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The environment of the fast rotating star Achernar[★]

III. Photospheric parameters revealed by the VLTI

A. Domiciano de Souza¹, P. Kervella², D. Moser Faes^{2,3}, G. Dalla Vedova¹, A. Mérand⁴, J.-B. Le Bouquin^{5,6}, F. Espinosa Lara^{7,8}, M. Rieutord^{7,8}, P. Bendjoya¹, A. C. Carciofi³, M. Hadjara^{1,9}, F. Millour¹, and F. Vakili¹

¹ Laboratoire Lagrange, UMR 7293, Université de Nice-Sophia Antipolis (UNS), CNRS, Observatoire de la Côte d'Azur, 06300 Nice, France
e-mail: Armando.Domiciano@oca.eu

² LESIA, Observatoire de Paris, CNRS UMR 8109, UPMC, Université Paris Diderot, 5 place Jules Janssen, 92195 Meudon, France

³ Instituto de Astronomia, Geofísica e Ciências Atmosféricas, Universidade de São Paulo (USP), Rua do Matão 1226, Cidade Universitária, 05508-900 São Paulo, Brazil

⁴ European Southern Observatory, Alonso de Córdova 3107, Casilla 19001 Santiago 19, Chile

⁵ Univ. Grenoble Alpes, IPAG, 38000 Grenoble, France

⁶ CNRS, IPAG, 38000 Grenoble, France

⁷ Université de Toulouse, UPS-OMP, IRAP, 31028 Toulouse, France

⁸ CNRS, IRAP, 14 avenue Édouard Belin, 31400 Toulouse, France

⁹ Centre de Recherche en Astronomie, Astrophysique et Géophysique (CRAAG), Route de l'Observatoire, BP 63, Bouzareah, 16340 Alger, Algérie

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ABSTRACT

Context. Rotation significantly impacts on the structure and life of stars. In phases of high rotation velocity (close to critical), the photospheric structure can be highly modified, and present in particular geometrical deformation (rotation flattening) and latitudinal-dependent flux (gravity darkening). The fastest known rotators among the nondegenerate stars close to the main sequence, Be stars, are key targets for studying the effects of fast rotation on stellar photospheres.

Aims. We seek to determine the purely photospheric parameters of Achernar based on observations recorded during an emission-free phase (normal B phase).

Methods. Several recent works proved that optical/IR long-baseline interferometry is the only technique able to sufficiently spatially resolve and measure photospheric parameters of fast rotating stars. We thus analyzed ESO-VLTI (PIONIER and AMBER) interferometric observations of Achernar to measure its photospheric parameters by fitting our physical model CHARRON using a Markov chain Monte Carlo method. This analysis was also complemented by spectroscopic, polarimetric, and photometric observations to investigate the status of the circumstellar environment of Achernar during the VLTI observations and to cross-check our model-fitting results.

Results. Based on VLTI observations that partially resolve Achernar, we simultaneously measured five photospheric parameters of a Be star for the first time: equatorial radius (equatorial angular diameter), equatorial rotation velocity, polar inclination, position angle of the rotation axis projected on the sky, and the gravity darkening β coefficient (effective temperature distribution). The close circumstellar environment of Achernar was also investigated based on contemporaneous polarimetry, spectroscopy, and interferometry, including image reconstruction. This analysis did not reveal any important circumstellar contribution, so that Achernar was essentially in a normal B phase at least from mid-2009 to end-2012, and the model parameters derived in this work provide a fair description of its photosphere. Finally, because Achernar is the flattest interferometrically resolved fast rotator to-date, the measured β and flattening, combined with values from previous works, provide a crucial test for a recently proposed gravity darkening model. This model offers a promising explanation to the fact that the measured β parameter decreases with flattening and shows significantly lower values than the classical prediction of von Zeipel.

Key words. stars: rotation – stars: individual: Achernar – methods: observational – methods: numerical – techniques: interferometric – techniques: high angular resolution

1. Introduction

The rapidly rotating Be star Achernar (α Eridani, HD 10144) is a key target in stellar physics for a deeper understanding of

(1) the physical structure and evolution of fast rotators; and (2) the physical mechanism(s) connected with the Be phenomenon (e.g., episodic mass and angular momentum losses, disk formation and dissipation). It is thus crucial to determine a realistic model of Achernar's photosphere by measuring its main relevant physical parameters such as radius, rotation velocity,

[★] Based on observations performed at ESO, Chile under VLTI PIONIER and AMBER programme IDs 087.D-0150 and 084.D-0456.

temperature distribution (gravity darkening), mass, and inclination. Because it is the closest and brightest Be star in the sky, the photosphere of Achernar and its close vicinity can at least be partially resolved by modern high angular resolution instruments that can probe spatial scales ranging from ~ 1 to ~ 100 mas.

In particular, the ESO-Very Large Telescope Interferometer (VLTI; Hagenauer et al. 2010) instruments are well-adapted to this study. Observations performed in 2002 with the commissioning beam-combiner VLTI/VINCI revealed a strong apparent oblateness (rotational flattening) and suggested an extended structure that accounts for a few percent of the photospheric flux (Domiciano de Souza et al. 2003; Kervella & Domiciano de Souza 2006). This strong flattening could not be explained by the commonly adopted stellar rotation models, and two possibilities were proposed to account for it: differential rotation (Jackson et al. 2004), and a residual circumstellar disk (Carciofi et al. 2008). By studying the time variation of $H\alpha$ line profiles, Vinicius et al. (2006) showed that a weak but measurable emission (relative to a reference spectra) was detectable at the epoch of the VLTI/VINCI observations; this supports the hypothesis of a residual disk.

In addition, direct high angular resolution imaging revealed a faint, lower-mass binary companion to the Be star, at angular separations of ~ 50 – 300 mas (Kervella et al., in prep.; Kervella et al. 2008; Kervella & Domiciano de Souza 2007).

These works show that studying Achernar as a simple fast rotator to extract its photospheric parameters is a delicate task, since one has to consider its $B\leftrightarrow Be$ cycle as well as the possible influence of the binary companion. In this paper we seek to determine the purely photospheric parameters of Achernar based on a physical model of rapidly rotating stars and on VLTI observations recorded during a quiescent, emission-free phase (normal B phase).

The VLTI observations and data reduction are described in Sect. 2. In Sect. 3 we present a detailed investigation of the possible influence of a circumstellar disk and/or the binary companion on the interferometric observations. The adopted model and the photospheric parameters of Achernar measured from a model-fitting procedure are presented in Sects. 4 and 5. Deviations from the photospheric model and the photosphere vicinity of Achernar possibly revealed by the VLTI observations are investigated in Sect. 6, in particular using interferometric image reconstruction. Finally, the conclusions of this work are given in Sect. 7.

2. Interferometric observations and data reduction

2.1. VLTI/PIONIER

Near-infrared interferometric data of Achernar were obtained in 2011/Aug.-Sep. and 2012/Sep. with the PIONIER beam combiner (Le Bouquin et al. 2011) at the ESO-VLTI (Hagenauer et al. 2010). We used the largest quadruplet available with the Auxiliary Telescopes (AT) at that time (A1-G1-K0-I1) to resolve the stellar photosphere as much as possible. The resulting uv coverage is shown in Fig. 1. Depending on the night, the data were dispersed over three or seven spectral channels across the H band. Table 2 summarizes the log of observations.

The observations of Achernar were interspersed with interferometric calibrator stars to estimate the transfer function of the instrument. We selected these calibrators in the catalog by Cohen et al. (1999), adapted by Bordé et al. (2002), and in the JMMC Stellar Diameters Catalog¹ (JSDC, Lafrasse et al. 2010)

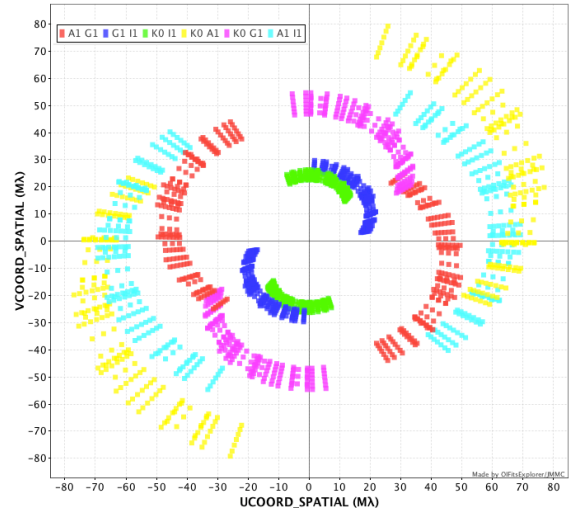


Fig. 1. uv coverage of VLTI/PIONIER observations of Achernar. The AT baselines used are identified with different colors. Image adapted from the OIFITSExplorer/JMMC tool.

using the SearchCal tool developed by the JMMC² (Bonneau et al. 2006). The main properties of the selected stars are listed in Table 1. We chose to use two types of calibrators: bright calibrators (HD 9362 and HD 12524) and fainter calibrators (HD 6793 and HD 187691). The bright calibrators provide a high photometric signal-to-noise ratio (S/N), and a very high precision on the calibration of the visibilities and closure phases. The fainter stars provide a cross-check of the adopted angular size of the bright calibrators and of their measured closure phases. Their small angular diameter results in a high fringe visibility ($V \approx 80\%$) and a very low systematic calibration uncertainty. We observed no deviation of the selected calibrators from central symmetry that might have been caused by binarity, for example.

Data were reduced and calibrated with the package `pndrs` (Le Bouquin et al. 2011). Each observation provides six squared visibilities V^2 and four closure phases CP. This dataset is available upon request in the standard OIFITS format.

2.2. VLTI/AMBER

Domiciano de Souza et al. (2012a) described and analyzed VLTI/AMBER HR differential phase observations of Achernar around the Bry line. The observations were recorded in 2009 (Oct. 25, Oct. 26, Oct. 30, and Nov. 1) with the high spectral resolution mode and using the FINITO fringe tracker. In this paper we reanalyze these AMBER differential phases together with the PIONIER data, since they were both taken during a diskless phase, as demonstrated in the next section.

3. Disk and companion status during the VLTI observations

The Be and binary nature of Achernar may imply temporal variabilities of observables with possible detectable spectro-interferometric signatures. It is thus important to determine which physical components should be included in the models to interpret VLTI observations from a given epoch. Indeed, Carciofi et al. (2008) showed that the presence of a residual circumstellar disk is a promising explanation of the strong flattening measured

¹ <http://cdsarc.u-strasbg.fr/viz-bin/Cat?II/300>

² <http://www.jmmc.fr/>

Table 1. Interferometric calibrators used for the PIONIER observations of Achernar.

Name	Sp. type	m_V	m_H	m_K	\mathcal{D}_{LD} (mas)	\mathcal{D}_{UD} (mas)	Ref. code
HD 6793	G5III	5.34	3.25	3.24	1.08 ± 0.08	1.06 ± 0.08	B06
HD 9362	K0IIIb	3.95	1.75	1.65	2.24 ± 0.02	2.17 ± 0.02	B02
HD 12524	K5III	5.16	1.69	1.52	2.77 ± 0.03	2.67 ± 0.03	B02
HD 187691	F8V	5.12	3.86	3.90	0.72 ± 0.05	0.70 ± 0.05	B06
HD 216956	A4V	1.16	1.05	1.05	2.22 ± 0.02	2.20 ± 0.03	A09
HD 14641	K5III	5.82	2.19	2.02	2.20 ± 0.03	2.12 ± 0.02	B02

Notes. *VHK* magnitudes are given, as well as limb-darkened (LD) and uniform-disk (UD) angular diameters. The references are B02: [Bordé et al. \(2002\)](#), B06: [Bonneau et al. \(2006\)](#), A09: [Absil et al. \(2009\)](#). The interferometric signature of fast-rotation and debris disk of HD 216956 is significantly below the observational uncertainties so that this star was used as a suitable calibrator.

Table 2. Log of VLTI/PIONIER observations of Achernar.

Date	Nb observations	Nb spec. channels
2011 Aug. 06	4	3
2011 Sep. 22	10	7
2011 Sep. 23	9	7
2012 Sep. 16	9	3
2012 Sep. 17	3	3

in the 2002 VLTI/VINCI observations ([Domiciano de Souza et al. 2003](#)). The presence of this residual disk is supported by a 2002 $H\alpha$ profile that shows a weak but measurable emission superposed on the stronger photospheric absorption ([Vinicius et al. 2006](#)).

Based on our observations of Achernar ([Kervella et al.](#), in prep.), the binary companion was located close to apastron (separation $\sim 200\text{--}300$ mas) during the PIONIER observations, which is outside the field of view of this instrument. These observations were performed at the VLT instruments NACO and VISIR and are based on several high angular resolution imaging techniques such as direct imaging, lucky imaging, adaptive optics, and aperture masking. Although the stellar photosphere is not resolved by these observations, they allow one to follow the time evolution of the binary system by resolving both components at different orbital phases.

Concerning the possible influence of a Be circumstellar disk, a more thorough analysis is required as described below.

3.1. Search for polarimetric and spectroscopic signatures of a Be circumstellar disk

To investigate the presence and strength of a possible circumstellar disk during the VLTI (PIONIER and AMBER) observations (Sect. 2), we analyzed contemporaneous broadband polarimetry (B and V) and hydrogen line profiles ($H\alpha$ and $H\beta$). These observations span from 2009 July to 2012 November.

Imaging polarimetry in the B and V bands was obtained using the IAGPOL polarimeter attached to the 0.6 m Boller & Chivens telescope at OPD/LNA³, Brazil. We used a CCD camera with a polarimetric module described by [Magalhães et al. \(1996\)](#), consisting of a rotating half-wave plate and a calcite prism placed in the telescope beam. A typical observation consists of 16 consecutive half-wave plate positions separated by 22.5° . In each observing run at least one polarized standard star HD 41117 or HD 187929 was observed to calibrate the observed position angle. Details of the data reduction can be found in

Table 3. Summary of broadband polarization data that are contemporaneous to the VLTI observations.

Date	Band	Polarization(%)
2009 Sep. 21	B	0.008 ± 0.011
2009 Nov. 18	B	0.014 ± 0.026
2011 Jun. 29	B	0.016 ± 0.038
2011 Sep. 2	B	0.014 ± 0.036
2011 Sep. 2	V	0.025 ± 0.015
2011 Sep. 9	B	0.027 ± 0.018
2011 Sep. 9	V	0.023 ± 0.017
2011 Sep. 29	B	0.008 ± 0.030
2011 Sep. 29	V	0.013 ± 0.018
2011 Oct. 19	B	0.026 ± 0.039
2011 Oct. 19	V	0.013 ± 0.016
2011 Nov. 3	V	0.015 ± 0.036
2012 Jul. 1	V	0.017 ± 0.015
2012 Nov. 21	V	0.035 ± 0.050

Notes. These data are plotted in Fig. 2.

[Magalhães et al. \(1984\)](#). A summary of our polarimetric data is presented in Table 3.

The IAGPOL data, shown in Fig. 2, exhibit values compatible with no intrinsic polarization, having a weighted average polarization of only $0.019 \pm 0.012\%$ during the observed period. This average is used in Sect. 3.2 as an upper limit to the polarization from a possible residual disk. This low polarization level contrasts with the measurements from a period of stellar activity in 2006, where the presence of circumstellar material lead to a polarization 10 times higher (up to 0.19% in B band), as shown by [Carciofi et al. \(2007\)](#). These authors also reported a clear spectroscopic signal with an $H\alpha$ emission-to-continuum (E/C) ratio of ~ 1.06 . The polarization values shown here also suggest no significant contribution from the interstellar medium to this quantity.

In addition to the polarimetric data, $H\alpha$ and $H\beta$ spectra of Achernar contemporaneous to the VLTI observations were also analyzed in search for possible signatures of a circumstellar disk. We obtained seven spectra at OPD/LNA, using the Cassegrain spectrograph (ECass) with 600 groove mm^{-1} grating blazed at 6563 \AA in first order, resulting in a reciprocal dispersion of $1.0 \text{ \AA pixel}^{-1}$. FEROS and HARPS spectra were also used to complement the OPD data. The spectroscopic observations are summarized in Table 4.

Following [Rivinius et al. \(2013\)](#), we adopted the FEROS spectra from early 2000 as a reference photospheric spectrum for Achernar. In Fig. 3 we plot the $H\alpha$ and $H\beta$ line profiles (top panels) and the difference profiles, computed as the difference between the observed profiles and the reference FEROS spectrum

³ Observatório Pico dos Dias/Laboratório Nacional de Astrofísica.

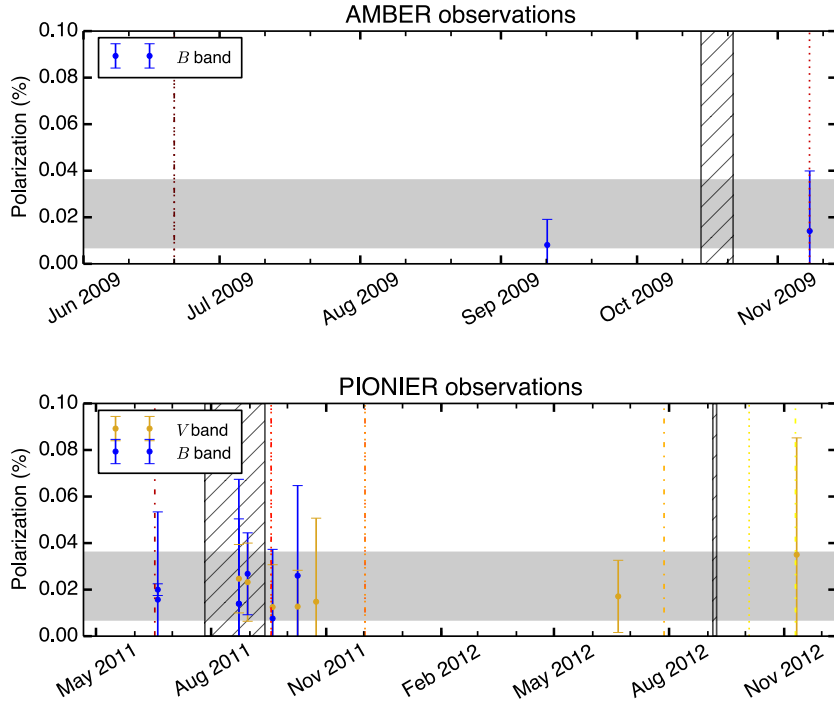


Fig. 2. Polarimetric observations at the epochs of ESO-VLTI AMBER and PIONIER data of Achernar analyzed in this work (vertical hatched bars). All the measurements are compatible with null/negligible polarization. The horizontal gray bars indicate the weighted average of the polarization: $0.019 \pm 0.012\%$. Vertical lines correspond to epochs of $H\alpha$ (dotted) and $H\beta$ (dot-dashed) data observations with colors corresponding to the spectra shown in Fig. 3. The spectroscopic and polarimetric data are thus contemporaneous and embrace the interferometric observations in time.

Table 4. Summary of spectroscopic data of Achernar that are contemporaneous to the VLTI observations.

Date	H line	Instrument	Min. Resolution
2000 Jan. 11	$H\alpha + H\beta$	ESO/FEROS	54 000
2009 Jul. 1	$H\alpha + H\beta$	ECass/OPD	3400
2009 Nov. 18	$H\beta$	ECass/OPD	3400
2011 Jun. 27	$H\alpha$	ECass/OPD	5400
2011 Sep. 28	$H\alpha + H\beta$	ECass/OPD	3400
2011 Dec. 12	$H\alpha + H\beta$	ESO/HARPS	109 000
2012 Aug. 7	$H\alpha$	ECass/OPD	5400
2012 Oct. 14	$H\beta$	ECass/OPD	3400
2012 Nov. 20	$H\alpha$	ECass/OPD	5400

Notes. The typical S/N ratio is 300. The $H\alpha$ and $H\beta$ spectra are shown in Fig. 3.

(bottom panels). All difference profiles are completely featureless, with difference values typically between -0.012 and 0.012 .

Thus, the polarimetric and spectroscopic data above suggest that the presence of a strong Be disk contemporaneous to the interferometric data can be discarded. In the following we quantify this assumption based on physical models of Be disks constrained by the observational limits imposed by the contemporaneous polarimetry (below $0.019 \pm 0.012\%$) and spectroscopy (disk signatures below 0.012 in absolute values relative to a photospheric profile).

3.2. Residual disk

We investigate here whether the presence of a weak residual disk that is hard to detect from non-angularly resolved observations could still affect the interferometric observations of

Achernar. This weak disk is constrained by the limits imposed by contemporaneous polarimetric and spectroscopic data determined in the previous section.

Using radiative transfer simulations from the HDUST code (Carciofi & Bjorkman 2006), we computed a grid of models based on our previous grid used to investigate the 2002 phase of Achernar (Carciofi et al. 2008): a large and dense disk in hydrostatic equilibrium (i.e., geometrically thin) and a smaller and more tenuous disk with enhanced scale height (i.e., geometrically thick). We adopted a power-law radial density profile,

$$\rho(r) = \rho_0 \left(\frac{R_{\text{eq}}}{r} \right)^m, \quad (1)$$

where R_{eq} is the stellar equatorial radius where the disk starts (inner disk radius), ρ_0 is the density of the disk at R_{eq} (density scale), and m is chosen as 3.5 corresponding to the steady-state regime of a viscous accretion disk (VDD) model (cf. Haubois et al. 2012, and references therein). To study the influence of the disk on the different observables we varied ρ_0 considering two sets of disk sizes R_d and scale heights H_0 at the inner disk radius. Table 5 details the parameters of these two sets of VDD models. In addition to these VDD models, we also used HDUST to compute a reference ellipsoidal photospheric model of Achernar compatible with the more physical photospheric model determined in Sect. 4.

The dependence of the polarimetric and spectroscopic observables on the density ρ_0 for the two VDD models are shown in Fig. 4, where the quantities predicted from the models are compared with our observational constraints. By comparing the modeled and observed limits determined in Sect. 3 for the polarization and difference $H\alpha$ spectra, we can set strict upper limits to ρ_0 : $\rho_0 < 0.52 \times 10^{-12} \text{ g cm}^{-3}$ (thin disk) and $\rho_0 < 0.65 \times 10^{-12} \text{ g cm}^{-3}$ (thick disk). As shown in Fig. 4, these limits are mainly imposed by the polarimetric data.

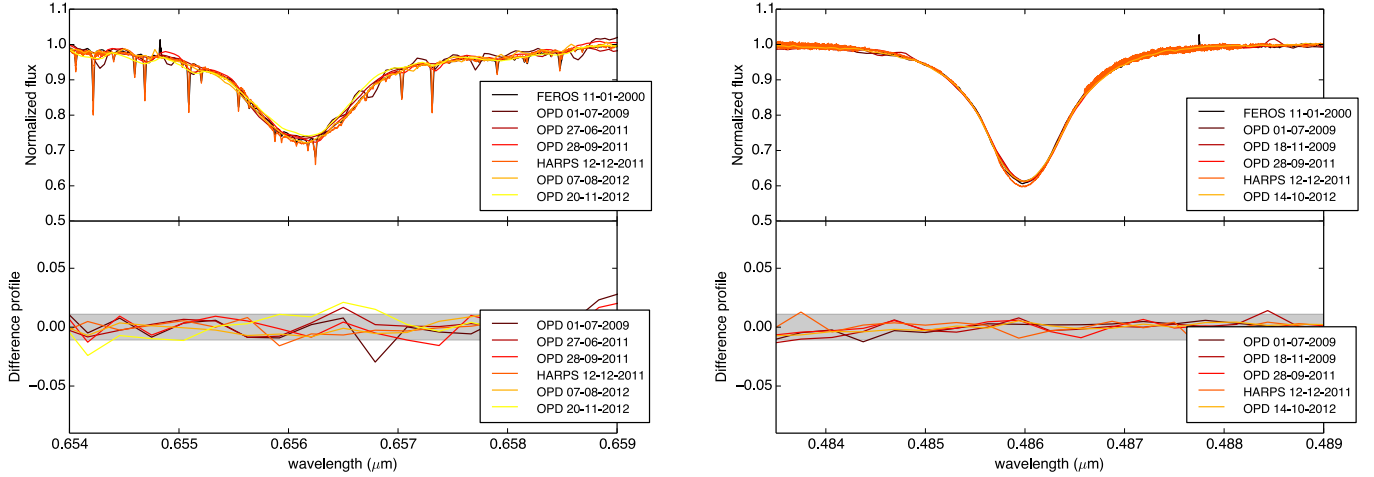


Fig. 3. *Top:* H α (*left*) and H β (*right*) line profiles of Achernar at the epoch of interferometric observations. *Bottom:* difference in flux of the line profiles with respect to the reference FEROS spectrum from 2000 Jan. 11. This spectrum can be considered as a good approximation to the pure photospheric profile of Achernar (Rivinius et al. 2013). Whenever possible (enough spectral resolution) the telluric lines seen in some spectra have been removed before computing the differences. The horizontal shaded (gray) areas indicate the typical error on the difference profiles and also set a limit to them.

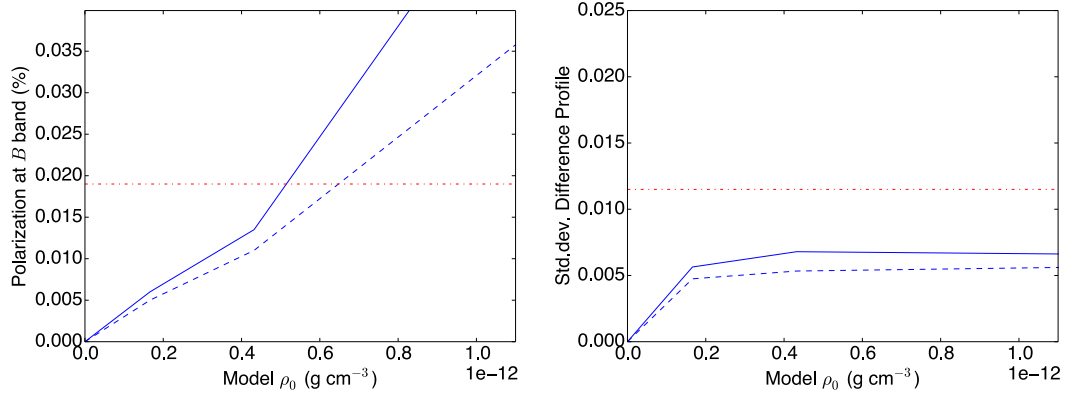


Fig. 4. Polarization in the B band (*left*) and standard deviation of difference H α profile (*right*) as a function of disk-base density ρ_0 for the residual disk models from Table 5 (model 1: full line; model 2: dashed line). The standard deviation is the root mean square of the disk model spectrum minus the pure photospheric profile. The horizontal dot-dashed lines represent the observational limits of average polarization and difference profile determined from observations performed at the epoch of interferometric observations, as explained in Sect. 3. While the measured H α difference profile level does not impose a limit to ρ_0 , the measured average polarization sets a strict upper limit to this quantity: $\rho_0 < 0.52 \times 10^{-12} \text{ g cm}^{-3}$ for the thin-disk model and $\rho_0 < 0.65 \times 10^{-12} \text{ g cm}^{-3}$ for the thick-disk model.

Table 5. Parameters of the two geometrical configurations of the residual VDD models.

Disk Model	ρ_0 range ($10^{-12} \text{ g cm}^{-3}$)	R_d (R_\odot)	H_0 (R_\odot)
1 (thin)	0.2–7.5	11.0	0.37
2 (thick)	0.2–7.5	10.1	0.73

Notes. The photospheric parameters are kept constant for the simulations. For a given density ρ_0 the total mass of the disk is the same for both models.

Figure 5 shows detailed a comparison of the VDD modeled H α line profiles for these two ρ_0 limits with the photospheric profile. As expected, the difference profiles have almost everywhere values within the ± 0.012 limit determined from the observed difference profiles (Sect. 3). Only at the wings of the H α profiles the VDD models present some weak signatures differing slightly from the pure photospheric profile. This detailed investigation of H α profiles combined with the results from Fig. 4

thus shows that the limits to ρ_0 imposed by polarimetry are also reliable upper limits to hydrogen spectral lines.

By adopting these limits to ρ_0 we now evaluate the signatures that a possible residual disk might have on our interferometric observations of Achernar. These evaluations are shown in Fig. 6, which compares the H band squared visibilities V^2 , and Br γ differential phases computed with the two VDD models (Table 5) with the expected values for the purely photospheric model. All deviations from the photospheric model are well within the typical observational errors on these interferometric quantities.

Therefore, in the following analysis we can safely rule out any effects of the known companion and of a significant residual disk around Achernar on our interferometric observations.

4. Achernar's photospheric parameters from VLTI observations

Based on the results from the previous section we adopted a model of a fast rotating, single B star without circumstellar

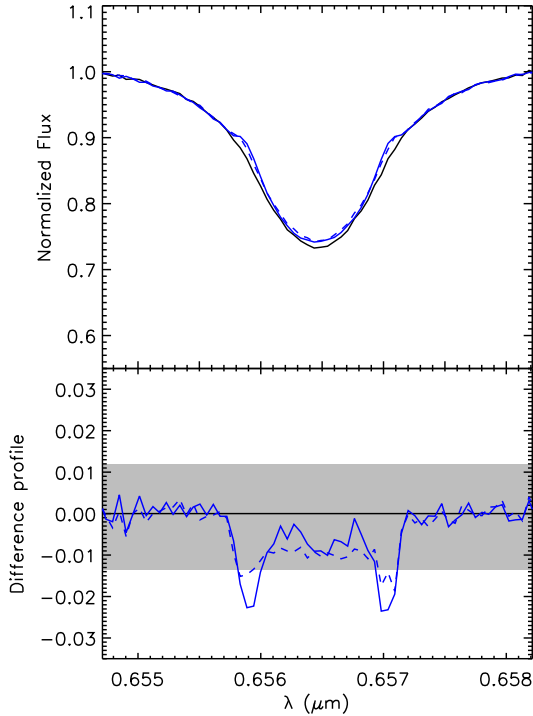


Fig. 5. *Top:* $H\alpha$ line profile for the pure photospheric model (black solid line) and with a residual disk (VDD model) as defined in Table 5 and computed for the upper limit values of ρ_0 (cf. Fig. 4): $0.52 \times 10^{-12} \text{ g cm}^{-3}$ (thin disk; blue solid line) and $0.65 \times 10^{-12} \text{ g cm}^{-3}$ (thick disk; blue dashed line). *Bottom:* the difference between the disk models relative to the photospheric model. The observational limit set to the difference profiles defined in Sect. 3 is indicated by the shaded (gray) region.

environment as a starting point to interpret the interferometric data of Achernar.

4.1. Photospheric model of fast-rotating stars

Most recent works describe the photospheric structure of rapidly rotating, nondegenerate, single stars of intermediate to high masses by adopting a Roche model (rigid rotation and mass concentrated in the stellar center) with a generalized form of the von Zeipel gravity darkening (von Zeipel 1924). We adopted this model since it has proven to well reproduce many distinct observables on rapid rotators (e.g., this work on Achernar and the cited references on other stars). Whether this is the only/best representation for their photospheres could be tested based on future and more precise observations.

Many codes exist that provide similar numerical implementations of this model, hereafter called the RVZ model. The reference numerical code for the RVZ model used here is the IDL-based program CHARRON (Code for High Angular Resolution of Rotating Objects in Nature). We present below a short description of CHARRON in the context of the present work. A more detailed description is given by Domiciano de Souza et al. (2012a,b, 2002).

The stellar photospheric shape follows Roche equipotential (gravitational plus centrifugal),

$$\Psi(\theta) = -\frac{GM}{R(\theta)} - \frac{\Omega^2 R^2(\theta) \sin^2 \theta}{2} = -\frac{GM}{R_{\text{eq}}} - \frac{V_{\text{eq}}^2}{2}, \quad (2)$$

where θ is the colatitude, M is the stellar mass, and R_{eq} and V_{eq} are the equatorial radius and rotation velocity. Solving this cubic equation provides the colatitude-dependent stellar radius $R(\theta)$.

Gravity darkening is considered by relating the local effective gravity $g_{\text{eff}}(\theta) (= |\nabla\Psi(\theta)|)$ to the local effective temperature $T_{\text{eff}}(\theta)$ by,

$$T_{\text{eff}}(\theta) = \left(\frac{C}{\sigma}\right)^{0.25} g_{\text{eff}}^{\beta}(\theta), \quad (3)$$

where σ is the Stefan-Boltzmann constant and β is the gravity-darkening coefficient, which is more general than the $\beta = 0.25$ value from von Zeipel (1924), but which is still assumed to be constant over the stellar surface. We note that for the spectral type of Achernar we can neglect any radiative acceleration effects since it is far from the Eddington limit. The proportionality constant C can be derived from stellar physical parameters such as mass and luminosity (e.g., Maeder & Meynet 2000) or related to a fixed point on the photosphere (the stellar pole, for example). In this work, the constant C and the stellar luminosity L are related to the average effective temperature \bar{T}_{eff} over the total stellar surface S_{\star} (area of the Roche photosphere),

$$L = \sigma \int T_{\text{eff}}^4(\theta) dS = \sigma \bar{T}_{\text{eff}}^4 S_{\star} = C \int g_{\text{eff}}^{4\beta}(\theta) dS. \quad (4)$$

\bar{T}_{eff} can be directly related to the bolometric flux F_{bol} and to the mean angular diameter $\overline{\mathcal{D}}$ (diameter of spherical star having a surface area S_{\star}) by,

$$F_{\text{bol}} = \sigma \bar{T}_{\text{eff}}^4 \frac{S_{\star}}{4\pi d^2} = \sigma \bar{T}_{\text{eff}}^4 \frac{\overline{\mathcal{D}}^2}{4}, \quad (5)$$

where d is the distance to the star.

In our numerical implementation of the RVZ model the stellar surface is divided into a predefined grid with nearly identical surface area elements (typically $\sim 50\,000$ surface elements). From $T_{\text{eff}}(\theta)$ and $g_{\text{eff}}(\theta)$ defined in the above equations, a local specific intensity from a plane-parallel atmosphere $I = I(g_{\text{eff}}, T_{\text{eff}}, \lambda, \mu)$ is associated with each surface element, where λ is the wavelength and μ is the cosine between the normal to the surface grid element and the line of sight (limb darkening is thus automatically included in the model). The local specific intensities I are interpolated from a grid of specific intensities that are pre-calculated using the spectral synthesis code SYNSPEC (Hubeny & Lanz 2011) and the ATLAS9 stellar atmosphere models (Kurucz 1979). For Achernar, we adopted atmosphere models with turbulent velocity of 2 km s^{-1} and solar abundance in agreement with its spectral type and short distance.

From the local specific intensities we obtained wavelength-dependent intensity maps of the visible stellar surface at the chosen spectral domain and resolution, such as the image given in Fig. 11. The interferometric observables (e.g., squared visibilities, closure phases, differential phases) are then directly obtained from the Fourier transform of these sky-projected photospheric intensity maps, which for a given star in the sky also depend on its rotation-axis inclination angle i and on the position angle of its sky-projected rotation axis PA_{rot} (counted from north to east until the visible stellar pole).

Thus, the main input parameters of the photospheric RVZ model for fast rotators used to interpret the interferometric observations of Achernar are M , R_{eq} , V_{eq} , β , \bar{T}_{eff} , i , PA_{rot} , and d .

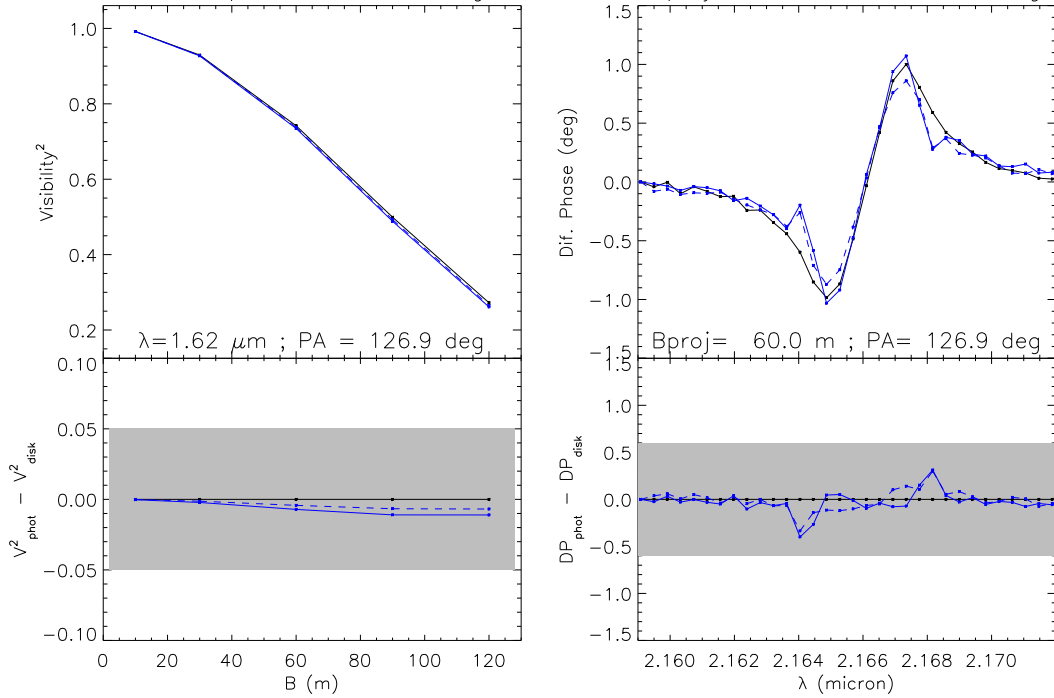


Fig. 6. Interferometric observables, squared visibilities V^2 in the H band (*left*), and $\text{Br}\gamma$ differential phases (*right*), computed for the pure photospheric model (black solid line) and for the two residual-disk models as defined in Table 5 at the upper limit values of ρ_0 (cf. Fig. 4): $0.52 \times 10^{-12} \text{ g cm}^{-3}$ (thin disk; blue solid line) and $0.65 \times 10^{-12} \text{ g cm}^{-3}$ (thick disk; blue dashed line). The baseline position angle PA was chosen to lie along the stellar equator (cf. Sect. 4.2), so that the effects of the residual disk are maximized on these comparisons. The baseline length for the differential phase calculations roughly corresponds to half of the maximum available length. *Bottom*: the difference between the interferometric observables from the disk models relative to the photospheric model. The shaded areas correspond to the typical observational errors from our PIONIER and AMBER observations. These difference plots show that the disk contribution to the interferometric observables is only a small fraction of the observation errors even at the upper limit ρ_0 , discarding any detectable influence of a circumstellar disk on the present interferometric observations of Achernar.

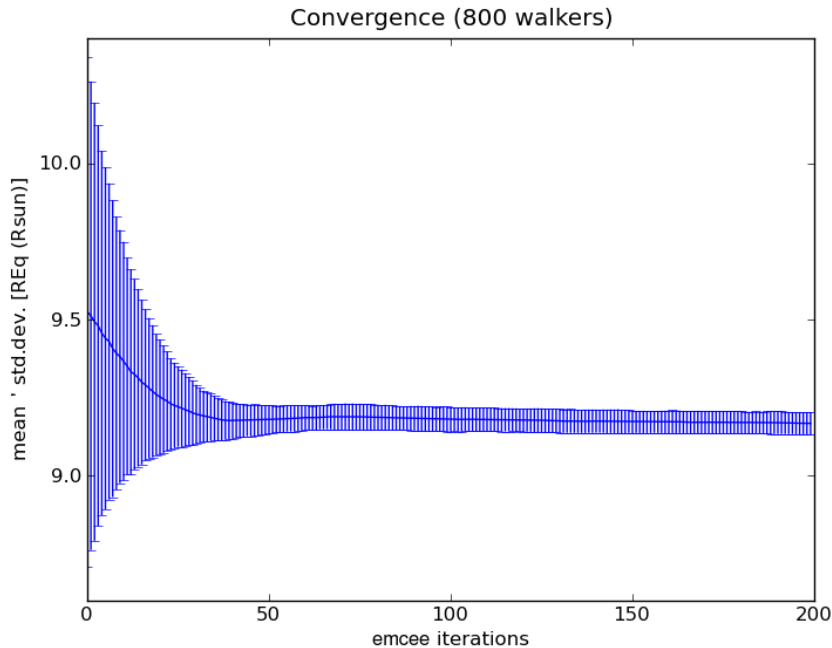


Fig. 7. Convergence of equatorial radius R_{eq} during the burn-in phase of the MCMC fit of the CHARRON RVZ model to the VLTI/PIONIER data using the emcee code (800 walkers and 200 iteration steps).

4.2. Fitting of the CHARRON model to VLTI/PIONIER data with an MCMC method

We used the CHARRON model to constrain several photospheric parameters of Achernar from the PIONIER observations (described in Sect. 2.1), which consists of a homogenous

data set obtained with the same beam-combiner instrument at ESO-VLTI. To be compatible with the observations, the CHARRON intensity maps were calculated over the H band with a spectral resolution of ~ 20 – 40 . We note that in broadband observations, the effect of bandwidth smearing (mixing of different spatial frequencies in a given wavelength bin) can lead to a

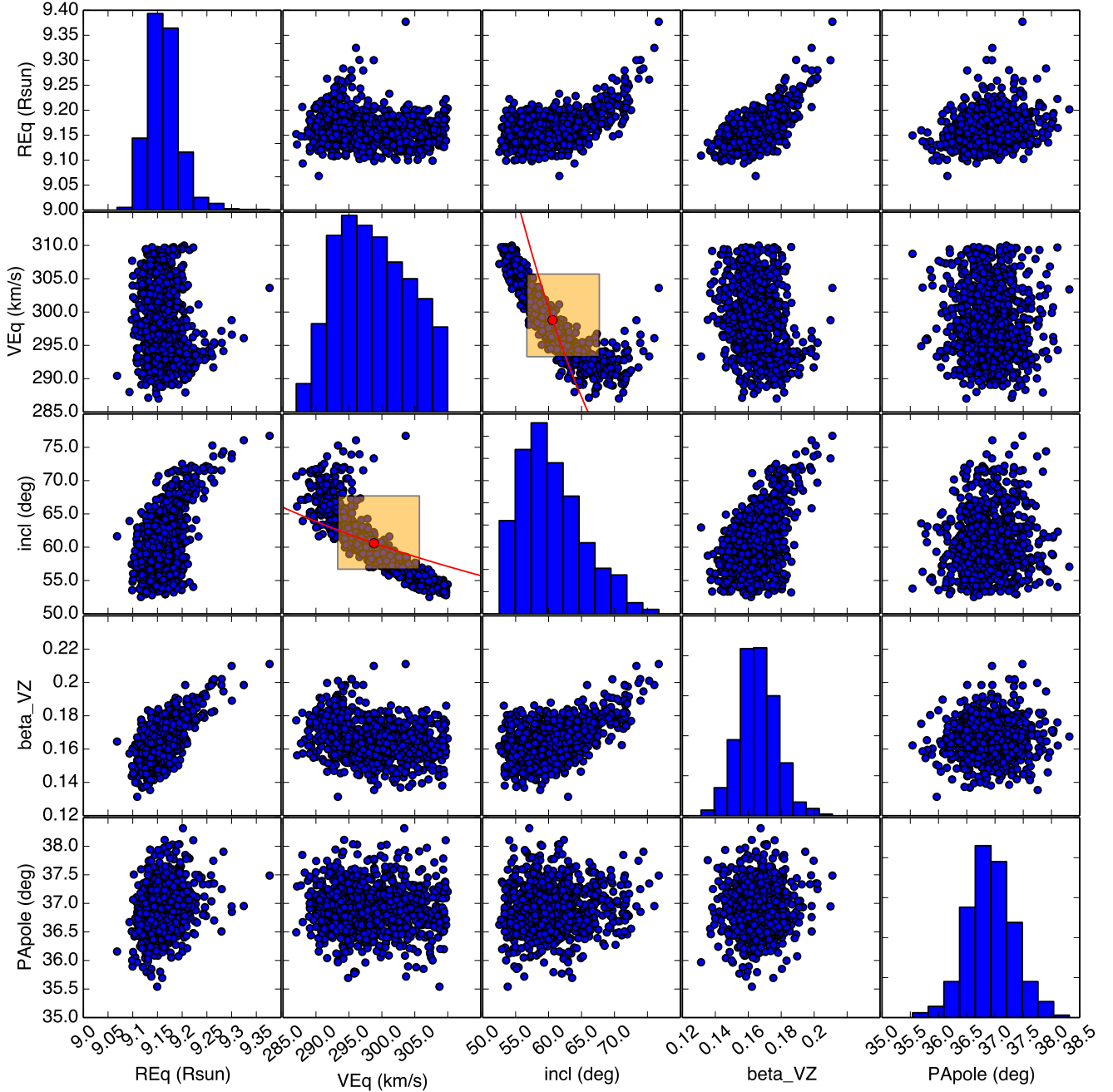


Fig. 8. Histogram distributions and two-by-two correlations for the free parameters (R_{eq} , V_{eq} , i , β , and PA_{rot}) of the best-fit CHARRON RVZ model determined with the emcee code (800 walkers). The mean values and associated uncertainties obtained from these histograms are given in Table 6. The parameters do not show strong correlations in the region defined by the uncertainty around the mean values. The stronger correlation is shown by V_{eq} and i , which roughly follow a curve of constant $V_{\text{eq}} \sin i$ ($=260.3 \text{ km s}^{-1}$), represented by the solid lines, with the circles indicating the mean values in the histograms. The rectangles cover the corresponding uncertainty ranges on V_{eq} and i .

decrease of visibility contrast and should in principle be considered. However, we checked that the bandwidth-smearing effect does not need to be considered in the present analysis because (1) the squared visibilities are higher than 0.3–0.4, which minimizes this effect (Kervella et al. 2003); and (2) the data span a few wavelength bins over the H band so that the range of spatial frequencies mixed is narrow. Based on results from previous works, M , \bar{T}_{eff} , and d were fixed to the following values:

- $M = 6.1 M_{\odot}$. Value from Harmanec (1988), previously adopted by Domiciano de Souza et al. (2012a). This mass also agrees (1) with the estimate from

Jerzykiewicz & Molenda-Zakowicz (2000) ($M = 6.22 \pm 0.16 M_{\odot}$) based on evolutionary tracks; and (2) with the mass estimate from an on-going work on Achernar’s binary system (Kervella et al., in prep.);

- $\bar{T}_{\text{eff}} = 15\,000 \text{ K}$. Value adopted by Domiciano de Souza et al. (2012a) following Vinicius et al. (2006). A critical discussion on this value and comparisons with other works are presented in Sect. 5;
- $d = 42.75 \text{ pc}$. We adopted the updated distance derived from the new reduction of the Hipparcos astrometric data and provided by van Leeuwen (2007).

Table 6. Physical parameters of Achernar derived from the fit of the RVZ model (CHARRON code) to VLTI/PIONIER H band data using the MCMC method (emcee code).

Free model parameters fitted	Values and uncertainties
Equatorial radius: $R_{\text{eq}} (R_{\odot})^a$	9.16 (+0.23; -0.23)
Equatorial rotation velocity: $V_{\text{eq}} (\text{km s}^{-1})$	298.8 (+6.9; -5.5)
Rotation-axis inclination angle: $i (^{\circ})$	60.6 (+7.1; -3.9)
Gravity-darkening coefficient: β	0.166 (+0.012; -0.010)
Position angle of the visible pole: $\text{PA}_{\text{rot}} (^{\circ})$	216.9 (+0.4; -0.4)
Derived parameters	Values
Equatorial angular diameter: $\mathcal{D}_{\text{eq}} = 2R_{\text{eq}}/d$ (mas)	1.99
Polar radius: $R_{\text{p}} (R_{\odot})$	6.78
$R_{\text{eq}}/R_{\text{p}}; \epsilon \equiv 1 - R_{\text{p}}/R_{\text{eq}}$	1.352; 0.260
Apparent flattening (major to minor axis ratio)	1.30
Mean angular diameter: $\overline{\mathcal{D}}$ (mas)	1.77
$V_{\text{eq}} \sin i$ (km s^{-1})	260.3
Critical rotation rate ^b : $V_{\text{eq}}/V_{\text{c}}; \Omega/\Omega_{\text{c}}$	0.883; 0.980
Keplerian rotation rate ^c : $V_{\text{eq}}/V_{\text{k}}; \Omega/\Omega_{\text{k}}$	0.838; 0.838
Polar temperature: T_{p} (K)	17 124
Equatorial temperature: T_{eq} (K)	12 673
Luminosity: $\log L/L_{\odot}$	3.480
Equatorial gravity: $\log g_{\text{eq}}$	2.772
Polar gravity: $\log g_{\text{p}}$	3.561
Rotation period: P_{rot} (h)	37.25
Rotation frequency: ν_{rot} (d^{-1})	0.644

Notes. Details of the fit are given in Sect. 4.2. ^(a) The uncertainty in the distance d from van Leeuwen (2007) was added quadratically to the fit uncertainty on R_{eq} . ^(b) Critical (Roche model) linear (V_{c}) and angular (Ω_{c}) velocities: $V_{\text{c}} = \Omega_{\text{c}} R_{\text{eq,c}} = \sqrt{GM/R_{\text{eq,c}}}$, with $R_{\text{eq,c}} = 1.5R_{\text{p}}$ (critical Roche equatorial radius). ^(c) Keplerian (orbital) linear (V_{k}) and angular (Ω_{k}) velocities: $V_{\text{k}} = \Omega_{\text{k}} R_{\text{eq}} = \sqrt{GM/R_{\text{eq}}}$.

The free parameters are thus R_{eq} , V_{eq} , i , β , and PA_{rot} .

The model-fitting was performed using the emcee code (Foreman-Mackey et al. 2013), which is a Python implementation of a Markov chain Monte Carlo (MCMC) method proposed by Goodman & Weare (2010). This code has been recently used by Monnier et al. (2012) to interpret interferometric observations.

From a given likelihood function of the parameters, emcee provides histograms of the free model parameters (samplings of the posterior probability) from which one can estimate the best parameter values and associate uncertainties. In the present work, the measurement errors on V^2 and CP are all assumed to be independent and normally distributed so that the likelihood function is proportional to $\exp(-\chi^2)$, where χ^2 has its usual definition and is composed of $\chi^2 = \chi_{V^2}^2 + \chi_{\text{CP}}^2$ (sum of χ^2 from the V^2 and CP data, respectively). To equally explore an homogenous range of initial values, we adopted initial uniform distributions for the five free CHARRON parameters that cover a wide range of physically consistent values.

The emcee algorithm explored the defined parameter space using 800 walkers in a 200 steps initial phase (burn-in) and 150 steps in the final phase, starting from the last state of the burn-in chain (for details of using the code see Foreman-Mackey et al. 2013). Convergence of the parameters distribution was typically attained within $\lesssim 100$ steps during the burn-in phase (an example for R_{eq} is shown in the electronically available Fig. 7).

The final histograms of the five free parameters and their two-by-two correlations are shown in Fig. 8 (available electronically). The best-fit values of the free parameters are the mean of these histograms. The uncertainties on the parameters were defined as corresponding to a range enclosing $\pm 34.15\%$ of the parameter distribution relative to the mean value (this corresponds to the commonly used rule for normal distributions). The

reduced χ^2 of the best-fit model is $\chi_r^2 = 1.9$ (for 1777 degrees of freedom DOF and free free parameters).

Table 6 summarizes the best-fit parameter values and uncertainties measured on Achernar from the MCMC fit of CHARRON RVZ model to the VLTI/PIONIER data. Other derived stellar parameters are also given in the table. The V^2 and CP corresponding to this best-fit model are plotted together with the observations in Figs. 9 and 10. The sky-projected intensity map of the visible stellar photosphere for this model is shown in Fig. 11.

As a completely independent check of the results above, we have also performed a Levenberg-Marquardt fit to the PIONIER data using a different RVZ model developed by one of us (A. Mérand). The best-fit parameter values obtained agree well (within the emcee error bars) with the values derived from the emcee fit of the CHARRON RVZ model.

5. Discussion

5.1. Radius and angular diameter

Long-baseline interferometry is traditionally known to deliver stellar angular diameters (and radii, if distances are available). These size measurements are directly dependent on the chosen photospheric model and on how fairly this model can represent the stellar photosphere. As shown in Sect. 4, the stellar radius is a function of the co-latitude for fast rotators, and the apparent stellar photosphere is dependent on additional parameters such as gravity darkening, effective temperature, rotation velocity, and polar inclination (discussed in the following subsections).

As explained in the previous sections, the equatorial radius R_{eq} determined here (or more generally the photospheric $R(\theta)$) is based on a physical model fitted to observations taken on a normal B phase of Achernar. As expected, the R_{eq} measured

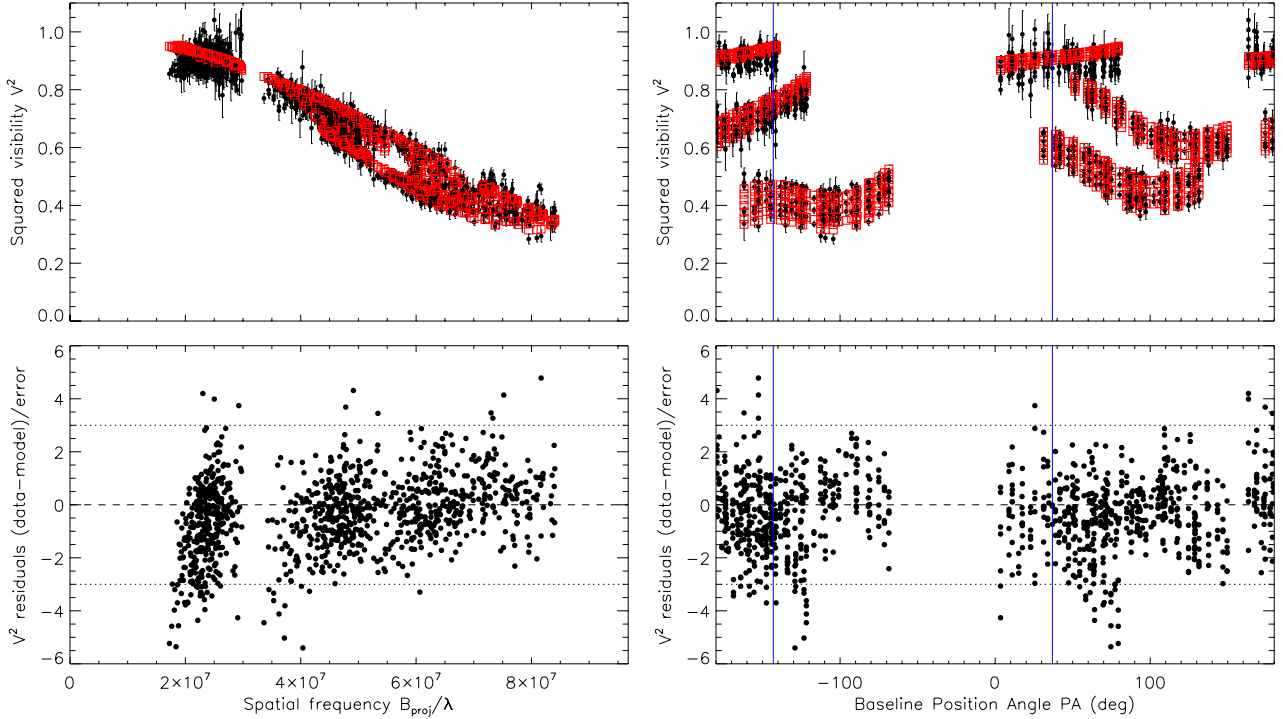


Fig. 9. *Top:* squared visibilities V^2 observed on Achernar (filled circles and error bars) and computed (opened squares) from the best-fit CHARRON model (Table 6) as a function of spatial frequency (*left column*) and baseline PA (*right column*). *Bottom:* V^2 residuals from observations relative to the best-fit model in units of corresponding uncertainties. Vertical solid lines indicate the position angles of the visible ($216.9^\circ \equiv -143.1^\circ$) and hidden ($16.9^\circ = 216.9^\circ - 180^\circ$) stellar poles. The horizontal dotted lines delimit the $\pm 3\sigma$ region around zero (dashed line).

in this work is smaller than the previous results derived from VLTI/VINCI observations, obtained in an epoch with a small, but non-negligible influence of a residual disk (Domiciano de Souza et al. 2003; Kervella & Domiciano de Souza 2006; Carciofi et al. 2008).

We discuss the stellar size derived from the VLTI/AMBER observations by Domiciano de Souza et al. (2012a), we postpone the discussion to Sect. 5.5, where we consider the whole set of model parameters.

Considering the stellar size derived from the VLTI/AMBER observations by Domiciano de Souza et al. (2012a) in Sect. 5.5, where we consider the whole set of model parameters.

5.2. Photometry and effective temperature

The photometric magnitudes in the *UBVJHK* bands and the bolometric flux derived from the CHARRON best-fit model are compared with measurements reported in the literature in Table 7. We first note from the table that these observed magnitudes and bolometric fluxes show uncertainties and/or a dispersion of measured values of about 10%–20%, which are at least partially caused by a combination of instrumental and intrinsic effects from the star. Indeed, Achernar is known to present multiple flux variabilities at time scales from hours to years, which are caused, for example, by pulsations (Goss et al. 2011), binarity (Kervella & Domiciano de Souza 2007), and the $B\zeta$ Be cycle (e.g., Vinicius et al. 2006). Thus, the observed magnitudes and bolometric flux should not be considered as tight constraints to the model-fitting, although they provide an important consistency check on the best-fit model parameters. Indeed, the modeled magnitudes and bolometric flux given in Table 7 agree with the observations within their uncertainties and/or dispersion of measured values.

By using Eq. (5) we can cross-check the consistency between the adopted mean effective temperature \bar{T}_{eff} , the measured bolometric flux F_{bol} , and the mean angular diameter $\bar{\theta}$ reported in Tables 6 and 7. From the F_{bol} provided by Code et al. (1976) and Nazé (2009) one thus obtains $\bar{T}_{\text{eff}} = 15\,094$ K and $14\,703$ K. We note that the temperature of $14\,510$ K estimated by Code et al. (1976) is somewhat lower than the value estimated here because they considered the higher angular diameter (1.92 mas) reported by Hanbury Brown et al. (1974), based on intensity interferometry observations at the Narrabri Observatory. As expected, this diameter is between the major and minor diameters derived in the present work. However, the measurements from Hanbury Brown did not allow taking into account the angular size variation with the baseline position angle caused by the rotational flattening of Achernar. Thus, recalling that the average effective temperature of $\approx 15\,000$ K reported by Vinicius et al. (2006) was derived from different methods, the adopted $\bar{T}_{\text{eff}} = 15\,000$ K agrees well with several independent measurements (bolometric fluxes, photometry, spectroscopy, and interferometry).

5.3. Inclination and rotation velocity

The inclination angle $i (=60.6_{-3.9}^{+7.1})$ measured in this work is compatible (within $\approx 1.5\sigma$) with the values ($i \sim 65\text{--}70^\circ$) estimated by Vinicius et al. (2006) and Carciofi et al. (2007).

Different values have been previously reported on the projected rotation velocity $V_{\text{eq}} \sin i$ of Achernar, with mainly three distinct range of values: $V_{\text{eq}} \sin i \sim 223\text{--}235$ km s $^{-1}$ (e.g., Slettebak 1982; Chauville et al. 2001; Vinicius et al. 2006), $V_{\text{eq}} \sin i = 292 \pm 10$ km s $^{-1}$ (Domiciano de Souza et al. 2012a), and $V_{\text{eq}} \sin i \sim 410$ km s $^{-1}$ (e.g., Hutchings & Stoeckley 1977; Jaschek & Egret 1982).

Table 7. Observed and modeled *UBVJHK* photometry and bolometric flux F_{bol} of Achernar.

Catalogue or reference	<i>U</i>	<i>B</i>	<i>V</i>	<i>J</i>	<i>H</i>	<i>K</i>	F_{bol} (10^{-9} W m $^{-2}$)
2MASS ^a				0.815 ± 0.254	0.865 ± 0.320	0.880 ± 0.330	
NOMAD Tycho-2 ^b		0.473	0.527				
Johnson et al. (1966)		0.32	0.47				
Code et al. (1976)							54.4 ± 4.3
Jaschek & Egret (1982)	-0.36	0.30	0.46				
Nazé (2009)							48.98
CHARRON RVZ model	-0.279	0.339	0.472	0.783	0.828	0.886	53.05
Model in 2012 paper	-0.387	0.215	0.333	0.596	0.631	0.684	62.90

Notes. The model values are based on the parameters given in Table 6 for the best emcee fit of CHARRON RVZ model to PIONIER data. For comparison, we also show the values derived from the model given by Domiciano de Souza et al. (2012a), based on the AMBER differential phases. ^(a) Cutri et al. (2003); Skrutskie et al. (2006). ^(b) Hog et al. (2000); Zacharias et al. (2005).

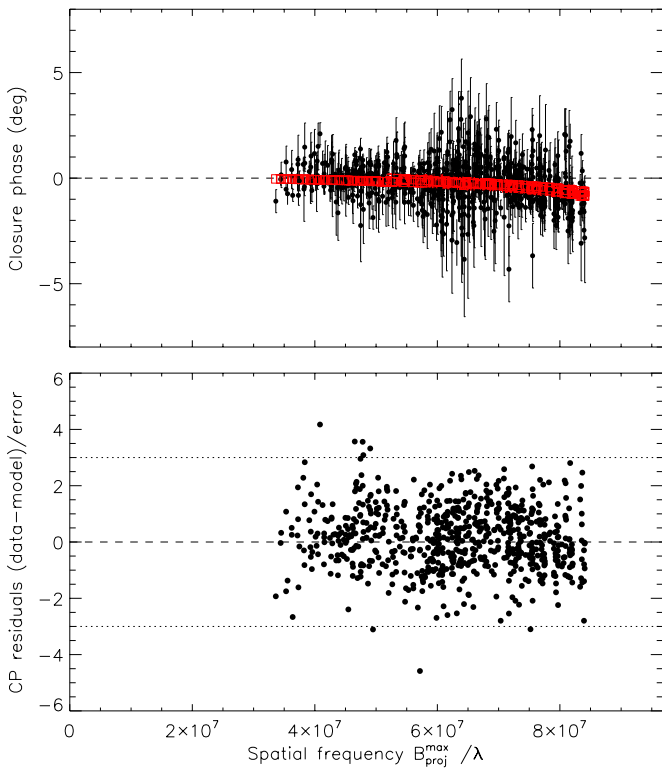


Fig. 10. *Top:* closure phases (CP) observed on Achernar and computed from the best-fit CHARRON model (Table 6) as a function of the spatial frequency (for the longest projected baseline $B_{\text{proj}}^{\text{max}}$ in the corresponding triangle configuration). *Bottom:* CP residuals from observations relative to the best-fit model in units of corresponding uncertainties. The horizontal dotted lines delimit the $\pm 3\sigma$ region around zero (dashed line). Since the photosphere is only partially resolved, the CP signatures of fast rotation are weak (within $\sim \pm 1^\circ$).

In this work we determine $V_{\text{eq}} \sin i = 260.3_{-12}^{+19}$ km s $^{-1}$, where these uncertainties were computed by properly adding the individual uncertainties estimated on i and V_{eq} (cf. Table 6 and Fig. 8). This estimated $V_{\text{eq}} \sin i$ lies between the lower and intermediate values found in the literature, as mentioned above, and it is compatible with them within 2σ to 3σ , i.e., $\approx 30\text{--}40$ km s $^{-1}$.

Some clues for explaining the discrepancies in the measured $V_{\text{eq}} \sin i$ may be given by the fact that different methods for estimating this quantity can lead to different results depending on their sensitivity to the nonuniform photospheric intensity distribution caused by the gravity darkening. For example, it is

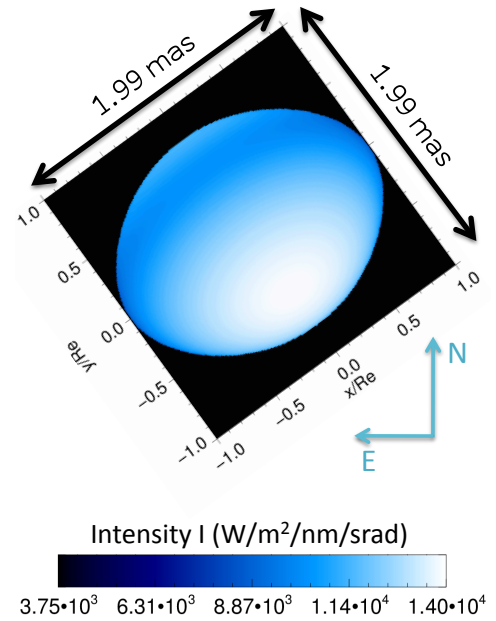


Fig. 11. Intensity map of Achernar corresponding to the best-fit of the CHARRON RVZ model to the VLTI/PIONIER *H* band observations. The spatial coordinates indicated in angular milliarcseconds (mas) units and also normalized to the equatorial radius $R_{\text{eq}} = 9.16 R_{\odot}$. The complete list of the measured stellar parameters is given in Table 6.

known that because of gravity darkening, the $V_{\text{eq}} \sin i$ obtained from visible/IR spectroscopy are generally underestimated in fast-rotating stars (Townsend et al. 2004; Frémat et al. 2005). Moreover, the actual $V_{\text{eq}} \sin i$ of Achernar seems to significantly vary in time, as recently shown by Rivinius et al. (2013), who reported $V_{\text{eq}} \sin i$ variations with amplitudes $\lesssim 35$ km s $^{-1}$ that are correlated to the B \rightarrow Be phase transitions. Interestingly, this amplitude of $V_{\text{eq}} \sin i$ variations is on the same order of the differences between the $V_{\text{eq}} \sin i$ values measured in this work and those reported by several other authors, as discussed above.

Finally, Goss et al. (2011) identified a low-amplitude frequency of 0.68037 ± 0.00003 d $^{-1}$ from time-series analysis of photometric light-curves of Achernar. We note that this frequency is relatively close (but still $\sim 2.5\sigma$ above) to the rotation frequency $\nu_{\text{rot}} = 0.644 \pm 0.015$ d $^{-1}$ derived in the present work (uncertainty estimated by properly adding quadratically the relative maximum individual uncertainties on R_{eq} and V_{eq}). Whether or not the measured frequency is related to the rotation of Achernar remains to be further investigated.

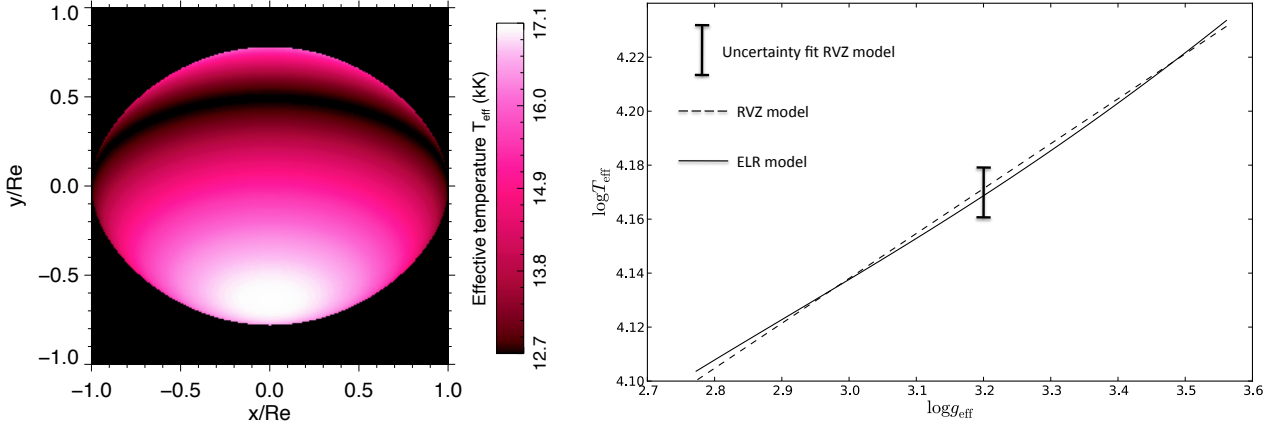


Fig. 12. *Left:* effective temperature map of Achernar corresponding to the best-fit of the CHARRON RVZ model to the VLTI/PIONIER H band observations (model parameters in Table 6). The spatial coordinates are normalized to the measured equatorial radius $R_{\text{eq}} = 9.16 R_{\odot}$. The polar and equatorial effective temperatures of Achernar are $T_{\text{p}} = 17\,124$ K (white) and $T_{\text{eq}} = 12\,673$ K (black). *Right:* $\log T_{\text{eff}}$ as a function of $\log g_{\text{eff}}$ of Achernar for the ELR model (solid line from Espinosa Lara & Rieutord 2011). The calculations were performed considering a Roche model with the same stellar parameters as in Table 6, except for the gravity darkening, which is directly obtained from the ELR model. The dashed straight line shows the $\log T_{\text{eff}}$ versus $\log g_{\text{eff}}$ corresponding to the best-fit RVZ model with the measured gravity-darkening coefficient $\beta (=0.166^{+0.012}_{-0.010})$. The vertical bar indicates the uncertainty in T_{eff} associated with the measured uncertainty in this best-fit β value alone. We also note that by fitting a straight line to the ELR model (solid curve) results in an identical $\beta (=0.166)$ as measured with the CHARRON RVZ model, which exactly matches the dashed straight line. Thus, although the ELR model predicts a slightly more complex gravity-darkening relation than the RVZ model (Eq. (3)), these two gravity-darkening models agree within the uncertainties derived from the RVZ model fit to the PIONIER observations.

5.4. Gravity darkening

The gravity-darkening parameter β determined in this work is significantly lower than the von Zeipel law ($\beta = 0.25$), a result in agreement with β values derived from recent interferometric observations of fast-rotating stars (see for example the recent review from van Belle 2012, and references therein).

These low β (<0.25) were explained theoretically by Espinosa Lara & Rieutord (2011), who derived an alternative gravity-darkening law (ELR model hereafter) by relaxing the assumption of barotropicity that leads to the von Zeipel law. The ELR model includes a divergence-free flux vector and the ratio $T_{\text{eff}}^4/g_{\text{eff}}$ is allowed to vary with latitude, leading to an analytical relation between T_{eff} and g_{eff} without the need of assuming a constant β parameter as in Eq. (3). Let us compare in more detail the gravity darkening derived from the best-fit of the CHARRON RVZ model with the prediction from the ELR model. Both models adopt the Roche approximation so that they consider an identical photospheric shape $R(\theta)$. Based on the best-fit parameters in Table 6, Fig. 12 compares the $\log T_{\text{eff}}$ versus $\log g_{\text{eff}}$ relations for the two gravity darkening models. The T_{eff} map of the RVZ model is also illustrated in Fig. 12. As shown in the figure, the two models agree within the parameter uncertainties, but the present observation errors do not yet allow us to probe the small differences in $T_{\text{eff}}(\theta)$ predicted by the models.

Although the detailed $T_{\text{eff}}(\theta)$ cannot be investigated, it is clear that the ELR model reproduces an average $T_{\text{eff}}(\theta)$ dependence that is totally compatible with measurements from the RVZ model, but without the need of using a β parameter. Indeed, by estimating an equivalent β value (e.g., from $\log(T_{\text{eq}}/T_{\text{p}})/\log(g_{\text{eq}}/g_{\text{p}})$), Espinosa Lara & Rieutord (2011, in their Fig. 4) showed a good agreement between their predictions and the β coefficients measured on four fast rotators as a function of flattening ϵ ($\equiv 1 - R_{\text{p}}/R_{\text{eq}}$).

In Fig. 13 we extend this comparison by adding α Lyr (Vega; Monnier et al. 2012) and Achernar (α Eri; present work). These two new stars provide a crucial test for the ELR model since they have, respectively, the lowest and highest flattening in the

sample. Figure 13 thus compares β and ϵ from the ELR model with values measured on six fast rotators (listed from hotter to colder spectral types): α Eri (Achernar, B3-6Vpe; this work), α Leo (Regulus, B8IVn; Che et al. 2011), α Lyr (Vega, A0V; Monnier et al. 2012), α Aql (Altair, A7IV-V; Monnier et al. 2007), α Cep (Alderamin, A7IV; Zhao et al. 2009), β Cas (Caph, F2IV; Che et al. 2011).

Five out of the six stars agree relatively well with the ELR model (in particular Altair and Achernar), considering the observational uncertainties. The only exception is β Cas, and a more detailed study would be required to decide if the discrepancy is due to a bias in the measured flattening related to its low inclination (as discussed by Espinosa Lara & Rieutord 2011) and/or maybe related to the fact that this is star is the coldest one in the sample. This agreement between observational and theoretical results is therefore a promising perspective for a more profound understanding of the gravity-darkening effect in rotating stars.

Based on the curve β versus flattening ϵ given in Fig. 13 and derived from the ELR model, we can deduce a linear relation that roughly follows this curve:

$$\beta \approx 0.25 - 0.328\epsilon. \quad (6)$$

This linear approximation reproduces the curve in Fig. 13 within 1% (3%) for $\epsilon \lesssim 0.27$ (0.30). We recall, however, that the use of a β parameter is neither required nor compatible with the ELR model, which does not describe the gravity darkening by a power law as in Eq. (3).

5.5. Comparison with the VLTI/AMBER differential phases

We now compare the best-fit CHARRON model determined from the PIONIER data (Table 6) with the AMBER differential phases, described in Sect. 2.2 and by Domiciano de Souza et al. (2012a). The differential phases computed directly from the PIONIER best-fit model already well reproduce the AMBER observations, resulting in $\chi_{\text{r}}^2 = 1.3$ (DOF = 3808). This χ_{r} is only slightly higher than the 1.2 value found by Domiciano de Souza et al. (2012a) from the same model, but

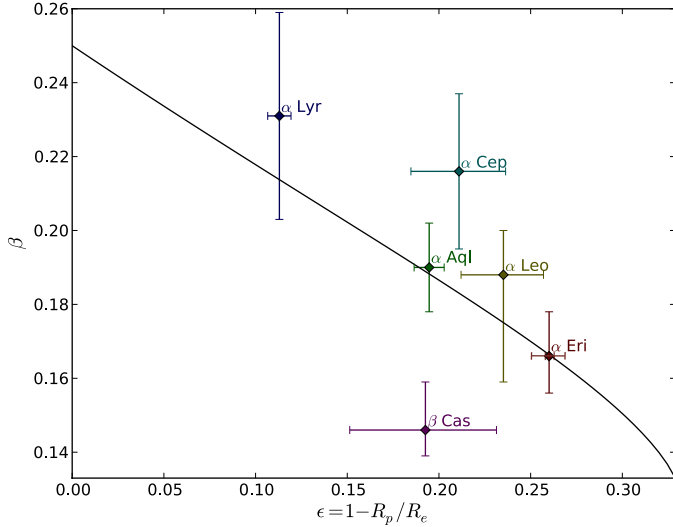


Fig. 13. Gravity-darkening coefficient β estimated from the ELR model (Espinosa Lara & Rieutord 2011) as a function of the rotation flattening ϵ compared with values measured from interferometric observations of six rapidly rotating stars (references in Sect. 5.4, Achernar (α Eri) being the flattest one). The estimate of β is obtained from a fit to the $\log T_{\text{eff}}$ versus $\log g_{\text{eff}}$ curves directly predicted by the ELR model, such as in Fig. 12 (right). The ELR model predictions and interferometric measurements have a good general agreement (see Sect. 5.4 for a more detailed discussion).

with a somewhat different set of parameters. Indeed, for all AMBER baselines and wavelengths considered, the absolute differences between both sets of modeled differential phases are smaller than 0.5° , which is lower than the typical uncertainties in the differential phases for these AMBER observations (median value of 0.6°).

Conversely, the photospheric model parameters derived from the AMBER differential phases (Domiciano de Souza et al. 2012a) are far from reproducing the PIONIER observations, resulting in a 10 times higher χ_r^2 ($=19.2$). Moreover, compared to the best-fit model determined in this work, the model from Domiciano de Souza et al. (2012a) presents a worse agreement with the photometric observations as shown in Table 7 (brighter star in particular because of the higher β and size). Thus, the CHARRON RVZ photospheric model with parameters as in Table 6 provides the best general agreement with the whole set of polarimetric, spectroscopic, photometric, and interferometric (PIONIER and AMBER) observations of Achernar considered in this work.

6. Beyond the photospheric model ?

We have shown in Sect. 3 that the interferometric data analyzed in this work are not influenced by a strong circumstellar disk or by the known binary companion. This conclusion agrees with the good quality of the fit obtained by adopting a single photospheric fast rotator RVZ model in Sect. 4. In spite of this satisfactory result, and relying on the relatively high-precision PIONIER data, we take the analysis a step farther to search for possible more subtle components in the close environment of Achernar and/or indications of small deviations from the adopted fast-rotator RVZ model. To this aim, two complementary approaches were adopted: (1) model-fitting of the RVZ model plus an additional analytical component; and (2) image reconstruction.

6.1. Photospheric physical model plus analytical component

We used the emcee code to fit a model consisting of the photospheric best-fit RVZ model determined in Sect. 4 plus an analytical 2D Gaussian ellipse. The free parameters of the 2D Gaussian ellipse and their initial range of values (initial uniform distribution of values) are

- major axis *FWHM* a_{GE} : 0.5 mas to 20 mas
- minor-to-major-axis ratio r_{GE} : 0.1 to 1
- position angle of the major axis PA_{GE} : 0° to 180°
- flux ratio (relative to the stellar total flux) F_{GE} : 0% to 10%
- horizontal (equatorial direction) shift relative to the center of the star x_{GE} : -15 mas to 15 mas
- vertical (polar direction) shift relative to the center of the star y_{GE} : -15 mas to 15 mas.

This approach is similar to, but more general than, the one adopted by Kervella & Domiciano de Souza (2006) since it allows to simultaneously test different faint circumstellar structures such as a faint companion or a weak polar wind or equatorial disk.

As before, the emcee algorithm explored the entire parameter space (within the above defined boundaries) using 800 walkers in a 200 steps burn-in phase and 150 steps in the final phase. Since the RVZ model already provides a good fit to the data, the parameters of the additional 2D Gaussian ellipse are not expected to be strongly constrained, leading to $\chi_r^2 = 1.79$, which is only slightly lower than the value obtained for the RVZ model alone. Two parameters of the 2D Gaussian ellipse were nevertheless relatively well constrained: $a_{\text{GE}} = 5.2 \pm 2.4$ mas and $F_{\text{GE}} = 0.7\% \pm 0.1\%$. The fit also shows that the position of this possible additional component is roughly centered on the star, with a shift uncertainty smaller than ~ 5 mas for both directions (x_{GE} and y_{GE}). The remaining parameters are poorly constrained by the data.

6.2. Image reconstruction

As a model-independent study of the PIONIER data we also performed an image reconstruction of Achernar using the MIRA⁴ software (Thiébaut 2008). MIRA is based on an iterative process, aimed at finding the image that minimizes a joint criterion under constraints of positivity and normalization,

$$f(x) = f_{\text{data}}(x) + \mu f_{\text{prior}}(x), \quad (7)$$

where x are the set of image pixels, $f_{\text{data}}(x)$ is the penalty function of the measurements, $f_{\text{prior}}(x)$ is a term that enforces additional a priori constraints, and μ (≥ 0) is the hyperparameter, i.e., the weight of the priors.

The hyperparameter has to be chosen as large as possible to maximize the weight of the constraints arising from physical modeling and to ensure the convergence of the reconstruction at a minimal value of the penalty χ^2 . As we have satisfying a model of the target, we used an elliptical Lorentzian a priori ($f_{\text{prior}}(x)$) with (1) the same minor-axis position angle as Achernar, 216.9° ($\equiv 36.9^\circ$ for a centrallysymmetrical ellipse); (2) a major-to-minor axis ratio of 1.3 corresponding to the apparent flattening; and (3) a *FWHM* = 3.2 mas in the major-axis direction, corresponding to a size slightly bigger than Achernar's angular diameter, to avoid missing possible structures close to the photosphere.

To determine the best value of the hyperparameter, we performed several ($\sim 10^3$) independent reconstructions with 200 iterations and random μ values ranging from 1 to 10^9 . In Fig. 14

⁴ Multi-aperture image reconstruction algorithm.

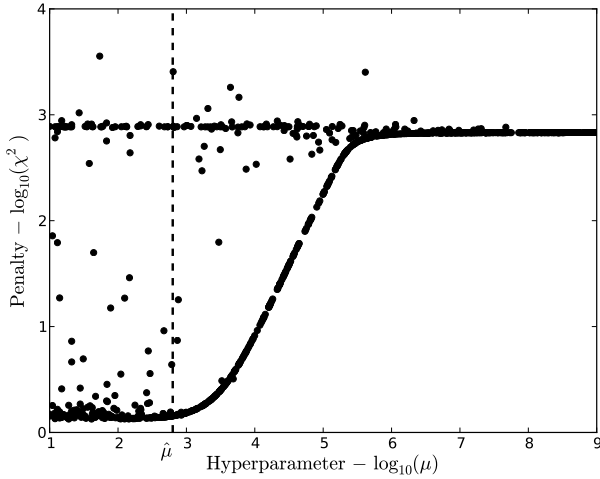


Fig. 14. Penalty factor χ^2 as a function of the hyperparameter μ for a set of reconstructed MIRA images (log scales). Based on this curve, the value $\hat{\mu}$ ($=630$) was chosen for the image reconstruction of Achernar.

(available electronically), we show the distribution of χ^2 for converged reconstructions as a function of μ for each reconstruction. This procedure revealed that there is a plateau of minimum χ^2 ($=1.4$), reached for values of μ lower than $\hat{\mu} \sim 630$.

After determining the parameters of the reconstruction, we followed the procedure described by Millour et al. (2012) to create the reconstructed image of Achernar as the weighted average of several hundred converged reconstructed images,

$$\bar{I}(x) = \frac{\sum_i 1/\chi_i^2 I_i(x - \bar{x}_i)}{\sum_i 1/\chi_i^2}, \quad (8)$$

where each image i was centered on its photocenter position \bar{x}_i before summation. The weight of each reconstruction is $1/\chi_i^2$, with a limit penalty value of $\chi_i^2 \leq 5$ to reject low-quality reconstructed images.

Figure 15 shows the reconstructed image of Achernar, both given by MIRA with a 0.07 mas resolution pixel (over-resolved image) and convolved by a Gaussian beam of $FWHM = 1.6$ mas (diffraction limit of the PIONIER observations). Although this diffraction limit does not provide a highly resolved image of the photosphere, it is enough to investigate the close circumstellar environment. Indeed, the reconstructed MIRA image clearly shows the presence of a compact object (stellar photosphere) without any signature of extended circumstellar component. This is more clearly seen in the right panel of Fig. 15, which shows the subtraction of the MIRA and best-fit CHARRON images, convolved by the 1.6 mas Gaussian beam. The difference between these images is at most 1.5% in modulus (relative to the total flux of the MIRA image) and below $\sim 0.5\%$ almost everywhere.

Both the results from the image reconstruction and from the fit of the RVZ model plus an analytical 2D Gaussian ellipse presented in this section show that no additional component is present in the PIONIER data within $\sim \pm 1\%$ level of intensity. This agrees well with the conclusions based on polarimetric and spectroscopic data and modeling shown in Sect. 3.

7. Conclusions

Based on ESO-VLTI interferometric observations of Achernar obtained in a normal B star phase, we derived its photospheric

parameters by fitting our physical model CHARRON using a MCMC method. A best-fit photospheric model was derived from squared visibilities and phase closures recorded with the PIONIER beam combiner in the H band. This model agrees well with AMBER HR differential phase observations around the Bry line.

The interferometric observations were complemented by spectroscopic, polarimetric, and photometric data to investigate the status of the circumstellar environment of Achernar during the VLTI observing runs, to cross-check our model-fitting results, and to set constraints on the model parameter space (photosphere and possible residual disk). In particular, polarimetry was crucial to constrain the disk density, imposing quite well-defined upper limits.

We note that our photospheric model of Achernar agrees with many observations from distinct techniques: PIONIER V^2 and CP, AMBER differential phases, V - and B -band polarimetry, $H\alpha$ and $H\beta$ line profiles, and $UBJHK$ photometry. Moreover, our results are compatible with the theoretical model of gravity darkening proposed by Espinosa Lara & Rieutord (2011, ELR model), which we also showed to be consistent with previously published results from different fast rotators over a wide range of rotational flattening (Achernar being the flattest one in the sample). Observational validation of gravity-darkening models such as the ELR model is an important step in the understanding of rapidly rotating stars since it has the great advantage of reducing the number of free parameters (β coefficient is not needed anymore). Indeed, by relying on a few input parameters and hypotheses, the ELR model reproduces five out of the six measured gravity-darkening β coefficients, which is motivating and promising for a more profound understanding of this important effect in stellar physics.

Taking advantage of the good quality and uv coverage of the PIONIER observations, we also pushed the analysis a little farther and performed an interferometric image reconstruction that did not reveal any signatures of additional circumstellar components and/or deviations from the photospheric Roche-von Zeipel (RVZ) model within a $\sim \pm 1\%$ level of intensity. This result also agrees with a fit of an additional analytical component to the RVZ model. Although the spatial resolution of the image is rather low (spatial frequencies restricted to the first visibility lobe), this is, to our knowledge, the first reconstructed image of the photosphere of a Be star.

The results of this work thus provide the first determination of the pure photospheric parameters of a Be star in a normal B phase. The measured photospheric parameters are R_{eq} , V_{eq} , i , β , and PA_{rot} . Concerning Achernar specifically, these parameters can be used as a reference input photospheric model for future studies based on modeling that includes circumstellar disk and photosphere.

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⁵ Available at <http://cdsweb.u-strasbg.fr/>

⁶ Available at <http://www.jmmc.fr/oifitsexplorer>

⁷ Available at <http://www.jmmc.fr/searchcal>

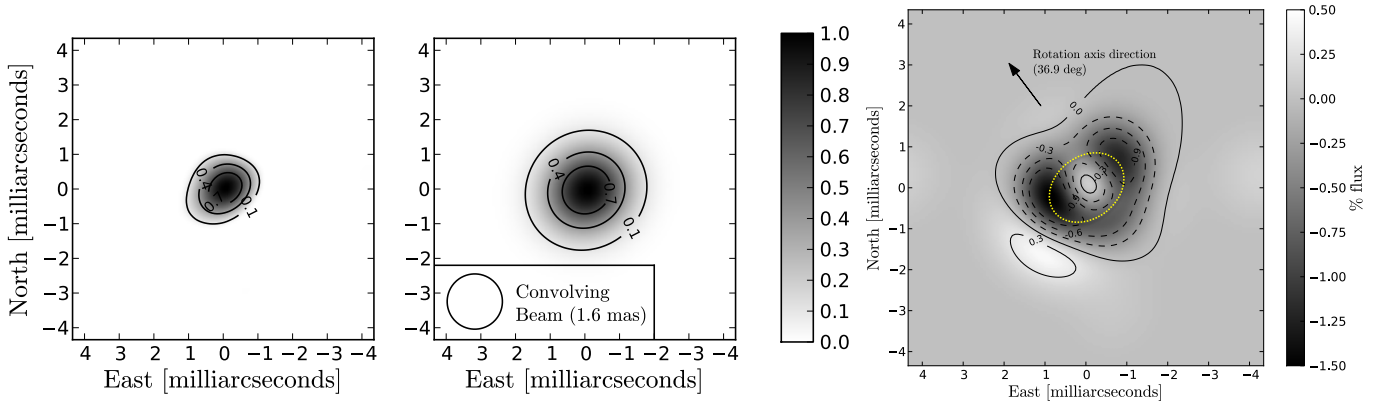


Fig. 15. *Left:* image reconstruction of Achernar obtained by applying the MIRA software to the H band VLTI/PIONIER observations. *Middle:* convolution of this reconstructed MIRA image convolved by a Gaussian beam of $FWHM = 1.6$ mas ($=0.61\lambda/B_{\max}$) corresponding to the diffraction limit of the PIONIER observations. *Right:* Reconstructed MIRA image minus the best-fit CHARRON image (Fig. 11 convolved by the Gaussian diffraction limit beam to match the resolution of reconstructed image). The difference between the images is very small, $<1.5\%$ in modulus, relative to the total MIRA image flux), indicating that essentially only the photosphere of Achernar contributes to the PIONIER data, without any additional circumstellar component. The dotted ellipse approximately represents the border of the apparent photosphere of Achernar given by the best-fit CHARRON RVZ model.

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References

- Absil, O., Mennesson, B., Le Bouquin, J.-B., et al. 2009, *ApJ*, 704, 150
Bonneau, D., Clausse, J.-M., Delfosse, X., et al. 2006, *A&A*, 456, 789
Bordé, P., Coudé du Foresto, V., Chagnon, G., & Perrin, G. 2002, *A&A*, 393, 183
Carciofi, A. C., & Bjorkman, J. E. 2006, *ApJ*, 639, 1081
Carciofi, A. C., Magalhães, A. M., Leister, N. V., Bjorkman, J. E., & Levenhagen, R. S. 2007, *ApJ*, 671, L49
Carciofi, A. C., Domiciano de Souza, A., Magalhães, A. M., Bjorkman, J. E., & Vakili, F. 2008, *ApJ*, 676, L41
Chauville, J., Zorec, J., Ballereau, D., et al. 2001, *A&A*, 378, 861
Che, X., Monnier, J. D., Zhao, M., et al. 2011, *ApJ*, 732, 68
Code, A. D., Bless, R. C., Davis, J., & Brown, R. H. 1976, *ApJ*, 203, 417
Cohen, M., Walker, R. G., Carter, B., et al. 1999, *AJ*, 117, 1864
Cutri, R. M., Skrutskie, M. F., van Dyk, S., et al. 2003, *VizieR Online Data Catalog: II/246*
Domiciano de Souza, A., Vakili, F., Jankov, S., Janot-Pacheco, E., & Abe, L. 2002, *A&A*, 393, 345
Domiciano de Souza, A., Kervella, P., Jankov, S., et al. 2003, *A&A*, 407, L47
Domiciano de Souza, A., Hadjara, M., Vakili, F., et al. 2012a, *A&A*, 545, A130
Domiciano de Souza, A., Zorec, J., & Vakili, F. 2012b, in *SF2A-2012: Proc. Annual meeting of the French Society of Astronomy and Astrophysics*, eds. S. Boissier, P. de Laverny, N. Nardetto, et al. 321
Espinosa Lara, F., & Rieutord, M. 2011, *A&A*, 533, A43
Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, *PASP*, 125, 306
Frémat, Y., Zorec, J., Hubert, A., & Floquet, M. 2005, *A&A*, 440, 305
Goodman, J., & Weare, J. 2010, *Commun. Appl. Math. Comput. Sci.*, 5, 65
Goss, K. J. F., Karoff, C., Chaplin, W. J., Elsworth, Y., & Stevens, I. R. 2011, *MNRAS*, 411, 162
Haguenauer, P., Alonso, J., Bourget, P., et al. 2010, in *SPIE Conf. Ser.*, 7734, 04
Hanbury Brown, R., Davis, J., & Allen, L. R. 1974, *MNRAS*, 167, 121
Harmanec, P. 1988, *Bull. Astron. Inst. Czechosl.*, 39, 329
Haubois, X., Carciofi, A. C., Rivinius, T., Okazaki, A. T., & Bjorkman, J. E. 2012, *ApJ*, 756, 156
Hog, E., Fabricius, C., Makarov, V. V., et al. 2000, *VizieR Online Data Catalog: I/259*
Hubeny, I., & Lanz, T. 2011, *Synspec: General Spectrum Synthesis Program, astrophysics Source Code Library*
Hutchings, J. B., & Stoeckley, T. R. 1977, *PASP*, 89, 19
Jackson, S., MacGregor, K. B., & Skumanich, A. 2004, *ApJ*, 606, 1196
Jaschek, M., & Egret, D. 1982, in *Be Stars*, eds. M. Jaschek, & H.-G. Groth, *IAU Symp.*, 98, 261
Jerzykiewicz, M., & Molenda-Zakowicz, J. 2000, *Acta Astron.*, 50, 369
Johnson, H. L., Mitchell, R. I., Iriarte, B., & Wisniewski, W. Z. 1966, *Communications of the Lunar and Planetary Laboratory*, 4, 99
Kervella, P., & Domiciano de Souza, A. 2006, *A&A*, 453, 1059
Kervella, P., & Domiciano de Souza, A. 2007, *A&A*, 474, L49
Kervella, P., Thévenin, F., Morel, P., Bordé, P., & Di Folco, E. 2003, *A&A*, 408, 681
Kervella, P., Domiciano de Souza, A., & Bendjoya, P. 2008, *A&A*, 484, L13
Kurucz, R. L. 1979, *ApJS*, 40, 1
Lafrasse, S., Mella, G., Bonneau, D., et al. 2010, in *SPIE Conf. Ser.*, 7734
Le Bouquin, J.-B., Berger, J.-P., Lazareff, B., et al. 2011, *A&A*, 535, A67
Maeder, A., & Meynet, G. 2000, *ARA&A*, 38, 143
Magalhães, A. M., Benedetti, E., & Roland, E. H. 1984, *PASP*, 96, 383
Magalhães, A. M., Rodrigues, C. V., Meade, M., et al. 1996, in *Polarimetry of the Interstellar Medium*, eds. W. G. Roberge & D. C. B. Whittet, *ASP Conf. Ser.*, 97, 202
Millour, F. A., Vannier, M., & Meilland, A. 2012, in *SPIE Conf. Ser.*, 8445
Monnier, J. D., Zhao, M., Pedretti, E., et al. 2007, *Science*, 317, 342
Monnier, J. D., Che, X., Zhao, M., et al. 2012, *ApJ*, 761, L3
Nazé, Y. 2009, *A&A*, 506, 1055
Rivinius, T., Baade, D., Townsend, R. H. D., Carciofi, A. C., & Štefl, S. 2013, *A&A*, 559, L4
Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, *AJ*, 131, 1163
Slettebak, A. 1982, *ApJS*, 50, 55
Thiébaud, E. 2008, in *SPIE Conf. Ser.*, 7013
Townsend, R. H. D., Owocki, S. P., & Howarth, I. D. 2004, *MNRAS*, 350, 189
van Belle, G. T. 2012, *A&ARv*, 20, 51
van Leeuwen, F. 2007, *A&A*, 474, 653
Vinicius, M. M. F., Zorec, J., Leister, N. V., & Levenhagen, R. S. 2006, *A&A*, 446, 643
von Zeipel, H. 1924, *MNRAS*, 84, 665
Zacharias, N., Monet, D. G., Levine, S. E., et al. 2005, *VizieR Online Data Catalog: I/297*
Zhao, M., Monnier, J. D., Pedretti, E., et al. 2009, *ApJ*, 701, 209