



HAL
open science

An Accurate Inter-Turn Short Circuit Faults Model Dedicated to Induction Motors

Babaa Fatima, Ouafae Bennis

► **To cite this version:**

Babaa Fatima, Ouafae Bennis. An Accurate Inter-Turn Short Circuit Faults Model Dedicated to Induction Motors. 2020. <hal-02455498>

HAL Id: hal-02455498

<https://hal.science/hal-02455498v1>

Preprint submitted on 26 Jan 2020

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



HAL Authorization

An Accurate Inter-Turn Short Circuit Faults Model Dedicated to Induction Motors

Babaa Fatima¹, O. BENNIS²

¹ Electrical Laboratory of Constantine “LEC”, University of Constantine 1, 25000 Constantine, Algeria (9 pt)

² Prisme Laboratory, University of Orleans, 28000 Chartres, France (9 pt)

Article Info

Article history:

Received

Revised

Accepted

Keyword:

Induction Machines

New Model

Inter-Turn Short-Circuit Fault
indicator fault

ABSTRACT (10 PT)

The paper present a new practical and more precise model for induction motors after introducing inter turn short circuits faults. The proposed model is based on coupled magnetic circuit theory. To verify the exactitude of the model, simulation results for induction machine under interturn short circuit fault are presented. In spite of its simplicity, the proposed model is able to provide useful indications for diagnostic purposes. To demonstrate the effectiveness of the model, experimental study is presented at the end of the paper. (9 pt).

*Copyright © 2019 Institute of Advanced Engineering and Science.
All rights reserved.*

1. INTRODUCTION (10 PT)

Many of the works presented in literature have shown that a most of failures in induction machines are caused by stator winding faults. For example, the turn-to-turn short circuit faults, in stator windings, represent 30%–40% of the existing faults in induction machines [1]. In most cases inter-turn short circuits fault is caused by thermal, thermomechanical, vibrational and environmental factors occurs during the operational phase [2-4]. More recently, the cage induction motor is the most electromechanical form used in many areas such as electromechanical drive for industrial, commercial and domestic applications.

Diagnosing failures of industrial systems, if it can be possible to identify in a timely manner, represents one of the means of increasing gain points of productivity. Any reliable method of diagnosis should be based on the study of the electromagnetic and mechanical behaviour of the motor in both healthy and under fault conditions. For a good and effective understanding diagnosis, an accurate and appropriate analytical model is required. A large number of mathematical models of three-phase induction motors have been seriously studied in the past decades [5-11]. Induction motor models are developed based on suitable mathematical descriptions, which have relevant dynamic description of the processes associated with induction motor operation in healthy and faulty conditions. It is agreed that the difficulty in obtaining an accurate model is a tradeoffs between complex, effectiveness and reliable characteristic. Although it is difficult to control the factors influencing machine function and all nonidealities existing in a reality., A model must be available in order to extract the fault indicators. So, there is a real need to develop an accurate model that can take into account the impact of default and predict it before it grows and damages the machine completely. The developed model relies on coupled magnetic circuit theory and allows detection of electrical faults, like shorted faults in stator windings. In this paper, a judicious, precise and effective mathematical model that could be used to monitor induction machine in healthy and faulty conditions is proposed. To demonstrate the effectiveness of the model, simulation and experimental results are shown at the end of this paper.

2. MOTOR MODEL IN ABC MODEL COORDINATES INCLUDING INTER-TURN SHORT CIRCUITS FAULT



2.1. Healthy machine

to modeling three-phase induction motor, it is necessary to put some hypotheses to achieve a simple and useful model:

- there is no magnetic saturation during operation.
- magneto-motive force (MMF) and flux are considered sinusoidally distributed.
- harmonics in this model are neglected.
- magnetism of iron is considered as unlimited and the air gap is negligible and smooth.

Currents, voltages and flux linkage equations of the mathematical model are generally carried out in the stationary reference systems a, b and c.

$$\begin{cases} [V_s] = [R_s] \cdot [I_s] + \frac{d[\Phi_s]}{dt} \\ [V_r] = [R_r] \cdot [I_r] + \frac{d[\Phi_r]}{dt} \end{cases} \quad (1)$$

where:

$$\begin{cases} [\Phi_s] = [L_{ss}] \cdot [I_s] + [M_{sr}] \cdot [I_r] \\ [\Phi_r] = [M_{sr}]^T [I_s] + [L_{rr}] \cdot [I_r] \end{cases} \quad (2)$$

with,

$$[I_s] = [i_{sa} \ i_{sb} \ i_{sc}]^t \quad [I_r] = [i_{ra} \ i_{rb} \ i_{rc}]^t \quad [V_s] = [v_{sa} \ v_{sb} \ v_{sc}]^t$$

$[R_s] = R_s \cdot 1_{3 \times 3}$; is the stator matrix resistance, and the stator inductance matrix is given by:

$$[L_{ss}] = \begin{pmatrix} L_{saa} & M_{sab} & M_{sac} \\ M_{sba} & L_{sbb} & M_{sbc} \\ M_{sca} & M_{scb} & L_{scc} \end{pmatrix} \quad [L_{rr}] = \begin{pmatrix} L_{raa} & M_{rab} & M_{rac} \\ M_{rba} & L_{rbb} & M_{rbc} \\ M_{rca} & M_{rcb} & L_{rcc} \end{pmatrix}$$

where

$L_{saa} = L_{sbb} = L_{scc} = l_s$; the stator self inductance,

$M_{sab} = M_{sac} = M_{sbc} = M_{ba} = M_{ca} = M_{cb} = M_s$; the stator phase mutual inductance.

$L_{raa} = L_{rbb} = L_{rcc} = l_r$; the rotor self inductance,

$M_{rab} = M_{rac} = M_{rbc} = M_{ra} = M_{rb} = M_{rc} = M_r$; the rotor phase mutual inductance.

$[M_{sr}]$ the mutual inductance matrix between the stator and rotor, which is function of θ , the spatial position of the rotor.

$$[M_{sr}] = M_{sr} \begin{bmatrix} \cos(\theta) & \cos\left(\theta + \frac{2\pi}{3}\right) & \cos\left(\theta - \frac{2\pi}{3}\right) \\ \cos\left(\theta - \frac{2\pi}{3}\right) & \cos(\theta) & \cos\left(\theta + \frac{2\pi}{3}\right) \\ \cos\left(\theta + \frac{2\pi}{3}\right) & \cos\left(\theta - \frac{2\pi}{3}\right) & \cos(\theta) \end{bmatrix}$$

2.2. Turn-to-turn shorted circuit model

Turn-to-turn short circuit fault causes one or more additional windings in faulty phase and reduce the effective winding. (see Figure. 1.)

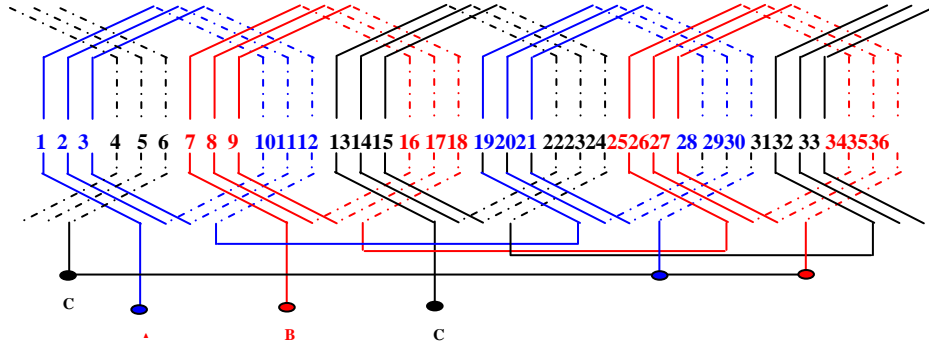


Figure 1. Diagram of stator phases windings including inter-turn short circuits fault in phase A.

To consider a short-circuit fault, it is required to define two parameters indispensable for the understanding of the model [12], [13]. η_{cc} is a short-circuited turns parameter and it defined as:

$$\eta_{cc} = \frac{\text{Number of inter-turns short-circuit windings}}{\text{Total number of inter-turns in one phase}}$$

Turn faults equation can be expressed as:

$$0 = R_{cc} i_{cc} + \frac{d}{dt} \phi_{cc} \quad (3)$$

Where

$$\phi_{cc} = [M_{ccs}] [i_s] + [M_{ccr}] [i_r] + L_{cc} i_{cc}$$

$$[M_{scc}] = \eta_{cc} I_{sp} \begin{bmatrix} \cos(\theta_{cc}) \\ \cos\left(\theta_{cc} - \frac{2\pi}{3}\right) \\ \cos\left(\theta_{cc} + \frac{2\pi}{3}\right) \end{bmatrix} \quad [M_{rcc}] = \eta_{cc} I_{sp} \begin{bmatrix} \cos(\theta_{cc} - \theta) \\ \cos\left(\theta_{cc} - \theta - \frac{2\pi}{3}\right) \\ \cos\left(\theta_{cc} - \theta + \frac{2\pi}{3}\right) \end{bmatrix} \quad (4)$$

When the short circuit occurs in the phase s_a , θ_{cc} can be given as $\theta_{cc} = 0$.

3. INTER- TURN SHORT CIRCUITS FAULTS MODEL IN (α, β) COORDINATES (10 PT)

Three-phase quantities (voltages, currents and flux linkage) are converted in (α, β) coordinates to resolve differential equations with variable coefficients. The 2-phase stationary (α, β) is used to reduce the number of equations and to eliminate the interdependence found in the mutual inductances matrix between stator and rotor. These fictive coils are electrically and magnetically equivalent to the real coil.

Clark transformation equation is of the form:

$$[X_{o\alpha\beta}] = [X_{ro} \quad X_{r\alpha} \quad X_{r\beta}]^t = [C]^{-1} \cdot [X_3] \quad (5)$$

⊛

with:

$$[C] = \sqrt{\frac{2}{3}} \cdot \begin{pmatrix} \frac{1}{\sqrt{2}} & 1 & 0 \\ \frac{1}{\sqrt{2}} & -1/2 & \sqrt{3}/2 \\ \frac{1}{\sqrt{2}} & -1/2 & -\sqrt{3}/2 \end{pmatrix} \quad (6)$$

After applying the transformation, the model becomes:

$$\begin{cases} \begin{bmatrix} V_{s\alpha} \\ V_{s\beta} \end{bmatrix} = 0 = \begin{pmatrix} R_s & 0 \\ 0 & R_s \end{pmatrix} \begin{pmatrix} i_{s\alpha} \\ i_{s\beta} \end{pmatrix} + \frac{d}{dt} \begin{bmatrix} \phi_{s\alpha} \\ \phi_{s\beta} \end{bmatrix} \\ \begin{bmatrix} V_{r\alpha} \\ V_{r\beta} \end{bmatrix} = 0 = \begin{pmatrix} R_r & 0 \\ 0 & R_r \end{pmatrix} \begin{pmatrix} i_{r\alpha} \\ i_{r\beta} \end{pmatrix} + \frac{d}{dt} \begin{bmatrix} \phi_{r\alpha} \\ \phi_{r\beta} \end{bmatrix} + \frac{d\theta_r}{dt} \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{bmatrix} \phi_{r\alpha} \\ \phi_{r\beta} \end{bmatrix} \end{cases} \quad (7)$$

Equation of flux linkage can be expressed as:

$$\begin{cases} \begin{bmatrix} \phi_{s\alpha} \\ \phi_{s\beta} \end{bmatrix} = \begin{pmatrix} L_s & 0 \\ 0 & L_s \end{pmatrix} \begin{pmatrix} i_{s\alpha} \\ i_{s\beta} \end{pmatrix} + \begin{pmatrix} M & 0 \\ 0 & M \end{pmatrix} \begin{pmatrix} i_{r\alpha} \\ i_{r\beta} \end{pmatrix} \\ \begin{bmatrix} \phi_{r\alpha} \\ \phi_{r\beta} \end{bmatrix} = \begin{pmatrix} L_r & 0 \\ 0 & L_r \end{pmatrix} \begin{pmatrix} i_{r\alpha} \\ i_{r\beta} \end{pmatrix} + \begin{pmatrix} M & 0 \\ 0 & M \end{pmatrix} \begin{pmatrix} i_{s\alpha} \\ i_{s\beta} \end{pmatrix} \end{cases} \quad (8)$$

with: $M = \frac{3}{2} m_{sr}, L_r = l_r - m_r, L_s = l_s - m_s$

$$[\phi_{cc}] = \eta_{cc}^2 l_s i_{cc} + \eta_{cc} \sqrt{\frac{2}{3}} \begin{pmatrix} L_s & 0 \\ 0 & L_s \end{pmatrix} \begin{pmatrix} i_{s\alpha} \\ i_{s\beta} \end{pmatrix} + \eta_{cc} \sqrt{\frac{2}{3}} M \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} i_{r\alpha} \\ i_{r\beta} \end{pmatrix} \quad (9)$$

After transformation into (α, β) coordinates, the mathematical model of the induction motor is given as follows:

$$V_{s\alpha} = R_s i_{s\alpha} + \frac{d}{dt} \left(L_s i_{s\alpha} + \eta_{cc} L_s \sqrt{\frac{2}{3}} i_{cc} + M i_{r\alpha} \right) \quad (10)$$

$$V_{s\beta} = R_s i_{s\beta} + \frac{d}{dt} \left(L_s i_{s\beta} + M i_{r\beta} \right) \quad (11)$$

$$V_{r\alpha} = 0 = R_r i_{r\alpha} + \frac{d}{dt} \left(M i_{s\alpha} + \eta_{cc} M \sqrt{\frac{2}{3}} i_{cc} + L_r i_{r\alpha} \right) + \frac{d\theta}{dt} (M i_{s\beta} + L_r i_{r\beta}) \quad (12)$$

$$V_{r\beta} = 0 = R_r i_{r\beta} + \frac{d}{dt} (M i_{s\beta} + L_r i_{r\beta}) - \frac{d\theta}{dt} \left(M i_{s\alpha} + \eta_{cc} M \sqrt{\frac{2}{3}} i_{cc} + L_r i_{r\alpha} \right) \quad (13)$$

$$V_{cc} = 0 = \eta_{cc} R_s i_{cc} + \frac{d}{dt} \left(\eta_{cc} L_s \sqrt{\frac{2}{3}} i_{s\alpha} + \eta_{cc}^2 l_s i_{cc} + \eta_{cc} M \sqrt{\frac{2}{3}} i_{r\alpha} \right) \quad (14)$$

From previous equations, if we precede a good rearranging the machine equations can be expressed as:

$$V_{s\alpha} = R_s \left(i_{s\alpha} + \eta_{cc} \sqrt{\frac{2}{3}} i_{cc} \right) + \frac{d}{dt} \left\{ \begin{array}{l} L_s \left(1 + \eta_{cc} \frac{2}{3} \right) \left(i_{s\alpha} + \eta_{cc} \sqrt{\frac{2}{3}} i_{cc} \right) + \\ + M \left(1 + \eta_{cc} \frac{2}{3} \right) i_{r\alpha} \end{array} \right\} \quad (15)$$

To facilitate the comprehension of the equation system we put:

$$i_{s\alpha} + \eta_{cc} \sqrt{\frac{2}{3}} i_{cc} = i_{s\alpha}' \quad (16)$$

The new equation system becomes:

$$\begin{cases} \frac{V_{s\alpha}}{\left(1 + \eta_{cc} \frac{2}{3}\right)} = \frac{R_s}{\left(1 + \eta_{cc} \frac{2}{3}\right)} i_{s\alpha}' + \frac{d}{dt} \left\{ L_s i_{s\alpha}' + M i_{r\alpha} \right\} \\ V_{s\beta} = R_s i_{s\beta} + \frac{d}{dt} (L_s i_{s\beta} + M i_{r\beta}) \\ V_{r\alpha} = 0 = R_r i_{r\alpha} + \frac{d}{dt} (M i_{s\alpha}' + L_r i_{r\alpha}) + \frac{d\theta}{dt} (M i_{s\beta}' + L_r i_{r\beta}) \\ V_{r\beta} = 0 = R_r i_{r\beta} + \frac{d}{dt} (M i_{s\beta}' + L_r i_{r\beta}) - \frac{d\theta}{dt} (M i_{s\alpha}' + L_r i_{r\alpha}) \end{cases} \quad (17)$$

The last system of equations is complemented with the electromagnetic torque Γ_e that is obtained from the magnetic coenergy W_{co} .

$$\Gamma_e = [i_{sabccc}]^t \frac{\partial}{\partial \theta} [M_{sr}] [i_{rabc}] \quad (18)$$

$$\Gamma_e = \sqrt{\frac{3}{2}} M_{sr} \left(- \left(\frac{1}{3} i_{s\alpha} + \eta_{cc} i_{cc} \right) \times i_{r\beta} + i_{s\beta} \times i_{r\alpha} \right) \quad (19)$$

4. SIMULATION RESULTS

To extract in a precise way the information related to the stator defaults and to validate the mathematical model, we used the spectra of stator current to make possible accurately the visualization of the indices for detection and identification of the shorted faults. The differential equations obtained are treated in the fourth order Runge-Kutta method. In the corresponding FFT spectrum of the current (show Figure. 2) it can be possible to identify precise frequencies correlated to early fault. We clearly observe that amplitude of some negative and positive frequencies are responsive of the fault. Theses frequencies increase with the augmentation of interturn short circuit. We remark the augmentation of $-f$ frequency. This inverse sequence is reflected on the rotor side and produces new components in the stator currents at frequencies $\pm 3f$ these frequencies which appear after application of the interturn short circuit fault are very quoted in the literature. This result shows the correctness of our model.

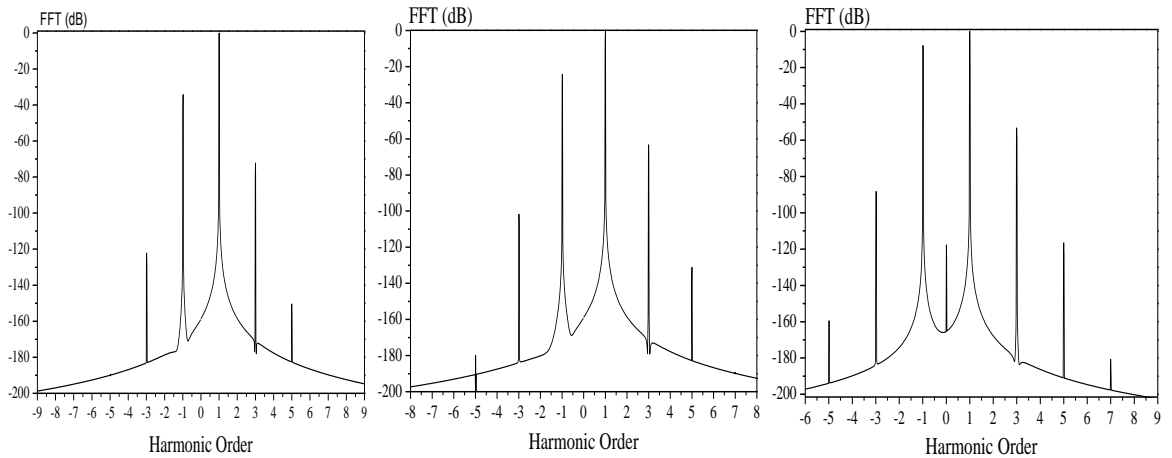


Figure 2. Simulation result of the spectra of the vector of Park of an induction machine under 2% , 10% and 20% of inter-turn short circuit fault

5. EXPERIMENTAL RESULTS

The experimental platform has been developed to study different conditions of operation of the electric machine in the healthy state or with shorted faults under different load conditions. The load is a magnetic powder brake, which makes it possible to apply the different load torques. The tested induction machine used in experimentation is a three-phase asynchronous motor, 50 Hz, 4 poles, 1.1 kW, rated at 400V, 2.95 A and 1450 rpm. The machine have re-winding with intermediate wires were distributed over two of the three phases with the objective of choosing previously a number of shorted turns. The welded connections are taken back to a terminal plate [12]. Measurements of the stator currents and voltages of the machine are performed using the voltage and current sensors. Then these values are recorded by the LeCroy Wave Runner 6050 oscilloscope which includes 4 signal acquisition channels, offers 5GS/s on each ADC channel and 1 MB of standard memory. The sampling frequency chosen for each data acquisition is 25kHz, for a duration of 2s. After acquisition, MATLAB programs are used for frequency domain analysis. To confirm experimentally the exactitude of the model we present normalized FFT spectral of the stator current motor in healthy condition and with 2% interturn shorted faults: no load condition. (see Figure. 3.). These figures clearly show the same simulation fault frequencies. In the case of healthy conditions we remark the presence of negative sequence component frequency. It is universally known, that an electrical or magnetic non rotational asymmetry of induction machine or an asymmetry in the supply voltages can be detected through stator current negative component. After application of 2% interturn shorted faults the magnitudes of some frequencies are increase with the application of the fault. The complete observation from these frequencies faults are given in Figure. 4 for 10 and 20 of interturn shorted fault respectively. In a general way we remark that magnitude of third negative and five positive frequencies are very influenced by the fault. The experiment results have a satisfactory conformity with the simulation one what confirms the validity of the developed model. Interturn shorted faults are detected by study the comparison of specific frequencies amplitudes with and without the fault. It is also possible to know the percentage of the fault according to the amplitude in decibel.

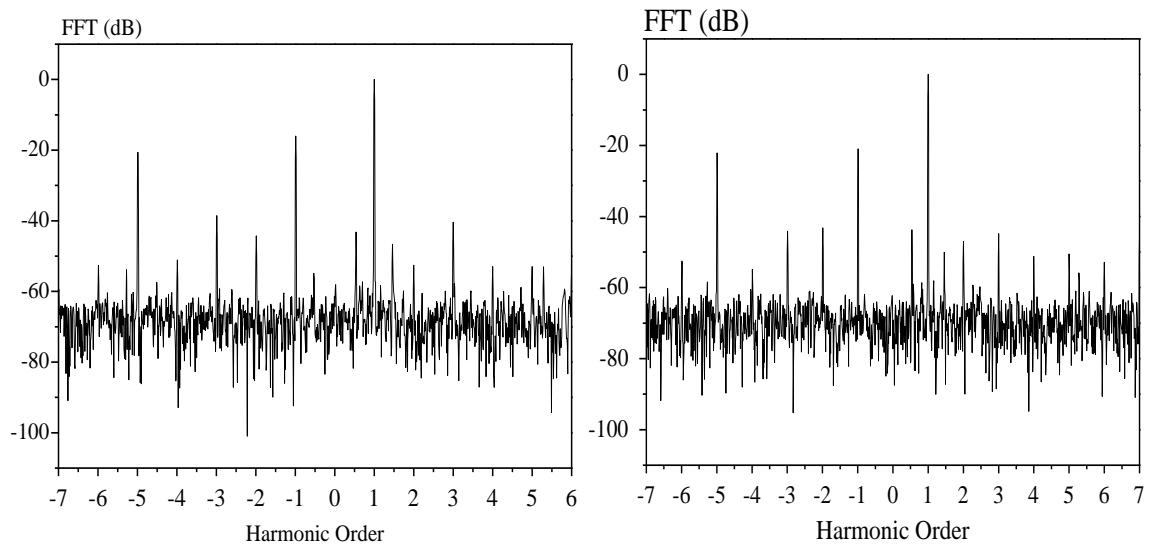


Figure 3. Normalized FFT spectrum of the stator current, machine in healthy machine (left), and 2% inter turn short circuits faults (right), no load condition

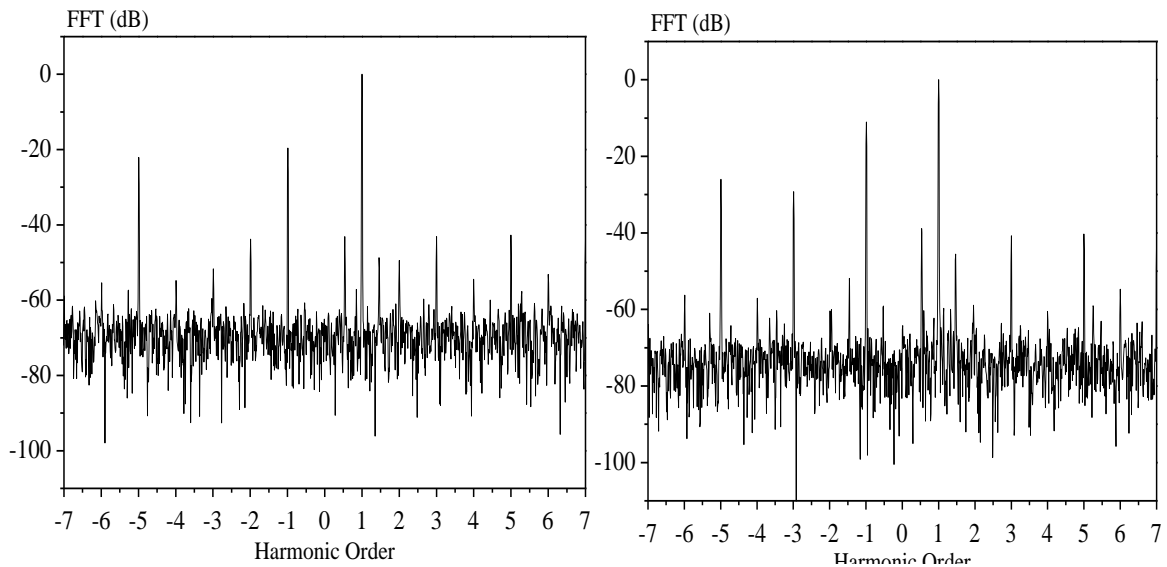


Figure 4. Normalized FFT spectrum of the stator current, machine with 10% (left) and 20% (right) of inter turn short circuits faults: no load condition

6. CONCLUSION (10 PT)

An accurate model for induction motors with turn to turn shorted faults is developed using reference frame transformation theory. Using motor current signature analysis method (MCSA) to diagnose and extract a good and accurate indicator related of the default, we confirm the effectiveness of the proposed model. The proposed model reduces the number of variable and cancelled the complexity of the rotor angular position. The originality of this paper is also to demonstrate the relationship between the interturn short circuit and unbalanced voltage supply. We remark in the model that the resemblance between interturn short circuit and unbalanced voltage supply is only reducing of amplitude of the voltage supply, and a same difference in its resistance.

REFERENCES (10 PT)


The main references are international journals and proceedings. All references should be to the most pertinent and up-to-date sources. References are written in **IEEE style**. Please use a consistent format for references – see examples below (9 pt):

- [1] H. Henao, G. and A. Capolino, M. Fernandez and Cabanas, and F. Filippetti, and C. Bruzzese, and E. Strangas, "Trends in fault diagnosis for electrical machines: A review of diagnostic techniques," *IEEE industrial electronics magazine*, vol. 8, pp. 31-42, 2014.
- [2] M. h. Drif and A. J. M. Cardoso, "Stator fault diagnostics in squirrel cage three-phase induction motor drives using the instantaneous active and reactive power signature analyses," *IEEE Transactions on Industrial Informatics*, vol. 10, pp. 1348-1360, 2014.
- [3] L. Xiao, H. Sun, F. Gao, S. Hou, L. Li, "A New Diagnostic Method for Winding Short-Circuit Fault for SRM Based on Symmetrical Component Analysis." *Chinese Journal of Electrical Engineering*, Vol.4. No.1, March 2018.
- [4] L. Maraaba, Z. Al-Hamouz, and M. Abido, "An Efficient Stator Inter-Turn Fault Diagnosis Tool for Induction Motors," *Energies*, vol. 11, p. 653 (2018).
- [5] S. M. A. Cruz and A. J. Marques Cardoso, "Modelling and simulation of stator winding faults in three-phase induction motors, including rotor skin effect," *Conference Record ICEM 2002 15th international Conference on electrical Machines, Brugge, Belgium* (August 2002).
- [6] A. Gandhi, T. Corrigan, and L. Parsa, "Recent advances in modeling and online detection of stator interturn faults in electrical motors," *IEEE Trans. Ind. Electron.*, vol. 58, no. 5, pp. 1564–1575 (May 2011).
- [7] A. Garcia-Perez, R. de Jesus Romero-Troncoso, E. Cabal-Yepez, and R. A. Osornio-Rios, "The application of high-resolution spectral analysis for identifying multiple combined faults in induction motors," *IEEE Trans. Ind. Electron.*, vol. 58, no. 5, pp. 2002–2010 (May 2011).
- [8] H. Abdallah and K. Benatman, "Stator winding inter-turn short circuit detection in induction motors by parameter identification," *IET Electric Power Applications*, vol. 11, pp. 272-288 (2017).



- [9] A. Gandhi, T. Corrigan, and L. Parsa, "Recent advances in modeling and online detection of stator interturn faults in electrical motors," *IEEE Trans. Ind. Electron.*, vol. 58, no. 5, pp. 1564–1575 (May 2011).
- [10] A. Berzoy, A. A. Mohamed, and O. Mohammed, *et al.*, "Complex-Vector Model of Interturn Failure in Induction Machines for Fault Detection and Identification," *IEEE Transactions on Industry Applications*, vol. 53, pp. 2667-2678 (2017).
- [11] Andrzej Radecki, "Stator winding inter-turn short-circuit modelling of a squirrel-cage induction motor," *Power Electronics and Drives*, Vol. 1(36), No. 1 (2016).
- [12] F. Babaa ,and Abdelmalek Khezzar and Mohamed el kamel Oumaamar, "Experimental investigation and comparative study of interturn short-circuits and unbalanced voltage supply in induction machines," *Frontiers in Energy*, 2013.
- [13] Tallam, R.M and Habetler and T.G and Harley, R.G, "Stator winding turn-fault detection for closed-loop induction motor drives," *Industry Applications Conference, 2002. 37th IAS Annual Meeting. Conference Record of the*, Volume: 3 , 13-18, pp:1553 – 1557 (oct.2002).

BIOGRAPHIES OF AUTHORS (10 PT)

First author's Photo (3x4cm)	Fatima Babaa (BSc, MSC., Ph. D), born in 1975, received the engineer degree in electrical engineering in 2005 and the M.Sc. degree in 2007 and the Ph. D. degree in 2014 from Mentouri university 1 of Constantine, Algeria. Currently, she is Teaching at the Electrical Engineering Institute of the University of Constantine.
	Ouafae Bennis Received the Ph D degree in 1982 from the university of Toulouse III. She's associed professor at University of Orleans, and researcher at Prisme Laboratory France, from 1992.