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# A new control scheme of cable-driven parallel robot balancing between sliding mode and linear feedback

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**Abstract:** This paper deals with the design of a robust control scheme for a suspended Cable-Driven Parallel Robot (CDPR), composed of eight cables and a moving platform (MP), dedicated to pick-and-place metal plates with different shapes, sizes and masses. The set composed of the MP and a metal plate can have a mass of up to 700 kg. In the proposed control solution, a decentralized control scheme is implemented on the robot. In order to achieve good accuracy and robust control, a recently developed controller balancing between sliding mode and linear (SML) algorithms is implemented on a CDPR prototype located at IRT Jules Verne, Nantes, France. The performances of the SML controller are analyzed along a test trajectory for several payloads. The results obtained without any information on the platform or metal plate mass are compared to those of standard proportional-derivative (PD) based control schemes.

*Keywords:* Cable-driven parallel robot, Robust control, Sliding mode, Experimental results

## 1. INTRODUCTION

Cable-Driven Parallel Robots (CDPRs) are a particular class of parallel robots whose moving-platform (MP) is connected to a fixed base frame by cables, as illustrated in Fig. 1.

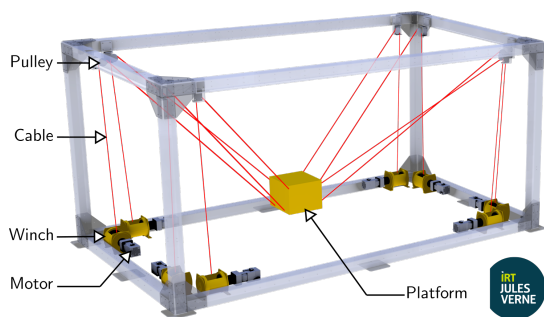


Fig. 1. CAROCA prototype 3D model in a suspended configuration.

The cables are coiled on motorized winches. Passive pulleys may guide the cables from the winches to the cable exit points. Accordingly, the motion of the MP is controlled by modifying the cable lengths. CDPRs have several advantages such as a relatively low mass of moving parts and a potential large workspace. As a consequence, they can be used in several applications such as heavy load handling (Albus et al. (1992)), painting and sandblasting

of large structures (Gagliardini et al. (2018)), fast pick-and-place operations (Kawamura et al. (2000)), haptic devices (Fortin-Coté et al. (2014)), support structures for giant telescopes (Yao et al. (2010)), and search and rescue deployable platforms (Merlet and Daney (2010)). It should be noticed that redundant actuated CDPRs are more appropriate than cranes for accurate pick-and-place operations and large and heavy parts because they suffer less from load swinging. Moreover, CDPRs can control both the position and the orientation of the object in contrary to standard cranes. Accordingly, this paper deals the determination of a control solution for a suspended semi-industrial CDPR prototype for pick and place operations of metal plates. Due to the variability of the load, and in order to get high accuracy and repeatability of the MP pose, robust control is required.

CDPR control strategies are often based on PD controllers (Kawamura et al. (2000)), that can be completed with feedforward terms to predict the moving-platform dynamic behavior (Lamaury et al. (2013); Santos et al. (2019)). Nonlinear control methods include the more recent developments of sliding-mode controllers, particularly interesting due to their robustness to uncertainties and perturbations (Edwards and Spurgeon (1998)). Sliding mode control has been increasingly considered for CDPR control in several applications (Zeinali and Khajepour (2010); El-Ghazaly et al. (2015); Santos et al. (2019)) both in simulation and experimentally, with good per-

performances against perturbations. The drawback of sliding mode control is the existence of discontinuities in the control input due to the use of the sign function (Utkin (1992), Shtessel et al. (2014)). As a consequence, the *chattering* phenomenon appears: it is a high frequency oscillation that leads to vibrations on the actuators and can prematurely deteriorate gearheads and other mobile parts in the kinematic chains. Higher order and gain adaptive sliding mode control methods have been developed to reduce chattering such as (Utkin (1992); Shtessel et al. (2014); Levant (1993)), and have been implemented on a CDPR in (Schenk et al. (2018)). An other drawback of sliding mode control is that the power consumption is generally higher than with linear control methods as the system is constantly excited to achieve high tracking accuracy. Recently, new control methods based on linear and sliding mode algorithms have been developed to achieve both lower chattering and energy consumption compared to pure sliding mode controllers (Tahoumi et al. (2018b)). The controller then balances between the two control types to get a good trade-off between robustness and smoothness of the control output. In the sequel, this controller is defined as the sliding-mode/linear (SML) controller. The objective of the SML controller is to take advantage of both control strategies: *i*) reduced chattering and energy consumption compared to sliding mode control and *ii*) accuracy, stability and robustness in spite of perturbations and uncertainties.

The objective of the paper is to evaluate the performances, for the considered pick-and-place application, of a new generation of controllers based on sliding mode. The SML controller (PC1-SML) has been experimentally compared to a simple PD controller (PC1-PD), and to a control scheme implementing a PD controller with a feedforward term that compensates for the MP mass (PC2-PD). First, the empty MP of known mass is moved along a test trajectory. Then the trajectory is repeated while carrying metal plates of unknown mass, that constitute a perturbation to the system: a metal plate M1 of mass equal to 122 kg, then a metal plate M2 of mass equal to 249 kg.

The paper is organized as follows. Section 2 presents the CDPR semi-industrial prototype used for the experimental tests as well as its modeling. Section 3 describes the experimental setup and the test trajectory. The control scheme and controllers are detailed in Sec. 4. Experimental results are presented and analyzed in Section 5. Finally, conclusions are drawn and future work is presented in Section 6.

## 2. PROTOTYPE DESCRIPTION AND MODELING

This section deals with the description and modeling of the CDPR prototype, named CAROCA (Gagliardini et al. (2018)), (see Fig. 2) and used for the experimental comparison of the control schemes.

### 2.1 CAROCA prototype and ROCKET project

CAROCA is a reconfigurable CDPR prototype developed at IRT Jules Verne, Nantes, France, dedicated to industrial operations. A video of a logistics application on the

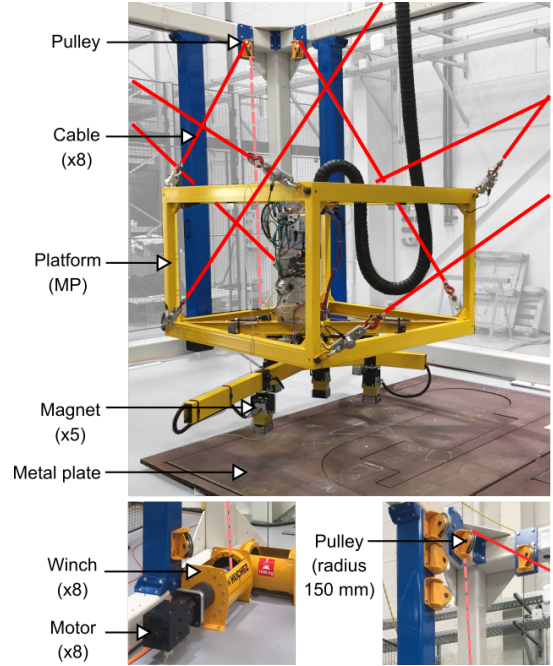


Fig. 2. The moving-platform (MP) of mass equal to 366 kg, equipped with five magnets to pick the metal plates.

prototype is available<sup>1</sup>. In this paper, its application is the displacement of metal plates of highly variable shape and mass, up to 700 kg, with good accuracy and repeatability, in the order of one centimeter.

This prototype is reconfigurable, because its pulleys can be displaced in a discrete manner on its frame, allowing the robot to be mounted both in a suspended configuration and in a fully-constrained configuration depending on the targeted application. In this paper, only the suspended configuration is considered. The size of the prototype is 7 m long, 4 m wide and 3 m high. It is composed of 8 cables coiled around 120 mm diameter Huchez<sup>TM</sup> winches, that are pulling a moving-platform. The winches are actuated by B&R Automation<sup>TM</sup> synchronous motors of nominal speed and nominal torques equal to 2200 rpm and 15.34 Nm, respectively. A two-stage gearbox of reduction ratio equal to 40 is assembled between each motor and each winch. As a consequence, the prototype is able to lift up to 1 ton. Figure 2 presents the moving-platform (MP) of size 1.5 m × 1.5 m × 1 m and mass 366 kg. Five magnets are embedded under the moving platform to pick metal parts. The robot is also equipped with Tractel<sup>TM</sup> force sensors located between the cables and the anchor points of the platform (Fig. 2). Hardware such as motors and control bay are standard industrial components commercialized by B&R Automation<sup>TM</sup>. The robot programming is done under Automation Studio 4.1<sup>TM</sup> and runs in a 2 ms real-time loop (500 Hz).

### 2.2 Inverse Geometric Model (IGM)

Figure 3 depicts the main geometric parameters of a CDPR and its  $i^{th}$  loop-closure equation,  $i \in \{1, \dots, m\}$ ,  $m$  being the number of cables attached to the MP,  $\mathcal{F}_b$

<sup>1</sup> CDPR logistics application at IRT Jules Verne (YouTube): [bit.ly/irtjvlogisticscdpr](https://bit.ly/irtjvlogisticscdpr)

is the robot base frame, and  $\mathcal{F}_p$  is the MP frame. Cable exit points are denoted as  $A_i$ , while cable anchor points are denoted as  $B_i$ . Vector  ${}^b\mathbf{a}_i$  points from  $O$  to  $A_i$  and is expressed in frame  $\mathcal{F}_b$ . Vector  ${}^p\mathbf{b}_i$  point from  $P$  to  $B_i$  and is expressed in frame  $\mathcal{F}_p$ . Vector  ${}^b\mathbf{p}$  is the position vector of point  $P$ , the MP geometric center, expressed in  $\mathcal{F}_b$ .

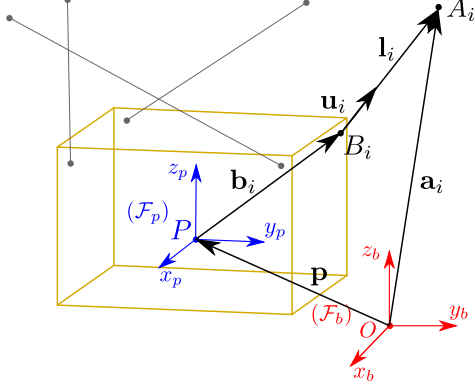


Fig. 3. CDPR geometric parameterization.

Vector  $\mathbf{l}_i$  represents the  $i^{\text{th}}$  cable vector and points from  $B_i$  to  $A_i$ , and reads as :

$${}^b\mathbf{l}_i = l_i {}^b\mathbf{u}_i = {}^b\mathbf{a}_i - {}^b\mathbf{p} - {}^b\mathbf{R}_p {}^p\mathbf{b}_i \quad (1)$$

with  ${}^b\mathbf{R}_p$  the rotation matrix from frame  $\mathcal{F}_b$  to frame  $\mathcal{F}_p$ .  $l_i$  is the length of the  $i^{\text{th}}$  cable and  $\mathbf{u}_i$  is the unit vector of the  $i^{\text{th}}$  cable vector, defined as

$$l_i = \|\mathbf{l}_i\|_2 \quad {}^b\mathbf{u}_i = \frac{{}^b\mathbf{l}_i}{\|\mathbf{l}_i\|_2} \quad (2)$$

where  $\|\cdot\|_2$  denotes the Euclidean norm of a vector.

In order to benefit from the most accurate modeling, the CDPR pulleys can be included in the geometric model of the CDPR, as described in (Gagliardini (2016); Picard et al. (2018)).

### 2.3 Static equilibrium

The static equilibrium of the platform is given by

$$\mathbf{W}\mathbf{t} + \mathbf{w}_e + \mathbf{w}_g = 0 \quad (3)$$

with  $\mathbf{W}$  the wrench matrix of the robot and expressed as

$$\mathbf{W} = \begin{bmatrix} {}^b\mathbf{u}_1 & \dots & {}^b\mathbf{u}_i & \dots & {}^b\mathbf{u}_m \\ {}^b\mathbf{b}_1 \times {}^b\mathbf{u}_1 & \dots & {}^b\mathbf{b}_i \times {}^b\mathbf{u}_i & \dots & {}^b\mathbf{b}_m \times {}^b\mathbf{u}_m \end{bmatrix} \quad (4)$$

$\mathbf{t}$  is the cable tension vector.  $\mathbf{w}_g$  the wrench applied to the platform due to gravity and  $\mathbf{w}_e$  an external wrench expressed in frame  $\mathcal{F}_b$ .

### 2.4 Inverse Kinematic Model (IKM)

For CDPRs, the forward Jacobian matrix  $\mathbf{A}$  relates the MP twist  $\mathbf{v}$  and the cable unwinding velocities:

$$\mathbf{A}\mathbf{v} = \dot{\mathbf{i}} = \frac{r_w}{R} \dot{\mathbf{q}} \quad \text{with} \quad \mathbf{v} = [{}^b\dot{\mathbf{p}} \quad {}^b\boldsymbol{\omega}]^T \quad (5)$$

$\dot{\mathbf{i}} = [\dot{i}_1 \dots \dot{i}_i \dots \dot{i}_8]^T$  being the vector containing the cable velocities,  $\dot{\mathbf{q}} = [\dot{q}_1 \dots \dot{q}_i \dots \dot{q}_8]^T$  being the vector containing the motor velocities,  $R$  the gearbox reduction ratio,  $r_w$  the winch radius,  ${}^b\mathbf{p}$  the Cartesian position of MP and  ${}^b\boldsymbol{\omega}$  its angular velocity, expressed in  $\mathcal{F}_b$ .  $\mathbf{A}$  and  $\mathbf{W}$  are related by the equation:

$$\mathbf{W} = -\mathbf{A}^T \quad (6)$$

### 2.5 Dynamic model

From (Gagliardini et al. (2018)), the dynamic model of the CDPR reads as

$$\mathbf{W}\mathbf{t} - \mathbb{I}_p \dot{\mathbf{v}} - \mathbf{C}\mathbf{v} + \mathbf{w}_e + \mathbf{w}_g = 0 \quad (7)$$

with  $\mathbb{I}_p$  the spatial inertia of the platform and  $\mathbf{C}$  the matrix of the centrifugal and Coriolis wrenches.

Given that the center of mass of the platform  $G$  does not coincide with the origin of  $\mathcal{F}_p$ , the wrench  $\mathbf{w}_g$  due to the gravity acceleration  $\mathbf{g}$  is defined as

$$\mathbf{w}_g = \begin{bmatrix} m_p \mathbf{I}_3 \\ \mathbf{MS}_p \end{bmatrix} \mathbf{g} \quad (8)$$

with  $m_p$  the mass of the platform,  $\mathbf{I}_3$  the  $3 \times 3$  identity matrix,  $\mathbf{MS}_p = {}^b\mathbf{R}_p [m_p x_G \quad m_p y_G \quad m_p z_G]^T$  the first momentum of the moving platform defined with respect to frame  $\mathcal{F}_b$ . The vector  $\mathbf{S}_p = [x_G \quad y_G \quad z_G]^T$  defines the position of  $G$  in  $\mathcal{F}_p$ .  $\mathbf{MS}_p$  is the skew-symmetric matrix associated to  $\mathbf{MS}_p$ .

$\mathbb{I}_p$  represents the spatial inertia of the platform, and reads as

$$\mathbb{I}_p = \begin{bmatrix} m_p \mathbf{I}_3 & -\mathbf{MS}_p \\ \mathbf{MS}_p & \mathbf{I}_p \end{bmatrix} \quad (9)$$

with  $\mathbf{I}_p$  the inertia tensor matrix of the platform, that can be computed from the platform's inertia tensor  $\mathbf{I}_g$  using the Huygens-Steiner theorem

$$\mathbf{I}_p = {}^b\mathbf{R}_p \mathbf{I}_g {}^b\mathbf{R}_p^T - \frac{\mathbf{MS}_p \mathbf{MS}_p^T}{m_p} \quad (10)$$

$\mathbf{C}$  is the matrix of the centrifugal and Coriolis wrenches with

$$\mathbf{C}\mathbf{v} = \begin{bmatrix} {}^b\hat{\boldsymbol{\omega}} {}^b\boldsymbol{\omega} \mathbf{MS}_p \\ {}^b\hat{\boldsymbol{\omega}} \mathbf{I}_p {}^b\boldsymbol{\omega} \end{bmatrix} \quad (11)$$

where  ${}^b\hat{\boldsymbol{\omega}}$  the skew-symmetric matrix associated to  ${}^b\boldsymbol{\omega}$ .

### 2.6 State system

The dynamics of the motors (Lamaury and Gouttefarde (2013)) are given by

$$\boldsymbol{\tau}_m = \mathbf{I}_q \ddot{\mathbf{q}} + \mathbf{F}_v \dot{\mathbf{q}} + \mathbf{F}_s \text{sign}(\dot{\mathbf{q}}) + \frac{R}{r_w} \mathbf{t} \quad (12)$$

where  $\mathbf{I}_q$  is the diagonal matrix containing the moment of inertia of the gearmotors and winches associated to each motor, and  $\mathbf{F}_c$  and  $\mathbf{F}_v$  are respectively the diagonal matrices containing the static and viscous friction coefficients for each motor.

From the motor dynamic model (equation 12), the CDPR inverse kinematic model (equation (5)) and the CDPR dynamic model (equation (7)), defining the state vector as  $\mathbf{x} = [\mathbf{q} \quad \dot{\mathbf{q}}]^T$  and the system input as  $\mathbf{u} = \boldsymbol{\tau}_m$ , the system can be represented as a standard nonlinear system of the form

$$\dot{\mathbf{x}} = f(\mathbf{x}) + g(\mathbf{x})\mathbf{u} \quad (13)$$

The system is nonlinear and affine in the control input  $\mathbf{u}$ . Furthermore,  $f(\mathbf{x})$  is uncertain due to the presence of  $\mathbf{w}_e$  in (equation (7)).



### 3. TEST TRAJECTORY AND EXPERIMENTAL SETUP

In order to evaluate the performance of different control methods, a desired trajectory describing a typical pick-and-place application has been generated. The trajectory is generated using s-curves, that ensure continuous velocity and acceleration trajectory profiles. The  $x$ -axis of the frame  $\mathcal{F}_b$  is defined along the width of the CDPR, the  $y$ -axis along its length and the  $z$ -axis along its height. The trajectory consists of (see Fig. 4):

- (1) AB: 200 mm vertical displacement up;
- (2) BC: arc along the diagonal of the base footprint, with simultaneous displacements of 300 mm up, 300 mm along the  $x$ -axis and 1400 mm along the  $y$ -axis;
- (3) CD: arc along the diagonal of the base footprint, with simultaneous displacements of 300 mm down, 300 mm along the  $x$ -axis and 1400 mm along the  $y$ -axis;
- (4) DE: 200 mm vertical displacement down;

The platform moves from A to E in 30 s.

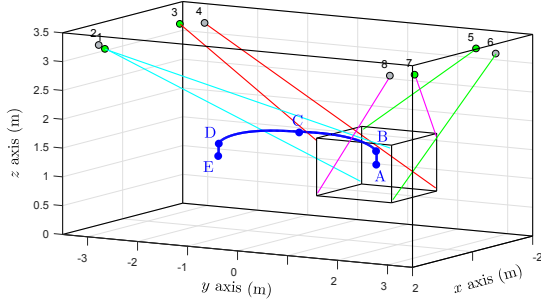
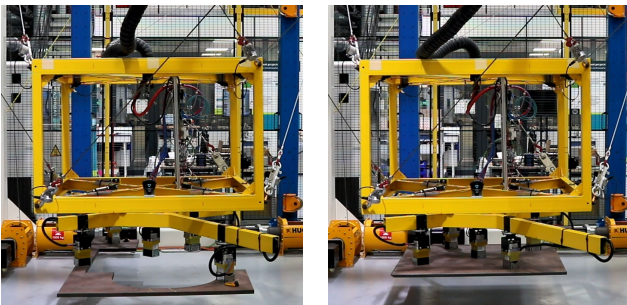


Fig. 4. Test trajectory (blue) and CDPR configuration.

This test is first performed on the CDPR with the empty platform of mass 366 kg. In order to evaluate the control robustness, two metal plates are successively carried by the platform. Three cases are then considered:

- (1) the empty moving-platform of mass 366 kg (MP);
- (2) the MP and a metal plate M1 of mass 122 kg, for a total load of 488 kg (MPM1);
- (3) the MP and a metal plate M2 of mass 249 kg, for a total load of 615 kg (MPM2)

Note that the mass variation is significant, namely +33% (M1) and +68% (M2) with respect to the MP mass, respectively.



(a) MPM1 (488 kg).

(b) MPM2 (615 kg).

Fig. 5. MP carrying a metal plate: (a) M1, (b) M2.

### 4. CONTROL STRATEGIES

Accordingly to equation (12), Fig. 6 presents the system input, output and perturbation signals. The system input is the motor torque vector  $\tau_m$ . The usual outputs of the system are the actual motor positions  $\mathbf{q}$  and motor velocities  $\dot{\mathbf{q}}$ . The considered perturbation is gravity wrench  $\mathbf{w}_g$  of the moving-platform and the embedded metal plate.

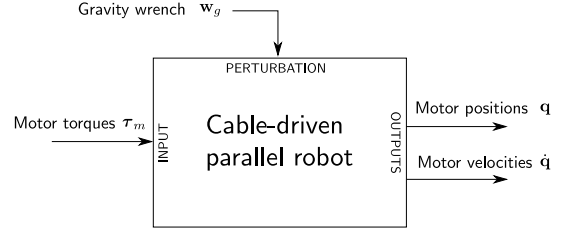


Fig. 6. Diagram of the CDPR.

#### 4.1 Control schemes

No direct information on the platform pose is readily available from the system sensors, and solving the direct geometric model of a CDPR is not an easy task since more than one solution is possible from a fixed set of motor positions, even considering straight and inelastic cables (Merlet (2015)). As a consequence, the following control architectures only rely on the system internal sensors *i.e.* the motor angular positions and velocities. Decentralized control architectures have been considered for their simplicity of implementation, with one controller separately tuned for each motor.

*PC1: Basic control scheme.* The first control architecture is denoted as PC1 (Fig. 7). The *controller* box at the center of the control schemes is left unspecified in this section. In the sequel, proportional-derivative controller or the sliding mode based controller will be introduced. The corresponding control architecture is then referenced as PC1-PD or PC1-SML, accordingly.

$\mathbf{c}_d$  is the 6-dimensional vector containing the desired Cartesian position and orientation of the MP,  $\mathbf{v}_d$  the desired MP twist (linear and angular platform velocities).  $\mathbf{q}_d$ ,  $\dot{\mathbf{q}}_d$  and  $\tau_m$  are the desired motor angular positions, velocities obtained from the inverse geometric (IGM) and kinematic (IKM) models, respectively. In this first scheme, the motor torque vector  $\tau_m$  is the control signal, each signal being of dimension 8.

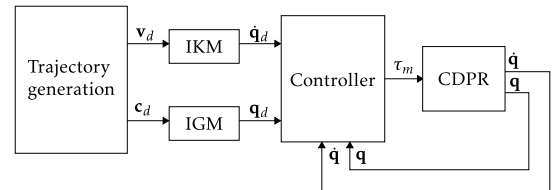


Fig. 7. PC1 control architecture.

The MP Cartesian MP pose and twist are converted into desired motor positions and velocities using the CDPR inverse geometric (IGM) and kinematic (IKM) models.

*PC2: Control scheme with feedforward.* Feedforward terms (see Fig. 8 blue blocks) are commonly included in CDPR control strategies to predict the dynamics of the platform and improves the accuracy of the robot (Lamaury et al. (2013); Vafaei et al. (2010)).

From Eq. (7), a feedforward term compensating part of the gravity is defined as

$$\boldsymbol{\tau}_{da} = \frac{r_w \mathbf{W}^\dagger (\mathbb{I}_p \dot{\mathbf{v}}_d + \mathbf{w}_g)}{R} \quad (14)$$

with  $\tau_{da}$  the feedforward torque,  $\mathbf{w}_g$  the wrench due to the gravity,  $r_w$  the radius of the winches and  $R$  the gearhead ratio.  $\mathbf{W}^\dagger$  denotes the Moore-Penrose pseudo-inverse of  $\mathbf{W}$ . However, for metal plate handling, the mass of the metal plates is supposed to be unknown. As a consequence, only the MP mass is considered in the feedforward term, that gives

$$\mathbf{w}_g = [0 \ 0 \ -m_{MP}g \ -m_{MP}gy_G \ m_{MP}gx_G \ 0]^\top \quad (15)$$

with  $m_{MP}$  the MP mass and  $\mathbf{g}$  the gravity vector expressed in  $\mathcal{F}_b$ .  $x_G$  and  $y_G$  are the Cartesian coordinates of the MP center of gravity  $G$  expressed in  $\mathcal{F}_p$ . Note that  $x_G$  and  $y_G$  are supposed to be null along the trajectory.

Also, a linear friction model (Khalil and Dombre (2004)) has been implemented in each actuation chain to compensate the losses in the motors, gearbox and winches:

$$\boldsymbol{\tau}_{fc} = \mathbf{F}_c \text{sign}(\dot{\mathbf{q}}_d) + \mathbf{F}_v \dot{\mathbf{q}}_d \quad (16)$$

with  $\boldsymbol{\tau}_{fc}$  the friction compensation and  $\dot{\mathbf{q}}_d$  the desired motor rate vector.

Figure 8 presents the PC2 control architecture with feedforward, where  $\dot{\mathbf{v}}_d$  contains the Cartesian acceleration and angular acceleration of the platform. The control torques in  $\boldsymbol{\tau}_m$  applied to the motors is based finally on  $\boldsymbol{\tau}_c$ ,  $\boldsymbol{\tau}_{da}$  and  $\boldsymbol{\tau}_{fc}$ .

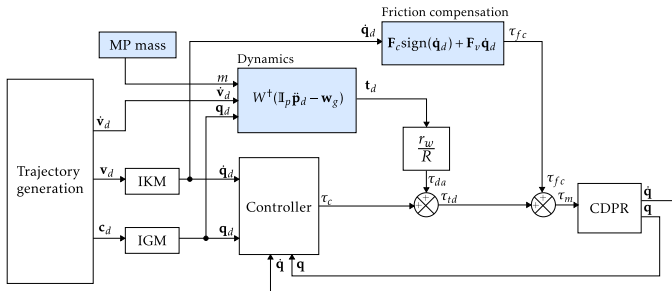


Fig. 8. PC2 control architecture with feedforward terms.

#### 4.2 Control algorithms

The control algorithms are described thereafter.

*PD controller.* Proportional-derivative (PD) controllers are already widely used in industry and machinery. The choice of a PD controller compared to the full PID is based here on its asymptotic stability (Khalil and Dombre (2004)). Its main drawbacks are the static error between the desired and real position of the robot as well as a tuning that often requires iteration. In addition, this controller can be sensitive to noise and its settings are optimal only around an operating point.

The 8-dimensional output signal of the controller  $\boldsymbol{\tau}_c$  is therefore defined by

$$\boldsymbol{\tau}_c = \mathbf{K}_p \mathbf{e}_q + \mathbf{K}_d \mathbf{e}_{\dot{q}} \quad (17)$$

with  $\mathbf{e}_q$  the difference between the desired and actual motor positions and  $\mathbf{e}_{\dot{q}}$  being the difference between the desired and actual motors velocities. In PC1-PD (Fig. 7),  $\mathbf{u} = \boldsymbol{\tau}_m = \boldsymbol{\tau}_c$ , while in PC2-PD (Fig. 8),  $\mathbf{u} = \boldsymbol{\tau}_m = \boldsymbol{\tau}_c + \boldsymbol{\tau}_{da} + \boldsymbol{\tau}_{fc}$ .

In a decentralized control architecture, each motor is independently controlled: then, the matrices  $\mathbf{K}_p$  and  $\mathbf{K}_d$  are diagonal. For simplicity and since the identified motor friction coefficients have been found to be similar across all motors, the 8 decentralized controllers have been tuned in a similar manner:  $K_p = K_{p,1} = K_{p,2} \dots$  and  $K_d = K_{d,1} = K_{d,2} \dots$ . However, it could be possible to independently adjust the gains of each motor according to their errors along the test trajectory or interdependence. The PD controller has been tuned to achieve accuracy and stability with the MP, using the standard method proposed by (Ziegler and Nichols (1995)). The obtained gains  $K_p$  and  $K_d$  are given in Table 1.

Table 1. PD controller gains.

Gain	$K_p$	$K_d$
ROMP values	0.3	0.03

*SML controller.* Similarly to the PD controller, eight individual SML controllers have been implemented. Note that in this paper, the SML controller is applied only to PC1 scheme (Fig. 7).

Define the sliding vector  $\boldsymbol{\sigma}$  as

$$\boldsymbol{\sigma} = (\dot{\mathbf{q}}_d - \dot{\mathbf{q}}) + \lambda(\mathbf{q}_d - \mathbf{q}) \quad (18)$$

$$= \mathbf{e}_{\dot{q}} + \lambda \mathbf{e}_q \quad (19)$$

with  $\mathbf{q}_d$  and  $\mathbf{q}$  respectively the desired and current motor angular positions,  $\dot{\mathbf{q}}_d$  and  $\dot{\mathbf{q}}$  respectively the desired and current motor velocities,  $\mathbf{e}_q$  and  $\mathbf{e}_{\dot{q}}$  the corresponding tracking errors and  $\lambda$  a strictly positive parameter ( $\lambda > 0$ ).

Sliding mode control must ensure that the sliding variable reaches and is maintained at zero in a finite time (Utkin (1992); Shtessel et al. (2014)): given the definition (18) of  $\boldsymbol{\sigma}$ , when the sliding variable of the  $i^{\text{th}}$  motor  $\sigma_i$  tends to zero, the convergence of  $e_{q,i}$ , the  $i^{\text{th}}$  component of  $\mathbf{e}_q$ , to zero is guaranteed exponentially with a rate depending on the parameter  $\lambda$ . This is described as the *transient phase*. Then, the controller is in the steady state: the sliding variable  $\sigma_i$  is maintained around zero and the dynamic of the control is defined by the differential equation  $\dot{e}_{q,i} = -\lambda e_{q,i}$ , as such the higher  $\lambda$ , the faster the correction. This is described as the *sliding phase*.

$\boldsymbol{\sigma}$  has a relative degree of one with respect to  $\boldsymbol{\tau}_m$ . The time derivative of the sliding variable equals

$$\dot{\boldsymbol{\sigma}} = \mathbf{e}_{\dot{q}} + \lambda \mathbf{e}_{\dot{q}} \quad (20)$$

$$= (\ddot{\mathbf{q}}_d - \ddot{\mathbf{q}}) + \lambda(\dot{\mathbf{q}}_d - \dot{\mathbf{q}}) \quad (21)$$

$$= (\ddot{\mathbf{q}}_d + \lambda(\dot{\mathbf{q}}_d - \dot{\mathbf{q}})) - \ddot{\mathbf{q}} \quad (22)$$

$\ddot{\mathbf{q}}_d$  and  $\ddot{\mathbf{q}}$  being the desired and actual motor acceleration vectors, respectively.  $\ddot{\mathbf{q}}$  is correlated to the motor torques  $\boldsymbol{\tau}_m$  by equation (12).  $\dot{\boldsymbol{\sigma}}$  then takes the form

$$\dot{\boldsymbol{\sigma}} = \mathbf{a}(\mathbf{q}) + \mathbf{b}(\mathbf{q})\boldsymbol{\tau}_m \quad (23)$$

where  $b(\mathbf{q}) \neq 0$ .

In order to design the twisting algorithm, the sliding variable is derived a second time ; one gets:

$$\ddot{\sigma} = (\ddot{\mathbf{q}}_d - \ddot{\mathbf{q}}) + \lambda(\dot{\mathbf{q}}_d - \dot{\mathbf{q}}) \quad (24)$$

$$= (\dot{\mathbf{q}}_d + \lambda(\dot{\mathbf{q}}_d - \dot{\mathbf{q}})) - \dot{\mathbf{q}} \quad (25)$$

$$= h(\mathbf{q}) + j(\mathbf{q})\dot{\tau}_m \quad (26)$$

with  $j(\mathbf{q}) \neq 0$ .

Each component of  $\dot{\tau}_m$  (Tahoumi et al. (2018a)), is defined as

$$\dot{\tau}_{m,i} = -K_1[\sigma_i]^{\frac{\alpha}{2-\alpha}} - K_2[\dot{\sigma}_i]^\alpha \quad (27)$$

with  $\dot{\tau}_{m,i}$  the  $i^{th}$  component of  $\dot{\tau}_m$  and

$$[\sigma_i]^\alpha = |\sigma_i|^\alpha \text{sign}(\sigma_i) \quad (28)$$

$K_1$  and  $K_2$  are the controller gains, and  $\alpha \in [0 \ 1]$  based on the following adaptation law:

$$\alpha = \max \left( -\beta \left( \frac{|\sigma_i|}{|\sigma_i| + \epsilon_\sigma} + \frac{|\dot{\sigma}_i|}{|\dot{\sigma}_i| + \epsilon_{\dot{\sigma}}} \right) + 1, 0 \right) \quad (29)$$

with  $\beta$ ,  $\epsilon_\sigma$  and  $\epsilon_{\dot{\sigma}}$  constant parameters chosen such that  $\beta > 1$  and  $\epsilon_\sigma, \epsilon_{\dot{\sigma}} > 0$ . Values of these parameters for the experiments are provided in table 2. The control input  $\tau_m$  is then obtained by integrating its time derivative from Eq. (27).

The principle of the SML controller (Eqs. (27)-(29)) is the following: the value of the variable  $\alpha$  depends on the current tracking errors. If the absolute values of  $|\sigma_i|$  and  $|\dot{\sigma}_i|$  are large, it means that the closed-loop system is not accurate: the controller should lean towards a robust controller, namely the sliding mode control. That is the case because in such a situation,  $\alpha \rightarrow 0$ , from Eq. (27), the control becomes a twisting one (Levant (1993)):

$$\dot{\tau}_{m,i} = -K_1 \text{sign}(\sigma_i) - K_2 \text{sign}(\dot{\sigma}_i) \quad (30)$$

that ensures, in practice, the convergence of  $\sigma_i$  and  $\dot{\sigma}_i$  to a vicinity of  $(0, 0)$ , in finite time.

On the other hand, if these errors are small, in order to reduce chattering and energy consumption, the controller should lean towards the linear control behavior: that is the case because  $\alpha \rightarrow 1$ .  $\alpha$  regulates the trade-off between accuracy and chattering reduction.  $\dot{\tau}_{m,i}$  then tends towards the expression

$$\dot{\tau}_{m,i} = -K_1 \sigma_i - K_2 \dot{\sigma}_i \quad (31)$$

In order to guarantee convergence of the closed-loop system, the gains  $K_1$  and  $K_2$  must be positive and follow the condition (Levant (1993)):

$$\begin{aligned} K_1 > K_2 > 0, \quad (K_1 - K_2)j_m > h_M \\ (K_1 + K_2)j_m - h_M > (K_1 - K_2)j_m + h_M \end{aligned} \quad (32)$$

with  $h_M$ ,  $j_m$  and  $j_M$  positive constants such that for each motor

$$|h_i(q)| \leq h_M \quad (33)$$

$$0 < j_m \leq j_i(q) \leq j_M \quad (34)$$

The reduced energy consumption of the SML controller compared to the twisting algorithm is ensured by the following condition (Tahoumi et al. (2018a)):

$$K_1 \epsilon_\sigma + K_2 \epsilon_{\dot{\sigma}} < K_1 - K_2 \quad (35)$$

Recall that  $K_1$  and  $K_2$  are the gains of the controller: they must be chosen sufficiently large in order to counteract

perturbations and uncertainties effects.  $\beta$  and  $\epsilon_\sigma, \epsilon_{\dot{\sigma}}$  have opposing effects on the evolution of  $\alpha$ . These parameters should be chosen to calibrate the controller behavior with respect to the desired compromise between accuracy and chattering/consumption reduction: the higher  $\beta$  or the smaller  $\epsilon_\sigma, \epsilon_{\dot{\sigma}}$ , the lower  $\alpha$ . Then, the system leans towards sliding mode. As a consequence, the control accuracy is improved with higher energy consumption. On the other hand, if  $\beta$  is decreased or  $\epsilon_\sigma, \epsilon_{\dot{\sigma}}$  are increased,  $\alpha$  will increase: the chattering and energy consumption will be reduced as the linear control contribution increases. However, the robustness, and then the accuracy, are reduced.

Table 2. SML controller parameter values.

Parameter	$\lambda$	$\beta$	$\epsilon_\sigma$	$\epsilon_{\dot{\sigma}}$	$K_1$	$K_2$
ROMP values	0.15	1.01	4	80	4	2

Since only the motor position and velocity are provided on the prototype, the motor angular acceleration errors  $e_{\ddot{\mathbf{q}}}$  appearing in  $\ddot{\sigma}$  are derived from the motor velocity errors with the usual Euler method.

## 5. EXPERIMENTAL RESULTS

The objective of the experiments is to compare the performances of the SML controller without knowledge of the MP and metal plate mass (PC1-SML), to those of the PD controller (PC1-PD) in the same conditions, and of the PD controller with feedforward for the compensation of the MP mass (PC2-PD). A video of the metal plate handling experiments is available<sup>2</sup>.

### 5.1 Motor position errors

Figure 9 presents the *Root Mean Square* (RMS) of Motors 1 to 8 position errors along the test trajectory, for each controller and load. As expected, the PC1-PD gives the highest RMS in all scenarios, up to 12 degrees, due to the controller static error. PC2-PD provides the smallest RMS for load MP, as the mass of the platform is exactly compensated by the feedforward term. Thus, the static error is greatly reduced. However, the RMS of PC2-PD motor position error naturally increases as a metal plate of unknown mass is carried. It appears that PC1-SML provides the most consistent results no matter the load, the motor position errors being always smaller than 4 degrees. Slight differences in the performances from one motor to another could be attributed to the impact of the new center of mass of the set constituted of the MP and the metal plate.

A single motor is considered in the sequel for a more detailed analysis. Fig. 10 presents Motor 4 angular error  $e_{q4}$  along the trajectory, with the three controllers and the three payloads. Again, the static errors of PC1-PD and PC2-PD are clearly visible as the mass increases. The maximum error is reached around 11 degrees for the heaviest load (MPM2) for PC1-PD. The compensation of the MP mass limits this maximum error to around 4 degrees for PC2-PD. Although  $e_{q,4}$  has a more oscillating behavior with PC1-SML, it is noteworthy that it is the most robust one amongst the three controllers. Indeed, its value oscillates around zero for all loads.

<sup>2</sup> Metal plate handling video (Dropbox): [bit.ly/ifac2020id3263](https://bit.ly/ifac2020id3263)

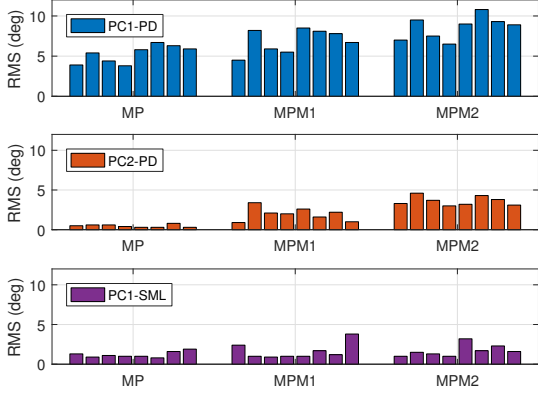


Fig. 9. Root Mean Square (RMS) of position error (degrees) for Motors 1 to 8 (left to right) against load.

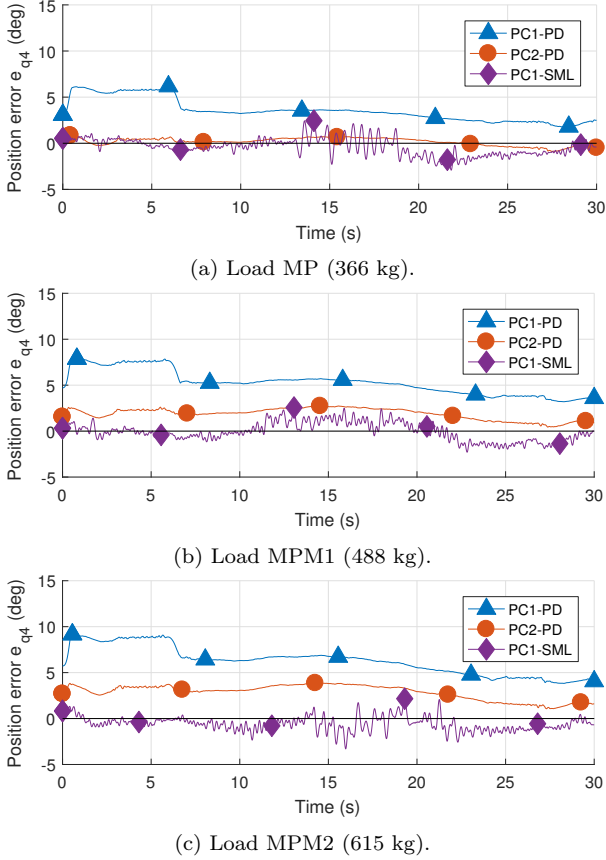


Fig. 10. Motor 4 position error  $e_{q,4}$  (degrees).

The control input of Motor 4 associated with each controller is plotted in Fig. 11. All controllers generate a similarly shaped torque output, although chattering is visible in the case of the sliding mode, that is to be expected: this is the cost of robustness. Static friction in the gearbox can be observed around  $t = 1$  s and  $t = 6$  s, when the motor changes direction. The friction is anticipated in the feedforward term of PC2-PD, and is quickly corrected by the SML controller, leading to similarly shaped signals.

### 5.2 MP position error along $z$ -axis

The MP pose has been tracked using a HTC VIVE Tracker. Figure 12 presents the Cartesian error along the vertical axis between the desired and measured position of

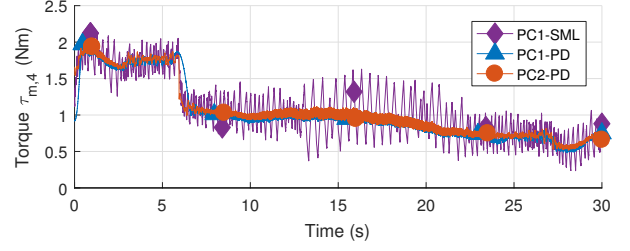


Fig. 11. Motor 4 control input  $\tau_m$  (Nm) for load MPM2 (615 kg).

the MP center  $P$  (see Fig. 3), for the heaviest load MPM2. The observations made on the motor position errors are also visible: the PC1-PD controller leads to the largest error while the addition of the feedforward term in PC2-PD reduces this error. The sliding mode controller provides the smallest error although a static error of around 20 mm remains. This error is certainly due to cable elasticity, which is not negligible for the 615 kg load, and will need to be compensated in the future.

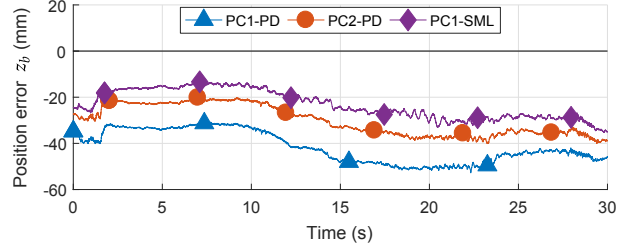


Fig. 12. MP Cartesian position error along  $z$ -axis (mm) for load MPM2 (615 kg).

### 5.3 Evolution of $\alpha$

The mean value of  $\alpha$  along the trajectory across all motors is presented in Fig. 13. As expected, the larger the payload, the closer the controller to sliding mode control *i.e.* the lower  $\alpha$ . Figure 14 shows the evolution of  $\alpha$  for Motor 4 for the heaviest load (MPM2), versus time. It can be noticed that with the current tuning of the SML controller, the values of  $\alpha$  are relatively low with an average value of 0.12 in general, namely the controller is mostly a sliding mode one along the trajectory, due to the system high level of uncertainties. It is noteworthy that around  $t = 7$  s and  $t = 27$  s,  $\alpha$  reaches higher values for short periods of time. Meanwhile, Fig. 11 shows reduced chattering in  $\tau_m$  and Fig. 10 presents lower motor position oscillations. Contrarily, around  $t = 15$  s, as  $\alpha$  lower values lead to higher oscillations. The control is effectively smoother when  $\alpha$  increases.

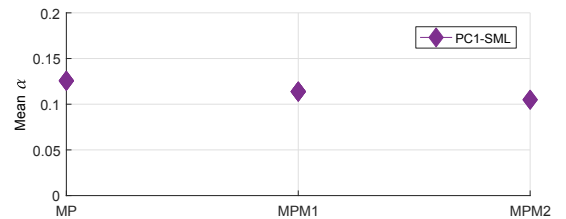


Fig. 13. Mean of  $\alpha$  along trajectory, across all motors and for each load.



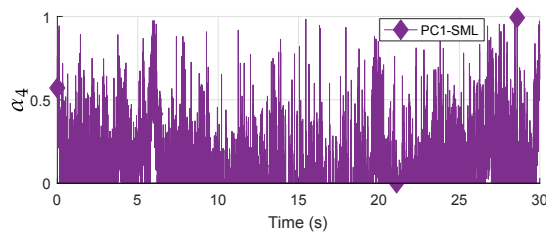


Fig. 14. Evolution of  $\alpha_4$  for load MPM2 (615 kg).

## 6. CONCLUSION

Although, a proportional-derivative based control scheme can be applied for smooth control signal of a cable-driven parallel robot, it is very restrictive due to the required knowledge of the carried mass in order to achieve good accuracy. If no information is available on the load mass, the novel control scheme balancing between sliding mode and linear algorithms is relevant for its robustness towards uncertainties and stability, with reducing chattering and oscillations when the parameter  $\alpha$  increases. Future work will focus on further reducing oscillations, and include a cable elasticity compensation to improve the control robustness and pose accuracy of the moving-platform.

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