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A. Goyal, V. Doquet, Amade Pouya. Grain Boundary Sliding and Strain Rate Sensitivity of Coarse and Fine/Ultrafine Grained 5083 Aluminum Alloys. Metallurgical and Materials Transactions A, 2019, 51 (3), pp.1109-1122. 10.1007/s11661-019-05583-5. hal-02481466

HAL Id: hal-02481466 https://hal.science/hal-02481466v1

Submitted on 9 Nov 2020

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² Grain Boundary Sliding and Strain Rate Sensitivity ⁴ of Coarse and Fine/Ultrafine Grained 5083 Aluminum ⁵ Alloys



A. GOYAL, V. DOQUET, and A. POUYA

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The viscoplastic behavior of coarse and bimodal fine/ultrafine grained (F/UFG) Al5083 alloy was investigated between 20 °C and 200 °C through tensile tests at various strain rates, and stress relaxation tests to deduce the strain rate sensitivity (SRS). The plastic strain fields were measured by correlation of SEM images. In the F/UFG material at high temperature, very high strains were measured in shear bands which sometimes crossed the whole gage width and exhibited intensive grain boundary sliding (GBS). Both the SRS and ductility rose with the temperature, and as the strain rate decreased, mainly due to a rising contribution of GBS, which accommodated a much larger fraction of the global strain in the F/UFG material. The boundary between the temperature–strain rate domains where grain refinement led either to strengthening or to softening was determined. Finite element simulations of tension and relaxation tests with viscoplastic grains and sliding grain boundaries captured the macro-scale behavior of the F/UFG material. It also provided some insight into the mechanisms of correlated and cooperative GBS and grain rotation along percolation paths (both inter and intragranular), probably, responsible for macro shear banding.

https://doi.org/10.1007/s11661-019-05583-5

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I. INTRODUCTION

28 ULTRAFINE grained (UFG) metals or alloys gen-29 erally exhibit a substantially higher flow stress than their 30 coarse grained (CG) counterparts, at room temperature. 31 Their fracture strain is most often lower than that of CG 32 materials at room temperature. However, it tends to 33 increase as the strain rate decreases due to of a 34 modification in the plastic strain distribution leading to a lot of diffuse-and thus harmless-micro-bands, 35 36 instead of a few sharp and intense shear bands observed at higher rates.^[1–3] 37

Regarding the high-temperature behavior of these materials, most investigations focused on the superplastic regime, characterized by a strain rate sensitivity (SRS) close to 0.5, which is controlled by grain boundary sliding (GBS)^[4,5] and is observed at comparatively lower temperatures than in CG materials.^[6–9] The intermediate range between room temperature and

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Manuscript submitted August 30, 2019.

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superplastic regime has, comparatively, received much 45 less attention. 46

However, it has been shown by Kapoor *et al.*^[10] that 47 above a strain rate-dependent temperature, instead of 48 GBS-induced hardening, GBS-induced softening occurs 49 50 in Al-1.5Mg,. Since many potential applications of UFG alloys involve heating above ambient temperature, it is 51 necessary to determine the temperature and strain rate 52 domains in which a beneficial effect of the ultrafine 53 54 microstructure can be expected. This is one of the 55 purposes of this study on Al 5083 alloy.

Since the evolutions in ductility with strain rate 56 57 mentioned above seem to correlate with the degree of 58 strain localization, and thus to the SRS, this parameter was measured as a function of temperature and strain 59 rate, through stress relaxation tests in CG and UFG Al 60 5083 alloys. The plastic strain fields in these materials 61 were measured by digital image correlation (DIC) before 62 and after tensile tests run at room or high temperature. 63 The discontinuities induced by GBS along the micro--64 grids laid on the surface for digital image correlation 65 (DIC) were used to estimate the contribution of GBS to 66 the overall deformation, which appeared to explain most 67 68 of the temperature and strain rate-dependence of the 69 SRS.

In the seventies, Raj and Ashby^[11] proposed an 70 analytical model of grain boundary sliding accommodated either elastically, or by diffusion. They formulated 72 a linear, threshold-free relation between the GB sliding 73

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74 rate and the resolved shear stress, in which viscosity 75 increased with the roughness of the GB, and with the presence of second phase particles along its length. Ashby and Verral^[12] introduced a GBS-induced neigh-76 77 78 boring grains switching mechanism, without any elon-79 gation or change in crystal orientation. They predicted a grain size-dependent evolution of the SRS associated 80 81 with the transition from this deformation mechanism to 82 dislocation-controlled creep, as the strain rate rises.

83 A 2D, plane strain finite element analysis of creep 84 with free grain boundary sliding accommodated by elasticity and diffusion processes was later developed by Crossman and Ashby,^[13] who considered a regular array 85 86 87 of hexagonal grains with power law creep inside. They 88 investigated the influence of the viscous stress exponent, 89 n, inside the grains, and of the strain rate on the 90 contribution of GB sliding to the overall deformation. They obtained a modified power law equation for the steady creep rate that predicts an acceleration when 3 GBS occurs, but no modification of the creep exponent. The 2D computational approach of Tvergaard^[14,15] in 4 the eighties was close to that of Crossman and Ashby, but laid emphasis on the consequences of GB sliding in terms of cavities nucleation and growth along the grain 98 boundaries normal to the tensile axis, while Hsia et al.^[16] 99 directly introduced a density, of micro-cracks along such 100 GBs and investigated the effect of GB sliding on the growth rate of such cracks. All the works mentioned 101 above considered a periodic array of hexagonal grains. Onck and Van Der Giessen^[17] investigated the effect 102

103 104 of microstructural variations on the creep rate of a 105 polycrystalline aggregate with freely sliding boundaries, 106 by slightly perturbing an initially regular array of hexagonal grains. The computed creep rate was 107 108 enhanced by up to 60 pct by the introduction of some 109 irregularity, due to increased GB sliding.

Bower and Wininger^[18] proposed a sophisticated 2D 110 crystal plasticity finite element (CPFE) approach where, 111 in addition to GB sliding, GB migration assisted by 112 113 diffusion was modeled. They used a front tracking 114 scheme and adaptive mesh generation techniques to follow the changes in grain structure. The model was used by Agarwal *et al.*^[19] to predict the rate-sensitive 115 116117 SRS of fine-grained (7 to 10 μ m) Al5083 alloy above 118 450 °C. Some discrepancies with experimental data were found at low strain rate, but according to Du et al.[20] 119 120 the introduction of a threshold shear stress for GB 121 sliding improved the predictions. Both studies were 122 based on the same polycrystalline aggregate with 18 123 irregular grains, taken from a micrograph, as well as the 124 crystal orientations. The simulations were not repeated 125 with different numbers of grains and different sets of 126 orientations, so that their statistical representativeness can be questioned. In addition, only {111} (110) slip was 127 considered, while non-octahedral slip systems were found to operate above 200 °C in Al 5083 alloy.^[21] 128 129

130 Many authors used molecular dynamics (MD) simulations to investigate GB mobility. Qi and Krajewski^[22] 131 132 used MD to simulate GBS in aluminum at 750 K and 133 reported three regimes depending on the applied stress: 134 (i) at low applied stress, no sliding was observed, 135 indicating the existence of a threshold stress (ii) at intermediate stress, the amount of sliding increased 136 linearly with time, confirming the linear viscous nature 137 of GBS described by Raj and Ashby, and (iii) at high 138 stress, the amount of sliding increased parabolically with 139 time. According to the MD simulations done by Du $et al.^{[23]}$ the segregation of solute atoms (Mg and Si in 140141 A15083 alloy) at GBs affects the threshold stress for GB 142 sliding. While these atomic scale simulations provide 143 valuable insight into the GB deformation mechanisms 144 and their variations from one type of GB to another, it 145 is difficult to get quantitative data, since the simulations 146 147 are run at pico-seconds time scales and generally include 148 only two neighboring grains, without any triple point, as 149 in a polycrystal.

A solution for scale transition was proposed by 150 Warner et al.[24] who performed 2D "atomistics-in-151 formed" crystal plasticity finite element (CPFE) simu-152 lations for nano-crystalline copper, with 200 grains and 153 GB constitutive equations derived from prior MD 154 simulations. However, since MD simulations were run 155 for a few specific types of GB (symmetric or asymmetric 156 tilt boundaries), the shear strength of high-angle GBs in 157 CPFE simulations was assigned randomly. A "thermal 158 correction" to the 0 K molecular statics results had to be 159 160 applied, since the stress levels computed with MD at very high strain rates and 0 K are unrealistically large. 161

Compared to these sophisticated micromechanical 162 approaches, the 2D finite element model including GBS 163 in a phenomenological way developed in the present 164 work is quite simplified. However, it will be shown to 165 capture the mechanical behavior of UFG Al 5083 166 between 20 °C and 200 °C, in a wide range of strain 167 rates, and to provide some insight into the cooperative 168 phenomena (GBS and grain rotation). 169

II. EXPERIMENTAL STUDY

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A. Experimental Procedures

A cast and annealed plate of Al-5083 alloy (with the 172 composition shown in Table I) was used to machine 173 specimens of CG material, or rods for ECAP processing. 174 This as-received material had equiaxed grains with a 175 mean size of 93 μ m, and contained coarse dendritic 176 intermetallic particles, mostly along the grain bound-177 aries, as shown in Figure 1. 178

179 20×20 mm rods cut from the plate were submitted to 3 ECAP passes at room temperature, with a back 180 pressure of 60 MPa, following route C (rotation of the 181 sample by 180 deg between consecutive passes), in a 182 lubricated die, with an angle of 90 deg. The material was 183 then annealed at 200 °C during 6 hours. The resulting 184 microstructure was partly characterized by EBSD, in a 185 Philips Quanta 600 FEG-ESEM, using the hkl software, 186 a tension of 20 KV and a step size of 75 nm. A typical 187 orientation map in a small area along the insertion axis/ 188 exit axis plane is presented in Figure 2(b). It proved 189 190 difficult to reach a good indexation rate with EBSD, but Transmission Kikuchi Diffraction (TKD) on a FIB-cut 191 thin foil allowed a more accurate characterization, and 192 confirmed the grain size statistics issued from EBSD 193

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194 data collected on $100 \times 100 \ \mu m$ areas along 3 orthog-195 onal planes. The mean grain size was 680 nm, but the 196 microstructure was heterogeneous, with areas in which 197 the mean grain size was around 300 nm, as well as less 198 refined areas, with micron-sized grains (Figure 2(c)). 199 The fraction of high-angle grain boundaries (i.e., with a 200 misorientation larger than 15 deg) was around 65 pct. 201 This fine/ultrafine bimodal microstructure will be

Table I. Chemical Composition of Al 5083 Alloy

Composition	Weight Percent
Mg	5.2
Fe	0.24
Mn	0.45
Si	0.27
Cr	0.09
Al	balance



Fig. 1-Microstructure of coarse grained A15083 Al alloy.

denoted by F/UFG in the following. The grains were 202 elongated in the shearing direction of ECAP, at an angle 203 around 55 deg. The intermetallic particles were broken 204 or debonded and formed rows along the shearing 205 direction of ECAP (Figure 2(a)). 206

Flat dog-bone shaped specimens, with a 17 mm long 207 and 4 mm wide gage length, as well as 8 mm high 208 cvlindrical specimens with a diameter of 8 mm were 209 machined parallel to the extrusion axis for tensile tests 210 211 and relaxation tests in compression, respectively. The surface of the dog-bone specimens was electro-polished. 212 213 To measure the strain fields using digital image corre-214 lation (DIC), several $600 \times 600 \,\mu\text{m}$ patches of gold grids with a 5 μ m pitch were printed along the gage 215 length, using E-beam lithography. 4096 \times 3775 pixels SEM images of the 600 \times 600 μ m² areas covered with 216 217 grids were captured before and after the tensile tests. 218 The image resolution was thus around 146 nm pixel $^{-1}$. 219 The CmV DIC software^[25] was used with a subset size of 220 $4.4 \times 4.4 \ \mu m^2$ 221

222 The tests at high temperature were run on a servo-hy-223 draulic machine equipped with a thermal chamber. The 224 tests were displacement-controlled, and the tensile tests 225 were run at different rates, chosen, based on available 226 data from the literature, so as capture the transition from GB-induced strengthening to GB-induced soften-227 ing, at each temperature. The sample strain was mea-228 sured by monitoring the relative displacement of two 229 dots painted near the ends of the gage length. SEM 230 images of the micro-grids captured before and after the 231 tensile tests were used for DIC. 232

The relaxation tests were performed in compression 233 on cylindrical specimens lubricated with a Teflon spray. 234 The samples were first deformed in compression with a 235 constant displacement rate corresponding approxi-236 mately to a strain rate of 2×10^{-3} s⁻¹ up to 3 to 237 5 pct strain. Then the crosshead displacement was 238 239 stopped for 2 hours, while the stress and strain were recorded, each time the load changed by 50 N. Since the 240tests were displacement-controlled, the plastic strain 241



Fig. 2—Microstructure of F/UFG 5083 Al alloy, (a) elongated intermetallic particles, (b) EBSD map (Euler angles), and (c) grain size distribution.

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rate, $\dot{\varepsilon}_p$ was calculated using the method proposed by 242

Lee and Hart^[26] as: 243

$$\dot{\varepsilon}_p = -\frac{\dot{\sigma}}{\left[\frac{Kh}{A} - \sigma\right]},\tag{1}$$

where σ is the true stress, K the combined stiffness of the 246 machine and the sample, and A and h are the cross-sec-247 248 tion and height of the specimen, respectively. The strain 249 rate sensitivity: 250

$$S = \frac{\partial \ln \sigma}{\partial \ln \dot{\varepsilon}}$$
[2]

252 was calculated from the slope of plastic strain rate vs 253 true stress bi-logarithmic plots.

B. Macro-scale Behavior

Author Proof 5 Figure 3 compares the tensile curves of CG and F/ UFG alloys at various strain rates, at 20 °C, 100 °C, 6 and 200 °C. Both materials exhibited serrated flow, due 8 to dynamic strain aging induced by solute Mg atoms. At la room temperature, grain refinement significantly \cap increased the flow stress, and reduced the ductility, as 261 generally reported in the literature for F/UFG alloys. At 262 100 °C, the difference in flow stress between the two microstructures was reduced, and at 200 °C, the tensile 263264curves of the F/UFG alloy lied above or below that of 265 the CG alloy, depending on the strain rate. For a given 266 temperature, ductility was strongly strain rate-depen-267 dent, as discussed below. Necking was very limited, and 268 fracture was generally slanted.

269 Figure 4 shows the evolution of the plastic strain rate 270 with the true stress during the relaxation tests run at 271 various temperatures on CG and F/UFG materials. The 272 curves are neither straight nor parallel, which reveals 273 evolutions of the strain rate sensitivity with the temper-274 ature as well as with the strain rate. These evolutions are 275 represented in Figure 5. For a given temperature and 276 strain rate, the SRS was higher in the F/UFG material. 277 In both materials, it rose with the temperature and, at a 278 given temperature, with decreasing strain rate.

Using tension and relaxation data, the temperature 279 280 and strain rate domains in which microstructure refinement leads to strengthening (low temperature, high 281 strain rate regime) or to softening (high temperature, 282 low strain rate regime) were identified and plotted on 283 Figure 6. Data from Ko *et al.*^[6] for the same alloy and from Kapoor *et al.*^[27] for Al-1.5Mg are also plotted, and 284 285 are in good agreement with the present results. 286

As mentioned above, in both materials, ductility 287 above 100 °C increased as the strain rate decreased. The 288 289 SRS also rose as the strain rate decreased, and a linear 290 correlation was found between ductility and SRS, for 291 each material, as shown in Figure 7. Fracture was thus 292 controlled by strain localization, that a high SRS tends 293 to hinder.

294 C. Micro-scale Strain Distribution and Deformation Mechanisms 295

Figure 8 compares strain fields measured in both 296 materials, at room temperature after a few percent 297 tensile strain, at 5.8×10^{-5} s⁻¹. In the CG alloy, the 298 299 fracture of intermetallic particles located along the grain 300 boundaries triggered strain localization in short bands 301 connecting them, without any preferential orientation.

302 By contrast, in the F/UFG alloy, intermetallic parti-303 cles, already broken or debonded by ECAP, and aligned 304 in the same direction as the elongated grains, triggered the formation of hundreds of micron-long shear bands. 305 At this temperature (0.34 T_{melting}), grain boundary 306 sliding in this material produced measurable disconti-307 nuities in the grids only in stress concentration areas, 308 near fractured particles (Figure 9). 309

At 100 °C (0.43 T_{melting}) and above, GB sliding was 310 311 observed in the CG material (Figure 10).

312 To estimate the frequency of this phenomenon, the 313 number of sliding GBs intercepted by a series of parallel 314 lines was counted, and was divided by the total number of GBs intercepted by the same lines. To estimate the 315 strain due to GBS, the micro-grids shifts, u, parallel to 316 the tensile axis were measured along a series of 317 318 transverse grid lines of total length t, and Bell and Langdon's formula^[28]: 319



Fig. 3—Tensile curves (a) at room temperature, (b) 100 °C, and (c) 200 °C.

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Fig. 4-Stress relaxation curves for (a) CG and (b) F/UFG materials.



Fig. 5—Evolutions of the strain rate sensitivity for (a) CG and (b) F/UFG materials.

320

$$\varepsilon_{\text{GBS}} = \frac{1}{t} \sum_{0}^{t} u \times \tan(\theta), \qquad [3]$$



Fig. 6—Domains of grain boundary-induced hardening or softening.

where θ denotes the angle between a grain boundary and 322 the tensile axis—was used. At 100 °C, 9.5 pct of the GBs 323 had sled after 6 pct tensile strain at $1.5 \times 10^{-5} \text{ s}^{-1}$, but 324 this mechanism accounted only for 0.6 pct of the global 325 strain. At 200 °C (0.55 T_{melting}) 44 to 68 pct of the grain 326 boundaries had sled, depending on the strain rate and 327 strain level, but the contribution of this mechanism to 328 329 the global strain remained limited to 0.8 to 3.8 pct, as reported in Table II. 330

Figure 11 shows strain maps in F/UFG samples 331 deformed to fracture at 100 °C and 200 °C. Very high 332 strains—up to 50 pct at 100 °C and 90 pct at 200 °C— 333 are measured inside shear bands that sometimes cross 334 the whole gage width. 335

Strain localization and void sheeting inside such 336 bands led to slanted fracture. A zoom inside such a 337 band reveals intensive grain boundary sliding 338 (Figure 12). 339

The method described above was used to estimate the 340 contribution of GBS to the global strain. Since the 341 orientation of each sliding GB was difficult to measure 342

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in that case, a common value of 55 deg representative of 343 344 the orientation of GBs after ECAP was assumed for the 345 angle θ in Eq. [3]. The results are reported in Table III. 346 While for the CG alloy, GBS accounted for less than 347 4 pct of the global strain, in the F/UFG alloy, it 348 accounted for up to 29 pct (and even up to 80 pct within intense shear bands). As expected of a thermally-acti-349 350 vated phenomenon, it increased with the temperature, 351 and for a given temperature, as the strain rate decreased.



Fig. 7—(*a*) Effect of the strain rate on ductility, and (*b*) correlation of ductility with the SRS.

For the F/UFG alloy, the measured SRS correlates 352 directly with the contribution of GBS, as illustrated by 353 Figure 13. 354

III. MODELING AND SIMULATION 355

A 2D, infinitesimal strain, plane stress model with an 356 isotropic viscoplastic behavior for the grains and elas-357 tic-viscous sliding interfaces was developed, using the 358 DISROC finite element code.^[29] No attempt to capture 359 the mechanical anisotropy probably induced by the 360 crystallographic texture inherited from ECAP was 361 made. The aim was rather to capture the effects of 362 strain rate and temperature on the uniaxial macroscopic 363 response of the F/UFG material, and to use the 364



Fig. 9—Grain boundary sliding at room temperature in the F/UFG material triggered locally by the stress concentration near broken intermetallic particles.



Fig. 8—Strain fields measured at room temperature during tensile tests at $6 \times 10^{-5} \text{ s}^{-1}$ (a) in the CG materials strained by 5.1 pct and (b) in the F/UFG material strained by 4.3 pct.

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Fig. 10—Grain boundary sliding in CG samples: (a) after 6.5 pct strain at 1.5×10^{-5} s⁻¹ at 100 °C and (b) after 4.7 pct strain at 7×10^{-6} s⁻¹ at 200 °C.

 Table II.
 Fraction of Sliding GBs and Contribution of GBS to the Global Plastic Strain in the CG Material, Depending on Temperature, Strain, and Strain Rate

$T(^{\circ}C)$	Strain Rate (s ⁻¹)	Strain Level (Pct)	Pct of Sliding GBs (Pct)	Contribution	of GBS (Pct of Global Strain) (Pct)
100	1.5×10^{-5}	6	9		0.6
200	4.1×10^{-3}	12	44		0.8
200	1.8×10^{-3}	23	68		1.8
200	7.0×10^{-6}	5	55	Y	3.8



Fig. 11—Strain fields measured in F/UFG samples (a) at 100 °C, after 22.7 pct strain at 3×10^{-6} s⁻¹ and (b) at 200 °C after 33.9 pct strain at 4.5×10^{-3} s⁻¹.

365 identified model to investigate micro-scale cooperative phenomena (in terms of GBS and grains rotation) and 366 367 their effects on the heterogeneity of the strain field. 368 Crystal plasticity was thus not used, for the reasons 369 evoked in the introduction: lack of representativeness of 370 a single set of orientations that would call for repeated 371 simulations, lack of data on non-octahedral slip systems, 372 known to be active at the temperatures of interest.

In a first stage, to calibrate the model, adjust mesh
parameters and investigate the effect of the number of
simulated grains, equiaxed grains with a nearly uniform

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size were considered. In a second stage, the model was 376 applied to more realistic grains morphologies, inspired 377 from the EBSD mapping shown on Figure 2. 378

A. Mesh and Boundary Conditions

For the first stage, various equiaxed microstructures were randomly generated using the classical Voronoi tessellation method. The mean grain size was controlled by the area of the simulation box, A_{box} and the number of grains, N:

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$$d_{\rm grain} = \sqrt{\frac{A_{\rm box}}{N}}$$
[4]

387 388 It was adjusted to 680 nm, the mean grain size 389 measured for the F/UFG material. A mesh with linear 390 triangular elements for the grains and linear quadrilat-391 eral elements for the grain boundaries was adopted. 392 After a convergence study, an element size equal to 0.01 393 times the simulation box edge was chosen along the 394 GBs, and 0.05 times the simulation box edge for grains 395 cores (Figure 14(a)).

396 Figure 14(a) presents the boundary conditions and 397 loadings. The bottom left corner node was fixed and the 398 vertical displacement of the bottom line was zero. A constant vertical displacement rate, \dot{U}_{ν} , corresponding to a constant global strain rate, ¿ was imposed at the top line, to simulate tensile tests, while a constant vertical displacement, corresponding to a fixed strain was applied to simulate stress relaxation. Due to the unavailability of periodic boundary conditions in the Disroc FE code, the left and right borders were free surfaces. One of the shortcomings of these boundary 407 conditions was that the motions of GBs cutting a side 408 surface are unconstrained and thus more pronounced 409 than for GBs ending inside the model, while, conversely,



Fig. 12-Grain boundary sliding inside a shear band in a F/UFG sample strained by 49.8 pct at 200 °C at 1.4×10^{-4} s⁻¹.

sliding of those cutting the upper or lower surface is 410 411 more constrained. This bias however got smaller and smaller as the number of grains increased. 412

In a second stage, a more realistic microstructure with 413 262 grains (Figure 14(c)), inspired from the EBSD map 414 shown on Figure 2(b), was designed, using the Voronoï 415 tessellation method, but with the measured center of 416 gravity of the grains used as "seeds" in the algorithm, 417 instead of points randomly generated by a Poisson's 418 process. This makes it possible to take into account the 419 heterogeneity of grains size and their elongated mor-420 phology. In addition, to reduce the above-mentioned 421 artifact associated with unconstrained/over-constrained 422 sliding of GBs cutting the sides of the model, a uniform 423 buffer layer of material without sliding GBs, but with 474 the same behavior as the grain cores was added all 425 around, and the boundary conditions were applied on 426 its external contour. The thickness of this external layer 427 was equal to 1 grain diameter *i.e.*, for 262 grain model it 428 was 6.2 pct of the edge of the central part. 429

B. Constitutive Equations for the Grains 430

431 The strain rate inside a grain was decomposed into elastic, plastic, and viscous components: 432 433

έg

$$=\dot{\dot{\varepsilon}}_{\rm el,g}+\dot{\dot{\varepsilon}}_{\rm p,g}+\dot{\dot{\varepsilon}}_{\rm v,g}.$$
[5]

435 The Young's modulus E(T) was temperature-depen-436 dent, while the Poisson's ratio, v, was assumed to remain 437 constant. An isotropic strain hardening model was 438 chosen. A Voce-type hardening function was adopted 439 440 for the isotropic hardening variable, R:

$$R = R_0 + Q(1 - e^{-bp}), \qquad [6]$$

where R_0 , Q and b are material constants, and p denotes 443 the cumulated plastic strain. Von-Mises yield criterion is 444 chosen. The yield function was thus: 445 446

$$\sqrt{3J_2(\sigma)} - R = 0.$$
 [7]

448 The viscous strain inside the grains was calculated 449 450 using an Arrhenius-type equation with power law in 451 effective stress: 452

$$\dot{\varepsilon}_{\rm v,g} = a(\sigma - \sigma_{\rm c})^n,$$
 [8]

where a and σ_c are temperature-dependent material 454 455 parameters.

Table III. Contribution of GBS to the Global Plastic Strain in the F/UFG Material, Depending on Temperature, Strain, and Strain Rate

<i>T</i> (°C)	Strain Rate (s ⁻¹)	Strain Level (Pct)	Contribution of GBS (Pct of Global Strain) (Pct)
100	1.8×10^{-5}	12.9	9
100	3.0×10^{-6}	22.7	13
150	1.6×10^{-5}	27.5	22
200	4.5×10^{-3}	33.9	18
200	1.4×10^{-4}	49.8	29

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457 The displacement rate vector at a grain boundary had 458 an elastic and a viscous component:

$$\dot{U} = \dot{U}_{\rm el} + \dot{U}_{\rm v}.$$
[9]

461 462 The tangential and normal stresses were related to the 463 elastic displacement by an elastic stiffness matrix, K: 464

$$\begin{pmatrix} \tau \\ \sigma \end{pmatrix} = \begin{pmatrix} K_t & K_{tn} \\ K_{nt} & K_n \end{pmatrix} \begin{pmatrix} U_t - U_{t,v} \\ U_n - U_{n,v} \end{pmatrix}$$
[10]



Fig. 13—Correlation between the strain rate sensitivity of the F/UFG alloy and the measured contribution of grain boundary sliding to its global deformation.

$$K_{\rm n} = \frac{K_0}{1 + \frac{U_{\rm n}}{e}},$$
 [11]

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where K_0 and e are constants. The closure displacement 475 was thus limited by the initial (purely computational) 476 "thickness", e of the interface, taken as 1 pct of the 477 478 simulation box size. Closure corresponds to negative values of U_n . The normal stiffness, K_n approaches 479 infinity when the closure displacement, U_n tends to -e. 480 The normal stress is proportional to the normal dis-481 placement for small openings (with a proportionality 482 483 constant K_0 and saturates at K_0e for large positive openings (never reached in the present simulations). In 484 485 order not to modify the global elastic behavior by elastic GBS, the GB elastic stiffness parameters, K_0 and K_t were 486 not independent, but related to the Young's and shear 487 modulus, respectively. 488

the normal stiffness, $K_{\rm n}$.

For the viscous part, no normal creep was allowed, 489 only viscous sliding was considered. A temperature-dependent threshold was introduced, *i.e.*, the sliding rate 491





Fig. 14—(a) Example of mesh and boundary conditions used for the model calibration stage, (b) description of a sliding interface, and (c) more realistic microstructure inspired from the EBSD mapping shown on Fig. 2(b).

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492 was supposed to be zero if the shear stress did not reach 493 the threshold stress, τ_c , and was proportional to the net 494 shear stress otherwise.

495

$$\dot{U}_{t,v} = b_t \langle \tau - \tau_c \rangle.$$
[12]

497 498 To take into account the thermally-activated nature of GB sliding, an Arrhenius-type expression inspired from the work of Raj and Ashby^[11] and Agarwal 499 500 et al.^[19] was assumed for the proportionality constant: 501 502

$$b_t = \frac{b_0}{kT} e^{\frac{-Q_{\text{GBS}}}{kT}},$$
[13]

where b_0 is a material parameter (6.64 × 10⁻²⁸ m⁴ s⁻¹, 504 according to Reference 18), Q_{GBs} is the activation energy for GBS (1.4 × 10⁻¹⁹ J, according to Reference 505 506 18) and k is Boltzmann's constant. uthor Proof

The macroscopic viscoplastic strain E_{vp} sees the contributions from the matrix viscoplastic strain and from the viscous displacement jumps U_k across sliding interfaces of contour Γ_k and normal n_k (Figure 14(b)):

$$E_{\rm vp} = \frac{1}{V} \left[\int\limits_{V} \varepsilon_{\rm vp} \cdot \mathrm{d}V + \sum_{k} \int\limits_{\Gamma_k} \frac{1}{2} (U_{\rm v,k} \otimes n_k + n_k \otimes U_{\rm v,k}) \mathrm{d}s \right].$$
[14]

514 515 The contribution of GBS to the global viscoplastic 516 strain can thus be computed as the second term of the 517 right hand side of Eq. [14] divided by $E_{\rm vp}$.

518 2. Determination of the minimum number of simulated 519 grains for convergence

520 To determine the minimum number of grains required 521 in the model so as to get rid of the scatter from one 522 randomly-generated microstructure to the other-in 523 terms of global stress-strain behavior, but also in terms 524 of predicted contribution of GBS-, five different microstructures each with 15, 22 and 30 grains of 525 526 similar mean grain size were randomly generated (Figure 15(a)). A tensile test up to 10 pct strain was 527 simulated at 5 \times 10⁻³ s⁻¹ for each of these microstruc-528 529 tures, using the same parameters. The five simulated 530 stress-strain curves for a given number of grains, as well 531 as the evolutions of the contribution of GB sliding to the 532 global strain are compared in Figures 15(b) and (c).

533 For the model with 15 grains, the difference between 534 the maximum and the minimum predicted GBS contri-535 butions was as high as 25 pct. Model #1 and model #3 536 showed the highest and the lowest contributions of 537 GBS, respectively, which correlated well with their 538 respective highest and lowest cumulated lengths of 539 GBs projected on the maximum shear stress directions, 540 and with the presence of well oriented GBs cutting free 541 surfaces in model #1. Note that the highest contribution 542 of GBS also corresponded to the softest macro-scale 543 response, and vice versa. Macro-scale convergence was 544 achieved for 22 grains, and the bias due to the free side 545 surfaces was reduced as well. However, some scatter 546 (approximately 5 pct difference) was still observed in the

contribution of GB sliding to the global strain. 547 548 Microstructures with 30 grains had to be used to get 549 reproducible stress-strain curves as well as reproducible predictions of GBS contribution. 550

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3. Assumptions made and identification procedure

As a whole, 12 parameters, some of which tempera-552 ture-dependent, had to be identified. Out of those, only 553 10 are actually independent, since K_0 and K_t were deduced from the global elastic moduli. The Young's 554 555 modulus was identified from the tensile tests at each 556 temperature. The hardening parameters R_0 , Q, and b557 558 were identified from the room temperature tensile tests. 559 While b was assumed independent of the temperature, R_0 and Q were deduced from the yield stress, at each 560 temperature. The three viscosity parameters of the 561 grains, a, n and the threshold stress σ_c were identified 562 from available tension and relaxation data. An initial 563 guess for the GB sliding proportionality constant, b_{t} , 564 was obtained by extrapolating the equation provided by 565 Agarwal et al.^[9] for A15083 for higher temperatures to 566 the medium temperature range of interest. 567

C. Identified Model and Insight into Micro-scale Phenomena

A comparison of experimental and simulated stress-570 571 strain or strain rate-stress curves at each temperature is shown on Figure 16, and the corresponding best-fit sets 572 of parameters are gathered in Table IV. 573

The model captures the large change in tensile 574 575 strength with strain rate for the F/UFG material. The 576 simulated relaxation curve at 200 °C nicely reproduces 577 the experimental one, while a less satisfactory agreement 578 is obtained at 100 °C and 150 °C.

579 The contribution of grain boundary sliding during the 580 simulated tensile tests is plotted vs the inelastic strain in 581 Figure 17.

582 Because the threshold stress for GB sliding ($\approx 2 \times \tau_c$) was always lower than the threshold stresses for plastic 583 584 and viscous flow inside the grains (R_0 and σ_c , respec-585 tively), 100 pct of the inelastic strain was initially accommodated by GB sliding. This fraction then 586 decreased as inelastic deformation developed inside the 587 grains, and tended towards a steady-state value, which 588 was always much larger in the UFG material. Such 589 590 evolutions bear some similitude with that of the ratio of plastic dissipation due to GBS to the total plastic 591 dissipation computed for nano-crystalline copper by Warner *et al.*^[24] using atomistically-informed CPFE. 592 593 This ratio also started at 100 pct and decreased towards 594 595 a grain size-sensitive value. As expected, the contribu-596 tion of GBS was predicted to increase with decreasing strain rate at a given temperature (Figure 17(a)) and 597 with increasing temperature, at a fixed 598 rate 599 (Figure 17(b)).

The SRS computed for the F/UFG material is plotted 600 601 on Figure 18 vs the predicted contribution of GBS to the global inelastic strain, after 10 pct tensile strain, at 602 various rates and temperatures. The experimental data 603 are also plotted for comparison. The model captures the 604 experimentally observed direct correlation. 605

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Fig. 15—Convergence study in terms of number of grains: (a) meshes, (b) computed stress-strain curves, and (c) contribution of GBS to the global inelastic strain.

Figure 19 shows the viscous sliding along GBs at 607 various stages of a tensile test at 200 °C and 608 2×10^{-4} s⁻¹. Initially, GB sliding was triggered by 609 the far field, and thus occurred along GBs oriented 610 close to the maximum shear stress direction 611 (± 45 deg), and often along less constrained, surface-cutting GBs. Upon further straining, sliding 612 was triggered along connected GBs, not as well 613 aligned with the far-field shear stress, and were 614 pushed by an already gliding GB. This led to 615 cooperative GBS along "percolation paths" that 616 sometimes crossed the gage width. This phenomenon 617

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Fig. 16—Experimental and simulated curves for (a) tensile and (b) relaxation tests on F/UFG material at 100 °C, 150 °C, and 200 °C.

Table IV. Identified Set of Parameters

	100 °C	150 °C	200 °C
E (MPa)	62000	56900	51700
ν	0.3	0.3	0.3
R_0 (MPa)	325	292	225
Q (MPa)	125	75	50
\overline{b}	45	45	45
$a (s^{-1} MPa^{-n})$	1.5×10^{-18}	8.5×10^{-14}	2.5×10^{-12}
п	5.5	4	4
$\sigma_{\rm c}$ (MPa)	89	48	15
$K_{\rm n}$ (MPa mm ⁻¹)	4.26×10^{9}	3.91×10^{9}	3.55×10^{9}
$K_{\rm t}$ (MPa mm ⁻¹)	1.64×10^{9}	1.50×10^{9}	1.37×10^{9}
$b_{\rm t} ({\rm mm}{\rm s}^{-1}{\rm MPa})$	2×10^{-10}	4.5×10^{-9}	5.0×10^{-8}
$\tau_{\rm c}$ (MPa)	42	10	2

618 might explain the intense shear bands crossing the 619 whole gage length observed in F/UFG material at 620 high temperature.

Figure 20 reports some simulation results for a tensile 621 test until 10 pct strain at 5 \times 10⁻³ s⁻¹ and 200 °C on the 622 623 more realistic, heterogeneous microstructure shown on 624 Figure 14(c). Figure 20(a) shows the axial viscoplastic 625 strain field, Figure 20(b) shows the viscous sliding along GBs, Figure 20(c) corresponds to the rotation field 626 627 (antisymmetric part of the displacement gradient), and Figure 20(d) the average rotation in each grain. From 628 629 Figure 20(a), it appears that in some places (see the 630 enlarged areas), transgranular shear bands are induced 631 by sliding along a neighboring GB, which relaxes the shear stress along the GB, so that this stress is 632 redistributed in the next grain, and triggers viscoplastic 633



Fig. 17—Predicted effects of (a) strain and strain rate at 200 °C and (b) strain and temperature at $2 \times 10^{-5} \text{ s}^{-1}$ on the contribution of GBS to the global inelastic strain in F/UFG material.



Fig. 18—Correlation between measured/computed SRS and measured/computed contribution of GBS to the global deformation.

flow. This intensified transgranular plastic flow might in turn activate GBS along an GB located on the other side of the grain. Percolation *through the grains* and not only *along the GBs* might thus contribute to the development of long shear bands. 638

It can also be concluded that GBS increases the 639 heterogeneity of the plastic strain field: a variation from 640 0.57 to 2.5 times the mean plastic strain is observed here, 641 in spite of similar constitutive equations in all the 642

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Fig. 19—Viscous sliding along GBs at various steps for a simulation run at 2×10^{-4} s⁻¹ and 200 °C in the F/UFG material.

"grains". Such a range is not so far from the range 643 obtained by the statistical analysis of plastic strain fields 644 measured by DIC in the F/UFG material, which was 645 typically 0 to 3 times the mean value.^[21] 646

Time-dependent grains rotation has been shown, 647 through in situ SEM or TEM straining and crystal 648 orientation mappings, to contribute significantly to the 649 viscoplastic deformation of UFG materials, even at room temperature^[30–32] and to be a collective process, occurring in small groups of neighboring grains.^[32] This 650 651 652 feature is retrieved by the simulations, as illustrated by 653 654 Figure 20(d), which shows clusters of grains rotated by up to ± 1.5 deg. Neighboring grains often exhibit 655 rotations of opposite sign (as if they were contacting 656 gears) so that the overall rotation vanishes. The forma-657 tion of such grain clusters, often inclined by \pm 45 deg 658 relative to the tensile axis, might also contribute to the 659 development of shear bands. Figure 20(c) shows that 660 grains do not rotate as a block. The rotation is generally 661 more pronounced near their sliding GBs-where it can 662 reach \pm 5 deg, which should lead to an accumulation of 663 geometrically-necessary dislocations-than in their core. 664 665 Furthermore, GBS and grain rotation are clearly 666 correlated phenomena: grains that do not exhibit GBS do not rotate significantly, and the largest rotations are 667 668 associated with substantial GBS.

IV. CONCLUSIONS AND PERSPECTIVES 669

The boundary between the temperature-strain rate 670 domains where the F/UFG Al 5083 alloy is stronger or 671 softer than its CG counterpart was determined and is 672 consistent with data from the literature (Figure 6). 673



Fig. 20—Results from the simulation of a tensile test at 5×10^{-3} s⁻¹ at 200 °C until 10 pct strain on the microstructure from Fig. 14(c).

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674 The SRS of the F/UFG material, which is higher than 675 that of CG material, rises with the temperature and as the 676 strain rate decreases (Figure 5). It is controlled by grain boundary sliding (Figure 13), and controls the ductility, 677 which is thus strongly rate-dependent (Figure 7). 678

679 Both CG and F/UFG materials exhibit more and 680 more GBS as the temperature rises and as the strain rate decreases. However, in the former, this mechanism 681 accounts at most for 4 pct of the global strain below 682 683 200 °C, while in the latter, its contribution can reach 684 29 pct (Tables II and III).

A 2D phenomenological FE-model with viscoplastic 685 686 grains and viscous sliding GBs was developed and identi-687 fied. It captured the macroscopic behavior of the F/UFG 688 material over a wide range of rates and temperatures.

689 The model also showed that GBS increases the 690 heterogeneity of the plastic strain field. It provided some insight into the correlated and cooperative mechanisms of GBS and grain rotation that are probably 3 responsible for macro shear banding in the F/UFG 4 material. The simulations suggested that such coopera-5 tive phenomena occur along percolation paths that can 6 be intergranular as well as transgranular.

<u>Author Proof</u> Several further developments of the model can be 698 envisaged: (1) the uniform threshold stress for GB sliding 699 used here might rather be a random variable to capture the differences in GBs ability to slide and (2) a grain size 700 701 dependence of the model parameters might be introduced. 702 The latter objective would however require a substantial 703 experimental database on several batches of material with 704 different mean grain size, for calibration. 705

ACKNOWLEDGMENTS

707 An ECAP facility of LEM3 laboratory in Metz was 708 used to produce the UFG material, under the supervi-709 sion of Dr. J.J. Fundenberger, who is gratefully 710 acknowledged.

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