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Experimental and numerical investigation of natural convection flows in two horizontal thermoacoustic cavities

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Abstract

This study aims at exploring the potential generation of natural convective flows in thermoacoustic devices. To this effect, two thermoacoustic setups are considered without acoustic oscillations, each setup thus constituting a cavity filled with air and comprising a porous medium heated on one of its ends. In the first configuration, the porous medium is a ceramic stack. In the second configuration, an ambient heat exchanger using circulating ambient water is placed on the other end of the porous medium (which is a regenerator). The wall temperature is measured in several points using thermocouples and natural convection flows developing in these cavities are measured in a vertical plane using Particle Image Velocimetry. Moreover numerical calculations are performed based on simplified 3D configurations, using immersed solid bodies at prescribed temperature to represent the heating or cooling elements and describing the porous media as homogeneous and either isotropic or anisotropic. Navier-Stokes equations under Boussinesq assumption are solved in the entire domain with the addition of a Darcy correction term in the porous media. Excellent qualitative and quantitative agreement on velocity fields is obtained between experimental and

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numerical simulation results for both configurations, which validates the model description. It is shown that the observed natural convection flows are fully three-dimensional and of significant magnitude so that they could potentially interfere with thermoacoustic effects.

Keywords: natural convection; thermoacoustics; porous medium; Particle Image Velocimetry; numerical simulation

1. Introduction

Thermoacoustic devices use thermal and dynamic interactions between the acoustic oscillations of a working inert gas and conducting solid walls to generate either heat pumping for refrigerating purposes or mechanical work for engine operating purposes [1]. These interactions are called the thermoacoustic effect. They occur nearby the solid walls, in a thermal boundary layer area: the gas experiences acoustic oscillations, while exchanging heat with the solid wall. In order to increase the exchange surface area, a porous medium is used. This porous medium is placed between two heat exchangers, forming the thermoa-

- coustic core (TAC). The heat exchangers enable to either impose a temperature gradient along the porous medium, in order to produce acoustic power (engine), or to benefit from the heat pumping effect steered by an imposed acoustic oscillation (refrigerator). The thermoacoustic core represents the active part of the device, where the energy conversion takes place. Usually, thermoacoustic
- devices also include an acoustic resonator for sustaining the acoustic wave, and potentially an acoustic source or a linear electric generator, depending on the desired conversion effect. Thermoacoustic devices represent an interesting ecological alternative (almost no moving parts, the use of inert gas, simplicity) for industrial applications: cryogenics [2], air conditioning [3], domestic refrig-
- ²⁰ eration, solar powered thermoacoustic engines [4], electric energy generators (conversion of the acoustic power into electric power) [5], waste heat recovery (for example, thermoacoustic heat pumps are used to upgrade the waste heat for renewed use in the industrial process) [6]. However thermoacoustic devices

still suffer from poor performance generally caused by the existence of several

²⁵ nonlinear phenomena interfering with the process of energy transfer and deteriorating the global performance of the device. These nonlinear phenomena are related to jet-driven streaming, acoustic streaming, harmonic generation, end-effects and natural convection, and are not well described or just partially. Among these phenomena, natural convection has been the least investigated.
³⁰ The present study focuses on the effect of natural convection flows.

The influence of natural convection on starting conditions for a thermoacoustic engine was pointed out in an early paper of Gardner and Swift [7]. They observed that in the engine under study, the acoustic oscillation did not start although the design parameters were respected. This appeared to be due to a

- distortion of the mean temperature field, which was identified by the authors as originating from gravity-driven convection in the stack. The experimental procedure was modified, in order to reduce the convection flow, by decreasing the mean pressure and start the oscillation at a lower pressure. Once the oscillation was stabilized, the mean pressure was changed to its designed value. This is the
- ⁴⁰ option generally chosen by thermoacousticians: try to avoid or to reduce natural convection; but most of the time it is impossible to completely avoid it, since the devices come in a variety of geometries. The influence of the tilt angle on the starting condition of a solar powered thermoacoustic engine was analyzed more recently using Thermal Infrared Imager temperature measurements in the TAC
- [8]. In cousin devices that are pulse tube refrigerators, natural convection was also pointed out as a major source of losses [9, 10] but no detailed analysis was performed and no estimate or measurement of the natural convection velocity field is available.
- Apart from these few experimental evidence of natural convective flows in real devices, some experimental studies aimed at characterizing natural convection in simplified academic configurations. Natural convection and heat transfer inside a horizontal empty resonator, taking place between a hot heat exchanger and a cold heat exchanger, was investigated experimentally using thermal infrared imaging and particle image velocimetry (PIV) [11], and for different tilt

angles [12]. It was shown that heat transfer mode changed from natural convection to forced convection with the addition of acoustic oscillation.

The role of natural convection on the distortion of Rayleigh streaming flow was exhibited in some recent experimental studies [13, 14, 15]. Measurement of the sole convection velocity field along a vertical section of the resonator under

⁶⁰ a temperature gradient was performed in [14] in order to explain the distorted streaming velocity field observed, but the measurement was very localized and there was no theoretical explanation of the complex velocity measurements obtained. Measurements of the mean velocity field in the entire cold resonator part of a simple standing-wave thermoacoustic engine were recently performed

- ⁶⁵ by Ramadan et al. [15]. Using both PIV and LDV techniques, they showed the existence of a mean flow with or without thermoacoustic oscillations. This flow was identified as natural convection combined, when acoustic waves are present, with Rayleigh streaming. However, in this preliminary study, measurements were performed only in the central horizontal plane, which is limiting for
- ⁷⁰ the study of natural convection. More generally, a characterization of the 3D nature of the natural convection velocity field suggested by all above-cited studies is still lacking and its influence on the overall thermoaoustic heat transfer not yet quantified. This is because dedicated adequate measurements of natural convection flow and temperature distribution are difficult in real devices, due
- $_{75}$ $\,$ to the many coupled intricate physical phenomena.

From the numerical point of view, natural convection is not yet included in thermoacoustic designing tools. It is therefore necessary to develop a numerical tool that can predict the magnitude and flow pattern of natural convection flows as well as the associated temperature distribution. So far it is unreal-

- ²⁰ istic to integrate all effects in one complete numerical code, for a given complex device: acoustics, thermoacoustic energy conversion, acoustic streaming, natural convection without powerful computing resources. This is due to the existence of several distinct time scales (acoustic, thermal diffusion) and spatial scales (wavelength, viscous and thermal boundary layer thickness, device's
- characteristic scales). Such simulations would therefore be very time consum-

ing, since long physical times would have to be discretized in small time steps, and extended physical domains discretized with fine mesh. Morever, for a better understanding of how several physical processes interact, it seems relevant to study them separately in a first approach. Therefore, this study focuses on

- ⁹⁰ the natural convection flow in thermoacoustic device configurations, with no acoustic oscillation. As will be shown further, the geometrical configuration of thermoacoustic devices can generally be considered as a series of heated cavities, some of which are filled with a porous medium. Each cavity is submitted to a temperature difference, which can generate a heat-driven flow.
- ⁹⁵ Convection flows through non homogenous and anisotropic porous media in cavities heated from the side are quite well described, with studies started in the 1980s [16]. The same problem in mixed fluid and porous cavities was treated extensively in the literature [17, 18]. The convection flow depends strongly on the geometry of the cavities and the previous general studies cannot be directly
- applied to the specific case of a thermoacoustic engine. The specific geometry of a thermoacoustic stack was considered in [19], where natural convection in a 2D differentially heated horizontal cavity, filled with a stack of plates, was considered. This study showed that a Darcean porous model gives correct orders of velocity scales, and allows for a qualitative description of the solutions. A
- ¹⁰⁵ preliminary 3D numerical study of the effects of natural convection in a cylindrical guide containing an assembly of a hot heat exchanger and porous medium was conducted recently [20]. The influence of the porous medium's physical characteristics (permeability, thermal conductivity, anisotropy) on the flow and temperature fields was investigated.
- The numerical approach of [20] is pursued in this paper on realistic configurations, and confronted with experiments resulting from extending the preliminary study in [15]. In the present analysis, the experimental and numerical models were elaborated and calibrated jointly in order to improve the description of natural convection flows in a thermoacoustic system. The first objective of this
- ¹¹⁵ paper is to predict natural convection flows in configurations that are representative of such systems. The second objective is to show that the model works

well by comparison with possible measurements in parts of the device.

As mentioned above, to isolate natural convection from other phenomena, we chose to work with a thermoacoustic cavity but not with a thermoacoustic

- device; i.e. no acoustic oscillation was generated in the cavity. Whether or not natural convection should be accounted for in the design of a thermoacoustic device is going to depend highly on the device's geometry and its orientation with respect to gravity. It is also going to depend particularly on the thermophysical parameters of all constituting elements, and specifically the thermoa-
- ¹²⁵ coustic core. Therefore, and in order to explore increasingly realistic geometries, we investigate two different configurations: the first one consists in a very simplified thermoacoustic core that is composed of an electric heater attached to a ceramic stack; the second one is composed of the same two elements followed by an ambient heat exchanger. These two configurations are further referred to ¹³⁰ as horizontal cavity without ambient heat exchanger (or 1^{st} configuration), and horizontal cavity with ambient heat exchanger (or 2^{nd} configuration).

In the following, the first configuration is investigated in section 2. The experimental setup and method are described (section 2.1) and the numerical method is presented (section 2.2). Experimental and numerical results are then ¹³⁵ compared and discussed, and the potentiality of the numerical model for predicting purposes is assessed (section 2.3). The configuration with ambient heat exchanger is considered in section 3, following the same approach.

2. Horizontal cavity without ambient heat exchanger $(1^{st}$ configuration)

140 2.1. Experimental setup, measurement systems and procedure

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For this first comparison between experimental and numerical approaches, a very simple thermoacoustic cavity is used. As shown in Figure 1a, the resonator is made of a glass tube with inner and outer diameters of 39 mm and 44 mm, respectively. The total length of the resonator is 738 mm and the thermoacoustic core is placed at a distance of 129 mm away from one end of the resonator. The thermoacoustic core consists of an electric heater attached to one side of a 400 CPSI (Cell Per Square Inch) ceramic stack that has length of 60 mm. The axial coordinate is also defined in Figure 1a, with x = 0 corresponding to the right end of the ceramic stack. In such a simple thermoacoustic engine, applying high

enough temperature gradient along the stack generates sustainable standing acoustic waves. A more detailed description for the experimental setup can be found in [15]. In order to isolate the natural convection flow, the two small plugs at the ends of the resonator tube were removed to cease any acoustic oscillations and velocity measurements were performed in the central vertical plane. It was checked previously [15] that the removal of the plugs does not affect the natural convection flow.

A PIV system is used to measure the natural convection flow in the central vertical plane. The PIV system consists of a double pulse Nd:YAG laser source that illuminates the vertical plane. Two cameras (Imager Pro X) with spatial resolution of $2048 \times 2048 \, pixels^2$ and maximum repetition rate of $15 \, Hz$ are used to record the images. Each camera is equipped with a Nikon lens (Model: Sigma 105mm). The two cameras are placed next to each other in order to increase the size of the measurement Field Of View (FOV). An atomizer aerosol generator (Model: TOPAS ATM 210) is used to atomize oil to produce seeding particles

with a mean particle diameter of $0.4 \,\mu m$. In order to achieve better correlation between the acquired double-images, the time between laser pulses is adjusted to allow the seeding particles to displace a distance of about 1/4 the size of the interrogation area [21].

The measurement procedure followed in the current study is similar to the

- ¹⁷⁰ procedure we followed in our previous work [15]. In order to have enough seeding particles after the system reaches to the steady-state conditions (i.e. the change in the temperature over the PIV measurement period does not exceed 5%), the preheating technique is followed. A $31.5 W \pm 1\%$ electrical power is applied to the hot heat exchanger (coiled resistance). After the preheating of the system,
- ¹⁷⁵ the seeding particles are introduced from one extremity and flow until reaching the other extremity of the duct so that the seeding particles are dispersed over

the whole duct. The system is left for 3 minutes in order to eliminate the effects of the seeding introduction on the natural convection flow. Finally, the PIV measurements are started and 100 double-images captured. The natural

convection flow distribution is measured in the central vertical plane, covering the axial distance from x = 0 mm (end of ceramic stack) to x = 520 mm. Since wall temperatures are very important for the study of the natural convection flow, several thermocouples are used to measure the wall temperatures and the temperatures at the center of the two side sections of the ceramic stack. As shown by Figure 1b (red dots), on the tube wall for each axial position there are two temperature measurements corresponding to the top and bottom of the

The uncertainty of the measured quantities (i.e. temperature and the velocity) is estimated by repeating the measurements (3 times) under the same input electric power to the electrical heater and calculating the standard deviation of these quantities. The estimated value of the uncertainty in the temperature measurements is thus found to be ± 1 % of the reported mean temperatures. For the velocity measurements, the uncertainty of the measurements is calculated over the whole measurement area and then the spatial-average uncertainty is calculated. The spatial-average uncertainty is found to be ± 13 % of the reported velocities.

2.2. Numerical model

tube wall.

2.2.1. Numerical simulation parameters

A simplified 3D configuration is introduced in order to model the experi-²⁰⁰ mental configuration described in the previous section (Figure 2a). The domain under study is a horizontal cylindrical tube of length L and radius R, filled with air and closed at both ends.

The ceramic stack, constituted of horizontal capillaries of square cross section with side length a = 1mm, is modeled as a homogeneous and anisotropic porous medium of length L_p and radius R (see Figure 2a and Table 1a). Its porosity ϵ , defined as the ratio of gas volume to total volume is calculated based on the given geometry. The equivalent permeability in the axial direction is $K_{xx} = \frac{a^2 \epsilon}{8}$ (calculated using [18]), its permeability in the radial and azimutal directions are approximately zero (in the code they are set to $10^{-12}m^2$). The equivalent thermal conductivity is assumed isotropic and homogeneous, of scalar value $k_p = \epsilon k_{fluid} + (1 - \epsilon) k_{solid}$ (again based on [18]). The numerical values of these parameters are given by Table 1b.

The hot exchanger (coiled resistance), placed at a distance L_L from the left end, is modelled as 2 solid rings of width e_h and a central core maintained at certain hot temperature (the central core being hotter than the outside ring). 215 Temperature values prescribed in this hot heat exchanger are: 420 K on the outside ring, 523 K on the middle ring, and 627 K in the central core. Therefore the "average" hot temperature is estimated as $T_{hot} = 520 K$. Along the tube wall, temperature is imposed as a function of the axial coordinate only, based on the measured temperature distribution, as shown by Figure 2b. Since 220 for each axial position there are two measures of temperature (at the top and bottom of the outside wall) reported in Figure 1b, the average value between the two measured values was calculated and prescribed for the corresponding axial position. On the left of the HHX, the temperature distribution is then fit with an exponential function. Along the porous medium a linear variation is 225 used. Finally on the right of the porous medium the temperature distribution is fit with another exponential function (Figure 2b).

The thermophysical parameters for air are calculated for atmospheric pressure and at a reference temperature chosen to be $T_{ref} = 320 K$ which is the global mean temperature of the air.

2.2.2. Governing equations

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In the fluid domain, the Navier-Stokes equations are written as classically under Boussinesq assumptions. The reference air density ρ , thermal conductivity k, heat capacity c_p , dynamic viscosity μ , and volume expansion coefficient at constant pressure $\beta = 1/T_{ref}$ for an ideal gas are constant and equal to their value for a reference temperature T_{ref} and atmospheric pressure. The thermophysical characteristics of the porous medium are its porosity ϵ , its permeability tensor **K**, and its equivalent thermal conductivity k_p . A scalar phase variable X is introduced to identify the nature of the medium (X = 1 for gas, X = 0 for the porous medium) so that a Darcy term appears as additional term in the right hand side of the momentum equation in the case of the porous medium zone. Therefore the equations can be written in a unified form as:

$$\nabla \cdot \mathbf{V} = 0$$

$$\frac{\partial(\rho \mathbf{V})}{\partial t} + \nabla \cdot (\rho \mathbf{V} \otimes \mathbf{V}) = -\nabla p + \mu \Delta \mathbf{V} - \rho \beta (T - T_{ref}) \mathbf{g} - (1 - X) \mu \mathbf{K}^{-1} \mathbf{V}$$

$$\rho c_p \left(\frac{\partial T}{\partial t} + (\mathbf{V} \cdot \nabla) T \right) = \nabla \cdot \left[(X \ k + (1 - X) \ k_p) \ \nabla T \right]$$

In the above equations \mathbf{V} is the velocity vector, p is the nonhydrostatic pressure, T is the temperature, t is time and \mathbf{g} is the acceleration of gravity.

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On all solid boundaries (i.e. the cylinder walls and the heat exchanger solid parts), a no-slip condition is imposed, and the temperature is prescribed as detailed in the previous section.

2.2.3. Numerical method

- Computations are performed with the in-house code SUNFLUIDH, which has been developed at LIMSI for simulations of unsteady incompressible flows. The previous governing equations are solved in the entire domain using a finite volume approach with a second order discretization in space and time. An implicit treatment of the viscous and thermal conductive terms ensures better numerical stability with regard to the time step which only depends on the
- ²⁵⁵ CFL criterion. The equation set is solved by means of an ADI method [22]. An incremental projection method is used in order to ensure the divergence-free velocity field ([23],[24]). This implies to solve a Poisson's equation at each time step which is carried out with a multigrid-SOR algorithm [25]. The solution corresponds to the time-variation of pressure from which the correction term is
- estimated in order to get the divergence-free velocity field. The mesh is bodyfitted regular.

The numerical domain is meshed using 64 points regularly spaced along the

radial direction, 64 points regularly spaced along the azimutal direction, and 512 points placed regularly along the axis. The mesh size in the axial direction

is $\Delta x = 1.4 \, mm$. In the radial direction, $\Delta r = 0.61 \, mm$. It was checked through a mesh-refinement study that this spatial resolution is adequate for the given configuration. The time step is adjusted throughout the simulation in order to satisfy a CFL< 0.5 criterion.

2.3. Results and discussion

- Figure 3 shows the experimental and numerical velocity vector maps and colored contours of the axial velocity component for the central vertical plane at the right side of the porous medium, which corresponds to the measurement field of view (close-up views for the figures near the porous medium (i.e. x = 0) are also shown in Figure 3). Figure 4 shows the numerical temperature field over the same region. The vortex flow observed is indeed that of natural convection of air in a cylindrical fluid cavity, triggered by a horizontal temperature gradient (the temperature of the right side of the porous medium is still much higher than the ambient temperature, as shown on Figure 4). The numerical temperature at the center of the right end section of the porous medium is found
- to be equal to 320 K, in good agreement with the measured value of 328 K (see Figure 1b). Experimental and numerical results agree remarkably well (Figure 3), considering the numerous simplifications and approximations made in the numerical model. It should be pointed out that the numerical calculation converges to a steady solution, in agreement with experimental results (in which
- the temperature and thus velocity fields only change very slowly in time). The main difference lies in that for $x > 150 \, mm$ a small flow remains observable along the whole experimental field of view, while in the numerical simulation it becomes negligible. This could be due to the fact that the temperature imposed on the tube boundary is based on the measurement of the outside temperature
- ²⁹⁰ and not on the inside, which should be slightly higher, therefore extending the natural convection flow. Also the presence of the openings on the tube ends (open plugs) is not modeled (a closed end with no slip condition is imposed in

the numerical domain). In addition, the maximum amplitude and the extent of the convection flow in the field of view are highly dependent on the value of

- the driving ΔT imposed through prescribed boundary temperature values. The temperature on the glass tube is not controlled and the ambient temperature varied slightly during the experiment (about 2 degrees). The effect of changing ΔT by $\pm 2K$ (i.e. representing 12% of $\Delta T = 17K$ for the experimental field of view) could also explain the observed discrepancy between the measurements
- and the numerical results : A rough model gives the max velocity amplitude as a linear function of ΔT . The corresponding variation of the extent of the convection cell is harder to estimate. Figure 5 shows the axial profile of the vertical velocity component obtained from experiments and numerical simulations at the central vertical plane, again on the right side of the porous medium, for several
- values of the radial coordinate r (which on this plane measures the height). Here again the agreement between experimental and numerical results is very good, except for the limit $x \to 0$ (end of the porous medium) where the local geometry changes are not accounted for in the model (the porous medium being considered homogeneous). Also, the porous medium being very anisotropic, the model
- used for the hot exchanger (and particularly its solid-fluid geometry shown on Figure 2a) influences the velocity near x = 0. As expected, the velocity profiles are not symmetric with respect to the x-axis, and show the development of the convection boundary layer along the "hotter" section x = 0, in the bottom half between r = -15 mm until r = 0. The maximum velocity then decreases
- because when the flow reaches the top tube wall it is forced to turn. Figure 6 shows the axial profiles of the axial velocity component obtained from experiments and numerical simulations in the same locations as Figure 5. Here again the agreement between experimental and numerical results is very good, except for the limit $x \to 0$ (end of the porous medium). As expected, the velocity is
- negative for the lower part of the tube, and positive for the upper part, forced by the upward flow along the hotter porous medium end x = 0. Figure 7 shows the vertical profile of the axial velocity component obtained from experiments and numerical simulations on the central vertical plane, on the right side of the

porous medium, for several values of the axial position. The agreement between experiments and numerical simulations is good, but the maximum values are about 20% off. Also, as noted on Figure 3, for $x > 150 \, mm$, there is a small discrepancy between numerical and experimental results.

Figures 8a and 8b show velocity vector maps and colored contours of the axial velocity component obtained from numerical simulations and experimental data from [15] on the central horizontal plane, on the right side of the porous medium. There is again excellent agreement between experiments and numerical simulations. Convective velocities are of course a lot smaller on that plane than on the central vertical plane. Figure 8c shows the numerical and experimental transverse profile (as a function of the radial coordinate) of the axial velocity component on the central horizontal plane at x=60 mm. On this plane the flow is symmetric with respect to the x-axis.

In order to better understand the convective flow observed in the measurement field of view, contours of the axial velocity component and temperature in the central vertical plane obtained from numerical simulations are shown within

the porous medium on Figure 9a and 9b, and left of the hot heat exchanger on Figure 9c and 9d. The flow inside the porous medium is indeed characteristic of natural convection flow in a cavity filled with a strongly anisotropic porous medium (Figure 9a). The flow is constrained to remain in the horizontal plane, and the permeability being very small, conduction dominates convection (with

³⁴⁵ mostly horizontal stratification of temperature), and the flow is very slow. Also, because of the porous medium's anisotropy, the model used for the hot heat exchanger influences the flow in the right fluid cavity, i.e. in the measurement field of view: For example the no-slip condition on the solid core and rings and the zero permeability in the radial and azimutal directions put high constraints

on the development of the flow in the porous medium. The flow thus retains the geometry of the hot heat exchanger (Figure 9a). In the left fluid cavity the convection vortex turns in the opposite direction, because the cooler boundary is on the left (Figure 9c).

In order to get an insight in driving effects in the thermoacoustic cavity, the

- maximum velocity in different regions is examined thereafter in light of classically defined reference Rayleigh numbers and associated velocity scales. On the right side of the hot heat exchanger, the flow is driven by the temperature difference $\Delta T = T_{hot} - T_{cold}$. The flow in this region should then be that of a differentially heated cavity partly filled with an anisotropic porous medium. Using
- the axial permeability K_{xx} and equivalent thermal conductivity k_p , the porous medium Rayleigh number is $Ra_p = \frac{\rho g \beta \Delta T H K_{xx}}{\mu \alpha_p}$, with $\alpha_p = \frac{k_p}{\rho c_p}$ the porous medium equivalent thermal diffusivity, and H a reference height [18]. Using all geometrical and thermophysical parameters presented previously (Table 1), and taking the reference height H = R, this porous Rayleigh number is $Ra_p = 1.1$.
- The associated velocity scale is $V_{refp} = \frac{\alpha_p}{H} Ra_p = 0.02 \, m/s$ [18]. The maximum velocity in the region on the right of the hot heat exchanger is about $0.04 \, m/s$, which is indeed on the order of this velocity scale. The characteristics of the porous medium therefore determine the strength of the convection flow.
- On the left of the hot heat exchanger, the flow is driven by the temperature difference between the left end of the cylindrical tube and the heat exchanger (imposed based on the experiments and equal to about $\Delta T_l = 110K$). The flow in this region should then be that of a differentially heated fluid cavity. The reference fluid Rayleigh number is classically given as $Ra = \frac{\rho g \beta \Delta T_1 H^3}{\mu \alpha}$, with $\alpha = \frac{k}{\rho c_p}$ the fluid thermal diffusivity, and H a reference height [17]. Using the same reference height H = R, this fluid Rayleigh number is $Ra = 3.36 \times 10^5$. The associated velocity scale is $V_{ref} = \frac{\alpha}{H} Ra^{1/2} = 0.38 m/s$ [17]. The maximum velocity in the region on the left of the hot heat exchanger is about 0.15 m/s(Figure 9c), which is indeed on the order of this velocity scale. The strength of the convection flow in this region will then be determined by the effectiveness of the isolation of this "hot" part of the tube.

When this simple thermoacoustic engine is functioning (with plugs in place), acoustic velocities of about 2 m/s and streaming velocities of about of 1 cm/shave been observed for the same applied electrical power [15]. Therefore the present results confirm that natural convection is significant and that this phenomenon is important in understanding mean velocity measurements in such a

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device. This phenomenon, as acoustic streaming and jet streaming, is a source of heat flux that should be taken into account for a realistic thermal balance in such a device. Moreover, the above presented results show that a simple model as the one proposed here gives realistic results, meaning that a thermoacoustic

- ³⁹⁰ core is satisfactorily described as a homogeneous porous medium in terms of natural convection effects. Finally, it was found that the use of Rayleigh numbers give a correct order of magnitude for the convective velocity, that can be used for a preliminary estimate. In the following section we consider a configuration slightly more complicated and more representative of an optimized ³⁹⁵ system because an ambient heat exchanger is added. Our aims here are the
- same as above, i.e. investigate the natural convection flows in such a system both experimentally and numerically.

3. Natural convection flow in a cavity with ambient heat exchanger

3.1. Experimental setup, measurement systems and procedure

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In this second experimental setup, many factors were taken into considerations in the design process to overcome difficulties encountered in the 1st configuration. First, the resonator duct is chosen to have a square cross-sectional area to facilitate the PIV measurements in the vertical plane (x - z plane in Figure 10a) at different transverse locations (y-direction). Second, an Ambient

- ⁴⁰⁵ Heat Exchanger (AHX) is added on the right side of the regenerator to keep its temperature constant. At the left side of the regenerator ends is placed an electric resistance as in the 1st configuration. Third, a thermal insulation is used to cover the hot part of the resonator and hence to reduce the heat loss through the walls of the resonator tube. As shown in Figure 10a, the setup
- consists of a square duct with inner side length of 44 mm and the total length of the duct is 2655 mm. The left part of the duct is made of aluminum whereas the right part of the duct is made of acrylic to grant an optical access for the laser measurements. Two loudspeakers (Model: PHL B20/2410) are attached to the ends of the duct. As before, in order to isolate the natural convection

- ⁴¹⁵ flow, no acoustic wave was generated in the resonator, that is the loudspeakers were turned off. The thermoacoustic core consists of a regenerator placed between the Hot Heat Exchanger (HHX) and the AHX. The coordinate system is also defined in Figure 10a, with x = 0 corresponding to the right end of the AHX. As shown in Figure 10b, the regenerator is made of stainless steel wire
- ⁴²⁰ meshes stacked in a steel canister with a total length of 40mm. The volumetric porosity (i.e. the ratio of the gas volume to the total volume) of the regenerator is 80%. The HHX is made of an insulated electric heater wire with total length of 450mm and an outer diameter of 5mm. The electrical wire is formed as shown in Figure 10c, yielding a porosity of the hot heat exchanger of 43% and a
- length in the axial direction (i.e. x-axis) of 10mm. As shown in Figure 10d, the AHX is made of three parts. The central part, which is responsible for the heat exchange between the gas and the water, is printed (using 3D printing technology) from steel powder. The other two parts (white in Figure 10d) are printed from plastic to avoid the heat transfer through the walls. The three parts are
- ⁴³⁰ glued together and assembled with the resonator duct. The central part of the AHX is made of fins with thickness of 1mm and plate spacing of 1mm. Also, there are two water paths where the water flow direction in one of them is in the opposite direction to the other to achieve a temperature uniformity over the cross-section of the AHX. The inner and outer diameters of the water tubes are 3mm and 5mm, respectively. The total length of the AHX in the axial direction

(i.e. x-axis) is 20mm and its porosity is 40.5%.

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The same PIV system as for the first setup was used and a similar experimental procedure was followed. Here the input electrical power was $30 W \pm 1\%$ and the temperatures of the walls of the aluminum duct are measured (see Figure 10e). Thermocouples are placed beneath the thermal insulation and in

- contact with the walls of the duct to accurately measure the wall temperatures. It was checked that thanks to the AHX, the temperature of the right part of the resonator duct (i.e. acrylic duct) remains at the ambient temperature therefore, no temperature measurements were conducted on the walls of the acrylic
- 445 duct. The PIV measurements performed in this system focus on measuring the

natural convection flow at the end of the AHX in the vertical plane (i.e. x - zplane) and at 7 different transverse locations (i.e. $y = 0, \pm 5mm, \pm 15mm$ and $\pm 19mm$).

The uncertainty in the temperature measurements is ± 1 % of the reported mean temperatures. The value of the spatial-average uncertainty in the velocity measurements is reduced to ± 6 % (compared to ± 13 % in the first experimental setup in which a circular duct is used) because the laser light reflections are less when the duct walls are flat (i.e. square duct).

3.2. Numerical model

As previously, a simplified 3D configuration is introduced in order to model the experimental configuration (Figure 11). The horizontal duct has a square cross-section (with side length equal to the inner side length of the experiment l = 44 mm).

The regenerator is modelled as a homogeneous parallelepipedic isotropic ⁴⁶⁰ porous medium block of length $L_p = 40 \, mm$ and cross-section width 38 mm, inserted in a steel case (as in the experiment). Its thermophysical characteristics are its porosity $\epsilon = 0.8$, its permeability $K_{xx} = K_{yy} = K_{zz} = K =$ $10^{-8} m^2$ (based on experimental work performed on similar materials [26]), and its equivalent thermal conductivity $k_p = 3.16 W.m^{-1}.K^{-1}$ (calculated as $k_p = \epsilon k_{fluid} + (1 - \epsilon) k_{solid}$).

The hot heat exchanger (electric wire) is modelled as 6 vertical solid plates of axial width $e_h = 10 \, mm$ (as in the experiment) and transverse width equal to $4 \, mm$, maintained at given hot temperature $T_{hot} = 438 \, K$.

The ambient heat exchanger, placed on the right side of the porous medium, ⁴⁷⁰ is modelled as 6 horizontal solid plates of axial width $e_c = 20 \, mm$ (as in the experiment) and transverse width equal to $4 \, mm$ maintained at given cold (water) temperature $T_{cold} = 291 \, K$. In between the solid plates, the vertical fins are modelled as a homogeneous anisotropic porous medium (i.e. stack of thin plates). The characteristics of that porous medium are its porosity ⁴⁷⁵ $\epsilon = 0.4$ (as in the experiment), its permeability assumed anisotropic $K_{xx} =$ $K_{zz} = d_1^3/(12d_1 + d_2) = 10^{-8}m^2$ (where d_1 is the plate's insterspace and d_2 the plate's width, based on [18]), $K_{yy} \approx 0$, and its thermal conductivity $k_p = 27.4 W.m^{-1}.K^{-1}$ (calculated from the porosity and thermal conductivities of gas and plates).

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On the left of the HHX, in order to model the thermal insulation, the duct walls are adiabatic. Therefore the steady temperature in that region should be homogeneously equal to the hot temperature T_{hot} , and the natural convection flow should not extend very far. For that reason and in order to lower computational costs, the length of the duct left of the HHX is reduced to $L_l = 160 \text{ mm}$. Since the thermal insulation also covers part of the regenerator, the duct walls are adiabatic along the insulation (with axial extension identical to that used in the experiment). The temperature of the remainder of the duct wall along the regenerator is prescribed equal to $T_{amb} = 294 \text{ K}$. The ambient tem-

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The temperature difference $T_{amb} - T_{cold} = 3 K$ being quite small, the natural convection flow should not extend very far. For that reason and in order to lower computational costs, the length of the duct right of the AHX is reduced so that the total computational length is smaller than that of the experiment and equal to L = 430 mm. The reference ambient temperature T_{amb} is used to calculate the thermophysical parameters of the fluid.

perature T_{amb} is prescribed along the duct walls on the right side of the AHX.

The numerical domain is meshed using 64 points regularly spaced along the cross sectional sides in the y and z directions. The mesh size in the axial direction is $\Delta x = 1.6 \times 10^{-3} m$. This spatial resolution is adequate for the given problem configurations. The time step is adjusted throughout the simulation in order to satisfy a CFL< 0.5 criterion.

3.3. Results and discussion

As for the previous configuration both simulation and experiments reach a steady state. Figures 12 to 14 show the velocity vector map overlapped on the color map of the axial velocity component of the natural convection flow ⁵⁰⁵ obtained from experiments and numerical simulations at the exit of the AHX on vertical plane for 3 different transverse locations y = -19mm (Figure 12), y = -5mm (Figure 13), and y = 0 (center plane, Figure 14). Experimental and numerical results agree remarkably well, both qualitatively and quantitatively, considering the numerous simplifications and approximations made in

- the numerical model. As in the case of the first experiment -without AHX-, the natural convection vortices extend for a longer axial distance in the experiments than in numerical calculation. Again, this could be due to the fact that the temperatures imposed on the tube boundary are based on the measurement of the outside temperature instead of the inside. The convection vortex is in the op-
- ⁵¹⁵ posite direction than in the configuration without ambient heat exchanger, and the maximum axial velocity component is about half. The direction of the flow comes from the fact that the ambient heat exchanger is very effective, so that the tubes containing the cold water are cooler than the ambient temperature on the right fluid cavity. Therefore the fluid tends to move downward in the vicin-
- ity of the AHX and then is forced to turn right at the bottom of the duct. The order of magnitude of the velocity can be compared to the natural convection reference velocity in a fluid cavity calculated using $\Delta T_r = T_{amb} - T_{cold} = 3 K$ and a reference height H = 44 mm. The calculation gives the Rayleigh number $Ra = 1.63 \times 10^4$ and $V_{ref} = 0.07 \times 10^{-3} m/s$. The maximum velocity in that
- region is about 0.025 m/s (Figures 12, 13, 14), which is indeed on the order of this velocity scale. In order to better understand the convection flow, contours of the calculated axial velocity component and temperature in the central vertical plane around the regenerator (the measurement field of view does not extend left of x = 0) are shown on Figure 15. Analysis of this figure and of
- Figure 12 shows that in this experiment the AHX prevents the development of a strong natural convection flow on the right part of the duct. Therefore the duct is clearly separated in two parts, left of the AHX and right of the AHX.

Since the regenerator is placed between the heat exchangers, the flow is similar to the natural convection flow in a porous differentially heated cavity (Figure 15). However the regenerator's permeability being very small, so are velocities (on the order of 0.002 m/s) and isothermal lines are almost vertical, i.e. the regenerator acts like a conducting solid. The order of magnitude of the velocity can be compared to the porous natural convection reference calculated using $\Delta T = T_{hot} - T_{cold} = 147 K$, H = 44 mm. The calculation gives the porous Rayleigh number $Ra_p = 1.26 \times 10^{-1}$ and $V_{refp} = 2.2 \times 10^{-3} m/s$. The maximum velocity in the regenerator is about 0.002 m/s (Figure 15), which is indeed on the order of this velocity scale. Both the ambient heat exchanger and the isolation of the hot duct contribute to the concentration of temperature gradients in the regenerator only. The convection flow inside the regenerator depends then mostly on its permeability.

On the left of the HHX the flow is clearly driven by the flow between the mesh wires of the regenerator (Figure 15). The temperature in that region is almost homogeneously hot.

In sum, the simple model proposed here predicts the natural convection flow inside the entire device, with good agreement with measurements in the field of view.

4. Conclusion

Natural convection flows were analyzed both experimentally and numerically for two different horizontal thermoacoustic cavities, when no acoustic oscillations were present. The first cavity consisted of a cylindrical resonator filled with air and containing a thermoacoustic core made of a ceramic stack placed next to a wire resistance (hot heat exchanger). The second cavity consisted of a duct with square cross-section filled with air and containing a thermoacoustic core made of a regenerator placed between a wire resistance (hot heat exchanger) and an ambient heat exchanger (using a water stream for the heat exchange). Temperature was measured by thermocouples in several points along the cavities, and velocity fields were obtained from PIV measurements in several vertical planes (only the central vertical plane in the first experiment). The numerical model consisted in solving Navier-Stokes equations under Boussinesq

 $_{\tt 565}$ $\,$ assumptions inside a simplified cavity based on each experimental setup. In the

first experiment, the cylindrical cavity was of similar geometry and dimensions as the experiment, the hot heat exchanger was modeled as several immersed solid bodies at given temperature, and the ceramic stack was modelled as a homogeneous anisotropic porous medium. The temperature along the cylindrical

tube was prescribed as a boundary condition based on the experimental measurements. In the second experiment, the cavity was also modeled based on experiments, the regenerator being modeled as a homogeneous isotropic porous medium and the ambient heat exchanger as an immersed solid body at given temperature inside a homogeneous anisotropic porous medium. The temperature boundary conditions were also based on experimental measurements.

It was shown that the flow and temperature distributions are fully threedimensional. They depend on the thermophysical properties of the working gas and of the porous media constituting the thermoacoustic stack or regenerator and heat exchangers, as well as on the geometrical characteristics of the

device and the temperature conditions. There was excellent qualitative and quantitative agreement on the velocity fields between experimental and numerical simulation results for both configurations. Also the velocity scales observed in the different regions of the thermoacoustic cavities were in good agreement with classical scales for natural convection flows within a porous or fluid cavity.

- It should therefore be possible to predict the strength and patterns of natural convection flows inside functioning thermoacoustic devices using an approach similar to the one proposed here. It was noted that the observed natural convection flows could be quite significant in such devices and potentially interfere with thermoacoustic effects. We hope the fairly simple models used here will be fur-
- ⁵⁹⁰ ther used by others to assess potential natural convection effects and contribute to optimal design of thermoacoustic devices. However, possible interaction and coupling between thermoacoustic and natural convection effects was not studied here and is the topic of ongoing work.

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Figure 1: (a): Schematic for the thermoacoustic resonator and image of the thermoacoustic core. (b): Thermocouples locations and results of measurements (in K) in the 1st configuration.

R	L	L_L	e_h	L_p	T_{hot}	T_{cold}
mm	mm	mm	mm	mm	K	K
39	738	129	5.8	60	520	293

ρ	μ	k	c_p	ϵ	K_{xx}	k_p					
$kg.m^{-3}$	$kg.m^{-1}s^{-1}$	$W.m^{-1}.K^{-1}$	$J.kg^{-1}.K^{-1}$		m^2	$W.m^{-1}.K^{-1}$					
1.07	$1.9\cdot 10^{-5}$	$2.8\cdot 10^{-2}$	1004	0.64	8.10^{-8}	$9.18.10^{-1}$					
(b)											

Table 1: (a): geometrical and thermal parameters, (b): Thermophysical parameters for air and porous medium, 1^{st} configuration.



Figure 2: (a): Numerical configuration for the 1^{st} configuration, (b): temperature prescribed in the numerical model along the tube wall, as a function of axial position (solid line), and measurements on top/bottom of the outside tube wall (red squares) reported from Figure 1b.





Figure 3: Velocity vector maps and colored contours of the axial velocity component obtained from experiments (a) and numerical simulations (b) on the central vertical plane, on the right side of the porous medium. Zooms on the left part of the figures, for experimental results (c) and numerical simulations (d).



Figure 4: Calculated temperature map on the central vertical plane, on the right side of the porous medium.



Figure 5: Axial profile of the vertical velocity component on the right of the porous medium (squares: experiments, solid line : numerical simulation) on the central vertical plane at (a): r = -15mm, (b): r = -10mm, (c): r = -5mm, (d): r = 0, (e): r = 5mm, (f): r = 10mm, (g): r = 15mm.



Figure 6: Axial profile of the axial velocity component on the right of the porous medium (squares: experiments, solid line: numerical simulation) on the central vertical plane at (a): r = -15mm, (b): r = -10mm, (c): r = -5mm, (d): r = 0, (e): r = 5mm, (f): r = 10mm, (g): r = 15mm.



Figure 7: Vertical profile of the axial velocity component on the right of the porous medium (squares: experiments, solid line: numerical simulation) on the central vertical plane at (a): x = 0mm, (b): x = 10mm, (c): x = 40mm, (d): x = 70mm, (e): x = 100mm, (f): x = 130mm, (g): x = 150mm (h): x = 180mm.







Figure 8: Velocity vector maps and colored contours of the axial velocity component (a): experiments, (b): numerical simulations on the central horizontal plane, on the right side of the porous medium. (c): Distribution of the axial velocity component as a function of the radial coordinate (squares: experiments, solid line : numerical simulation) on the central horizontal plane at x = 60mm.



Figure 9: Contour of the axial velocity component (a) and temperature (b) in the central vertical plane in the porous medium region. Contour of the axial velocity component (c) and temperature (d) in the central vertical plane in the cavity left of the hot heat exchanger.



Figure 10: (a): Schematic for the 2^{nd} experimental setup. Photos for (b): the regenerator, (c): the hot heat exchanger, (d): the ambient heat exchanger. (e): Thermocouples locations and results of measurements.



Figure 11: Numerical configuration for the 2^{nd} configuration.



Figure 12: Velocity vector map overlapped on the color map of the axial velocity component at the exit of the AHX on vertical plane at y = -19mm (top: experiments, bottom: numerical simulations).



Figure 13: Velocity vector map overlapped on the color map of the axial velocity component at the exit of the AHX on vertical plane at y = -5mm (top: experiments, bottom: numerical simulations).



Figure 14: Velocity vector map overlapped on the color map of the axial velocity component at the exit of the AHX on vertical plane at y = -0 (top: experiments, bottom: numerical simulations).



Figure 15: Contours of the axial velocity component (top) and temperature (bottom) in the vertical central plane (numerical simulation results).