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Judd-Ofelt analysis and crystal field calculations of Er³⁺ ions in new oxyfluorogermanotellurite glasses and glass-ceramics

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ABSTRACT

New 30 GeO₂-30 TeO₂-15 ZnO-10 Na₂CO₃-10 CaF₂-3 La₂O₃-x ErF₃ (x=2, 4) glasses have been synthesized and submitted to varied heat treatments to provoke nanocrystallization in their matrix. The Er³⁺-doped materials containing typically 50 Å-sized nanocrystallites have been characterized by DSC, ultrasonicometry, XRD, HRTEM, EDS, SAED, optical spectroscopy and VSM techniques. A Judd-Ofelt analysis could be performed from the absorption spectra and led to refined intensity parameters. The local structural changes around Er³⁺ cations were mostly evidenced by important modifications of the hypersensitive optical absorption bands (⁴I_{15/2}→²H_{11/2}, ⁴I_{15/2}→⁴G_{11/2}) and lesser modifications of the emission cross sections and experimental lifetimes. Besides, cycling around the crystallization temperature with a VSM showed some kind of “crossover” between the Curie-Weiss behavior of the Er³⁺ cations dissolved in the glass and those dissolved in the nanocrystallites, with a striking change of magnetic interactions sign from anti- to ferromagnetic. The crystal field Hamiltonian could be refined in C₂ symmetry, thanks to the emission and excitation spectra recorded at 80 K, and the crystal field strength calculated.

1. Introduction

The development of new optical materials easy to synthesize, inexpensive and with remarkable physicochemical and optical properties continues to evolve. Among the great diversity of materials families that exist, the rare-earth-doped oxyfluorinated nanostructured glass-ceramics meet all of the above criteria [1-5]. Tellurite-based glasses are known for their low melting point, infrared transparency and good thermal and mechanical stability [6]. The addition of GeO₂ in tellurite glasses increases chemical durability, UV-visible transmission and improves the thermal stability while decreasing the refractive index of the glass [7-9]. Er³⁺ ion-doped transparent glass-ceramics have been given special attention because of their outstanding optical properties which can be tuned according to the application foreseen, such as solid lasers, planar waveguide amplifiers for dense wavelength division multiplexing (DWDM), and optical gratings [10-18]. Indeed, Er³⁺ is one of the most efficient ions to obtain infrared emission in the 1.53-1.6 μm “eye safe” spectral range, which is very important for the manufacture of lasers for telemetry [19-21].

In this work, Er³⁺-doped oxyfluorogermanotellurate matrix were synthesized to try to obtain a material with both optical properties close to those of fluorinated single crystals and physico-chemical properties and transparency of the precursor glasses. The intensity parameters ($\Omega_{2,4,6}$) and the spectroscopic parameters (β , τ_{rad} , A_{DE} , A_{DM}) related to the laser performance were evaluated from the experimental data by the normalized Judd-Ofelt method. Crystal field strength around Er³⁺ cations and its impact on 4f⁶ electrons energy level diagram were obtained by means of a parameterized Hamiltonian refined with emission and excitation spectra recorded at 80 K. The Er³⁺-doped oxyfluorogermanotellurite glasses have been synthesized and submitted to thermal annealing in order to induce the nucleation of nanocrystals, possibly of CaF₂ and doped with Er³⁺ ions. The materials were characterized by differential scanning calorimetry (DSC), ultrasonicometry, X-ray diffraction (XRD), high-resolution transmission electron microscopy (HRTEM), energy dispersive spectroscopy (EDS), selected area electron diffraction (SAED), electron probe microanalysis/wavelength dispersion spectroscopy (EPMA/WDS), optical spectroscopy and vibrating sample method magnetometry (VSM).

2. Experimental

The samples were prepared with the following composition (in mol%): 30 GeO₂-30 TeO₂-15 ZnO-10 Na₂CO₃-10 CaF₂-3 La₂O₃-x ErF₃ (with x=2 or x=4). The glasses were elaborated by conventional melting, the starting powders being weighed in the desired amounts according to the selected compositions with an accuracy of ± 1 mg. After grinding, the powders were placed in a covered platinum crucible and melted for 1 h at 1323 K. The melts were then rapidly quenched into a preheated stainless steel thin plate at T_g-20 K to avoid thermal shock. The glass was subsequently heat-treated at T_g-20 K, in order to relax the mechanical stresses arising from the quenching. Finally, the glasses were polished for structural, optical and spectroscopic measurements. As suggested by DSC measurements (Fig. 1), the as-prepared oxyfluoride glasses were heat-treated at 728 K (2 h) to obtain transparent glassy ceramics. The Er contents were determined by EDS and EPMA/WDS. In the remainder of this paper, we shall use an average concentration of 5.288× and 10.349× 10²⁰ Er³⁺ cm⁻³ for the 2%- and 4%-doped oxyfluoride samples, respectively. The composition of the glasses (Na, Ca, Zn, Ge, Te, La, O, F) was determined by EPMA/WDS, in order to allow for the energy resolution of the Ca-K_α (3.691 keV) and Te-L_α lines (3.769 keV), and of F-K_α (0.677 keV) and La-M lines (0.833 keV, even if for La we used the L line at 4.651 keV). The main differences observed between the initial and the final compositions (see Table 1 of the supplementary information file, hereafter called SI) are likely to be due to losses by sublimation and volatilization of TeO₂ during the melting stage of the precursor glass (the vapour pressure of TeO₂ is higher than 0.3 atm at temperatures higher than 905 K [22-23]). The differences between initial and final F contents are likely to be due to the oxidation of ErF₃ and CaF₂ in air at high temperature.

The differential thermal analysis of the glasses were performed by means of a differential thermal analyzer DTA Model SDT Q600 TA instrument, with a heating rate of 10 K/min. The samples were heated in alumina crucibles from room temperature to 1400 K under N₂ atmosphere with a 100 ml/min flow. The X-ray diffraction was carried out in a powder diffractometer (PANalytical X'pert Pro) in the 2θ range 10-80° with Cu K_α radiation (λ=1.54056 Å) generated at 40 kV and 30 mA. The transmission spectra were recorded by means of a UV-Vis-NIR VARIAN Cary 5000 spectrophotometer in the 400-2000 nm spectral range. The IR absorption spectra were measured with a BRUKER Equinox 55 spectrophotometer. Density measurements were performed by ultrapycnometry using a Helium QUANTACHROME Ultrapyc 1200e Pycnometer. We found the density by averaging over sixty measurements. We performed three

measurement runs for each sample. Each measurement run gave us twenty values, taking three minutes to measure each value. The density of the 2 and 4 mol % Er³⁺-doped glasses is 4.652 and 4.808 g/cm³, respectively.

We used a high-resolution transmission electron microscope (HRTEM, JEM-2200FS) equipped with energy dispersive spectrometer (EDS) system to try to analyze the microstructure and the elements' distribution of heat-treated glasses, but the samples proved to be unstable under the beam both onto a standard or a cryogenic (105 K) sample holder.

The magnetic susceptibility was measured in field heated and cooled modes (10 K/mn) using an EZ-7 MICROSENSE Vibrating Sample Magnetometer operated in the 295-923 K temperature range under an applied magnetic field of 1 T. Two glass samples of mass 50 mg and 11.7 mg were cemented on a quartz rod, the diamagnetic contribution of which was also measured and subtracted from our data. When arrived at the highest temperature selected for each sample, a 15 minutes stage was imposed to the sample and then, the measurement in cooling mode was started. The visible (550 nm) and near IR (950-1700 nm) fluorescence spectra were measured with a Horiba Jobin Yvon Fluorolog spectrometer at 80, 120, 200 K and room temperature in ambient atmosphere, under Xe lamp illumination. Selected decay times were recorded at 80, 120, 200 K and room temperature in the visible and NIR spectral range by exciting the sample at 380 nm for the ⁴S_{3/2}→⁴I_{15/2} Er³⁺ transition and at 650 nm for the ⁴I_{13/2}→⁴I_{15/2}, ⁴I_{11/2}→⁴I_{15/2} Er³⁺ transitions. An estimate of the linear refractive index was performed by extraction from the experimental data of optical transmission in the spectral range of constant optical transparency of the samples, ~1900-2000 nm. We used the Fresnel's expression relating optical transmission coefficient and linear refractive index (T=2n/(n²+1)). The linear refractive index obtained is 1.87 and this value, which will be used in the remainder of this paper, is generally in good agreement with the literature for germano-tellurite glass [24-25].

3. Results and discussion

3.1 Thermal stability of G-GTOF glasses

The DSC thermogram recorded on the 30 GeO₂-30 TeO₂-15 ZnO-10 Na₂CO₃-10 CaF₂-3 La₂O₃-2 ErF₃ base glass is shown in Figure 1. The characteristic temperatures were determined to be: transition temperature T_g=686 K, starting point of crystallization temperature T_x=732 K, crystallization temperature T_c=745 K and ΔT=T_x-T_g=47 K, the latter being the thermal stability criterion against crystallization.

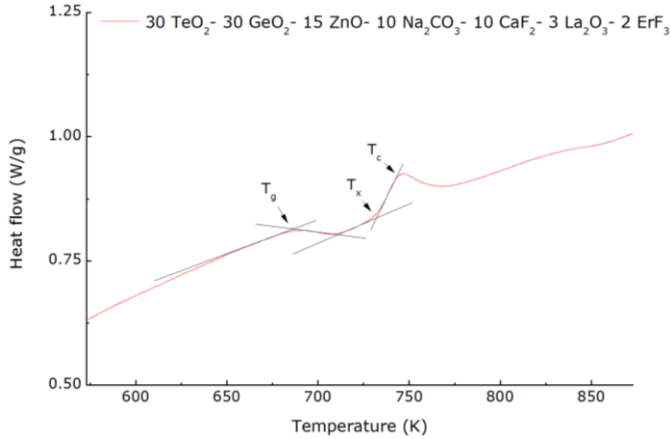


Figure 1. DSC curve of the 30 GeO₂-30 TeO₂-15 ZnO-10 Na₂CO₃-10 CaF₂-3 La₂O₃-2 ErF₃ glass samples prepared in this study.

The characteristic temperatures of the 30 GeO₂-30 TeO₂-15 ZnO-10 Na₂CO₃-10 CaF₂-3 La₂O₃-2 ErF₃ glass are similar to what we had in the same composition doped 2% Yb³⁺ [26], and to what has been published in similar studies [27-28]. The exothermic phenomenon from 745 K is due to the crystallization of the CaF₂ phase. As mentioned before, based on the results of the thermal analysis we treated the precursor glasses for 2 hours at 728 K to obtain transparent glassy ceramics.

3.2 X-ray diffraction (XRD) on thermally treated glasses

The heat treatment at 728 K causes the partial crystallization of the precursor glasses (see in Figure 2). The peaks of crystallization obtained in the “2 ErF₃”-doped glass comes from the crystallization of the CaF₂ cubic phase Fm-3m [29]. In Figure 2, we mention the (hkl) indices corresponding to the Fm-3m cubic phase of CaF₂. The relative intensity of the (220) diffraction peak is much lower, as compared to that of the (111), than in the pure CaF₂ crystallized phase. Provided that preferential orientation effects can be discarded to account for this, by measuring the samples in powder form, the change in diffraction peak relative intensities might be ascribed to partial substitution of Ca²⁺ cations for RE³⁺ ones. The size of the crystallites calculated by the Scherrer relation $L = \lambda / (\beta \times \cos(\theta))$ (with L the size of the crystallites in nm, $\lambda = 1.54056 \text{ \AA}$, β the integral width of the diffraction peak in radians and θ the Bragg angle (°)) [30], is on the order of 5 nm, in the “2 ErF₃”-doped sample. Other unidentified diffraction peaks appear on the diffractogram of the “4 ErF₃”-doped glass. This might mean that the crystallization

temperature of the “pure” CaF₂ phase was exceeded, because it is well known that its nucleation temperature decreases with the F-content in the matrix [31-32].

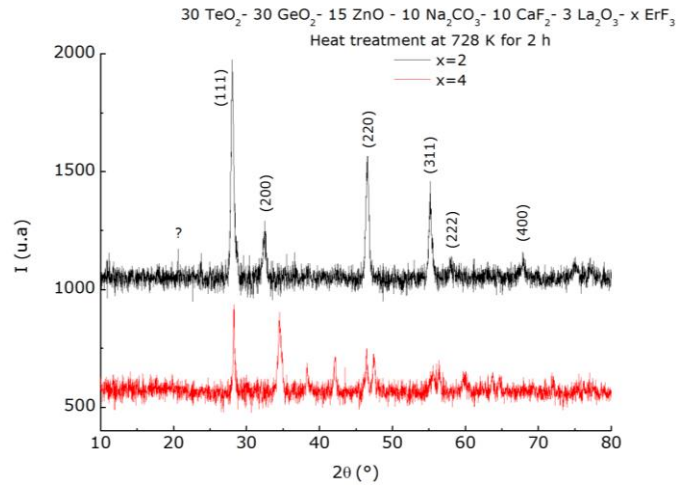


Figure 2. X-ray diffraction patterns of two heat-treated glasses. The indexation mentioned in the black diffractogram corresponds to the Miller indices of the CaF₂ cubic phase Fm-3m.

3.3 High-resolution transmission electron microscopy (HRTEM), selected area electron diffraction (SAED) and EDS analysis of heat-treated Er³⁺-doped glass

The SI file (Fig. 1) gives TEM and HRTEM images together with the SAED pattern of a “2 ErF₃”-doped and heat-treated sample at 728 K for 2 h. The HRTEM contrast analysis of this sample revealed the presence of nanocrystallites, which was confirmed by SAED spots. The EDS quantitative analysis based on the Er element M-line led to an amount of 0.9 to 2 at. % over the five crystallized zones investigated. However, these nanocrystallites could not be studied in details because they evolved under the electron beam. From a chemical point of view, all samples were found to be homogeneous (no Ca “contrast” as the one established, for instance, in [26]) over five mappings.

3.4 Absorption spectroscopy and Judd-Ofelt analysis

Figure 3 shows the absorption cross section of Er³⁺-doped and heat-treated glasses. The absorption bands correspond to transitions between the spin-orbit multiplets ground state ⁴I_{15/2} to the 13 excited states ⁴I_{13/2}, ⁴I_{11/2}, ⁴I_{9/2}, ⁴F_{9/2}, ⁴S_{3/2}, ²H_{11/2}, ⁴F_{7/2},

${}^4F_{5/2}$, ${}^4F_{3/2}$, ${}^2H_{9/2}$, ${}^4G_{11/2}$, ${}^4G_{9/2}$ and ${}^2K_{15/2}$. The absorption peak cross section values are typical of forced electric-dipole and/or magnetic-dipole induced optical transitions and the width of the absorption bands reflects the inhomogeneous broadening of the Er^{3+} ions transitions in the samples [33]. By superimposing the spectra of the four samples ($x=2$ and $x=4$, untreated and heat-treated, see Section 2), it happens that the only absorption bands which exhibit a modification in cross section value (the width and peak positions remaining unchanged) are the ${}^4I_{15/2} \rightarrow {}^2H_{11/2}$ and ${}^4I_{15/2} \rightarrow {}^4G_{11/2}$. This means that both heat-treatment and increase in Er^{3+} -content modify selectively the odd components of the crystal field around Er^{3+} cations in these samples. This variation suggests a modification of the crystal field around Er^{3+} cations.

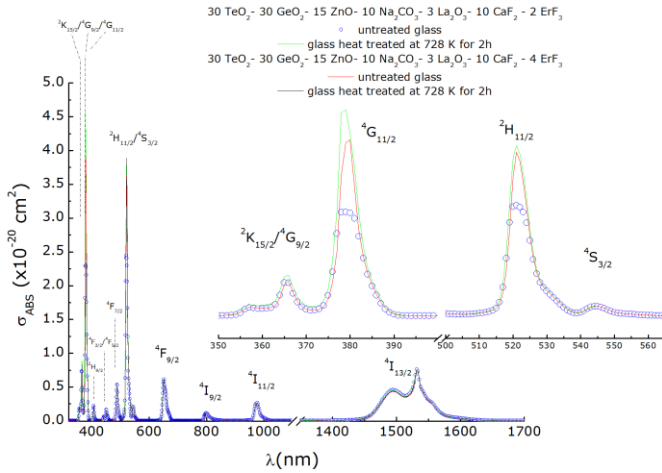


Figure 3. Absorption cross sections of the four glasses and glassy ceramics investigated in this study (see Section 2. Experimental). The insert is a zoom over the two pseudo-quadrupolar hypersensitive transitions of the Er^{3+} $4f^1$ electronic configuration.

The integrated absorption cross section of each transition can be used as input data to perform Judd-Ofelt analysis [34-45], which is necessary to obtain transition probabilities, branching ratios and radiative lifetimes. The latter two are necessary for calibrating the emission spectra in cross section units by the Fuchtbauer-Ladenburg (FL) method. Each of the absorption bands were integrated in order to perform Judd-Ofelt analysis according to both the normalized procedure of Goldner [46-48] and the unnormalized procedure, with and without the thermalized ${}^4K_{15/2}$ - ${}^4G_{9/2}$ - ${}^4G_{11/2}$ levels bands, and in all cases with thermalized ${}^2H_{11/2}$ and ${}^4S_{3/2}$ levels (Table 1). Since the only transitions which have a $U^{(2)} \neq 0$, or a $U^{(2)}$ matrix element 10 to 100 times higher than the $U^{(2)}$ ones of the other transitions, are the “pseudo-quadrupolar” hypersensitive ones

${}^4I_{15/2} \rightarrow {}^2H_{11/2}$ and ${}^4I_{15/2} \rightarrow {}^4G_{11/2}$ ones [47-48], and since the ${}^4I_{15/2} \rightarrow ({}^4K_{15/2}, {}^4G_{9/2}, {}^4G_{11/2})$ absorption band integrated cross sections also turns out to be the only one to almost equal that of the highest experimental integrated cross sections (${}^4I_{15/2} \rightarrow {}^4I_{13/2}$, $\approx 44 \times 10^{-20} \text{ cm}^2 \cdot \text{nm}$), it is clear that including or not the ${}^4I_{15/2} \rightarrow {}^4G_{11/2}$ transition in the refinement procedure affects mostly the Ω_2 -value in the normalized procedure, and a little bit the Ω_4 - and Ω_6 -values in the unnormalized one.

Absorption transition	Number	λ_{av} (nm) (*)	Experimental S^{ED} (10^{-20} cm^2)	Calculated S^{ED} (10^{-20} cm^2)
${}^4I_{15/2} \rightarrow$				
${}^4I_{13/2}$	1	1518.7	1.95191	1.70033
${}^4I_{11/2}$	2	978.0	0.63096	0.53791
4I_9	3	809.7	0.33803	0.30834
4F_9	4	655.3	1.35371	1.50901
${}^4S_{3/2}, {}^2H_{11/2}$	5,6	524.8	4.64197	5.59816
4F_7	7	489.6	0.84593	0.87718
${}^4F_5, {}^4F_3$	8,9	450.2	0.28853	0.32593
2H_9	10	407.7	0.25508	0.2438
${}^4G_{11/2}, {}^4G_{9/2}, {}^2K_{15/2}$	11,12,13	376.4	10.71863	7.73976

Table 1. Data used in the Judd-Ofelt calculations. (*) λ_{av} was calculated according to the classical expression. S^{ED} stands for “electric-dipole” oscillator “strength”.

Transition	λ_{av} (nm)	A_{DE} (s^{-1})	A_{DM} (s^{-1})	β	τ_{rad} (ms)
${}^4I_{13/2} \rightarrow {}^4I_{15/2}$	1518.7	157.51	68.04	1	4.433
${}^4I_{11/2} \rightarrow {}^4I_{15/2}$	977.8	217.67	0	0.8254	3.792
$\rightarrow {}^4I_{13/2}$	2745.7	30.26	15.80	0.1746	
${}^4I_9 \rightarrow {}^4I_{15/2}$	801.4	263.85	0	0.7955	
$\rightarrow {}^4I_{13/2}$	1696.6	64.39	0	0.1941	3.015
$\rightarrow {}^4I_{11/2}$	4442.1	1.42	2.02	0.0104	
${}^4F_9 \rightarrow {}^4I_{15/2}$	654.2	2435.84	0	0.9076	
$\rightarrow {}^4I_{13/2}$	1149.4	136.48	0	0.0509	0.373
$\rightarrow {}^4I_{11/2}$	1977.1	89.66	9.80	0.0371	
$\rightarrow {}^4I_9$	3562.5	7.905	4.19	4.5068×10^{-3}	
${}^4S_{3/2} + {}^2H_{11/2}$					
$\rightarrow {}^4I_{15/2}$	541.4	38967.6	0	0.9424	
$\rightarrow {}^4I_{13/2}$	841.3	1195.13	256.83	0.0351	
$\rightarrow {}^4I_{11/2}$	1213.0	353.71	29.54	9.2685×10^{-3}	0.0242
$\rightarrow {}^4I_9$	1668.6	458.29	2.21	0.0111	
$\rightarrow {}^4F_9$	3138.7	85.61	0.35	2.0789×10^{-3}	
${}^4F_7 \rightarrow {}^4I_{15/2}$	487.1	2830.0	0	0.7167	
$\rightarrow {}^4I_{13/2}$	717.1	665.94	0	0.1687	
$\rightarrow {}^4I_{11/2}$	970.6	276.03	0	0.0699	0.253
$\rightarrow {}^4I_9$	1241.9	135.42	12.88	0.0376	
$\rightarrow {}^4F_9$	1906.6	9.49	14.19	5.9961×10^{-3}	
$\Omega_2 = 6.338 \times 10^{-20} \text{ cm}^2$, $\Omega_4 = 1.929 \times 10^{-20} \text{ cm}^2$, $\Omega_6 = 0.943 \times 10^{-20} \text{ cm}^2$, $\delta_{RMS} = 8.4$					

Table 2. Judd-Ofelt parameters and spectroscopic factors of Er^{3+} cations in the “2 ErF_3 ”-doped glass sample.

Branching ratios and radiative lifetimes relevant for the ${}^4I_{13/2} \rightarrow$, ${}^4I_{11/2} \rightarrow$ and $({}^2H_{11/2}, {}^4S_{3/2}) \rightarrow {}^4I_{15/2}$ emission bands calibration in cross section units were virtually unaffected by both the refinement procedure and the fact of taking into account or not the ${}^4I_{15/2} \rightarrow {}^4G_{11/2}$ transition. The results for the normalized procedure with the ${}^4I_{15/2} \rightarrow {}^4G_{11/2}$ transition included in the Judd-Ofelt analysis are shown in Table 2, and

those for the other calculation procedures in the SI file (Tables 2-4). The δ_{rms} obtained (with normalization factor $\sigma=0.025 \times S_{\text{exp}}$), ≈ 8.4 , is slightly higher than the typical values found in Goldner's work [46], especially for Er^{3+} ions, but still satisfactory given the fast convergence and stability of the refinement. The highest ratios of calculated electric-dipole transition strengths over measured ones were found on the ${}^4\text{I}_{15/2} \rightarrow ({}^4\text{S}_{3/2}, {}^2\text{H}_{11/2})$ (≈ 1.2) and the ${}^4\text{I}_{15/2} \rightarrow ({}^4\text{K}_{15/2}, {}^4\text{G}_{9/2}, {}^4\text{G}_{11/2})$ (≈ 0.72) transitions (Table 5 of the SI file). The $\Omega_2=6.338 \times 10^{-20}$ cm^2 intensity parameter is close to those found in $\text{Er}^{3+}:\text{CaF}_2$ crystals [49] and 10 $\text{BaO}-5 \text{PbF}_2-4 \text{La}_2\text{O}_3-\text{Er}_2\text{O}_3-80 \text{TeO}_2$ [44] glass materials, but the $\Omega_4=1.929 \times 10^{-20}$ cm^2 and $\Omega_6=0.943 \times 10^{-20}$ cm^2 intensity parameters are closer to the values found in the 75 $\text{TeO}_2-15 \text{GeO}_2-10 \text{Nb}_2\text{O}_5-5 \text{Li}_2\text{O}-0.5 \text{wt.}\% \text{Er}_2\text{O}_3$ [50] glass. In $\text{Er}^{3+}:\text{KPb}_2\text{Cl}_5$ crystal, a higher Ω_2 -value was found (7.63×10^{-20} cm^2) together with lower $\Omega_4=1.68 \times 10^{-20}$ cm^2 and $\Omega_6=0.43 \times 10^{-20}$ cm^2 set of values [51]. These comparisons suggest qualitatively that Er^{3+} cations are bonded less covalently in our glass than in KPb_2Cl_5 crystals, but more covalently than in CaF_2 crystals. And given the rather high Ω_2 - and moderately high Ω_6 -values, we believe that Er^{3+} ions in our glass are partially surrounded by F^- anions, in a low point group symmetry local environment [52]. $\Omega_2/\Omega_6=6.72$ and $\Omega_4/\Omega_6=2.05$ stand among "high" ratios of intensity parameters, so-called spectroscopic-"quality" parameters, in this kind of glass materials. This favors branching ratios for transitions between multiplets ending on the ${}^4\text{I}_{13/2}$ level, as compared to those of transitions terminating on the ground state, which exhibits the highest $U^{(2,4,6)}$ matrix elements, for instance, ${}^4\text{I}_{11/2}$ and ${}^4\text{I}_{9/2}$ levels. In the heat-treated (and consequently partially crystallized) glass, the only intensity parameter that substantially increases is Ω_2 . According to [52], this could suggest that part of the Er^{3+} ions inserted in the nanocrystals become more surrounded by O^{2-} anions than F^- ones, but this should be taken with pinches of salt because no corresponding covalency effect is observed through the Ω_6 parameter.

3.5 Excitation and emission spectroscopies at 80 K and crystal field calculations

Figure 4 displays the excitation spectrum of the ${}^4\text{S}_{3/2}$, ${}^4\text{I}_{11/2}$ and ${}^4\text{I}_{13/2}$ levels emission spectra recorded at 80 K in the "2 ErF_3 "-doped and untreated glass. No peak position variation was observed between 300 K and 80 K (see Figure 2 of the SI file). Moreover, no effect of the heat-treatment nor of the Er^{3+} concentration on the peak positions was observed (see Figure 3 of the SI file).

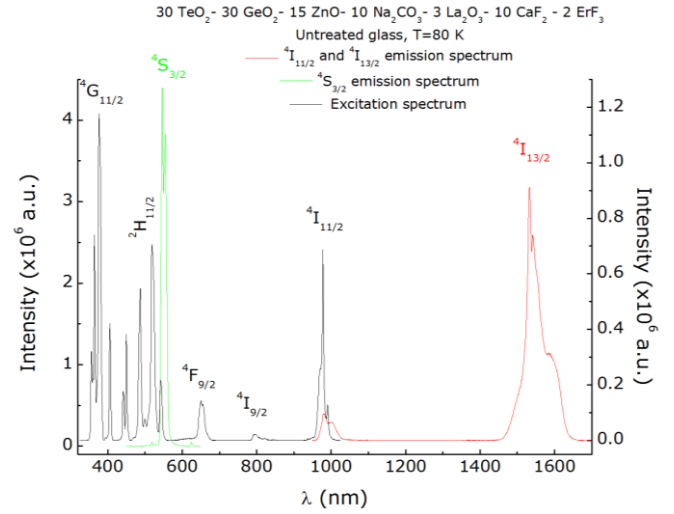


Figure 4. "2 ErF_3 "-doped and thermally untreated glass excitation and emission spectra recorded at 80 K.

In order to calculate the partition function of each multiplet and the crystal field strength, we used the energy levels of 6 multiplets ${}^{2S+1}\text{L}_J$ of the $4f^{11} \text{Er}^{3+}$ electronic configuration. They include 20 crystal field levels, experimentally determined from the emission and the excitation spectra recorded at 80 K, of the ${}^4\text{I}_{15/2}$, ${}^4\text{I}_{13/2}$, ${}^4\text{I}_{11/2}$, ${}^4\text{F}_{9/2}$, ${}^4\text{S}_{3/2}$ and ${}^2\text{H}_{11/2}$ multiplets, and their 6 centroids (see Table 3), that were used as the input data in a parameterized Hamiltonian. The free-ion parameters chosen for our calculations were obtained from Carnall *et al.* [53] and already given in [51] and [54], as well as the expression of the crystal field Hamiltonian. The crystal field potential at the Er^{3+} ion sites was not known *a priori*, neither initial B^k_q parameters nor its point group. So, to initiate the calculations, we first noticed that the ground state (${}^4\text{I}_{15/2}$) experimentally looked like it was composed of 2 Kramers doublets (d) and 3 pseudo-quadruplets (q), the degeneracies of which were lifted by some 10-12 cm^{-1} , positioned in a certain order (d-q-q-d-q). By trial and error using an Oh cubic group, we could simulate and reproduce approximately this energy level diagram ($\Gamma_7-\Gamma_8^{(1)}-\Gamma_8^{(2)}-\Gamma_6-\Gamma_8^{(3)}$). Then, a nonzero B^2_0 parameter was introduced using a C_{4v} point group, and let free to evolve to account roughly for the lifting of the pseudo-quadruplets degeneracies. Subsequently, several point groups were tested (C_4 , S_4 , D_{2d} , C_{3v}) and no rms deviation value lower than ~ 20 cm^{-1} could be obtained, so that finally, a C_2 Hamiltonian using the best B^k_q parameters refined in the previous stages was introduced. This firmly established low point group symmetry is remarkably consistent with the high Ω_2 parameter value found in the Judd-Ofelt analysis. The set of B^k_q parameters was then varied by means of a least-squares procedure based on the 20 energy levels of the above-

mentioned multiplets. The B_q^k 's which gave the best fit to the experimental energy levels, with a rms deviation value of 6.9 cm^{-1} , are (in cm^{-1}), $B_0^2=891.315$, $B_2^2=287.125$, $B_4^0=84.297$, $\text{Re}B_2^4=106.943$, $\text{Im}B_2^4=-54.001$, $\text{Re}B_4^4=45.729$, $\text{Im}B_4^4=-86.293$, $B_0^6=-167.264$, $\text{Re}B_2^6=43.215$, $\text{Im}B_2^6=-16.669$, $\text{Re}B_4^6=22.875$, $\text{Im}B_4^6=15.583$, $\text{Re}B_6^6=-14.120$ and $\text{Im}B_6^6=39.120$. The calculated and experimental energy levels are reported in Table 3.

Er ³⁺ multiplet	Experimental results	CF results	Centroid	Crystal field splitting	Partition function Z
⁴ I _{15/2}	<i>0.0, 36.0, 46.8, 82.0, 93.2, 134.1, 220.6, 229.6</i>	<i>0.0, 36.7, 50.9, 82.2, 96.7, 140.7, 221.1, 233.3</i>	<i>106.4</i>	233.3	5.107
⁴ I _{13/2}	<i>6523.2, 6635.7, 6684.5</i>	<i>6525.8, 6555.3, 6579.8, 6601.4, 6631.7, 6691.5, 730.4</i>	<i>6615.3</i>	204.6	4.764
⁴ I _{11/2}	<i>10209.3, 10261.7, 10288.2</i>	<i>10216.9, 10242.1, 10263.8, 10283.5, 10324.0, 10361.5</i>	<i>10280.2</i>	144.6	4.509
⁴ I _{9/2}	12500.0	12495.3, 12515.1, 12536.6, 12546.9, 12555.1	12530.0 ^(*)	59.8	4.261
⁴ F _{9/2}	<i>15372.8, 15420.2, 15479.9</i>	<i>15376.3, 15425.3, 15478.5, 15508.4, 15572.4</i>	<i>15472.3</i>	196.1	3.324
⁴ S _{3/2}	18298.3	18300.0, 18415.4	18356.0	115.4	1.575
² H _{11/2}	<i>19267.8, 19286.4</i>	<i>19268.9, 19283.6, 19287.5, 19296.5, 19302.6, 19315.6</i>	<i>19287.6</i>	46.7	5.373
⁴ F _{7/2}	20512.8	20515.9, 20617.5, 20669.0, 20745.1	20638.0 ^(*)	229.2	2.427
⁴ F _{5/2}	22246.9	22247.4, 22268.2, 22319.1	22287.0 ^(*)	71.7	2.614
⁴ F _{3/2}	22650.1	22650.7, 22801.3	22710.0 ^(*)	150.6	1.486
² H _{9/2}	24630.5	24628.2, 24655.0, 24667.0, 24683.3, 24716.0	24671.0 ^(*)	87.8	4.134
⁴ G _{11/2}	26560.4	26560.7, 26586.7, 26596.4, 26605.7,	26590.0 ^(*)	62.0	5.037

		26617.2, 26622.7			
⁴ G _{9/2}	27472.5	27474.9, 27486.9, 27490.1, 27491.0, 27495.8	27478.0 ^(*)	20.9	4.704
² G _{7/2}	27777.8	27777.4, 27792.6, 27801.6, 27810.3	27781.0 ^(*)	32.9	3.674
² K _{15/2}	28089.9	28089.2, 28175.5, 28251.6, 28320.9, 28390.3, 28479.0, 28591.0, 28744.2	28375.0 ^(*)	655.0	2.973

Table 3. Comparison of observed and calculated low-lying crystal field sublevel energies of the “2 ErF₃”-doped and untreated glass and calculated positions of upper-lying ones. Numbers in italics are those which were used in the crystal field parameters refinement. The other numbers were calculated a posteriori using the refined parameters and centroids together with manually fixed centroids marked by (*). Except for the partition function column, all numbers are in cm^{-1} .

All the wavefunctions calculated from this refinement were found to be composed of almost pure states ($\geq 99\%$ of the $2S^{+1}L_J$ multiplet), except for the excited states of the thermalized (⁴F_{5/2}/⁴F_{3/2}) multiplets and the lowest crystal field sublevel of the ²G_{7/2} multiplet, which exhibited a few % admixtures of ⁴F_{3/2} and ⁴F_{5/2} states, and ⁴G_{9/2} state, respectively. The ⁴I_{15/2,13/2,11/2,9/2} crystal field sublevels were even found purer than 99.9%. In order to compare the crystal field strength exerted around the Er³⁺ 4f electrons with the one observed in such crystals as KPb₂Cl₅ or Tl₃PbBr₅, we calculated the N_v number introduced by Auzel and Malta and found that the crystal field strength of this glass is about 1589 cm^{-1} . This value stands almost exactly between the value found in KPb₂Cl₅ (1787 cm^{-1}) and the one estimated in Tl₃PbBr₅ (1326 cm^{-1}). In addition, all the multiplets crystal field splittings are much lower ($\leq 10\%$, ²K_{15/2} excluded) than the spin-orbit integral (2376 cm^{-1}) of the Er³⁺ free-ion. Consequently, the ground state ⁴I_{15/2} crystal field sublevels are likely to be fully populated at room and higher temperatures.

3.6 Er³⁺ ions emission spectroscopy and fluorescence decays in the “2 ErF₃”-doped and untreated glass

With the branching ratios and radiative lifetimes issued from the Judd-Ofelt analysis on the one hand (Section 3.4), the partition functions brought about by the crystal field

calculations on the other hand (Section 3.5), we could calibrate the room temperature ${}^4S_{3/2} \rightarrow {}^4I_{11/2}$ and ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ emission bands in cross section units, by both the FL and the reciprocity methods (RM). They are shown in Figure 5. They were derived experimentally by exciting the crystal at 380 nm for visible (${}^2H_{11/2}, {}^4S_{3/2} \rightarrow {}^4I_{15/2}$) emission, or at 650 nm for ${}^4I_{11/2} \rightarrow {}^4I_{15/2}$ NIR and ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ IR emissions. Although the peak cross section values are typical of a non centrosymmetric environment, which forces the electric-dipole mechanism to operate, and the spectra exhibit some “structure”, the emission bands are so (inhomogeneously) broad that they are not resolved. The emission cross sections for the (${}^2H_{11/2}, {}^4S_{3/2}$), ${}^4I_{11/2}$ and ${}^4I_{13/2}$ multiplets increase slightly in the “4 ErF₃”-doped composition. In the “2 ErF₃”-doped glass, the effect of heat treatment is rather limited: it increases the emission cross sections of the (${}^2H_{11/2}, {}^4S_{3/2}$) and ${}^4I_{11/2}$ levels but leaves unchanged the emission cross section of the ${}^4I_{13/2}$ level. However, the integrated emission of the ${}^4I_{13/2}$ level displays a different temperature dependence in the glassy ceramics and in the glass material. The data shown in Figure 6 of the SI file for the “2 ErF₃-doped” samples show that the thermal quenching is less pronounced in the glassy ceramics than in the glass material. This could suggest that part of the Er³⁺ ions dissolved in the nanocrystals. The radiative lifetime refined in such a way that the FL- and RM-calibrated ${}^4I_{11/2}$ and ${}^4I_{13/2}$ emission spectra, match approximately together at the zero-phonon wavelength, is ≈ 16.6 and 9.9 ms, respectively. As compared to the values found by the Judd-Ofelt calculations, these values are unreasonable but nevertheless, this discrepancy set aside, both RM- and FL- spectra agree in peak positions, widths and relative intensities for the ${}^4I_{11/2}$ and the ${}^4I_{13/2}$ levels.

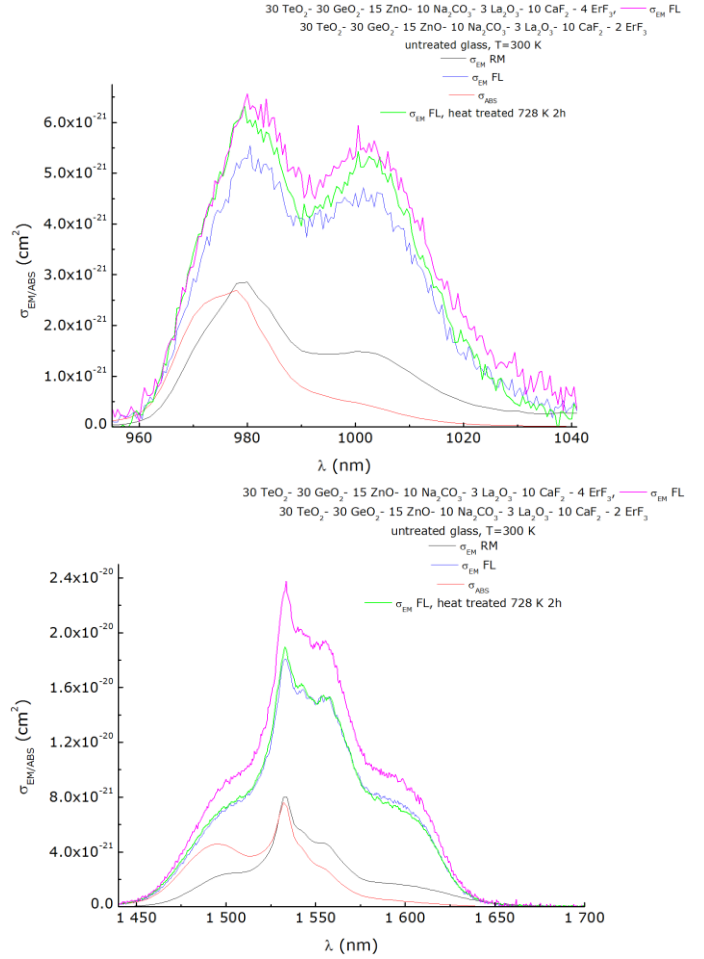
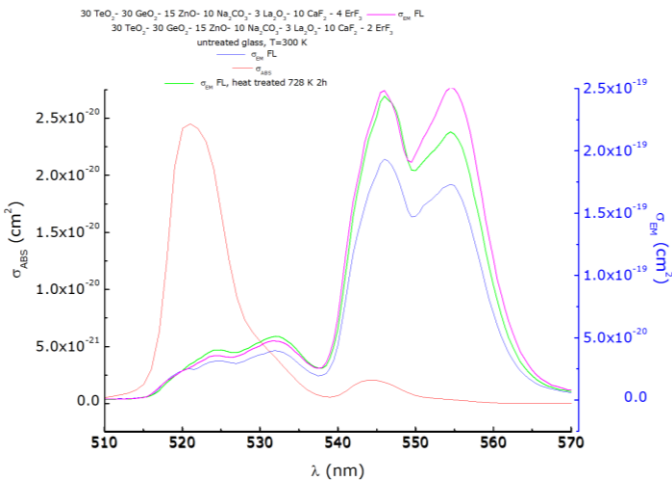


Figure 5. Absorption, RM- and FL-calibrated emission spectra in Er³⁺-doped glasses and glass-ceramics. Emission spectra were obtained by exciting at 380 nm the visible (${}^2H_{11/2}, {}^4S_{3/2} \rightarrow {}^4I_{15/2}$) emission, or by exciting at 650 nm the ${}^4I_{11/2} \rightarrow {}^4I_{15/2}$ NIR and ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ IR emissions.



Er³⁺ ions fluorescence decays as a function of temperature in “2 ErF₃”-doped glasses shown in figure 6 can be fitted to an exponential law over time ranges which vary with the emission level: 4, 0.1 and 2 times τ_{rad} for the ${}^4S_{3/2}$, ${}^4I_{11/2}$ and ${}^4I_{13/2}$ multiplets, respectively. The resulting experimental lifetimes lead to fluorescence quantum yields of 3.4 and 67.2% for the two latter levels, reflecting the overall possible effects of intrinsic non radiative decays and quenching by impurities. The heat treatment on the “2 ErF₃”-doped composition does not affect the ${}^4S_{3/2}$ lifetime, but increases slightly that of the ${}^4I_{11/2}$ level and substantially that of the ${}^4I_{13/2}$ level (by a factor $\times 1.4$). On the other hand, the lifetimes of the ${}^4S_{3/2}$, ${}^4I_{11/2}$ and ${}^4I_{13/2}$ levels at room temperature decrease drastically with the increase in dopant concentration (Figs. 4 and 5 of the SI file). This is likely to be due to quenching by impurities.

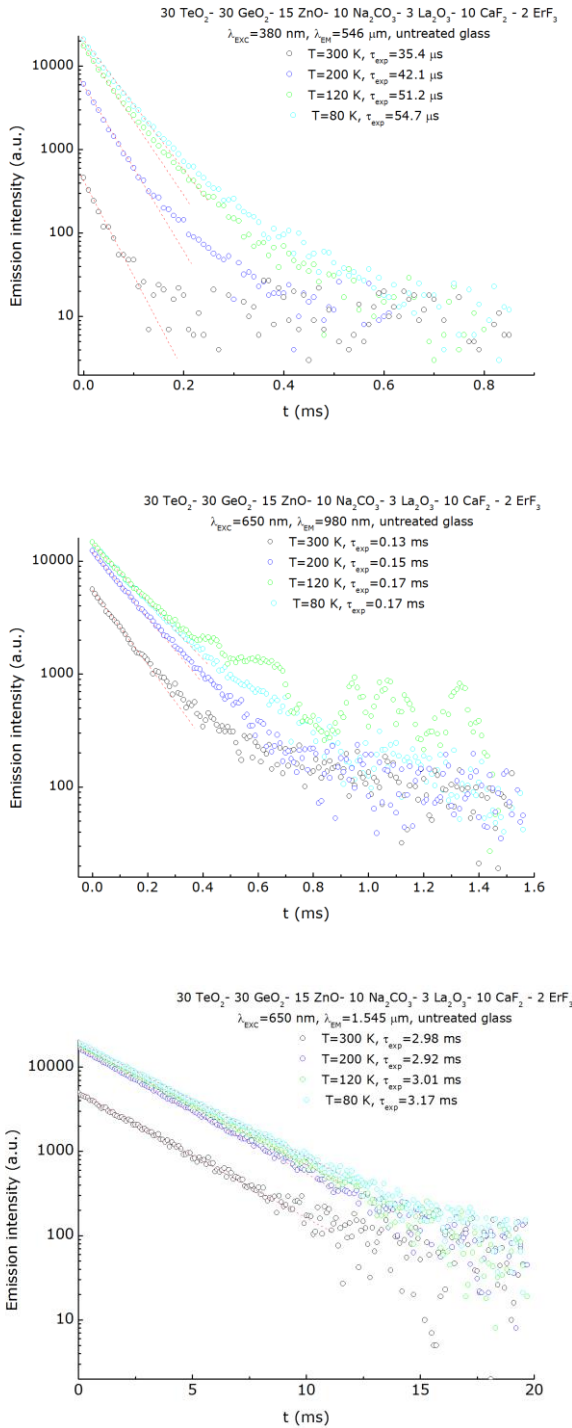


Figure 6. Er^{3+} ions fluorescence decays at $\lambda_{em}=456$ ($^4S_{3/2}$), 980 ($^4I_{11/2}$) and 1545 ($^4I_{13/2}$) nm in the “2 ErF_3 ”-doped and untreated glass as a function of temperature.

3.7 Magnetic susceptibility of Er^{3+} -doped glass and glassy ceramics

Another way to investigate the potential impact of structural changes near the Er^{3+} cations is to measure the magnetic susceptibility of the glass and the glassy ceramics as a function of temperature, and cycling around the crystallization temperature. Figure 7 shows the magnetic susceptibility measurements (in the MKSA units system) of the “2 ErF_3 ”- and “4 ErF_3 ”-doped glasses. The excitation and emission spectroscopies (Fig. 4) combined with crystal field calculations (Table 3) established that the ground state ($^4I_{15/2}$) energy splitting is 335 K, which is smaller than both the spin-orbit integral and the thermal activation energy scanned in our measurements (300–950 K), but however much higher than the magnetic characteristic energy due to the applied magnetic field, typically $Jg\mu_B\mu_0H/k_B\sim 6$ K.

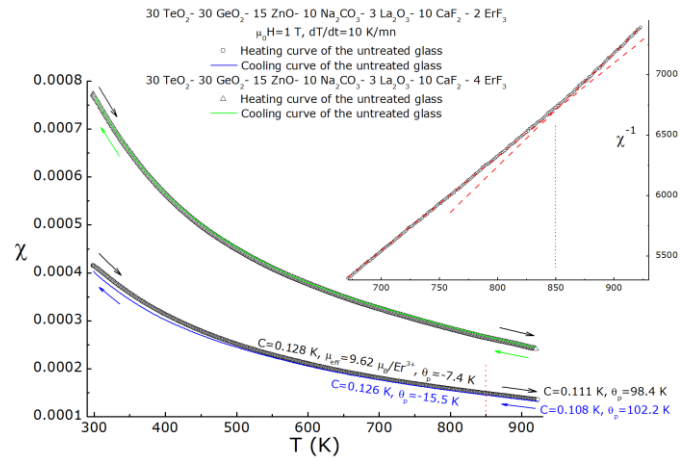


Figure 7. MKSA magnetic susceptibility of “2 ErF_3 ”- and “4 ErF_3 ”-doped glasses, measured upon cycling around the crystallization temperature, and zoom of the high temperature inverse magnetic susceptibility of the former glass. Between the black and the blue curves, a 15 mn-long stage at 930 K is applied.

These energy considerations explain why, contrary to the Yb^{3+} -doped glass analog [26], the paramagnetic susceptibility curves shown in Fig. 7 can all be fitted to a Curie-Weiss (CW) law from room temperature to 800 K. Note that 800 K is 50 degrees above the crystallization temperature. In the “2 ErF_3 ”-doped glass, this CW behavior is characterized by an effective magnetic moment of $\approx 9.62 \mu_B/Er^{3+}$, equal, given the error bar, to the theoretical free ion value, and it is characterized by slightly antiferromagnetic (AFM) interactions between the Er^{3+} cations ($\theta_p=-7.4$ K). At some higher temperature, close to 850 K, a change of paramagnetic behavior is observed in which the Curie constant decreases slowly but above all the magnetic interactions between Er^{3+} cations become substantially ferromagnetic (FM), with one order of magnitude gain in absolute value of the Curie paramagnetic

temperature, $\theta_p=+98.4$ K. After the 15 minutes stage at 930 K, the system exhibits the same CW behavior (same Curie constant and slightly larger paramagnetic Curie temperature) and reversibly “switch back” to a CW behavior around 850 K where the C constant is the same as upon heating and the paramagnetic Curie temperature is again negative ($\theta_p=-15.5$ K, keeping in mind that this effect is not due to the change in volumic mass of the sample, which was taken into account in the calibration procedure of the magnetic susceptibility in MKSA units). This seemingly and almost reversible behavior suggests that the Er^{3+} cations initially dissolved in the glass undergo some local structure changes leading to a doubling of the Curie temperature. Even if T_g and T_c could not be directly detected on the magnetic χ versus temperature curve, these measurements suggest that the high temperature paramagnetic behavior is dominated by those Er^{3+} cations which are dissolved in the nanocrystallites. The change of sign (from AFM to FM) of the Er^{3+} magnetic interactions is striking and difficult to explain solely from these data. As a matter of fact, in Er^{3+} -doped CaF_2 crystals, the first and second order Zeeman contributions to the overall magnetic susceptibility can lead to FM and AFM interactions, respectively [55], and the net balance depends on Er^{3+} cations concentration and possible clusters formation. The same phenomenological behavior was observed in the 4 ErF_3 -doped glass.

4. Conclusions

New Er^{3+} -doped oxyfluorogermanotellurate glasses have been synthesized and submitted to varied heat treatments to provoke crystallization in their matrix. The nanocrystallites formed have been found to measure typically 50 Å and likely to be of Er^{3+} -doped CaF_2 , by XRD, HRTEM, EDS, SAED, optical spectroscopy and VSM techniques. Heat treatment increases Er^{3+} ions emission cross section at 546 and 980 nm but does not affect it at 1.5 μm , although it increases the experimental lifetime of the $^4\text{I}_{13/2}$ level. Cycling around the crystallization temperature with a VSM shows some kind of “crossover” between the Curie-Weiss behavior of the Er^{3+} cations dissolved in the glass and those dissolved in the nanocrystallites with a striking change of magnetic interactions sign from anti- to ferromagnetic. Judd-Ofelt analysis led to the following intensity parameters $\Omega_2=6.338\times 10^{-20}$ cm^2 , $\Omega_4=1.929\times 10^{-20}$ cm^2 , $\Omega_6=0.943\times 10^{-20}$ cm^2 , and the rather high Ω_2 -value was found consistent with crystal field calculations with a refined parameterized Hamiltonian of C_2 -symmetry, which eventually permitted to estimate the crystal field strength in this glass, $N_v=1589$ cm^{-1} .

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