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1 Title

2 Protein interaction energy landscapes are shaped by functional and also non-functional3 partners

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- 21 HS performed research
- 22 HS, MHM, SSM, WB, AL analyzed data
- 23 HS, MHM, AL designed research
- 24 HS, MHM, AL wrote the paper
- 25 AL conceived the project
- 26 The authors declare no conflict of interest.
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38 Abstract

39 In the crowded cell, a strong selective pressure operates on the proteome to limit the 40 competition between functional and non-functional protein-protein interactions. We 41 developed an original theoretical framework in order to interrogate how this competition 42 constrains the behavior of proteins with respect to their partners or random encounters. Our 43 theoretical framework relies on a two-dimensional (2D) representation of interaction energy 44 landscapes with 2D energy maps that reflect in a synthetic way the propensity of a protein to 45 interact with another protein. We investigated the propensity of protein surfaces to interact 46 with functional and arbitrary partners and asked whether their interaction propensity is 47 conserved during the evolution. Therefore, we performed several thousands of cross-docking 48 simulations to systematically characterize the whole energy landscapes of 74 proteins 49 interacting with different sets of homologs, corresponding to their functional partner's family 50 or arbitrary protein families. Then, we systematically compared the energy maps resulting 51 from the docking of a given protein with the different protein families of the dataset. 52 Strikingly, we show that the interaction propensity not only of the binding site but also of the 53 rest of the protein surface is conserved for docking partners belonging to the same protein 54 family. Interestingly, this observation holds for docked proteins corresponding to true but also 55 to arbitrary partners. Our theoretical framework enables the characterization of the energy 56 behavior of a protein in interaction with hundreds of selected partners and opens the way for 57 further developments to study the behavior of proteins in a specific environment.

58 Introduction

59 Biomolecular interactions are central for many physiological processes and are of utmost 60 importance for the functioning of the cell. Particularly protein-protein interactions have 61 attracted a wealth of studies these last decades [1-5]. The concentration of proteins in a cell 62 has been estimated to be approximately 2-4 million proteins per cubic micron [6]. In such a 63 highly crowded environment, proteins constantly encounter each other and numerous non-64 specific interactions are likely to occur [7–10]. For example, in the cytosol of S. cerevisiae a 65 protein can encounter up to 2000 different proteins [11]. In this complex jigsaw puzzle, each 66 protein has evolved to bind the right piece(s) in the right way (positive design) and to prevent 67 misassembly and non-functional interactions (negative design) [12–16]).

68 Consequently, positive design constrains the physico-chemical properties and the evolution of 69 protein-protein interfaces. Indeed, a strong selection pressure operates on binding sites to 70 maintain the functional assembly including the functional partner and the functional binding 71 mode. For example, homologs sharing at least 30% sequence identity almost invariably 72 interact in the same way [17]. Conversely, negative design prevents proteins to be trapped in 73 the numerous competing non-functional interactions inherent to the crowded environment of 74 the cell. Many studies were reported on the relationship between the propensity of proteins for 75 promiscuous interactions and their abundances or surface properties [18-21]. Particularly, it 76 has been shown that the misinteraction avoidance shapes the evolution and physico-chemical 77 properties of abundant proteins, resulting in a slower evolution and less sticky surfaces than 78 what is observed for less abundant ones [18,22–26]. The whole surface of abundant proteins 79 is thus constrained, preventing them to engage deleterious non-specific interactions that could 80 be of dramatic impact for the cell at high concentration [25]. Recently, it has been shown in E. 81 *coli* that the net charge as well as the charge distribution on protein surfaces affect the

diffusion coefficients of proteins in the cytoplasm [19,27]. Positively charged proteins move up to 100 times more slowly as they get caught in non-specific interactions with ribosomes which are negatively charged and therefore, shape the composition of the cytoplasmic proteome [27].

86 All these studies show that both positive and negative design effectively operate on the whole 87 protein surface. Binding sites are constrained to maintain functional assemblies (i.e. 88 functional binding modes and functional partners) while the rest of the surface is constrained 89 to avoid non-functional assemblies. Consequently, these constraints should shape the energy 90 landscapes of functional but also non-functional interactions so that non-functional 91 interactions do not prevail over functional ones. This should have consequences (i) on the 92 evolution of the propensity of a protein to interact with its environment (including functional 93 and non-functional partners) and (ii) on the evolution of the interaction propensity of the 94 whole surface of proteins, non-interacting surfaces being in constant competition with 95 functional binding sites. We can hypothesize that the interaction propensity of the whole 96 surface of proteins is constrained during evolution in order to (i) ensure that proteins correctly 97 bind functional partners, and (ii) limit non-functional assemblies as well as interactions with 98 non-functional partners.

In this work, we focus on protein surfaces as a proxy for functional and non-functional protein-protein interactions. We investigate their interaction energy landscapes with native and non-native partners and ask whether their interaction propensity is conserved during evolution. With this aim in mind, we performed large-scale docking simulations to characterize interactions involving either native or native-related (i.e. partners of their homologs) partners or arbitrary partners. Docking simulations enable the characterization of all possible interactions involving either functional or arbitrary partners, and thus to simulate

106 the interaction of arbitrary partners which is very difficult to address with experimental 107 approaches. Docking algorithms are now fast enough for large-scale applications and allow 108 for the characterization of interaction energy landscapes for thousand of protein couples. 109 Typically, a docking simulation takes from a few minutes to a couple of hours on modern 110 processors [28–30], opening the way for extensive cross-docking experiments [31–35]. 111 Protein docking enables the exploration of the interaction propensity of the whole protein 112 surface by simulating alternative binding modes. Here, we performed a cross-docking 113 experiment involving 74 selected proteins docked with their native-related partners and their 114 corresponding homologs, as well as arbitrary partners and their corresponding homologs. We 115 represented the interaction energy landscapes resulting from each docking calculation with a 116 two dimensional (2D) energy map in order to (i) characterize the propensity of all surface regions of a protein to interact with a given partner (either native-related or not) and (ii) easily 117 118 compare the energy maps resulting from the docking of a same protein with different sets of 119 homologous partners, thus addressing the evolution of the propensity of a protein to interact 120 with homologous partners either native or arbitrary.

121 **Results**

122

123 The interaction propensity of the whole surface of the human ubiquitin carboxyl-124 terminal hydrolase 14 is conserved for homologous protein ligands, be they functional 125 partners or random encounters

126 If positive and negative design constraint the propensity of the whole surface of proteins to 127 interact with their functional partners or random encounters, this should shape the evolution 128 of interaction energy landscapes of functional protein pairs but also of random encounter 129 pairs. Consequently, we expect that the interaction energy landscape involving a protein pair 130 (functional or arbitrary) is conserved for a homologous pair. Testing this hypothesis involves 131 being able to characterize the interaction propensity of the whole surface of a protein. 132 Therefore we designed a procedure based on a two-dimensional (2D) representation of 133 docking energy landscapes with 2D energy maps which reflect the propensity of a protein (i.e. 134 the receptor) to interact with the docked partner (i.e. the ligand) (Materials and Methods, Fig 135 1A-C). The procedure is asymmetrical and the resulting energy map provides the distribution 136 of all docking energies over the whole receptor surface thus reflecting the propensity of the 137 receptor to interact with the docked ligand. Fig 2 represents the energy maps computed for the 138 receptor 2AYN_A, the human ubiquitin carboxyl-terminal hydrolase 14 (family UCH) 139 docked with (i) its native partner (1XD3_B, ubiquitin-related family), a homolog of its partner 140 (defined as a native-related partner) (1NDD_B) and (ii) two arbitrary homologous ligands 141 (1YVB_A and 1NQD_B from the papain-like family). For all four ligands, either native-142 related or arbitrary partners, docking calculations lead to an accumulation of low-energy 143 solutions (hot regions in red) around the two experimentally known binding sites of the 144 receptor. The first one corresponds to the interaction site with the native partner, ubiquitin

145 (pdb id 2ayo). The second one corresponds to its homodimerisation site (pdb id 2ayn). This 146 indicates that native-related but also arbitrary partners tend to bind onto the native binding 147 sites of native partners as observed in earlier studies [34,36]. Indeed, the low energy solutions 148 tend to accumulate systematically in the vicinity of the two native interaction sites. Whereas 149 the low energy solutions obtained for both ligand families accumulate around the native 150 binding sites of 2AYN_A, the two ligand families display clear differences in the rest of the 151 map. Indeed, the energy maps obtained with the ligands of the ubiquitin-like family both 152 reveal two sharp hot regions around the native sites and a subset of well-defined cold regions 153 (i.e. blue regions corresponding to high energy solutions) placed in the same area in the map's 154 upper-right quadrant. In contrast, the energy maps obtained for the ligands of the papain-like 155 family display a large hot region around the two native binding sites of the receptor, 156 extending to the upper-left and bottom-right regions of the map and suggesting a large 157 promiscuous binding region for these ligands. The interaction propensity of the two binding 158 sites of 2AYN_A but also of the other regions of its surface seems to be conserved for 159 homologous ligands and specific to each ligand family whether the ligands correspond to 160 native-related partners or not (Fig 2).

161 Generalization to a large set of proteins

We asked whether this observation could be generalized to a large set of proteins. Therefore we built a database comprising 74 protein structures divided into 12 families of homologs (S1 Table and *Materials and Methods*). Each family displays different degrees of structural variability and sequence divergence in order to see the impact of these properties on the conservation of the interaction propensity inside a protein family. Each family has at least one native-related partner family (S1 Fig). For a protein A, we refer as native-related partners its native partner (when its three dimensional (3D) structure is available) and native partners of

169 proteins that are homologous to the protein A. Arbitrary pairs refer to pairs of proteins for 170 which no interaction has been experimentally characterized in the Protein Data Bank neither 171 for their respective homologs [37]. Docking calculations are performed with the ATTRACT 172 software [30]. Each protein (namely the receptor) is docked with the 74 proteins (namely the 173 ligands) of the dataset (Fig 3A and *Materials and Methods*) and the 74 corresponding energy 174 maps are calculated (Fig 3B and Materials and Methods). The 74 resulting energy maps are 175 compared together with a Manhattan distance and all the energy map distances are stored in 176 an energy map distance (EMD) matrix (Fig 3C and Materials and Methods). Each matrix 177 entry (i,j) corresponds to the distance $d_{i,j}$ between the energy maps of ligands i and j docked 178 with a receptor k (Fig 3C and *Materials and Methods*). Consequently, a small distance d_{ij} 179 between ligands i and j docked with a receptor k, reflects a high similarity of their energy 180 maps. In other words, the interaction propensity of the surface of the receptor k is similar for 181 both ligands *i* and *j*. One should notice that energy maps computed for two unrelated 182 receptors are not comparable since their surfaces are not comparable as well. Therefore, the 183 procedure is asymmetrical and receptor-centered. It only compares energy maps calculated for 184 different ligands docked with the same receptor. In order to prevent any bias from the choice 185 of the receptor, each of the 74 proteins plays alternately the role of receptor and ligand. 186 Consequently, the protocol presented in Fig 3 is repeated for the entire dataset where each 187 protein plays the role of the receptor and is docked with the 74 proteins that play the role of 188 ligands, thus resulting in 74 EMD matrices. In order to quantify the extent to which the 189 interaction propensity of a receptor is conserved for homologous ligands, we evaluated to 190 what extent distances calculated between homologous ligand pairs were smaller than 191 distances calculated between random pairs. Fig 4 represents the boxplots of energy map 192 distances calculated between random ligand pairs or between homologous ligand pairs docked 193 with their native-related receptor or with the other receptors of the dataset. Homologous

ligands display significantly lower energy map distances than random ligand pairs (Wilcoxon test p = 0) indicating that energy maps produced by homologous ligands are more similar than those produced by non-homologous ligands. Interestingly, this observation holds whether the receptor-ligand pair is a native pair or not. This suggests that the interaction propensity of a receptor is conserved for homologous partners be they native-related or not.

199

200 Energy maps are specific to protein families

201 The results presented above prompted us to assess the extent to which the interaction 202 propensity of a receptor is specific to the ligand families it interacts with. If so, a receptor 203 should lead to energy maps that are specific to the different ligand families and we should be 204 able to retrieve homology relationships of ligands solely from the comparison of their energy 205 maps. Therefore, we tested our ability to predict the homologs of a given ligand based only on 206 the comparison of its energy maps with those of the other ligands. In order to prevent any bias 207 from the choice of the receptor, the 74 EMD matrices are averaged in an averaged distances 208 matrix (ADM) (see *Materials and Methods*). Each entry (i,j) of the ADM corresponds to the 209 averaged distance between two sets of 74 energy maps produced by two ligands *i* and *j*. A low 210 distance indicates that the two ligands display similar energy maps whatever the receptor is. 211 We computed a receiver operating characteristic (ROC) curve from the ADM (see Materials 212 and Methods) which evaluates our capacity to discriminate the homologs of a given ligand 213 from non-homologous ligands by comparing their respective energy maps computed with all 214 74 receptors of the dataset. The true positive set consists in the homologous protein pairs 215 while the true negative set consists in any homology-unrelated protein pair. The resulting 216 Area Under the Curve (AUC) is equal to 0.79 (Fig 5). We evaluated the robustness of the 217 ligand's homologs prediction depending on the size of the receptor subset with a bootstrap

218 procedure by randomly removing receptor subsets of different sizes (from 1 to 73 receptors). 219 The resulting AUCs range from 0.77 to 0.79, and show that from a subset size of five 220 receptors, the resulting prediction accuracy no longer significantly varies (risk of wrongly 221 rejecting the equality of two variances (F-test) >5%), and is robust to the nature of the 222 receptor subset (S2 Fig). Finally, we evaluated the robustness of the predictions according to 223 the number of grid cells composing the energy maps. Therefore, we repeated the procedure 224 using energy maps with resolutions ranging from 144x72 to 48x24 cells. S2 Table presents 225 the AUCs calculated with different grid resolutions. The resulting AUCs range from 0.78 to 226 0.8 showing that the grid resolution has a weak influence on the map comparison. All 227 together, these results indicate that homology relationships between protein ligands can be 228 detected solely on the basis of the comparison of their energy maps. In other words, the 229 energy maps calculated for a receptor docked with a set of ligands belonging to a same family 230 are specific to this family. Interestingly, this observation holds for families displaying 231 important sequence variations (S1 Table). For example, the AUC computed for the UCH and 232 ubiquitin-related families are 0.98 and 0.88 respectively despite the fact that the average 233 sequence identity of these families does not exceed 45% (S3 Fig and S1 Table). This indicates 234 that energy maps are similar even for homologous ligands displaying large sequence 235 variations.

236

We then specifically investigated the energy maps of each family in order to see whether some ligands behave energetically differently from their family members. On the 74 ligands, only five (2L7R_A, 4BNR_A, 1BZX_A, 1QA9_A, 1YAL_B) display energy maps that are significantly different from those of their related homologs (Z-tests *p-values* for the comparison of the averaged distance of each ligand with their homologs versus the averaged

242 distance of all ligands with their homologous ligands $\leq 5\%$). In order to identify the factors 243 leading to differences between energy maps involving homologous ligands, we computed the 244 pairwise sequence identity and the root mean square deviation (RMSD) between the members 245 of each family. Interestingly, none of these criteria can explain the energy map differences 246 observed within families (Fisher test p of the linear model estimated on all protein families 247 >0.1) (see Fig 6B-C for the ubiquitin-related family, S4-S14B-C Fig for the other families, 248 and S3 Table for details). Fig 6A represents a subsection of the ADM for the ubiquitin-related 249 family (i.e. the energy map distances computed between all the members of the ubiquitin-like 250 family and averaged over the 74 receptors). Low distances reflect pairs of ligands with similar 251 energy behaviors (i.e. producing similar energy maps when interacting with a same receptor) 252 while high distances reveal pairs of ligands with different energy behaviors. 2L7R_A 253 distinguishes itself from the rest of the family, displaying high-energy map distances with all 254 of its homologs. RMSD and sequence identity contribute modestly to the energy map distances observed in Fig 6A (Spearman correlation test $p^{RMSD} = 0.01$ and $p^{seq} = 0.02$ (S3) 255 256 Table, Fig 6B-C)). Fig 6D shows a projection of the electrostatic potential calculated with 257 APBS [38] on the surface of the seven ubiquitin-related family members (for more details, see 258 S15 Fig and Materials and Methods). Fig 6E represents the electrostatic maps distances 259 computed between all members of the family. 2L7R_A clearly stands out, displaying a 260 negative electrostatic potential over the whole surface while its homologs harbor a remarkable 261 fifty-fifty electrostatic distribution (Fig 6D). The negatively charged surface of 2L7R_A is 262 explained by the absence of the numerous lysines that are present in the others members of 263 the family (referred by black stars, Fig 6D). Lysines are known to be essential for ubiquitin 264 function, enabling the formation of polyubiquitin chains on target proteins. Among the seven 265 lysines of the ubiquitin, K63 polyubiquitin chains are known to act in non-proteolytic events 266 while K48, K11, and the four other lysines polyubiquitin chains are presumed to be involved 267 into addressing proteins to the proteasome [39]. 2L7R_A is a soluble UBL domain resulting 268 from the cleavage of the fusion protein FAU [40]. Its function is unrelated to proteasomal 269 degradation, which might explain the lack of lysines on its surface and the differences 270 observed in its energy maps. Interestingly, the differences observed for the energy maps of 271 1YAL_B (Papain-like family) (S4 Fig) and 4BNR_A (eukaryotic proteases family) (S5 Fig) 272 regarding their related homologs can be explained by the fact that they both display a highly 273 charged surface. These two proteins are thermostable [41,42], which is not the case for their 274 related homologs, and probably explains the differences observed in their relative energy 275 maps. The V-set domain family is split into two major subgroups according to their averaged 276 energy map distances (S6A Fig). The first group corresponds to CD2 proteins (1QA9_A and 277 its unbound form 1HNF_A) and differs significantly from the second group (Z-test p = 0.03278 and p = 0.05 respectively). The second group corresponds to CD58 (1QA9_B and its unbound 279 form 1CCZ_A) and CD48 proteins (2PTT_A). Interestingly, CD2 is known to interact with its 280 homologs (namely CD58 and CD48) through an interface with a striking electrostatic 281 complementarity [43]. The two subgroups have thus evolved distinct and specific binding 282 sites to interact together. We can hypothesize that they have different interaction propensities 283 resulting in the differences observed between their corresponding energy maps. These five 284 cases illustrate the capacity of our theoretical framework to reveal functional or biophysical 285 specificities of homologous proteins that could not be revealed by classical descriptors such 286 as RMSD or sequence identity.

The AUC of 0.79 calculated previously with energy maps produced with the docking of either native-related or arbitrary pairs indicates that energy maps are specific to ligand families. To see whether this observation is not mainly due to the native-related pairs, we repeated the previous test while removing that time all energy maps computed with native-related pairs and calculated the resulting ADM. We then measured our ability to retrieve the homologs of

292 each ligand by calculating the ROC curve as previously. The resulting AUC is still equal to 293 0.79, revealing that our ability to identify a ligand's homologs is independent from the fact 294 that the corresponding energy maps were computed with native-related or arbitrary pairs (Fig 295 5). This shows that the energy maps are specific to protein families whether the docked pairs 296 are native-related or not. Consequently, the propensity of the whole protein surface to interact 297 with a given ligand is conserved and specific to the ligand family whether the ligand is native-298 related or not. This striking result may reflect both positive and negative design operating on 299 protein surfaces to maintain functional interactions and to limit random interactions that are 300 inherent to a crowded environment.

301

302 The interaction propensity of all surface regions of a receptor is evolutionary conserved 303 for homologous ligands

304 To see whether some regions contribute more to the specificity of the maps produced by 305 homologous ligands, we next dissected the effective contribution of the surface regions of the 306 receptor defined according to their docking energy value, in the identification of ligand's 307 homologs. We discretized the energy values of each energy map into five categories, leading 308 to a palette of five energy classes (see Fig 1D and *Materials and Methods*). These five-classes 309 maps highlight low-energy regions (i.e. hot regions in red), intermediate-energy regions (i.e. 310 warm, lukewarm and cool regions in orange, light-green and dark-green respectively) and 311 high-energy regions (i.e. cold regions in blue). We first checked that the discretization of the 312 energy maps does not affect our ability to identify the homologs of each of the 74 ligands 313 from the comparison of their five-classes maps. The resulting AUC is 0.77 (Table 1), showing 314 that the discretization step does not lead to an important loss of information.

315

316 Then, we evaluated the contribution of each of the five energy classes separately in the 317 ligand's homologs identification by testing our ability to retrieve the homologs of the 74 318 ligands from their one-class energy maps (either hot, warm, lukewarm, cool or cold) (see 319 Materials and Methods). Table 1 shows the resulting AUCs. Interestingly, the information 320 provided by each energy class taken separately is sufficient for discriminating the homologs 321 of a given ligand from the rest of the dataset (Table 1). The resulting AUCs range from 0.76 322 to 0.79 for the warm, lukewarm, cool and cold classes and are comparable to those obtained 323 with all classes taken together (0.77). This shows (i) that warm, lukewarm, cool, and cold 324 regions alone are sufficient to retrieve homology relationships between ligands and (ii) that 325 the localization on the receptor surface of a given energy class is specific to the ligand 326 families. Hot regions are less discriminative and lead to an AUC of 0.73. In order to see how 327 regions of an energy class are distributed over a receptor surface, we summed the one-class 328 maps of the corresponding energy class calculated for this receptor into a stacked map (S16 329 Fig - see Materials and Methods for more details). A stacked map reflects the tendency of a 330 surface region (i.e. map cells) to belong to the corresponding energy class. Fig 7 shows an 331 example of the five stacked maps (i.e. for cold, cool, lukewarm, warm and hot regions) 332 computed for the receptor 1P9D_U. Intermediates regions (i.e. warm, lukewarm and cool 333 regions) are widespread on the stacked map while cold and hot regions are localized on few 334 small spots (three and one respectively) no matter the nature of the ligand. S17 Fig shows for 335 the receptor 1P9D_U the 12 cold and hot stacked maps computed for each ligand family 336 separately. We can see that some cold spots are specific to ligand families and that their area 337 distribution is specific to families while all 12 ligand families display the same hot spot in the 338 map's upper-right quadrant. These observations can be generalized to each receptor. On 339 average, intermediate regions are widespread on the stacked maps and cover respectively 744,

340 1164 and 631 cells for cool, lukewarm and warm regions, while cold and hot regions cover no 341 more than respectively 104 and 110 cells respectively (S18 Fig). Interestingly, hot regions are 342 more colocalized than cold ones and are restricted to 2 distinct spots on average per stacked 343 map, while cold regions are spread on 3.7 spots on average (t-Test p = 7.42e-13). These 344 results show that ligands belonging to different families tend to dock preferentially on the 345 same regions and thus lead to similar hot region distributions on the receptor surface. This 346 observation recalls those made by *Fernandez-Recio et al.* [36], who showed that docking 347 random proteins against a single receptor leads to an accumulation of low-energy solutions 348 around the native interaction site and who suggested that different ligands will bind 349 preferentially on the same localization.

350

351 We can hypothesize that hot regions present universal structural and biochemical features that 352 make them more prone to interact with other proteins. To test this hypothesis, we computed 353 for each protein of the dataset, the 2D projection of three protein surface descriptors (see 354 Materials and Methods and S15 Fig): the Kyte-Doolittle (KD) hydrophobicity [44], the 355 circular variance (CV) [45] and the stickiness [25]. The CV measures the density of protein 356 around an atom and is a useful descriptor to reflect the local geometry of a surface region. CV 357 values are comprised between 0 and 1. Low values reflect protruding residues and high values 358 indicate residues located in cavities. Stickiness reflects the propensity of amino acids to be 359 involved in protein-protein interfaces [25]. It is calculated as the log ratio of the residues 360 frequencies on protein surfaces versus their frequencies in protein-protein interfaces. For each 361 receptor, we calculated the correlation between the docking energy and the stickiness, 362 hydrophobicity or CV over all cells of the corresponding 2D maps. We found a significant 363 anti-correlation between the docking energy and these three descriptors (correlation test p

364 between docking energies and respectively stickiness, hydrophobicity and CV < 2.2e-16, see 365 S4 Table)). Fig 8 represents the boxplots of the stickiness, hydrophobicity and CV of each 366 energy class (see S15 Fig and Materials and Methods section for more details). We observe a 367 clear effect of these factors on the docking energy: cold regions are the less sticky, the less 368 hydrophobic and the most protruding while hot ones are the most sticky, the most 369 hydrophobic and the most planar (Tukey HSD test [46], p of the differences observed 370 between each energy classes < 2.2e-16). One should notice that stickiness has been defined 371 from a statistical analysis performed on experimentally characterized protein interfaces and 372 therefore between presumed native partners. The fact that docking energies (physics-based) 373 calculated either between native-related or arbitrary partners is anti-correlated with stickiness 374 (statistics-based) defined from native interfaces, strengthens strongly the concept of stickiness 375 as the propensity of interacting promiscuously and provides physics-based pieces of evidence 376 for sticky regions as a proxy for promiscuous interactions.

We show that not only the area distribution on a receptor surface of hot regions but also those of intermediate and cold regions are similar for homologous ligands and are specific to ligand families (AUC ranging from 0.73 to 0.79) whether the ligands are native-related or not. This tendency is even stronger for intermediate and cold regions. Interestingly, the information contained in the cold regions that cover on average no more than 5.0% of the energy maps is sufficient to identify homology relationships between ligands.

383 Discussion

384 In this study, we address the impact of both positive and negative design on thousands of 385 interaction energy landscapes by the mean of a synthetic and efficient representation of the 386 docking energy landscapes: two-dimensional energy maps that reflect the interaction 387 propensity of the whole surface of a protein (namely the receptor) with a given partner 388 (namely the ligand). We show that the distribution on the protein surface of all regions, 389 including cold, intermediate and hot regions are similar for homologous ligands and are 390 specific to ligand families whether the ligands are native-related or arbitrary. This reveals that 391 the interaction propensity of the whole surface of proteins is constrained by functional and 392 non-functional interactions, reflecting both positive and negative design operating on the 393 whole surface of proteins, thus shaping the interaction energy landscapes of functional 394 partners and random encounters. These observations were made on a dataset of 74 protein 395 structures belonging to 12 families of structural homologs. 54 out of the 74 proteins of the 396 dataset have at least one known partner in the dataset. For the 20 remaining proteins, we were 397 not able to find evidences that they indeed interact with a protein of the dataset. However, we 398 showed that the interaction propensity of a receptor is conserved for homologous ligands 399 independently from the fact that these ligands correspond to native partners or not. Indeed, we 400 showed that ligand homology relationships could be retrieved from their energy maps 401 whether the maps were computed with native-related pairs or not (the corresponding AUCs 402 calculated with and without native pairs both equal to 0.79).

Most studies that aim at depicting protein interactions focus on the functional ones and on the characterization of the native assembly modes [14,47–51]. Nevertheless, the importance of non-specific interactions and non-native assembly modes in protein interactions is no longer in doubt [7,19,21,27,52–55]. Experimental and *in-silico* studies showed the impact of non407 specific interactions on the in-cell mobility of proteins [7,19,21,27]. In addition, an important 408 literature describes the relationship between the physico-chemical properties of proteins and 409 their ability for non-specific interactions [7,19,21,25,53]. In particular, Wang et al showed 410 that the propensity for non-specific interactions is determined by multiple factors such as the 411 protein charge, the conformational flexibility and the distribution of hydrophobic residues on 412 the protein surface [19]. Finally, recent studies have demonstrated the importance of non-413 native assembly modes and non-interacting regions in the protein association process [54] and 414 showed that it is relevant to consider them for predicting protein partners and binding 415 affinities [56,57]. Particularly, Marin-Lopez et al developed a method based on the sampling 416 of the conformational space of the encounter complexes formed during the binding process 417 and showed that ΔG can be predicted accurately from the scoring of all encounter complexes 418 sampled during a docking simulation, suggesting that the knowledge of the native pose is not 419 necessary [57]. All these works highlight the importance of taking into account the whole 420 surface of proteins as well as all the binding modes of a protein pair. This calls for the 421 development of new methods that enable the systematic and physical characterization of the 422 whole surface of a protein in interaction with a given partner. Here, we address the energy 423 behavior of not only known binding sites, but also of the rest of the protein surface, which 424 plays an important role in protein interactions by constantly competing with the native 425 binding site. We show that the interaction propensity of the rest of the surface is not 426 homogeneous and displays regions with different binding energies that are specific to ligand 427 families. This may reflect the negative design operating on these regions to limit non-428 functional interactions [14,16,58]. We can hypothesize that non-interacting regions participate 429 to favor functional assemblies (i.e. functional assembly modes with functional partners) over 430 non-functional ones and are thus evolutionary constrained by non-functional assemblies. The 431 fact that cold regions seem to be more specific to ligand families than hot ones may be

432 explained by the fact that they are on average more protuberant and more charged. They thus 433 display more variability than hot ones. Indeed, there is more variability in being positively or 434 negatively charged and protuberant (with an important range of protuberant shapes) than in 435 being neutral and flat. S19 Fig presents the electrostatic potential distribution of all energy 436 classes. Cold regions display a larger variability of electrostatic potential (F-test, p < 2.2e-16) 437 than hot regions that are mainly hydrophobic thus displaying neutral charge distributions in 438 average. Consequently, a same hot region may be attractive for a large set of ligands while a 439 cold region may be unfavorable to specific set of ligands, depending on their charges, shapes 440 and other biophysical properties.

441 Moreover, we show that hot regions are very localized (4.9% of the cells of an energy map) 442 and tend to be similar no matter the ligand. Similarly to protein interfaces that have been 443 extensively characterized in previous studies [47,48,48–50], hot regions are likely to display 444 universal properties of binding, i.e. they are more hydrophobic and more planar, and thus 445 more "sticky" than the other regions. They may provide a non-specific binding patch that is 446 suitable for many ligands. However, we can hypothesize that native partners have evolved to 447 optimize their interfaces (positive design) so that native interactions prevail over non-native 448 competing ones. Then positive design results in conserved binding sites and coevolved 449 interfaces in order to maintain the charge and shape complementarity between functional 450 partners. Indeed, we have previously shown that the docking of native partners lead to more 451 favorable binding energies than the docking of non-native partners when the ligand is 452 constrained to dock around the receptor's native binding site [33,59]. All these results suggest 453 a new physical model of protein surfaces where protein surface regions, in the crowded 454 cellular environment, serve as a proxy for regulating the competition between functional and 455 non-functional interactions. In this model, intermediate and cold regions play an important 456 role by preventing non-functional assemblies and by guiding the interaction process towards

457 functional ones and hot regions may select the functional assembly among the competing 458 ones through optimized interfaces with the native partner. This model recalls the transitive 459 model proposed by Marin-Lopez et al where a path connecting what they call "productive" 460 (near-native) and "non-productive" (non-native) assemblies can be defined [57]. This path 461 consists in distinct conformational states where each one is a macro-state of the binding 462 process involving either the native binding site of each partner, a single native binding site or 463 no native ones. The initial steps consist in macro-states which do not involve native binding 464 sites. Macro-states appearing later during the assembly process would play a mechanistic role 465 by drawing near the binding sites of the two partners. The latest stage would correspond to 466 near-native conformations where van der Waals and de-solvation energies play a major role in 467 the energy of interaction of the corresponding complexes while the electrostatic forces 468 contribute mostly in the energy of non-native assemblies [60,61]. Figure S21 shows the 469 effective electrostatic and van der Waals contributions in the total docking energy for the 470 different surface regions (i.e. cold, intermediate and hot regions). Interestingly, our results 471 concur with the observations made in [60,61] since we show that the contribution of 472 electrostatic in the total docking energy is more important in cold regions while van der 473 Waals energies predominate in hot ones. Characterizing the relationship between the macro-474 states defined by Marin-Lopez et al and the surface regions of different energy levels could 475 provide at the same time a structural, physical and readable characterization of the binding 476 process of two interacting proteins. In particular, it would be interesting to compare the 477 properties of the different macro-states (involving or not the native binding sites of the two 478 proteins) identified for functional and arbitrary pairs to see whether functional pairs displays 479 specific features that would have resulted from an optimization of the binding process.

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481 In this work, we used and extended the application of the 2D energy map representation 482 developed in [36] to develop an original theoretical framework that enables the efficient, 483 automated and integrative analysis of different protein surface features. Many other surface 484 representations have been developed to characterize protein surface properties [62–67]. These 485 representations include 2D projections or more sophisticated methods such as for example 486 using 3D Zernike descriptors as a representation of the protein surface shape [68.69] which is 487 a powerful tool to compare surface properties of either homologous or unrelated proteins 488 since it does not require any prior alignment. 2D maps provide the area distribution of a given 489 feature on the whole protein surface and their discretization enables the study of a given 490 surface property (e.g. protuberance, planarity, stickiness, positively charged regions, or cold 491 and hot regions for example). The advantage with the 2D energy maps is that they are easy to 492 build and manipulate and their straightforward comparison enables (i) the study of 493 relationships between different surface properties through the comparison of their area 494 distributions on a protein surface and (ii) the highlight of the evolutionary constraints exerted 495 on a given feature by comparing its area distribution on the surfaces of homologous proteins. 496 Particularly, this enables the identification and characterization of hot regions on a protein 497 surface which can be either specific or conserved for all ligands and opens up new 498 possibilities for the development of novel methods for protein binding sites prediction and 499 their classification as functional or promiscuous in the continuity of previous developments 500 based on arbitrary docking [33,34,36,59].

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502 Finally, our framework provides a proxy for further protein functional characterization as 503 shown with the five proteins discussed in the *Results* section *Energy maps are specific to* 504 *protein families*. The comparison of their respective energy maps enables us to reveal

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505 biophysical and functional properties that could not be revealed with classical monomeric 506 descriptors such as RMSD or sequence identity. Indeed, our framework can reflect the energy 507 behavior of a protein interacting with a subset of selected partners either functional or 508 arbitrary, thus revealing functional and systemic properties of proteins. This work goes 509 beyond the classical use of binary docking to provide a systemic point of view of protein 510 interactions, for example by exploring the propensity of a protein to interact with hundreds of 511 selected ligands, and thus addressing the behavior of a protein in a specific cellular 512 environment. Particularly, exploring the dark interactome (i.e. non-functional assemblies and 513 interactions with non-functional partners) can provide a wealth of valuable information to 514 understand mechanisms driving and regulating protein-protein interactions. Precisely, our 2D 515 energy maps based strategy enables its exploration in an efficient and automated way.

516 Materials and Methods

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518 **Protein dataset**

519 The dataset comprises 74 protein structures divided into 12 families of structural homologs 520 which were selected from the protein docking benchmark 5.0. (see S1 Table for a detailed list 521 of each family). We decided to systematically remove all Antibody/Antigens complexes since 522 they display specific evolutionary properties. Indeed, they did not co-evolve to interact and 523 we can hypothesize that the evolutionary constraints operating on their interaction energy 524 landscapes are different from those of other complexes. Each family is related to at least one 525 other family (its native-related partners family) through a pair of interacting proteins for 526 which the 3D structure of the complex is characterized experimentally (except the V set 527 domain family: the two native partners are homologous and belong to the same family) (S1 528 Fig). Each family is composed of a monomer selected from the protein-protein docking 529 benchmark 5.0 [70] in its bound and unbound forms, which is called the master protein. Each 530 master protein has a native partner (for which the 3D structure of the corresponding complex 531 has been characterized experimentally) in the database, which is the master protein for 532 another family, except the V set domain family, which is a self-interacting family. When 533 available, we completed families with interologs (i.e. pairs of proteins which have interacting 534 homologs in an other organism) selected in the INTEREVOL database [71] according to the following criteria: (i) experimental structure resolution better than 3.25 Å, (ii) minimum 535 536 alignment coverage of 75% with the rest of the family members and (iii) minimum sequence 537 identity of 30% with at least one member of the family. Since we were limited by the number 538 of available interologs, we completed families with unbound monomers homologous to the

539 master following the same criteria and by searching for their partners in the following protein-540 protein interactions databases [72–77]. We consider that all members of a family correspond 541 to native-related partners of all members of their native-related partner family. To address the 542 impact of conformational changes of a protein on its interaction energy maps, we added 543 different NMR conformers. We show that energy maps involving pairs of conformers are 544 significantly more similar than those obtained for other pairs of homologous ligands 545 (unilateral Wilcoxon test, p < 2.2e-16) showing that the conformational changes in a protein 546 (lower than 3Å) have a low impact on the resulting energy maps (S20 Fig).

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548 Docking experiment and construction of energy maps

A complete cross-docking experiment was realized with the ATTRACT software [30] on the 74 proteins of the dataset, leading to 5476 (74 x 74) docking calculations (Fig 1A). ATTRACT uses a coarse-grain reduced protein representation and a simplified energy function comprising a pseudo Lennard-Jones term and an electrostatic term. The calculations took approximately 20000 hours on a 2.7GHz processor. Prior to docking calculations, all PDB structures were prepared with the DOCKPREP software [78].

555 During a docking calculation, the ligand L_i explores exhaustively the surface of the receptor 556 R_k (whose position is fixed during the procedure), sampling and scoring thousands of 557 different ligand docking poses (between 10000 and 50000 depending on the sizes of the 558 proteins) (Fig 1A). For each protein couple R_k - L_i , a 2D energy map is computed which shows 559 the distribution of the energies of all docking solutions over the receptor surface. To compute 560 these maps, for all docking poses, the spherical coordinates (ϕ , θ) (with respect to the 561 receptor center of mass (CM)) of the ligand CM are represented onto a 2D map in an equal562 area 2D sinusoidal projection (Fig 1B) (see [36] for more details). Each couple of coordinates 563 (ϕ, θ) is associated with the energy of the corresponding docking conformation (Fig 1B). A 564 continuous energy map is then derived from the discrete one, where the map is divided into a 565 grid of 36 x 72 cells. Each cell represents the same surface and, depending on the size of the receptor, can span from 2.5 $Å^2$ to $13Å^2$. For each cell, all solutions with an energy score 566 below 2.7 kcal/mol⁻¹ from the lowest solution of the cell are retained, according to the 567 568 conformations filtering protocol implemented in [33]. The average of the retained energy 569 scores is then assigned to the cell. If there is no docking solution in a cell, a score of 0 is 570 assigned to it. Finally, the energies of the cells are smoothed, by averaging the energy values 571 of each cell and of the eight surrounding neighbors (Fig 1C).

572 For each map, the energy values are discretized into five energy classes of same range leading 573 to a discrete five-colors energy map (Fig 1D). The range is calculated for each energy map 574 and spans from the minimum to the maximum scores of the map cells. The range of the 575 energy classes of the map R_k -L_i is equal to (maxE – minE)/5, where maxE and minE 576 correspond to the maximal and minimal energy values in the R_k-L_i map. Each five-classes 577 energy map is then split into five one-class maps, each one representing an energy class of the 578 map (Fig 1E). The continuous, five-classes and one-class energy maps are calculated for the 579 5476 energy maps.

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581 Comparison of energy maps and identification of ligand's homologs

Since, we cannot compare energy maps computed for two unrelated receptors, the procedure is receptor-centered and only compares energy maps produced with different ligands docked with the same receptor. The referential (i.e. the receptor) is thus the same (in other words all grid cells are comparable) for all the energy maps that are compared. For each receptor R_k , we

586 computed a 74x74 energy map distance (EMD) matrix where each entry (i,j) corresponds to 587 the pairwise distance between the energy maps R_k - L_i and R_k - L_j resulting from the docking of 588 the ligands L_i and L_j on the receptor R_k (Fig 3). The pairwise distance $d_{Man}(R_k-L_i, R_k-L_j)$ 589 between the energy maps is calculated with a Manhattan distance according to equation (1)

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$$d_{Man}(R_k L_i, R_k L_j) = \sum_{n=1}^{36} \sum_{m=1}^{72} |a_{nm} - b_{nm}| \quad (1)$$

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593 where a_{nm} and b_{nm} are the cells of row index *n* and column index *m* of the energy maps R_k - L_i 594 and Rk-Li respectively. Low distances reflect pairs of ligands that induce similar energy maps 595 when they are docked on the same receptor. The procedure presented in Fig 3 is repeated for 596 each receptor of the database resulting in 74 EMD matrices. The 74 EMD matrices are 597 averaged into an averaged distances matrix (ADM). Each entry (i,j) of the ADM reflects the 598 similarity of the R_k - L_i and R_k - L_i energy maps averaged over all the receptors R_k in the dataset. 599 In order to estimate the extent to which family members display similar energy maps when 600 they are docked with the same receptor, we tested our ability to correctly identify the 601 homologs of the 74 ligands from the only comparison of its energy maps with those of the 602 other ligands. Because, energy maps are receptor-centered, we cannot compare the energy 603 maps computed for two unrelated receptors. The procedure consists in the comparison of 604 energy maps produced with different ligands docked with a same receptor. Two ligands (i,j)605 are predicted as homologs according to their corresponding distance (i,j) in the ADM. Values 606 close to zero should reflect homologous ligand pairs, while values close to one should reflect 607 unrelated ligand pairs. A Receiver Operating Characteristic (ROC) curve and its Area Under 608 the Curve (AUC) are computed from the ADM. True positives (TP) are all the homologous 609 ligand pairs and predicted as such, true negatives (TN) are all the unrelated ligand pairs and 610 predicted as such. False positives (FP) are unrelated ligand pairs but incorrectly predicted as 611 homologous pairs. False negatives (FN) are homologous ligand pairs but incorrectly predicted 612 as unrelated pairs. ROC curves and AUC values were calculated with the R package pROC 613 [79]. The ligand's homologs identification was also realized using the five-classes energy 614 maps or the one-class energy maps taken separately. The five energy class regions display 615 very different sizes, with median ranging from 63 and 66 cells for the cold and hot regions to 616 633 cells for the yellow one. To prevent any bias due to the size of the different classes, we 617 normalized the Manhattan distance by the size of the regions compared in the map. The rest 618 of the procedure is the same than those used for continuous energy maps (Fig 3).

To visualize the area distribution of the regions of a given energy class for all ligands on the receptor surface, the 74 corresponding one-class maps are summed into a stacked map where each cell's intensity varies from 0 to 74 (S16 Fig). To remove background-image from these maps, i.e. cells with low intensity (intensity < 17) and the areas of small size (< 4 cells), we used a Dirichlet process mixture model simulation for image segmentation (R package *dpmixsim*) [80].

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626 2D projection of monomeric descriptors of protein surfaces

We computed KD hydrophobicity [44], stickiness [25], CV [45] maps of each protein of the dataset, in order to compare their topology with the energy maps. Prior to all, proteins belonging to the same families were structurally aligned with TM-align [81] in order to place them in the same reference frame, making their maps comparable. Particles were generated around the protein surface with a slightly modified Shrake-Rupley algorithm [82]. The density of spheres is fixed at 1Å^2 , representing several thousands particles per protein. Each particle is located at 5Å from the surface of the protein. The CV, stickiness and KD hydrophobicity values of the closest atom of the protein are attributed to each particle. We also generated electrostatic maps reflecting the distribution of the contribution of the electrostatic potential on a protein surface. The electrostatics potential was computed with the APBS software suite [38] using the CHARMM force field [83]. In this case the procedure is different as the electrostatic potential is calculated at each particle position, using the multivalue executable from the APBS software suite.

The CV was calculated following the protocol described in [45] on the all-atom structures. Stickiness and hydrophobicity were calculated on ATTRACT coarse-grain models. After attributing a value to each particle, the position of their spherical coordinates is represented in a 2-D sinusoidal projection, following the same protocol as described in Fig 1 and *Materials and Methods* section *Docking experiment and construction of energy maps*. The map is then smoothed following the protocol in Fig 1.

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1 Fig. 1. 2D asymmetrical representation of docking energy landscapes and resulting 2 energy maps. (A) Three-dimensional (3D) representation of the ligand docking poses around 3 the receptor. Each dot corresponds to the center of mass (CM) of a ligand docking pose and is 4 colored according to its docking energy score. (B) Representation of the CM of the ligand 5 docking poses after an equal-area 2D sinusoidal projection. CMs are colored according to the 6 same scale as in A. (C) Continuous energy map (see *Materials and Methods* for more details). 7 (D) Five-class map. The energy map is discretized into five energy classes (E) One-class 8 maps. Top to bottom: one-class maps that highlight respectively hot, warm, lukewarm, cool 9 and cold regions.

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Fig. 2. Interaction propensity for the receptor 2AYN_A and four different ligands. 2D energy maps for the receptor 2AYN_A (ubiquitin carboxyl-terminal hydrolase (UCH) family) docked with the ligands 1XD3_B (native partner), 1NDD_B (homolog of the native partner), 14 1YVB_A and 2NQD_B (arbitrary partners). The star indicates the localization of the experimentally determined interaction site for the ubiquitin, the circle-cross indicates the homodimerization site of 2AYN_A.

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Fig. 3. Experimental Protocol. (*A*) A receptor protein is docked with all proteins of the dataset (namely the ligands) resulting in 74 docking calculations. (*B*) For each docking calculation, an energy map is computed as well as its corresponding five-classes and oneclass energy maps, with the procedure described in Fig 1 and *Materials and Methods*. (*C*) An energy map distance (EMD) matrix is computed, representing the pairwise distances between the 74 energy maps resulting from the docking of all ligands with this receptor. Each cell (i,j) of the matrix represents the Manhattan distance between the two energy maps resulting from the docking of ligands i and j with the receptor. A small distance indicates that the ligands iand j produce similar energy maps when docked with this receptor. In other words, it reflects that the interaction propensity of this receptor is similar for these two ligands. To prevent any bias from the choice of the receptor, the whole procedure is repeated for each receptor of the database, leading to 74 EMD matrices.

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Fig. 4. Boxplots of energy map pairwise distances between homologous ligand pairs from native-related partner families, homologous ligand pairs from arbitrary partner families and random ligand pairs. For each receptor, we computed (i) the average of energy map distances of pair of homologous ligands belonging to its native-related partner family(ies), (ii) the average of energy map distances of pair of homologous ligands belonging to its non-native-related partner families, and (iii) the average of energy map distances of arandom pairs. P-values are calculated with a unilateral Wilcoxon test.

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Fig. 5. Receiver operating characteristic (ROC) curve and its Area Under the Curve
(AUC). ROC are calculated on the averaged distance matrix (ADM) including either all pairs
(blue) or only arbitrary pairs (red) (see *Materials and Methods* for more details).

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Fig. 6. Ubiquitin-related family. (A) Energy map distances matrix. It corresponds to the subsection of the ADM for the ubiquitin-related family (for the construction of the ADM, see *Materials and Methods*). Each entry (i,j) represents the pairwise energy map distance of the ligand pair (i,j) averaged over the 74 receptors of the dataset. (B) Pairwise sequence identity

47 matrix between all members of the family. (C) Pairwise root mean square deviation (RMSD) 48 matrix between all members of the family. (D) Electrostatic maps and cartoon representations 49 of the seven members of the family. An electrostatic map represents the distribution of the 50 electrostatic potential on the surface of a protein (for more details, see S15 Fig and Materials 51 and Methods). On the electrostatic maps, lysines positions are indicated by stars. Cartoon 52 structures are colored according to the distribution of their electrostatic potential. (E)53 Electrostatic map distances matrix. Each entry (i,j) of the matrix represents the Manhattan 54 distance between the electrostatic maps of the proteins (i,j).

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56 Fig. 7. Stacked maps of 1P9D_U after the filtering of cells with too low intensity and 57 areas of too small size. The protocol to generate stacked maps is presented in S16 Fig. (A-E) 58 Stacked map for cold, cool, lukewarm, warm and hot regions respectively. The cell intensity 59 in a stacked map of a given energy class indicates the number of times the cell has been 60 associated to this energy class in all the corresponding one-class maps. One should notice that 61 stacked maps of two different energy classes can overlap because a map cell can be associated 62 to different energy classes depending on the docked ligands. S17 Fig presents cold and hot 63 stacked maps of 1P9D U computed for each ligand family.

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Fig. 8. Boxplots of three descriptors of the protein surface. (*A*) the stickiness values, (*B*) the Kyte-Doolittle hydrophobicity and (*C*) the CV values, depending on the energy class. The stickiness, hydrophobicity and CV values are calculated for each protein following the protocol described in *Materials and Methods*. For each of these criteria, *p*-values between the median values of two "successive" energy classes were computed using the Tukey HSD statistical test [46].

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Table 1. AUC obtained with different types of energy maps.

type of map	continuous	five-classes	hot energy	warm energy	lukewarm	cool energy	cold energy
	energy maps	energy maps	maps	maps	energy maps	maps	maps
AUC	0.79	0.77	0.73	0.76	0.76	0.76	0.79

The AUC are calculated from the ADM with the continuous energy maps (Fig 1C), the five-classes energy maps (Fig 1D) and the one-class energy maps (Fig 1E) (see Materials and Methods for more details).



Fig. 1



Fig 2.



Fig. 3







Fig. 5

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Fig 6.



Fig. 7

 $\varphi sin(\theta)$



Fig 8.