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Impact of polarised extragalactic sources on the measurement of CMB *B*-mode anisotropies

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ABSTRACT

One of the main goals of cosmology is to search for the imprint of primordial gravitational waves in the polarisation filed of the cosmic microwave background to probe inflation theories. One of the obstacles in detecting the primordial signal is that the cosmic microwave background B-mode polarisation must be extracted from among astrophysical contaminations. Most efforts have focus on limiting Galactic foreground residuals, but extragalactic foregrounds cannot be ignored at the large scale ($\ell \leq 150$), where the primordial B-modes are the brightest. We present a complete analysis of extragalactic foreground contamination that is due to polarised emission of radio and dusty star-forming galaxies. We update or use current models that are validated using the most recent measurements of source number counts, shot noise, and cosmic infrared background power spectra. We predict the flux limit (confusion noise) for future cosmic microwave background (CMB) space-based or balloon-borne experiments (IDS, PIPER, SPIDER, LiteBIRD, and PICO), as well as ground-based experiments (C-BASS, NEXT-BASS, QUIJOTE, AdvACTPOL, BICEP3+Keck, BICEPArray, CLASS, Simons Observatory, SPT3G, and S4). The telescope aperture size (and frequency) is the main characteristic that affects the level of confusion noise. Using the flux limits and assuming mean polarisation fractions independent of flux and frequency for radio and dusty galaxies, we computed the B-mode power spectra of the three extragalactic foregrounds (radio source shot noise, dusty galaxy shot noise, and clustering). We discuss their relative levels and compare their amplitudes to that of the primordial tensor modes parametrised by the tensor-to-scalar ratio r. At the reionisation bump ($\ell = 5$), contamination by extragalactic foregrounds is negligible. While the contamination is much lower than the targeted sensitivity on r for large-aperture telescopes at the recombination peak ($\ell = 80$), it is at a comparable level for some of the medium- (~ 1.5 m) and small-aperture telescope (≤ 0.6 m) experiments. For example, the contamination is at the level of the 68% confidence level uncertainty on the primordial r for the LiteBIRD and PICO space-based experiments. These results were obtained in the absence of multi-frequency component separation (i.e. considering each frequency independently). We stress that extragalactic foreground contaminations have to be included in the input sky models of component separation methods dedicated to the recovery of the CMB primordial B-mode power spectrum. Finally, we also provide some useful unit conversion factors and give some predictions for the SPICA B-BOP experiment, which is dedicated to Galactic and extragalactic polarisation studies. We show that SPICA B-BOP will be limited at 200 and $350 \,\mu m$ by confusion from extragalactic sources for long integrations in polarisation, but very short integrations in intensity.

Key words. cosmic background radiation - submillimeter: galaxies - radio continuum: galaxies

1. Introduction

The Λ CDM model is the standard model of cosmology. It is the simplest parametrisation of the Hot Big Bang model, with two principal ingredients: Λ refers to a cosmological constant (i.e. the energy density of the vacuum), and CDM stands for cold dark matter, that is, dark matter particles that move slowly. Because it is very successful in predicting a wide variety of observations related to the cosmic microwave background (CMB), the large-scale structure, and gravitational lensing, the Λ CDM model has reached the status of a paradigm. In this paradigm, an era of early exponential expansion of the Universe, dubbed cosmic inflation, has been proposed to explain why the Universe as revealed by the CMB radiation is almost exactly Euclidean and so nearly uniform in all directions. While the basic Λ CDM model fits all the data (with parameters known at the percent level), the physics of inflation is still unknown. Thus, one of the central goals of

modern cosmology is to determine the nature of inflation. One generic prediction is the existence of a background of gravitational waves, which produces a distinct, curl-like signature in the polarisation of the CMB. This is referred to as primordial *B*-mode polarisation (which is due to tensor perturbations). The detection of this primordial B-mode polarisation would provide clear proof that inflation did occur in the early Universe. Unfortunately, cosmic inflation does not provide a unique prediction for the amplitude of the primordial tensor modes parametrised by the tensor-to-scalar ratio r. We are in a situation where there is no natural range for r, in particular, there is no relevant lower bound. The natural goal is to be able to measure *r* beyond doubt for the Higgs inflation (which is an inflation scenario where the inflaton field is the Higgs boson), that is, $r \ge 2 \times 10^{-3}$ at 5σ . If this does not lead to a detection, it will discard the whole class of large-field models. If the inflaton field was nothing but the Higgs field, this would have tremendous consequences for physics. Thus a precise measurement of (or upper bound on) r is essential to constrain inflation physics. The current 95% CL upper limit on r as measured by *Planck*¹ combined with ground-based CMB experiments is r < 0.056 (Planck Collaboration X 2020) at a pivot scale of k = 0.002 Mpc⁻¹. The search for the primordial *B*-mode is an outstanding challenge that has motivated a number of experiments designed to measure the anisotropies of the CMB in polarisation with an ever-increasing precision.

B-modes are also generated by gravitational lensing of *E*-mode polarisation, providing a unique window into the physics of the evolved Universe and invaluable insights into late-time physics, such as the effect of dark energy and the damping of structure formation by massive neutrinos. These lensing *B*-modes are a nuisance for the primordial *B*-mode. Several approaches have been studied for the CMB *B*-mode delensing using large-scale structure surveys (galaxies or the cosmic infrared background (CIB), e.g. Smith et al. 2012; Sherwin & Schmittfull 2015; Manzotti et al. 2017), or assuming that the lensing potential can be estimated internally from CMB data (e.g. Carron et al. 2017; Sehgal et al. 2017).

In addition to instrumental challenges, future experiments targeting $r \sim 10^{-3}$ will have to solve the critical problem of component separation. In addition to lensing, polarised Galactic foreground contamination dominates the amplitude of the large-scale CMB B-modes by several orders of magnitude. The capabilities of future experiments to remove the contamination due to polarised Galactic emissions have been investigated for example by Errard et al. (2016), Remazeilles et al. (2016) and Philcox et al. (2018). We investigate the polarisation fluctuations caused by extragalactic contaminants: radio galaxies and dusty star-forming galaxies (DSFG). While polarised compact extragalactic sources are expected to be a negligible foreground for CMB *B*-modes near the reionisation peak ($\ell < 10$), they are expected to be the dominant foreground for $r = 10^{-3}$ when delensing has been applied to the data, from the recombination peak to higher multipoles, $\ell > 50$ (Curto et al. 2013).

Extragalactic radio sources are typically assumed to be Poisson distributed in the sky. The clustering of radio sources is strongly diluted by the broad distribution in redshifts of objects that contribute at any flux density. The contribution of clustering to the angular power spectrum is therefore small and can be neglected if sources are not subtracted down to very faint flux limits, $S \ll 10$ mJy (González-Nuevo et al. 2005).

For DSFG, we have to consider polarisation fluctuations not only for the Poisson distribution of point sources, but also for the clustering, that is, the CIB anisotropies (e.g. Knox et al. 2001; Negrello et al. 2004; Viero et al. 2013; Planck Collaboration XXX 2014). The CIB power spectrum can be represented as the sum of two contributions that are usually called the one-halo and two-halo terms. The one-halo represents the correlation of galaxies in the same dark matter halo (pairs of galaxies inside the same halo); the two-halo, capturing the galaxy correlations in different dark-matter haloes, describes the large-scale clustering. While we expect some polarisation fluctuations from the one-halo (which is close to Poisson fluctuations), polarised two-halo fluctuations are expected to be null, provided there is no correlation of the polarisation of galaxies within distinct halos. We could have a contribution from the large-scale clustering because of galaxy spin alignments in the filamentary dark-matter structure (e.g. Codis et al. 2018; Piras et al. 2018, and references therein). However, as recently shown by Feng & Holder (2020), this contribution is >100 and \geq 1000 times lower than the shot noise of DSFG at $\ell = 100$ and $\ell = 1000$, respectively. Thus we consider that it has a negligible effect because it is extremely weak.

We compute the expected level of polarised fluctuations from the shot noise of radio galaxies and DSFG and from the CIB onehalo using current or updated models for a large set of future CMB space-based or balloon-borne experiments (IDS, PIPER, SPIDER, LiteBIRD, and PICO)², as well as ground-based experiments (C-BASS, NEXT-BASS, QUIJOTE, AdvACTPOL, BICEP3+Keck, BICEPArray, CLASS, SO, SPT3G, and S4)³. Our predictions use a point-source detection limit that is selfconsistently computed for each experiment (taking the sensitivities into account and determining confusion noises using our number count models). We also include some predictions for SPICA B-POP. An accurate computation of the flux detection limit is mandatory to predict the shot noise of radio sources because changing the flux cut by 30% affects the shot noise by 30%, while it is less important for DSFG: a small variation in the flux cut leads to only a small variation in shot-noise power (Planck Collaboration XVIII 2011).

Our work extends previous studies that concentrated either on a single experiment (e.g. De Zotti et al. 2015), a restricted frequency area (e.g. Bonavera et al. 2017a; Curto et al. 2013), a given galaxy population (e.g. radio galaxies; Puglisi et al. 2018), or on high multipoles (e.g. Gupta et al. 2019 for $\ell \ge 2000$; e.g. Datta et al. 2019 for CMB EE). We are the first to use our radio and DSFG models in combination with the CIB and CMB contamination and instrument noise to iteratively predict the confusion noise that is due to extragalactic sources for all experiments and then derive the level of polarised fluctuations.

The paper is organised as follows. We present the evolutionary models for radio sources and DSFG and discuss their polarised emission in Sects. 2 and 3. In Sect. 4 we give the formalism for computing polarised shot noise from galaxy number counts in intensity. We then describe our halo model of CIB anisotropies that is used to compute the polarisation power spectra that arise from the clustering of DSFG (Sect. 5). We use these models to compute the flux limit (caused by the fluctuations of the background sky brightness below which sources cannot be detected individually, i.e. the confusion noise) for a large number of future CMB experiments and for SPICA B-POP (Sect. 6). The flux limits allow us to compute the expected level of radio and dusty galaxy polarised shot noises, which we discuss (together with the polarised one-halo) in Sect. 7.1, and which we compare to the CMB primordial B-mode power spectrum in Sect. 7.2 for all experiments. We conclude in Sect. 8.

¹ *Planck* (http://www.esa.int/Planck) is a project of the European Space Agency (ESA) with instruments provided by two scientific consortia funded by ESA member states and led by Principal Investigators from France and Italy, telescope reflectors provided through a collaboration between ESA and a scientific consortium led and funded by Denmark, and additional contributions from NASA (USA).

² The meaning of all abbreviations is: inflation and dust surveyor, primordial inflation polarisation explorer, lite (light) satellite for the studies of *B*-mode polarisation and inflation from cosmic background radiation detection, and probe of inflation and cosmic origins for IDS, PIPER, LiteBIRD and PICO, respectively.

³ The meaning of all abbreviations is: *C*-band all-sky survey, next band all-sky-survey, Q-U-I joint Tenerife, advanced Atacama cosmology telescope polarimeter, background imaging of cosmic extragalactic polarisation, cosmology large angular scale surveyor, Simons observatory, south pole telescope and stage-4 for C-BASS, NEXT-BASS, QUI-JOTE, AdvACTPOL, BICEP, CLASS, SO, SPT, and S4, respectively.

2. Radio sources

In this section, we present the evolutionary model we are choosing to describe the number counts of radio galaxies (Sect. 2.1), and its update (Sect. 2.2). We then discuss the polarised emission of radio galaxies (Sect. 2.3). Finally, we compute the shot noise using our model and compare it with observations from CMB experiments (Sect. 2.4.1).

2.1. Number counts at cm to mm wavelengths

Number counts of extragalactic radio sources are well determined at radio frequencies $\nu \lesssim 10 \,\text{GHz}$ down to flux densities of $S \leq 1 \text{ mJy}$ (and even $S \leq 0.03 \text{ mJy}$ at 1.4 GHz) based on data from deep and large area surveys (e.g. Bondi et al. 2008; De Zotti et al. 2010; Bonavera et al. 2011; Massardi et al. 2011; Miller et al. 2013; Smolčić et al. 2017; Puglisi et al. 2018; Huynh et al. 2020). At higher frequencies, that is, from tens of GHz to millimetre (mm) wavelengths, observational data on radio sources are mainly provided by CMB experiments (e.g. Planck Collaboration XXVI 2016; Datta et al. 2019; Gralla et al. 2020; Everett et al. 2020). Space missions such as WMAP and Planck, which cover the full sky, were able to detect only bright sources, with flux densities higher than a few hundred mJy at best. On the other hand, the better angular resolution of groundbased experiments allows them to reach deeper in flux density, but on smaller areas of the sky. The uncertainties on number counts are therefore still large, especially in the frequency range where the CMB dominates, that is, between 70 and 300 GHz.

Evolutionary models for extragalactic radio sources (e.g. Toffolatti et al. 1998; De Zotti et al. 2005; Massardi et al. 2010) are able to provide a good fit to data on luminosity functions and multi-frequency source counts from ~100 MHz to \gtrsim 5 GHz. They adopt a schematic description of radio source populations, divided into steep- and flat-spectrum (or blazars) sources, according to the spectral index of the power-law spectrum, $S(v) \propto v^{\alpha}$, at GHz frequencies that is lower or higher than -0.5. A simple power law is also used to extrapolate spectra to high frequencies, $v \gg 5 \,\text{GHz}$. However, especially for blazars, real source spectra are generally more complex than a power law, which can hold only for limited frequency ranges. As a consequence, these models tend to over-predict the number counts of radio sources at $v \gtrsim$ 100 GHz, as measured by the Atacama Cosmology Telescope (ACT) at 148 GHz (Marriage et al. 2011), for instance, or by Planck in all the High Frequency Instrument (HFI) channels (Planck Collaboration XIII 2011; Planck Collaboration Int. VII 2013). The main reason for this disagreement is the spectral steepening observed in Planck radio source catalogues above ~70 GHz (Planck Collaboration XIII 2011; Planck Collaboration XV 2011; Planck Collaboration Int. XLV 2016) that was previously suggested by other data sets (González-Nuevo et al. 2008; Sadler et al. 2008).

A first attempt of taking this steepening in blazar spectra into account was made by Tucci et al. (2011). They described the spectral behaviour of blazars at cm–mm wavelengths statistically by considering the main physical mechanisms responsible for the emission. In agreement with classical models of the synchrotron emission in the inner jets of blazars (Blandford & Königl 1979; Konigl 1981; Marscher & Gear 1985), the spectral high-frequency steepening was interpreted as caused, at least partially, by the transition from the optically thick to the optically thin regime. The frequency v_M at which the spectral break occurs depends on the relevant physical parameters of AGNs: the redshift, the Doppler factor (δ) , and the linear dimension of the region (approximated as homogeneous and spherical) that is mainly responsible for the emission at the break frequency. In particular, Tucci et al. (2011) showed that the break frequency can be written in an approximated form as

$$v_M \approx C(\alpha_{fl}, \alpha_{st}, S_{\nu_0}) \frac{D_L}{r_M \sqrt{(1+z)^3 \delta}},$$
(1)

where $D_{\rm L}$ is the luminosity distance of the sources, and *C* is a function of the spectral indices before and after the break frequency (α_{fl} and α_{st} respectively) and of the flux density S_{ν_0} at a reference frequency (typically 5 GHz; see their Appendix B). Finally, the parameter r_M is the distance from the AGN core of the jet region that dominates the emission at the frequency ν_M (for a conical jet model, this parameter can be easily related to the dimension of the emitting jet region). It defines the dimension and thus the compactness of the emitting region at that frequency. This is the most critical parameter for determining ν_M because the uncertainty on its actual value is large.

Based on 5 GHz number counts and on information of spectral properties of radio sources at GHz frequencies, the Tucci et al. (2011) model provided predictions of number counts at cm/mm wavelengths by extrapolating flux densities of radio sources from low (1-5 GHz) to high frequencies. The model considered three populations of radio sources (steep-, inverted-, and flat-spectrum sources), and a different high-frequency spectral behaviour for each of them. Here we focus on blazars, which are the dominant class at $\nu \gtrsim 70 \,\text{GHz}$. The most successful model studied in the paper (referred to as "C2Ex") assumes different distributions of the break frequency for BL Lac objects and flat-spectrum radio quasars (FSRQs). According to this, most FSRQs should bend their otherwise flat spectra between 10 and 100 GHz, whereas in BL Lac, spectral breaks are expected typically at $v \gtrsim 100 \,\text{GHz}$ (implying that the observed synchrotron radiation comes from more compact emitting regions than FSRQs). This dichotomy has indeed been found in the Planck radio catalogues (Planck Collaboration XIII 2011; Planck Collaboration Int. XLV 2016). This model provides a very good fit to all the data of bright ($S \gtrsim 100 \text{ mJy}$) radio sources for number counts and spectral index distributions up to ~500- 600 GHz (Planck Collaboration XIII 2011; Planck Collaboration Int. VII 2013).

A partial agreement is also found when other surveys, deeper in flux than *Planck*, are considered. In Fig. 1 we compare the number counts from the model with observational data at frequencies between 70 and 220 GHz. Beyond *Planck*, data are from ACT (150, 218 GHz; Marsden et al. 2014; Datta et al. 2019) and SPT and SPT (95, 150, 220 GHz; Mocanu et al. 2013a). The model tends to underestimate SPT/ACT counts in the flux density range Bonavera et al. (2017a), Gupta et al. (2019) mJy. Very recently, however, Everett et al. (2020) presented the number counts from the full 2500 square degrees of the SPT-SZ survey; they extended previous SPT results (see the green points in Fig. 1). These new data agree better with the C2Ex model estimates at 220 GHz.

2.2. Updated model for number counts

The recent data from ACT and SPT experiments give us the opportunity to better constrain the model parameters for blazars. We described above that the break frequency depends on a set of physical parameters related to AGNs. Tucci et al. (2011) imposed most of them on the basis of observational constraints (as the redshift distribution of the different radio source populations; the Doppler



Fig. 1. Normalized differential number counts $(S^{5/2}n(S))$ from the Tucci et al. (2011) model (black lines) and observations (*Planck*, black points; ACT, cyan points; SPT, blue and green points) between 70 and 220 GHz. Red lines represent the model, but with the updated parameter values as described in the text. The very recent measurements from ACT at 148 GHz (cyan dots from Datta et al. 2019) and from SPT-SZ (green dots from Everett et al. 2020) are not used in the fit, but are shown for comparison.

factor; spectral indices) and on the basis of typical assumptions for AGN model (equipartition condition, narrow conical jets, etc.). The only free parameter used in the model is the distance r_M to the AGN core of the emitting jet region at the break frequency. In the best model of Tucci et al. (2011), r_M is taken to be log-uniformly distributed in the range of [0.3, 10] pc for FSRQs and in the range of [0.01, 0.3] pc for BL Lacs.

We now determine the best estimate of the r_M range by fitting number counts from Planck, ACT (Marsden et al. 2014) and SPT (Mocanu et al. 2013a) between 70 and 220 GHz. This is done only for BL Lacs, while for FSRQs we maintain the same range of r_M values as before. We verified that a change in the r_M interval for this class of objects does not improve the fit of the number counts at sub-Jy level significantly (i.e. for ACT/SPT data). This is not surprising because FSRQs provide the dominant contribution to number counts of bright sources, with $S \gg 100 \,\mathrm{mJy}$ (see Fig. 1). At these flux levels, the strong constraints come from *Planck* measurements, which are already well described by the model. On the other hand, at fainter fluxes, the relevance of BL Lacs increases, and we expect them to become the dominant population at a few dozen mJy. This is exactly the range of fluxes in which the model slightly underestimates the observed number counts. By increasing the contribution of BL Lacs, we should remove or reduce the discrepancy between model and SPT/ACT data without affecting the predictions for the very bright sources.

Jointly with r_M , we considered the spectral index α_{st} of blazars after the break frequency (i.e. in the optically thin regime) as an additional free parameter in the fit. Tucci et al. (2011) assumed this to be distributed as a Gaussian around

 $\langle \alpha_{st} \rangle = -0.8$ with a dispersion of 0.2, in agreement with the canonical values for the optically thin synchrotron spectral index. No differences between the two classes of blazars were considered. However, Planck Collaboration XIII (2011), Planck Collaboration Int. XLV (2016) found that the average spectral index of blazars after the spectral break is somewhat flatter than -0.8.

The results of the fit give more compact radio-emission regions in BL Lacs than previous values, with $0.0025 \le r_M \le 0.05$ pc, that is, about a factor 5 smaller than before. In addition, the average high-frequency spectral index is flatter, $\langle \alpha_{st} \rangle = -0.7$, consistent with the trend observed in *Planck* data.

Number counts predicted by the updated model differ mainly at low- to intermediate-flux densities, S < 0.1 mJy, and provide an improved fit to observational data at 95 and 150 GHz (see Fig. 1). The reduced χ^2 is now very close to 1. SPT data at 95 GHz are still slightly higher, between 20 and 60 mJy, but the discrepancy is reduced and is not significant. The change in the average value of $\langle \alpha_{st} \rangle$ also produces a small increase in the number counts of FSRQs at $\nu > 100$ GHz. Number counts from the updated model are provided online⁴.

2.3. Statistical properties of polarised emission

Polarisation in radio sources is typically observed to be a few percent of the total intensity at cm or mm wavelengths (e.g. Murphy et al. 2010; Battye et al. 2011; Sajina et al. 2011; Massardi et al. 2013; Galluzzi et al. 2019), and only very few

⁴ https://people.lam.fr/lagache.guilaine/Products

Table 1. Shot-noise power of residual radio sources, $D_{\ell} = \ell(\ell + 1)C_{\ell}/2\pi \, [\mu K_{CMB}^2]$, at $\ell = 3000$, estimated in ACT and SPT data, and predicted by models.

	A	СТ		SPT	
v[GHz]	148	218	95	150	220
$S_{\rm cut}$ [mJy]	15	15		6.4	
Dunkley+13	3.2 ± 0.4	1.4 ± 0.2	7.2 ± 0.8	1.4 ± 0.2	0.7 ± 0.1
George+14			7.81 ± 0.75	1.06 ± 0.17	
Tucci+11	2.6	1.4	5.9	1.0	0.48
Updated	3.2	1.7	6.6	1.3	0.67

objects show a fractional polarisation, $\Pi = P/S$, as high as ~10%. Steep-spectrum radio sources are on average more polarised than flat-spectrum sources at $v \leq 20$ GHz (Tucci et al. 2004; Klein et al. 2003). Their fractional polarisation strongly depends on the frequency, from ~2.5% at 1.4 GHz to ~5.5% at 10.5 GHz (Klein et al. 2003). At low frequencies, flat-spectrum sources are instead characterised by an almost constant and low degree of polarisation (~2.5%).

Extensive studies of high-frequency polarisation properties have been conducted by Tucci & Toffolatti (2012) and Massardi et al. (2013) using the Australia Telescope 20 GHz (AT20G) survey (Murphy et al. 2010). This is a quite deep survey in intensity (with a completeness level of 91% at $S \ge$ 100 mJy and 79% at $S \ge$ 50 mJy in regions south of declination -15°) with a high detection rate in polarisation. Moreover, simultaneous measurements at 5 and 8 GHz are also available for a consistent fraction of objects. These analyses found that the distribution of the polarisation degree (in blazars) is well described by a log-normal function (see also Battye et al. 2011) with an average fractional polarisation of ~3%. No clear correlation between the fractional polarisation and the flux density was observed, with a slight dependence on the frequency of the polarisation degree.

At frequencies $v > 20 \,\text{GHz}$, polarisation measurements of very bright sources ($S \gtrsim 1 \text{ Jy}$) seem to indicate an increase in fractional polarisation with frequency. Using the VLA for polarisation measurements of a complete sample of the WMAP catalogue, Battye et al. (2011) found that $\langle \Pi^{rad} \rangle = 2.9, 3.0, \text{ and } 3.5\%$ at 8.4, 22, and 43 GHz, respectively, and a fractional polarisation that is typically higher at 86 GHz than at 43 GHz. This was confirmed by measurements at 86 GHz from Agudo et al. (2010), obtained with the IRAM 30 m Telescope. They found that for sources with detected polarisation at 15 GHz, the fractional polarisation at 86 GHz is higher than at 15 GHz by a mean factor of \sim 2. However, these results were not confirmed using new data and/or improved data analysis procedures (Hales et al. 2014; Bonavera et al. 2017b; Galluzzi et al. 2017; Puglisi et al. 2018; Trombetti et al. 2018; Datta et al. 2019; Gupta et al. 2019). No significant trends of the polarisation degree with flux density or with frequency are found at the frequencies of interest for CMB B-mode search. Latest measurements of fractional polarisation at $\nu > 50 \text{ GHz}$ vary from ~1.5 to 3.5% and are obtained either using log-normal fits to the distribution of observed polarisation fractions, or using stacking or statistical approaches. To compute the radio source contamination in polarisation to the CMB *B*-mode (Sect. 7), we assumed a constant $\langle \Pi^{rad} \rangle = 2.8\%$, in agreement with the recent Planck (e.g. Puglisi et al. 2018), SPT (Gupta et al. 2019) and ACT (Datta et al. 2019) measurements, and radio source follow-ups from 90 to 220 GHz.

2.4. Shot-noise predictions

In this section, we compare the shot-noise level from residual radio sources found in observational data with values expected from our reference model, to confirm the validity of the model. As the radio shot noise level is highly sensitive to the flux limit, we also provide some useful empirical relations that allow us to compute the shot-noise level as a function of the flux limit.

2.4.1. Shot-noise levels in current CMB experiments

We report the residual shot-noise level in ACT and SPT data estimated by Dunkley et al. (2013) and George et al. (2015), and compare them with predictions from the Tucci et al. (2011) model before and after our update in Table 1. The agreement is quite good for both cases, although the shot-noise level of the updated model is closer to the observational estimates.

In Table 2 we report auto- and cross-power spectra (shot noise only) due to residual radio sources in *Planck* data according to the updated model. We also compute the error of these predictions due to an uncertainty in the flux cut of 20 and 30%. Moreover, we give a tentative estimate of the error associated with the uncertainty on the model that is computed as the difference between results from the old and the updated model. The uncertainties we find are probably quite conservative, but they are nevertheless smaller than the errors due to a 20% uncertainty in S_{cut} at frequencies where radio sources are dominant (i.e. $v \leq 217 \text{ GHz}$).

The consistency between the measured Poisson amplitude in the *Planck* auto- and cross-power spectra at 100, 143, and 217 GHz with the updated model discussed here has previously been investigated in Planck Collaboration XI (2016, see their Table 20). The agreement is good, except at 100 GHz, where the predicted amplitude is significantly lower than the observed value. However, this discrepancy was attributed by the authors to a residual unmodelled systematic effect in the data rather than to a foreground modelling error. Moreover, the Poisson power at 100 GHz is found to be smaller in Planck Collaboration V (2020), which agrees better with the model prediction (7.8 Jy² sr⁻¹ for our model with a flux cut of 340 mJy compared to 10.5 Jy² sr⁻¹ for *Planck*, but with an unknown flux cut).

2.4.2. Shot-noise level as a function of flux limits

It can be useful to know the dependence of the shot-noise level from residual radio sources on the flux cut S_{lim} . We considered the *Planck* frequencies, and a range of flux limits between 1 mJy and 1 Jy, that is, more or less the range covered by CMB experiments.

We start with auto-power spectra. We know that differential number counts for radio sources scale approximately as $n(S) \propto S^{-2}$, and power spectra as $C_{\ell} \propto S_{\text{lim}}$. Therefore it is convenient to consider the quantity $\mathcal{D}_{SN} = C_{\ell}/S_{\text{lim}}$. At a given frequency, we fit $\mathcal{D}_{SN} \equiv \mathcal{D}_{SN}(S_{\text{lim}})$ as a double power law:

$$\mathcal{D}_{SN}(S_{\rm lim}) = \frac{2A}{\left(\frac{S_{\rm lim}}{S_0}\right)^{\alpha} + \left(\frac{S_{\rm lim}}{S_0}\right)^{\beta}}.$$
(2)

 $\mathcal{D}_{SN}(S_{\text{lim}})$ from the updated model and the best fits given by Eq. (2) are shown in Fig. 2. The parameters of the fits are provided in Table 3.

Cross-power spectra depend on the flux cuts at the two considered frequencies. In order to describe $C_{\ell}^{\nu_1,\nu_2} \equiv C_{\ell}^{\nu_1,\nu_2}(S_{\lim}^{\nu_1}, S_{\lim}^{\nu_2})$, we chose to use a sixth-degree polynomial function. After computing cross-power spectra in an uniform grid of log(S_{\lim}/Jy) between -3 and 0, we determined the polynomial fit using the IDL routine SFIT. For arbitrary flux limits (but always between 1 mJy and 1 Jy) at frequencies ν_1 and ν_2 , cross-power spectra can be estimated by means of

$$\log \left[C_{\ell}^{\nu_{1},\nu_{2}}(S_{\lim}^{\nu_{1}}, S_{\lim}^{\nu_{2}}) \right] = \sum_{i,j=0}^{6} K_{i,j} \left[\frac{\log(S_{\lim}^{\nu_{1}}) + 3}{0.2} \right]^{j} \left[\frac{\log(S_{\lim}^{\nu_{2}}) + 3}{0.2} \right]^{i} ,$$
(3)

where $K_{i,j}$ are the coefficients of the fit⁵. We verified that the fit has a typical error of 2–3%, with maximum errors of about 10–15% (usually at the borders of the grid). Figure 2 also shows examples of cross-power spectra and the corresponding fits when $S_{\lim}^{\nu_1}$ is fixed.

3. Dusty star-forming galaxies

Similarly to the previous section, we present here the evolutionary model we chose to describe the number counts of DSFGs (Sect. 3.1). We then discuss their polarised emission (Sect. 3.2). Finally, we compute the shot noise using our model and compare it with recent observations (Sect. 3.3).

3.1. Model for the number counts

Since their discoveries in the 1990s, DSFGs have revolutionized the field of galaxy formation and evolution (e.g. Casey et al. 2014). The continuous advent of new experiments (either spacebased - ISO, Spitzer, Herschel, Planck - or ground-based, e.g. SCUBA/JCMT, Laboca/APEX, IRAM, and ALMA) makes the study of high-z dusty galaxies one of the most important areas of extragalactic astronomy. Accompanying the new measurements, many empirical or semi-analytical models have been developed in the past 20 years (e.g. Lagache et al. 2003; Béthermin et al. 2011; Gruppioni et al. 2011; Lapi et al. 2011; Cai et al. 2013; Casey et al. 2018; Popping et al. 2020). We chose to use the model of Béthermin et al. (2012a) here because it provides one of the best fits to the number counts from the mid-IR to radio wavelengths, including counts per redshift slice in the SPIRE bands. Moreover, it gives a reasonable CIB redshiftdistribution, which is important for computing cross-power spectra (Béthermin et al. 2013). Finally, as it has been developed in-house, it can be run for numerous wavelengths and different bandpasses, which is mandatory for our analysis.

v_1	v_2	S _{cut}	C_{ℓ}	$\sigma[S]$	Cut]	σ [model]
		[JY]	[Jy ² sr ⁻¹]	20%	30%	
30	30	0.43	18.36	3.30	4.97	0.45
30	44		15.48	2.87	4.29	0.50
30	70		12.30	2.32	3.50	0.57
30	100		9.58	1.80	2.70	0.62
30	143		7.28	1.34	2.05	0.58
30	217		5.65	1.05	1.57	0.57
30	353		5.44	1.06	1.58	0.79
30	545		4.67	0.91	1.37	0.87
30	857		4.04	0.78	1.18	0.97
44	44	0.76	25.11	4.43	6.63	0.77
44	70		15.34	2.70	4.24	0.65
44	100		10.60	1.97	2.88	0.55
44	143		7.68	1.36	2.12	0.45
44	217		6.11	1.12	1.65	0.45
44	353		8.06	1.49	2.21	0.99
44	545		7.42	1.39	2.10	1.16
44	857		6.60	1.24	1.88	1.36
70	70	0.50	13.46	2.53	3.75	0.63
70	100	0.00	8.71	1.66	2.43	0.56
70	143		6.32	1.14	1.79	0.47
70	217		5.04	0.92	1.39	0.44
70	353		5.98	1.13	1.69	0.86
70	545		5.23	0.99	1.50	0.98
70	857		4.59	0.87	1.30	1.11
100	100	0.34	7.76	1.47	2.21	0.51
100	143		5.36	0.98	1.52	0.48
100	217		4.26	0.78	1.18	0.47
100	353		4.36	0.82	1.23	0.73
100	545		3.75	0.70	1.06	0.81
100	857		3.25	0.61	0.91	0.88
143	143	0.25	4.83	0.92	1.36	0.46
143	217		3.60	0.68	1.00	0.46
143	353		3.31	0.62	0.92	0.61
143	545		2.82	0.52	0.78	0.66
143	857		2.43	0.45	0.67	0.70
217	217	0.20	3.22	0.61	0.90	0.44
217	353	0.20	2.70	0.50	0.75	0.55
217	545		2.31	0.42	0.63	0.59
217	857		1.99	0.36	0.55	0.62
353	353	0.40	4.86	0.87	1.30	0.75
353	545		4.27	0.75	1.13	0.96
353	857		3.69	0.65	0.98	1.04
545	545	0.60	5.79	1.00	1.49	1.07
545	857		5.16	0.89	1.33	1.36

Table 2. Auto- and cross-power spectra due to residual radio sources for *Planck* according to the updated model for the flux cuts reported in the Table.

Notes. Flux cut values correspond to those used to compute some conservative point-source masks inside the *Planck* collaboration for consistency analysis.

1.21

1.80

1.59

7.38

857

857

1.0

The model is based on the main assumption that star-forming galaxies have two modes of star formation: main sequence (MS) and starburst (SB). Main-sequence galaxies are secularly evolving galaxies with a tight correlation between stellar mass (M_{\star}) and star formation rate (SFR) at a given redshift. The evolution of MS and SB galaxies is based on the Sargent et al. (2012) formalism, which jointly used the mass function of star-forming

⁵ $K_{i,j}$ are provided at https://people.lam.fr/lagache.guil aine/Products.

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Fig. 2. Left panel: power spectra (divided by the flux limit) of residual radio sources as a function of the flux limit from 30 to 857 GHz (from top to bottom). Points are from the updated T11 model; solid lines are fits using Eq. (2) with parameters given in Table 3. *Right panel*: cross-power spectra at the frequencies indicated in the figure as a function of the flux limit $S_{lim}^{\nu_2}$ ($S_{lim}^{\nu_1}$ is equal to 0.4 Jy for $\nu_1 = 30$, 70 GHz and 0.1 Jy for $\nu_1 = 100$, 143 GHz). Solid lines are obtained from Eq. (3).

Table 3. Best-fit parameters of Eq. (2) as a function of frequency

ν	$\log(A)$	$\log(S_0)$	α	β
30	1.715	-2.610	0.1658	-0.509
44	1.558	-3.000	0.1223	-0.656
70	1.406	-3.231	0.0967	-0.754
100	1.290	-3.307	0.0829	-0.966
143	1.240	-3.293	0.0948	-0.769
217	1.204	-3.173	0.1152	-0.479
353	1.118	-3.035	0.1222	-0.410
545	1.094	-1.639	0.2154	-0.198
857	0.991	-1.012	0.2999	-0.161

galaxies, the redshift evolution of the sSFR (specific star formation rate, sSFR = SFR/ M_{\star}), and its distribution at fixed M_{\star} , with a separate contribution from MS and SB galaxies to reproduce IR luminosity functions. The model uses redshift-dependent templates for the spectral energy distributions (SED) of MS and SB, based on fits of Draine & Li (2007) models to *Herschel* observations of distant galaxies as presented in Magdis et al. (2012). Finally, as strongly lensed sources contribute ~20% to (sub-)mm counts around 100 mJy, magnification caused by strong lensing ($\mu > 2$) is also included in the model (see Béthermin et al. 2012a for more details).

We show in Fig. 3 the comparison of the model with some measured far-IR/sub-millimetre counts. We also show the counts from Béthermin et al. (2017), obtained using an updated version of the two star-formation mode galaxy evolution model of Béthermin et al. (2012a), combined with abundance matching to populate a dark matter light cone and thus simulate the clustering. Béthermin et al. (2017) produced 2 deg² simulated maps (called SIDES) and extracted the sources as done in the observations. They convincingly showed that the limited angular resolution of single-dish instruments has a strong effect on far IR and sub-millimetre continuum observations. In particular, at 350 and 500 μ m, they reported that the number counts measured by *Herschel* between 5 and 50 mJy are biased towards high values by a factor ~2. When these resolution effects are taken into account, they reproduce a large set of observables

very well, such as number counts and their evolution with redshift and CIB power spectra. This demonstrates that any model should thus underestimate the measured single-dish number counts from ~100 to $1000\,\mu\text{m}$ in a given range of fluxes (see Figs. 4 and 5 in Béthermin et al. 2017). This is indeed the case for Béthermin et al. 2012a (Fig. 3), which agrees very well with the intrinsic SIDES model (and not with the observed SIDES counts). We also show in Fig. 3 the recent counts obtained from the ALMA ALPINE program (Béthermin et al. 2020) at $850 \,\mu m$, which are not affected by blending due to limited angular resolution, and agree well with the model. For bright fluxes (≥ 1 Jy), the redshift grid of the model is too coarse to estimate the Euclidian plateau properly. We therefore directly computed the value of the plateau using Eq. (6) of Planck Collaboration Int. VII (2013). Although it is mostly systematically $\sim 1\sigma$ lower, the model agrees to first order with the Euclidian plateau measured by Planck (Planck Collaboration Int. VII 2013). For the purpose of this paper, number counts at such bright fluxes are not relevant, as their contribution to shot noise and confusion noise is negligible. For example, at 272 GHz (1.1 mm), the confusion noise has converged for a flux cut of $\sim 10 \text{ mJy}$ (i.e. the confusion noise for sources with flux <10 mJy is nearly equal to that of sources with flux <10 Jy). Therefore we are very confident in our use of the Béthermin et al. (2012a) model to compute the shot-noise levels from DSFG. We clearly validate the use of our model to compute the confusion noises in Sect. 6.3.1. The Béthermin et al. (2017) model could not be used for this purpose as it does not give any analytical predictions and the volume of the dark-matter simulation is too small to derive accurate predictions for the largevolume surveys discussed here.

3.2. Polarised emission

Little is known about the polarisation emission of dusty galaxies. Dust enshrouding star-forming galaxies absorbs UV radiation from stars, and re-emits light at longer wavelengths, which is responsible for the far-IR SED of CIB galaxies. Thermal emission from interstellar dust in CIB galaxies, as in our Galaxy, is polarised because the dust grains are aligned with interstellar magnetic fields. The degree of polarisation is not very well known; it is likely to be low because the complex structure of



Fig. 3. Galaxy number counts at 350, 500, and $850\,\mu\text{m}$. The model we used (Béthermin et al. 2012a) is shown with the continuous line. It agrees very well with the most recent Béthermin et al. (2017) model (SIDES, long-dashed line). Measurements are from *Herschel* at 350 and 500 μ m (Oliver et al. 2010; Clements et al. 2010; Glenn et al. 2010; Béthermin et al. 2012c), *SCUBA2*, and ALMA at 850 μ m (Geach et al. 2017; Béthermin et al. 2020), and *Planck* at very bright fluxes (Planck Collaboration Int. VII 2013). The models are below the *Herschel* measurements at intermediate fluxes because these measurements are biased high due to the relatively low angular resolution combined with galaxy clustering (as demonstrated in Béthermin et al. 2017).

galactic magnetic fields with reversals along the line of sight and the disordered alignment of dust grains reduce the global polarised flux when it is integrated over the whole galaxy.

Very few measurements exist for individual galaxies. Measurements at 850 μ m of M82 by Greaves et al. (2002) gave a global net polarisation degree of only 0.4%, while Arp 220 measurements at 850 μ m by Seiffert et al. (2007) gave a 99% confidence upper limit of 1.54%. Using the stacking technique with Planck data on a sample of ~4700 DSFG, Bonavera et al. (2017a) estimated the average fractional polarisation at 143, 217, and 353 GHz. They obtained a mean fractional polarisation $\langle \Pi \rangle$ of 3.10 ± 0.75 and $3.65 \pm 0.66\%$ at 217 and 353 GHz, respectively, after correcting for noise bias. The uncorrected value of $\langle \Pi \rangle$ at 217 GHz is 1.15±0.74%, implying that the detection is significant at the 1.55σ level. At 353 GHz, the detection significance increases from 2.8σ to 5.5σ before and after the correction. Trombetti et al. (2018) revisited these estimates, exploiting the intensity distribution analysis of the *Planck* polarisation maps. They did not detect any polarisation signal from DSFG at a similarly high significance as Bonavera et al. (2017a). They derived a 90% confidence upper limit on the median fractional polarisation at 353 GHz of $\langle \Pi \rangle \leq 2.2\%$. The upper limit at the same confidence level is looser at 217 GHz, $\langle \Pi \rangle \leq 3.9\%$, where dusty galaxies are substantially fainter. These upper limits are consistent with the median values reported in Bonavera et al. (2017a), which are 1.3 ± 0.7 and $2.0 \pm 0.8\%$ at 217 and 353 GHz, respectively. Recently, Gupta et al. (2019) identified 55 sources as DSFG in their SPT sample, and no polarisation signal was detected for these sources. Their 95% confidence level upper limits are quite high and consistent with earlier results. Finally, De Zotti et al. (2018) made an estimate for spiral galaxies seen edge-on based on the average value of the Stokes Q parameter measured using the Planck dust polarisation maps of the Milky Way. They estimated a mean polarisation degree averaged over all possible inclination angles of 1.4%. These low values of fractional polarisation are understood as due to the complex structure of galactic magnetic fields and to the disordered alignment of dust grains. To study the contamination from polarised emission of DSFG to the CMB *B*-modes (Sect. 7), we accordingly adopted $\langle \Pi^{IR} \rangle = 1.4\%$.

3.3. Shot-noise predictions

Béthermin et al. 2017 (see also Negrello et al. 2005; Valiante et al. 2016) showed that counts obtained from single-dish antenna observations in the far-IR to mm are biased high because of source multiplicity and clustering in the large beams (10-30 arcsec). This may cause strong discrepancies between shot noises measured from the integral of the observed number counts and shot noises measured from CIB power spectra. For Herschel/SPIRE, another complexity is introduced into the comparison: the beam profile and aperture efficiency vary across the passband and return a relative spectral response function (RSRF) that is different for point sources and extended emission. To compare model predictions to shot-noise measurements from CIB power spectra, we therefore also ran the model with the RSRF for extended source. Comparisons between model and observations are given in Tables 4 and 5 for Herschel/SPIRE and Planck/HFI, respectively. The shot-noise levels from observations are obtained either by fitting the CIB power spectra using the halo model (Viero et al. 2013; Planck Collaboration XXX 2014) or by fitting the total power spectra using a parametric model and assuming a power law for the CIB (Mak et al. 2017). In the first case, there is a strong degeneracy between the onehalo term and the shot noise, especially at the *Planck* angular resolution.

It is very difficult to derive any conclusion from Tables 4 and 5 because (i) some measured values are incompatible (i.e. when the shot noise derived with a higher flux limit is lower than that derived with a lower flux limit). This is the case for *Planck* at 545 and 353 GHz and for *Herschel* at the three wavelengths. ii) the model is not systematically higher or lower than the measurements. In the frequencies of interest ($\nu \leq 500$ GHz), observations and model predictions agree by 20%, which we assume to be the uncertainty in our prediction. We stress that in contrast to the radio, a small variation in the flux limit *S*_{lim} leads to only a small variation in shot-noise power. For example, changing *S*_{lim} by 30% leads to a variation of the shot-noise level seen by *Planck* by less than 1% at 217 GHz (Planck Collaboration XVIII 2011).

Table 4. *Herschel*/SPIRE shot-noise levels as measured from CIB anisotropies and predicted using the integral of the number counts as modelled by Béthermin et al. (2012a).

Wavelength	Flux limit ⁽¹⁾	Measured ⁽¹⁾	Predicted point source	Predicted extended	Flux limit (2)	Measured ⁽²⁾	Predicted point source	Predicted extended
[µm]	[mJy]	$[Jy^2 sr^{-1}]$	$[Jy^2 \text{ sr}^{-1}]$	$[Jy^2 sr^{-1}]$	[mJy]	$[Jy^2 sr^{-1}]$	$[Jy^2 \text{ sr}^{-1}]$	$[Jy^2 \ sr^{-1}]$
250	300	8.2×10^3	9983	9485	600	<7063	11033	10455
350	300	5.8×10^{3}	5631	5122	600	4571	5929	5386
500	300	2.3×10^{3}	2193	1745	600	1518	2262	1799

Notes. Values for the shot noise are given in the photometric convention $\nu I_{\nu} = \text{cst}$, obtained using either the point source or the extended emission RSRF (see text for more details). Flux limits are coming from CIB power spectra analyses and are much higher than SPIRE sensitivity. ⁽¹⁾From Viero et al. (2013). ⁽²⁾From Serra et al. (2016).

Table 5. Observed and predicted Planck/HFI shot-noise levels.

Frequency [GHz]	Flux limit ⁽¹⁾ [mJy]	Measured $^{(1)}$ [Jy ² sr ⁻¹]	Predicted [Jy ² sr ⁻¹]	Flux limit ⁽²⁾ [mJy]	Measured $^{(2)}$ [Jy ² sr ⁻¹]	Predicted [Jy ² sr ⁻¹]
857	710	4966	5594	1000	5929	5761
545	350	1859	1664	600	1539	1700
353	315	315	275	400	226	277
217	225	23	21	_	_	_

Notes. Values for the shot noise are given in the photometric convention $\nu I_{\nu} = \text{cst.}^{(1)}$ From Planck Collaboration XXX (2014), shot noise from their Table 9, corrected to $\nu I_{\nu} = \text{constant}$ and corrected from the calibration difference between PR1 and PR2 data releases (at 545 and 857 GHz). At 217 GHz, the contribution from radio sources has also been removed. ⁽²⁾From Mak et al. (2017).

4. Polarised shot noise from point sources: formalism

We explain below why we expect a polarisation term if galaxies have random orientations. We define the complex linear polarisation of a source with flux *S*,

$$P_s = S \prod \exp(2i\psi),\tag{4}$$

where Π is the fractional polarisation, and ψ is the polarisation angle.

If the polarisation angles of different sources are uncorrelated, then

$$\langle P_s \rangle = 0, \tag{5}$$

but the variance is non-zero (de Zotti et al. 1999),

$$\sigma_P^2 = \frac{1}{\pi} \int_0^{\pi} |P_s - \langle P_s \rangle|^2 d\psi = S^2 \Pi^2.$$
 (6)

We derive the shot-noise fluctuations of polarised point sources following Tucci et al. (2004). For Poisson-distributed sources, the temperature power spectrum follows

$$C_{\ell}^{TT} = \int_0^{S_{\text{limit}}} S^2 \frac{\mathrm{d}N}{\mathrm{d}S} \mathrm{d}S \;. \tag{7}$$

We can consider a similar expression for the polarisation power spectrum,

$$C_{\ell}^{P} = \int_{0}^{P_{\text{limit}}} P^{2} \frac{\mathrm{d}N}{\mathrm{d}P} \mathrm{d}P, \qquad (8)$$

where $P = \sqrt{Q^2 + U^2}$ and $C_{\ell}^P = C_{\ell}^Q + C_{\ell}^U = C_{\ell}^{EE} + C_{\ell}^{BB}$.

Because the emission will contribute equally to EE and BB on average, we can consider

$$C_{\ell}^{EE} = C_{\ell}^{BB} = \frac{1}{2}C_{\ell}^{P}.$$
(9)

The power spectrum due to sources with a given fractional polarisation is

$$C_{\ell}^{P}(\Pi) = \int_{0}^{\Pi S_{\rm lim}} P^{2} \frac{\mathrm{d}N}{\mathrm{d}P} \mathrm{d}P = \Pi^{2} \int_{0}^{S_{\rm lim}} S^{2} \frac{\mathrm{d}N}{\mathrm{d}S} \mathrm{d}S , \qquad (10)$$

assuming that Π does not vary with S. When the distribution of fractional polarisation for all sources is considered, the power spectrum becomes

$$C_{\ell}^{P} = \int_{0}^{1} \mathcal{P}(\Pi) C_{\ell}^{P}(\Pi) d\Pi = \langle \Pi^{2} \rangle C_{l}^{TT} , \qquad (11)$$

where is $\mathcal{P}(\Pi)$ is the probability density function of fractional polarisation.

This formulation is very convenient, as C_{ℓ}^{P} is defined as a function of a flux cut derived in total intensity. Thus it assumes that sources are masked from polarisation maps using total intensity data. This is the case with current CMB experiments and will probably also be most likely the case with future CMB data with the use of higher angular resolution and sensitivity surveys to remove the source contamination. With this formulation, we can also consider different source populations with different fractional polarisations.

The probability density function can be constrained from the observed distributions of fractional polarisations. However, because of the lack of constraints at CMB frequencies (\sim 90– 200 GHz) for radio and dusty galaxies, we considered a fix polarisation fraction for each population (see Sect. 7).

5. Clustering of dusty star-forming galaxies

To compute polarisation power spectra due to the clustering of CIB galaxies, we used the halo model, which provides a phenomenological description of the galaxy clustering at all relevant angular scales (Cooray & Sheth 2002). Assuming that all

galaxies are located in virialised dark matter halos, the CIB clustering power spectrum is expressed as the sum of two components: a one-halo term, accounting for correlations between galaxies in the same halo, and a two-halo term, due to correlations between galaxies belonging to separated dark matter halos. The first term, together with the shot-noise power spectrum, dominates the small-scale clustering, and the second is prominent at large angular scales. Thus, the total CIB angular power spectrum at frequencies ν and ν' can be written as

$$C_{\text{tot}}^{\nu\nu'}(l) \equiv C_{\text{clust}}^{\nu\nu'}(l) + C_{\text{SN}}^{\nu\nu'} = C_{1h}^{\nu\nu'}(l) + C_{2h}^{\nu\nu'}(l) + C_{\text{SN}}^{\nu\nu'}.$$
 (12)

In the following section, after briefly introducing the model and its main parameters (we refer to Shang et al. 2012; Viero et al. 2013; Planck Collaboration XXX 2014 for a detailed discussion), we show that the amplitudes of CIB polarisation power spectra are a small fraction of the one-halo term of the clustering spectra at most, and we derive upper limits on these amplitudes by fitting the model to current measurements of CIB angular power spectra from *Herschel*/SPIRE (Viero et al. 2013).

5.1. Halo model with luminosity dependence

In the Limber approximation (Limber 1954), the CIB clustering power spectrum at frequencies ν and ν' is

$$C_{\text{clust}}^{\nu\nu'}(l) = \int \frac{\mathrm{d}z}{\chi^2} \frac{\mathrm{d}\chi}{\mathrm{d}z} a^2(z) \bar{j}(\nu, z) \bar{j}(\nu', z) P^{\nu\nu'}(k = l/\chi, z), \tag{13}$$

where the term $\chi(z)$ denotes the comoving distance at redshift z, and a(z) is the scale factor. The total emissivity from all CIB galaxies $\overline{j}_{\nu}(z)$ is computed from the luminosity function dn/dL as

$$\bar{j}_{\nu}(z) = \int dL \frac{dn}{dL} (L, z) \frac{L_{(1+z)\nu}}{4\pi},$$
(14)

where the galaxy luminosity $L_{\nu(1+z)}$ is linked to the observed flux S_{ν} as

$$L_{\nu(1+z)} = \frac{4\pi\chi^2(z)S_{\nu}}{(1+z)} \,. \tag{15}$$

Finally, the term $P^{\nu\nu'}(k, z)$ is the 3D power spectrum of the emission coefficient, expressed as

$$\langle \delta j(\boldsymbol{k}, \boldsymbol{\nu}) \delta j(\boldsymbol{k}', \boldsymbol{\nu}') \rangle = (2\pi)^3 \bar{j}_{\boldsymbol{\nu}} \bar{j}_{\boldsymbol{\nu}'} P_j^{\boldsymbol{\nu}\boldsymbol{\nu}'} \delta^3(\boldsymbol{k} - \boldsymbol{k}').$$
(16)

This term includes the two-halo and one-halo term. Expressing the luminosity of central and satellite galaxies as $L_{\text{cen},\nu(1+z)}(M_{\text{H}}, z)$ and $L_{\text{sat},\nu(1+z)}(m_{\text{SH}}, z)$ (where M_{H} and m_{SH} denote the halo and sub-halo masses, respectively), Eq. (14) can be written as the sum of the contributions from central and satellite galaxies as

$$\bar{j}_{\nu}(z) = \int dM \frac{dN}{dM}(z) \frac{1}{4\pi} \Big\{ N_{\text{cen}} L_{\text{cen},(1+z)\nu}(M_{\text{H}}, z) + \int dm_{\text{SH}} \frac{dn}{dm} (m_{\text{SH}}, z) L_{\text{sat},(1+z)\nu}(m_{\text{SH}}, z) \Big\}.$$
(17)

Here dN/dm and dn/dm denote the halo and sub-halo mass function from Tinker et al. (2008) and Tinker et al. (2010), respectively, and N_{cen} is the number of central galaxies inside a halo, which was assumed to be equal to zero if the mass of the host halo is lower than $M_{min} = 10^{11} M_{\odot}$ (Shang et al. 2012) and one otherwise.

Introducing f_{ν}^{cen} and f_{ν}^{sat} as the number of central and satellite galaxies weighted by their luminosity as

$$f_{\nu}^{\text{cen}}(M,z) = N_{\text{cen}} \frac{L_{\text{cen},(1+z)\nu}(M_{\text{H}},z)}{4\pi},$$
 (18)

$$f_{\nu}^{\text{sat}}(M, z) = \int_{M_{\min}}^{M} dm \frac{dn}{dm} (m_{\text{SH}}, z | M) \\ \times \frac{L_{\text{sat}, (1+z)\nu}(m_{\text{SH}}, z)}{4\pi},$$
(19)

the 3D CIB power spectrum at the observed frequencies v, v' in Eq. (16) can be expressed as the sum of one-halo term and two-halo term as

$$P_{1h,\nu\nu'}(k,z) = \frac{1}{\bar{j}_{\nu}\bar{j}_{\nu'}} \int_{M_{\min}}^{\infty} dM \frac{dN}{dM}$$
(20)
 $\times \left\{ f_{\nu}^{cen}(M,z) f_{\nu'}^{sat}(M,z) u(k,M,z) + f_{\nu'}^{cen}(M,z) f_{\nu'}^{sat}(M,z) u(k,M,z) + f_{\nu'}^{sat}(M,z) f_{\nu'}^{sat}(M,z) u(k,M,z)^2 \right\},$
$$P_{2h,\nu\nu'}(k,z) = \frac{1}{\bar{j}_{\nu}\bar{j}_{\nu'}} D_{\nu}(k,z) D_{\nu'}(k,z) P_{\mathrm{lin}}(k,z),$$
(21)

where

$$D_{\nu}(k,z) = \int_{M_{\min}}^{\infty} dM \frac{dN}{dM} b(M,z) u(k,M,z) \\ \times \left\{ f_{\nu}^{\operatorname{cen}}(M,z) + f_{\nu}^{\operatorname{sat}}(M,z) \right\}.$$
(22)

The term u(k, M, z) is the Fourier transform of the halo density profile (Navarro et al. 1997) with a concentration parameter from Duffy et al. (2010), and b(M, z) denotes the halo bias (Tinker et al. 2010). The linear dark matter power spectrum $P_{\text{lin}}(k)$ in Eq. (21) is computed using CAMB⁶.

The parametrisation of the term $L_{(1+z)\nu}(M, z)$ is the key ingredient of the model. Following Shang et al. (2012), we assumed a simple parametric function to describe the link between galaxy luminosity and its host dark matter halo, where the dependence of the galaxy luminosity on frequency, redshift, and halo mass is factorised in three terms as

$$L_{(1+z)\nu}(M,z) = L_0 \Phi(z) \Sigma(M) \Theta[(1+z)\nu].$$
(23)

The free normalisation parameter L_0 is constrained by the data and has no physical meaning. The galaxy SED is modelled as (see Blain et al. 2003, and reference therein)

$$\Theta(\nu, z) \propto \begin{cases} \nu^{\beta} B_{\nu}(T_{\rm d}) & \nu < \nu_0; \\ \nu^{-2} & \nu \ge \nu_0; \end{cases}$$
(24)

where the Planck function B_{ν} has an emissivity index $\beta = 1.5$, (Planck Collaboration Int. XVII 2014; Serra et al. 2016). The power-law functional form at frequencies $\nu \ge \nu_0$ has previously been used in a number of similar analyses (Hall et al. 2010; Viero et al. 2013; Shang et al. 2012; Planck Collaboration XXX 2014), and it agrees better with observations than the exponential Wien tail. The free parameter T_d is the mean temperature of the dust in CIB galaxies, averaged over the considered redshift range. We assumed a redshift-dependent, global normalisation of the *L*-*M* relation of the form

$$\Phi(z) = (1+z)^{\delta}, \qquad (25)$$

and we considered a log-normal function to describe the luminosity-mass relation as

$$\Sigma(M) = M \frac{1}{(2\pi\sigma_{L/M}^2)^{0.5}} \exp\left[-\frac{(\log_{10}M - \log_{10}M_{\rm eff})^2}{2\sigma_{L/M}^2}\right].$$
 (26)

The term $\sigma_{L/M}$ (fixed to $\sigma_{L/M} = 0.5$, as in Shang et al. 2012; Viero et al. 2013; Planck Collaboration XXX 2014; Serra et al. 2016) accounts for the range of halo masses that contribute most to the IR luminosity. The parameter $M_{\rm eff}$ describes a narrow range of halo masses around $M_{\rm eff} \sim 10^{12} M_{\odot}$ associated with a peak in the star-formation efficiency that is caused by various mechanisms that suppress star formation in high and low halo masses (Benson et al. 2003; Silk 2003; Bertone et al. 2005; Croton et al. 2006; Dekel & Birnboim 2006; Béthermin et al. 2012b; Behroozi et al. 2013).

5.2. Results

We constrained the main parameters of our halo model using six measurements of CIB angular auto- and cross-power spectra at 250, 350, and 500 μ m from *Herschel*/SPIRE (Viero et al. 2013) in the multipole range 200 < l < 23 000, and assumed the extended flux limit case. To further constrain the model, we also computed the star formation rate density in the range 0 < z < 6, and we fit to the compilation of star formation rate density measurements from Madau & Dickinson (2014).

We performed a Monte Carlo Markov chain (MCMC) analysis of the parameter space using a modification of the publicly available code CosmoMC (Lewis & Bridle 2002), and varied the following set of four halo model parameters:

$$\mathscr{P} \equiv \{M_{\rm eff}, T_d, \delta, L_0\},\tag{27}$$

together with six free parameters $A_{i=1,...6}$ for the amplitudes of the shot-noise power spectra. We obtained a good fit to the data, with a total χ^2 of 104.9 for 97 degrees of freedom. Mean values and marginalised limits for all free parameters used in the fit and comparison between *Herschel*/SPIRE measurements of the CIB power spectra with our best estimates of the one-halo, two-halo, and shot-noise, are shown in Serra et al. (2016). Shot noises derived from this model are very close to those found for the Béthermin et al. (2017) simulations. This gives us confidence about the level of the one-halo term.

5.3. CIB power spectrum in polarisation

The polarisation fraction Π for a given intensity of dust emission *I* can be expressed in terms of the Stokes parameters *Q* and *U* as

$$\Pi = \frac{\sqrt{(Q^2 + U^2)}}{I},$$
(28)

where Q and U are related to the polarisation angle ψ , through

$$Q = \mathbf{I} \times \Pi \cos(2\psi) \tag{29}$$

$$U = -\mathbf{I} \times \Pi \sin(2\psi). \tag{30}$$

Polarisation power spectra can be computed with the same formalism as we used to compute the CIB intensity power spectrum by substituting the galaxy luminosity $L_{(1+z)\nu}(M, z)$ for Q and U as

$$L_{(1+z)\nu}(M,z) \to L^Q_{(1+z)\nu}(M,z) = L_{(1+z)\nu}(M,z)\Pi\cos(2\psi)$$
(Q) (31)

$$L_{(1+z)\nu}(M,z) \to L_{(1+z)\nu}^U(M,z) = L_{(1+z)\nu}(M,z)\Pi\sin(2\psi)$$
 (U). (32)

It is easy to see that if the polarisation among different sources is uncorrelated (as discussed in Sect. 1), the two-halo term cannot produce any polarisation power spectrum because computing it involves an average over the polarisation angle of all sources, which is zero.

The contribution from the one-halo term is slightly more complicated. The dark matter halos that contribute most to the CIB power spectra have a mass in the range $12.5 < Log(M_H) < 13.5$, and the typical number of satellite galaxies in this range is too small (typically fewer than 5) to average the quantities $L^Q_{(1+z)\nu}(M, z)$ and $L^U_{(1+z)\nu}(M, z)$ to zero. As a result, when the one-halo contribution is computed, it is possible that terms proportional to

$$f_{\nu}^{\text{sat}}(M,z)f_{\nu'}^{\text{sat}}(M,z)\Pi^2\cos(2\psi)^2u(k,M,z)^2 \text{ for } Q$$
 (33)

$$f_{\nu}^{\text{sat}}(M,z)f_{\nu'}^{\text{sat}}(M,z)\Pi^2 \sin(2\psi)^2 u(k,M,z)^2 \text{ for U}$$
 (34)

give a positive contribution to the polarisation power spectra. We did not consider here the terms proportional to $f^{\text{sat}} f^{\text{cen}}$ because it has been shown in simulations and observationally that the tidal field of a large central galaxy can torque its satellites such that the major axis of satellite galaxies points towards their hosts (see e.g. Fig. 8 in Pereira et al. 2008 or Fig. 6 in Joachimi et al. 2015) and we therefore do not expect any polarised signal. While accurate estimates of the amplitude of the polarisation power spectrum would require numerical simulations, we here estimate the maximum contribution from the one-halo term, and we show that it is almost negligible with respect to the contribution from the shot noise (see Sect. 7.1). The maximum amplitude of polarisation can be obtained assuming the (unphysical) case where the polarisation angle ψ of all sources is perfectly correlated and equal to zero (for Q) or $\pi/2$ (for U). Assuming $\langle \Pi^{IR} \rangle$ the mean fractional polarisation of all DSFG, it is easy to see that the maximum amplitude of the polarisation power spectra is simply $\langle \Pi^{IR} \rangle^2$ times the amplitude of the one-halo contribution to the CIB intensity power spectrum, keeping only the term proportional to $f_{\nu}^{\text{sat}}(M, z)^2$. Thus, the EE of BB CIB power spectra are computed following:

$$C_{\ell}^{EE} = C_{\ell}^{BB} = \frac{1}{2} \times P_{1h} [\propto f^{\text{sat}}(M, z)^2] \times \langle \Pi^{\text{IR}} \rangle^2.$$
(35)

Maximising the contribution of the one-halo term is supported by the evidence of strong clustering of dusty star-forming galaxy on sub-arcmin scales (Chen et al. 2016) as well as the observed abundance of proto-cluster cores on such scales (Negrello et al. 2017). Deriving the polarised CIB power spectrum by simply scaling the total (two- and one-halo) CIB power spectrum in temperature using a fractional polarisation (as done in Curto et al. 2013 or Trombetti et al. 2018) obviously overestimates its contribution.

6. Confusion noise for future polarised experiments

Using our models for radio and DSFG number counts and for the CIB anisotropies, we can now compute the confusion noise and the point-source flux limit (Sect. 6.3) for any CMB experiments, given their characteristics (Sects. 6.1 and 6.2). We describe our method and its validation in Sect. 6.3.1, and we discuss the contributions of the different components (instrument noise, radio, DSFG, CMB) to the point-source sensitivity limit in Sect. 6.3.2. Section 6.3.3 is dedicated to our predictions of confusion noise (in intensity and polarisation) for SPICA B-BOP.

Table 6. CMB space-based and balloon-borne experiments.

Experiment	Frea	FWHM	f_{clay}	σ_{i}^{P}	σ_{inst}	$\sigma_{\rm rod}$	(T IP	$\sigma_{\rm obst}$	<i>σ</i> _{cmp}	$\sigma_{\rm tot}$	Stim	S Nradio	SNIP
Liperinein	GHz	arcmin	98Ky %	μK_{CMB} .arcmin	mJy	mJy	mJy	mJy	mJy	mJy	mJy	$Jy^2 sr^{-1}$	$Jy^2 sr^{-1}$
Planck	30	32.30	100	210.00	8.21	28.18	1.53	1.56	104.20	108.30	541.40	22.75	0.07
	44	27.90	100	240.00	17.00	26.78	1.40	1.34	148.70	152.10	760.50	25.21	0.07
	70	13.10	100	300.00	23.35	8.03	0.66	0.81	61.26	66.06	330.30	9.02	0.06
	100	9.70	100	117.60	12.15	4.99	0.85	1.25	53.94	55.54	277.70	6.42	0.19
	143	7.20	100	70.20	8.63	2.96	1.68	2.21	40.35	41.46	207.30	4.04	1.29
	217	4.90	100	105.00	11.15	1.34	3.87	4.05	16.83	20.99	105.00	1.79	14.95
IDC	353	4.90	100	438.60	28.69	1.58	14.53	2.56	10.46	38.03	190.20	2.47	209.40
IDS	150	6.00	3	5.50	0.71	2.95	1.95	2.50	42.01	42.24	211.20	4.03	1.72
	220	4 40	3	9.50	0.00	0.96	3.60	3.49	12.06	13.13	65 64	1 14	16.01
	250	3.60	3	11.00	0.83	0.62	4.21	3.65	6.11	8.33	41.65	0.70	32.74
	280	4.90	3	16.00	1.51	1.21	7.90	8.85	14.94	19.17	95.87	1.47	62.41
	320	3.90	3	24.00	1.51	0.81	8.90	8.73	6.11	13.98	69.92	1.03	124.80
	360	3.20	3	41.00	1.67	0.63	9.76	8.61	2.50	13.37	66.87	0.94	223.10
PIPER	200	21.00	85	31.40	14.13	25.77	14.12	41.04	634.30	636.40	3182	36.03	10.82
	270	15.00	85	45.90	13.69	12.48	22.80	59.77	277.70	285.60	1428	16.50	55.07
	350	14.00	85	162.00	30.90	9.55	41.51	112.50	163.30	205.10	1026	11.11	210.00
CDIDED	600	14.00	85	2659.2	53.56	11.12	132.00	388.60	17.24	414.40	2072	15.08	2125
SPIDER	94	42.00	7	11.00	4.51	82.96	5.34	13.25	1/1/	1719	8593	93.16	0.39
	40	60.20	/	25.10	5.14	102.40	8.03	27.80	028.00	057.80	4780	04.84	2.41
LIEDIKD	40 50	56.80	100	21.10	3.14	193.40	6.01	6.51	1122	1133	5663	99.23	0.17
	60	49.00	100	18 20	4 05	111 40	4 96	6 34	1167	1172	5862	92.26	0.18
	68	41.60	100	11.30	2.67	75.03	3.58	5.61	973.60	976.50	4883	78.92	0.18
	78	36.90	100	9.70	2.56	58.44	3.12	5.94	893.80	895.80	4479	71.37	0.20
	89	33.00	100	8.40	2.49	48.10	3.03	6.74	817.70	819.10	4096	63.61	0.25
	100	30.20	100	5.80	1.89	42.59	3.30	8.07	771.50	772.80	3864	57.73	0.35
	119	26.30	100	4.20	1.51	36.04	4.23	11.12	689.70	690.70	3454	49.22	0.68
	140	23.70	100	4.40	1.75	31.64	5.83	15.93	652.10	653.10	3266	43.97	1.50
	166	25.50	100	4.80	2.38	35.63	10.00	30.18	909.00	910.20	4551	50.11	3.94
	195	23.20	100	5.80	2.86	30.48	14.50	43.88	792.50	794.40	3972	42.24	9.56
	235	21.30	100	5.70	2.59	25.27	22.54	69.29 59.45	000.90	000.40 225.70	3302	33.72	26.83
	280	12.90	100	8.60	1.94	7 30	32.68	70.31	128.80	154.90	774 70	8 70	172.10
	402	10.80	100	15.80	1.55	5.80	44 02	101.80	62 44	127.40	637.00	6.93	399.00
PICO	21	38.40	100	19.10	0.44	35.70	2.00	2.44	83.31	90.69	453.40	23.56	0.07
1100	25	32.00	100	13.50	0.37	24.99	1.46	1.57	71.28	75.57	377.80	18.18	0.06
	30	28.30	100	8.30	0.28	21.97	1.28	1.23	73.55	76.79	383.90	16.71	0.06
	36	23.60	100	5.90	0.24	17.68	1.07	0.94	67.08	69.38	346.90	13.83	0.05
	43	22.20	100	5.70	0.30	17.40	1.04	0.93	81.80	83.64	418.20	14.84	0.05
	52	18.40	100	4.00	0.26	13.24	0.85	0.84	76.41	77.56	387.80	12.31	0.05
	62	12.80	100	4.40	0.27	6.97	0.56	0.60	47.11	47.63	238.20	7.10	0.05
	75	10.70	100	3.50	0.25	5.35	0.55	0.67	43.47	43.80	219.00	6.01	0.06
	90	9.50	100	2.10	0.18	4.53	0.65	0.89	44.03	44.28	221.40	5.45	0.11
	108	7.90	100	1.70	0.10	3.20	0.85	1.09	30.22	28.59	181.90	4.08	0.20
	129	6.20	100	1.30	0.17	2 10	1.27	2.16	28.50	28.85	193.40	2.97	2.06
	186	4.30	100	3,50	0.32	0.91	2.15	1.98	10.83	11 26	56 29	1.08	5.97
	223	3.60	100	4.30	0.34	0.61	3.04	2.56	6.33	7.51	37.53	0.68	17.07
	268	4.20	100	2.60	0.22	0.87	5.97	5.89	9.64	12.81	64.06	1.02	48.55
	321	2.60	100	3.80	0.16	0.40	5.92	4.46	1.54	7.58	37.91	0.58	124.30
	385	2.50	100	3.30	0.09	0.45	8.90	6.86	0.89	11.28	56.41	0.79	303.80
	462	2.10	100	6.60	0.08	0.40	11.20	8.21	0.25	13.89	69.46	0.88	681.70
	555	1.50	100	46.50	0.16	0.27	11.41	7.47	0.03	13.64	68.19	0.80	1386
	666	1.30	100	164.00	0.14	0.24	13.35	8.44	0.0	15.80	78.99	0.85	2529
	799	1.10	100	816.00	0.12	0.21	14.47	8.58	0.0	16.82	84.11	0.84	4146

Notes. From left to right: Experiment name, frequency, angular resolution, sky fraction, and instrument noise (σ_{inst}^{P} , in polarisation). The standard deviations (σ) in mJy give the contributions of instrument noise, radio and dusty (IR) galaxies, CIB clustering, and CMB, to the total noise (σ_{tot}) when a point-source flux is measured (in intensity). They are corrected for the flux lost by the aperture photometry procedure. S_{lim} is the point-source flux limit (computed from σ_{tot} using Eq. (43)). SN_{radio} and SN_{IR} are the radio and dusty galaxy shot noises, respectively, corresponding to a flux cut equal to S_{lim} .

6.1. Future CMB experiments

We considered all future CMB experiments, either already selected, funded, or in advanced discussion. Their name, frequency, angular resolution, sky coverage, and instrument noise (in intensity) are given in Table 6 for balloon-borne and space-based experiments and in Table 7 for ground-based experiments. We also considered *Planck* for reference and for cross-checks of our computations. The characteristics of each experiment were extracted from: Planck Collaboration I (2020) for *Planck*; Taylor (2018) for C-BASS; López-Caniego et al. (2014) for QUIJOTE; Calabrese et al. (2014) for AdvACTPOL;

 Table 7. Same as Table 6, but for CMB ground-based experiments.

CBASS 5 45.00 100 600.00 9.23 87.02 - 6.77 7.25 88.07 40.30 7.83 NEXTBASS 7 32.40 100 213.60 0.61 23.88 - 2.19 6.77 2.49 12.460 8.33 - 9 7.250 100 22.60 0.93 16.41 12.85 18.47 7.89 7.98 0.05 11 22.50 100 18.60 1.22 13.01 1.13 8.58 7.40 7.05 1.08 0.05 12 12.00 13.00 0.22 13.20 100 34.00 0.22 4.40 0.61 0.55 5.78 6.41 31.21 0.05 21 13.80 100 33.00 0.33 2.00 2.23 1.55 4.73 3.75 2.11 0.13 3.20 2.21 1.60 0.00 1.75 1.13 3.52 0.12 1.13 0.52 1.13	Experiment	Freq. GHz	FWHM arcmin	f _{sky} %	$\sigma^P_{ m inst}$ $\mu { m K}_{CMB}. { m arcmin}$	σ_{inst} mJy	$\sigma_{\it rad} \ { m mJy}$	σ_{IR} mJy	$\sigma_{ m clust}$ mJy	$\sigma_{ m CMB}$ mJy	$\sigma_{ m tot}$ mJy	S _{lim} mJy	$\frac{SN_{ m radio}}{ m Jy^2~sr^{-1}}$	SN_{IR} Jy ² sr ⁻¹
NEXT-BASS 7 32.40 100 228.00 0.56 29.44 - 27.0 100 27.60 100 226.00 0.61 23.84 - 2.19 6.71 24.91 11.40 18.33 - 11.0 27.60 100 226.00 0.61 226.01 18.01 6.71 24.91 17.20 12.55 0.71 14.1 17.20 12.65 0.77 13.1 12.80 10.01 13.60 12.81 13.71 12.85 18.47 92.37 10.83 1.12 10.83 12.71 12.85 18.47 90.72 12.81 13.81 13.81 13.48 14.80 10.01 13.81 13.83 14.71 13.81	C-BASS	5	45.00	100	6000.00	9.32	87.02	_	6.67	7.25	88.07	440.30	78.80	_
8 3000 100 21.50 0.61 23.88 - 21.9 6.71 24.91 12.460 13.5 - 10 27.60 100 204.00 0.79 18.83 1.39 1.71 8.00 20.91 12.85 0.72 1.65 0.73 1.61 1.35 8.17 1.80 1.02 1.03 1.31 8.85 18.74 7.80 0.90 0.05 11 22.80 100 18.60 0.22 1.30 1.31 8.58 7.40 7.40 2.40 0.03 0.20 1.51 0.30 0.26 3.15 0.42 6.44 0.41 0.55 5.29 8.28 1.43 0.32 0.22 0.15 0.42 1.46 0.33 0.20 0.23 0.25 5.51 1.10 5.50 1.32 0.12 0.13 0.22 0.23 0.12 1.10 5.510 1.10 5.510 1.10 5.510 1.10 5.510 1.10 5.5	NEXT-BASS	7	32.40	100	228.00	0.56	29.54	-	2.70	6.57	30.39	151.90	24.84	-
9 2/6.0 100 204.0 0.09 20.30 - 180 0.93 1.44 10/20 1.25 0.00 11 25.20 100 195.60 0.03 16.24 1.24 1.25 1.20 1.02 1.17 1.21 1.18 1.25 1.60 1.61 1.17 1.02 1.02 1.23 8.13 8.17 0.02 1.23 8.13 8.13 8.13 8.13 0.13 1.23 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00 0.22 4.90 0.41 0.40 4.26 6.43 3.70 2.84 0.00 20 1.13 0.10 0.30 0.22 4.90 0.30 0.25 5.75 6.44 3.33 2.22 0.00 0.02 0.11 1.01 5.50 6.41 3.42 1.10 0.10 1.10 5.50 6.41 3.42 1.21 0.01 1.01 0.10 1.01 0.11		8	30.00	100	213.60	0.61	23.88	-	2.19	6.71	24.91	124.60	18.33	-
110 21.50 100 100 100 100 100 100 100 100 100 100 100 100 100 110 </td <td></td> <td>9</td> <td>27.60</td> <td>100</td> <td>204.60</td> <td>0.69</td> <td>20.20</td> <td>- 1.20</td> <td>1.80</td> <td>6.93 8.00</td> <td>21.44</td> <td>107.20</td> <td>14.55</td> <td>0.07</td>		9	27.60	100	204.60	0.69	20.20	- 1.20	1.80	6.93 8.00	21.44	107.20	14.55	0.07
13 22.80 100 186.60 1.02 1.307 1.63 1.13 8.88 15.74 76.09 1.03 14 22.80 100 43.80 0.24 6.44 6.61 0.56 5.27 3.86 1.87 0.05 0.07 2.9 0.03 0.00 1.00 1.00 1.00 1.00 1.00 1.00 0.02 1.00 1.00 0.02 1.00 1.00 0.02 1.00 1.00 0.02 1.00 1.00 0.02 0.02 0.23 0.02 1.05 3.07 0.57 5.46 3.20 0.00 0.30 0.25 3.07 5.61 11.00 5.50 0.12 0.07 5.10 11.00 5.50 0.12 0.01 1.1 5.50 0.10 0.02 1.01 1.02 0.01 1.1 1.1 1.1 1.1 1.1 0.02 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1		10	27.60	100	204.60	0.79	16.85	1.39	1.71	8.00	20.39	92 37	12.03	0.07
14 22.80 100 196.20 1.36 13.17 102 109 10.20 17.3 8.12 0.05 15 15.60 100 38.40 0.24 4.90 4.70 0.40 4.62 6.54 37.00 2.84 0.03 20 13.20 100 39.00 0.25 4.44 4.54 6.55 75.75 6.64 3.22 2.02 0.02 25 10.80 100 30.00 0.38 0.23 0.25 5.75 6.64 3.22 0.12 28 8.40 100 30.00 3.26 9.23 1.73 2.56 6.12 5.50 1.1 1.35 0.12 1.174 2.15.0 6.10 1.11.0 5.55 0.67 3.23 1.13 1.56 1.13 1.35 1.14 2.39 1.23 1.13 1.35 1.13 1.35 1.14 1.39 1.14 1.39 1.14 1.39 1.14 1.39 1.14		13	22.80	100	186.60	1.02	13.07	1.03	1.13	8.58	15.74	78.69	7.99	0.05
15 15.60 100 43.80 0.24 6.44 0.61 0.56 5.29 8.38 8.18 9.40 0.00 420 0.83 0.81 7.40 7.00 0.84 0.00 20 10.80 100 34.00 0.25 4.54 6.456 5.7 7.85 0.00 0.02 28 8.00 16 300.00 2.76 9.54 5.07 5.10 11.0 55.00 10.2 QUIOTE 11 55.20 16 300.00 4.28 1.73 2.76 1.81 1.10 1.12 0.17 30 2.20 16 500.00 4.24 1.35 1.01 1.12 1.01 0.22 1.01 1.13 1.12 1.13 30 2.00 50 1.50 0.02 1.44 2.30 0.30 1.01<		14	22.80	100	196.20	1.36	13.17	1.02	1.09	10.92	17.23	86.13	8.12	0.05
17 13.20 100 38.40 0.22 4.59 0.47 0.40 6.26 6.54 2.70 2.89 0.00 22 10.80 100 3.700 0.26 3.15 0.34 0.25 5.75 6.74 3.22 0.20 0.23 3.25 5.75 6.44 3.22 0.22 0.23 0.15 3.87 4.38 2.11 0.10 5.55 2.72 0.62 0.11 5.55 2.12 0.00 1.61 5.56 0.70 5.51 1.41 5.50 1.6 0.000 3.86 9.40 4.90 6.55 6.75 4.73 9.10 0.00 0.00 1.41 1.42 9.55 0.67 0.53 2.22 1.61 6.000 1.61 1.42 9.43 0.43 0.42 0.00 1.01 0.00 1.00 0.22 0.15 0.12 0.13 0.15 0.13 0.45 2.20 1.60 0.22 0.15 0.12 0.13 0.1		15	15.60	100	43.80	0.24	6.44	0.61	0.56	5.29	8.38	41.89	4.06	0.04
20 13.20 100 34.20 0.25 4.54 0.45 0.38 8.81 7.40 37.00 2.24 0.00 25 10.80 100 37.80 0.26 3.15 0.34 0.25 5.75 6.44 3.23 2.22 0.02 28 8.40 100 35.00 0.33 0.22 0.23 0.55 0.64 3.32 0.27 9.04 5.09 1.10 0.55.00 4.53 0.17 0.11 1.05 0.04 0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.02 0.01 1.01 0.02 0.01 1.01 0.02 0.01 0.01 0.01 0.01 0.01 0.01 0.01 0.01 0.01 0.02 0.03 0.05 0.03 0.05 0.04 1.1 0.53 0.01 0.02 0.03 0.05 0.04 0.02 0.02 0.02 0.03 0.05 </td <td></td> <td>17</td> <td>13.20</td> <td>100</td> <td>38.40</td> <td>0.22</td> <td>4.59</td> <td>0.47</td> <td>0.40</td> <td>4.62</td> <td>6.54</td> <td>32.70</td> <td>2.89</td> <td>0.03</td>		17	13.20	100	38.40	0.22	4.59	0.47	0.40	4.62	6.54	32.70	2.89	0.03
22 10.80 100 39.00 0.29 3.15 0.34 0.25 5.75 27.85 2.05 0.02 28 8.40 100 36.00 0.73 2.02 0.25 5.75 6.44 3.23 2.22 0.15 3.87 4.38 2.10 1.39 0.00 11 55.20 1.6 300.00 3.86 94.00 4.90 6.55 7.92 1.11.00 65.70 7.15 1.479 0.17 7.51 64.79 2.178 0.07 0.07 5.10 64.79 0.17 0.07 0.07 0.07 0.07 0.07 0.08 0.07 6.47 0.22 0.05 0.60 1.61 1.429 0.95 0.54 0.07 0.55 0.57 7.92 0.00 1.00 0.04 1.11 5.33 0.02 1.45 1.420 0.05 1.45 1.430 1.45 1.430 1.45 1.430 1.45 1.430 1.447 1.447 1.45		20	13.20	100	34.20	0.25	4.54	0.45	0.38	5.81	7.40	37.00	2.84	0.03
25 10.80 100 37.80 0.56 3.28 0.35 0.25 5.75 6.44 33.2 2.22 0.02 QUIDOTE 11 55.20 16 300.00 3.86 0.15 3.87 4.88 21.91 1.79 1.100 55.00 4.38 21.91 1.71 13 55.20 16 300.00 3.86 9.40 4.73 2.26 4.12 54.32 21.10 17.87 0.17 19 36.00 16 300.00 5.35 9.21 1.74 1.75 57.5 48.00 1.00 1.20 0.07 0.48 0.56 2.80 0.08 0.07 100 0.22 50 11.00 0.22 0.13 0.12 0.07 0.48 0.55 0.50 1.83 BICEP3+Keck[2018] 95 2.400 1 2.10 0.50 2.37 4.73 399.20 40.03 20.22 31.0 1.53 40.11 83.1		22	10.80	100	39.00	0.29	3.15	0.34	0.26	4.56	5.57	27.85	2.05	0.02
12.6 8.40 100 30.000 2.75 62.3 61.3 5.30 4.38 4.38 1.19 1.59 0.12 QUIDOTE 11 35.20 16 300.00 3.86 94.00 4.90 6.55 7.62 11.10 55.00 4.70 7.07 55.10 11.00 55.00 4.70 7.07 55.10 14.72 0.70 7.51 64.72 2.12.00 0.70 0.70 0.80 0.76 0.83 0.76 8.80 7.61 64.72 0.70 0.80 0.76 64.70 1.00 0.02 0.11 1.10 0.53 2.90 1.10 0.02 0.76 0.76 0.78 3.80 9.92 400.30 0.02 3.01 1.60 0.42 1.15 3.00 0.42 1.16 3.00 1.1 1.83 9.92 400.30 0.02 3.77 0.24 110 1.30 5.00 1.2 1.75 1.420 1.50 45.00 1.1 <td></td> <td>25</td> <td>10.80</td> <td>100</td> <td>37.80</td> <td>0.36</td> <td>3.28</td> <td>0.33</td> <td>0.25</td> <td>5.75</td> <td>6.64</td> <td>33.23</td> <td>2.22</td> <td>0.02</td>		25	10.80	100	37.80	0.36	3.28	0.33	0.25	5.75	6.64	33.23	2.22	0.02
QCDOTE 11 5.5.20 16 300.00 2.36 94.00 4.90 6.57 7.92 121.80 69.00 4.129 0.112 17 36.00 16 300.00 4.29 28.24 1.73 2.26 46.12 54.32 54.25 1.6 0.07 30 22.20 16 60.00 1.61 14.29 0.95 8.8 40.76 43.24 0.06 0.39.25 16.6.3 0.06 0.07 0.58 0.05 1.45 0.05 1.46 0.05 1.01 0.42 0.05 0.46 0.05 1.01 0.42 0.05 0.05 0.05 1.01 0.42 0.05	OLILIOTE	28	8.40 55.20	100	30.00	0.55	2.02	5.00	7.07	55.10	4.38	21.91	1.39	0.02
17 36.00 16 300.00 4.29 28.24 17.3 2.26 46.12 54.32 271.60 17.87 0.07 30 22.20 16 60.00 1.61 14.29 0.8 0.76 43.24 216.20 0.01 0.04 AdvACTPOL 90 22.0 50 11.00 0.22 0.13 0.45 2.30 0.9 30 22.0 0.06 0.32 0.15 0.13 0.45 2.33 0.08 0.07 200 50 35.40 0.69 0.66 0.79 0.36 0.41 11 5.3 0.08 0.07 0.36 0.41 11 5.3 0.08 0.17 1.45 44.33 8.65 2.40 1.11 1.48 8.32 0.15 0.11 1.43 8.42 1.11 5.33 0.020 3.70 0.24 1.41 1.43 1.43 1.51 1.77 0.29 0.03 0.020 3.70 0.24 1.41 <td>QUIUIE</td> <td>13</td> <td>55.20</td> <td>16</td> <td>300.00</td> <td>3.86</td> <td>93.94</td> <td>4 90</td> <td>6 55</td> <td>76.92</td> <td>121.80</td> <td>609.00</td> <td>43.52</td> <td>0.12</td>	QUIUIE	13	55.20	16	300.00	3.86	93.94	4 90	6 55	76.92	121.80	609.00	43.52	0.12
19 66.00 16 300.00 5.35 92.1 1.74 2.17 57.51 64.79 32.390 19.12 0.07 40 16.80 16 60.00 1.61 14.29 0.57 3.80 39.25 19.63 7.68 0.04 AdvACTPOL 90 2.20 50 1.100 0.22 0.13 0.12 0.07 0.48 0.56 2.80 0.08 0.07 150 1.30 50 9.80 0.23 0.06 0.79 0.36 0.04 1.11 5.30 0.11 1.839 BICEP3+Keck[2018] 95 24.00 1 2.10 0.52 1.83 1.20 0.002 3.07 0.24 95 24.00 1 1.00 0.24 1.83 9.50 29.02 2.010 1.44 150 15.00 1 1.00 0.24 2.95 2.95 2.95 2.95 2.95 2.95 2.95 2.95 2.95 <td></td> <td>17</td> <td>36.00</td> <td>16</td> <td>300.00</td> <td>4.29</td> <td>28.24</td> <td>1.73</td> <td>2.26</td> <td>46.12</td> <td>54.32</td> <td>271.60</td> <td>17.87</td> <td>0.07</td>		17	36.00	16	300.00	4.29	28.24	1.73	2.26	46.12	54.32	271.60	17.87	0.07
30 22.20 16 60.00 1.61 1.42 9.05 0.57 0		19	36.00	16	300.00	5.35	29.21	1.74	2.17	57.51	64.79	323.90	19.12	0.07
Ho 16 60.00 2.14 9.55 0.67 38.00 32.55 19.50 7.68 0.04 AdvACTPOL 90 2.20 50 9.80 0.22 0.13 0.48 0.55 2.80 0.08 0.07 150 1.30 0.90 50 35.40 0.69 0.06 0.79 0.36 0.04 1.1 5.33 0.02 37.70 0.24 BICEP3+Keck[2018] 95 24.00 1 2.10 0.52 182.30 7.56 5.45 5.50 75.00 85.00 87.90 83.02 0.00 83.92 0.01 1.44 1.00 0.24 85.5 2.786 1.25 0.50 0.70 0.24 1.51 1.50 1.10 0.24 1.37 1.32 2.41 8.41 41.49 1.50 1.49 0.10 1.34 3.56 1.51 3.40 1.50 1.49 0.10 1.34 3.56 1.51 1.41 9.50 2.24		30	22.20	16	60.00	1.61	14.29	0.95	0.85	40.76	43.24	216.20	10.01	0.04
AdvACTPOL 90 2.20 50 11.00 0.22 0.13 0.12 0.07 0.48 0.52 2.00 0.80 0.07 IS0 0.90 50 35.40 0.69 0.06 0.79 0.36 0.04 1.11 5.53 0.11 18.39 BICEP3+Keck[2018] 95 24.00 1 2.70 1.45 44.93 Ke5 27.86 1.64 2.40 37.70 0.24 40 57.00 1 6.60 0.52 182.30 7.65 6.94 55.04 7.99.09 2000 83.92 0.15 410 55.00 1 1.00 0.24 2.95 5.36 5.73.93 7.95.09 7.90.0 83.01 1.94 220 11.00 1.44 4.00 1.05 7.31 9.27 1.84.1 44.03 75.20 7.86 88.06 0.15 1.44 4.40 7.99 1.46 2.40.1 7.91 1.44 7.40.3 7.72.0		40	16.80	16	60.00	2.14	9.55	0.67	0.57	38.00	39.25	196.30	7.68	0.04
150 1.30 50 9.80 0.23 0.06 0.32 0.15 0.13 0.145 2.23 0.05 1.48 BICEP3+Keck[2018] 95 24.00 1 2.10 0.50 29.58 2.37 4.97 399.20 0.03 2002 37.70 0.24 BICEPArray[2023] 30 76.00 1 5.60 0.52 182.30 7.65 6.54 550.40 579.30 2002 37.70 0.24 150 15.00 1 1.00 0.24 29.58 2.37 4.97 399.20 400.30 2020 37.70 0.24 150 15.00 1 1.00 0.24 29.58 2.37 4.97 19.92 12.40 12.40 5.99 5.29 CLASS 38 90.00 70 39.00 6.72 18.36 6.40 74.00 78.86 88.06 0.15 148 24.00 70 15.00 6.5.1 6.16 6.44 </td <td>AdvACTPOL</td> <td>90</td> <td>2.20</td> <td>50</td> <td>11.00</td> <td>0.22</td> <td>0.13</td> <td>0.12</td> <td>0.07</td> <td>0.48</td> <td>0.56</td> <td>2.80</td> <td>0.08</td> <td>0.07</td>	AdvACTPOL	90	2.20	50	11.00	0.22	0.13	0.12	0.07	0.48	0.56	2.80	0.08	0.07
Dices 240 0.50 25.40 1 2.10 0.50 25.8 2.37 4.97 399.20 200.20 37.70 0.24 BICEP3+Keck[2023] 30 76.00 1 5.60 0.52 182.30 7.65 6.94 550.40 579.90 2900 83.92 0.15 40 57.00 1 6.20 0.52 182.30 7.65 6.94 550.40 579.90 2900 83.92 0.15 4150 15.00 1 1.00 0.24 2.95.8 2.37 4.97 599.20 24.90 1.04 1.94 1.14 1.96.0 1.14 1.90 1.24 2.01 1.94 1.94 1.90 1.92 2.92 1.14 1.94.00 1.90 1.33 2.41.0 1.84.0 1.84.01 88.01 4.80 1.85 4.26.0 5.99 5.29.2 CLASS 38 90.00 70 15.00 6.34 3.21 1.81.9 7.83.0 85.0		150	1.30	50	9.80	0.23	0.06	0.32	0.15	0.13	0.45	2.23	0.05	1.46
BIC EP3 + RCCR[2015] 99 24.00 1 2.10 0.30 2.93.5 2.3.1 4.97 399.2 0.00.3 2.00.2 37.10 0.44 2.41 BIC EPArray[2023] 30 76.00 1 5.60 0.52 182.30 7.65 6.94 550.40 579.90 2900 8.3.92 0.15 95 24.00 1 1.00 0.24 29.58 2.37 4.97 399.20 400.30 2002 37.70 0.24 150 15.00 1 4.00 0.28 1.377 4.28 9.56 249.30 1249 20.10 1.706 270 9.00 1 6.60 1.18 4.50 13.36 2.401 84.01 84.51 442.60 599 52.92 5.64 13.02 7.759.00 16.1 7.759.00 16.1 7.759.00 16.6 15.10 1.44 45.51 7.46.9 7.759.00 16.6 16.72 15.80 1.49 45.51 9.220 <td>DICED2 . K . 1 [2010]</td> <td>230</td> <td>0.90</td> <td>50</td> <td>35.40</td> <td>0.69</td> <td>0.06</td> <td>0.79</td> <td>0.36</td> <td>0.04</td> <td>1.11</td> <td>5.53</td> <td>0.11</td> <td>18.39</td>	DICED2 . K . 1 [2010]	230	0.90	50	35.40	0.69	0.06	0.79	0.36	0.04	1.11	5.53	0.11	18.39
BICEPArray[2023] 30 76.00 1 5.00 17.30 17.40 17.40 17.40 17.40 17.40 17.40 17.40 17.40 17.40 17.40 17.41 17.40 17.40 17.41 17.40 17.40 17.41 17.40 17.41 17.40 17.41 17.40 17.41 17.40 17.41 17.40 17.41 17.41 17.41 17.41	BICEP3+Keck[2018]	95 150	24.00	1	2.10	0.50	29.58 44.93	2.37	4.97	399.20 1261	400.30	2002 6311	57.70 64.84	0.24
And Find Find Find	BICEPArray[2023]	30	76.00	1	5.60	0.52	182 30	7.65	6.94	550.40	579.90	2900	83.92	0.15
95 24.00 1 1.00 0.24 29.58 2.37 4.97 399.20 400.30 2002 37.70 0.24 150 15.00 1 4.40 0.28 13.77 4.28 9.56 243.90 124.9 20.10 1.94 270 9.00 1 6.60 1.18 4.50 13.36 24.01 84.11 49.50 15.12 755.90 10.66 1.18 4.50 13.36 24.01 84.11 47.60 757.20 378.6 86.06 0.15 148 24.00 70 15.00 6.34 32.51 6.89 19.31 711.40 71.20 350.2 2.84 372.30 396.60 18.33 61.30 0.13 39 63.00 10 37.70 1.25 2.88 4.77 75.70 67.70 37.01 31.64 5.92 5.84 37.20 31.80 1593 25.17 1.64 225 11.00 10 3.70	DieErinay[2025]	40	57.00	1	6.20	0.75	142.60	5.96	5.56	739.50	753.20	3766	86.13	0.15
150 15.00 1 1.00 0.28 13.77 4.28 9.56 249.90 1249 20.10 1.94 200 11.00 1 4.40 1.165 7.31 9.27 18.41 149.00 18.51 432.60 5.99 52.92 CLASS 38 90.00 70 39.00 6.72 158.70 6.61 6.04 74.03 75.20 378.6 88.60 0.15 144 24.00 70 15.00 6.34 32.51 6.89 19.31 711.40 712.40 356.2 45.53 2.04 217 18.00 70 43.00 16.77 19.05 14.12 6.39 817.60 835.40 4177 9.30 0.16 39 63.00 10 2.70 3.77 17.49 4.47 16.63 817.90 838.60 93.32 5.11 14.64 13.86 1593 25.17 6.49 30 0.00 10 2.2.60		95	24.00	1	1.00	0.24	29.58	2.37	4.97	399.20	400.30	2002	37.70	0.24
220 11.00 1 4.40 1.05 7.31 9.27 18.41 149.60 151.20 755.90 10.61 17.06 CLASS 38 90.00 70 39.00 6.72 158.70 6.61 6.04 740.30 757.20 378.6 88.00 0.15 93 40.00 70 15.00 6.34 32.51 6.89 19.31 711.40 712.40 3562 45.53 2.04 217 18.00 70 43.00 16.77 19.05 51.04 41.49 453.10 455.90 2280 26.60 16.72 SO-SAT 27 91.00 10 49.50 4.31 136.50 5.92 5.84 717 93.01 0.16 93 30.00 10 2.707 3.71 17.14 71.40 71.70 318.60 1593 25.17 1.64 225 11.00 10 8.90 1.27 7.79 89 19.74 149.30 <td></td> <td>150</td> <td>15.00</td> <td>1</td> <td>1.00</td> <td>0.28</td> <td>13.77</td> <td>4.28</td> <td>9.56</td> <td>249.30</td> <td>249.90</td> <td>1249</td> <td>20.10</td> <td>1.94</td>		150	15.00	1	1.00	0.28	13.77	4.28	9.56	249.30	249.90	1249	20.10	1.94
270 9.00 1 6.60 1.18 4.50 13.26 24.01 88.01 88.01 88.05 61.15 93 40.00 70 10.00 3.83 73.16 4.68 11.50 1479 1481 7406 86.26 0.35 148 24.00 70 15.00 6.34 32.51 6.89 19.31 711.40 71.24 0.352 2.62.0 2.60.0 16.72 SO-SAT 27 91.00 10 49.50 4.43 136.50 5.92 5.84 372.30 39.660 1983 68.13 0.13 39 63.00 10 3.70 1.05 41.25 2.88 6.47 67.70 33.86 0.27 145 17.00 10 4.70 1.37 17.49 4.47 10.63 31.790 31.8.0 15.93 0.44 19.40 250 9.00 10 2.20 3.00 15.02 0.97 0.02		220	11.00	1	4.40	1.05	7.31	9.27	18.41	149.60	151.20	755.90	10.61	17.06
CLASS 38 90.00 70 39.00 6.72 158.70 6.61 6.04 740.30 757.20 378.6 88.06 0.15 93 40.00 70 10.00 38.33 73.16 6.89 11.50 1479 1481 7406 85.29 23.0 26.60 16.72 SO-SAT 27 91.00 10 49.50 44.31 136.50 5.92 884 372.30 396.60 198.3 68.13 0.13 39 63.00 10 29.70 3.77 171.40 71.2 6.39 817.60 835.40 417.79 30.10 16.6 225 11.00 10 8.70 2.17 1.64 25.58 10.49 19.40 280 9.00 10 2.260 3.92 4.41 14.70 2.68 81.25 87.02 435.10 5.77 64.59 SO-LAT 27 7.40 40 10.40 0.73 1.49 0.10		270	9.00	1	6.60	1.18	4.50	13.36	24.01	84.01	88.51	442.60	5.99	52.92
95 40.00 70 15.00 6.3.8 7.16 4.68 11.20 14.49 74.06 80.29 0.5.5 217 18.00 70 43.00 16.77 19.05 15.10 41.49 453.10 455.90 2280 26.60 16.72 SO-SAT 27 91.00 10 49.50 4.43 136.50 5.92 5.84 372.30 396.60 1983 68.13 0.13 93 30.00 10 3.70 1.05 41.25 2.88 6.47 675.70 675.00 3385 54.66 0.27 145 17.00 10 4.70 1.37 17.49 4.47 162.80 81.25 87.02 35.10 40.9 19.04 225 11.00 10 8.90 2.12 7.27 9.89 19.74 149.30 15.10 7.58.0 10.49 19.40 280 9.00 10 2.26 3.00 15.02 0.97 0.02 <td>CLASS</td> <td>38</td> <td>90.00</td> <td>70</td> <td>39.00</td> <td>6.72</td> <td>158.70</td> <td>6.61</td> <td>6.04</td> <td>740.30</td> <td>757.20</td> <td>3786</td> <td>88.06</td> <td>0.15</td>	CLASS	38	90.00	70	39.00	6.72	158.70	6.61	6.04	740.30	757.20	3786	88.06	0.15
143 24,00 70 43,00 16,77 19,05 15,10 41,49 43,10 16,240 35,02 42,33 22,80 26,60 16,72 SO-SAT 27 91,00 10 49,50 4,43 136,50 5.92 5,84 372,30 396,60 1983 68,13 0,13 39 63,00 10 27,07 17,140 7,12 6,38 817,60 835,40 4177 93,01 0,16 93 30,00 10 4,70 1,37 17,49 4,47 10,63 317,90 318,60 1593 25,17 1,64 225 11,00 10 8,90 2,12 7,27 9,88 16,74 149,30 15,120 75,80 10,49 19,40 280 9,00 10 22,60 3,92 4,41 14,76 26,80 81,22 75,80 10,49 19,40 39 5,10 40 50,90 0,52 0,74 0,11<		93	40.00	70	10.00	5.85	/3.16	4.68	11.50	14/9	1481	7406	86.29 45.52	0.35
SO-SAT 27 91.00 10 49.50 4.43 136.5 5.92 5.84 372.30 396.60 1983 68.13 0.13 39 63.00 10 29.70 3.77 171.40 7.12 6.39 817.60 835.40 4177 93.01 0.16 93 30.00 10 3.70 1.05 41.25 2.88 64.7 675.70 677.00 3385 54.66 0.27 145 17.00 10 8.90 2.12 7.27 9.89 19.74 149.30 151.20 755.80 10.49 19.40 280 9.00 10 22.60 3.92 4.41 14.76 26.80 81.25 87.02 435.10 5.77 64.59 SO-LAT 27 7.40 40 100.40 0.73 1.49 0.19 0.12 2.50 3.00 4.50 0.50 0.01 93 2.20 40 11.30 0.24 0.13		217	24.00 18.00	70	43.00	16 77	32.31 19.05	15 10	41 49	453.10	455.90	2280	45.55 26.60	2.04
39 63.00 10 29.70 3.77 171.40 7.12 6.39 817.60 835.40 4177 93.01 0.16 93 30.00 10 3.70 1.05 41.25 2.88 64.7 675.70 677.00 3385 54.66 0.27 145 17.00 10 4.70 1.37 17.49 4.47 10.63 317.90 318.60 15.93 25.17 1.64 280 9.00 10 22.60 3.92 4.41 14.76 2.68 81.25 87.02 435.10 5.77 64.59 SO-LAT 27 7.40 40 100.40 0.73 1.49 0.10 0.12 2.50 3.00 15.02 0.97 0.02 39 5.10 40 50.90 0.24 0.13 0.13 0.08 0.50 0.59 2.96 0.09 0.09 145 1.40 40 14.10 0.34 0.07 0.33 0.0	SO-SAT	27	91.00	10	49.50	4.43	136.50	5.92	5.84	372.30	396.60	1983	68.13	0.13
93 30.00 10 3.70 1.05 41.25 2.88 6.47 675.70 677.00 3385 54.66 0.27 145 17.00 10 4.70 1.37 17.49 4.47 10.63 317.90 318.60 1593 25.17 1.64 225 11.00 10 22.60 3.92 4.41 14.76 26.80 81.25 87.02 435.10 5.77 64.59 SO-LAT 27 7.40 40 100.40 0.73 1.49 0.19 0.12 2.50 3.00 15.02 0.97 0.02 39 5.10 40 50.90 0.52 0.74 0.11 0.07 1.50 0.75 2.96 0.09 0.09 145 1.40 40 11.30 0.24 0.13 0.08 0.55 0.59 2.96 0.09 0.09 145 1.40 40 31.10 0.67 0.07 0.83 0.38 0.66		39	63.00	10	29.70	3.77	171.40	7.12	6.39	817.60	835.40	4177	93.01	0.16
145 17.00 10 4.70 1.37 17.49 4.47 10.63 317.90 318.60 1593 25.17 1.64 225 11.00 10 8.90 2.12 7.27 9.89 19.74 149.30 151.20 755.80 10.49 19.40 280 9.00 10 22.60 3.92 4.41 14.76 26.80 81.25 87.02 435.10 5.77 64.59 SO-LAT 27 7.40 40 100.40 0.73 1.49 0.19 0.12 2.50 3.00 15.02 0.97 0.02 93 5.10 40 50.90 0.52 0.74 0.11 0.07 1.76 1.99 9.94 0.50 0.01 145 1.40 40 14.10 0.34 0.07 0.83 0.38 0.66 1.14 5.68 0.11 1.64 280 0.90 40 76.40 1.32 0.08 1.38 0.65 </td <td></td> <td>93</td> <td>30.00</td> <td>10</td> <td>3.70</td> <td>1.05</td> <td>41.25</td> <td>2.88</td> <td>6.47</td> <td>675.70</td> <td>677.00</td> <td>3385</td> <td>54.66</td> <td>0.27</td>		93	30.00	10	3.70	1.05	41.25	2.88	6.47	675.70	677.00	3385	54.66	0.27
225 11.00 10 8.90 2.12 7.27 9.89 19.74 14.9.30 151.20 755.80 10.49 19.40 280 9.00 10 22.60 3.92 4.41 14.76 26.80 81.25 87.02 435.10 5.77 64.59 SO-LAT 27 7.40 40 100.40 0.73 1.49 0.19 0.12 2.50 3.00 15.02 0.97 0.02 93 5.10 40 50.90 0.52 0.74 0.11 0.07 1.76 1.99 9.94 0.50 0.01 93 2.20 40 11.30 0.24 0.31 0.15 0.17 0.52 2.61 0.06 1.21 225 1.00 40 31.10 0.67 0.07 0.83 0.38 0.06 1.14 5.68 0.11 16.40 280 0.90 40 76.40 1.32 0.08 1.38 0.06 1.02 <td></td> <td>145</td> <td>17.00</td> <td>10</td> <td>4.70</td> <td>1.37</td> <td>17.49</td> <td>4.47</td> <td>10.63</td> <td>317.90</td> <td>318.60</td> <td>1593</td> <td>25.17</td> <td>1.64</td>		145	17.00	10	4.70	1.37	17.49	4.47	10.63	317.90	318.60	1593	25.17	1.64
280 9.00 10 22.60 3.92 4.41 14.76 26.80 81.25 87.02 435.10 5.77 64.39 SO-LAT 27 7.40 40 100.40 0.73 1.49 0.19 0.12 2.50 3.00 15.02 0.97 0.02 39 5.10 40 50.90 0.52 0.74 0.11 0.07 1.76 1.99 9.94 0.50 0.09 93 2.20 40 11.30 0.24 0.13 0.15 0.17 0.52 2.61 0.06 1.21 225 1.00 40 31.10 0.67 0.07 0.83 0.38 0.06 1.14 5.68 0.11 16.40 280 0.90 40 76.40 1.32 0.08 1.38 0.65 0.03 2.02 10.11 0.18 56.62 SPT-3G 95 1.60 6 6.00 0.13 0.06 0.13 0.09 <td< td=""><td></td><td>225</td><td>11.00</td><td>10</td><td>8.90</td><td>2.12</td><td>7.27</td><td>9.89</td><td>19.74</td><td>149.30</td><td>151.20</td><td>755.80</td><td>10.49</td><td>19.40</td></td<>		225	11.00	10	8.90	2.12	7.27	9.89	19.74	149.30	151.20	755.80	10.49	19.40
SO-LAT 27 7.40 40 100.40 0.73 1.49 0.12 2.50 3.00 15.02 0.97 0.02 39 5.10 40 50.90 0.52 0.74 0.11 0.07 1.76 1.99 9.94 0.50 0.01 93 2.20 40 11.30 0.24 0.13 0.13 0.08 0.50 0.59 2.96 0.09 0.09 145 1.40 40 14.10 0.34 0.07 0.31 0.15 0.17 0.52 2.61 0.06 1.21 225 1.00 40 31.10 0.67 0.07 0.83 0.38 0.06 1.14 5.68 0.11 16.40 280 0.90 40 76.40 1.32 0.08 1.38 0.65 0.03 2.02 10.11 0.18 56.62 SPT-3G 95 1.60 6 6.00 0.10 0.05 0.16 0.22 1.12 0.03 0.09 148 1.20 6 3.50 0.71 <	00 L 15	280	9.00	10	22.60	3.92	4.41	14.76	26.80	81.25	87.02	435.10	5.77	64.59
393 2.20 40 13.00 0.32 0.11 0.01 1.70 1.99 9.94 0.30 0.00 93 2.20 40 11.30 0.24 0.13 0.13 0.08 0.50 0.59 2.96 0.09 0.09 145 1.40 40 14.10 0.34 0.07 0.83 0.38 0.06 1.14 5.68 0.11 16.40 225 1.00 40 31.10 0.67 0.07 0.83 0.38 0.06 1.14 5.68 0.11 16.40 280 0.90 40 76.40 1.32 0.08 1.38 0.65 0.03 2.02 10.11 0.18 56.62 SPT-3G 95 1.60 6 6.00 0.10 0.06 0.10 0.05 0.16 0.22 1.12 0.03 0.09 231 1.00 40 8.40 0.05 3.18 1.03 0.05 2.27 3.77 <td>SO-LAI</td> <td>27</td> <td>7.40</td> <td>40</td> <td>100.40</td> <td>0.73</td> <td>1.49</td> <td>0.19</td> <td>0.12</td> <td>2.50</td> <td>3.00</td> <td>15.02</td> <td>0.97</td> <td>0.02</td>	SO-LAI	27	7.40	40	100.40	0.73	1.49	0.19	0.12	2.50	3.00	15.02	0.97	0.02
145 1.40 40 11.10 0.21 0.13 0.15 0.16 0.22 1.11 0.18 56.62 SPT-3G 95 1.60 6 0.00 0.10 0.06 0.10 0.05 1.30 0.16 0.22 </td <td></td> <td>93</td> <td>2 20</td> <td>40</td> <td>11 30</td> <td>0.32</td> <td>0.14</td> <td>0.11</td> <td>0.07</td> <td>0.50</td> <td>0.59</td> <td>2.94</td> <td>0.00</td> <td>0.01</td>		93	2 20	40	11 30	0.32	0.14	0.11	0.07	0.50	0.59	2.94	0.00	0.01
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		145	1.40	40	14.10	0.34	0.07	0.31	0.15	0.17	0.52	2.61	0.06	1.21
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		225	1.00	40	31.10	0.67	0.07	0.83	0.38	0.06	1.14	5.68	0.11	16.40
SPT-3G 95 1.60 6 6.00 0.10 0.06 0.10 0.05 0.16 0.22 1.12 0.03 0.09 148 1.20 6 3.50 0.07 0.05 0.28 0.13 0.09 0.34 1.68 0.04 1.30 223 1.00 6 6.00 0.13 0.06 0.79 0.37 0.06 0.89 4.45 0.08 15.05 CMB-S4-SAT 20 11.00 40 8.40 0.05 3.14 0.35 0.27 3.77 4.93 24.64 1.96 0.02 30 72.80 40 4.50 0.69 197.60 8.18 7.20 958.30 978.50 4892 99.25 0.17 85 25.50 40 0.90 0.19 31.25 2.10 3.94 387.70 388.90 1945 38.53 0.17 95 25.50 40 0.80 0.20 32.54 2.53		280	0.90	40	76.40	1.32	0.08	1.38	0.65	0.03	2.02	10.11	0.18	56.62
148 1.20 6 3.50 0.07 0.05 0.28 0.13 0.09 0.34 1.68 0.04 1.30 223 1.00 6 6.00 0.13 0.06 0.79 0.37 0.06 0.89 4.45 0.08 15.05 CMB-S4-SAT 20 11.00 40 8.40 0.05 3.14 0.35 0.27 3.77 4.93 24.64 1.96 0.02 30 72.80 40 3.50 0.31 181.70 7.62 6.92 548.80 578.20 2891 83.92 0.15 40 72.80 40 4.50 0.69 197.60 8.18 7.20 958.30 978.50 4892 99.25 0.17 85 25.50 40 0.90 0.19 31.25 2.10 3.94 387.70 388.90 1945 38.53 0.17 95 25.50 40 0.80 0.20 32.54 2.53 5.41	SPT-3G	95	1.60	6	6.00	0.10	0.06	0.10	0.05	0.16	0.22	1.12	0.03	0.09
223 1.00 6 6.00 0.13 0.06 0.79 0.37 0.06 0.89 4.45 0.08 15.05 CMB-S4-SAT 20 11.00 40 8.40 0.05 3.14 0.35 0.27 3.77 4.93 24.64 1.96 0.02 30 72.80 40 3.50 0.31 181.70 7.62 6.92 548.80 578.20 2891 83.92 0.15 40 72.80 40 4.50 0.69 197.60 8.18 7.20 958.30 978.50 4892 99.25 0.17 85 25.50 40 0.90 0.19 31.25 2.10 3.94 387.70 388.90 1945 38.53 0.17 95 25.50 40 0.80 0.20 32.54 2.51 16.73 613.70 614.60 3073 41.15 1.78 155 22.70 40 3.50 0.99 10.25 11.07 2		148	1.20	6	3.50	0.07	0.05	0.28	0.13	0.09	0.34	1.68	0.04	1.30
CMB-S4-SAT 20 11.00 40 8.40 0.05 3.14 0.35 0.27 3.77 4.93 24.64 1.96 0.02 30 72.80 40 3.50 0.31 181.70 7.62 6.92 548.80 578.20 2891 83.92 0.15 40 72.80 40 4.50 0.69 197.60 8.18 7.20 958.30 978.50 4892 99.25 0.17 85 25.50 40 0.90 0.19 31.25 2.10 3.94 387.70 388.90 1945 38.53 0.17 95 25.50 40 0.80 0.20 32.54 2.53 5.41 463.10 464.30 2321 41.80 0.25 145 22.70 40 1.20 0.47 29.54 6.15 16.73 613.70 614.60 3073 41.15 1.78 155 22.70 40 3.50 0.99 10.25 11.07		223	1.00	6	6.00	0.13	0.06	0.79	0.37	0.06	0.89	4.45	0.08	15.05
30 72.80 40 5.30 0.31 181.70 7.02 6.92 548.80 578.20 2891 83.92 0.15 40 72.80 40 4.50 0.69 197.60 8.18 7.20 958.30 978.50 4892 99.25 0.17 85 25.50 40 0.90 0.19 31.25 2.10 3.94 387.70 388.90 1945 38.53 0.17 95 25.50 40 0.80 0.20 32.54 2.53 5.41 463.10 464.30 2321 41.80 0.25 145 22.70 40 1.20 0.47 29.54 6.15 16.73 613.70 614.60 3073 41.15 1.78 155 22.70 40 1.30 0.54 29.76 7.41 20.64 654.00 655.00 3275 41.76 2.59 220 13.00 40 6.00 1.56 9.44 19.58 46.53 202.90 209.30 1046 12.63 54.35 7.40 <td>CMB-S4-SAT</td> <td>20</td> <td>11.00</td> <td>40</td> <td>8.40</td> <td>0.05</td> <td>3.14</td> <td>0.35</td> <td>0.27</td> <td>3.77</td> <td>4.93</td> <td>24.64</td> <td>1.96</td> <td>0.02</td>	CMB-S4-SAT	20	11.00	40	8.40	0.05	3.14	0.35	0.27	3.77	4.93	24.64	1.96	0.02
40 72.50 40 4.50 0.09 197.00 8.13 7.20 978.50 402 972.25 0.17 85 25.50 40 0.90 0.19 31.25 2.10 3.94 387.70 388.90 1945 38.53 0.17 95 25.50 40 0.80 0.20 32.54 2.53 5.41 463.10 464.30 2321 41.80 0.25 145 22.70 40 1.20 0.47 29.54 6.15 16.73 613.70 614.60 3073 41.15 1.78 155 22.70 40 1.30 0.54 29.76 7.41 20.64 654.00 655.00 3275 41.76 2.59 220 13.00 40 3.50 0.99 10.25 11.07 24.80 220.80 22.70 1113 14.88 17.36 270 13.00 40 6.00 1.56 9.44 19.58 46.53 202.90 209.30 1046 12.63 54.35 13.00 40<		30 40	72.80	40	3.30	0.51	181.70	7.02 8.18	0.92	058 30	578.20 078.50	4802	83.92 00.25	0.15
95 25.50 40 0.80 0.20 32.54 2.53 5.41 66.10 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 10.74 50.50 11.74 10.50 10.74 50.50 22.11 11.74 10.74 <td></td> <td>+0 85</td> <td>25 50</td> <td>40</td> <td>0.90</td> <td>0.19</td> <td>31 25</td> <td>2.10</td> <td>3.94</td> <td>387 70</td> <td>388.90</td> <td>1945</td> <td>38 53</td> <td>0.17</td>		+0 85	25 50	40	0.90	0.19	31 25	2.10	3.94	387 70	388.90	1945	38 53	0.17
145 22.70 40 1.20 0.47 29.54 6.15 16.73 613.70 614.60 3073 41.15 1.78 155 22.70 40 1.30 0.54 29.76 7.41 20.64 654.00 655.00 3275 41.76 2.59 220 13.00 40 3.50 0.99 10.25 11.07 24.80 220.80 222.70 1113 14.88 17.36 270 13.00 40 6.00 1.56 9.44 19.58 46.53 202.90 209.30 1046 12.63 54.35 CMB-S4-LAT 30 7.40 40 30.80 0.28 1.54 0.19 0.12 3.07 3.45 17.24 1.03 0.02 40 5.10 40 17.60 0.19 0.74 0.11 0.07 1.85 2.01 10.04 0.51 0.01 95 2.20 40 2.90 0.06 0.13 0.14		95	25.50	40	0.80	0.20	32.54	2.53	5.41	463.10	464.30	2321	41.80	0.25
155 22.70 40 1.30 0.54 29.76 7.41 20.64 654.00 655.00 3275 41.76 2.59 220 13.00 40 3.50 0.99 10.25 11.07 24.80 220.80 222.70 1113 14.88 17.36 270 13.00 40 6.00 1.56 9.44 19.58 46.53 202.90 209.30 1046 12.63 54.35 CMB-S4-LAT 30 7.40 40 30.80 0.28 1.54 0.19 0.12 3.07 3.45 17.24 1.03 0.02 40 5.10 40 17.60 0.19 0.74 0.11 0.07 1.85 2.01 10.04 0.51 0.01 95 2.20 40 2.90 0.06 0.13 0.14 0.08 0.52 0.56 2.82 0.08 0.10 145 1.40 40 2.80 0.07 0.06 0.31 0.15		145	22.70	40	1.20	0.47	29.54	6.15	16.73	613.70	614.60	3073	41.15	1.78
220 13.00 40 3.50 0.99 10.25 11.07 24.80 220.80 222.70 1113 14.88 17.36 270 13.00 40 6.00 1.56 9.44 19.58 46.53 202.90 209.30 1046 12.63 54.35 CMB-S4-LAT 30 7.40 40 30.80 0.28 1.54 0.19 0.12 3.07 3.45 17.24 1.03 0.02 40 5.10 40 17.60 0.19 0.74 0.11 0.07 1.85 2.01 10.04 0.51 0.01 95 2.20 40 2.90 0.06 0.13 0.14 0.08 0.52 0.56 2.82 0.08 0.10 145 1.40 40 2.80 0.07 0.06 0.31 0.15 0.17 0.40 1.98 0.04 1.18 220 1.00 40 9.80 0.21 0.06 0.76 0.36		155	22.70	40	1.30	0.54	29.76	7.41	20.64	654.00	655.00	3275	41.76	2.59
270 13.00 40 6.00 1.56 9.44 19.58 46.53 202.90 209.30 1046 12.63 54.35 CMB-S4-LAT 30 7.40 40 30.80 0.28 1.54 0.19 0.12 3.07 3.45 17.24 1.03 0.02 40 5.10 40 17.60 0.19 0.74 0.11 0.07 1.85 2.01 10.04 0.51 0.01 95 2.20 40 2.90 0.06 0.13 0.14 0.08 0.52 0.56 2.82 0.08 0.10 145 1.40 40 2.80 0.07 0.06 0.31 0.15 0.17 0.40 1.98 0.04 1.18 220 1.00 40 9.80 0.21 0.06 0.76 0.36 0.06 0.87 4.37 0.09 13.97 270 0.90 40 23.60 0.42 0.07 1.23 0.58 <t< td=""><td></td><td>220</td><td>13.00</td><td>40</td><td>3.50</td><td>0.99</td><td>10.25</td><td>11.07</td><td>24.80</td><td>220.80</td><td>222.70</td><td>1113</td><td>14.88</td><td>17.36</td></t<>		220	13.00	40	3.50	0.99	10.25	11.07	24.80	220.80	222.70	1113	14.88	17.36
CMB-S4-LAI 30 7.40 40 30.80 0.28 1.54 0.19 0.12 3.07 3.45 17.24 1.03 0.02 40 5.10 40 17.60 0.19 0.74 0.11 0.07 1.85 2.01 10.04 0.51 0.01 95 2.20 40 2.90 0.06 0.13 0.14 0.08 0.52 0.56 2.82 0.08 0.10 145 1.40 40 2.80 0.07 0.06 0.31 0.15 0.17 0.40 1.98 0.04 1.18 220 1.00 40 9.80 0.21 0.06 0.76 0.36 0.06 0.87 4.37 0.09 13.97 270 0.90 40 23.60 0.42 0.07 1.23 0.58 0.03 1.42 7.12 0.13 44.55		270	13.00	40	6.00	1.56	9.44	19.58	46.53	202.90	209.30	1046	12.63	54.35
40 5.10 40 17.60 0.19 0.74 0.11 0.07 1.85 2.01 10.04 0.51 0.01 95 2.20 40 2.90 0.06 0.13 0.14 0.08 0.52 0.56 2.82 0.08 0.10 145 1.40 40 2.80 0.07 0.06 0.31 0.15 0.17 0.40 1.98 0.04 1.18 220 1.00 40 9.80 0.21 0.06 0.76 0.36 0.06 0.87 4.37 0.09 13.97 270 0.90 40 23.60 0.42 0.07 1.23 0.58 0.03 1.42 7.12 0.13 44.55	CMB-S4-LAT	30	7.40	40	30.80	0.28	1.54	0.19	0.12	3.07	3.45	17.24	1.03	0.02
95 2.20 40 2.90 0.06 0.13 0.14 0.08 0.52 0.56 2.82 0.08 0.10 145 1.40 40 2.80 0.07 0.06 0.31 0.15 0.17 0.40 1.98 0.04 1.18 220 1.00 40 9.80 0.21 0.06 0.76 0.36 0.06 0.87 4.37 0.09 13.97 270 0.90 40 23.60 0.42 0.07 1.23 0.58 0.03 1.42 7.12 0.13 44.55		40	5.10	40	17.60	0.19	0.74	0.11	0.07	1.85	2.01	10.04	0.51	0.01
140 1.40 40 2.80 0.07 0.00 0.11 0.17 0.40 1.98 0.04 1.18 220 1.00 40 9.80 0.21 0.06 0.76 0.36 0.06 0.87 4.37 0.09 13.97 270 0.90 40 23.60 0.42 0.07 1.23 0.58 0.03 1.42 7.12 0.13 44.55		95 145	2.20	40 70	2.90	0.06	0.13	0.14	0.08	0.52	0.56	2.82	0.08	0.10
270 0.90 40 23.60 0.42 0.07 1.23 0.58 0.03 1.42 7.12 0.13 44.55		220	1.40	40	2.80	0.21	0.06	0.76	0.15	0.17	0.40	4.37	0.04	13.97
		270	0.90	40	23.60	0.42	0.07	1.23	0.58	0.03	1.42	7.12	0.13	44.55

Hui et al. (2018) for BICEP+keck and BICEPArray; Essinger-Hileman et al. (2014) for CLASS; Errard et al. (2016) for PIPER; Ade et al. (2019) for Simons Observatory; Rahlin et al. (2014) for SPIDER; Young et al. (2018) for PICO; Abazajian et al. (2019) for CMB-S4; Hill-Valler (2019) for NEXT-BASS; the online presentation for SPT-3G⁷; the online presentation for LiteBIRD⁸; the online presentation for IDS⁹.

6.2. Unit conversions and bandpass corrections

In the mm wavelength domain, two different units are often used. While for studies of Galactic emission or extragalactic sources, the unit is Jansky (Jy), K_{CMB} is the natural unit for CMB. Transforming Jy into K_{CMB} is not only a unit conversion, but also requires a colour correction (to account for the different spectral energy distribution that is implicitly assumed in the two units). This transformation is detailed in Appendix A. The conversion factors that are given in Tables 10 and 11 assume a square bandpass, with a δv and a central frequency v given in the tables. Colour corrections are not computed for each experiment as it requires precisely knowing the bandpasses (e.g. for Planck, assuming a square bandpass rather than the true bandpass leads to error in the colour corrections that are of the same order as the correction). Consequently, all the numbers given in the tables in Jy are given for the true spectra (but σ_{inst} and σ_{CMB} , which are given for the convention vIv = constant, use the square bandpasses).

For current experiments with known bandpass, accurate unit conversions are given in Appendix A. For current experiments, a comparison of foreground levels (CIB and SZ especially) also necessitates their extrapolation between nearby frequencies of different experiments. To this end, useful conversion factors are given in Appendix A.

6.3. Confusion noise and flux limit

As we showed in Eq. (11), we chose to use a flux cut in total intensity rather than in polarised intensity mainly for two reasons: (i) we assumed that sources are removed or masked from polarisation maps using total intensity data, for which we could have a high-resolution survey complete to some level in total intensity, as opposed to the equivalent in polarised intensity (e.g. Battye et al. 2011; Datta et al. 2019), and (ii) source number counts in polarisation are very scarce, and more polarisation data are required to constrain dN/dP. By contrast, thanks to the numerous data in intensity obtained in the past decade, accurate modelling is available for number counts in intensity. Consequently, we computed the confusion noise and flux limit in intensity for each CMB experiment listed in Sect. 6.1.

6.3.1. Method and validation

The confusion noise¹⁰ is usually defined as fluctuations of the background sky brightness below which sources cannot be detected individually. These fluctuations are caused by intrinsi-

cally discrete extragalactic sources. In the far-IR, sub-mm, and mm, the confusion noise is an important part of the total noise budget because of the limited size of the telescopes compared to the wavelength. The confusion noise is even often greater than the instrument noise and therefore severely limits the survey depth (e.g. Lagache et al. 2003; Dole et al. 2003; Negrello et al. 2004; Nguyen et al. 2010).

When the flux of a point source is measured, the root mean square (rms) fluctuations due to extragalactic point sources are the sum of three components:

$$\sigma_{\rm conf}^2 = \sigma_{SNrad}^2 + \sigma_{SNir}^2 + \sigma_{\rm Clus}^2, \qquad (36)$$

where σ_{SNrad} , σ_{SNir} , and σ_{Clus} are the rms fluctuations associated with the radio shot noise, dusty galaxy shot noise, and dusty galaxy clustering, respectively (we recall that clustering from radio sources is neglected, see Sect. 1). They are related to the power spectrum P_k following

$$\sigma_i^2 = \int 2\pi k P_k^i T_k W_k \mathrm{d}k\,,\,$$
(37)

where W_k is the power spectrum of the beam (we assume Gaussian beams), and *i* stands for *SNrad*, *SNir*, and *Clus*, respectively. T_k is the transfer function linked to the flux measurement of the sources. We assumed that fluxes are measured using aperture photometry,

$$f(r) = h_1 \prod \left(\frac{r}{2R_1}\right) - h_2 \prod \left(\frac{r}{2R_2}\right), \qquad (38)$$

where \prod is the rectangular function, and R_1 and R_2 are the radii of the two circular apertures (with $R_2 > R_1$) and

$$h_1 = \frac{R_2^2}{R_2^2 - R_1^2} \tag{39}$$

$$h_2 = \frac{R_1^2}{R_2^2 - R_1^2} \,. \tag{40}$$

The Fourier transform of f(r) is

$$F(k) = \pi R_1^2 \frac{2J_1(2\pi kR_1)}{2\pi kR_1} h_1 - \pi R_2^2 \frac{2J_1(2\pi kR_2)}{2\pi kR_2} h_2 , \qquad (41)$$

which gives the following power spectrum for our aperture photometry filter:

$$T_k = \left(\frac{\pi R_1^2 R_2^2}{R_2^2 - R_1^2}\right)^2 \left[\frac{2J_1(2\pi kR_1)}{2\pi kR_1} - \frac{2J_1(2\pi kR_2)}{2\pi kR_2}\right]^2.$$
 (42)

The confusion noise can be determined using two criteria, the so-called photometric and source density criteria (Dole et al. 2003; Lagache et al. 2003). The photometric case is derived from the fluctuations of the signal due to the sources below the detection threshold S_{lim} in the beam. The source density case is derived from a completeness limit and evaluates the density of the sources detected above the detection threshold S_{lim} , such that only a small fraction of sources is missed because they cannot be separated from their nearest neighbour. The choice of the criterion depends on the shape of the source counts and the solid

⁷ https://indico.fnal.gov/event/20244/session/6/ contribution/69/material/slides/0.pdf

⁸ https://agenda.infn.it/event/15448/contributions/

^{95798/}attachments/65895/80698/sugai_public.pdf

⁹ http://research.iac.es/congreso/cmbforegrounds18/ media/talks/day2/IDS_v1.pdf

¹⁰ We only considered the confusion noise due to extragalactic sources because in the high Galactic latitude cosmological fields, the cirrus confusion noise is negligible, contributes very little to the total noise (Dole et al. 2003), or can be mitigated using component separation methods.

angle of the beam (Dole et al. 2003). The transition between the two is at about $200\,\mu$ m, depending on telescope diameters (Lagache et al. 2003). In this paper, we therefore use the photometric criterion.

The photometric criterion is related to the quality of the photometry of detected sources, the flux measured near S_{lim} being severely affected by fainter sources in the beam. It is defined by the implicit equation,

$$S_{\rm lim} = q_{\rm phot} \times \sigma_{\rm tot}(S_{\rm lim}), \qquad (43)$$

where q_{phot} measures the photometric accuracy (we assume $q_{\text{phot}} = 5^{11}$), and S_{lim} is the confusion limit. σ_{tot} is defined as

$$\sigma_{\rm tot} = \sqrt{F^2 \times [\sigma_{\rm conf}^2 + \sigma_{\rm CMB}^2] + \sigma_{\rm inst}^2}, \qquad (44)$$

where σ_{conf}^2 is given in Eq. (36) and σ_{inst} is the instrument noise per beam (given in Tables 6 and 7). We also added the noise introduced by CMB fluctuations, σ_{CMB} , which is given by Eq. (37), where we replaced P_k by the power spectrum of the CMB. *F* is a correction factor that accounts for the flux lost by the aperture photometry procedure (which does not cover the entire beam size). With our choice of R_1 and R_2 (see below), and assuming Gaussian beams, $F \simeq 3$ for all experiments considered here.

In the range of confusion limits of CMB experiments, only P_k^{SNrad} and P_k^{SNir} depend on S_{\lim} . They are derived following

$$P_k = \int_0^{S_{\rm lim}} S^2 \frac{\mathrm{d}N}{\mathrm{d}S} \mathrm{d}S , \qquad (45)$$

where dN/dS are the number counts given by the models described in Sect. 2.2 and Sect. 3.1 for radio and dusty galaxies, respectively.

Confusion noises and flux limits are given in Tables 6 and 7. They were obtained using $R_1 = FWHM/2$ and $R_2 = 2 \times R_1$.

We confirmed that our confusion noises agree very well with those measured by ISO/ISOPHOT, Herschel/SPIRE, and *Planck*. For SPIRE, we obtain $\sigma_{conf} = 6.4$, 6.6, and 5.3 mJy beam⁻¹, while Nguyen et al. (2010) measured 5.8 ± 0.3 , 6.3 ± 0.4 , and 6.8 ± 0.4 mJy beam⁻¹ at 250, 350 and 500 μ m, respectively. For Planck, we compared our flux limit to the flux cuts given in the PCCS2 source catalogue for 90% completeness (in the extragalactic zone) in Table 8. This comparison is indicative as the 90% completeness flux limit is not strictly equivalent to the confusion noise¹¹. The overall agreement is better than $\sim 2\sigma$. However, our flux cut is systematically below the PCCS2 flux limit for the highest frequencies (217, 353, 545, and 857 GHz). We verified that this underestimate can be easily explained by the cirrus contamination, which may be quite high in the extragalactic zone (covering $|b| > 30^{\circ}$) and which is ignored in the present paper. Finally, we also verified our results for SPT by substituting σ_{inst} from SPT-3G in the SPT-SZ survey. Considering $\sigma_{\text{inst}}^{SPT-SZ} = 2$, 1.2, and 4 mJy, we obtain $S_{\text{lim}} = 11$,

Table 8. Flux limits for *Planck* frequencies from the PCCS2 source catalogue (Planck Collaboration XXVI 2016) for 90% completeness in the extragalactic zone and using our model.

-			
Frequency GHz	PCCS2 mJy	This paper mJy	Ν
30	426 ± 87	541	+ 1.3
44	676 ± 134	761	+ 0.6
70	489 ± 101	330	- 1.6
100	269 ± 55	278	+ 0.2
143	177 ± 35	207	- 0.9
217	152 ± 29	105	- 1.6
353	304 ± 55	190	- 2.1
545	555 ± 105	330	- 2.1
857	791 ± 168	569	- 1.3

Notes. The last column gives the $N\sigma$ difference between the two estimates (considering only the uncertainty on the flux limit given for the PCCS2).

7.1 and 20.5 mJy, at 95, 150, and 220 GHz, respectively, which agrees very well with Mocanu et al. (2013b, see their Table 3, for 95% completeness limit). The very good agreement with previous far-IR, sub-mm, and mm experiments gives us confidence in our computations.

6.3.2. Contributions to the point-source sensitivity

Ground-based experiments have a maximum frequency of 280 GHz. The contribution of the different components to the point-source sensitivity mostly depends on the frequency and size of the telescope apertures.

The smallest telescopes, with sizes <1 m (BICEP, CLASS, SO-SAT, and CMB-S4-SAT) or the low-frequency telescopes (C-BASS, NEXT-BASS, and QUIJOTE, with $\nu < 40$ GHz) have quite poor angular resolutions. The contribution of radio sources dominates up to ~10–15 GHz, then the confusion noise from the CMB becomes dominant. If we can remove the CMB, the CIB clustering dominates the noise budget at the higher frequencies ($\nu > 200$ GHz). Instrument noise is always much lower than the astrophysical components.

As expected, a telescope with a larger aperture returns lower flux limits because the confusion noise is much lower (and the instrument noise is generally lower as well). For larger aperture telescopes (AdvACTPOL, SO-LAT, SPT-3G, and CMB-S4-LAT), the instrument noise is at the same order of magnitude as confusion noises. For $\nu > 145$ GHz, the dominant contribution to the σ_{tot} comes from the shot noise of DSFG.

In space, telescopes have smaller apertures in general and instrument noise is always negligible compared to confusion noise. Confusion from the CMB always dominates, except at the highest frequencies ($\nu \ge 300$ GHz). Except for the CMB, galaxy clustering above ~150–200 GHz contributes much. PIPER, SPI-DER, and LiteBIRD have large $S_{\rm lim}$ (>1 Jy) that will consequently lead to a large contamination to the CMB-B mode measurements.

6.3.3. The case of B-POP

We also considered the SPICA B-POP polarised experiment, which is at shorter wavelength. B-POP will provide $100-350 \,\mu m$ images of linearly polarised dust emission with an angular resolution, signal-to-noise ratio, and dynamic ranges comparable

¹¹ We chose a standard signal-to-noise ratio $S/N = 5\sigma$, which is usually sufficient to obtain a reliability close from 100% (e.g. >95% at S/N = 5 in Planck Collaboration XXVI 2016). It is extremely difficult to assess the reliability of a survey as a function of S/N before actual data are available because it is sensitive to many unknown parameters (non-Gaussian noise and systematics, non-Gaussian foregrounds, exact statistics of the sources, and choice of source extraction method). In addition, the exact threshold associated with a given reliability can also vary with regions in case of heterogeneous depth and/or foreground contamination, as for *Planck*.

Table 9. Confusion noise, flux limit, and DSFG shot noise level for the

 SPICA B-POP experiment.

λ µm	FWHM arcsec	$\sigma_{ m conf} \ { m mJy}$	S _{lim} mJy	SN_{IR} Jy ² sr ⁻¹
100	9	8.0×10^{-2}	0.40	6.4
200	18	3.9	19.6	3.9×10^{3}
350	32	7.1	35.3	4.1×10^{3}

to those achieved by *Herschel* images of the cold ISM in total intensity. The angular resolution of B-BOP at $200 \,\mu\text{m}$ will also be a factor ~30 better than Planck polarisation data.

At these wavelengths and with this high angular resolution, only the shot noise of DSFG contributes to the confusion noise (σ_{conf}). Flux limits are about 0.4, 19.6, and 35.3 mJy at 100, 200, and 350 μ m, respectively (see Table 9). This is sightly above the SPIRE/*Herschel* 350 μ m flux limit due to the smaller telescope aperture. For one pointing (2.5' × 2.5'), confusion noise levels are reached in 9.9, 0.02, and 0.02 seconds at 100, 200, and 350 μ m, respectively¹². For a 1 Sq. Deg. survey, they are reached in 1.6 hours, 9.7 seconds, and 12.1 seconds. This shows that the 200 and 350 μ m maps, even on large areas, will be severely limited in depth by extragalactic confusion.

In polarisation, after masking all the sources detected in intensity, up to S_{lim} , the r.m.s of polarised intensity due to confusion is

$$\sigma_{\rm conf}^P = \sqrt{(\sigma_{\rm conf}^Q)^2 + (\sigma_{\rm conf}^U)^2} = \sigma_{\rm conf} \times \langle \Pi^{\rm IR} \rangle \,. \tag{46}$$

Assuming a fractional polarisation for DSFG $\langle \Pi^{IR} \rangle = 1.4\%$ (see Sect. 3.2) and $\sigma_{conf}^{Q} = \sigma_{conf}^{U}$, we obtain a confusion noise in polarisation $\sigma_{conf}^{Q,U} = 0.79$, 38.6, 70.3 µJy after masking all the sources detected in intensity at 100, 200, and 350 µm, respectively. These $\sigma_{conf}^{Q,U}$ levels are reached in 57 h, 5.8 min, and 7.0 min for a single pointing, and 33 737, 57, and 69 hours for a 1 Sq. Deg. survey, at 100, 200, and 350 µm, respectively. In polarisation, confusion is therefore not expected to be reached at 100 µm, but could be reached for the deepest integrations at longer wavelengths. Confusion from galaxies could ultimately limit the sensitivity of the high-latitude polarimetric deep surveys of the interstellar medium of our Galaxy at 200 and 350 µm.

7. Contamination of the CMB B-modes

In order to provide reliable predictions of the radio source and DSFG contamination to CMB anisotropy polarisation measurements, we have to assume a fractional polarisation for each population of galaxies. For radio sources, at the frequencies where the contamination of the *B*-modes is minimum (i.e. ~90– 300 GHz), there are still few polarisation measurements and very scarce polarisation fraction measurements for the different types of radio sources (see Sect. 2.3). Thus, we used a constant $\langle \Pi^{rad} \rangle = 2.8\%$, in agreement with the recent *Planck*, SPT, and ACT measurements and radio source follow-ups from 90 to 220 GHz. For DSFG, the situation is even worse and polarisation properties are almost completely unexplored. As discussed

in Sect. 3.2, we adopted $\langle \Pi^{IR} \rangle = 1.4\%$. As all our BB power spectra are proportional to the square of the fractional polarisation, it is very easy to obtain polarised power spectra for other choices of fractional polarisation:

$$C_{\ell}^{\text{BB,Radio}}(\Pi^{\text{rad}}) = C_{\ell}^{\text{BB,Radio}} \left(\frac{\Pi^{rad}}{0.028}\right)^2 \,, \tag{47}$$

$$C_{\ell}^{\text{BB,CIB}}(\Pi^{IR}) = C_{\ell}^{\text{BB,CIB}} \left(\frac{\Pi^{IR}}{0.014}\right)^2, \qquad (48)$$

$$C_{\ell}^{\text{BB},IR}(\Pi^{IR}) = C_{\ell}^{\text{BB},IR} \left(\frac{\Pi^{IR}}{0.014}\right)^2 \,. \tag{49}$$

7.1. Polarised power spectra of the extragalactic components

We list in Tables 10 and 11 the level of BB power spectra for radio (C_{ℓ}^{rad}) and DSFG (C_{ℓ}^{IR}) shot noise, and the clustering (C_{ℓ}^{CIB}) for three multipoles ($\ell = 80$, 1000, and 4000).

We first compare in Fig. 4 the relative level of DSFG shot noise and clustering power spectra at $\ell = 80$. We recall that the clustering power spectra are an upper limit as we estimated the maximum contribution of the one-halo term (see Sect.5.3). The ratio $C_{\ell}^{IR}/C_{\ell}^{CIB}$ is mostly constant, and between 2 and 3 for 120 < $\nu < 700$ GHz. At lower frequencies, it is much higher (from 4 to 30) and thus C_{ℓ}^{CIB} can be neglected. Consequently, we did not compute the clustering power spectra for frequencies $\nu \le$ 90 GHz. The ratio increases very slowly with ℓ , by up to ~30% at $\ell = 4000$ and $\nu < 400$ GHz.

We then compare in Fig. 5 the level of the radio power spectra and DSFG+clustering power spectra as a function of frequency. As expected, the general trend is an increase in $\Delta = \frac{C_\ell^{IR} + C_\ell^{CIB}}{C_\ell^{Rad}}$ with frequency, roughly proportional to v^7 for 80 < v < 400 GHz. We can distinguish three families of points, depending on the telescope size, with Δ varying by a factor ~250:

- For the large-aperture telescopes (≥ 6 m, i.e. SPT-3G, S4-LAT, SO-LAT, AdvActPol), $\Delta \simeq 100 \times \left(\frac{v}{200 \text{ (mJ)}}\right)^7$.
- LAT, SO-LAT, AdvActPol), $\Delta \simeq 100 \times \left(\frac{\nu}{220 \, \text{[GHz]}}\right)^7$. – For the medium-aperture telescopes (~1.5 m, i.e. *Planck*, IDS, PICO), $\Delta \simeq 4 \left(\frac{\nu}{220 \, \text{[GHz]}}\right)^7$.
- − For the small-aperture telescopes (≤0.6 m, i.e. LiteBIRD, SPIDER, CLASS, SO-SAT, S4-SAT, BICEP), $\Delta \simeq 0.4 \times \left(\frac{\nu}{220 \, [\text{GHz}]}\right)^7$.

Thus, the DSFG power spectra level is higher than that of radio galaxies at a frequency that decreases with telescope size: ~247, 180, and 114 GHz, from small to large apertures. These results do not depend on the multipole (as $C_{\ell}^{IR}/C_{\ell}^{\text{CIB}}$ varies weakly with ℓ).

7.2. Comparison with the CMB B-modes

We first illustrate the contaminations of extragalactic components to the CMB *B*-mode power spectrum at two frequencies, ~220 GHz (Fig. 6) and 145 GHz (Fig. 7). At each frequency, we plot the power spectra for two different aperture telescopes to illustrate the turnover between radio/DSFG dominant contaminations. The CMB *B*-mode power spectrum was calculated for the *Planck* 2018 cosmology (using TT, TE, EE+lowE+lensing+BAO and a pivot scale for *r* of 0.002 Mpc⁻¹, Planck Collaboration VI 2020).

¹² These values were computed using the André et al. (2019) sensitivity forecasts (see their Table 1). They correspond to the time needed to reach $\sigma_{inst} = \sigma_{conf}$.

Table 10. C_{ℓ}^{BB} of the extragalactic foreground components for space-based and balloon-borne experiments: radio galaxies, dusty galaxies (IR), and CIB one-halo (completely negligible for $\nu \leq 90$ GHz and thus not computed).

Experiment	ν	δν	С	C_{ℓ}^{BB} Radio	C_{ℓ}^{BB} IR	C_{ℓ}^{BB} CIB ($\ell = 80$)	C_{ℓ}^{BB} CIB ($\ell = 1000$)	C_{ℓ}^{BB} CIB ($\ell = 4000$)
	GHz	%		Jy ² sr ^{−1}	Jy ² sr ⁻¹	Jy ² sr ⁻¹	Jy ² sr ⁻¹	Jy ² sr ⁻¹
Planck	30	30	26.81	8 018 10-3	654210^{-6}			
1 шиск	30 44	30	20.81 56.17	$9.882 10^{-3}$	$6.766 10^{-6}$	_	_	_
	70	30	131.85	$3.537 10^{-3}$	$5.973 10^{-6}$	_	_	_
	100	30	237.01	2.51510^{-3}	$1.840 10^{-5}$	451710^{-6}	$4 367 10^{-6}$	$4.032.10^{-6}$
	143	30	377.14	$1.583 10^{-3}$	$1.267 10^{-4}$	$4.387 10^{-5}$	4.212 10 ⁻⁵	3.835 10 ⁻⁵
	217	30	480.18	7.00910^{-4}	$1.465 10^{-3}$	4.98610^{-4}	$4.724 10^{-4}$	4.18910^{-4}
	353	30	294.65	9.67510^{-4}	$2.052 10^{-2}$	$6.724 10^{-3}$	$6.164 10^{-3}$	$5.125 10^{-3}$
IDS	150	30	395.55	1.581 10 ⁻³	1.684 10 ⁻⁴	5.998 10 ⁻⁵	5.751 10 ⁻⁵	5.223 10 ⁻⁵
	180	30	454.58	$1.027 10^{-3}$	4.92010^{-4}	$1.671 10^{-4}$	$1.595 10^{-4}$	1.43510^{-4}
	220	30	480.08	4.47310^{-4}	1.56910^{-3}	5.32110^{-4}	5.04010^{-4}	4.46610^{-4}
	250	30	463.95	2.75410^{-4}	3.20910^{-3}	$1.106 10^{-3}$	$1.041 \ 10^{-3}$	9.09710^{-4}
	280	30	426.14	5.74710^{-4}	6.11610^{-3}	$2.008 \ 10^{-3}$	$1.877 \ 10^{-3}$	1.62010^{-3}
	320	30	356.86	4.04910^{-4}	$1.223 \ 10^{-2}$	4.05210^{-3}	3.75010^{-3}	3.17410^{-3}
	360	30	281.64	3.68310^{-4}	$2.186 10^{-2}$	7.36910^{-3}	$6.745 10^{-3}$	5.58910^{-3}
PIPER	200	30	474.77	1.41210^{-2}	$1.060 \ 10^{-3}$	$3.087 10^{-4}$	$2.935 10^{-4}$	2.62210^{-4}
	270	30	440.61	6.46810^{-3}	$5.397 10^{-3}$	$1.677 \ 10^{-3}$	$1.570 10^{-3}$	$1.361 10^{-3}$
	350	16	301.91	4.35510^{-3}	$2.058 \ 10^{-2}$	6.44810^{-3}	5.916 10-3	4.92510^{-3}
	600	10	31.88	5.911 10 ⁻³	$2.083 10^{-1}$	7.684 10 ⁻²	6.487 10 ⁻²	4.589 10 ⁻²
SPIDER	94	24	216.11	3.65210^{-2}	3.78910^{-5}	1.595 10 ⁻⁶	1.554 10-6	1.457 10-6
	150	24	396.64	2.54210^{-2}	2.359 10 ⁻⁴	5.998 10 ⁻⁵	5.751 10 ⁻⁵	5.223 10-5
LiteBIRD	40	30	46.82	3.891 10-2	1.667 10-5	-	-	-
	50	30	71.49	3.855 10-2	1.73110^{-3}	-	-	-
	60	23	100.42	3.61710^{-2}	1.79610^{-5}	-	-	-
	68	23	125.69	$3.094 10^{-2}$	$1.765 10^{-5}$	-	-	-
	/8	23	159.42	2.798 10 2	1.993 10 5	-	-	-
	89	23	198.20	$2.494\ 10^{-2}$	2.4/6 10 5	-	-	-
	100	23	237.76	$2.263 10^{-2}$	3.390 10 5	4.51/10 °	4.36/10 °	4.032 10 °
	119	20	303.30 269 76	1.92910^{-2}	$0.055 10^{-4}$	$1.3//10^{-5}$	$1.32/10^{-5}$	1.21910^{-5}
	140	20	308.70	$1.724 10^{-2}$	1.405 10	3.090 10 -4	3.353 10 -4	5.240 10 ⁻⁵
	100	30	431.24	1.90410 1.65610^{-2}	$9.365 10^{-4}$	$1.082\ 10$ 2 733 10^{-4}	$2.600 \ 10^{-4}$	9.34910^{-4}
	235	30	471.10	1.03010 1.32210^{-2}	$9.303\ 10$ 2.620 10^{-3}	2.73310 7 830 10 ⁻⁴	$2.000\ 10$ 7 300 10 ⁻⁴	2.32310 6 504 10 ⁻⁴
	235	30	475.27	$5.453 10^{-3}$	653410^{-3}	$2.008 10^{-3}$	$1.877 10^{-3}$	$1.620 10^{-3}$
	337	30	324.81	$3,44610^{-3}$	$1.687 10^{-2}$	530510^{-3}	$4.886 10^{-3}$	$4.098 10^{-3}$
	402	23	209.33	$2.715 10^{-3}$	$3.910 10^{-2}$	$1.269 10^{-2}$	$1.147 10^{-2}$	$9.275 10^{-3}$
PICO	21	25	13.33	9.236 10 ⁻³	$7.227 10^{-6}$	_	_	_
	25	25	18.80	$7.127 10^{-3}$	$6.041 10^{-6}$	_	_	_
	30	25	26.88	$6.550 10^{-3}$	5.58610^{-6}	_	_	_
	36	25	38.31	5.42110^{-3}	4.964 10 ⁻⁶	-	-	-
	43	25	53.89	5.81710^{-3}	5.16010^{-6}	-	-	-
	52	25	77.10	4.82610^{-3}	4.95310^{-6}	_	_	_
	62	25	106.48	2.78210^{-3}	4.47910^{-6}	_	_	_
	75	25	148.98	2.35410^{-3}	$6.148\ 10^{-6}$	-	-	-
	90	25	201.67	2.13610^{-3}	$1.114\ 10^{-5}$	-	-	-
	108	25	266.03	1.59910^{-3}	$2.575 \ 10^{-5}$	8.41310^{-6}	$8.117 10^{-6}$	7.46510^{-6}
	129	25	336.61	1.55810^{-3}	$6.925 \ 10^{-5}$	$2.447 10^{-5}$	$2.354 10^{-5}$	2.15210^{-5}
	155	25	408.65	1.08010^{-3}	$2.015 \ 10^{-4}$	7.14910^{-5}	$6.851 10^{-5}$	6.21410^{-5}
	186	25	463.34	4.24910^{-4}	5.85510^{-4}	2.09610^{-4}	$1.997 10^{-4}$	1.79110^{-4}
	223	25	480.81	2.66610^{-4}	$1.673 10^{-3}$	5.82310^{-4}	5.51010^{-4}	4.87410^{-4}
	268	25	444.34	4.01410^{-4}	4.75810^{-3}	1.611 10 ⁻³	1.50910^{-3}	1.30910^{-3}
	321	25	355.82	2.25810^{-4}	$1.218 10^{-2}$	4.126 10-3	3.817 10 ⁻³	3.229 10-3
	385	25	237.49	3.078 10-4	$2.977 10^{-2}$	1.03110^{-2}	9.368 10-3	7.650 10-3
	462	25	126.74	3.463 10 ⁻⁴	6.681 10 ⁻²	2.44210^{-2}	2.16610^{-2}	1.688 10 ⁻²
	555	25	51.31	3.142 10 ⁻⁴	$1.358 10^{-1}$	5.530 10-2	4.746 10 ⁻²	3.470 10 ⁻²
	666	25	15.07	3.317 10 ⁻⁴	2.47810^{-1}	1.17710^{-1}	9.688 10 ⁻²	6.511 10 ⁻²
	799	25	3.00	3.298 10 ⁻⁴	4.06310^{-1}	2.35710^{-1}	1.839 10	1.10910^{-1}

Notes. They are given in Jy² sr⁻¹. The unit conversion factor is also given (C = MJy sr⁻¹[νI_{ν} = constant] K_{CMB}^{-1}). The power spectra in Jy² sr⁻¹ have to be divided by C^2 to obtain power spectra in μK_{CMB}^2 .

We compare in Fig. 6 *Planck* at 217 GHz with LiteBIRD at 235 GHz. While the contamination by radio galaxies is twice lower than by DSFG for *Planck*, the power spectrum of radio galaxies is five times larger than that of DSFG for LiteBIRD

(even if the frequency of 235 GHz is higher). It is at the same level of the r = 0.01 (r = 0.001) *B*-mode power spectrum for $\ell = 160$ ($\ell = 83$). For *Planck*, the total contamination is negligible compared to the last 95% CL upper limit $r_{0.002} < 0.056$

Table 11. Same as Table 10, but for CMB ground-based experiments.

Experiment	ν	δν	С	C_{ℓ}^{BB} Radio	C_{e}^{BB} IR	C_{ℓ}^{BB} CIB ($\ell = 80$)	C_{ℓ}^{BB} CIB ($\ell = 1000$)	C_{ℓ}^{BB} CIB ($\ell = 4000$)
-	GHz	%		Jy ² sr ⁻¹	$Jy^2 sr^{-1}$	Jy ² sr ⁻¹	Jy ² sr ⁻¹	Jy ² sr ⁻¹
C-BASS	5	20	0.77	3.08910^{-2}	_	-	_	_
NEXT-BASS	7	20	1.67	9.737 10 ⁻³	-	-	-	-
	8	20	2.11	7.185 10 ⁻³	-	-	-	-
	9	20	2.70	$5.704 \ 10^{-3}$	-	-	-	-
	10	20	5.12 4.18	4.93910^{-3}	$5.949 10^{-6}$	_	_	_
	13	20	5.31	$3.133 10^{-3}$	4.89910^{-6}	_	_	_
	14	20	6.76	3.183 10 ⁻³	4.77910^{-6}	_	_	_
	15	20	7.69	1.59210^{-3}	3.51910^{-6}	_	-	-
	17	20	9.73	$1.134 \ 10^{-3}$	$2.925 10^{-6}$	-	-	-
	20	20	12.24	1.11210^{-3}	2.68710^{-6}	-	-	-
	22	20	15.30	8.020 10 ⁻⁴	2.282 10-6	-	-	-
	25	20	19.28	8.706 10 ⁻⁴	2.234 10 °	-	-	-
OUHOTE	20	18	3 70	$\frac{3.43710}{1.70610^{-2}}$	1.799 10			
QUIDIE	13	15	5.16	1.70010 1.63810^{-2}	$1.203\ 10^{-5}$	_	_	_
	17	12	8.80	$7.005 10^{-3}$	6.59010^{-6}	_	_	_
	19	11	10.98	7.49510^{-3}	6.64910^{-6}	-	-	-
	30	27	26.85	3.92410^{-3}	4.31810^{-6}	-	-	-
	40	24	46.95	3.01110^{-3}	3.72310^{-6}	-	-	-
AdvACTPOL	90	30	201.20	3.272 10 ⁻⁵	7.137 10 ⁻⁶	-	-	-
	150	30	395.55	1.956 10-5	$1.427 10^{-4}$	5.998 10-5	5.751 10-5	5.223 10-5
DICED2 - K1-[2019]	230	30	4/7.65	4.163 10 3	1.802 10 5	6.994 10 +	6.607 10 4	5.825 10 4
BICEP3+Reck[2018]	95 150	30 30	219.11	$1.4/8 10^{-2}$	2.37510^{-4}	2.082 10 ° 5 998 10 ⁻⁵	2.023 10 ⁻⁵	1.880 10 ° 5.223 10 ⁻⁵
BICEPArray[2023]	30	30	26.81	$\frac{2.34710}{329010^{-2}}$	1 448 10 ⁻⁵	-	-	-
Diebrinky[2020]	40	30	46.82	3.376 10 ⁻²	1.47410^{-5}	_	_	_
	95	30	219.11	1.47810^{-2}	2.37510^{-5}	2.08210^{-6}	2.023 10 ⁻⁶	1.88610^{-6}
	150	30	395.55	7.87910^{-3}	$1.898 10^{-4}$	$5.998 10^{-5}$	5.751 10 ⁻⁵	5.223 10 ⁻⁵
	220	30	480.08	4.15910^{-3}	1.67210^{-3}	5.321 10-4	5.040 10-4	4.466 10 ⁻⁴
	270	30	440.61	2.349 10-3	5.186 10-3	$1.677 \ 10^{-3}$	1.570 10-3	1.361 10 ⁻³
CLASS	38	30	42.42	3.45210^{-2}	1.497 10-5	-	-	-
	93	30	211.94	3.38310^{-2}	$3.465 10^{-9}$	1.108 10 ° 5 528 10 ⁻⁵	1.085 10 ° 5 211 10 ⁻⁵	1.028 10 ° 4.826 10 ⁻⁵
	217	30	480.18	1.78310 1.04310^{-2}	$1.639 10^{-3}$	4.98610^{-4}	$4.724 10^{-4}$	4.82010 4.18910^{-4}
SO-SAT	27	30	21.81	2.671 10 ⁻²	1.257 10 ⁻⁵	-	-	-
	39	30	44.60	$3.646 10^{-2}$	1.57010^{-5}	-	_	_
	93	30	211.94	2.14310^{-2}	$2.615 10^{-5}$	$1.108 \ 10^{-6}$	1.08510^{-6}	1.02810^{-6}
	145	30	382.56	9.867 10 ⁻³	1.61010^{-4}	$4.847 10^{-5}$	4.651 10 ⁻⁵	4.231 10 ⁻⁵
	225	30	479.26	4.11210^{-3}	1.90110^{-3}	6.15710^{-4}	5.823 10 ⁻⁴	5.145 10 ⁻⁴
20 J 17	280	30	426.14	2.262 10-3	6.330 10-3	2.008 10-3	1.877 10-3	1.620 10-3
SO-LAI	27	30	21.81	3.79110^{-4}	1.614 10 [°]	-	-	-
	93	30	211.94	346710^{-5}	8 623 10 ⁻⁶	-110810^{-6}	1.08510^{-6}	1.02810^{-6}
	145	30	382.56	2.374 10 ⁻⁵	$1.184 10^{-4}$	4.847 10 ⁻⁵	4.651 10 ⁻⁵	4.231 10 ⁻⁵
	225	30	479.26	4.308 10 ⁻⁵	$1.607 \ 10^{-3}$	6.15710^{-4}	5.823 10-4	5.14510^{-4}
	280	30	426.14	6.88010^{-5}	5.54910^{-3}	$2.008 \ 10^{-3}$	$1.877 10^{-3}$	1.62010^{-3}
SPT-3G	95	27	219.42	$1.175 10^{-5}$	9.260 10 ⁻⁶	2.08210^{-6}	2.023 10-6	1.886 10 ⁻⁶
	148	26	391.20	1.453 10 ⁻⁵	1.277 10 ⁻⁴	5.538 10-5	5.311 10-5	4.826 10 ⁻⁵
CH CH CH CH T	223	23	481.20	3.326 10 ⁻⁵	1.4745 10 ⁻³	5.823 10-4	5.51010-4	4.874 10-4
CMB-84-8AT	20	25	12.10	7.67910 ⁺ 3.20010 ⁻²	2.352 10 3	-	-	-
	30 40	30	20.81 46.82	3 891 10 ⁻²	1.440 10 ⁻⁵	-	_	_
	85	24	183.92	$1.510 10^{-2}$	$1.699 10^{-5}$	_	_	_
	95	24	219.71	1.63910^{-2}	$2.477 10^{-5}$	2.08210^{-6}	2.02310^{-6}	1.88610^{-6}
	145	22	383.91	1.61310^{-2}	1.74910^{-4}	$4.847 \ 10^{-5}$	4.65110^{-5}	4.231 10 ⁻⁵
	155	22	409.13	1.63710^{-2}	2.53910^{-4}	7.149 10 ⁻⁵	6.851 10 ⁻⁵	6.214 10 ⁻⁵
	220	22	481.78	5.833 10 ⁻³	$1.701 \ 10^{-3}$	5.321 10 ⁻⁴	5.040 10 ⁻⁴	4.466 10 ⁻⁴
	270	18	442.72	4.951 10 ⁻³	5.326 10-3	1.677 10-3	1.570 10-3	1.361 10-3
CMB-S4-LAT	30	30.0	26.81	4.057 10-4	1.587 10-0	-	-	_
	40	30	40.82	1.983 10 ⁺ 3.261 10 ⁻⁵	1.18910 ⁻⁶	- 2 082 10 ⁻⁶	- 2 023 10 ⁻⁶	- 1 886 10 ⁻⁶
	145	30	382.56	$1.755 10^{-5}$	$1.156 10^{-4}$	$4.847 10^{-5}$	$4.651 10^{-5}$	$4.231 10^{-5}$
	220	30	480.08	3.350 10 ⁻⁵	1.36910^{-3}	5.321 10 ⁻⁴	5.040 10 ⁻⁴	4.46610^{-4}
	270	30	440.61	4.97110^{-5}	4.36610^{-3}	$1.677 \ 10^{-3}$	$1.570 10^{-3}$	$1.361 10^{-3}$

(Planck Collaboration X 2020). In Fig. 7 we show the level of the extragalactic components for the ground-based S4-SAT and S4-LAT experiments. Contamination by radio sources dominates for S4-SAT at a level of $r = 1.7 \times 10^{-3}$ at $\ell = 80$. For S4-LAT, the

dominant contamination comes from DSFG shot noise, at a level of $r = 1.2 \times 10^{-5}$ at $\ell = 80$.

We finally compute the equivalent tensor-to-scalar ratio (r_{eq}) of the total extragalactic contamination (radio galaxy shot noise,

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Fig. 4. Ratio of shot noise and clustering (one-halo CIB anisotropies) for dusty galaxies at $\ell = 80$ for all CMB experiments ($\ell = 80$ corresponds to the recombination B-peak).



Fig. 5. Ratio between the BB power spectra of [IR shot noise + clustering] and radio shot noise, at $\ell = 80$ for all CMB experiments.

DSFG shot noise, and clustering) for each individual frequency at given multipoles. We show in Fig. 8 the variation in r_{eq} as a function of frequencies at the recombination B-peak, $\ell = 80$. Minimum r_{eq} is reached for $90 \le \nu \le 300$ GHz depending on the experiment. Similarly to Fig. 5 (and see Sect 7.1), we can distinguish three cases according to the telescope aperture size:

– Large-aperture telescopes. The minimum contamination is at the level of $r_{eq} = 7.4 \times 10^{-6}$ for SPT-3G at 95 GHz. For SO-LAT, AdvACT, and S4-LAT, r_{eq} is about 1.5 and 2×10^{-5} at 90– 93 and 145–150 GHz, respectively. These levels are well below the targeted σ_r of these experiments (by a factor of $\gtrsim 20-400$).

– Medium-aperture telescopes. The minimum contamination is at the level of $r_{\rm eq} \simeq 10^{-4}$ and is reached at $\nu \simeq 200$ GHz. While this is ~40 times higher than $\sigma_{\rm r}$ for IDS alone, it is at the same level as $\sigma_{\rm r}$ for PICO (Hanany et al. 2019).

– Small-aperture telescopes. The contamination reaches a level of $4.3-5.4 \times 10^{-4}$ for S4-SAT, SO-SAT, and BICEPArray at ~220 GHz. It increases to 8.5×10^{-4} for CLASS at 217 GHz, and 1.1×10^{-3} for LiteBIRD at 235 and 280 GHz and PIPER at 200 and 270 GHz. Finally, it is about 2.5×10^{-3} for SPIDER at



Fig. 6. Extragalactic foreground power spectra for *Planck* (coloured dashed lines) and LiteBIRD (coloured continuous lines) at 217 and 235 GHz, respectively. The three continuous black lines are the primordial CMB *B*-mode power spectrum for r = 0.1, 0.01, and 0.001 from top to bottom. The dash-three-dots line is the lensing *B*-mode.



Fig. 7. Extragalactic foreground power spectra for S4-SAT (coloured dashed lines) and S4-LAT (coloured continuous lines) at 145 GHz. The three continuous black lines are the primordial CMB *B*-mode power spectrum for r = 0.1, 0.01, and 0.001 from top to bottom. The dash-three-dots line is the lensing *B*-mode. As the two experiments are at the same frequency, the two C_{ℓ}^{CIB} curves are confounded.

150 GHz. The level of contamination (of 4 to 8×10^{-4} from 150 to 270 GHz) is below the targeted σ_r for the Bicep/Keck experiment, for which they project $0.002 < \sigma_r < 0.006$ by the end of the planned BICEP Array program, assuming current modelling of polarised Galactic foregrounds and depending on the level of delensing that can be achieved with higher angular resolution maps from the South Pole Telescope (Hui et al. 2018). For LiteBIRD, the contamination reaches the 68% confidence level uncertainty, that is $\sigma_r < 10^{-3}$ (this σ_r includes statistical, instrumental systematic, and Galactic foreground uncertainties, Matsumura et al. 2016).

This comparison between $r_{\rm eq}$ and $\sigma_{\rm r}$ was made considering each frequency for $r_{\rm eq}$ independently, while $\sigma_{\rm r}$ is usually estimated for each experiment by combining the whole



Fig. 8. Equivalent tensor-to-scalar ratio (r_{eq}) of the sum of the extragalactic foregrounds at the recombination B-peak, $\ell = 80$, for the different CMB experiments (r_{eq} is computed for each individual frequency).



Fig. 9. Ratio of equivalent *r* of the extragalactic foregrounds (r_{eq}) and instrument noise (r_{eq}^{inst}) , at $\ell = 80$.

set of available bands and under specific assumptions (e.g. taking systematic effects or foregrounds residual impacts into account). Multi-frequency component separations should be able to decrease the level of extragalactic foreground contamination.

To offer a complementary view, rather than comparing r_{eq} with σ_r , we could compare r_{eq} with the equivalent instrument

noise r_{eq}^{inst} computed independently at each frequency. We calculate r_{eq}^{inst} following

$$r_{\rm eq}^{\rm inst} = \left(\frac{\sigma_{\rm inst}^P}{\frac{180}{\ell} \times 60}\right)^2 \times \frac{1}{D_{\ell}^{BB}(r=1,\ell)},\tag{50}$$



Fig. 10. Equivalent tensor-to-scalar ratio (r_{eq}) of the sum of the extragalactic foregrounds at $\ell = 5$, corresponding to the reionisation B-bump. We also show the σ_r for LiteBIRD, PICO, and CLASS (dashed lines). For *Planck*, the current 1σ upper limit is r < 0.028 and is thus not visible in the figure.

where σ_{inst}^{P} is the instrument noise in polarisation (given in Tables 6 and 7). We show in Fig. 9 the ratio of r_{eq} and $r_{\text{eq}}^{\text{inst}}$ for all frequencies and experiments. A contamination of at least 10% ($r_{\text{eq}}/r_{\text{eq}}^{\text{inst}} \ge 0.1$) for $70 \le v \le 250$ GHz is reached for BICEP at 95 and 150 GHz, CLASS, SO-SAT, and SPIDER at 93 GHz, LiteBIRD from 78 to 140 GHz, S4-SAT from 85 to 155 GHz, and PICO from 75 to 129 GHz. Combining higher and lower frequencies to decrease the Galactic foreground residuals may also add more contamination from extragalactic sources (because of their different mean polarised SEDs and because they are not correlated from high to low frequencies). For example, for PICO, $0.9 \le r_{\text{eq}}/r_{\text{eq}}^{\text{inst}} \le 2.7$ for $21 \le v \le 52$ GHz and for S4-SAT, it is >10 for v = 30-95 GHz.

The scale dependency of extragalactic foregrounds compared to the CMB makes the ratio of the primordial CMB signal over foregrounds more favourable at larger scale, in particular at the reionisation B-bump ($\ell = 5$). Only nearly full-sky ($f_{sky} \ge 70\%$) experiments can provide some measurements at such low multipoles. The *r* equivalent in this case is very small (2.7×10^{-6} for PICO at 186 GHz, $3.7-3.4 \times 10^{-5}$ for LiteBIRD at 195-235 GHz, and 2.5×10^{-5} for CLASS at 217 GHz; see Fig. 10). They are much smaller than the targeted limits on the primordial *r* for PICO and LiteBIRD, and $\sigma_r = 8.5 \times 10^{-3}$ for CLASS (including diffuse Galactic thermal dust and synchrotron foregrounds, Watts et al. 2015). For *Planck*, the level of contamination by polarised extragalactic sources is much lower than the current *B*-mode upper limit (Planck Collaboration VI 2020).

Finally, we consider the ratio of the extragalactic foreground and CMB lensing BB power spectra (at $\ell = 1000$). This ratio is ~120 times higher than the equivalent tensor-to-sclar ratio r_{eq} at $\ell = 80$. It extends from ~10⁻³ for large-aperture experiments to ~10⁻¹ for small-aperture experiments. As is already known, ground-based large-aperture telescopes will provide the ability to delens the maps from future satellite CMB missions, such as LiteBIRD (e.g. Namikawa & Nagata 2014).

8. Conclusion

We have computed the expected level of polarised fluctuations from the shot noise of radio galaxies and DSFG and from the CIB clustering using current or updated models. Using these models, we predicted the point-source detection limits (confusion noises, in intensity) for future CMB space-based or balloon-borne experiments (IDS, PIPER, SPIDER, LiteBIRD, and PICO) and ground-based experiments (C-BASS, NEXT-BASS, QUIJOTE, AdvACTPOL, BICEP3+Keck, BICEPArray, CLASS, SO, SPT3G, and S4). These limits were computed by taking the instrument noise, the three extragalactic foregrounds, and the CMB into account. The models, as well as the pointsource detection flux limits, were validated using most recent measurements on number counts, CIB power spectra, confusion noises, and shot noise levels. As expected, we found that the confusion noise levels are mostly driven by the telescope-aperture sizes and frequency.

Assuming a constant polarisation fraction consistent with current observational results for the radio sources of $\langle \Pi^{\rm rad} \rangle = 2.8\%$, and assuming for the dusty source $\langle \Pi^{\rm IR} \rangle = 1.4\%$, we then predicted the shot noises and CIB one-halo clustering B-mode power spectra. We compared the amplitude of the different extragalactic foregrounds as a function of frequency and telescope-aperture size. We found that CIB clustering is almost negligible. The relative levels of radio and DSFG shot noises are mainly driven by the telescope sizes, which can be classified into three categories: large-aperture (≥ 6 m, i.e. SPT-3G, S4-LAT, SO-LAT, AdvActPol), medium-aperture (~1.5 m, i.e. Planck, IDS, PICO), and small-aperture (≤ 0.6 m, i.e. LiteBIRD, SPIDER, CLASS, SO-SAT, S4-SAT, BICEP-Keck) telescopes. While we have an equal contribution between radio shot noise and DSFG shot noises (+ clustering) at $v \simeq 120$ GHz for large-aperture telescopes, it reaches $v \simeq 280 \,\text{GHz}$ for small-aperture telescopes, which are thus dominated by the radio shot noise at the frequencies dedicated to the CMB measurement. González-Nuevo et al. (2005) showed that the contribution of radio source clustering to the temperature angular power spectrum is small and can be neglected if sources are not subtracted down to very faint flux limits, $S \ll 10$ mJy. However, future ground-based experiments such as S4-LAT will be able to reach flux limits of the order of 2-3 mJy. At these levels, the clustering of radio sources might not be negligible for $\ell < 30$ compared to the shot-noise level (González-Nuevo et al. 2005).

We also predict the confusion noise for SPICA B-BOP and showed that confusion could ultimately limit the sensitivity of deep polarised surveys at 200 and $350 \,\mu\text{m}$ (with the confusion noise in polarisation reached in 57 and 69 h for a 1 square degree field at 200 and $350 \,\mu\text{m}$, respectively).

Finally, we computed the equivalent tensor-to-scalar ratio (r_{eq}) of the total extragalactic contamination (radio galaxy shot noise, DSFG shot noise, and clustering) for given multipoles. At the reionisation B-bump ($\ell = 5$), the extragalactic contamination will not limit the measurements. At the recombination B-peak $(\ell = 80)$, the contamination for large-aperture telescope experiments is much below the targeted primordial r, but this is not the case for some of the small- and medium- aperture telescopes. For example for the LiteBIRD and PICO space experiments, the contamination is at the level of the 68% confidence level uncertainty on the primordial r (not considering a multi-frequency component separation that should globally decrease r_{eq}). On the other side of the multipole range, extragalactic components represent 10–20% of the CMB lensing BB power spectrum at $\ell = 1000$ for LiteBIRD. Moreover, a similar slope is observed between the extragalactic components and the CMB lensing BB power spectrum up to $\ell = 200$ and between the extragalactic components and the primordial *B*-mode power spectrum for $15 \leq \ell \leq 50$, leading to degeneracies in any model fitting. Removing this extragalactic contamination from the data is thus mandatory

for some of the small- and medium-aperture telescope experiments.

Foreground mitigation was studied for the Galactic components. We showed that it requires a multi-frequency coverage (but see Philcox et al. 2018 for a method based on anisotropy statistics, or Aylor et al. 2019 for the use of neural network). It will be difficult to apply this multi-frequency approach to extragalactic foregrounds, as the three extragalactic components are degenerated (i.e. same power spectra at the multipole of interest) and the sum of the three does not have a well-defined frequency dependency. Moreover, even if more precise polarised source counts for radio galaxies will be obtained in the near future, the variation in radio shot noise with flux limit (changing the flux cut by 30% affects the shot noise by 30%, see Table 2), together with the variability of radio sources, may prevent us from using more accurate modelling to precisely predict the shot-noise level.

Polarised Galactic foregrounds are dominated by dust and synchrotron emissions with spatial variation of their SEDs. Using a parametric maximum-likelihood approach, Errard et al. (2016) found that combinations from ground- and space-based and balloon-borne experiments can significantly improve component separation performance, delensing, and cosmological constraints over individual datasets. In particular, they reported that a combination of post-2020 ground- and space-based experiments could achieve constraints such as $\sigma_r \sim 1.3 \times 10^{-4}$ after component separation and iterative delensing. However, such results (see also e.g. Stompor et al. 2016) are often derived ignoring complexities in the Galactic foreground emission due to synchrotron and dust, and neglecting potential other contaminants such as anomalous microwave emission and extragalactic foregrounds. Moreover, they adopted component separation methods that essentially assume a model that matches the simulated foregrounds under study well. Remazeilles et al. (2016) tested some of these assumptions explicitly and reported biases in the derived value of r of more than 1σ by neglecting the curvature of the synchrotron emission law, for instance. Given their levels for some of mid- and small-aperture telescopes, extragalactic foregrounds have clearly to be considered in the component separation methods dedicated to the extraction of the CMB B-modes. For this purpose, our detailed computation of flux limits and shot-noise levels will allow including these foregrounds precisely into the input sky models.

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Appendix A: Colour corrections and unit conversions for *Planck*/HFI, ACT, SPT, and *Herschel*/SPIRE

A.1. Colour corrections

Table A.1. Colour corrections C (Eq. (A.2)) for dusty star-forming galaxies are given for two different CIB spectral energy distributions ("model" refers to the model of Béthermin et al. (2012a), while "measure" refers to the Gispert et al. (2000) fit of FIRAS measurements).

Experiment	Frequency	C ^{model} [GHz]	C^{measure}
	100	1.0759	1.0824
	143	1.0171	1.0124
Planck/HFI	217	1.1190	1.1076
,	353	1.0973	1.0941
	545	1.0677	1.0675
	857	0.9948	0.9939
IRAS	3000	0.9605	0.9446
	148	1.0720	1.0719
ACT	218	1.0422	1.0384
	277	1.0227	1.0217
	150	1.1411	1.1350
SPT	220	1.0059	1.0046
	95	1.1386	1.1525
	1200	0.9880	0.9808
Herschel/SPIRE	857	0.9887	0.9875
(extended RSRF)	600	0.9739	0.9763
	1200	1.0053	0.9945
Herschel/SPIRE	857	1.0193	1.0187
(point-source RSRF)	600	1.0469	1.0503

Notes. For SPIRE, we give the colour corrections for the two spectral responses (extended or point-source RSRF).

Following the IRAS convention, the spectral intensity data I_{ν} are often expressed at fixed nominal frequencies, assuming the source spectrum is νI_{ν} = constant (i.e. constant intensity per logarithmic frequency interval, labelled "ref" hereafter). The colour-correction factor *C* is defined such that

$$I_{\nu_0}^{\rm act} = \frac{I_{\nu_0}^{\rm ref}}{C}, \qquad (A.1)$$

where $I_{\nu_0}^{\text{act}}$ is the actual specific intensity of the sky at frequency ν_0 , $I_{\nu_0}^{\text{ref}}$ is the corresponding value given with the IRAS (Neugebauer et al. 1984) or DIRBE (Silverberg et al. 1993) convention¹³, and ν_0 is the frequency corresponding to the nominal wavelength of the band. With these definitions,

$$C = \frac{\int (I_{\nu}/I_{\nu_0})^{\text{act}} R_{\nu} d\nu}{\int (\nu_0/\nu) R_{\nu} d\nu},$$
(A.2)

where $(I_{\nu}/I_{\nu_0})^{\text{act}}$ is the actual specific intensity of the sky (SED) normalised to the intensity at frequency ν_0 , and R_{ν} is the spectral response.

A.2. Colour corrections for CIB and IR shot-noise

We give here colour corrections that are useful for joined CIB analyses in HFI, ACT, SPT, and *Herschel*/SPIRE. To have an

Table A.2. MJy sr⁻¹[νI_{ν} = constant] to K_{CMB} unit conversion.

Experiment	Frequency	MJy sr ⁻¹ [νI_{ν} = constant] $K_{\rm CMB}^{-1}$
	857	2.288
	545	57.980
	353	287.228
Planck/HFI	217	483.485
	143	371.658
	100	244.059
	70	133.69
	44	56.82
	30	24.33
	148	401.936
ACT	218	485.311
	277	431.584
	95	234.042
SPT	150	413.540
	220	477.017
	1200	3.0568×10^{-2}
Herschel/SPIRE	857	2.124
(extended RSRF)	600	41.275

Notes. To convert an intensity in K_{CMB} into an equivalent specific intensity MJy sr⁻¹, the original intensity has to be multiplied by the factors given in the table.

Table A.3. y_{SZ} to K_{CMB} unit conversion.

Experiment	Frequency	$y_{SZ} K_{\rm CMB}^{-1}$		
	857	0.0383		
	545	0.0692		
Planck/HFI	353	0.1611		
	217	5.142		
	143	-0.3594		
	100	-0.2482		
	148	-0.390		
ACT	218	9.16(*)		
	277	0.379		
	95	-0.243		
SPT	150	-0.416		
	220	9.44		
	1200	0.0240		
Herschel/SPIRE	857	0.0365		
(extended RSRF)	600	0.0646		

Notes. To convert an intensity in K_{CMB} to y_{SZ} , the original intensity has to be multiplied by the factors given in the table. ^(*)This number varies by about 10% w.r.t. to the boundaries of the bandpass taken in the integrals.

idea of the errors linked to the SED used to compute *C*, we used two different CIB SEDs,

- from Gispert et al. (2000) fit of FIRAS measurements
- from Béthermin et al. (2012a) empirical model of galaxy evolution.

We recommend using the CIB from Béthermin et al. (2012a) as it comes from a unified model based on our current understanding of the evolution of main-sequence and starburst galaxies. It reproduces all recent measurements of galaxy counts from the mid-IR to the radio, including counts per redshift slice. It is probably more accurate than the FIRAS measurements. Colour

¹³ The DIRBE and IRAS data products give $I_{\nu_0}(\nu I_{\nu} = constant)$.

Table A.4. Factors to convert the CIB intensity (in Jy/sr with the convention $vI_v = \text{constant}$) into the HFI, ACT, and SPT bandpasses (see Eqs. (A.3) and (A.5)). v_1 and v_2 are given in the first column and first line, respectively (e.g. $K(v_1, v_2) = K(857, 545) = 1.989$.

		Planck/HFI					ACT			SPT			
		857	545	353	217	143	100	148	218	277	95	150	220
	857	1	1.989	5.712	24.155	97.650	269.51	83.00	25.50	12.43	294.03	75.08	25.62
	545		1	2.872	12.15	49.10	135.52	41.74	12.82	6.25	147.85	37.75	12.88
HFI 353 217 143 100	353			1	4.229	17.10	47.18	14.53	4.465	2.176	51.48	13.14	4.485
	217				1	4.043	11.16	3.436	1.056	0.5146	12.17	3.108	1.061
	143					1	2.760	0.8500	0.2612	0.1273	3.011	0.7688	0.2624
	100						1	0.3090	0.09463	0.046121	1.090	0.2786	0.09506
ACT	148							1	0.3073	0.1498	3.542	0.9045	0.3087
	218								1	0.4874	11.53	2.944	1.005
	277									1	23.66	6.040	2.061
SPT	95										1	0.2553	0.08713
	150											1	0.3413
	220	•••	•••	•••					•••	•••			1

Notes. The factors were computed using the Béthermin et al. (2012a) CIB SED. Some factors can be deduced from combinations of others. We give all of them for convenience.

corrections C are given in Table A.1. We can use the same colour corrections for the star-forming galaxy shot noise and the clustered power spectrum (as the SEDs are very similar).

A.3. Colour corrections for radio shot noise

For the radio galaxy shot noise SED we can use a power law $S_{\nu} \propto \nu^{\alpha}$, with $\alpha = -0.5/-0.6$. This is the average spectral index for radio sources that mainly contribute to the shot-noise power spectrum. With this SED, we find that the colour corrections are all lower than 0.7% for $20 \le \nu \le 857$ GHz. We can thus neglect them.

A.4. Unit conversions (tSZ, K_{CMB} , MJy sr⁻¹)

In unit conversion, data are presented in a different unit, but remain consistent with a given SED (e.g. MJy sr⁻¹ can be expressed as an equivalent brightness in *K*). With colour correction, data are expressed with respect to a different assumed SED at the same reference frequency. Changing from $K_{\rm CMB}$ to MJy sr⁻¹ with a different spectral index involves both a unit conversion and a colour correction. We give some unit conversions for SPT, ACT, and HFI in Tables A.2 and A.3. Spectral responses are the official 2013 released ones for *Planck*/HFI. For ACT and SPT, they have been provided by the teams. For SPT, we use the SPT-SZ bandpasses.

A.5. Converting CIB power spectra between HFI, ACT, SPT, and SPIRE

The purpose here is to convert the measurement through one bandpass into a measurement as it would be obtained through another bandpass (often close in frequency, e.g. HFI at 143 GHz versus SPT at 150 GHz). This means that we wish to find K such that

$$I_{\nu_{0_1}}^{\text{ref}} = K I_{\nu_{0_2}}^{\text{ref}}.$$
 (A.3)

For clarity, we write I_1 and I_2 the fiducial monochromatic flux densities from spectral response 1 and 2 (with the convention νI_{ν} = constant) at their respective reference frequencies ν_1 and ν_2 . Combining Eq. (A.1) and A.2 gives

$$I_{\nu_0}^{\text{ref}} = \frac{1}{\nu_0} \times \frac{\int I_{\nu}^{\text{act}} R_{\nu} \, d\nu}{\int R_{\nu} / \nu \, d\nu}.$$
 (A.4)

It then follows

$$K = \frac{I_{1}^{\text{ref}}}{I_{2}^{\text{ref}}} = \frac{\nu_{2}}{\nu_{1}} \times \frac{\int R_{2}/\nu \, d\nu}{\int R_{1}/\nu \, d\nu} \times \frac{\int R_{1} I_{\nu}^{\text{act}} \, d\nu}{\int R_{2} I_{\nu}^{\text{act}} \, d\nu},$$
(A.5)

where R_1 and R_2 are the normalised spectral responses 1 and 2, respectively. Values for *K* for HFI, ACT, and SPT are given in Table A.4. For HFI 545 and 857 GHz and *Herschel*/SPIRE 500 and 350 μ m channels, *K*(545 GHz, 500 μ m) = 0.899808 and *K*(857 GHz, 350 μ m) = 1.00685.

We can note that K(143, 148) and K(143, 150) are <1 because the HFI 143 GHz bandpass is sensitive to lower frequencies than ACT 148 GHz and SPT 150 GHz.

Example of the use of K factors. the HFI-alone likelihood gives the best C_{ℓ} CIB amplitude at 143 GHz in μK_{CMB} . To convert it for ACT at 148 GHz into μK_{CMB} follows

$$C_{\ell}^{148} = C_{\ell}^{143} \times 371.658^2 \times \frac{1}{0.8500^2} \times \frac{1}{401.936^2}.$$
 (A.6)