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Robust Control of VSC-HVDC System with Input and States Constraints

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Abstract—This paper proposes a robust control strategy for a High Voltage Direct Current (HVDC), in order to improve the dynamic behavior performance under a wide range of operating conditions, parameters uncertainties, input and state constraints. It proposes first to model the HVDC and investigates the robust control based on Model Recovery Anti-windup (MRAW) to improve regional performance and stability of HVDC systems with saturating actuators. More precisely, in this paper sufficient conditions based on Linear Matrix Inequalities (LMIs) are derived for robust stabilization, in the sense of Lyapunov method. First, a robust controller is designed to show a desirable nominal performance by ignoring states and control inputs constraints. Next, an additional compensator is designed to mitigate the adverse effects due to state and the control constraints. The proposed strategy validations are performed using a MATLAB/Simulink software.

I. INTRODUCTION

In the transmitting power over long distances, High Voltage Direct Current (HVDC) transmission systems are used because there are several advantages for the Voltage Source Converter (VSC) based HVDC transmission (VSC-HVDC) compared to the conventional, thyristor based HVDC. One of the advantages of VSC-HVDC is that it can supply inductive or capacitive reactive power to the connected AC system in addition to supplying real power interchange with the DC link. Moreover, VSC- HVDC has high speed and high voltage switches [1]-[4]. Its known that, VSC- HVDC dynamics are effect by changing its operating conditions, so the controller design problem to provide required performance over an expected range of operating conditions is arises. In addition, controller design for state and actuator constrained VSC-HVDC systems is a challenging problem. It becomes more complex if the multivariable HVDC system is subject to parameter uncertainties, which is quite common in many physical systems. The parameter uncertainties may come with the change of environment (temperature change, pressure change, load change, etc.), changes of AC grid parameters due to disturbances like short-circuits [5], [6], ageing of components, measurement error, etc.. Parameter uncertainties make the values of the parameters deviate from the nominal values and may degrade the system performance or even cause instability of the system.

Several authors have presented mathematical models and control strategies for VSC-HVDC transmission that include small signal stability [7], decoupling control in converter stations using feedback linearization [8], LMI based robust control [9]-[16], and adaptive control [17]-[19]. Most of these papers have not considered the parameter uncertainties and/or the hard constraints.

The main contributions of this paper are twofold: The primary objective is to investigate and propose a reliable model of VSC-HVDC systems. The second main contribution corresponds to the proposition of a robust control based on Model Recovery Anti-windup (MRAW), in order to improve the dynamic behavior performance under wide range of operating conditions, parameters uncertainties, input and state constraints and minimize the tracking reference error. The sufficient conditions are formulated in the format of LMIs. The effectiveness of the robust controllers is demonstrated using the simulation studies with the aid of the MATLAB software package. The rest of the paper is organized as follows. In section II, a state space of the HVDC dynamics is presented. In section III, the control problem representation is formulated. The proposed controller structure is developed in section IV. Simulation results are presented that illustrates the effectiveness of the proposed strategies in section V. Finally, the conclusions and future prospects are presented in section VI.

II. VSC-HVDC POWER STRUCTURE AND ITS DYNAMICS NONLINEAR MODEL

VSC-HVDC transmission power structure is depicted in Figure 1. For system modelling, a monopolar HVDC system with mettalic return is considered. It has two conversion stations that employ bidirection three-phased (voltage-source) AC-DC power converters. They are interlinked by means of a DC cable and their connection with AC grid is realised by using a step-up trans- former. The AC grid is represented by infinite buses and equivalent AC lines. As in real application, converters are operating in switched mode. Therefore, filtering elements are found on each station: capacitors on DC side and line reactors (inductors) on AC side. A supplementary lowpass filter is inserted between line reactor and transformer in order to alleviate the high frequency switching components. Both VSC of HVDC link are operated in pulse-width modulation (PWM) in order to interchange averaged sinusoidal variables with AC grid. VSC control is focused precisely to shaping this averaged behaviour. The state space can be given as the following,



Fig. 1. HVDC power structure simplified.

(1)

$$\dot{x}(t) = Ax(t) + Bu(t)$$

Where

where, (°)is denoted to the optimal operating point, $a_{11} = -\frac{R_s}{L_{g1}} - \frac{r_{g1}}{L_{g1}}, a_{13} = \frac{R_s}{L_{g1}}, a_{22} = -\frac{R_s}{L_{g1}} - \frac{r_{g1}}{L_{g1}}, a_{24} = \frac{R_s}{L_{g1}},$ $a_{31} = \frac{R_s}{L_{r1}}, a_{33} = -\frac{R_s}{L_{r1}} - \frac{r_{r1}}{L_{r1}}, a_{35} = u_1^o \frac{-1}{2L_{r1}},$ $a_{44} = -\frac{R_s}{L_{r1}} - \frac{r_{r1}}{L_{r1}}, a_{45} = u_2^o \frac{-1}{2L_{r1}}, a_{53} = u_1^o \frac{3}{2C_1}, a_{54} = u_2^o \frac{3}{2C_1},$ $a_{66} = -\frac{r_{DC}}{L_{DC}}, a_{67} = -\frac{1}{2L_{DC}}, a_{710} = u_3^o \frac{3}{2C_2}, a_{711} = u_4^o \frac{3}{2C_2},$ $a_{88} = -\frac{R_s}{L_{g2}} - \frac{r_{g2}}{L_{g2}}, a_{99} = -\frac{R_s}{L_{g2}} - \frac{r_{g2}}{L_{g2}}, a_{107} = u_3^o \frac{-1}{2L_{r2}},$ $a_{108} = \frac{R_s}{L_{r2}}, a_{10} = -\frac{R_s}{L_{r2}} - \frac{r_{r2}}{L_{r2}}, a_{117} = u_4^o \frac{-1}{2L_{r2}},$

The outputs of the HVDC are defined as the following;

$$y_{1} = V_{DC1} = x_{5}$$

$$y_{2} = P_{2} = \frac{3}{2}x_{10}^{o}R_{s}x_{8} + \frac{3}{2}x_{11}^{o}R_{s}x_{9} + \frac{3}{2}x_{8}^{o}R_{s}x_{10}$$

$$- 3x_{10}^{o}R_{s}x_{10} + \frac{3}{2}x_{9}^{o}R_{s}x_{11} - 3x_{11}^{o}R_{s}x_{11}$$

$$y_{3} = Q_{1} = -\frac{3}{2}x_{4}^{o}R_{s}x_{1} + \frac{3}{2}x_{9}^{o}R_{s}x_{2} + \frac{3}{2}x_{2}^{o}R_{s}x_{3} - \frac{3}{2}x_{1}^{o}R_{s}x_{4}$$

$$y_{4} = Q_{2} = -\frac{3}{2}x_{11}^{o}R_{s}x_{8} + \frac{3}{2}x_{10}^{o}R_{s}x_{9} + \frac{3}{2}x_{9}^{o}R_{s}x_{10}$$

$$- \frac{3}{2}x_{8}^{o}R_{s}x_{11}$$
(2)

where the states variables and the control input is defined as the following,

$$\begin{array}{lll} x_1 = i_{g1d} & x_2 = i_{g1q} & x_3 = i_{1d}^{\infty} & x_4 = i_{1q}^{\infty} \\ x_5 = v_{DC1} & x_6 = i_{DC} & x_7 = v_{DC2} & x_8 = i_{g2d} \\ x_9 = i_{g2q} & x_{10} = i_{2d}^{\infty} & x_{11} = i_{2q}^{\infty} \\ u_1 = \beta_{1d} & u_2 = \beta_{1q} & u_3 = \beta_{2d} & u_4 = \beta_{2q} \\ \end{array}$$

where i_{DC} is the DC line current, v_{DC1} is the DC voltage for VSC on left side, i_{g1d} and i_{g1q} are the grid current on d and q axis for AC filter on the left side, respectively, i_{g2d} , i_{g2q} are the grid current on d and q axis for AC filter on the right side, β_{1d} , β_{1q} , v_{DC1} are variables for VSC on left 'side, β_{2d} , β_{2q} , v_{DC2} are variables for VSC on right side (β_{ij} , $i \in \{1, 2\}, j \in \{1, 2\}$ are the duty rations of the converter, i.e., the controls of the VSC system), i_{2d}^{∞} , i_{2q}^{∞} , are AC grid currents on the right side, i_{1d}^{∞} , i_{1q}^{∞} , are AC grid currents on the left side, L_{g1} , L_{g2} , r_{g1} , r_{g2} , L_{r1} , L_{r2} , r_{r1} , r_{r2} , R_s , C_1 , C_2 , r_{DC} , L_{DC} , E and w are constants, P_2 , Q_1 , Q_2 are active power and reactive power, repectively. The system parameters are given values of these constants are provided as:

Variable Names	Constants	Values
AC grid inductance	$L_{g1} = L_{g2}$	0.11Ω
AC grid resistance	$r_{g1} = r_{g2}$	0.01Ω
Filter inductance	$L_{r1} = L_{r2}$	0.025Ω
Filter resistance	$r_{r1} = r_{r2}$	0.08Ω
AC filter resistance	R_s	2Ω
DC capacitor filter	$C_1 = C_2$	$220 * 10^{-6} F$
DC line resistance	r_{DC}	1.39Ω
DC line inductance	L_{DC}	$1.59 * 10^{-2} H$
Grid voltage	E	$187 * 10^{3}V$
Grid frequency	w	314 rad/sec

III. PROBLEM FORMULATION

The objective is to design robust controller based on LMI for HVDC transmission systems taking into consideration parameter uncertainties, constraints on states and control inputs. With this constraints the aim of this controller is to regulate output variable according to the following:

 Consider the following linear system with parameter uncertainties, constrained states and controls, therefore (1) rewritten as the following,

$$\dot{x}(t) = (A + \Delta A)x(t) + (B + \Delta B)sat(u(t))$$

$$y(t) = Cx(t)$$
(3)

where $x(t) \in \mathbb{R}^{n \times 1}$ and $u(t) \in \mathbb{R}^{m \times 1}$ are the state vectors and the HVDC control input, respectively, $C \in \mathbb{R}^{g \times n}$ is the system output matrix, $\Delta A \in \mathbb{R}^{n \times n}$ and $\Delta B \in \mathbb{R}^{n \times m}$ are the uncertainties of the constant system matrices $A \in \mathbb{R}^{n \times n}$ and $B \in \mathbb{R}^{n \times m}$, respectively, in our application n = 11, m = 4, g = 4 and function sat represents the nominal saturation as defined after in (11).

2) In this study, the parameter uncertainties are assumed given by,

$$\Delta A = EF_1(t)H_1 \qquad \Delta B = EF_2(t)H_2 \qquad (4)$$

where E, H_1 and H_2 are known real constant matrices which characterize the parameter uncertainties for the nominal matrices A and B, $F_1(t)$ and $F_2(t)$ are unknown real matrices with Lebesgue measurable elements, satisfying

$$F_i(t)^T F_i(t) \le I$$
 $i = 1, 2$ (5)

where I is identity matrix.

3) Let the state be constrained as follows

$$\gamma = \{ x \in \Re^{n \times 1} / -q \le x \le q; \quad q \in \Re^{n \times 1} \}$$
(6)

From (6), we can seen that $-q \leq x \leq q$ is equivalent to $x \leq q$ and $-x \leq q$ which in augmented form can be expressed as $[I; -I]x \leq [q;q]$, where I stands for the identity matrix. If we define M = [I; -I] and N = [q;q], then (6) can be written as the following

$$\gamma(M,N) = \{x \in \Re^{n \times 1} / Mx \le N\}$$
(7)

Therefore $M \in \Re^{h \times n}$ and $N \in \Re^{h \times 1}$ are known. In this paper, we consider the current and voltage variables $(x_3, x_4, x_3, x_4, x_{10}, x_{11})$ are constrained as the following;

$$-2000Amp \le x_3 \le 2000Amp -2000Amp \le x_4 \le 2000Amp 10KV \le x_5 \le 380KV 10KV \le x_7 \le 380KV -2000Amp \le x_{10} \le 2000Amp -2000Amp \le x_{11} \le 2000Amp$$
(8)

4) also, let the control input be constrained as follows

$$\Lambda = \{ u \in \Re^{m \times 1} / -z \le u \le z; \quad z \in \Re^{m \times 1} \}$$
(9)

In our application, the constraints on control inputs u_1 , u_2 , u_3 and u_4 are considered between -z = -1 & z = 1 as the following

$$\begin{array}{ll} -1 \le u_1 \le 1 & -1 \le u_2 \le 1 \\ -1 \le u_3 \le 1 & -1 \le u_4 \le 1 \end{array}$$
(10)

and the actuator saturation, which is defined by

$$sat(u) = \begin{cases} u_{min} & if \quad u(t) \le u_{min} \\ u(t) & if \quad u_{max} \le u(t) \le u_{min} \\ u_{max} & if \quad u(t) \ge u_{max} \end{cases}$$
(11)

where $u_{min} = -1$ and $u_{max} = 1$ are minimum and maximum control inputs, respectively.

5) Controlling the DC voltage for VSC on left side $(y_1=V_{DC1})$, active $(y_2=P_2)$ and reactive powers $(y_3=Q_1, y_4=Q_2)$ to their set points (so that the controlled output y_i (i = 1, 2, 3, 4) tracks its reference value $y_{i,ref}$

(i = 1, 2, 3, 4). Accordingly, the tracking error ϵ_i (i = 1, 2, 3, 4) approaches zero when the time tends to infinity. In order to force to zero the steady-state tracking error, we add new state which corresponds to the integral of the tracking error ϵ_i (i = 1, 2, 3, 4). Therefore we define $\xi_i = \int \epsilon_i dt$ (i = 1, 2, 3, 4) with $\epsilon_i = y_i - y_{i,ref}$ therefore,

$$x_{12} = \xi_1 = \int \epsilon_1 dt = \int (y_1 - y_{1,ref}) dt = \int (V_{DC1} - V_{DC1,ref}) dt x_{13} = \xi_2 = \int \epsilon_2 dt = \int (y_2 - y_{2,ref}) dt = \int (P_2 - P_{2,ref}) dt x_{14} = \xi_3 = \int \epsilon_3 dt = \int (y_3 - y_{3,ref}) dt = \int (Q_1 - Q_{1,ref}) dt x_{15} = \xi_4 = \int \epsilon_4 dt = \int (y_4 - y_{4,ref}) dt = \int (Q_2 - Q_{2,ref}) dt$$
(12)

The augmented by integrators state space model is deducted from the six equations below:

$$\begin{cases} \dot{x}(t) = Ax(t) + Bu(t) \\ \dot{x}_{12}(t) = y_1 - y_{1,ref} = V_{DC1} \\ - V_{DC1,ref} = x_5 - V_{DC1,ref} \\ \dot{x}_{13}(t) = y_2 - y_{2,ref} = P_2 - P_{2,ref} = \frac{3}{2}x_{10}^*R_s x_8 \\ + \frac{3}{2}x_{11}^*R_s x_9 + \frac{3}{2}x_8^*R_s x_{10} - 3x_{10}^*R_s x_{10} \\ + \frac{3}{2}x_9^*R_s x_{11} - 3x_{11}^*R_s x_{11} - P_{2,ref} \\ \dot{x}_{14}(t) = y_3 - y_{3,ref} = Q_1 - Q_{1,ref} = -\frac{3}{2}x_4^*R_s x_1 \\ + \frac{3}{2}x_3^*R_s x_2 + \frac{3}{2}x_2^*R_s x_3 - \frac{3}{2}x_1^*R_s x_4 - Q_{1,ref} \\ \dot{x}_{15}(t) = y_4 - y_{4,ref} = Q_2 - Q_{2,ref} = -\frac{3}{2}x_{11}^*R_s x_8 \\ + \frac{3}{2}x_{10}^*R_s x_9 + \frac{3}{2}x_9^*R_s x_{10} - \frac{3}{2}x_8^*R_s x_{11} \\ - Q_{2,ref} \end{cases}$$
(13)

We consider the set point is given by $y_{1,ref}=V_{DC1,ref}=320KV$, $y_{2,ref}=P_{2,ref}=100MW$, $y_{3,ref}=Q_{1,ref}=250MVA$, $y_{4,ref}=Q_{2,ref}=250MVA$.

IV. THE PROPOSED ROBUST CONTROLLER WITH STATE AND CONTROL CONSTRAINTS STRATEGY

This section presents a systematic robust control scheme for HVDC to compensate the effect parameter uncertainties and regulate output variable taking in consideration the constraints on states and control inputs. For the robust control scheme implementation based on the MRAW (Model Recovery Antiwindup). Sufficient conditions are derived for robust stabilization in the sense of Lyapunov stability. The sufficient conditions are formulated in the format of LMIs. First, a robust controller is designed to show a desirable nominal performance by considering the state and the control constraints in a LMI formalism and take in consideration the parameter uncertainties. Then, an additional MRAW compensator is designed to mitigate the adverse effects due to state and the control constraints as shown in the following subsections.

A. The Proposed Robust Controller with State and Control Constraints Strategy

The closed-loop system with robust controllers is depicted in Figure 2. To design the proposed controller, we consider two



Fig. 2. Overall HVDC system schematic diagram with compensation structure for states and control inputs constrained based on MRAW strategy.

classes of robust controllers that meet the saturation constraints (8) and (10) and compensate the effect parameter uncertainties which is defined in (4), one is given by

$$u(t) = KX(t) = K_s X(t) \tag{14}$$

and the other is given by

$$u(t) = \begin{bmatrix} K_s & I \end{bmatrix} \begin{bmatrix} X(t) \\ \phi(t) \end{bmatrix} = K_a \begin{bmatrix} X(t) \\ \phi(t) \end{bmatrix}$$
(15)

where X(t) is given in (13) and $\phi(t)$ is based on the dynamics of the MRAW, which is given by,

$$\dot{x}_d(t) = Ax_d(t) + B\varphi$$

$$\phi(t) = K_d C x_d(t) + K_d D\varphi$$
(16)

where $x_d(t)$ is the state vector of the MRAW. The advantage of adding MRAW architecture is to compensate the undesired effects of control saturation. The closed-loop system with these controllers is given in Figure 2, where the dashed part is absent and $K = K_s$ for (14) while the dashed part is present and $K = K_a$ for (15).

B. Proposed Stability and Robustness for HVDC Systems with Parameter Uncertainties and Constraints Strategy

In this section, we derive the closed loop system stability conditions and calculate the robust controller gains and MRAW compensation gains.

1) Dynamics of Closed-Loop System in Absence of MRAW Compensator:

In this section, robust stabilization sufficient condition and corresponding synthesis approach for uncertain HVDC systems with sector saturating actuator and states saturating are design in the absence of MRAW compensator. The stability and robustness analysis with reference to an uncertain control system described by (8) under the constrains on the states and the control inputs is summarized in the following theorem 1. The proof is shown in the appendix A.

Theorem 1: The uncertain HVDC system (3) and (4) subject the constrained states and the control inputs is robustly stabilizable if the controller gains are set to $K = OZ^{-1}$, there exist positive definite symmetric matrix $P = Z^{-1}$ and scalars ι , δ and β_i , such that the following LMI is satisfied,

$$\begin{bmatrix} \widehat{A}Z + Z\widehat{A}^T + (\widehat{B}O) + (\widehat{B}O)^T + \delta EE^T & ZH_1^T + OH_2^T \\ H_1Z + H_2O & -\delta I \end{bmatrix} \leq 0$$
(17)

$$\begin{bmatrix} \iota \beta_i N_i - M_i Z M_i^T & \beta_i \\ \beta_i & 1 \end{bmatrix} \ge 0 \qquad \qquad for \quad 1 \le i \le h$$
(18)

$$\begin{bmatrix} 1 & O_j \\ O_j^T & Z \end{bmatrix} \ge 0 \qquad \qquad for \quad 1 \le j \le m \qquad (19)$$

where h and m are defined in (6) and (7), let O_j , N_i and M_i are the j^{th} and i^{th} row of O, N and M, respectively and ι is constant.

Proof. The proof can be given as the following. In order to carry out the analysis for robust control strategy, the closed-loop system should be obtained first. Therefore, robust control system of the state with integrators without control saturation can be obtained. Substituting (14) into (13) and (3), we obtain the dynamics of the closed loop system:

$$\dot{X}(t) = (\widehat{A} + \Delta \widehat{A})X + (\widehat{B} + \Delta \widehat{B})(KX(t))$$

$$Y(t) = \widehat{C}X(t)$$
(20)

Based on the useful lemma [20], we can proof the part of the parameter uncertainties (17). Based on [21], can easily be shown that $(max|KX| = \sqrt{KP^{-1}K^T})_{X^TPX \leq 1}$. Squaring this expression, inserting the definition of Z and O, and performing a Schur complement shows that the $KX \leq 1 \forall :$ $X^TPX \leq 1$ is equivalent to (19).

2) Dynamics of Closed-Loop System in Presence of MRAW Compensator:

To design the compensation gains (K_d) in (16), the closed-loop system related the augmented system state should be defined. In this case, we consider the HVDC system (3) without the parameter uncertainties ($\Delta A = 0$ and $\Delta B = 0$). After a suitable change of coordinates the interconnection between $\varphi = sat(u) - u(t)$ and (16), which is named the compact antiwindup closed-loop system as given in Figure 2. The compensation gains (K_d) is obtained based on the following theorem 2

Theorem 2: If there exists an MRAW controller (16), a symmetric positive definite matrix G and a positive scalar α such that the following LMI hold. Then, the antiwindup closed-loop system is asymptotically stable,

$$\begin{bmatrix} G\bar{A}^{T} + \bar{A}G & \bar{B}W + G\bar{C}^{T} & 0 & G\bar{C}^{T} \\ * & \bar{D}W + W\bar{D}^{T} - 2W & 0 & W\bar{D}^{T} \\ * & * & -\alpha I & 0 \\ * & * & * & -\alpha I \end{bmatrix} \leq 0$$
(21)

$$G = G^T \ge 0 \tag{22}$$

Proof. The closed loop system (20) without the parameter uncertainties ($\Delta \hat{A} = 0$ and $\Delta \hat{B} = 0$) with MRAW (15) and (16) can be rewetting as the following

$$\dot{X}(t) = \widehat{A}X(t) + \widehat{B}sat(u)$$

$$Y(t) = \widehat{C}X(t) + \widehat{D}sat(u)$$
(23)

From (23) and (16), we obtain,

$$\dot{X}(t) = [\widehat{A} + \widehat{B}K_s]X(t) + \widehat{B}K_d\widehat{C}x_d(t) + [\widehat{B}K_d\widehat{D} + \widehat{B}]\varphi$$

$$Y(t) = [\widehat{C} + \widehat{D}K_s]X(t) + \widehat{D}K_d\widehat{C}x_d(t) + [\widehat{D}K_d\widehat{D} + \widehat{D}]\varphi$$
(24)

Then from (16) and (24), the augmented closed loop model is written as:

$$\dot{X}_a(t) = \bar{A}X_a(t) + \bar{B}\varphi$$

$$Y_a(t) = \bar{C}X_a(t) + \bar{D}\varphi$$
(25)

Where
$$X_a(t) = \begin{bmatrix} X(t) \\ x_d(t) \end{bmatrix}$$
, $\bar{A} = \begin{bmatrix} \hat{A} + \hat{B}K_s & \hat{B}K_d\hat{C} \\ 0 & \hat{A} \end{bmatrix}$,
 $\bar{B} = \begin{bmatrix} \hat{B}K_d\hat{D} + \hat{B} \\ \hat{B} \end{bmatrix}$, $\bar{C} = \begin{bmatrix} \hat{C} + \hat{D}K_s & \hat{D}K_d\hat{C} \end{bmatrix}$,
 $\bar{D} = \begin{bmatrix} \hat{D}K_d\hat{D} & \hat{D} \end{bmatrix}$.

By applying the Lyapunov function $V(X_a(t)) = X_a(t)^T P_a X_a(t)$ on (25) and using the Schur complement method we can obtain (21) and (22).

V. SIMULATIONS AND RESULTS

In this section, we apply our results to HVDC (1). The control objective of this paper is to design a robust control law for the HVDC system (1) to ensure that all signals in the closed-loop system are bounded and regulate output variable in the presence of the parameter uncertainties, the constraints on states and control inputs.

Figure 3 and Figure 4 show the time response of constrained states (AC grid currents on the left side (i_{1q}^{∞}) , and on the right (i_{2d}^{∞})) and control actions, respectively, in the presence of parametric uncertainties, states and control input constrains. The parametric uncertainties within 20% is considered, this means that E, H_1 and H_2 matrices are selected about 20% from the nominal value from system matrix A and input matrix B. In addition the additive disturbance to the ouptut matrix is $Dis = [0.01 \ 0.01 \ 0.01 \ 0.01]^T$ (from the nominal value of the ouput), therefore Y = CX + DisCXsin(3t), where DisCXsin(3t) is additive disturbance term. If this percentage is increased, the system lost its perfermorane. Figure 5 and Figure 6 show the system ouputs (DC voltage, active and reactive power) and tracking error, respectively, from initial condition $x_o = [1046.7 - 5331.6 \ 1977 \ 749.3 \ 319891 - 61 \ 320063 \ 878 \ -5278 \ 498 \ -2000]^T$, together with control evolution. It can be seen that robust feedback is achieved with give a good tracking. Figure 7 shows the time response of control actions with and without limitation on the DC voltage. It can be seen that from Figure 7 without the constraints on V_{DC1} and without MRAW, that there are more oscillation on the control action compared to the limitation case and with MRAW. In summary results, we can be seen that the system trajectory follows the trajectory of the reference input. Thus, the proposed controller is robust against norm-bounded parametric uncertainties with respected constraints.



Fig. 3. Time response of the constrained states (AC grid currents on the left and the right side $(x_4 = i_{1q}^{\infty}, x_{10} = i_{2d}^{\infty})$).



Fig. 4. Time response of the control action.



Fig. 5. Time response of DC voltage, active and reactive power.



Fig. 6. DC voltage, active and reactive power tracking error.



Fig. 7. Time response of the control action with and without V_{DC} limitation.

VI. CONCLUSION

In this paper the mathematical models of the main components of the VSC-based HVDC transmission system were presented. There are two main difficulties in the controller design for real systems: parametric uncertainties and saturations. Parameter uncertainties often degrade system performance and may even lead to instability and saturation reduce the system performance. In this paper stabilization of HVDC system with parametric uncertainties and having restricted states and/or controls is studied. In the sense of Lyapunov method, for the HVDC system, sufficient conditions are formulated in the format of LMIs (Linear Matrix Inequalities). The MRAW is used to compensate the effect of the control saturation. The advantage of the MRAW architecture lies in the fact that the antiwindup filter keeps track (via MRAW states) of the amount of HVDC states response that is missing in the saturated closedloop due to the undesired effects of saturation. The design scheme was applied to the stabilizing control of the HVDC. The simulation results proved the effectiveness, robustness and better tracking performance of the proposed controller in controlling HVDC systems with parametric uncertainties and the inputs and states constraints. It is planned in the near future, first to validate this control methodology on a HVDC inserted in a more detailed AC grid and next to implement the overall proposed control strategy on the actual hardware platform. In addition, modify this methodology to deals with nonlinear model. In future work, the stability with respect to the constraints on the system and eliminate the effect of disturbance on system performance will study by synthesizing a Lyapunov quadratic function and by using LMI.

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