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Experimental study of recombining nitrogen plasmas. Part I: Vibronic population distributions and nonequilibrium molecular radiation

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Abstract

We present optical emission spectroscopy measurements in recombining nitrogen plasma flows at atmospheric pressure. An inductively coupled plasma torch is used to create an equilibrium plasma, which is then forced to recombine by flowing through a water-cooled tube. For certain conditions, the plasma is forced out of chemical equilibrium. The emission of $N_2(B^3\Pi_g)$, $N_2(C^3\Pi_u)$ and $N_2^+(B^2\Sigma_u^+)$ is studied to measure the nonequilibrium vibrational density distributions within these electronic states. These densities are found to be highly overpopulated in comparison with their corresponding equilibrium values, which is consistent with previous results in recombining flows. The measured densities are also compared with the predictions of a 2-temperature model. This 2-temperature model underpredicts the measured densities but is closer to the measured distributions than the equilibrium densities. The total measured radiation is approximately 100,000 times stronger than the corresponding equilibrium radiation. The 2-T model estimate of this radiation is much closer yet still underestimates by a factor of 10 the measured radiation. These data are intended as a new dataset to test the recombining plasma models used to simulate afterbody flows during atmospheric reentry.

Introduction

In recent years, there has been increased interest in manned Mars return missions [1]. There are numerous challenges to achieving such a mission. One such challenge is the reentry into the Earth atmosphere on the return voyage [2]. During reentry, the capsule enters the atmosphere at velocities above 10 km/s [3]. At these high velocities, the shock-heated plasma layer formed around the vehicle can result in a radiative heat flux higher than the convective flux [4] [5]. The radiation on the forebody has been the focus of much research [6] [7] [8] [9] and is relatively well modeled. However, uncertainties on the afterbody radiative heat flux can still be as high as 200% [3] [4]. One of the reasons for this uncertainty is the rapid expansion into the afterbody region which forces recombination and a subsequent departure from thermochemical equilibrium conditions. A fundamental study of recombination kinetics is therefore necessary to correctly predict the degree of nonequilibrium of recombining plasmas and the resulting radiation. Recent work has focused on the kinetics and radiation of recombining plasma flows, both experimentally and numerically: see for example Refs. [10] [11] [12]. This paper focuses on nitrogen recombination kinetics.

In a previous paper [13], we presented experiments for recombining nitrogen and air plasmas flows using the plasma torch facility at the EM2C laboratory. The plasma torch provides an equilibrium plasma at atmospheric pressure. The plasma then flows through a water-cooled tube at relatively high velocity (~ 1 km/s). The plasma exits the tube in a state of chemical nonequilibrium. The resulting radiation at the exit of the tube was found to be up to 100,000 times higher than if the plasma were in equilibrium at the measured gas temperature determined via Raman spectroscopy measurements of the $N_2(X^1\Sigma_g^+)$ ground state. Finally, CFD codes failed to predict any of the measured temperatures under any of the experimental conditions – even those where the plasma remained in equilibrium [13]. This same discrepancy between measurements and CFD codes was previously observed by other authors [14] [15].

These measurements therefore raised questions about the ability of the CFD codes to predict this temperature drop, the level of nonequilibrium, and the resulting radiation.

In this paper, we analyze the radiation of the plasma over the range 250-900 nm to obtain the absolute densities of vibrational states of $N_2(B^3\Pi_g)$, $N_2(C^3\Pi_u)$ and $N_2^+(B^2\Sigma_u^+)$. This was previously done only for the N_2 first positive system [13] up to 800 nm. We study two experimental conditions corresponding to two total mass flow rates. The mass flow rate has a significant impact on the degree of nonequilibrium observed in the plasma. In section 1, we present the experimental setup and conditions. The measured nonequilibrium radiation coming from the plasma is presented in section 2. The emission spectra are analyzed to provide information on the absolute densities of the vibrational levels of various electronic states of N_2 and N_2^+ and on the total radiative heat flux of the recombining plasma flows.

I) Experimental setup

The plasma torch facility is a TFAFA Model 66 inductively coupled plasma (ICP) torch powered by a 120-kVA radio-frequency (4 MHz) LEPEL Model T-50-3 power supply. The power supply can generate a maximum of 12 kV DC and 7.5 A to the oscillator plates. Details of the plasma torch facility are provided in previous publications [12] [16] [17]. The plasma produced within the torch exits through a 1-cm diameter nozzle at a speed between 400 and 800 m/s. The plasmas studied here are comprised of 1.2 or 1.9 g/s of N_2 or air, premixed with 1.5 g/s of argon to provide stable operating conditions for the torch. A water-cooled tube made of brass is mounted on top of the plasma torch exit nozzle. The length of the tube is either 10 or 15 cm. Emission and Raman measurements are performed at the entrance and exit of the modular tube. The plasma is forced to recombine by imposing rapid cooling via the cold wall (maintained at approximately 300 K). This setup is therefore intended as a simplified experimental model of a recombining flow in atmospheric reentry. Details of the experimental setup are presented in figure 1.

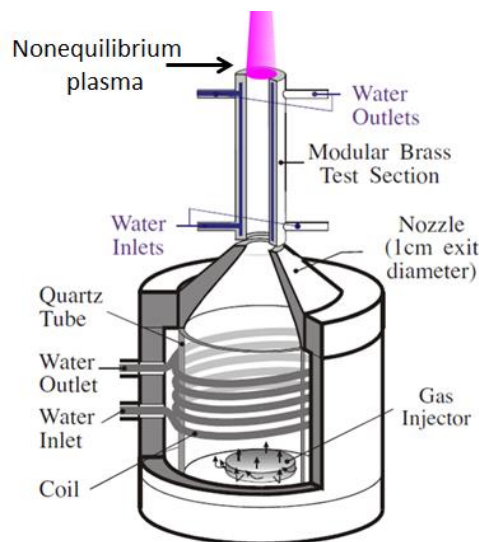


Figure 1: Water-cooled test-section mounted on top of the plasma torch exit nozzle

Optical emission spectroscopy was performed for several experimental conditions with the setup presented in Figure 2. The spectrometer is an Acton Instrument 2500i of 50-cm focal length with a 600 gr/mm grating blazed at 300 nm. We measured spectra from 250 to 900 nm to capture the emission bands of the first and second positive systems of N_2 , and of the first negative system of N_2^+ . The emission spectra are calibrated from pixel counts to absolute intensities using an Optronics Laboratories tungsten lamp (model OL550) between 400 and 900 nm, and a calibrated argon mini-arc for wavelengths below 400 nm. Spectra are taken each 0.5 mm along the line of sight and are Abel-inverted to get spatially

resolved local plasma emission. The three different mixtures considered in this study are summarized in Table 1.

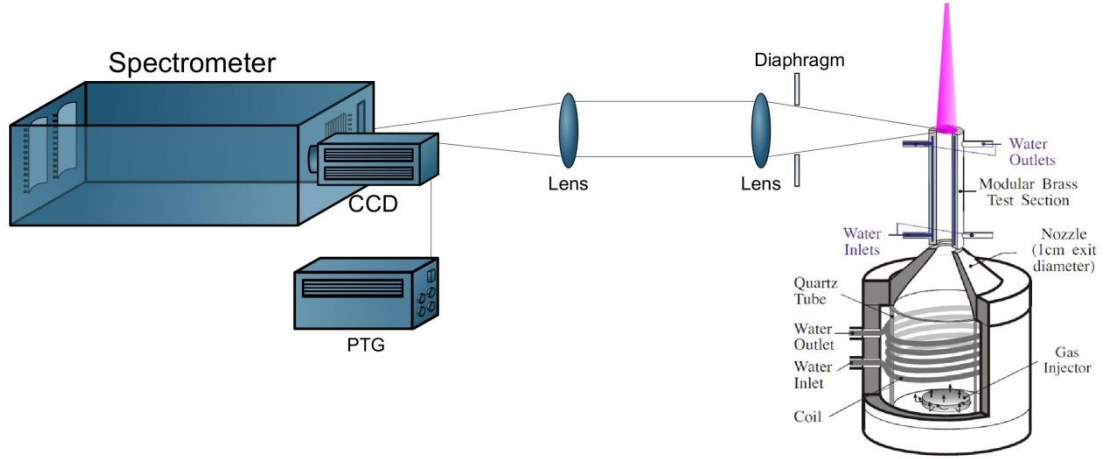


Figure 2: Experimental setup for optical emission spectroscopy (here at the tube exit)

Table 1: Mass flow rates and conditions for the different cases studied. The chemical conditions are taken from Ref [13].

	Mass flow rate	Reynolds number based on the tube diameter (1 cm)	Conditions at tube inlet	Conditions at tube exit
Air/Ar	$\dot{m}_{Air} = 1.9 \text{ g/s}$ $\dot{m}_{Ar} = 1.5 \text{ g/s}$	~ 3600 (turbulent)	LTE	LTE
N ₂ /Ar Low Flowrate (LF)	$\dot{m}_{N_2} = 1.2 \text{ g/s}$ $\dot{m}_{Ar} = 1.5 \text{ g/s}$	~ 2700 (slightly turbulent)	LTE	Thermal equilibrium, Chemical nonequilibrium
N ₂ /Ar High Flowrate (HF)	$\dot{m}_{N_2} = 1.9 \text{ g/s}$ $\dot{m}_{Ar} = 1.5 \text{ g/s}$	~ 3600 (turbulent)	LTE	Thermal equilibrium, Chemical nonequilibrium

II) Nonequilibrium radiation of N₂(B), N₂(C) and N₂⁺(B)

This section discusses the experimental results for each of the three cases outlined in Table 1.

Air/Ar plasma:

The test conditions for this test are presented in Table 1. The inlet gas is air (1.9 g/s) premixed with argon (1.5 g/s). The plasma is expected to stay in LTE throughout the test-section [13]. We measured a spectrum from 250 nm to 800 nm and compared it with the LTE spectrum computed with SPECAIR [18]. Results at 15 cm are presented in Figure 3. The good agreement between the experimental and computed LTE spectra supports the equilibrium assumption for this case. Note that, for this case, all temperature measurements agree within another. We present here only the spectrum measured at the center of the tube (i.e. the Abel-inverted spectrum at radial position $r=0$ cm), but we observed similar agreement across the tube for all Abel-inverted spectra.

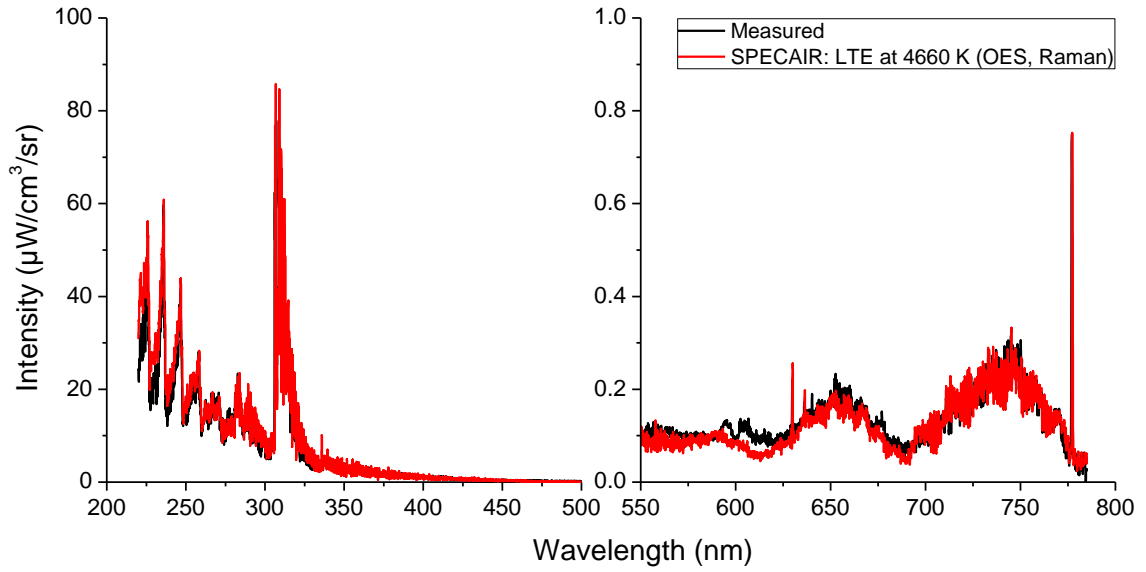


Figure 3: Measured (black) and computed (red) spectrum at the exit of the 15-cm tube for the Air/Ar plasma case.

N₂/Ar low flowrate plasma:

In this case, 1.2 g/s of nitrogen is premixed with 1.5 g/s of argon. In previous work [13], we measured the emission spectrum between 500 and 800 nm and we observed a departure from chemical equilibrium at 10 and 15 cm leading to an overpopulation of the vibrational levels of N₂(B). Here we extend these measurements from 250 to 900 nm in order to (a) validate the previous measurements, (b) access vibrational level $v = 1$ of N₂(B) at 870 nm, and (c) measure the transitions of N₂(C) → N₂(B) and N₂⁺(B) → N₂⁺(X) between 280 and 450 nm. We used the CEA code [19] to calculate the equilibrium composition of the plasma at the temperature measured using Raman spectroscopy. Details on the Raman spectroscopy measurements are given in our previous publication [20]. We use the radiation code SPECIAIR to compute equilibrium spectra with the given composition and temperature. We observe a large difference between the measured spectrum and the spectrum computed assuming equilibrium. Using an optimization algorithm coupled with Specair, we adjusted the populations of the vibrational levels of N₂(C), N₂⁺(B) and N₂(B) to match the measured emission spectra. This optimization algorithm minimizes the L₂ error between the experimental and computed spectra using a truncated Newton method.

To quantify the uncertainties, we used the following method: first a random noise was added to the computed spectra. The amplitude of the noise was adjusted to match the experimental uncertainty, found as the addition of the measured random noise and the uncertainties coming from the Abel inversion algorithm. The uncertainties vary from experiment to experiment, but the typical value is 5 % at the centerline of the tube and below 30 % elsewhere. Then the optimization algorithm was run on these new spectra and the error from the best fit was computed. This was performed a total of 100 times for each spectrum. Above 100 times both the standard deviation and the mean of the error did not change significantly and therefore 100 times was found to be sufficient. The standard deviation of the results was taken as the uncertainty on the measurement. This procedure tests the sensitivity of our algorithm to the experimental noise and yields a good estimate of the uncertainty of the fits. In figure 4, we plot the measured spectrum, the computed spectrum using SPECIAIR assuming equilibrium, and the spectrum resulting from the optimization algorithm at the exit of the 10-cm tube. We also show the fitted populations of the vibrational levels of N₂(C), N₂⁺(B) and N₂(B) used for the SPECIAIR calculations.

The plasma is near equilibrium but there is a slight overpopulation of the vibrational levels of $N_2(C)$, $N_2^+(B)$ and $N_2(B)$.

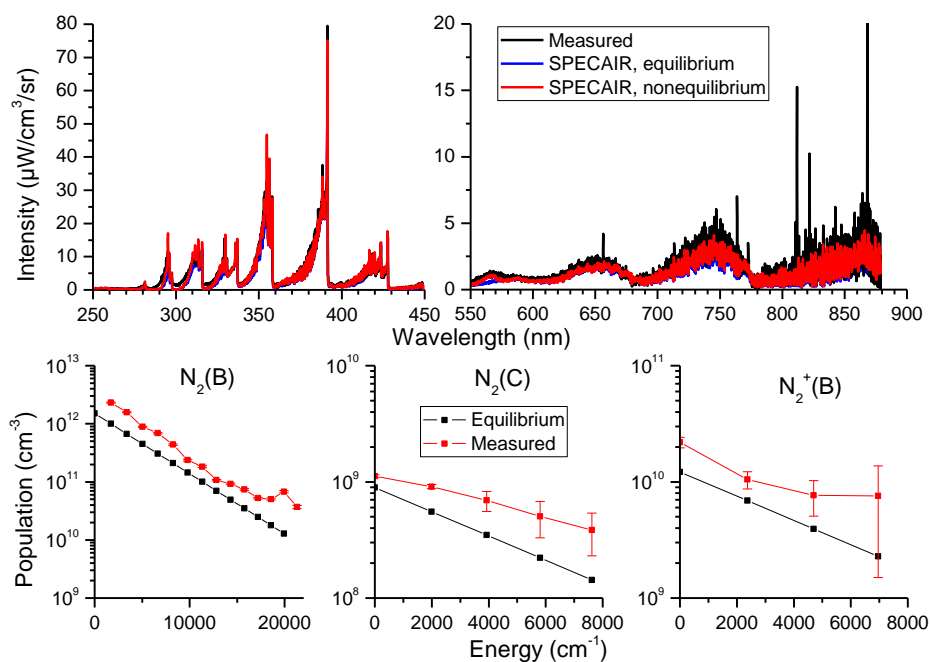


Figure 4: Top: comparison between measured and computed spectra at the exit of the 10-cm tube for the N_2/Ar low flowrate case at the center of the tube ($r=0$ cm). Equilibrium spectrum (blue) and fitted spectrum (red). Bottom: equilibrium and measured populations of emitting levels used for SPECAIR calculations.

We performed the same measurements at the exit of the 15-cm tube. Results are shown in Figure 5. We observe larger vibrational overpopulations of $N_2(C)$, $N_2^+(B)$ and $N_2(B)$ than for the 10-cm tube. Chemical nonequilibrium therefore increases with axial position. Note the presence of NO systems between 250 and 300 nm. This is explained by the presence of small quantities of water vapor impurities in the injection gas. Results are in good agreement if we add approximately 1% mole fraction of water into the plasma.

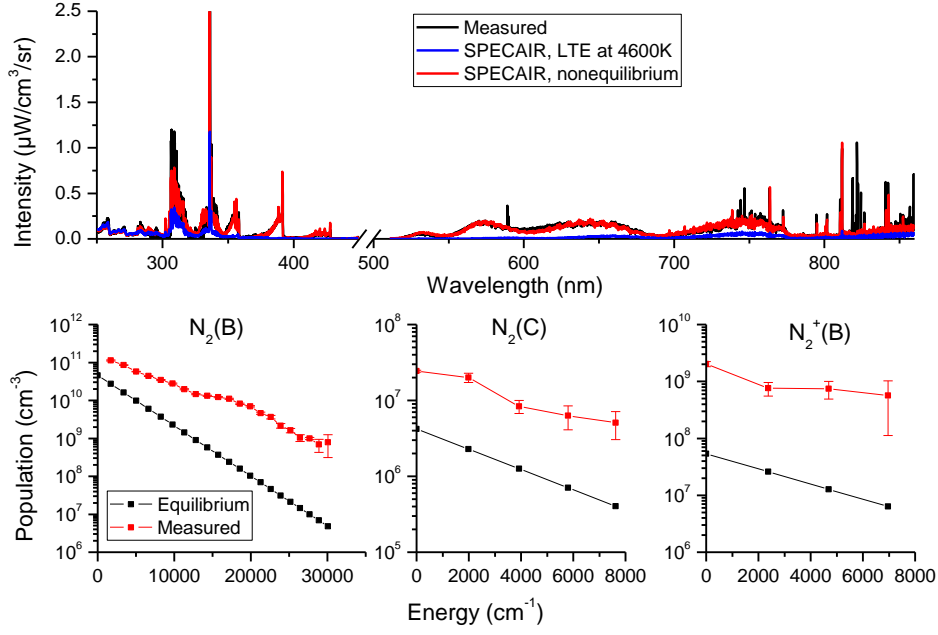


Figure 5: Top: comparison between measured and computed spectra at the exit of the 15-cm tube for the N_2/Ar low flowrate case at the center of the tube ($r=0$ cm). Equilibrium spectrum (blue) and fitted spectrum (red). Bottom: equilibrium and measured populations of emitting levels used for SPECAIR calculations.

We only present here the results for the centerline of the tube. However, this fitting procedure was performed for all spectra and as a function of radius. We also performed this analysis for all spectral bands observed, which correspond to emission from various vibrational levels of $N_2(B)$, $N_2(C)$ and $N_2^+(B)$. This enabled us to obtain the absolute populations of these states as a function of both radius and axial distance (i.e. tube length). The results for $N_2(B)$ are similar to the results of Ref. [13] and therefore will not be presented here. For $N_2(C)$ and $N_2^+(B)$, we present the radial distribution of vibrational levels densities for each axial position in Appendix A.

From a modeling perspective, it is important to correctly predict the populations of the excited states as the total radiation is proportional to these populations. Hypersonic CFD codes for atmospheric reentry often use multi-temperature models such as the 2-temperature model proposed by Park [6] [21] [22] [23]. This model uses a translational-rotational temperature T_{tr} and a vibrational-electronic temperature T_{ve} . The R-T relaxation times are assumed to be fast enough to consider a single temperature for translation and rotation, and likewise for the vibrational and electronic temperature. Vibrational-translational (VT) relaxation is determined using the Landau-Teller equation:

$$\frac{dE_{ve,s}}{dt} = \sum_c \left(x_c \frac{E_{ve,s}(T_{tr}) - E_{ve,s}(T_{ve})}{\tau_{V-T}^{s-c}} \right) \quad (1)$$

where $E_{ve,s}$ is the vibrational-electronic energy of species s , x_c the mole fraction of species c , and τ_{V-T}^{s-c} the relaxation time of species s colliding with species c in their ground state. The relaxation time is determined using the correlations given in the literature [24] [25]. Note that we make the simplifying assumptions that the VT time is the same for all electronic states of the considered species, and that the electronic states are in Boltzmann equilibrium with the ground state at the given T_{ve} .

We performed a 0-D simulation with the 2-temperature model from 0 to 15 cm along the centerline of the flow. The axial profile of translational temperature is obtained from a cubic interpolation of the

temperatures measured with Raman spectroscopy at 0, 10, and 15 cm (see Figure 6). The radial velocity profile is obtained by self-similarity with the temperature profile, as discussed and calculated in Ref. [13]. The centerline velocity at $x=0$ cm is about 800 m/s and about 500 m/s at $x=15$ cm. Three species are considered, N_2 , N, and argon. We consider uncertainties on the measured translational temperatures (about 5% at 0 cm, and 10% at 10 and 15 cm), on the shape of the interpolated temperature profile, and on the velocity (about 20%). Given these uncertainties, the Landau-Teller model gives $T_{ve} = 5950 \pm 200$ K at 10 cm and 5000 ± 150 K at 15 cm. The different translational temperature profiles taken in the calculations and the resulting vibrational temperature profiles are shown in Figure 6.

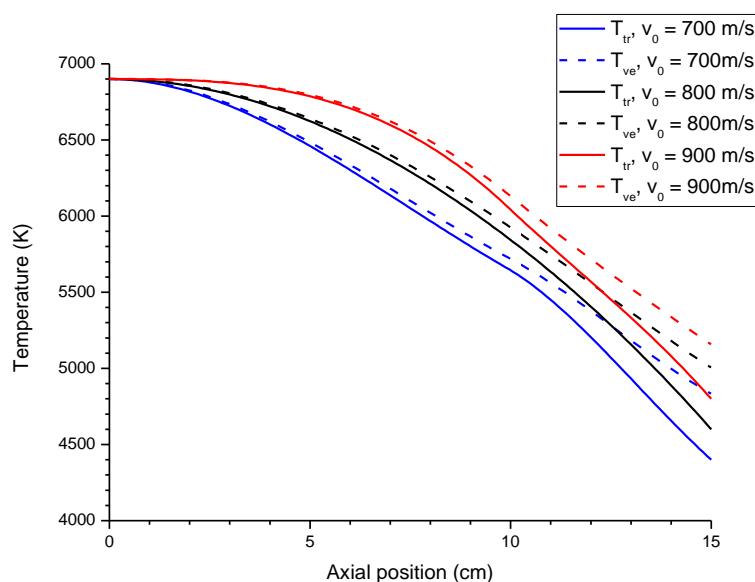


Figure 6: Translational temperature profiles (solid lines) based on the measured Raman temperatures, and vibrational temperature profiles (dashed lines) obtained from the Landau-Teller model for the N_2/Ar low flowrate case. The black curves correspond to the nominal case. The red and blue curves represent the upper and lower uncertainty bounds, respectively.

Figure 7 shows the measured vibrational population distributions of the N_2 states at 0, 10 and 15 cm, along with the distributions corresponding to equilibrium and those obtained with the 2-temperature model. The populations of the first three vibrational levels of $N_2(X)$ were measured by Raman spectroscopy in our previous work [20] and the rotational and vibrational temperatures of $N_2(X)$ were found to be equal. Therefore, the rotational and vibrational distribution of $N_2(X)$ are assumed to follow a Boltzmann distribution at the measured temperature. In all cases, the equilibrium distribution largely underestimates the measured populations. At 10 cm, the populations computed using the 2-T model underestimate the measurements by a factor of about 3. At 15 cm, better agreement is found for the first vibrational levels of N_2B and N_2C . However, a large discrepancy is observed for the higher vibrational levels of N_2B . This is because the $N_2(B, v=13)$ vibrational level is populated by inverse predissociation of $N(^4S)$, and therefore its overpopulation with respect to equilibrium varies as the square of the overpopulation of nitrogen atoms, as explained in Ref [12]. Since the atomic nitrogen population is nearly frozen along the axis of the tube, the overpopulation of $N(^4S)$ increases strongly along the axis of the tube. Therefore, the departure from the 2-temperature model predictions becomes stronger at 15 cm than at 10 cm. This mechanism of inverse predissociation is of course not considered in the 2-T model.

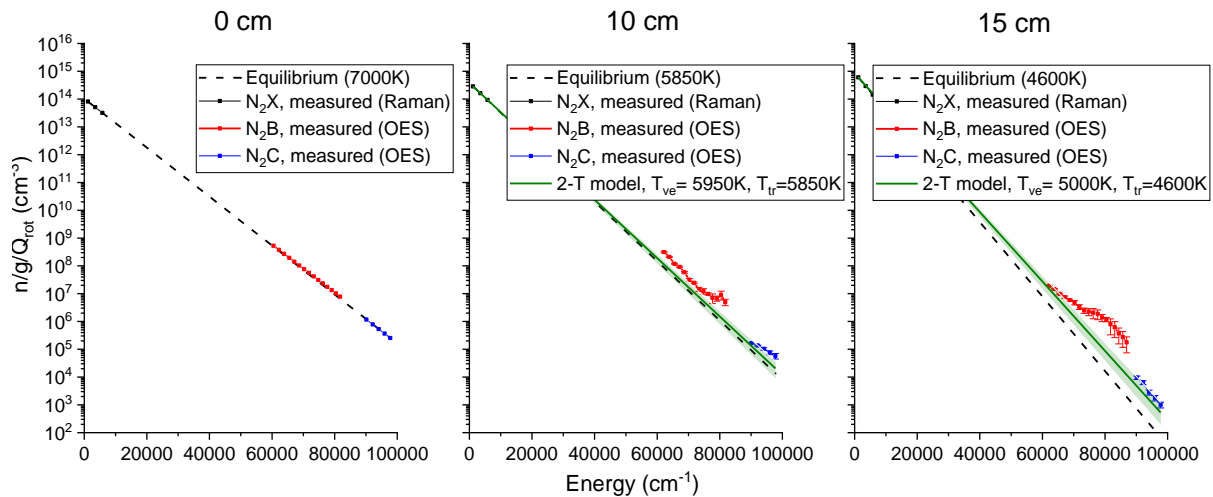


Figure 7: Comparison between the population distributions computed using the 2-temperature model (green) and the measurements (symbols) for the N_2/Ar low flowrate case. The green shaded swaths represent the uncertainty bands on the computed T_{ve} .

The radiation emitted by the plasma is proportional to the population of the excited states. Figure 8 compares the integrated intensity from 250 to 900 nm for the measured, equilibrium, and 2-T spectra. At 15 cm, the measured total radiation is about 4 times stronger than equilibrium, and 1.5 times larger than with the 2-T model. Thus, the 2-T model improves the radiation predictions. This experiment represents a case where the plasma stays relatively close to equilibrium but with still non-negligible nonequilibrium radiation. This is therefore a useful test case for numerical codes to check their ability to predict the radiation when a small departure from equilibrium is induced.

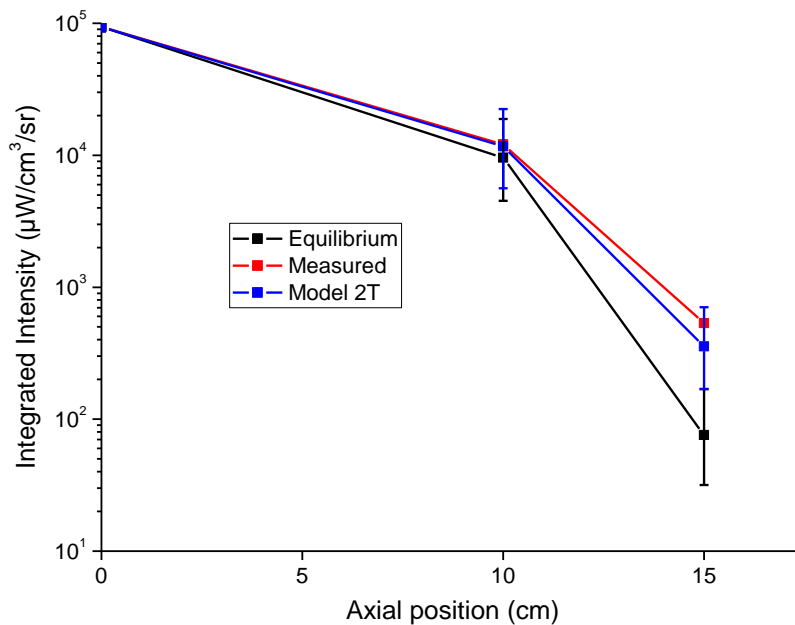


Figure 8: Radiative intensity (integrated between 250 and 900 nm) of the measured, equilibrium and 2-T spectra for the N_2/Ar low flowrate case.

N_2/Ar high flowrate plasma:

In this case, 1.9 g/s of nitrogen is premixed with 1.5 g/s of argon. Using the spectrum measured between 250 and 900 nm, we extract with our fitting routine the populations of the vibrational levels of $N_2(C)$, $N_2^+(B)$ and $N_2(B)$. Figure 9 shows the results at the exit of the 10-cm tube. We observe a larger departure from equilibrium than in the low flowrate case. This was already observed for $N_2(B)$ in Ref. [12] and there is a similar trend for $N_2(C)$ and $N_2^+(B)$. Results at 15 cm are presented in Figure 10. The vibrational levels of excited states of nitrogen are highly overpopulated relative to their equilibrium populations. The vibrational population distributions of $N_2(C)$ and $N_2^+(B)$ measured at each radial and axial position are presented in detail in Appendix A.

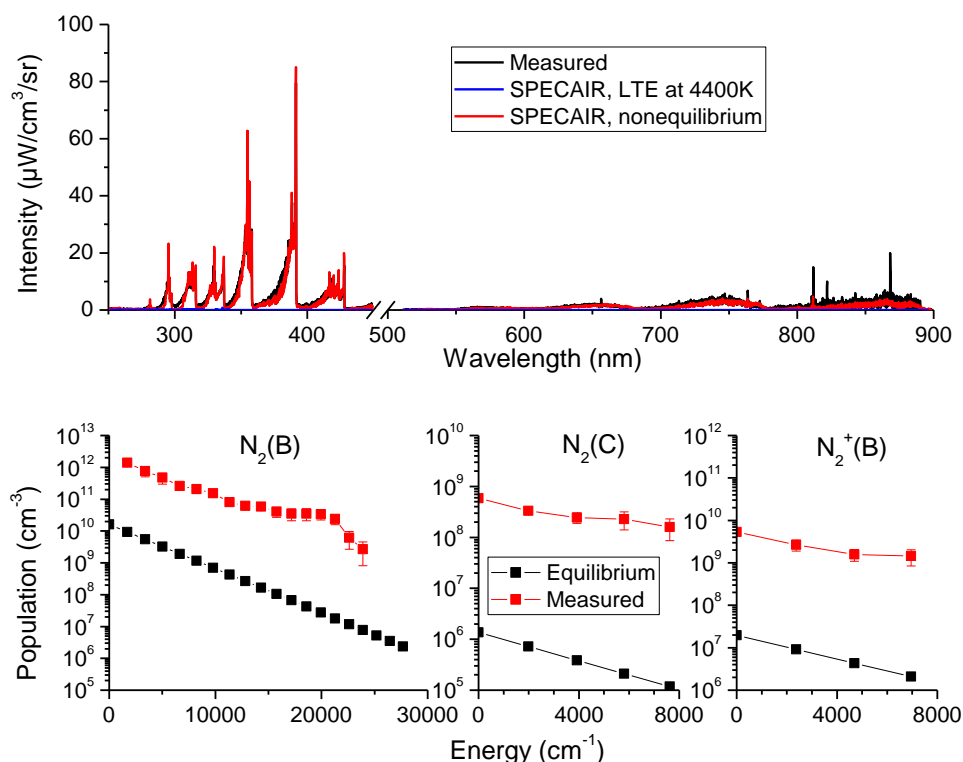


Figure 9: Top: comparison between measured and computed spectra at the exit of the 10-cm tube (at $r = 0$ cm) for the N_2/Ar high flowrate case. Equilibrium spectrum (blue) and fitted spectrum (red). Bottom: equilibrium and measured populations of emitting levels used for SPECAR calculations.

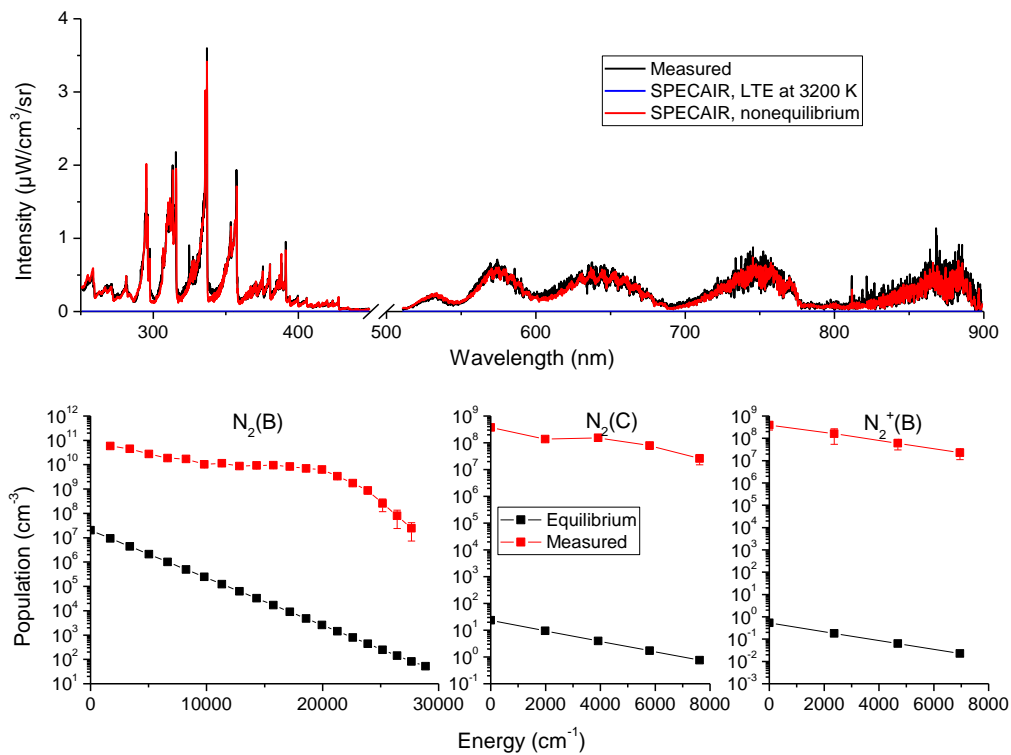


Figure 10: Top: comparison between measured and computed spectra at the exit of the 15-cm tube ($r = 0$ cm) for the N_2/Ar high flowrate case. Equilibrium spectrum (blue) and fitted spectrum (red). Bottom: equilibrium and measured populations of emitting levels used for SPECAIR calculations.

The Boltzmann plot shown in Figure 11 summarizes the population distributions of the various states measured, namely $\text{N}_2(\text{X})$, $\text{N}_2(\text{B})$ and $\text{N}_2(\text{C})$. We performed the same analysis as for the low flowrate case using a 2-T model and obtained $T_{\text{ve}} = 4700 \pm 300$ K at 15 cm. The corresponding distribution is also plotted in Figure 11. The chemistry is partly frozen in the tube, because the excited state densities do not change significantly along the axis of the tube. Note also that the population density remains fairly continuous between the $\text{N}_2(\text{B})$ and $\text{N}_2(\text{C})$ states. The 2-T model is closer to the experimental values than the equilibrium distribution, but discrepancies still appear at 10 cm and for higher energy levels at 15 cm. The non-Boltzmann distribution cannot be predicted using a 2T model. Therefore, a detailed vibrational specific kinetic model must be used in order to predict the measured distributions.

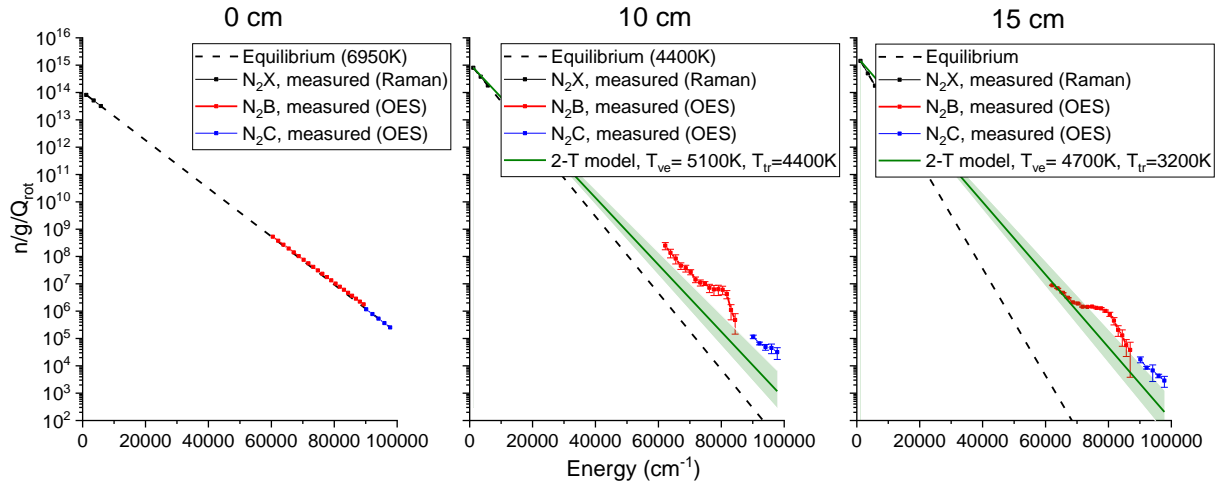


Figure 11: Comparison between the population distributions computed using the 2-temperature model (green) and the measurements (symbols) for the N_2/Ar HF case. The green shaded swaths represent the uncertainty bands on the computed T_{ve} .

Figure 12 shows the volumetric emission at the centerline of the plasma flow, integrated between 250 to 900 nm, obtained from the measurements, from the 2-T model, and from equilibrium population distributions. At 10 cm, the equilibrium radiation is 250 times smaller than the measurements and about 100,000 times smaller at 15 cm. The 2-T model improves the agreement with an underprediction by a factor of 13 at 10 cm and a factor of about 6 at 15 cm. The 2-T model is therefore unable to correctly predict the radiation coming from such recombining plasma flows.

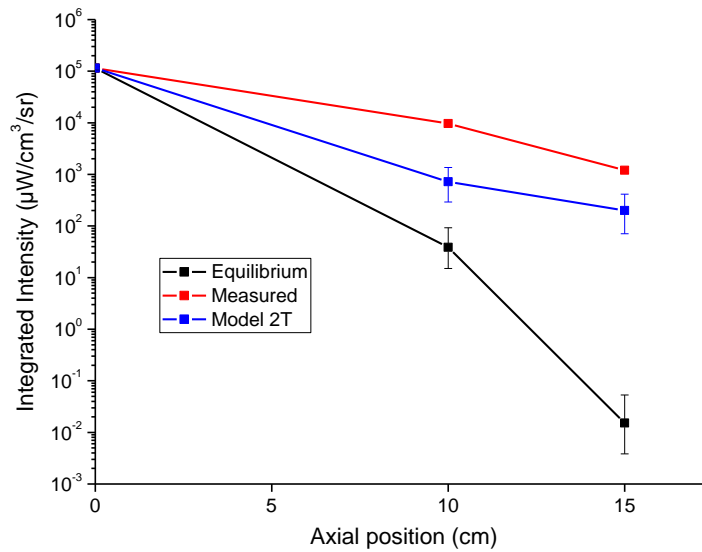


Figure 12: Comparison between the integrated intensity assuming equilibrium (at the measured temperature) and the measured one between 250 and 900 nm for the N_2/Ar HF case.

Discussion

In both N_2/Ar mixtures studied, the excited states of nitrogen were found to be highly overpopulated as compared to both equilibrium and 2-T model predictions. The main reason is believed to be the inverse predissociation of $N(^4S)$ into $N_2(B, v=13)$ as explained in ref [12].

Potentially, other reactions could also play a role as discussed in other papers. For example, Capitelli *et al* [26] showed that the population distribution of excited electronic states is sometimes affected by

superelastic electron collisions. However, they simulated conditions close to those of our experiments and found that superelastic collisions have no influence under our conditions.

Plain *et al* [27] reported that coupling effects between high-lying vibrational levels of $N_2(X)$ and $N_2(B)$ could affect the excited electronic state population distributions. This cannot be proven for the moment as our measurement of the vibrational level of $N_2(X)$ using Raman spectroscopy only yields results for low vibrational levels. A more sensitive diagnostic, e.g. CARS [28], would be necessary to gain access to higher-lying vibrational levels. In addition, measuring precisely the rotational distribution of $N_2(X)$ could also be relevant to confirm the predictions of Panesi *et al* [29] who found the rotational and vibrational temperatures of $N_2(X)$ to differ under certain conditions.

Finally, it should be noted that the chemistry in our experiments is partly frozen and therefore the recombination kinetics are slow. This explains why the 2-T model improves the agreement between the experiments and the predictions. However, this model is expected to give worse results in a case where recombination is faster. A detailed kinetic model is currently under development to simulate the experimental results reported here.

Conclusions

New experiments were performed in our plasma torch facility to measure emission from both equilibrium and nonequilibrium N_2/Ar and Air/Ar plasmas. Optical emission spectroscopy was used to measure spectra of the plasmas between 250 and 900 nm for three different test cases: a mixture of Air/Ar and two cases with N_2/Ar at low and high flowrates. For the Air/Ar mixture, the emission spectra agreed with those computed assuming equilibrium. This was expected as the plasma stays in equilibrium for this case. For the N_2/Ar mixtures, the plasma was found to be out of equilibrium. We were able to determine the vibrational population distributions of $N_2(B)$, $N_2(C)$ and $N_2^+(B)$ using SPECAIR and the measured spectra. These states were found to be overpopulated relative to equilibrium.

Finally, the measured radiation was integrated over the measured range of wavelength. This allows us to get the radiative heat flux which is the important property to model for reentry applications. Hypersonic CFD codes often use multiple temperatures models. Here, a 2-temperature model was employed to compare predictions with experiments. This was done using the Landau-Teller equation to compute the relaxation of the vibrational temperature to the translational one. Due to the rapid decrease in translational-rotational temperature, the vibrational temperature does not relax fast enough to equilibrate with the translational temperature. We compared the measured radiation with the 2-temperature model predictions and with equilibrium predictions. The measured radiation was found to be up to 100,000 times higher than equilibrium. The agreement with the 2-T model was much better, however this model still underestimates the measured radiation by an order of magnitude and is expected to be worse in a real entry scenario. This is an important consideration for reentry applications. Note also that due to the non-Boltzmann vibrational distribution of the population of states such as N_2B , only a vibrational specific kinetic model coupled to a CFD code will be able to correctly predict the radiation in recombining flows.

Acknowledgments

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Appendix A: Radial profiles of vibrational populations of $N_2(B)$, $N_2(C)$ and $N_2^+(B)$

In this appendix we present the radial distributions of vibrational populations for each case considered. This intends to serve as a test-case database for computational simulations. In Figures A1 and A2, we present the radial distribution of vibrational populations for the N_2/Ar low flowrate (LF) case at 10 and

15 cm, respectively. In Figures A3 and A4, we present the same results for the N_2/Ar high flowrate (HF) case.

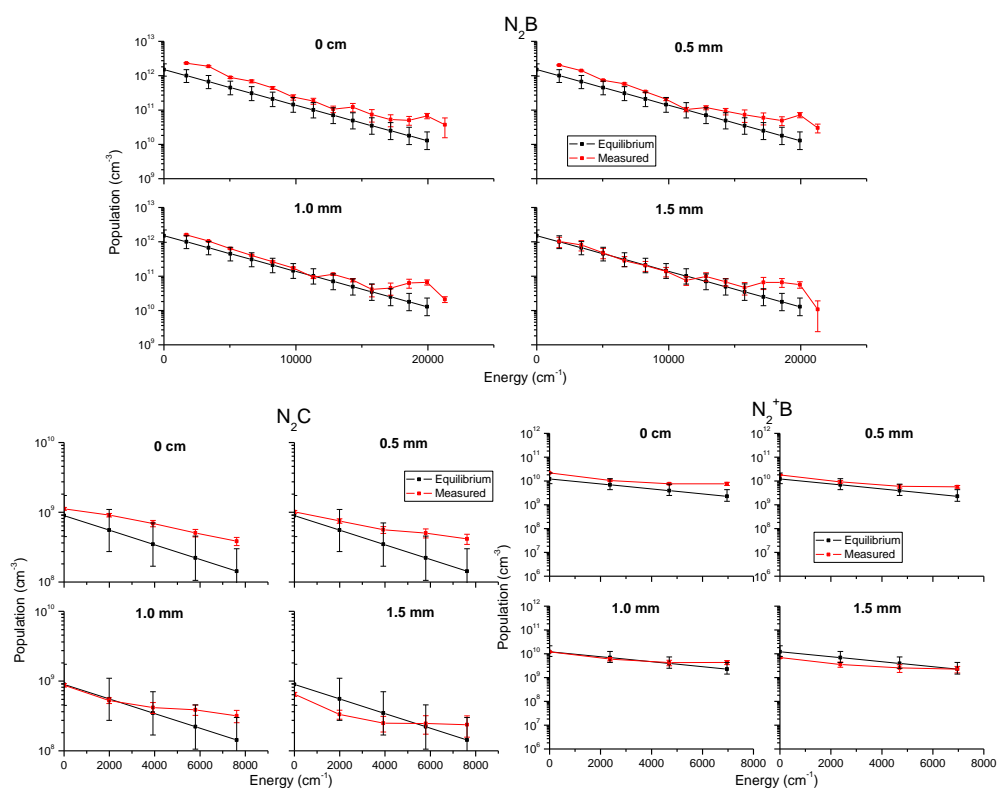


Figure A1: Radial distribution of measured and equilibrium densities of N_2B (top), N_2C (bottom left) and N_2^+B (bottom right) for the N_2/Ar LF case at the exit of the 10-cm tube.

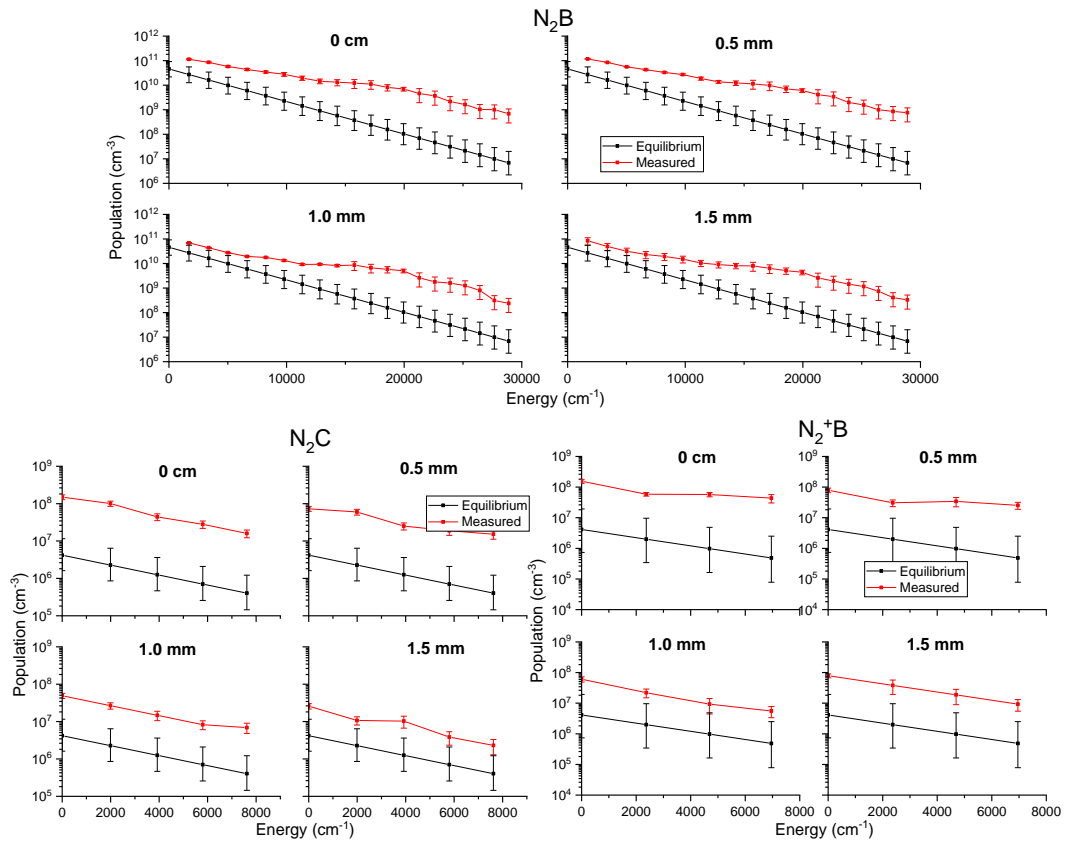
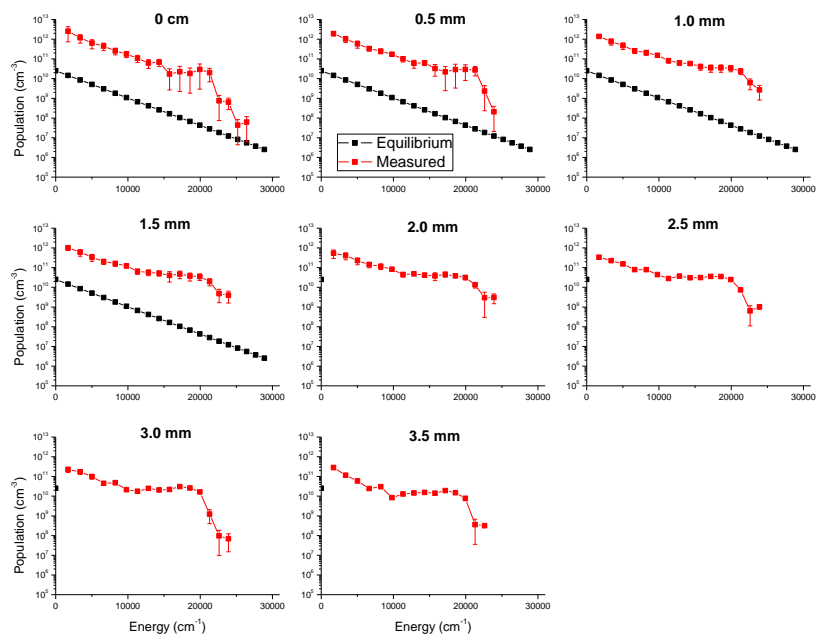


Figure A2: Radial distribution of measured and equilibrium densities of N_2B (top), N_2C (bottom left) and N_2^+B (bottom right) for the N_2/Ar LF case at the exit of the 15-cm tube.



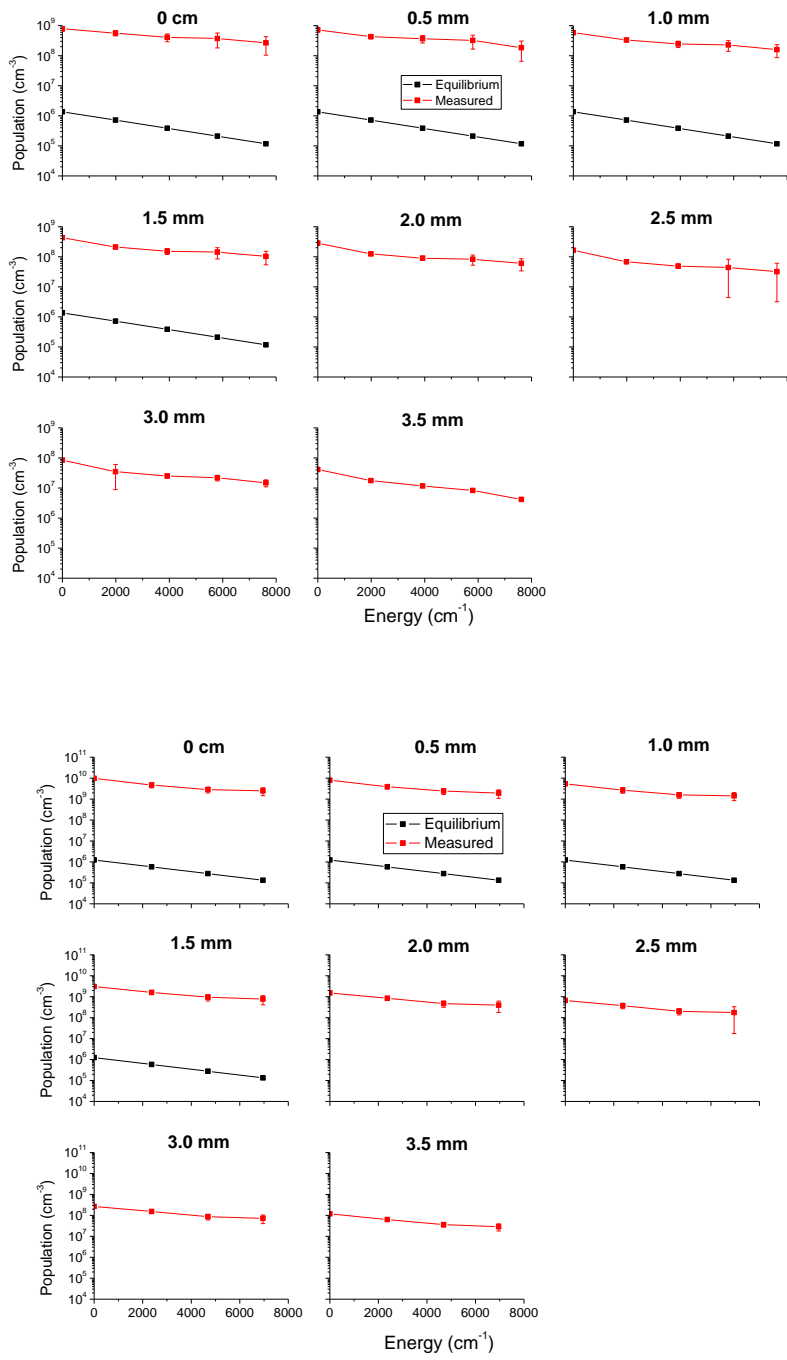
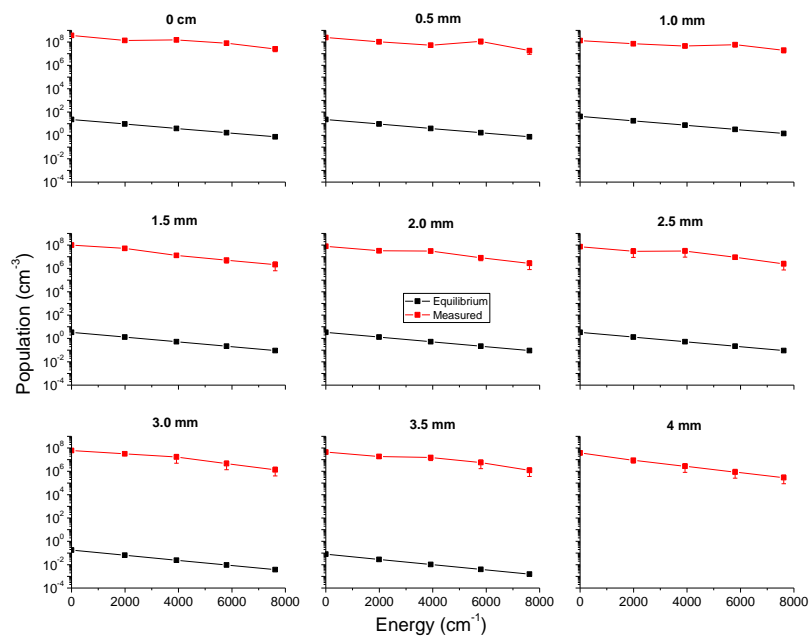
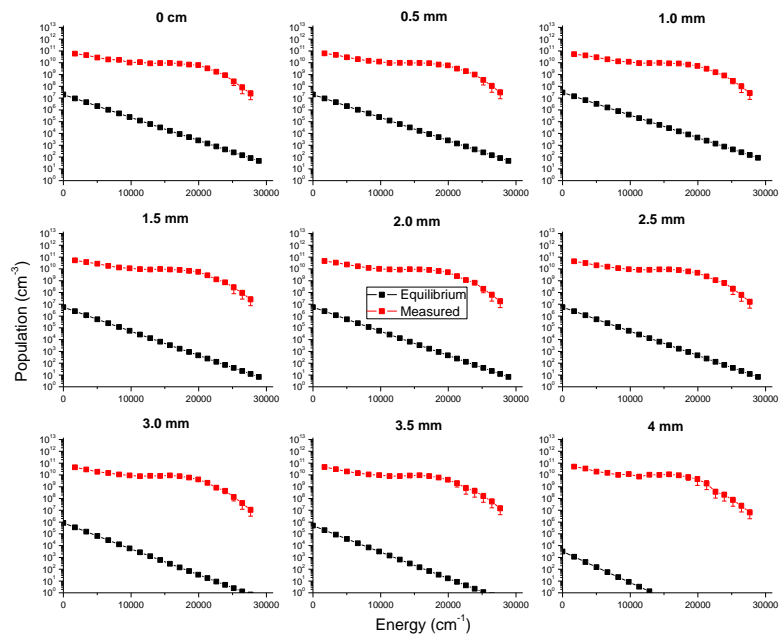


Figure A3: Radial distribution of measured and equilibrium densities of N_2B (top), N_2C (middle) and N_2+B (bottom) for the N_2/Ar HF case at the exit of the 10-cm tube.



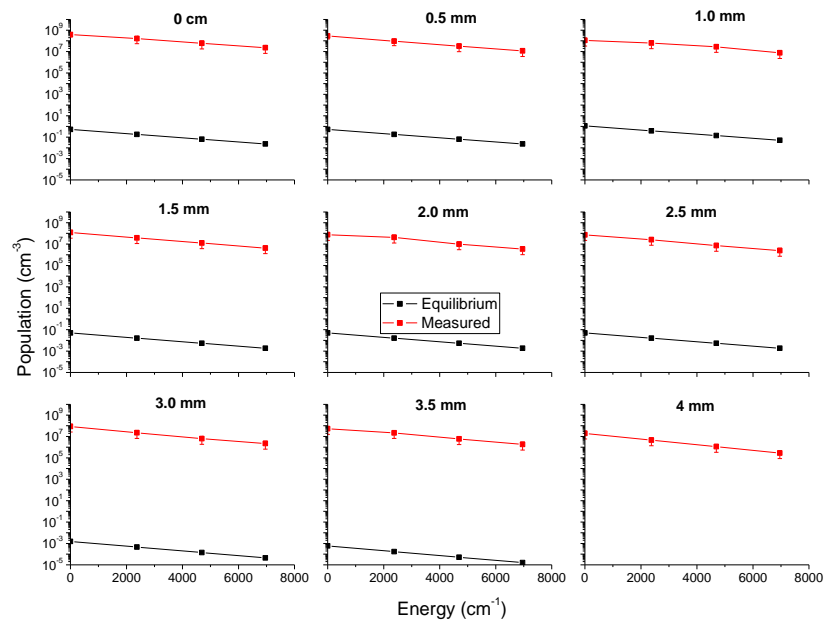


Figure A4: Radial distribution of measured and equilibrium densities of N_2B (top), N_2C (middle) and N_2+B (bottom) for the N_2/Ar HF case at the exit of the 15-cm tube.

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