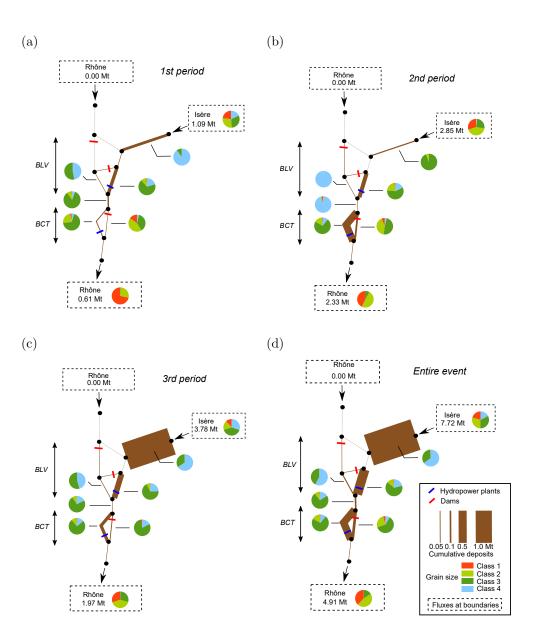


Figure 8: Mass and grain size composition of SPM deposited in the Isère-Rhône confluence system during the May-June 2008 flood event: first period (a), second period (b), third period (c) and entire event (d). See section 2.2 for definition of periods and Tab.2 for definition of grain size classes. The mass and grain size composition of SPM fluxes at boundaries are also shown. The thickness of the lines is proportional to the mass of SPM deposited in each reach. BLV = Bourg-lès-Valence scheme and BCT = Beauchastel scheme.

#### 4.4. Cumulative SPM fluxes

Measured and simulated SPM cumulative fluxes are presented in Tab. 3 and Fig. 9 for the three periods (see section 2.2) and for the entire May-June 2008 flood event at the monitoring stations in the Rhône River. In Fig. 9, the lefthand graphs display the cumulative fluxes estimated from observations whereas the right-hand graphs display the cumulative fluxes specified or simulated in the numerical model.

The relative deviation between the simulated and measured SPM cumulative fluxes was between +15 % and +36 % (see Tab. 3), except for the first period for 555 which larger values are observed since measured cumulative fluxes are small. At 556 Viviers station, the absolute deviation was around +0.8 Mt for the entire event 557 for a total measured SPM flux of 3.6 Mt at this station. This relatively small deviation validates the reconstruction of the  $C_{\rm SPM}$  time series at Beaumont-Monteux described in section 2.3, and the choice of the varying GSD for the 560 three periods (see section 4.2). At Arles station, the measured SPM flux for the 561 entire event was 4.2 Mt, and the simulated SPM flux was 5.7 Mt. Eyrolle et al. 562 (2012) estimated this flux to be 4.7 Mt  $\pm$  30 %. These results are of the same 563 order of magnitude and confirm the exceptional nature of the May-June 2008 flood event. 565

As for the Durance River, the model highlighted the weakness of the hy-566 pothesis made of a very fine grain size distribution for the entire event. During 567 the first week of the event, the relative deviation between measured and simulated fluxes increased from +50% to +133% between Viviers and Beaucaire (see Tab. 3). This is explained by the transfer of the SPM of the Durance directly 570 to Beaucaire without deposition because of a too fine grain size distribution as-571 sumed for the Durance River SPM input during this first period. The measured 572 SPM flux of 0.5 Mt only at Beaucaire during the first week indicated a large de-573 position of around 1.0 Mt at the Durance confluence. For the second and third periods, the hypothesis of a fine GSD for the Durance SPM input appeared 575 more realistic although still a little bit too fine as the measured and simulated 576 fluxes at Beaucaire were in better agreement. The fine SPM coming from the

Table 3: Measured and simulated SPM cumulative fluxes for the three periods (see section 2.2) and for the entire May-June 2008 flood event at the monitoring stations in the Rhône River, and relative deviations (RD) of the simulated fluxes to the measured flux.

	Rhône at Viviers			Rhône at Beaucaire			Rhône at Arles		
	Meas.	Model	RD	Meas.	Model	RD	Meas.	Model	RD
	Mt	Mt	%	Mt	Mt	%	Mt	Mt	%
Period 1	0.4	0.6	+50	0.6	1.4	+133	0.5	1.2	+140
Period 2	1.9	2.2	+16	2.6	3.0	+15	2.2	2.6	+18
Period 3	1.3	1.6	+23	1.7	2.1	+24	1.5	1.9	+27
Total	3.6	4.4	+22	4.9	6.5	+33	4.2	5.7	+36

Durance River during these two periods seemed to have travelled through the downstream Durance reach and Rhône River down to the Delta with limited 579 deposition. For the downstream Durance reach, this also could be explained 580 during the second period because of the much higher discharges and velocities. 581 The model was also useful for estimating the amount of SPM transported 582 in the Petit Rhône at Fourques, where no  $C_{\rm SPM}$  measurement were available. 583 The SPM flux of the Petit Rhône represented from 10 to 15 % of the SPM 584 fluxes measured at Beaucaire station. This is in good agreement with the water discharge distribution between the Petit Rhône and the Grand Rhône observed in long-term discharge time series (source CNR).

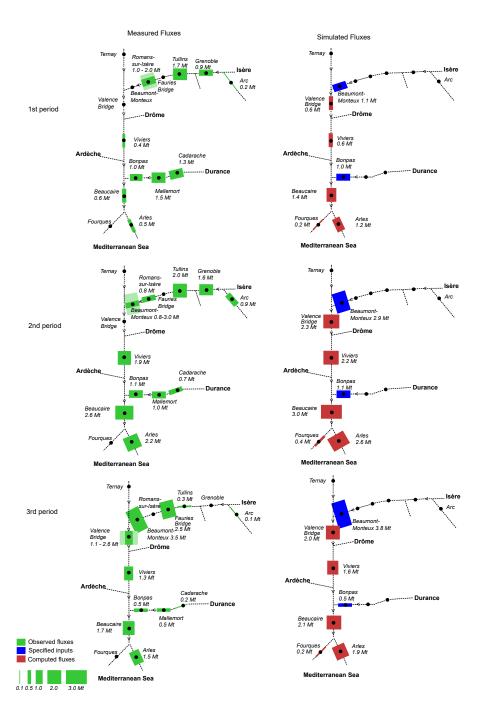


Figure 9: Monitored and simulated SPM cumulative fluxes (in Mt) along the Rhône River during the first, second and third periods of the 2008 flood event. Line thickness is proportional to SPM flux at the corresponding station.

#### 4.5. Origin of the SPM

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The origin of the SPM transported during the three periods of the event 589 and measured at Arles was clarified. In particular, the Isère River input that 590 was not measured during the first period could be quantified with the model. Fig. 10 shows the evolution of the measured and simulated  $C_{\text{SPM}}$  at Arles and 592 the proportion of SPM coming from both the Isère and the Durance Rivers. 593 The simulated  $C_{\text{SPM}}$  are close to the measured  $C_{\text{SPM}}$ , except the  $C_{\text{SPM}}$  peak 594 recorded on 01/06/2008. The maximum recorded  $C_{\text{SPM}}$  was about 5 g/L while the maximum simulated  $C_{\text{SPM}}$  was 4 g/L, being a difference of 20 %. Fig. 10 highlights the high contribution of the Durance River during the first days of 597 the event, and the increasing contribution of the Isère River during the rest of 598 the event. Approximately 50 % of the SPM fluxes came from the Durance River 599 and the remaining 50 % came from the Isère River. Marion et al. (2010) and Eyrolle et al. (2012) discussed the origin of the SPM transited and deposited 601 in the Grand-Rhône pro-delta during the May-June 2008 event. They assumed 602 that most of the SPM came from the Durance River, therefore they investigated 603 the origin of the SPM within the Durance river basin and ignored the equally 604 large contribution of the Isère River.

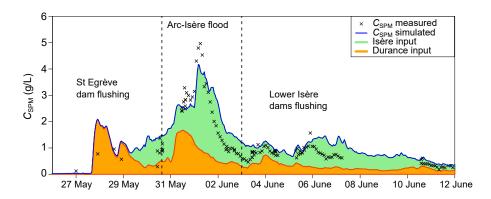


Figure 10: Simulated and measured  $C_{\rm SPM}$  in the Rhône at Arles during the May-June 2008 flood event with decomposition of the Isère and Durance Rivers SPM inputs.

Nearly 50 % of the SPM flux brought by the Isère River to the Rhône

River system deposited in the river network before reaching Viviers. Although
the model confirmed that the Rhône reservoirs acted as sediment sinks during
the May-June 2008 flood event, they can turn to act as sediment sources due to
resuspension during other floods. In the annual SPM fluxes computed by *Poulier*et al. (2019), there is evidence that the SPM deposited and stored during the
2008 event were later re-suspended and exported during floods.

#### 5. Conclusive comments

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This paper explores the potential of numerical simulation to predict the 614 sources and fate of SPM in regulated river networks. The main questions on numerical simulation tools addressed through this case study were: What is 616 the added value of 1-D modelling of SPM fluxes? What are the most sensitive 617 parameters? What are the main limitations and perspectives for improvement? 618 A 1-D hydrodynamical model was built and applied to a major hydro-619 sedimentary event in May-June 2008 in the Lower Rhône River, France. Such model would be the simplest and fastest possible hydrodynamical model that 62 could be constructed and some physical processes that may be important are 622 neglected in exchange for that simplicity. The Rhône River has a complex river 623 network with confluences, bifurcations and hydropower schemes. The simulation code (AdisTS) was able to model the SPM fluxes at a high spatial and 625 temporal resolution, which is useful to understand the SPM dynamics over the 626 whole river system on time scales ranging from hour to decades, thanks to fast 627 computational times. Especially, SPM supplies from the main tributaries and 628 deposition of the coarsest particles behind hydropower structures could be quantified precisely, at any time and at any cross-section of the river network. The model provides insights that are not available from observational data alone. Es-631 pecially, the model simulates the continuous dynamics and spatial distribution 632 of deposits, which would have allowed a better anticipation and management of sedimentation in critical areas of the Rhône reservoirs.

In the presented study case, approximately half of the 4.9 Mt of SPM mea-

sured at the outlet of the Rhône River catchment during the event were found to come from the Isère River and the other half from the Durance River whereas 637 previous studies estimated that most of the flux at the outlet came from the Durance River. Also, the model confirmed that a large amount of the SPM delivered by the Isère River was trapped behind the first hydro-electric scheme in 640 the Rhône River, a cause of conflicts between dam operators. The high temporal 641 and spatial resolution of fluxes computation is highly valuable for reconstructing past events and also for managing future events like natural floods or dam flushing operations, by testing multiple dam operation scenarios. If forecasts of water discharges and SPM inputs are available, such a model can be used 645 to compute real-time forecasts of SPM concentrations, fluxes and deposition 646 throughout the river network.

As a basis for hydraulic simulation, an accurate description of the channel geometry and of the artificial structures is necessary, along with a conventional 649 calibration of the friction coefficients along the river stretches. This was easily 650 achieved in our case study. As for SPM simulation, the quality of the numeri-651 cal results was found to be highly sensitive to suspended sediment parameters, 652 especially grain size, and to the operational rules of artificial structures. This 653 may lead to substantial errors because accurate information on grain size distri-654 bution is often difficult to obtain, grain size varies spatially and temporally, and 655 the coarsest particles may not be homogeneously distributed throughout the 656 river cross-section. In this study, sensitivity tests made on the grain size distribution of the SPM improved our knowledge of the Isère River input, despite the lack of measurements. Finer SPM particles were mostly transported during 659 the natural flood period while coarser SPM were transported during the dam 660 flushing periods. The simulation of deposition and erosion processes within the 661 hydropower schemes was necessary to reproduce the strong deposition of SPM 662 at the Isère confluence and further downstream. Deposits were mainly composed of the coarsest SPM (cf. Camenen et al., 2019), while finer SPM travelled 664 through the hydropower schemes without settling down. 665

Of course, observation and modelling supplement each other: dense and

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precise SPM observational data measured at key points of the river system
are necessary to specify the boundary conditions of numerical models, and to
calibrate and validate them. An extended sensitivity analysis could be done
to better infer upstream sediment supply, i.e. input concentrations and GSD.
In the present paper, we constrained the tests to prior knowledge based on
actual measurements and uncertainties. Another perspective of this work is to
compare 1-D numerical modelling with chemical fingerprinting for quantifying
SPM sources in the Rhône River for various hydrological conditions.

The 1-D numerical model applied in this study is typical of modern simu-675 lation tools used in river engineering applications. While the principles of 1-D 676 hydrodynamical codes have virtually not changed for fifty years or so, their 677 computation performance and the power of the available computers have been 678 greatly improved. Compared to 2-D or 3-D hydrodynamical codes, 1-D hydrodynamical codes offer much faster computational times allowing for real-time 680 or long-term simulations and uncertainty analysis through Monte Carlo sim-681 ulation or sensitivity analysis (Souhar and Faure, 2009), which is practically 682 challenging with higher level codes. The spatial resolution of 1-D hydrodynam-683 ical codes is sufficient for studying SPM dynamics on the river network scale, while 2-D or 3-D hydrodynamical codes would be required for studying local 685 processes, in the close vicinity of artificial structures for instance. However, most 686 1-D hydrodynamical codes still come with restrictive assumptions that call to be 687 improved through future research. Computing the flow and suspended sediment flux interactions between the main channel and the floodways, or floodplains, is still motivating active research. More generally, the spanwise distribution of 690 velocities, SPM concentrations and deposition/erosion fluxes throughout cross-691 sections has to be predicted from 1-D, i.e. cross-sectional average results. A 692 major limitation of 1-D hydrodynamical codes is the usual assumption of full, 693 instantaneous mixing of water and SPM downstream of confluences. In the case of the Rhône River, full mixing after a confluence is actually seldom reached 695 before the next bifurcation between the navigation canal and the by-passed 696 channel of the Old Rhône. Formulas for predicting the degree of mixing and the spanwise distribution of SPM concentrations still have to be elaborated, based on tracing experiments conducted in the laboratory and in the field.

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