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**1 Submesoscales enhance storm-driven vertical mixing**  
**2 of nutrients: insights from a biogeochemical large**  
**3 eddy simulation**

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4 **Abstract.** Storms deepen the mixed layer, entrain nutrients from the py-  
5 cnocline, and fuel phytoplankton blooms in mid-latitude oceans. However,  
6 the effects of oceanic submesoscale (0.1-10 km horizontal scale) physical het-  
7 erogeneity on the physical-biogeochemical response to a storm are not well  
8 understood. Here, we explore these effects numerically in a Biogeochemical  
9 Large Eddy Simulation (BLES), where a four-component biogeochemical model  
10 is coupled with a physical model that resolves some submesoscales and some  
11 smaller turbulent scales (2 km to 2 m) in an idealized storm forcing scenario.  
12 Results are obtained via comparisons to BLES in smaller domains that do  
13 not resolve submesoscales and to one-dimensional column simulations with  
14 the same biogeochemical model, initial conditions, and boundary conditions  
15 but parameterized turbulence and submesoscales. These comparisons show  
16 different behaviors during and shortly after the storm. During the storm, re-  
17 solved submesoscales double the vertical nutrient flux. The vertical diffusiv-  
18 ity is increased by a factor of 10 near the mixed layer base, and the mixing-  
19 induced increase in potential energy is double. Resolved submesoscales also  
20 enhance horizontal nutrient and phytoplankton variance by a factor of 10.  
21 After the storm, resolved submesoscales maintain higher nutrient and phy-  
22 toplankton variance within the mixed layer. However, submesoscales reduce  
23 net vertical nutrient fluxes by 50% and nearly shut off the turbulent diffu-  
24 sivity. Over the whole scenario, resolved submesoscales double storm-driven  
25 biological production. Current parameterizations of submesoscales and tur-

26 bulence fail to capture both the enhanced nutrient flux during the storm and  
27 the enhanced biological production.

## 1. Introduction

28 In the mid-latitudes, strong winds associated with storms intermittently enhance upper-  
29 ocean turbulence and hence vertical mixing of nutrients and phytoplankton [e.g., Marra  
30 et al., 1990; Rumyantseva et al., 2015; Carranza & Gille, 2015; Nicholson et al., 2016].  
31 These storm events can cause significant intra-seasonal variability of upper-ocean phyto-  
32 plankton concentrations and therefore significant divergence from the mean seasonal cycle  
33 [e.g., Waniek, 2003; Thomalla et al., 2011]. These variations in phytoplankton phenology  
34 impact the higher trophic levels of marine ecosystems [e.g., Cushing, 1990; Platt et al.,  
35 2003].

36 An unresolved question is to what degree quasi two-dimensional ocean submesoscales  
37 (defined here descriptively to refer to features with horizontal length scales from 0.1 to  
38 10 km, and small aspect ratio) interact with smaller-scale wind-driven three-dimensional  
39 upper-ocean turbulence ( $< 100$  m) to modify the physical-biogeochemical response to a  
40 storm. This study addresses this question in the oceanic context of a fairly typical autumn  
41 storm that was observed in the mid-latitude North Atlantic at  $48.78^{\circ}\text{N}$ ,  $16.38^{\circ}\text{W}$  during  
42 the OSMOSIS project [e.g., Rumyantseva et al., 2015; Painter et al., 2016] by showing how  
43 submesoscales impact net (submesoscale + turbulent) vertical nutrient flux and resulting  
44 biological production during and shortly after the passage of the storm in an ocean model.

45 In the absence of storms, prior work has shown that submesoscales can both enhance  
46 vertical tracer fluxes [e.g., Mahadevan & Archer, 2000; Lévy et al., 2001; Capet et al.,  
47 2008b] or suppress vertical fluxes by restratifying the ocean mixed layer or reducing the  
48 depth of the surface mixing layer in ocean models [e.g., Boccaletti et al., 2007; Fox-Kemper

49 et al., 2008; Mahadevan et al., 2012; Bachman et al., 2017b]. Enhanced vertical fluxes, for  
50 example, can induce a net increase in the nutrient delivery to the well-lit euphotic layer  
51 and therefore a net increase in phytoplankton growth in oligotrophic oceans [Mahadevan  
52 & Archer, 2000; Lévy et al., 2001].

53 During storms, winds can increase the vertical nutrient flux (thereby enhancing net  
54 phytoplankton growth in oligotrophic oceans), both by enhancing submesoscale vertical  
55 velocities [e.g., Mahadevan & Tandon, 2006; Capet et al., 2008a; Thomas et al., 2008;  
56 Mahadevan et al., 2008; Lévy et al., 2009; Brannigan, 2016] and via entrainment/mixing  
57 in submesoscale fronts [e.g., Lévy et al., 2009; Whitt et al., 2017b]. In addition, winds  
58 can enhance or suppress the mixed layer restratification rate depending on the magnitude  
59 and orientation of the wind stress relative to the horizontal density gradient in the ocean  
60 mixed layer and the frequency content of the wind [Thomas & Ferrari, 2008; Mahadevan  
61 et al., 2010; Long et al., 2012; Whitt et al., 2017a, b] as well as the surface wave field [Li  
62 et al., 2012; Haney et al., 2015]. For reviews of recent work on submesoscale impacts on  
63 biogeochemistry, see Klein & Lapeyre [2009]; Lévy et al. [2012]; Mahadevan [2016]; Lévy  
64 et al. [2018].

65 These conclusions are essentially based on regional and process-study primitive equation  
66 ocean models, in which submesoscales are at least partially resolved but small-scale turbu-  
67 lence is unresolved and parameterized. It is not clear whether submesoscale interactions  
68 with turbulent scales, and therefore the net impacts of submesoscales on biogeochemistry  
69 during storms, are realistically represented in such models.

70 Large Eddy Simulations (LES) that explicitly resolve some submesoscales as well as  
71 smaller-scale turbulence have started providing additional insights into the interactions

72 between submesoscales and turbulence. For example, such studies have shown energy  
73 transfers from submesoscales to small turbulent scales via submesoscale instabilities  
74 [e.g., Thomas & Taylor, 2010; Skillingstad & Samelson, 2012; Bachman et al., 2017a;  
75 Skillingstad et al., 2017]. If turbulent scale motions are more energetic as a result, this  
76 may enhance vertical fluxes. In a recent paper, Whitt & Taylor [2017] used LES to explore  
77 the physical response of submesoscales coupled with small-scale turbulence to a storm.  
78 Their simulations showed that energetic wind-driven submesoscale motions non-uniformly  
79 re-stratified the mixed layer while deepening the reach of boundary-layer turbulence during  
80 the storm. This result ensued from spatial heterogeneity in stratification and turbulence.

81 Here, we build on this previous study [Whitt & Taylor, 2017] by describing the in-  
82 fluence of submesoscales coupled with small-scale turbulence on biogeochemistry during  
83 and shortly after a strong storm using biogeochemical LES (BLES) (for some other re-  
84 cent examples of BLES without submesoscales, see Lewis et al. [2017] or Brereton et al.  
85 [2018]; for an LES with submesoscales and a plankton model but without nutrients or  
86 wind, see Taylor [2016], or for submesoscales and passive tracers under weak atmospheric  
87 forcing, see Smith et al. [2016]). Results are obtained by comparing simulations in which  
88 submesoscales are present or absent. These results highlight how submesoscale and smaller-  
89 scale turbulent nutrient fluxes are modified by the interaction between submesoscale and  
90 smaller-scale turbulence, and how this impacts biological production and nutrient and  
91 phytoplankton vertical and horizontal distributions. In a second step, we evaluate the ef-  
92 ficacy of existing commonly used parameterizations of submesoscales [Fox-Kemper et al.,  
93 2008] and small-scale turbulence [Large et al., 1994] in a column model against the BLES  
94 benchmarks. We find that the nutrient flux by small-scale turbulence is enhanced by

95 submesoscale interactions during the storm but suppressed shortly after the storm, with  
96 the consequence of an increased net biological production, and that the commonly used  
97 parameterizations fail at capturing these effects. These results motivate future physi-  
98 cal/biogeochemical theory and parameterization development, which can be validated by  
99 comparison with these BLES benchmarks and provide a framework for interpreting the  
100 simulation results, as well as additional BLES simulations to more fully quantify the sen-  
101 sitivity of the simulation results to the parameters that define the numerical experiments.

## 2. Methods

### 2.1. Models

#### 102 2.1.1. BLES setup

103 The BLES resolves the majority of the variance associated with three-dimensional fluid  
104 motions and is used to evaluate the impact of submesoscale/turbulent-scale interactions  
105 on biogeochemistry. The rotating stratified Boussinesq equations are solved on an  $f$ -  
106 plane without surface wave effects over horizontal wavelengths ranging from about 2 km  
107 to about 4 m, which include both submesoscales and smaller-scale turbulence. The nu-  
108 merical model, spatial domain and physical initial condition (of density, velocity, and  
109 pressure) are as described in Whitt & Taylor [2017] [see also Taylor, 2008]. Briefly, the  
110 model solves the Boussinesq equations together with the evolution equations for the four  
111 reactive biogeochemical tracers using a low-storage third order Runge-Kutta time march-  
112 ing method, a pseudospectral method to represent horizontal derivatives, and second or-  
113 der centered differences to represent vertical derivatives. Fluxes of momentum associated  
114 with subgrid-scale turbulence with wavelengths smaller than about 4 m are parameter-  
115 ized using a modified Smagorinsky model [Kaltenbach et al., 1994]. Subgrid-scale tracer



fluxes also depend on a variable subgrid-scale Prandtl number, which is parameterized in terms of the grid-scale gradient Richardson number as described in Whitt & Taylor [2017]. Subgrid-scale Schmidt numbers associated with biogeochemical tracers are set equal to the subgrid-scale Prandtl number.

Two configurations of the BLES are compared, a frontal zone configuration [e.g., Taylor & Ferrari, 2010; Thomas & Taylor, 2010; Skillingstad et al., 2017; Callies & Ferrari, 2018] (LES,F) with submesoscales, and a configuration without a front (LES,NF) where submesoscales are excluded. The LES,NF configuration captures the conventional effects of small-scale turbulence [e.g., McWilliams & Sullivan, 2000; Skillingstad et al., 2000; Pham & Sarkar, 2017]. Differences between the two configurations quantify how submesoscales modify these conventional effects. In the LES,F configuration, the flow is expressed as a periodic (in  $x$  and  $y$ ) perturbation from a fixed mean horizontal density gradient  $\langle M^2 \rangle_{x,y} = \langle \frac{g}{\rho_0} \frac{\partial \rho}{\partial y} \rangle_{x,y} = -\langle \frac{\partial b}{\partial y} \rangle_{x,y} = 5 \times 10^{-8} \text{ s}^{-2}$  and thermal wind shear  $\langle M^2 \rangle_{x,y}/f = 5 \times 10^{-4} \text{ s}^{-1}$  that are qualitatively representative of the OSMOSIS site during September of 2012. Here,  $\langle \rangle_{x,y}$  denotes a horizontal average,  $\rho$  is the density,  $\rho_0 = 1026 \text{ kg/m}^3$  is the reference density,  $g$  is the acceleration due to gravity, the buoyancy  $b = -g\rho/\rho_0$ , and  $f = 10^{-4} \text{ s}^{-1}$  is the Coriolis frequency. The chosen  $\langle M^2 \rangle_{x,y} = 5 \times 10^{-8} \text{ s}^{-2}$  is representative of roughly the 75th percentile of all horizontal buoyancy gradients  $|\nabla_h b|$  observed at 2 to 5 km length scales by ocean gliders during autumn at the OSMOSIS site [Thompson et al., 2016]. This means the chosen horizontal density gradient is strong but typical of the region and season; stronger gradients are expected roughly a quarter of the time and weaker gradients are expected roughly three quarters of the time. Hence, although we sometimes refer to the mean horizontal density gradient as a “front,” the

139 gradient is thought to be fairly typical of the open ocean and, in particular, is two orders  
140 of magnitude weaker than strong submesoscale fronts that are occasionally observed in  
141 boundary currents [*D'Asaro et al.*, 2011].

142 The turbulent physical initial condition at the onset of the storm with finite amplitude  
143 submesoscale eddies (Fig. 1) is obtained from a 3-day spin-up simulation that is initialized  
144 with low-amplitude red noise in the frontal zone with a vertical density profile based on  
145 the observed density profile above the Porcupine Abyssal Plain during September 2012.  
146 The spin-up simulation is forced by a constant air-sea buoyancy flux  $B_A = 3 \times 10^{-9} \text{ m}^2/\text{s}^3$   
147 (equivalent to about  $10 \text{ W}/\text{m}^2$  cooling) that is chosen to balance the restratifying effects  
148 of submesoscale mixed layer baroclinic instabilities, as discussed in Whitt & Taylor [2017]  
149 [see also Mahadevan et al., 2010, 2012]. At the start of the spin-up simulation, the fastest  
150 growing mixed layer baroclinic instability has a horizontal length scale of about 985 m  
151 and a growth timescale of about 13 hours, as discussed in Whitt & Taylor [2017] [see also  
152 Stone, 1966]. The domain size is chosen so that it contains two wavelengths of the fastest  
153 growing baroclinic mixed layer instability mode in each horizontal dimension. Hence, the  
154 domain is 1970 m by 1970 m by 80 m and covered by a grid with 1024 by 1024 by 160  
155 points that achieves a uniform resolution of 1.9 m by 1.9 m by 0.5 m in  $x$  (along-front) and  
156  $y$  (across-front) and  $z$  (vertical), respectively. As a result, the initial perturbations grow  
157 and the physical fields have strong submesoscale variability at the onset of the storm, as  
158 shown in Fig. 1.

159 The LES,NF configuration is identical to the LES,F configuration except that the do-  
160 main is smaller (492.5 m by 492.5 m by 80 m) and  $\langle M^2 \rangle_{x,y} = 0$ . In particular, this analog  
161 configuration uses the same code, the same grid resolution, the same surface boundary

162 conditions, and the same mean density profile  $\langle \rho \rangle_{x,y}(z)$  at day 0 as the large domain.  
163 But, there is no initial submesoscale variability. Rather, the LES,NF configuration is ini-  
164 tialized with low-amplitude white noise in the velocity components and no initial density  
165 perturbations.

### 166 **2.1.2. Storm forcing**

167 The storm forcing is represented by an idealized spatially-uniform but time-dependent  
168 surface stress that points  $45^\circ$  to the right of the geostrophic shear; it is inspired by an  
169 observed storm during September 24-26, 2012 at the OSMOSIS site [Rumyantseva et al.,  
170 2015]. The idealized stress ramps up linearly over two days to a maximum amplitude of  
171  $0.6 \text{ N/m}^2$  and then ramps down linearly to zero during the third day (as shown in Fig.  
172 2). Sensitivity studies with a maximum stress of  $0.3 \text{ N/m}^2$  are qualitatively similar and  
173 presented in the supplemental material (see Table 1 for a full list of simulations). Unless  
174 otherwise noted, the text refers to the cases with the stronger winds. The direction, magni-  
175 tude and duration of the wind forcing are chosen to be similar to the observed amplitude,  
176 direction and duration of the wind stress during the storm based on NCEP reanalysis  
177 winds, satellite sea surface temperature imagery, and results reported in Rumyantseva  
178 et al. [2015] and Buckingham et al. [2017].

179 In the presence of a mean horizontal buoyancy gradient at the surface (as in LES,F), the  
180 Ekman flow can produce a buoyancy tendency in the mixed layer via horizontal advection.  
181 For example, if the wind stress includes a down-front component, meaning a component  
182 in the direction of the thermal wind shear  $\mathbf{k}/f \times \nabla_h b$ , then the Ekman flow tends to  
183 reduce the mixed layer buoyancy, energize submesoscale symmetric instabilities aligned  
184 parallel to the front, and may cause entrainment. But, if a component of the wind is up

185 front, meaning opposite to the direction of the thermal wind shear, then the Ekman flow  
 186 tends to increase the mixed layer buoyancy and may cause subduction [Brannigan, 2016;  
 187 Whitt et al., 2017a, b]. In the simulations presented here, the wind includes a down-front  
 188 component, and the horizontally-averaged Ekman buoyancy flux  $EBF = \tau_x \langle M^2 \rangle_{x,y} / \rho_0 f$ ,  
 189 which is driven by the down-front component of the wind stress  $\tau_x$ , reaches maximum  
 190 magnitudes of  $2 \times 10^{-7} \text{ m}^2/\text{s}^3$  (or about  $660 \text{ W}/\text{m}^2$  Ekman heat flux) when the magnitude  
 191 of the stress is  $0.6 \text{ N}/\text{m}^2$  (Fig. 2). It may be noted that the horizontally-averaged EBF is  
 192 independent of the interior evolution of the simulations, because the stress is a spatially-  
 193 uniform surface boundary condition (and therefore uncorrelated with any interior spatial  
 194 variability of density), and the mean horizontal density gradient  $\langle M^2 \rangle_{x,y}$  is an externally-  
 195 imposed constant.

196 Following the storm, the simulations continue for about 3 days without wind stress. For  
 197 simplicity, the air-sea buoyancy flux is held constant at  $B_A = 3 \times 10^{-9} \text{ m}^2/\text{s}^3$  (or about  
 198  $10 \text{ W}/\text{m}^2$  heat loss) during and after the simulated storm.

199 It may be noted that the simulations presented here do not have realistic air-sea buoy-  
 200 ancy loss, which is usually enhanced during storms. That is because, although we have run  
 201 simulations with more realistic buoyancy loss (not shown), the stronger buoyancy loss has  
 202 little impact on the results. A wind stress of  $0.6 \text{ N}/\text{m}^2$  is a far stronger source of energy for  
 203 turbulent entrainment in a 40 m deep mixed layer than the roughly  $200 \text{ W}/\text{m}^2$  net heat  
 204 loss observed by Rumyantseva et al. [2015] (as can be inferred from scaling arguments  
 205 [Kraus and Turner, 1967; Pollard et al., 1972] and observations [Thomas et al., 2016]).  
 206 Further, even a realistic surface buoyancy flux would be about a factor of 3 smaller than  
 207 the EBF. Using the observationally-supported scalings reported in Thomas et al. [2016],

208 the depth-integrated dissipation of turbulent kinetic energy should have contributions of  
 209 about  $6 \times 10^{-5} \text{ m}^3/\text{s}^3$  from wind and  $8 \times 10^{-6} \text{ m}^3/\text{s}^3$  from EBF during peak wind. That  
 210 is to say, the direct injection of energy by the wind during the storm is the dominant  
 211 source of energy for the turbulence. Based on these scalings, the turbulence dynamics  
 212 are not expected to differ much between the various scenarios presented here, nor is the  
 213 biogeochemical response.

### 214 2.1.3. Biogeochemical model

215 The biogeochemical model is a modified version of the NPZD (nutrient, phytoplankton,  
 216 zooplankton, detritus) model implemented by Whitt et al. [2017b] and Whitt et al. [2017a],  
 217 which is based on classic models like that of Fasham et al. [1990] and a previous NPZD  
 218 implementation by Powell et al. [2006]. The biogeochemical model equations are:

$$\begin{aligned}
 219 \quad \frac{DN}{Dt} &= -UP + \gamma_n GZ + \delta D + \nabla \cdot ((\kappa_{SGS} + \kappa_0) \nabla N) - \beta(N - N_{80}), \\
 220 \quad \frac{DP}{Dt} &= UP - \sigma_d P - GZ + \nabla \cdot ((\kappa_{SGS} + \kappa_0) \nabla P), \\
 221 \quad \frac{DZ}{Dt} &= (1 - \gamma_n)GZ - \zeta Z - \hat{\zeta} Z^2 + \nabla \cdot ((\kappa_{SGS} + \kappa_0) \nabla Z), \\
 222 \quad \frac{DD}{Dt} &= \sigma_d P + \zeta Z + \hat{\zeta} Z^2 - \delta D + w_d \frac{\partial D}{\partial z} + \nabla \cdot ((\kappa_{SGS} + \kappa_0) \nabla D), \\
 223 \quad G &= R(1 - e^{-\Lambda P}), \\
 224 \quad U &= \frac{V_m N}{k_N + N} \frac{\alpha I}{\sqrt{V_m^2 + \alpha^2 I^2}}, \\
 225 \quad I &= I_0 \exp(k_w z),
 \end{aligned} \tag{1}$$

226 where  $D/Dt = \partial/\partial t + \mathbf{u} \cdot \nabla$  is the material derivative, the subgrid-scale diffusivity is given  
 227 by  $\kappa_{SGS}$  (which varies in time and space), the molecular diffusivity is set to a constant  
 228  $\kappa_0 = 10^{-6} \text{ m}^2/\text{s}$ , and the constant parameters are listed in Table 2.

229 The biogeochemical initial conditions (Fig. 3), which are imposed as horizontally-  
 230 uniform fields at  $t = 0$  d, are from an equilibrium (i.e., steady state) solution to the  
 231 biogeochemical model equations with the parameters in Table 2 and a constant verti-  
 232 cal diffusivity  $\kappa_{SGS} + \kappa_0 = 2 \times 10^{-5}$  m<sup>2</sup>/s. The initial  $Z$  and  $D$  profiles (not shown)  
 233 have a similar vertical structure to  $P$ , with maximum concentrations of 0.22 and 0.35  
 234 mmol/m<sup>3</sup> respectively. This equilibrium solution is calculated numerically by running  
 235 one-dimensional simulations of the biogeochemical model equations for 10 years with a  
 236 one-dimensional NPZD model described earlier [Whitt, 2017; Whitt et al., 2017b, a]. In  
 237 addition, numerical experimentation suggests that the resulting equilibrium profile is ef-  
 238 fectively independent of the initial conditions of  $N$ ,  $P$ ,  $Z$ , and  $D$  for the parameter set in  
 239 Table 2.

240 Due to the construction of the biogeochemical initial condition, the horizontally-  
 241 averaged nutrient  $\langle N \rangle_{x,y}$  and phytoplankton  $\langle P \rangle_{x,y}$  profiles have strong vertical gradients  
 242 throughout the top 60 m at day 0 (Fig. 3). In the upper 30 m, these strong vertical bio-  
 243 geochemical gradients contrast with weak vertical density gradients, which are relatively  
 244 permissive of turbulent mixing compared to the pycnocline below. Hence, shortly after  
 245 the simulations begin, storm-driven turbulence drives rapid vertical mixing and homoge-  
 246 nization of the mean biogeochemical concentrations over the top 30 m.

247 To reflect the idealized nature of the simulations, we refer to the simulated nutrient as  
 248 “nutrient” throughout the paper. In addition, it is not our intention to validate the model  
 249 or exactly reproduce observations here. However, the biogeochemical model parameters  
 250 in Table 2 are tuned within reasonable ranges (see the appendix) so that the chosen  
 251 initial equilibrium, which reflects the parameters, has a nutrient profile that is similar to

252 the observed dissolved silica profile in autumn 2012 above the Porcupine Abyssal Plain on  
253 September 21-22, 2012 a few days before the storm (Fig. 3 (b)). The subsurface maximum  
254 in the initial phytoplankton profile is also qualitatively consistent with observations of  
255 vertical profiles of chlorophyll fluorescence (Fig. 3 (a)).

#### 256 **2.1.4. Column set up in ROMS**

257 In order to assess the effectiveness of some existing ocean model parameterizations at  
258 representing the horizontally-averaged behavior of LES, results from the BLES models are  
259 compared to results from a one-dimensional column model implemented in the regional  
260 ocean modeling system (ROMS+NPZD) [e.g., Powell et al., 2006; Whitt et al., 2017b].  
261 Two ROMS configurations are used that can be viewed as parameterized analogues of  
262 the two LES configurations, one with parameterized submesoscales (ROMS,F) and one  
263 with no submesoscales (ROMS,NF). In the ROMS,NF configuration, the physical effects  
264 of turbulence are parametrized using the conventional KPP mixing scheme [Large et al.,  
265 1994], as implemented in the public version of ROMS (myroms.org). There are no effects  
266 of submesoscales and no horizontal density gradient, i.e.  $\langle M^2 \rangle_{x,y} = 0$ . In the ROMS,F  
267 configuration, the physical effects of both turbulence and submesoscales are parametrized  
268 rather than explicitly resolved, and the same mean horizontal density gradient as in the  
269 LES,F experiments is used, i.e.  $\langle M^2 \rangle_{x,y} = 5 \times 10^{-8} \text{ s}^{-2}$ .

270 In all column model experiments, ROMS solves for the time evolution of horizontal  
271 momentum, temperature (which is equivalent to density via a linear equation of state),  
272 and biogeochemical tracers on the same uniform vertical grid with 160 levels and 0.5  
273 m resolution that is used in the LES. Vertical fluxes are computed using a conservative

274 parabolic spline method. In addition, the column model is forced by the same surface  
 275 momentum and buoyancy fluxes and solves the same biogeochemical model equations.

276 The parameterizations for small-scale turbulence and for submesoscales are implemented  
 277 in the column version of ROMS as follows. First, the KPP surface layer scheme is modified  
 278 so that the boundary layer depth, and thereby the diffusivity and viscosity profiles, are  
 279 defined based on a bulk Richardson number that depends on the constant geostrophic  
 280 shear  $\langle M^2 \rangle_{x,y}/f$  as well as the evolving ageostrophic shear. Second, terms are added to  
 281 the right side of the temperature equation (which is also the density equation since we  
 282 are using linear equation of state) to represent horizontal advection of the background  
 283 lateral temperature gradient, including an extra term of the form  $v\langle M^2 \rangle_{x,y}/g\alpha$  where  $\alpha$  is  
 284 a constant thermal expansion coefficient. This extra advection term includes the Ekman  
 285 buoyancy flux EBF defined earlier. In addition, a second term is added to the right hand  
 286 side of the temperature equation of the form  $v^*\langle M^2 \rangle_{x,y}/g\alpha$ , where  $v^*$  is defined below.  
 287 This second new term in the temperature equation represents the restratifying effect of  
 288 submesoscale mixed layer baroclinic instabilities via the parameterization of Fox-Kemper  
 289 et al. [2008] (FFH), in which the temperature tendency associated with this restratifying  
 290 effect is expressed as  $-\nabla \cdot (\mathbf{u}^*T)$ , where

$$291 \quad v^* = -C \frac{MLD_3^2 \langle M^2 \rangle_{x,y}}{|f|} \frac{\partial \mu(z)}{\partial z} \quad (2)$$

292 and the other components of the bolus velocity vector  $\mathbf{u}^*$  are equal to zero in this case.  
 293 The time-dependent mixed layer depth  $MLD_3$  in (2) is defined in section 2.2.2 below.  
 294 The time-dependent vertical structure function  $\mu(z)$ , which depends on  $MLD_3$  as well as  
 295  $z$ , is given by (39) of FFH. The coefficient  $C = 0.06$ , which FFH find to be the best fit in a  
 296 series of simulations without diurnal convection or wind, but this parameter  $C$  is subject



297 to some uncertainty [e.g., Bachman & Taylor, 2016; Taylor, 2016; Callies & Ferrari, 2018].  
298 Finally, the convergence of the viscous vertical flux of geostrophic momentum is added  
299 to the tendency. This flux of geostrophic momentum is calculated like the viscous flux  
300 of ageostrophic momentum, by multiplying the same vertically and temporally variable  
301 viscosity coefficients to the constant background geostrophic shear profile.

## 2.2. Model diagnostics

### 2.2.1. Submesoscales and smaller-scale turbulence: scale separation

302  
303 Throughout this paper, the term submesoscale is used descriptively to refer to fea-  
304 tures of the velocity, density, and tracer fields that reside primarily in the ocean mixed  
305 layer with characteristic horizontal length scales of 0.1-10 km, and, unless stated other-  
306 wise, does not imply any particular physical process. In the context considered in this  
307 paper—the mid-latitude North Atlantic during autumn—this definition implies that sub-  
308 mesoscales have horizontal scales that are larger than the mixed layer depth, which is  
309 generally 10-100 m. Therefore, submesoscales have small aspect ratios and are distinct  
310 from conventional mixed layer turbulence, which is typically composed of features with  
311 horizontal wavelengths of the same order as or smaller than the mixed layer depth (i.e.,  
312  $\lesssim 0.1$  km horizontal scales) and order-one aspect ratios. Since some simulations reveal  
313 a change in the slope of kinetic energy and tracer spectra at a wavelength slightly larger  
314 than the mixed layer depth [Hamlington et al., 2014; Smith et al., 2016; Whitt & Taylor,  
315 2017], we define a separation at the horizontal wavelength of 150 m to separate smaller  
316 turbulence from larger submesoscales in the computation of the variances and vertical  
317 fluxes [the rationale behind this particular choice is discussed in Whitt & Taylor, 2017].  
318 For example, the total vertical nutrient flux  $\int \hat{w}(k) \hat{N}^*(k) dk$  is separated into its subme-

319 soscale and turbulent parts, using a separating wavenumber  $1/150$  cyc/m. The results  
 320 presented here do not change qualitatively if this separation wavenumber is increased or  
 321 decreased by a factor of two. Hence, we say the LES,F scenarios in the larger 2 km domain  
 322 contain submesoscales, and we say the LES,NF scenarios in the smaller 0.5 km domain  
 323 do not contain submesoscales (see Table 1 for a list of simulations).

### 324 2.2.2. Mixed-layer depths

325 Two different density thresholds are used to define two mixed-layer depths [see Brain-  
 326 erd & Gregg, 1995]: The first  $MLD_{05}$  is defined by a relatively small density threshold  
 327  $\Delta\langle\rho\rangle_{x,y} = 0.005$  kg/m<sup>3</sup> to approximately capture the subtle effect of intermittent strat-  
 328 ification within the turbulent boundary layer. Conversely, the second  $MLD_3$  is defined  
 329 by a more conventional density threshold  $\Delta\langle\rho\rangle_{x,y} = 0.03$  kg/m<sup>3</sup> to approximately capture  
 330 the depth that intermittent boundary-layer turbulence reaches. Unless otherwise noted,  
 331 “mixed layer depth” or “mixed layer base” refers to the more conventional  $MLD_3$ .

### 332 2.2.3. Net community production

333 Net community production  $NCP$  is equal to production by autotrophs minus respiration  
 334 by the entire community over a given time period. In this model,  $NCP = \int UP -$   
 335  $\gamma_n GZ - \delta D dt$ , that is the time integral of the reaction terms on the right hand side  
 336 of the  $N$  evolution equation.  $NCP$  has not been diagnosed online during the model  
 337 integration and was computed offline from changes in  $N$ . More precisely, the reduction in  
 338 full-column-integrated  $\langle N \rangle_{x,y}$  during the storm is equal to the storm-driven net community  
 339 production  $\langle NCP \rangle_{x,y}$ . Indeed, if the  $N$  evolution equation is integrated over the entire  
 340 model domain, then the advective and diffusive terms go to zero. In addition, since the  
 341 nutrient concentration at the bottom grid cell of the domain (80 m) is not modified by the

342 storm, the nutrient restoring tendency at the bottom grid cell does not induce a change in  
 343 full-column-integrated  $N$  during the storm. Hence, any simulated changes in full-column-  
 344 integrated  $\langle N \rangle_{x,y}$  during the storm are caused by the reactive tendency terms in the  $N$   
 345 equation, i.e.  $\langle NCP \rangle_{x,y}$ . Unless otherwise noted, column-integrated henceforth implies  
 346 integration over the full model domain depth, i.e.  $H = 80$  m.

#### 347 2.2.4. Primary productivity eddy reactions

Both nutrient variability as well as nutrient covariability with phytoplankton have a  
 rectified impact on primary productivity  $\langle UP \rangle_{x,y}$ . This effect is due to correlations in the  
 biogeochemical concentrations below the domain scale, e.g.  $\langle N'P' \rangle_{x,y}$  where the primes  
 denote deviations from the horizontal average [see Lévy & Martin, 2013; Martin et al.,  
 2015; Woodson & Litvin, 2015]. It may be noted that the leading order (quadratic) terms  
 of the eddy reactions in the mean primary productivity  $\langle UP \rangle_{x,y}$  are proportional to (by  
 Taylor's approximation):

$$\frac{\langle N'P' \rangle_{x,y}}{k_N + \langle N \rangle_{x,y}} - \frac{\langle N'P' \rangle_{x,y} \langle N \rangle_{x,y} + \langle N'N' \rangle_{x,y} \langle P \rangle_{x,y}}{(k_N + \langle N \rangle_{x,y})^2} + \frac{\langle N'N' \rangle_{x,y} \langle N \rangle_{x,y} \langle P \rangle_{x,y}}{(k_N + \langle N \rangle_{x,y})^3} \quad (3)$$

348 where the primes denote deviations from the lateral average and it is assumed that  
 349  $|N'|/(k_N + \langle N \rangle_{x,y}) \ll 1$ . In the LES scenarios presented in this paper, where  
 350  $\langle P \rangle_{x,y} \lesssim k_N + \langle N \rangle_{x,y}$ , the magnitude of the variances  $var(N)$  and  $var(P)$ , where  
 351  $var(N) = \langle N'N' \rangle_{x,y}$ , can be used to bound the magnitude of the ratio of primary produc-  
 352 tivity eddy reactions to the part of  $\langle UP \rangle_{x,y}$  associated with the mean, which is proportional  
 353 to  $\langle N \rangle_{x,y} \langle P \rangle_{x,y} / (k_N + \langle N \rangle_{x,y})$ . In particular, the ratios are bounded by products of the  
 354 coefficients of variation (e.g.,  $c_v(N)c_v(P)$  where  $c_v(N) = \sqrt{var(N)_{x,y}} / \langle N \rangle_{x,y}$ ), by the  
 355 Cauchy-Schwartz inequality.

#### 356 2.2.5. Potential energy change due to vertical mixing

357 The potential energy ( $PE = \int \rho g(z + H) dz$  where  $z$  ranges from  $-80$  m to  $0$  m and  
 358  $H = 80$  m is the domain depth [e.g., Crawford & Large, 1996; Burchard and Hofmeister,  
 359 2008]) can be increased in three ways in response to the storm. First, vertical mixing acts  
 360 to raise the center of mass and thereby increases the potential energy. Second, vertically-  
 361 sheared horizontal mean currents can act on the mean horizontal density gradient to  
 362 reduce the vertical stratification and hence also increase the potential energy. For wind-  
 363 driven (Ekman) currents, the corresponding buoyancy flux is referred to as an Ekman  
 364 buoyancy flux (EBF). Third,  $PE$  can increase due to a stabilizing air-sea buoyancy flux  
 365 (e.g., surface heating). See Whitt & Taylor [2017] for more details on the energetics.

In order to quantify the approximate increase in PE due to mixing, the change in PE due to lateral advection and the air-sea buoyancy flux,  $B_A$ , must be subtracted from the change in PE,  $\Delta PE$ , that is

$$\Delta PE^* = \Delta PE - \left( \Delta \int_{-D}^0 \rho g dz \right) \frac{1}{MLD_3} \int_{-MLD_3}^0 (z + H) dz. \quad (4)$$

366 Dividing the residual change in potential energy by the wind work  $\Delta PE^*/\Delta KE$ , where  
 367  $\Delta KE = \int \boldsymbol{\tau} \cdot \mathbf{u} dt$  and  $\mathbf{u}$  is the surface ocean velocity, approximately quantifies the fraction  
 368 of the wind work that goes toward increasing the potential energy via turbulent mixing,  
 369 i.e., a mixing ratio  $r_m = \Delta PE^*/\Delta KE$ .

### 370 2.2.6. Vertical diffusivity

The diffusivities in ROMS are a direct output of the model/KPP scheme. In the LES, the vertical diffusivities are estimated by adding the subgrid-scale contribution to the resolved vertical nutrient flux and dividing the result by the mean vertical nutrient gradient,

$$\kappa_N = \underbrace{\frac{-\langle wN \rangle_{x,y}}{\frac{\partial \langle N \rangle_{x,y}}{\partial z}}}_{\text{resolved}} + \underbrace{\frac{\langle (\kappa_{SGS} + \kappa_0) \frac{\partial N}{\partial z} \rangle_{x,y}}{\frac{\partial \langle N \rangle_{x,y}}{\partial z}}}_{\text{SGS model}}. \quad (5)$$

### 3. Results

#### 3.1. Mean properties of the LES solutions

371 The first question addressed in the results is: can the fairly typical horizontal den-  
372 sity gradient and submesoscale heterogeneity in the mixed layer impact the mean phys-  
373 ical/biogeochemical tracer response in this strongly forced scenario, in which the storm  
374 winds are the dominant source of energy to the boundary layer? And, if so, by how  
375 much? To contextualize the biogeochemical response to the storm, we first describe the  
376 influence of the front and submesoscales on the evolution of the mixed layer depth and  
377 stratification during the scenario. A description of how stratification evolves in the LES,F  
378 and LES,NF experiments with the weaker wind can be found in Whitt & Taylor [2017],  
379 and the stronger wind scenario presented here is qualitatively similar (the supplemental  
380 material contains figures showing comparisons between the simulations with stronger and  
381 weaker wind stresses, which are enumerated in Table 1).

##### 3.1.1. Density

383 At the onset of the storm, density is already fairly well mixed in the upper 30 m (Fig. 3).  
384 Yet, the storm is sufficiently strong to mix denser water up from the pycnocline, to deepen  
385  $MLD_3$  by approximately 10 m and to increase the surface density (Figs. 4 (c) and (f)).  
386 The deepening of  $MLD_3$  is approximately the same in the scenarios with and without  
387 submesoscales, but the  $MLD_3$  deepens roughly half as much when the wind stress is half  
388 as strong (suppl. Fig. 5). That is, the deepening of  $MLD_3$  is insensitive to the horizontal  
389 density gradient or the presence of submesoscale heterogeneity, up to the degree each  
390 are present in these simulations. However, this is not the case for  $MLD_{05}$ , which shoals  
391 during the storm with submesoscales and deepens without submesoscales (Fig. 4; see also

392 suppl. Fig. 5). The  $MLD_{05}$  is shallower in the simulation with submesoscales because the  
 393 vertical density gradient above  $MLD_3$  is sensitive to the presence of the submesoscales  
 394 during the storm. Without submesoscales, the vertical density gradient above  $MLD_3$   
 395 is concentrated very close to  $MLD_3$ , whereas with submesoscales the vertical density  
 396 gradient above  $MLD_3$  is distributed more evenly with depth. Hence, the curvature of  
 397 the vertical density profile is weaker near  $MLD_3$  with submesoscales, which is consistent  
 398 with enhanced vertical mixing of density across  $MLD_3$  during the storm in that case. We  
 399 can also note that the surface density is greater after the storm with submesoscales, but  
 400 this denser surface water could be attributable to the horizontal Ekman buoyancy flux  
 401 and/or enhanced vertical transport from the pycnocline. Therefore, the denser surface  
 402 water with submesoscales is not necessarily associated with increased vertical mixing.

403 In order to show that the submesoscale heterogeneity triggers enhanced vertical ex-  
 404 change of density from the pycnocline to the mixed layer during the storm, we quantify  
 405 the increase in potential energy due to vertical mixing alone ( $\Delta PE^*$ , defined in section  
 406 2.2.5). We find that  $\Delta PE^*$  is about twice as large with submesoscales as without (Fig.  
 407 5), and we obtain a quantitatively similar result for both wind stress magnitudes (suppl.  
 408 Fig. 6). The mixing ratio ( $r_m = \Delta PE^*/\Delta KE$ , defined in section 2.2.5) ranges from  
 409 about 1.5% without submesoscales to 3% with submesoscales (Fig. 5 (b)), and  $r_m$  is only  
 410 reduced by about 1/4 when the stress is half as strong, although both  $\Delta PE^*$  and the  
 411 kinetic energy input by the wind  $\Delta KE$  are reduced by about 2/3 with the weaker stress  
 412 (suppl. Fig. 6). These results show that the submesoscales enhance the net (subme-  
 413 soscale+turbulent) vertical transport of density across the mixed layer base relative to

414 the simulations without submesoscales, without significantly increasing the kinetic energy  
415 input by the wind.

416 Before discussing the biogeochemical response, it is worth noting that a parameteri-  
417 zation of  $r_m$  is a crucial explicit or implicit choice (e.g., via a bulk Richardson number  
418 threshold, as discussed in *Pollard et al.* [1972]) in many models of ocean boundary layer  
419 mixing and stratification [*Kraus and Turner*, 1967; *Pollard et al.*, 1972; Large et al., 1994;  
420 Crawford & Large, 1996; *Burchard and Hofmeister*, 2008], and these choices can strongly  
421 impact the modeled response of the mixed layer to wind forcing. However, this is the first  
422 time that LES results have been used to explicitly show that submesoscale heterogeneity  
423 can systematically enhance  $r_m$ , and no mixing scheme that is used operationally in ocean  
424 models includes a parameter to explicitly enhance the mixing efficiency to account for  
425 unresolved submesoscale effects like those simulated here. Based on this new result, it is  
426 to be expected that submesoscales also enhance the mean vertical nutrient flux  $\langle wN \rangle_{x,y}$   
427 and net community production  $\langle NCP \rangle_{x,y}$  in this nutrient-limited autumn storm scenario.  
428 In what follows, we quantify and explore these biogeochemical impacts in more detail.

### 429 3.1.2. Nutrient and phytoplankton

430 We start by examining how the horizontally-averaged phytoplankton and nutrient pro-  
431 files evolve during and after the storm in the LES,F and LES,NF simulations. By some  
432 measures, the mean biogeochemical response to the storm is similar with and without  
433 submesoscales (Fig. 4). Storm-driven turbulence fluxes nutrients and phytoplankton up  
434 towards higher light levels near the ocean surface. The storm-driven upward biogeochem-  
435 ical fluxes trigger a reduction in column-integrated nutrient  $\langle N \rangle_{x,y}$  and a nearly equal  
436 and opposite increase in column-integrated phytoplankton biomass  $\langle P \rangle_{x,y}$  (Fig. 6). This

437 mirroring of the changes in column-integrated  $\langle N \rangle_{x,y}$  and  $\langle P \rangle_{x,y}$  indicates that primary  
438 productivity is the dominant mechanism of column-integrated biogeochemical transforma-  
439 tion. These results are qualitatively similar under the weaker stress, but the changes in  
440 column-integrated  $\langle N \rangle_{x,y}$  and  $\langle P \rangle_{x,y}$  are about 1/3 to 1/2 as large, which is qualitatively  
441 consistent with less deepening of the  $MLD_3$  and less nutrient entrainment under weaker  
442 wind stress (suppl. Fig. 5). In addition, this evolution is qualitatively consistent with  
443 expectations based on available observations of the nutrient and/or chlorophyll responses  
444 to autumn storm passage [e.g., Babin et al., 2004; Rumyantseva et al., 2015].

445 However, the mean biogeochemical response to the storm also reveals some systematic  
446 differences with and without submesoscales. First, submesoscales enhance the column-  
447 integrated  $\langle NCP \rangle_{x,y}$  by about a factor of two, which is qualitatively consistent with the  
448 increased mixing ratio  $r_m$ . In addition, the column-integrated  $\langle NCP \rangle_{x,y}$  is also enhanced  
449 by submesoscales when the wind is half as strong, albeit by somewhat less than a factor  
450 of two (suppl. Fig. 5). We can also note a reduced curvature of the mean vertical  
451 nutrient and phytoplankton profiles near  $MLD_3$  in the scenario with submesoscales, which  
452 is consistent with the reduced curvature of the density profiles near  $MLD_3$  and enhanced  
453 vertical mixing there with submesoscales. Finally we also find faster surface accumulation  
454 of phytoplankton and stronger vertical gradients in both phytoplankton and nutrient  
455 that develop within the mixed layer in the scenarios with submesoscales compared to the  
456 scenarios without submesoscales. In the following section, we show how submesoscales  
457 modulate the net (submesoscale+turbulent) vertical fluxes of biogeochemical constituents  
458 to explain these results.



### 3.2. Horizontal variability in the LES solutions

459 Based on the results of the previous section, it is expected that average vertical nutri-  
 460 ent fluxes  $\langle wN \rangle_{x,y}$  will be sensitive to the presence of submesoscales. However, since the  
 461 biogeochemical dynamics, such as primary productivity and grazing, are non-linear, the  
 462 biogeochemical covariability at scales from meters to submesoscales, such as  $cov(N, P)$ ,  
 463 may rectify on larger-scale biogeochemical dynamics as well. In addition, the fluxes and  
 464 covariances are best understood in the context of the variances, such as  $var(N)$ , on which  
 465 they depend. Hence, this section addresses the following questions for the first time with  
 466 BLES: does submesoscale heterogeneity impact the horizontal biogeochemical variances,  
 467 such as  $var(N)$ , or key covariances, such as  $cov(N, P)$ , which impacts primary productiv-  
 468 ity, or  $cov(w, N) = \langle wN \rangle_{x,y}$ , in this storm scenario? To what degree do the submesoscales  
 469 ( $> 150$  m) and turbulent scales ( $< 150$  m) contribute to the total variances and covari-  
 470 ances during the different phases of the storm? Is there a rectified effect of submesoscales  
 471 on physical and biogeochemical variances and covariances at turbulent scales?

472 We find that the physical/biogeochemical variances and covariances are greatly modified  
 473 by the presence of submesoscales during and after the storm. To gain further perspective  
 474 on this aspect of the solutions, we first qualitatively compare the lateral variability of  
 475 the nutrient  $N$  and nutrient flux  $wN$  in snapshots from the different solutions during the  
 476 storm (Fig. 7) before proceeding to statistical measures of the variability. Just above  
 477  $MLD_3$  (i.e.,  $MLD_3 + 4$  m), the variability in nutrient concentration differs qualitatively  
 478 between LES,F and LES,NF. With submesoscales, the nutrient distribution reflects the  
 479 submesoscale vertical displacements of the nutricline (Figs. 7 (a)), which dominate the  
 480 total variability. However, the dominant characteristic scales of the nutrient flux  $wN$

481 (which are qualitatively similar to  $w$ , not shown) are much smaller. Yet, these dominant  
 482 small-scale structures in  $wN$  are modulated somewhat by the larger submesoscales (Fig.  
 483 7 (b)). In contrast, the LES,NF scenario exhibits no obvious qualitative evidence of  
 484 organization at submesoscales in either  $N$  or  $wN$  (Fig. 7), and the characteristic horizontal  
 485 scales of  $N$  and  $wN$  variability are comparable in magnitude to  $MLD_3$ . In this sense,  
 486 the simulated variability of  $N$  and  $wN$  in the LES,NF scenario is qualitatively consistent  
 487 with classic ideas about boundary layer turbulence, in which the largest aspect-ratio-one  
 488 turbulent eddies with a length scale similar to  $MLD_3$  dominate both the variances and  
 489 the fluxes. In contrast, the LES,F scenario is qualitatively inconsistent with classic ideas  
 490 about boundary layer turbulence in the same sense, because low-aspect-ratio structures  
 491 that are a factor of 10-50 times larger than  $MLD_3$  qualitatively dominate the variance.  
 492 (For a spectral perspective on this statement, compare the schematic power spectrum of  
 493 boundary layer turbulence in Fig. 1 of *Wynngaard* [2004], in which the power drops at  
 494 horizontal wavelengths greater than the boundary layer height, to simulated power spectra  
 495 in Fig. 5 of *Whitt & Taylor* [2017], in which the power rises at horizontal wavelengths  
 496 greater than the mixed layer depth).

### 497 **3.2.1. Biogeochemical variances in the LES solutions**

498 For a more statistical perspective on the dependence of the biogeochemical variability on  
 499 the submesoscales, we explicitly quantify and compare the vertical profiles of the nutrient  
 500 variance  $var(N)$ , and we show how submesoscales ( $>150$  m) and smaller turbulent scales  
 501 ( $<150$  m) contribute to the total variance in the LES,F and LES,NF scenarios (Fig. 8).  
 502 The phytoplankton variance profiles  $var(P)$  are qualitatively similar to  $var(N)$ , and the

503 results are qualitatively insensitive to reducing the wind stress by half (see suppl. Figs.  
504 7-8), so we only discuss the stronger wind scenario in this context.

505 During the storm (days 2-3),  $var(N)$  is maximal just below  $MLD_3$  and declines mono-  
506 tonically upwards so that it is 3-4 orders of magnitude smaller at the surface. With  
507 submesoscales, there is much greater total variance in the mixed layer due almost entirely  
508 to submesoscale ( $> 150$  m) variance, similar to weakly-forced LES simulations of passive  
509 tracers released in the pycnocline by Smith et al. [2016]. However, in a more novel re-  
510 sult, the presence of submesoscales also increases the variance of  $N$  at smaller ( $< 150$  m)  
511 turbulent scales during the storm by up to about an order of magnitude, particularly in  
512 the upper part of the mixed layer (Fig. 8 (C)). The enhanced smaller-scale  $N$  variance  
513 with submesoscales is likely due primarily to enhanced physical variance production from  
514 stronger mean and submesoscale vertical gradients (Fig. 4), since the smaller-scale tur-  
515 bulent kinetic energy and the dissipation of turbulent kinetic energy in the mixed layer  
516 are only modestly modified by submesoscales during the storm (see suppl. Fig. 12 here  
517 and Fig. 5 of Whitt & Taylor [2017]).

518 Although kinetic energy at submesoscales and turbulent scales declines substantially  
519 after the storm [Whitt & Taylor, 2017] (see also suppl. Fig. 12),  $var(N)$  generally increases  
520 after the storm and remains about 1-2 orders of magnitude greater with submesoscales  
521 than without. With submesoscales,  $var(N)$  achieves its maximum in the middle of the  
522 mixed layer, i.e. from about 10 to 30 m depth (Fig. 8 (F)), due to a substantial increase  
523 in submesoscale variance at these depths after the storm. This increase in submesoscale  
524 variance after the storm is likely due primarily to the near shutdown of turbulent mixing  
525 and the corresponding reduction of the rate of dissipation of submesoscale  $N$  variance

526 via turbulent mixing. On the other hand, production of submesoscale variance is not  
 527 substantially enhanced after the storm, since submesoscale kinetic energy declines after  
 528 the storm [Whitt & Taylor, 2017], and mean vertical tracer gradients are only slightly  
 529 enhanced with submesoscales (Fig. 4).

### 530 3.2.2. Biogeochemical covariances in the LES solutions

531 The rectified impacts of nutrient and phytoplankton variability on primary productiv-  
 532 ity, which is defined by  $\langle UP \rangle_{x,y}$  in (1), require spatial correlation,  $\text{corr}(N, P)$  in addition  
 533 to variance (see section 2.2.4). In the mixed layer,  $\text{corr}(N, P)$  is time and depth depen-  
 534 dent; it is positive during the storm and negative after the storm, but mostly order-one  
 535 (see suppl. Fig. 9). Therefore, eddy reactions are non-zero and larger in magnitude  
 536 with submesoscales due to the larger horizontal variances, and the eddy reactions can  
 537 take both signs. However, it may be noted that the smallness of both coefficients of  
 538 variation  $c_v(N)$  and  $c_v(P)$  directly imply the smallness of primary productivity eddy re-  
 539 actions relative to the part of  $\langle UP \rangle_{x,y}$  associated with the means, which is proportional to  
 540  $\langle N \rangle_{x,y} \langle P \rangle_{x,y} / (k_N + \langle N \rangle_{x,y})$  (see section 2.2.4). In addition, the storm-driven perturbation  
 541 to zooplankton production is small compared to the perturbation to primary production  
 542 in this scenario. So, we do not pursue questions about eddy reactions any further here,  
 543 although the dynamic nature of the variances of  $N$  and  $P$  and their correlation reflect non-  
 544 trivial physical/biogeochemical dynamics that have never been previously documented in  
 545 BLES, and future work is needed to fully investigate these dynamics in this and other  
 546 scenarios.

### 547 3.2.3. Nutrient fluxes in the LES solutions

548 Here, we quantify and discuss the vertical nutrient flux, and its submesoscale and tur-  
549 bulent parts in the LES,F and LES,NF scenarios (Fig. 9;  $var(N)$  is in Fig. 8;  $var(w)$  is  
550 in suppl. Fig. 12; and multi-scale correlation profiles  $corr(w, N)$  are in suppl. Fig. 13).  
551 Consistent with the results above, we find that both the total fluxes and their respec-  
552 tive submesoscale and turbulent parts differ by an order-one fraction with and without  
553 submesoscales, both during and after the storm.

554 First, we find that the presence of submesoscales substantially enhances the total vertical  
555 nutrient flux during the storm (between days 2-3, left column in Fig. 9). In addition, the  
556 effect of the submesoscales on the maximum total flux is qualitatively similar but greater  
557 in the scenario with stronger stress (a 115% increase) than the scenario with the weaker  
558 stress (a 34% increase, see suppl. Fig. 10). However, the total flux profiles exhibit a  
559 qualitatively similar vertical structure in scenarios with and without submesoscales. In  
560 both scenarios, the maximum flux occurs between about  $0.8MLD_3$  and  $0.9MLD_3$ , and  
561 the flux drops almost linearly to zero between the depth where it achieves its maximum  
562 and the surface above or about  $1.1MLD_3$  below. Yet, the strong fluxes penetrate deeper  
563 below the mixed layer  $MLD_3$  in the LES,F scenarios compared to the LES,NF scenarios,  
564 which is consistent with deeper penetration of high rates of dissipation of turbulent kinetic  
565 energy [Whitt & Taylor, 2017] and vertical velocity variance (suppl. Fig. 12) into the  
566 pycnocline/nutricline in the presence of submesoscales.

567 The partitioning of the flux between submesoscales ( $> 150$  m) and smaller turbulent  
568 scales ( $< 150$  m) during the storm differs significantly depending on the presence or  
569 absence of the submesoscales, and the differences are qualitatively similar with weaker  
570 wind (suppl. Fig. 10). Without submesoscales in LES,NF, the total flux is dominated

571 by smaller turbulent scales. On the other hand, with submesoscales in LES,F, subme-  
572 soscale and smaller-scale turbulent fluxes are both positive and submesoscales contribute  
573 an order-one fraction of the total flux. The strong submesoscale flux is qualitatively con-  
574 sistent with strong submesoscale  $N$  variance (Fig. 8), and it shows that the submesoscale  
575 heaving of the nutricline observed in Fig. 7 is also associated with some irreversible up-  
576 ward nutrient transport at submesoscales. With a weaker wind, the fraction of the total  
577 flux from submesoscales is larger, but the magnitude of the submesoscale flux is smaller  
578 (see suppl. Fig. 10). Incidentally, the decrease in submesoscale flux with the decrease  
579 in wind stress magnitude is qualitatively consistent with previous process studies with  
580 ocean models that parameterize small turbulent scales [e.g., Mahadevan & Tandon, 2006;  
581 Capet et al., 2008a; Thomas et al., 2008; Whitt et al., 2017b], although the causes of there  
582 relationships are not necessarily the same (see Whitt & Taylor [2017] for some relevant  
583 discussion). However, in a more novel result, the smaller-scale turbulent contribution to  
584 the nutrient flux is significantly greater during the storm with submesoscales than with-  
585 out, even though vertical velocity variance is only modestly altered throughout most of  
586 the mixed layer (suppl. Fig. 12). This enhanced flux (i.e., covariance) is qualitatively  
587 consistent with enhanced turbulent  $N$  variance with submesoscales, but the correlation  
588 between nutrient and vertical velocity is actually smaller, both in aggregate and at tur-  
589 bulent scales, in the simulations with submesoscales than without submesoscales (suppl.  
590 Fig. 13). Finally, perhaps the most intriguing feature of the nutrient flux profiles during  
591 the storm is the deeper penetration of the strong vertical fluxes below the mixed layer in  
592 the LES,F scenarios with submesoscales compared to the LES,NF scenarios without. This  
593 enhanced flux near  $MLD_3$  occurs in conjunction with a substantial increase in smaller-

594 scale turbulent vertical velocity variance (suppl. Fig. 12) and is due mostly although not  
595 entirely to stronger smaller-scale fluxes (Fig. 9).

596 After the storm, the nutrient flux profiles change dramatically compared to their coun-  
597 terparts during the storm. In particular, the magnitude of the total flux is reduced by  
598 about an order of magnitude in both simulations (note the different x-axes in the left  
599 and right columns in Figure 9). In addition, the maximum total flux is about a factor of  
600 two weaker with submesoscales than without. The partitioning of the total flux between  
601 submesoscales and turbulent scales is also very different between the two scenarios. In  
602 particular, the smaller-scale turbulent flux is much weaker in the scenario with the sub-  
603 mesoscales (LES,F) than in the scenario without submesoscales (LES,NF). Consequently,  
604 after the storm the total flux is achieved mostly by the submesoscale flux in LES,F and  
605 by the smaller-scale turbulent flux in LES,NF.

606 The shut-down of the turbulent flux after the storm in the LES,F scenario and cor-  
607 responding increase in vertical biogeochemical gradients is qualitatively consistent with  
608 earlier results showing how submesoscales influence the timing of the spring bloom by en-  
609 hancing the density stratification, suppressing turbulence, and thereby modifying vertical  
610 fluxes in deeper spring mixed layers [Taylor, 2016]. More generally, these results suggest  
611 that fronts/submesoscales may contribute to the rapid formation of biogeochemical gradi-  
612 ents within mixed layers after strong wind events during any time of year by suppressing  
613 turbulent fluxes even when the mixed layer depths have not yet shoaled significantly [e.g.,  
614 as observed by Carranza et al., 2018].

### 3.3. Comparisons between the LES and column model mean solutions

615 The comparison between the LES results of the previous section (LES,F and LES,NF)  
 616 and two analog column model simulations (ROMS,F and ROMS, NF) is presented with  
 617 the aim of evaluating the ability of existing ocean model parameterizations (encapsulated  
 618 in the column model) to plausibly represent the physical-biogeochemical dynamics sim-  
 619 ulated by LES. We focus mostly on the scenarios with the front/submesoscales, which  
 620 are the most interesting, but nevertheless show the results for the scenarios without a  
 621 front/submesoscales as a reference. For the two models (LES and ROMS), we compare  
 622 the total flux and total diffusivities (Figs. 10-11). Comparison of the mean density,  
 623 nutrient, phytoplankton profiles are shown in suppl. Figs. 2-4. Comparisons of the  
 624 column-integrated quantities, such as column integrated  $\langle N \rangle_{x,y}$  and  $\langle P \rangle_{x,y}$  as well as the  
 625 change in potential energy and the mixing ratio are in suppl. Figs. 5-6. In addition,  
 626 fluxes and diffusivities in scenarios with the weaker wind, which are qualitatively similar  
 627 to their counterparts in the scenarios with stronger wind, are shown in suppl. Figs. 10-11.

#### 3.3.1. Scenarios without a front or submesoscales

629 Broadly speaking, the column model ROMS,NF is rather effective at reproducing the  
 630 laterally-averaged evolution in the LES,NF simulation without a front/submesoscales by  
 631 all the metrics considered. Vertical tracer fluxes in ROMS,NF are a fairly good repre-  
 632 sentation of vertical tracer fluxes in LES,NF. The ROMS,NF scenario also produces very  
 633 similar mixed-layer depths and vertical diffusivity profiles during and after the storm  
 634 compared to the LES,NF scenario (Fig. 11). As a consequence, the mean profiles and  
 635 column integrals of phytoplankton and nutrient are also similar, under both weak and  
 636 strong wind (Figs. 12 (c)-(d); see supplementary Figs. 2-3 for the profile comparisons).



637 This result confirms previous findings [e.g., Large et al., 1994; Large & Crawford, 1995;  
638 Skillingstad et al., 2000; McWilliams & Sullivan, 2000; Pham & Sarkar, 2017] that the  
639 KPP parameterization is capable of capturing the change in vertical mixing in response  
640 to a storm in the absence of a front/submesoscales.

### 641 **3.3.2. Scenarios with a front and submesoscales**

642 The frontal zone version of the column model ROMS,F does not perform as well  
643 at capturing the physical/biogeochemical dynamics of the LES,F scenario with the  
644 front/submesoscales. In fact, the ROMS,F scenarios are in many ways more similar to  
645 the ROMS,NF and LES,NF scenarios than their analog LES,F scenarios, which shows  
646 that the submesoscale heterogeneity simulated by LES,F is the cause of the differences  
647 relative to LES,NF, not the front. As in previous sections, only the scenarios forced  
648 by the stronger winds are presented here; the scenarios forced by the weaker winds are  
649 qualitatively similar and appear in suppl. Figs. 2-6 and 10-11.

650 The most distinctive result emerging from the LES,F/LES,NF comparison above is that  
651 the presence of submesoscales in LES,F roughly doubles the vertical nutrient fluxes and  
652 mixing ratio during the storm, and the submesoscales indirectly cause turbulence and  
653 turbulent fluxes to penetrate below  $MLD_3$ . In contrast, the total vertical nutrient flux  
654 in the ROMS,F scenario is actually reduced compared to the ROMS,NF and LES,NF  
655 scenarios during the storm. As a result, the maximum vertical nutrient flux in ROMS,F  
656 is about a quarter of that in LES,F (Fig. 10 (a)). Further, ROMS,F fails to capture the  
657 deeper penetration of vertical fluxes below  $MLD_3$  that is simulated in LES,F.

658 Comparing the vertical diffusivity profiles  $\kappa_N$  during the storm (Fig. 10 (c)) shows  
659 that ROMS,F fails to capture the strong vertical nutrient fluxes in the mixed layer partly

660 because the mean nutrient gradients are too weak, not just because the diffusivities are too  
661 weak. For example, between about  $0.5MLD_3$  and  $0.9MLD_3$ , the diffusivity is actually  
662 lower in LES,F than ROMS,F, while the fluxes are about 3-4 times larger in LES,F  
663 than ROMS,F (mean nutrient profiles are compared in suppl. Fig. 3). On the other  
664 hand, just below the mixed layer (between about  $MLD_3$  and  $1.1MLD_3$ ), both the flux  
665 and diffusivity are much larger in the LES,F than ROMS,F. These results suggest that  
666 submesoscales systematically modify the empirical non-dimensional shape functions as  
667 well as the turbulent boundary layer depth, which characterize the diffusivity profiles in  
668 the mixing scheme [Large et al., 1994], during the storm.

669 After the storm, there is some indication that the physics encapsulated in the ROMS,F  
670 scenario may capture some of the essential physics in the LES,F scenario. In particular, the  
671 maximum total fluxes in the mixed layer are smaller in magnitude and occur at a shallower  
672 depth than in the corresponding LES,NF and ROMS,NF scenarios (c.f., Figs. 10 (b) and  
673 11 (b)). In addition, both the mixed layer depth  $MLD_{05}$  and the surface mixing layer  
674 depth shoal in the ROMS,F scenario. However, there are still some discrepancies between  
675 LES,F and ROMS,F. For example, the maximum nutrient flux is only about a quarter to  
676 a third of that in LES,F. In the upper half of the mixed layer, where vertical diffusivities  
677 in ROMS,F are mostly larger than in LES,F, the reduced vertical fluxes are caused by  
678 too-weak mean gradients. However, between  $0.5MLD_3$  and  $MLD_3$ , the reduced vertical  
679 fluxes are mostly caused by too-small vertical diffusivities. In addition, the reduced fluxes  
680 are presumably partially a result of missing submesoscale vertical fluxes, which dominate  
681 in LES,F after the storm, but are not included in ROMS,F.

682 Despite differences, these significantly reduced diffusivities after the storm—in both  
683 ROMS,F and LES,F—manifest in enhanced mean vertical gradients in phytoplankton  
684 above  $MLD_3$  by day 5-6 in the scenarios with a front compared to their counterparts  
685 without a front, that is LES,NF and ROMS,NF (suppl. Figs. 2-3). Hence, the relatively  
686 rapid formation of biogeochemical vertical gradients within the mixed layer in both LES,F  
687 and ROMS,F scenarios is partly attributable to the substantial reduction in vertical mixing  
688 in the scenarios in a frontal zone. However, as a result of the failure of the ROMS,F column  
689 model to capture the enhanced vertical nutrient fluxes during the storm, there is only a  
690 third to a half as much net community production and accumulation of column-integrated  
691 phytoplankton during and shortly after the storm (Fig. 12 (b)).

### 692 3.3.3. Summary of the comparisons between the column model and LES

693 Qualitatively and quantitatively, the conventional boundary layer column model  
694 ROMS,NF accurately captures the physical-biogeochemical evolution of the conventional  
695 boundary layer LES,NF without a front/submesoscales. This is encouraging, with the  
696 caveat that there is some indication that the performance of KPP may not be equally  
697 good in other parts of physical parameter space [Pham & Sarkar, 2017]. Regardless, the  
698 column model with a frontal zone ROMS,F fails to reproduce the physical-biogeochemical  
699 evolution in the LES with a frontal zone. In particular, the column model fails to cap-  
700 ture the fact that submesoscale physical variability in the mixed layer enhances vertical  
701 nutrient fluxes, phytoplankton accumulation, and net community production during the  
702 life cycle of the storm. However, the column model does capture the qualitatively reduced  
703 mixing within the mixed layer  $MLD_3$  and the related rapid emergence of vertical phy-

704 top plankton gradients within the mixed layer after the storm with a front/submesoscales  
705 compared to scenarios without a front/submesoscales.

706 The failure of the column model to capture the enhanced vertical mixing and nutrient  
707 fluxes during the storm rules out several a priori plausible explanations for this differ-  
708 ence between LES,F and LES,NF, including the Ekman buoyancy flux, vertical mixing  
709 of geostrophic momentum, and/or the restratifying buoyancy flux associated with mixed  
710 layer baroclinic instabilities as described by FFH via (2). However, these three factors  
711 could contribute indirectly, in combination with other properties of submesoscale vari-  
712 ability in LES,F, to induce enhanced mixing during the storm. On the other hand, the  
713 partial success of the column model in capturing the reduced vertical mixing and the more  
714 rapid formation of vertical gradients in phytoplankton after the storm suggests that the  
715 column model captures some of the essential physical-biogeochemical dynamics associated  
716 with the rapid formation of these vertical phytoplankton gradients in LES,F. In partic-  
717 ular, the combination of the Ekman buoyancy flux, mixing of geostrophic momentum,  
718 and restratification via (2) results in substantially reduced mixing within the mixed layer  
719 after the storm, and the more rapid formation of biogeochemical gradients within the  
720 mixed layer. Future work is required to generalize these results and to develop and test  
721 other hypotheses about the key physical-biogeochemical mechanisms responsible for the  
722 enhanced vertical mixing and net community production during the storm.

## 4. Conclusion and Discussion

### 4.1. Summary

723 This study uses process-oriented numerical simulations to address the questions  
724 of whether and to what degree submesoscale heterogeneity influences the physical-

725 biogeochemical response to a storm. Previous process studies using numerical models  
726 with parameterized turbulence have demonstrated that submesoscales have a significant  
727 impact on mixed layer tracer budgets and hence biogeochemical dynamics, including and  
728 perhaps especially under wind forcing [e.g., Franks & Walstad, 1997; Mahadevan et al.,  
729 2008; Lévy et al., 2009; Brannigan, 2016; Whitt et al., 2017b]. However, the results  
730 presented here highlight and address an important source of uncertainty affecting these  
731 previous studies: the turbulence parameterizations have neither been designed for nor  
732 validated in an ocean surface mixed layer with significant submesoscale heterogeneity.

733 The results presented here are an important contribution because they are derived from  
734 coupled physical-biogeochemical ocean simulations that explicitly resolve a significant  
735 range of both submesoscales and turbulent scales and thereby greatly reduce the uncer-  
736 tainty emanating from turbulence parameterizations. In particular, the LES presented  
737 here are all in the high-Peclet number regime, that is  $Pe \approx 50$  meaning that the resolved  
738 turbulent advective vertical tracer flux is about 50 times stronger than the subgrid-scale  
739 diffusive vertical tracer flux in the mixed layer during the storm (suppl. Fig. 11). Hence,  
740 the qualitative results are expected to be insensitive to further refinement of the grid  
741 resolution or changes to the subgrid-scale model. This expectation is supported by a grid  
742 refinement study (not shown), in which the first 1.7 days of the LES,NF scenario were  
743 re-run in a smaller domain (320 m wide), and the entrainment was effectively identical  
744 on grids with horizontal resolutions ranging from 2.2 m to 1.1 m, which span the 1.9 m  
745 resolution used for all the simulations reported above.

746 The results presented here answer the scientific question set forth in the affirma-  
747 tive: submesoscale heterogeneity in a frontal zone significantly modifies the physical-

748 biogeochemical response to the storm compared to otherwise identical scenarios without  
749 the submesoscales. Most importantly, submesoscales strongly enhance the wind-driven  
750 flux of tracers from the pycnocline to the mixed layer. For example, submesoscales en-  
751 hance the maximum vertical nutrient flux in the mixed layer by a factor of two and the  
752 turbulent diffusivity at the mixed layer base by a factor of ten. Interestingly, the decom-  
753 position of the vertical nutrient fluxes into larger submesoscales and smaller turbulent  
754 scales shows that submesoscales contribute to enhanced vertical fluxes during the storm  
755 in two ways. First, the vertical fluxes associated with submesoscale features directly trans-  
756 port nutrients from the pycnocline to the mixed layer, as observed in previous studies.  
757 However, these results also show that submesoscale physical variability in a frontal zone  
758 acts as a catalyst by enhancing the small turbulent-scale nutrient fluxes near and just be-  
759 low the mixed layer base. On the other hand, submesoscales suppress net vertical tracer  
760 fluxes after the storm by inducing a near shut-down of turbulent scale fluxes, although  
761 submesoscale fluxes actually increase after the storm. Hence, submesoscales facilitate a  
762 more rapid emergence of vertical phytoplankton gradients within the mixed layer after  
763 the storm. Consequently, mean phytoplankton accumulation rates are roughly twice as  
764 fast after the storm in the scenarios with submesoscales compared to their counterparts  
765 without.

766 Since the column model simulations do not capture this enhanced mean phytoplank-  
767 ton accumulation rate in the frontal zone configuration, existing physical-biogeochemical  
768 ocean models with horizontal grid spacings of 2 km or greater and the KPP and FFH  
769 parameterizations will not effectively capture the enhanced storm-driven phytoplankton  
770 growth simulated in LES. In addition, these results demonstrate that the combination of

771 processes added to the column model with a frontal zone, which include the destratifying  
772 Ekman buoyancy flux and vertical mixing of geostrophic momentum that would also be  
773 included in a submesoscale-permitting regional ocean model, cannot explain the enhanced  
774 fluxes and biogeochemical impacts on their own. Rather, other processes or combinations  
775 of processes must be invoked to explain the results. However, the significance of these  
776 results is far from fully understood at this point, because these results are derived from  
777 only a few case studies. In addition, since the underlying processes that explain these  
778 results are not fully understood, they may impact other properties of the upper ocean  
779 beyond biogeochemistry, including heat, salt, momentum, and kinetic energy budgets.

#### 4.2. Comparison with other process simulations

780 Although this is the first study to present LES that resolve substantial parts of the  
781 submesoscale range together with a fully-coupled biogeochemical model (with coupled  
782 nutrient/ecosystem dynamics), the results are consistent with and build on a few previous  
783 studies that have presented LES that resolve both submesoscales and turbulence and  
784 simulate passive tracers and/or phytoplankton.

785 For example, the result that submesoscales enhance the lateral biogeochemical variance  
786 by an order of magnitude or two after the storm is qualitatively consistent with the LES  
787 simulations of passive tracers in Smith et al. [2016], where it is shown that submesoscales  
788 enhance the lateral variance of tracers initialized near the base of the mixed layer by up  
789 to a factor of 20 under weak winds and weak cooling. However, the results presented  
790 here show that submesoscales significantly enhance nutrient and phytoplankton variance  
791 during the strong wind forcing for the first time, although the submesoscale tracer variance  
792 in the mixed layer is generally lower during the storm than afterwards. In addition, these

793 results show that submesoscales indirectly enhance smaller-scale turbulent tracer variance  
 794 during the storm.

795 In addition, the result that the submesoscales are associated with enhanced wind-driven  
 796 vertical mixing near the mixed layer base is qualitatively consistent with several earlier  
 797 LES in short/wide frontal zones, which have shown that strong turbulent vertical mixing  
 798 of tracers extends to deeper depths than predicted by KPP [Bachman et al., 2017a].  
 799 However, these earlier results are attributed to symmetric instability turbulence mixing  
 800 over the depth of the low potential vorticity layer  $H_q$  (defined to be the deepest depth  
 801 where  $\int_{H_q}^0 f \langle \frac{\partial b}{\partial z} \rangle_{x,y} + \langle \frac{\partial u}{\partial z} \rangle_{x,y} \langle \frac{\partial b}{\partial y} \rangle_{x,y} dz = 0$ ; see also Whitt et al. [2017b]). In the LES  
 802 simulations presented here, enhanced vertical mixing extends well below  $H_q$  and even  
 803 penetrates into the high stratification of the seasonal pycnocline below the mixed layer  
 804 [Whitt & Taylor, 2017]. In addition, these results show explicitly that the enhanced  
 805 vertical fluxes with submesoscales are due in large part to enhanced turbulent scale fluxes,  
 806 in addition to enhanced submesoscale vertical fluxes.

807 Finally, the result that submesoscales reduce net vertical fluxes after the storm is also  
 808 qualitatively consistent with the conclusions of Smith et al. [2016], in which it is shown  
 809 that submesoscales inhibit wind/wave driven vertical mixing of passive tracers released  
 810 near the mixed layer base under weak atmospheric forcing. In addition, the results are  
 811 consistent with the emerging hypothesis that submesoscales suppress net vertical fluxes  
 812 under weak forcing (e.g., after the storm), but submesoscales do not suppress [as in Taylor,  
 813 2016] or enhance (as in this case) net vertical fluxes as well as smaller-scale turbulent fluxes  
 814 under sufficiently strong forcing.



### 4.3. Comparison with observations

815 It is difficult to observe all the variables and spatio-temporal scales necessary to evaluate  
816 the hypotheses emerging from these simulations, but there are many observations of the  
817 bio-optical and physical response of the upper-ocean to a summer or autumn storm from  
818 satellites [e.g., Lin et al., 2003; Babin et al., 2004; *Fauchereau et al.*, 2011; *Lin*, 2012;  
819 Carranza & Gille, 2015] and a rapidly increasing but small number of subsurface bio-  
820 optical observations during and after storms from profiling subsurface floats [e.g., *Ye et al.*,  
821 2013; *Chacko*, 2017; *Girishkumar et al.*, 2019]. Like all our simulations, many of these  
822 prior observations, including the observations of Rumyantseva et al. [2015] and Painter  
823 et al. [2016], which motivated the present study, show that autumn storms increase the  
824 surface density, deepen the mixed layer, erode subsurface chlorophyll maxima and mix  
825 subsurface chlorophyll up toward the surface (thereby increasing the fraction of column-  
826 integrated chlorophyll in the mixed layer), and trigger an increase in column-integrated  
827 chlorophyll. However, the magnitude and qualitative nature of these responses are highly  
828 variable between different storms [see e.g., Painter et al., 2016] due to the wide variety of  
829 different physical and biogeochemical circumstances in which storms occur.

830 Although prior observations reveal mesoscale spatial variability in the surface temper-  
831 ature and chlorophyll response to autumn storms [e.g., Babin et al., 2004; *Lin*, 2012;  
832 Painter et al., 2016; *Girishkumar et al.*, 2019], most observations do not provide explicit  
833 information about the mesoscale lateral density variability in conjunction with explicit  
834 information about the corresponding lateral variability of submesoscales, turbulence and  
835 biogeochemistry during and after a storm. Without such data, it is difficult to observa-  
836 tionally evaluate the hypotheses emerging from the LES, specifically that even relatively

837 modest open-ocean mesoscale fronts (in comparison to areas without fronts) are associ-  
838 ated with: 1) enhanced submesoscale and turbulent-scale nutrient fluxes during a storm,  
839 2) more intermittent turbulence and suppressed net turbulent nutrient fluxes in the mixed  
840 layer after the storm, and 3) enhanced storm-driven new production.

841 Nevertheless, we can consider these hypotheses in light of some rare, nearly-simultaneous  
842 observations of turbulence, nutrients and submesoscales. For example, the OSMOSIS  
843 program, which motivated these process simulations, obtained observations of turbulent  
844 nutrient fluxes and submesoscales before and after an autumn storm. In addition, the  
845 OSMOSIS program provides broader context for these focused process studies, since re-  
846 sults are available showing the full seasonal cycle of bio-optical parameters like chlorophyll  
847 fluorescence, backscatter, among others [*Erickson and Thompson, 2018; Bol et al., 2018*].  
848 The observations during the storm at the OSMOSIS site reveal highly-intermittent tur-  
849 bulent nutrient fluxes near the mixed layer base at a single location for one day after  
850 the storm. Although Rumyantseva et al. [2015] find that the intermittent mixing is plau-  
851 sibly attributable to intermittent alignment between the ocean currents and the wind,  
852 our simulations with a front and submesoscales (LES,F) also reveal large spatio-temporal  
853 intermittency in turbulent nutrient fluxes near the mixed layer base, both during and  
854 after the storm even though the effective wind speed after the storm is zero. Figure 7 (b)  
855 shows how nutrient fluxes are modulated by submesoscales during the simulated storm;  
856 qualitatively similar results are found for turbulent nutrient fluxes after the storm, but  
857 not shown; see also Whitt & Taylor [2017]. In addition, the hypothesis that submesoscale  
858 variability could have contributed to the observed intermittency of the turbulent nutrient  
859 flux in the observations of Rumyantseva et al. [2015] is bolstered by satellite observations

860 of substantial submesoscale variability in the sea surface temperature before the storm  
861 [Buckingham et al., 2017]. However, subsurface observations of scales smaller than 2 km  
862 are not available.

863 Elsewhere, a high-resolution physical/biogeochemical survey in the vicinity of the  
864 Kuroshio front by Nagai & Clayton [2017] reveals submesoscale lateral variability in nutri-  
865 ent concentrations, which is qualitatively similar to the simulated submesoscale nutrient  
866 variability near the pycnocline in Figure 7 (a). In addition, Nagai & Clayton [2017] find  
867 that these nutrient anomalies have a rectified effect on the net turbulent nutrient flux,  
868 consistent with our LES results. However, their observations were not during/after a  
869 storm.

870 A future interdisciplinary observational study is needed to evaluate the hypothesis that  
871 mesoscale oceanic lateral density variability induces lateral variations in the submesoscale  
872 and turbulent-scale physical and biogeochemical response to a storm using multi-scale  
873 sampling of nutrients (in various forms), turbulence, and primary productivity during  
874 the life cycle of a storm at resolutions down to  $\sim 1$  km over a region  $\lesssim 100$  km in scale.  
875 Such a dataset is challenging to obtain due to the operational challenge associated with  
876 collecting water samples during a storm, but it may be possible with an array of robotic  
877 towed and/or autonomous samplers.

#### 4.4. Remaining uncertainties associated with the model configurations

878 Finally, it is worth reiterating that the results of these simulations should be viewed  
879 with caution due to a variety of outstanding uncertainties that have not been addressed  
880 here. Perhaps most significantly, the physics may be influenced by the small domain  
881 size and the absence of larger submesoscale and mesoscale structures. In addition, the

882 biogeochemical model is at best a qualitative representation of the real biogeochemical  
883 dynamics, and it is expected that the biogeochemical model may influence the details of  
884 the results. Further, we have only one initial condition and two fairly-idealized forcing  
885 scenarios, which omit surface wave effects.

886 If general results are to be obtained, then future work must explore sensitivities to the  
887 details of the forcing, including wind stress direction and frequency content, as well as air-  
888 sea buoyancy flux and surface wave effects. With regard to waves, real storms are expected  
889 to generate strong wind waves, which substantially modify the Lagrangian mean shear in  
890 the upper ocean. Hence, as several previous studies have shown, waves can substantially  
891 modify the upper-ocean turbulence [e.g., McWilliams & Sullivan, 2000; Li et al., 2012],  
892 submesoscale/turbulence interactions [Hamlington et al., 2014; Haney et al., 2015; Smith  
893 et al., 2016], and thereby vertical tracer transport. It is difficult to say how waves might  
894 impact the results in this scenario, because no previous study has considered the impacts  
895 of waves on submesoscale/turbulence interactions under strong storm winds, as in this  
896 scenario. However, we expect that the addition of wind waves, roughly aligned with the  
897 winds, would be an additional source of energy for smaller-scale turbulence and enhance  
898 entrainment. But, it is less clear how these waves would impact the relatively strong flow  
899 of kinetic energy to submesoscales during the storm in these simulations. Hence, a high  
900 priority for future work should be to explore submesoscale/turbulence interactions with  
901 strong waves and strong winds, building on studies with weak wind [e.g., Hamlington  
902 et al., 2014; Smith et al., 2016].

903 In addition, future work will have to explore the sensitivity of the results to the strength  
904 of the initial horizontal and vertical buoyancy gradients, the initial submesoscale pertur-

905 bations, as well as the domain size and the presence/absence of larger scale structures.  
906 Future work should also explore the sensitivity to the biogeochemical parameters and  
907 model formulation.

908 In summary, the results presented above demonstrate that submesoscale heterogeneity  
909 can modify the mixing-induced increase in potential energy and thereby the biogeochem-  
910 ical response to a storm by order-one fractions. These results are novel and because they  
911 are from explicit coupled physical-biogeochemical large eddy simulations, which are the  
912 first to couple an NPZD model to LES. In addition, comparisons between the LES and a  
913 vertical column ocean model show for the first time that submesoscale/turbulence inter-  
914 actions, which are not captured by current theory and ocean model parameterizations but  
915 simulated by LES, are responsible for the enhanced storm-driven biogeochemical response.  
916 Thus, submesoscale/turbulence interactions that are not represented in ocean/Earth sys-  
917 tem models may modify phytoplankton seasonal phenology in storm-driven mid-latitude  
918 oceans. Since the biogeochemical impacts of submesoscale/turbulent scale physics in these  
919 idealized experiments is rather strong, future work is needed to assess the broader sig-  
920 nificance, understand the sensitivity of the results to various parameters and values not  
921 considered here, and parameterize these cross-scale physical interactions as well as the  
922 combined physical-biogeochemical interactions.

923 Thus, further experiments to address outstanding uncertainties with expensive  
924 submesoscale-and-turbulence resolving BLES are justified. Nevertheless, a thorough ex-  
925 ploration of these sensitivities using LES may not be feasible. A promising alternative  
926 direction is to use high-resolution LES like those presented here selectively to facilitate  
927 the development and validation of ocean models with horizontal resolutions between 10-

100 m, which can be used to broadly explore the parameter space at a reasonable cost if they perform well in comparisons with LES. However, even this latter approach may require unconventional and expensive non-hydrostatic physical/biogeochemical ocean models. Nevertheless, non-hydrostatic ocean models at 10-100 m resolution are 2-4 orders of magnitude cheaper to run than non-hydrostatic LES at  $\sim 1$  m resolution in the same domain. In addition, some studies have used hydrostatic ocean models with horizontal resolutions down to about 100 m, although the validity of hydrostatic ocean model solutions of the ocean boundary layer at the scales below 2 km is not well understood. Thus, an important outstanding question is if and to what degree a hydrostatic ocean model with  $\sim 100$  m resolution, and therefore only a 10 by 10 or 20 by 20 grid over the 2 km box and a turbulence parameterization, can represent the dynamics simulated using BLES in this paper.

### Appendix: Rationale behind biogeochemical model parameters

The final set of biogeochemical model parameters in Table 2 was determined from many trial simulations of biogeochemical equilibrium profiles with different biogeochemical parameters but the same constant vertical diffusivity using a one-dimensional NPZD model Whitt [2017]. The approach to identifying the final parameter set in Table 2 was ad hoc; parameters are constrained to be reasonably consistent with published data, prior model studies focusing on the eastern North Atlantic, and via inspection of the resulting equilibrium modeled profiles in comparison with the observations reported in Rumyantseva et al. [2015] and Painter et al. [2016] and other available observations. The final parameter set in Table 2 was chosen primarily by identifying (by eye) equilibrium vertical profiles of nutrient ( $N$ ) that matched the observed dissolved silica (DIS) profile reasonably well (Fig.

3). The chosen parameters yield an initial profile that achieves this goal. Although more  
rigorous optimization is certainly possible, such an effort is beyond the scope of this paper  
and in our opinion is unlikely to yield qualitatively different results in the experiments  
presented here. The results are derived from comparisons between different physical mod-  
els with the same biogeochemical model and don't depend on the model being able to  
exactly reproduce observations as long as it is qualitatively reasonable. A rationale for  
some of the chosen parameters based on available data and previously published literature  
is reported below.

The surface photosynthetically available radiation (PAR) is set to  $I_0 = 50 \text{ W/m}^2$ , which  
is equal to the climatological PAR from the pixel nearest the study site ( $48.7^\circ \text{ N}$ ,  $16.4^\circ \text{ W}$ )  
averaged between September and October as obtained from the VIIRS instrument [Ocean  
Ecology Laboratory, Ocean Biology Processing Group NASA Goddard Space Flight Cen-  
ter., 2018]. The e-folding depth scale for the attenuation of light with depth is set to a  
constant  $1/k_w = 18.2 \text{ m}$ , which is intermediate between the observed e-folding depth of  
about  $10 \text{ m}$  [Rumyantseva et al., 2015] and the e-folding depth in clear water in the region  
of about  $30 \text{ m}$  [Fasham & Evans, 1995]. For the parameters in Table 2, the compensation  
depth where phytoplankton photosynthesis is equal to phytoplankton cellular respiration,  
that is where  $U = \sigma_d$ , and the 1% light level are both between  $80$  and  $90 \text{ m}$ . The initial  
equilibrium profiles are highly sensitive to the chosen e-folding depth  $1/k_w$ . If the other  
parameters are held fixed, neither the e-folding depth chosen by Fasham & Evans [1995]  
nor the value observed by Rumyantseva et al. [2015] produces an equilibrium profile that  
is a good match to observations before the storm. For simplicity, phytoplankton have  
no explicit influence on the PAR profile, unlike most other NPZD models. Rumyantseva

973 et al. [2015] observe relatively small temporal changes in the e-folding depth of the PAR  
974 profile during the storm event, so the dynamic nature of the PAR profile is thought to be  
975 a minor effect.

976 Thee phytoplankton parameters,  $\alpha$ ,  $V_m$ , and  $k_N$ , and  $\sigma_d$  were taken from the models  
977 of Fasham & Evans [1995], and are fairly typical of NPZD-class models. The mortality  
978 parameter  $\sigma_d$  only indirectly affects the solution (via its influence on the initial condition)  
979 in these short 6-day experiments, which are about a quarter of the phytoplankton specific  
980 mortality e-folding timescale. The zooplankton parameters,  $R$ ,  $\Lambda$ ,  $\gamma_n$ ,  $\zeta$  and  $\hat{\zeta}$  are less well  
981 known than the phytoplankton parameters and are tuned somewhat to produce reasonable  
982 initial conditions, but these are still fairly typical for NPZD-class models.

983 The detrital remineralization depth scale (sinking velocity  $w_d$  divided by specific rem-  
984 ineralization rate  $\delta$ ) in the models of Fasham & Evans [1995] ranges from 100 to 400 m.  
985 Here, a much smaller value of 2.5 m is used in order to get an equilibrium in the 80 m  
986 depth domain with such simplified forcing (i.e., with a constant vertical diffusivity and no  
987 surface mixing layer). This is mostly achieved by both reducing the sinking speed from  
988 3-6 m/d to  $w_d = 0.25$  m/d and increasing the detrital remineralization rate from 0.01-  
989  $0.06 \text{ d}^{-1}$  to  $0.1 \text{ d}^{-1}$ . These choices help in achieving realistic nutrient and phytoplankton  
990 profiles in a one-dimensional equilibrium without seasonal nutrient replenishment by deep  
991 mixing. The chosen sinking velocity is somewhat unconventional and therefore should be  
992 viewed largely as a tuning knob that helps to create an initial equilibrium profile that is  
993 similar to observations in this study. This is a reasonable approach in this case, because  
994 remineralization timescales are generally longer than the timescales of interest here (<6  
995 days) and neither export nor remineralization are explicitly considered in this paper.



1000 In order to crudely represent all external physical sources of nutrient that are missing  
1001 in this model, such as upwelling or vertical mixing of water with higher nutrient concen-  
1002 trations from deeper depths, nutrient is restored to a value of  $N_{80} = 2.5 \text{ mmol/m}^3$  over a  
1003 timescale  $1/\beta = 4$  days at the bottom grid cell only, that is at 80 m depth. The objective  
1004 of this restoring is primarily to achieve an equilibrium vertical nutrient profile like the  
1005 observed DIS profile observed during September 2012 (Fig. 3 (b)). The choice to tune  
1006 the model parameters to fit the observed DIS profile as opposed to other macronutrients  
1007 probably does not change the qualitative results very much. Observed dissolved inorganic  
1008 nitrogen (DIN) and phosphorous (DIP) profiles look much the same as DIS, hence initial-  
1009 izing with those profiles would also result in an enhanced vertical nutrient flux during the  
1010 storm. However, the observed stoichiometric ratios are not perfectly linear (see Fig. 13 of  
1011 Painter et al. [2016]). For example, the DIN:DIS ratio is about 5:1 at small concentrations  
1012 in the upper 60 m but follows a 2:1 line at higher concentrations between 60 m and 120  
1013 m. In addition, the DIN:DIP ratio follows an 18:1 line. The ratios of particulate organic  
1014 nitrogen (PON) to biogenic silica (BSi) are about 5:1 to 10:1 in the upper 50 m [see Fig.  
1015 14 of Painter et al., 2016].

1016 The quantitative results presented in this paper are sensitive to the chosen biogeochem-  
1017 ical parameters, which are reflected in the one-dimensional equilibrium solution used as  
1018 the initial condition for the forced experiments. However, it is beyond the scope of this  
1019 paper to show explicitly how either the biogeochemical initial conditions or the results  
1020 of the wind-forced experiments are sensitive to changes in the biogeochemical model pa-  
1021 rameters. The qualitative and quantitative sensitivity of one-dimensional NPZD-class  
1022 models to changes in the biogeochemical model parameters is discussed elsewhere [e.g.,

1019 McGillicuddy et al., 1995; Doney et al., 1996; Evans & Garçon, 1997; Franks, 2002; Beck-  
1020 mann & Hense, 2007]; recent and relevant discussions about the sensitivity of the phyto-  
1021 plankton and nutrient responses to wind-driven nutrient entrainment events in a similar  
1022 NPZD-class model can be found in Whitt et al. [2017b] and Whitt et al. [2017a] (n.b.,  
1023 supplemental section 4.1 of Whitt et al. [2017b]). The upshot is that the quantitative  
1024 biogeochemical results should not be viewed as an exact reproduction of specific ocean  
1025 conditions, despite some efforts documented above to choose parameters that are relevant  
1026 to the observations reported by Rumyantseva et al. [2015] and Painter et al. [2016] in  
1027 particular and the eastern North Atlantic more generally. However, the modeled biogeo-  
1028 chemical responses to the different transient forcing scenarios in different physical models,  
1029 all with the same biogeochemical model equations, parameters, and initial conditions,  
1030 provide perspective on the physics of the different scenarios as well as the qualitative  
1031 sensitivity of the biogeochemical response to physical differences alone. Hence, the dis-  
1032 cussion of the results focuses on the qualitative features of the biogeochemical solutions  
1033 and comparisons between scenarios over the precise quantitative features of the results,  
1034 which can nevertheless be obtained from the figures and the public data [Whitt, 2018].

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1046 ([github.com/danielwhitt/ROMS](https://github.com/danielwhitt/ROMS)) is publicly available, and the initial condition data nec-  
1047 essary to reproduce the simulation is archived online [Whitt, 2018]. The plotting scripts  
1048 and associated data are archived with the initial conditions.

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**Table 1.** List of simulations

Simulation and parameterizations	grid points (x,y,z)	grid resolution	max $ \tau $	$\langle M^2 \rangle_{x,y}$
1. LES with front (LES,F)	1024×1024×160	1.9×1.9×0.5 m	0.3 N/m <sup>2</sup>	$5.0 \times 10^{-8} \text{ s}^{-2}$
2. Column model with front, KPP, and FFH (ROMS,F)	2×2×160	39×39×0.5 m	0.3 N/m <sup>2</sup>	$5.0 \times 10^{-8} \text{ s}^{-2}$
3. LES without front (LES,NF)	256×256×160	1.9×1.9×0.5 m	0.3 N/m <sup>2</sup>	0 s <sup>-2</sup>
4. Column model with KPP (ROMS,NF)	2×2×160	39×39×0.5 m	0.3 N/m <sup>2</sup>	0 s <sup>-2</sup>
5. LES with front (LES,F)	1024×1024×160	1.9×1.9×0.5 m	0.6 N/m <sup>2</sup>	$5.0 \times 10^{-8} \text{ s}^{-2}$
6. Column model with front, KPP, and FFH (ROMS,F)	2×2×160	39×39×0.5 m	0.6 N/m <sup>2</sup>	$5.0 \times 10^{-8} \text{ s}^{-2}$
7. LES without front (LES,NF)	256×256×160	1.9×1.9×0.5 m	0.6 N/m <sup>2</sup>	0 s <sup>-2</sup>
8. Column model with KPP (ROMS,NF)	2×2×160	39×39×0.5 m	0.6 N/m <sup>2</sup>	0 s <sup>-2</sup>

**Table 2.** Biogeochemical Model Parameters

Parameter	Symbol	Value
Light attenuation due to seawater	$k_w$	0.055 m <sup>-1</sup>
Initial slope of the productivity-irradiance curve	$\alpha$	0.1 d <sup>-1</sup> (W/m <sup>2</sup> ) <sup>-1</sup>
Surface photosynthetically available radiation	$I_0$	50 W/m <sup>2</sup>
Phytoplankton max. uptake rate	$V_m$	1.5 d <sup>-1</sup>
Half-saturation for nutrient uptake by phy.	$k_N$	0.8 mmol /m <sup>3</sup>
Phytoplankton mortality rate to detritus	$\sigma_d$	0.04 d <sup>-1</sup>
Ivlev constant for zooplankton grazing	$\Lambda$	0.5 (mmol /m <sup>3</sup> ) <sup>-1</sup>
Maximum zooplankton grazing rate	$R$	0.9 d <sup>-1</sup>
Zooplankton excretion to nutrient	$\gamma_N$	0.3
Linear zooplankton mortality rate	$\zeta$	0.04 d <sup>-1</sup>
Quadratic zooplankton mortality rate	$\hat{\zeta}$	0.28 d <sup>-1</sup> (mmol/m <sup>3</sup> ) <sup>-1</sup>
Detritus remineralization rate	$\delta$	0.1 d <sup>-1</sup>
Detrital sinking velocity	$w_d$	-0.25 m/d
Restoring nutrient concentration at 80 m	$N_{80}$	2.5 mmol/m <sup>3</sup>
Inverse restoring timescale for nutrient at 80 m	$\beta_N$	0.25 d <sup>-1</sup>

**Figure 1.** Slices from showing the snapshots of the density and vertical velocity in a large eddy simulation of the frontal zone, just before the storm forcing begins. The horizontal slices (top panels) are at 21 m depth and the vertical slices (bottom panels) are 947 m across the front, as indicated by the dashed lines. Density anomaly (a) and vertical velocity (b) are shown. Black contours of the density (smoothed by convolving with a 150 m square boxcar kernel) are plotted every 0.0025 kg/m<sup>3</sup> on all panels. However, only the least dense 0.035 kg/m<sup>3</sup> of the density range is contoured in order to highlight the density variability in the mixed layer rather than the pycnocline. The bottom panels show only the top 50 m to highlight the surface properties of interest.

1286

**Figure 2.** Time series of the magnitude of the surface stress (solid lines), which is directed to the southeast  $45^\circ$  to the right of the mean geostrophic flow at the surface in both scenarios. The atmospheric and Ekman buoyancy flux  $B_A+EBF$ , where  $B_A = 3 \times 10^{-9} \text{ m}^2/\text{s}^3$  is constant, is indicated by the dotted lines. The thick black lines indicate two different averaging windows used in the subsequent analysis: days 2-3 and days 5-6.

**Figure 3.** Solid lines are initial model profiles of phytoplankton  $P$  ( $\text{mmol}/\text{m}^3$ ), nutrient  $N$  ( $\text{mmol}/\text{m}^3$ ), and density  $\rho$  ( $\text{kg}/\text{m}^3$ ). The model currency for  $N$  and  $P$  is the same:  $\text{mmol}/\text{m}^3$  of a single generalized “nutrient.” Solid and dotted black horizontal lines indicate the initial depths of  $MLD_{05}$  and  $MLD_3$ , respectively. Scattered black points are observed in-situ chlorophyll-a fluorescence ( $\text{mg}/\text{m}^3$ ) (a), dissolved inorganic silica ( $\text{mmol}/\text{m}^3$ ) (b), and the potential density ( $\text{kg}/\text{m}^3$ ) (c) from 3 profiles taken above the Porcupine Abyssal Plain during September 21-22, 2012 on cruise D381B [Painter et al., 2016]. Biogenic silica particulate concentrations (not shown) are scattered between about 0.05 and 0.25  $\text{mmol}/\text{m}^3$ , and exhibit no obvious subsurface maximum like chlorophyll-a fluorescence [Fig. 14a in Painter et al., 2016]. Only the top 60 m is shown to highlight the surface properties of interest.



**Figure 4.** Horizontally-averaged vertical profiles of phytoplankton  $\langle P \rangle_{x,y}$ , nutrient  $\langle N \rangle_{x,y}$ , and density  $\langle \rho \rangle_{x,y}$  averaged over two time periods during the evolution of the idealized storm life cycle, including  $t = 2 - 3$  days (during the storm), and  $t = 5 - 6$  days (after the storm). Mixed layer depths based on the  $\Delta \langle \rho \rangle_{x,y} = 0.005 \text{ kg/m}^3$  threshold ( $MLD_{05}$ , thin solid) and  $\Delta \langle \rho \rangle_{x,y} = 0.03 \text{ kg/m}^3$  threshold ( $MLD_3$ , dotted) are also shown. Note the dotted lines essentially overlap, that is  $MLD_3$  is about the same in both the F and NF cases.

**Figure 5.** (a) Time-integrated wind work,  $\Delta KE = \frac{1}{1 \text{ day}} \int_{t=5 \text{ days}}^{t=6 \text{ days}} \int_0^t \boldsymbol{\tau} \cdot \mathbf{u}_h(z=0) ds dt$  where  $s$  is a dummy time integration variable, and (b) the mixing ratio  $r_m = \Delta PE^* / \Delta KE$  where  $\Delta PE^*$  is the residual change in potential energy due to vertical mixing, which is defined in (4). In both  $\Delta KE$  and  $\Delta PE^*$ ,  $\Delta$  indicates that the difference is taken between an average over  $t = 5 - 6$  days and  $t = 0$  days.

**Figure 6.** Full-depth column integrals of phytoplankton  $\langle P \rangle_{x,y}$  (a) and storm-driven  $\langle NCP \rangle_{x,y}$  (b), averaged over three time periods. The reduction in column-integrated  $\langle N \rangle_{x,y}$  is equal to the storm-driven  $\langle NCP \rangle_{x,y}$  here.

**Figure 7.** Slices of nutrient concentration  $N$  (a),(c) and vertical nutrient flux  $wN$  (b),(d) during the storm forcing from the LES,F (a)-(b) and LES,NF (c)-(d) scenarios. The horizontal slices (top panels) are at -39.5 m and -38.5 m respectively, that is 4 m above  $MLD_3$  in both cases. The horizontal slices are at the depths indicated by the black dashed lines in the adjacent vertical slices/bottom panels, while the vertical slices are at the location indicated by the dashed lines in the adjacent horizontal slices. Solid black contours of density (smoothed with a 150 m moving average) are plotted every  $0.005 \text{ kg/m}^3$  on all panels. The vertical slices show only the top 50 m to highlight the surface properties of interest. The vertical velocities (not shown) are an order of magnitude stronger than in Fig. 1 (b).

**Figure 8.** Multi-scale vertical profiles of horizontal nutrient variance  $var(N)_{x,y}(z)$ , both during (a),(c),(e) and after (b),(d),(f) the storm. Submesoscales (a)-(b), that is wavelengths between 0.15 and 2 km, are separated from smaller-turbulent scales (c)-(d), that is wavelengths  $< 0.15$  km. The mixed layer depths  $MLD_3$  (dotted) and  $MLD_{05}$  (solid) are plotted as thin horizontal lines.

**Figure 9.** Multi-scale vertical nutrient fluxes  $\langle wN \rangle_{x,y}(z)$ , both during (a),(c),(e) and after (b),(d),(f) the storm. Submesoscale fluxes are shown in (a)-(b), turbulent scale fluxes are shown in (c)-(d), and total (submesoscale+turbulent) are shown in (e)-(f). The mixed layer depths  $MLD_3$  (dotted) and  $MLD_{05}$  (solid) are plotted as thin horizontal lines. Note the different  $x$ -axes.

**Figure 10.** Horizontally-averaged profiles of the total vertical flux (a)-(b) and diffusivity (c)-(d) of nutrient in the LES,F and ROMS,F scenarios with a front/submesoscales.  $MLD_3$  (dotted) and  $MLD_{05}$  (solid) are plotted for reference. Note the different x-axes in (a)-(b).

**Figure 11.** Horizontally-averaged profiles of the total vertical flux (a)-(b) and diffusivity (c)-(d) of nutrient in the LES,NF and ROMS,NF scenarios without a front/submesoscales.  $MLD_3$  (dotted) and  $MLD_{05}$  (solid) are plotted for reference. Note the different x-axes in (a)-(b).



**Figure 12.** Comparisons between LES and ROMS with (a)-(b) and without (c)-(d) a front/submesoscales. Full-depth column integrals of  $\langle P \rangle_{x,y}$  (a),(c) and  $\langle NCP \rangle_{x,y}$  (b),(d). All variables are presented as averages over three different time windows, as in Fig. 6.

Figure 1.

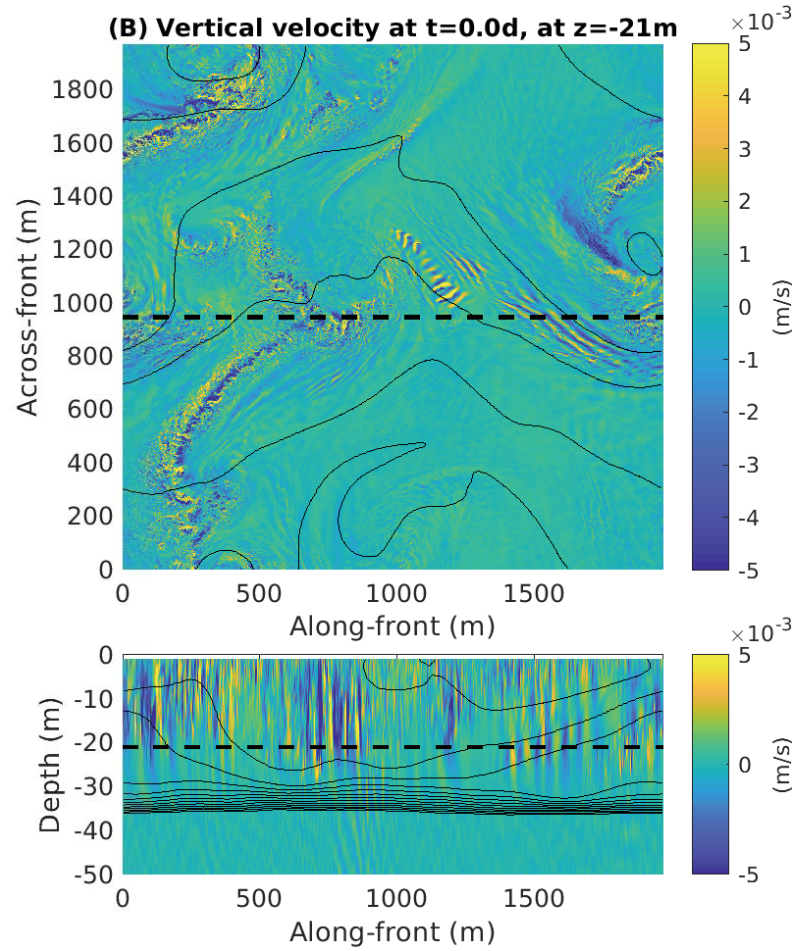
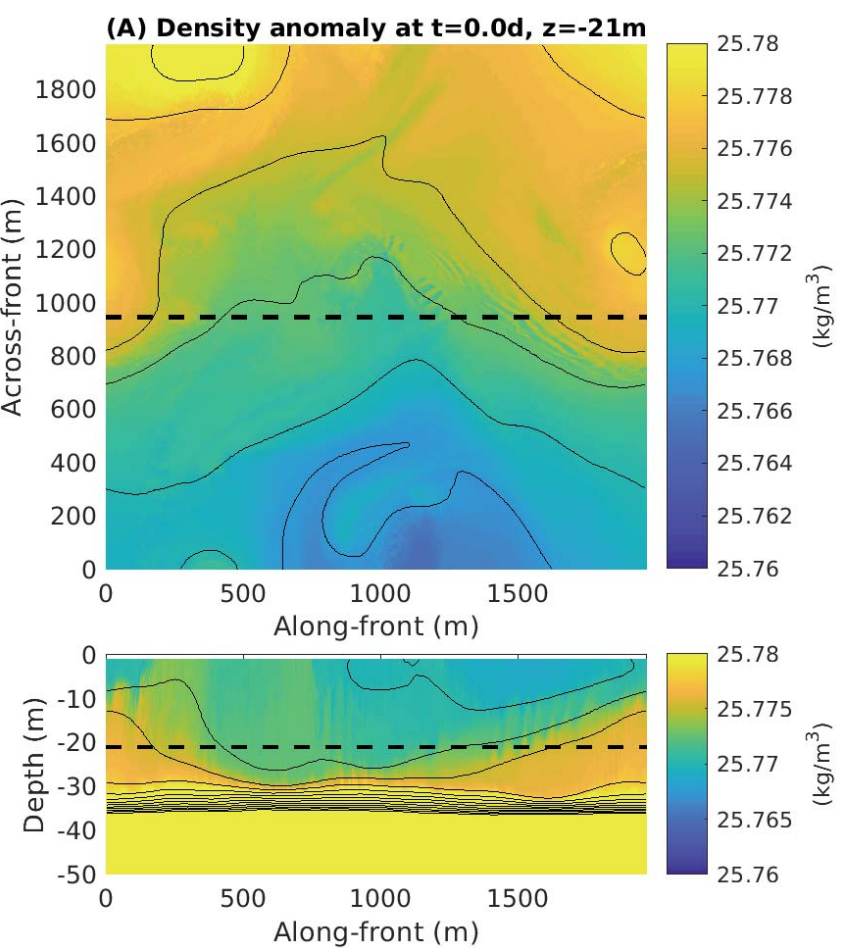


Figure 2.

Surface stress and Atmospheric+Ekman buoyancy flux

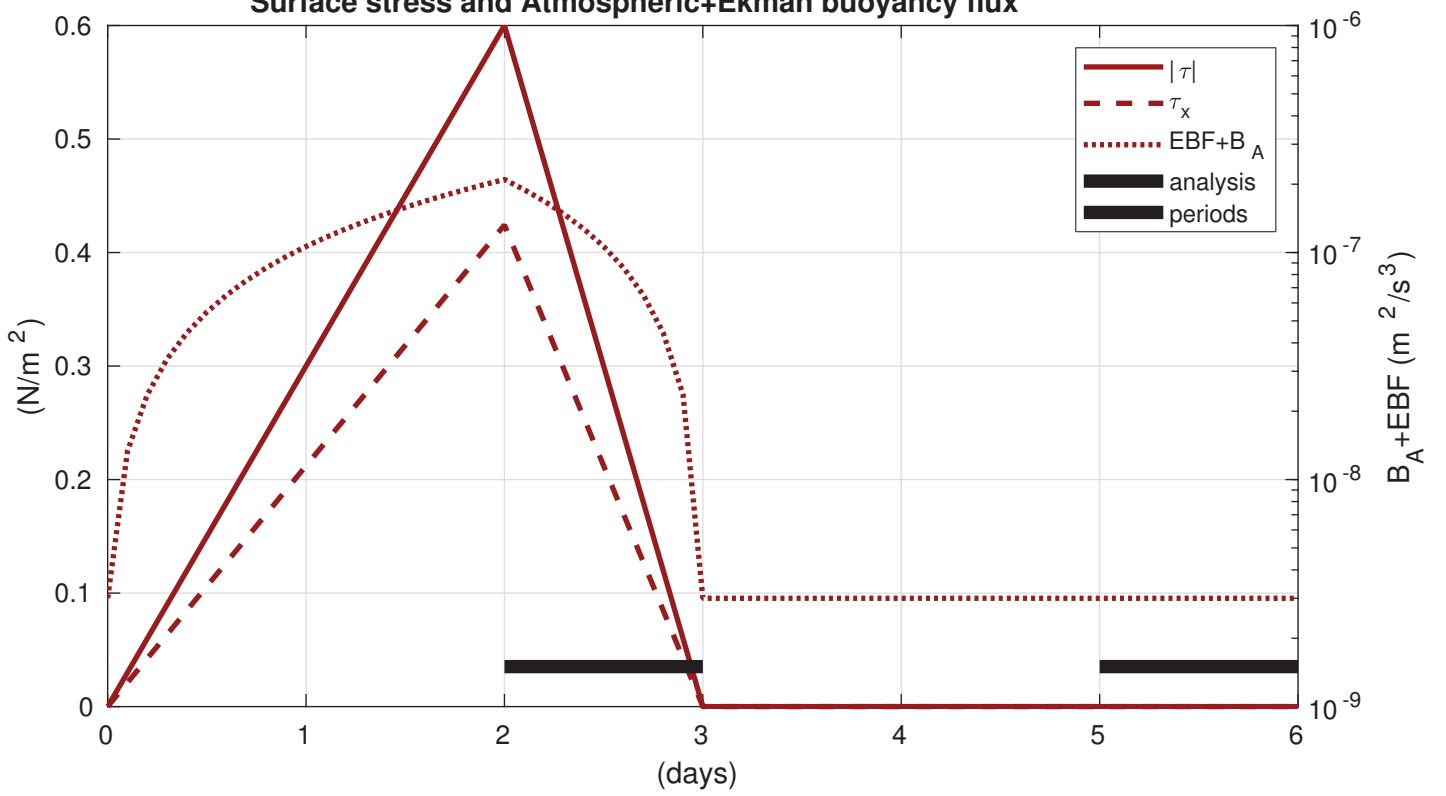
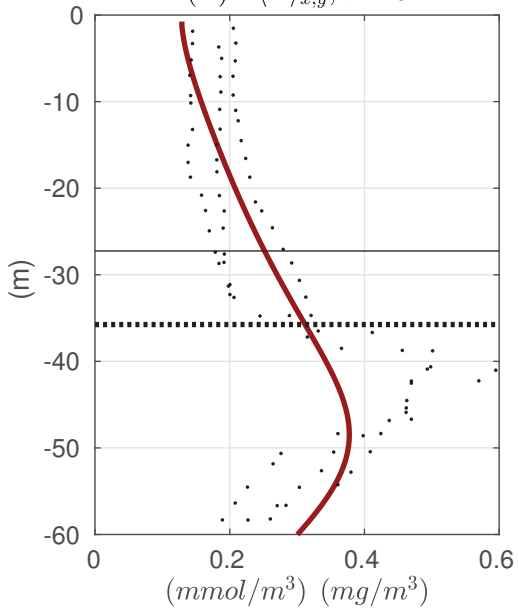
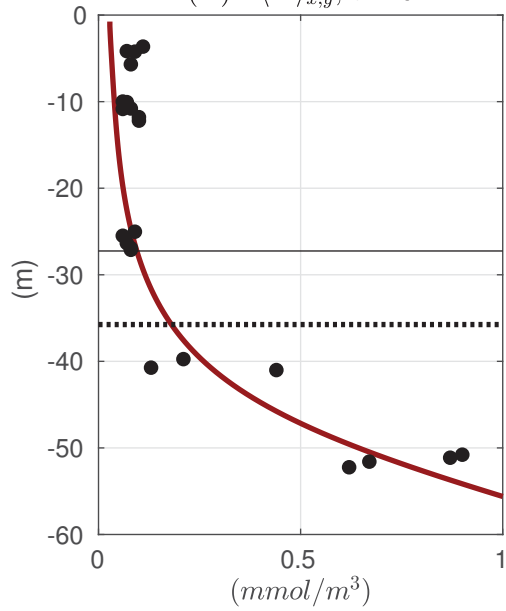


Figure 3.

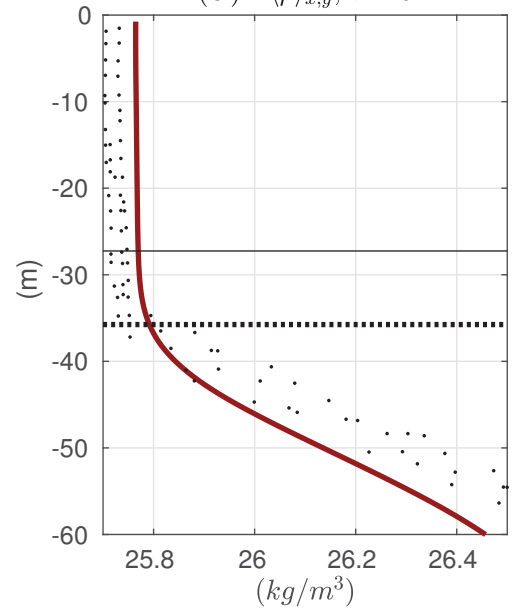
(A)  $\langle P \rangle_{x,y}, t = 0$



(B)  $\langle N \rangle_{x,y}, t = 0$



(C)  $\langle \rho \rangle_{x,y}, t = 0$



**Figure 4.**



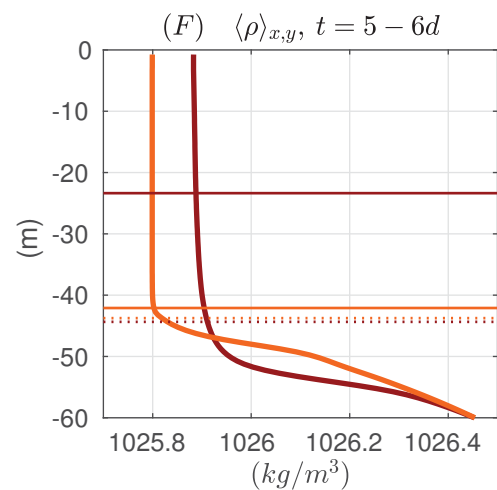
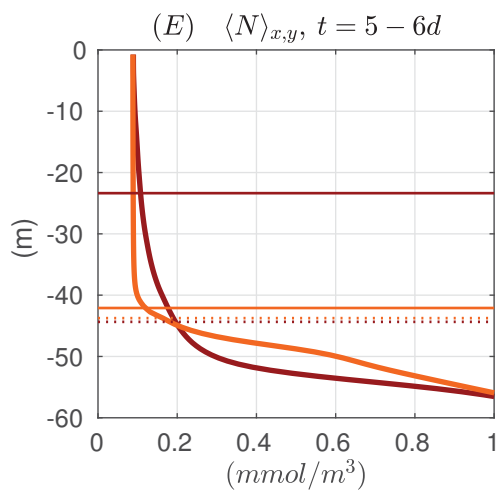
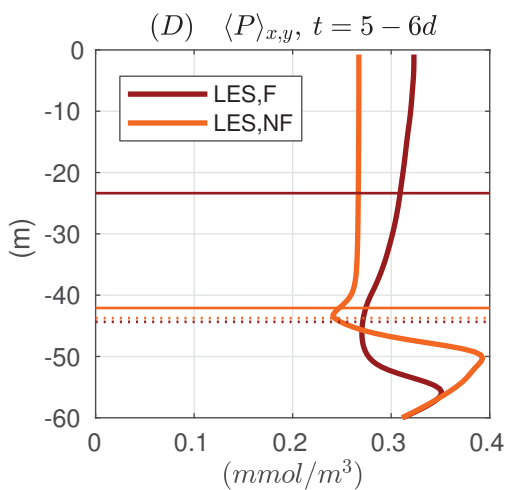
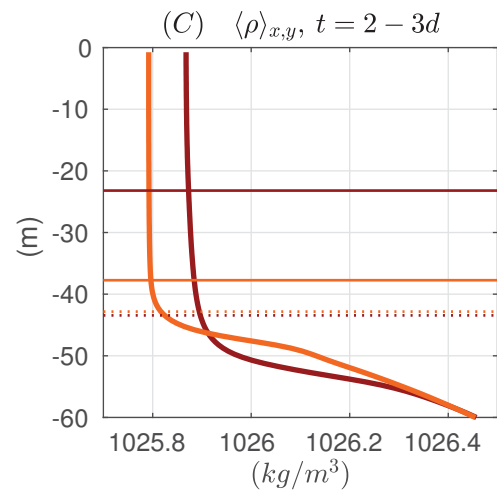
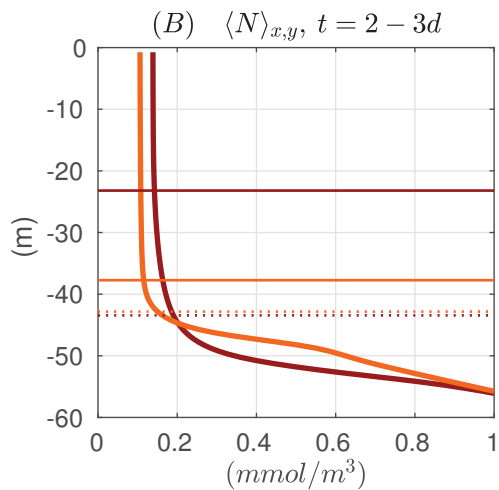
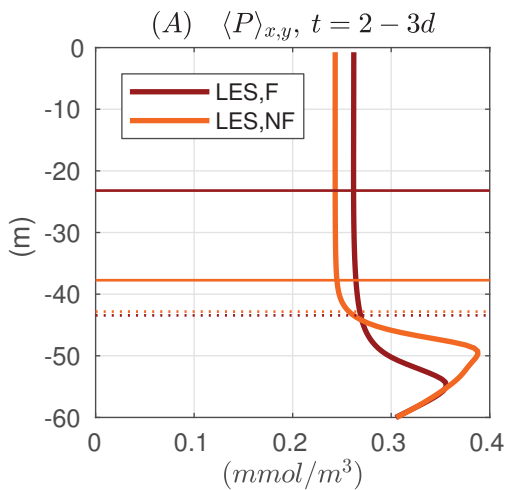


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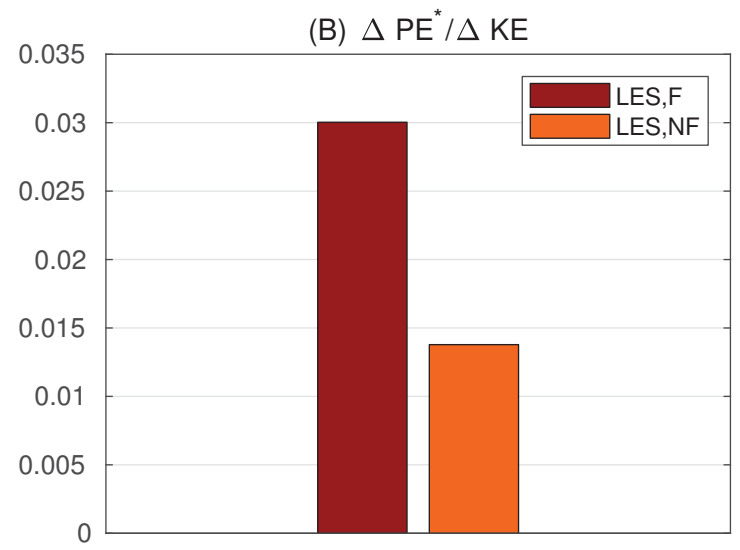
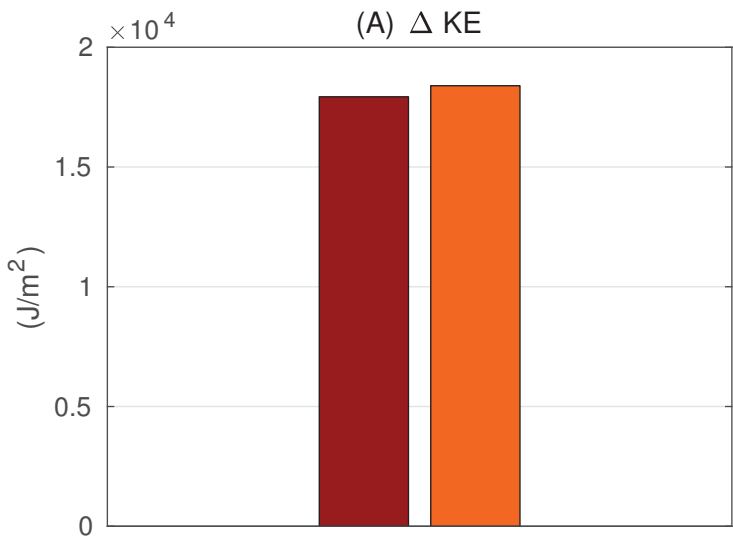


Figure 6.

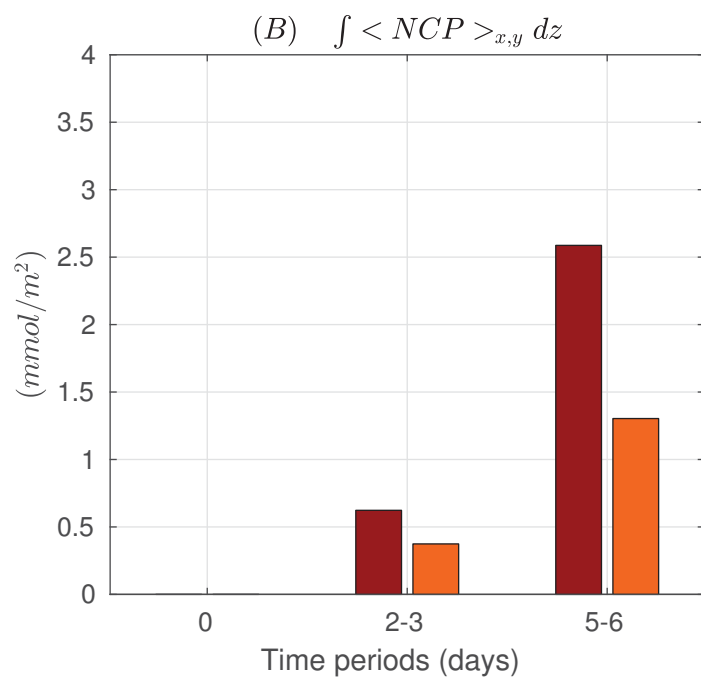
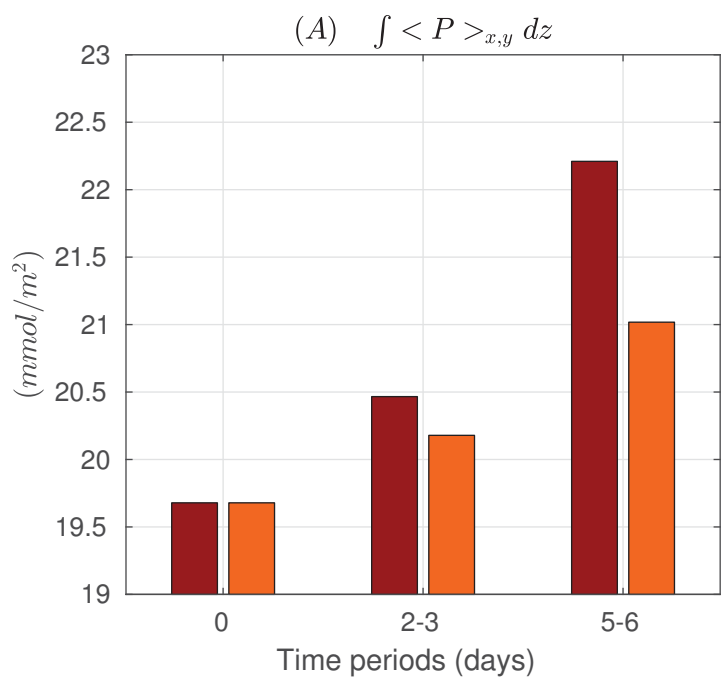


Figure 7.

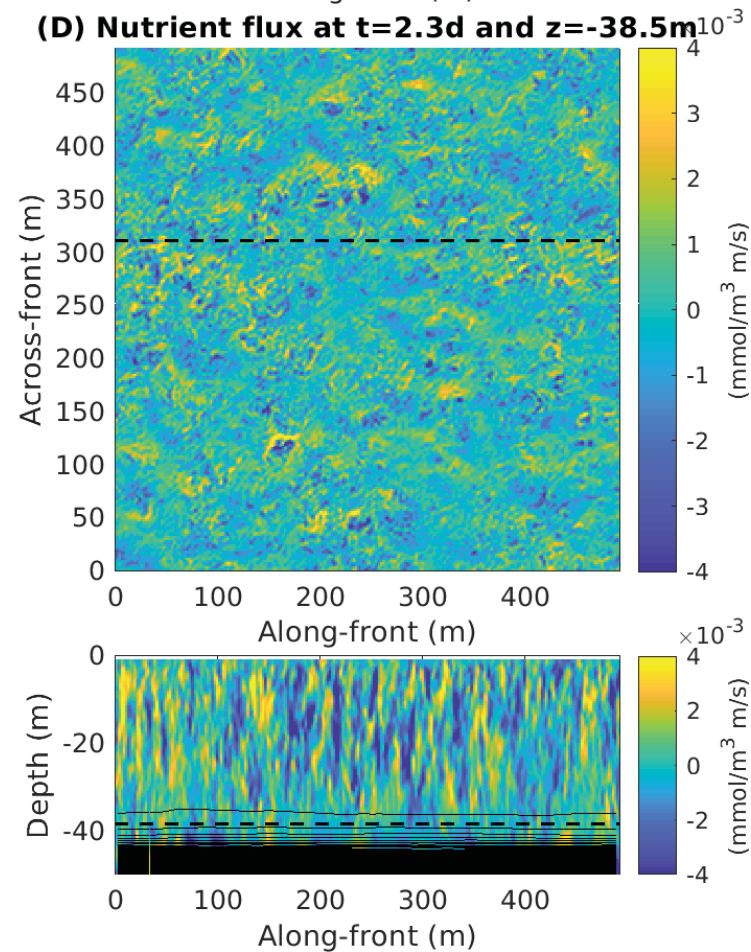
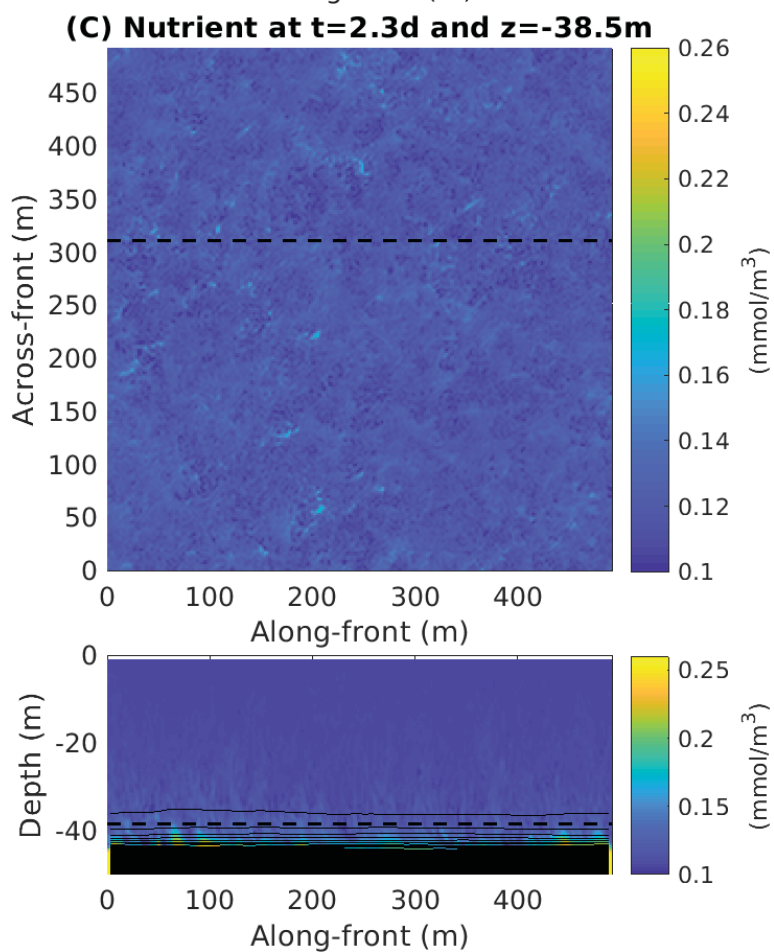
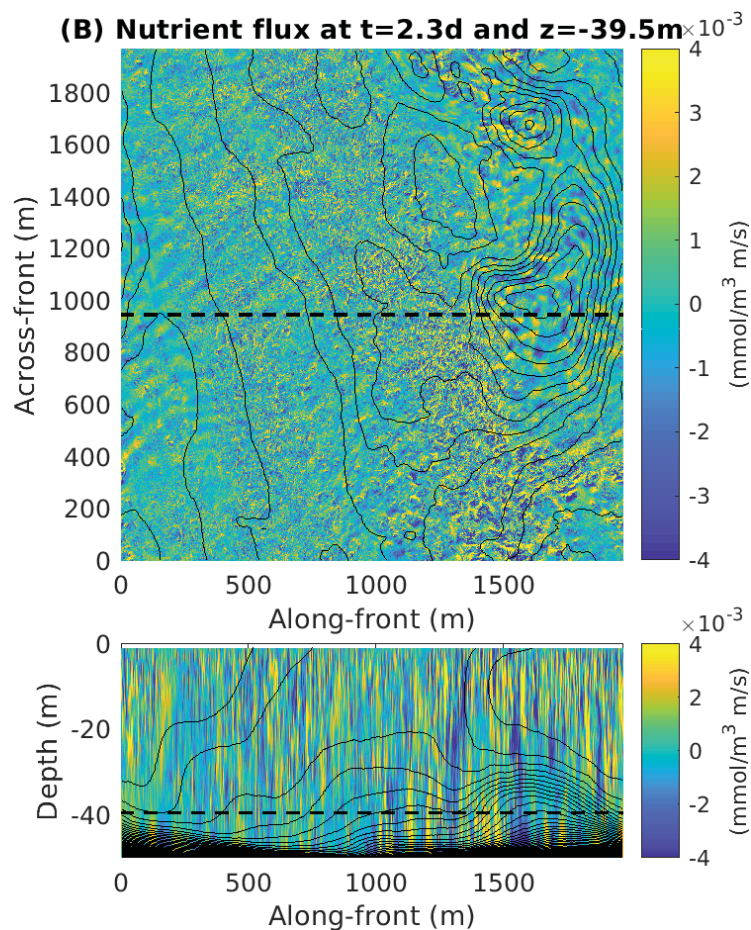
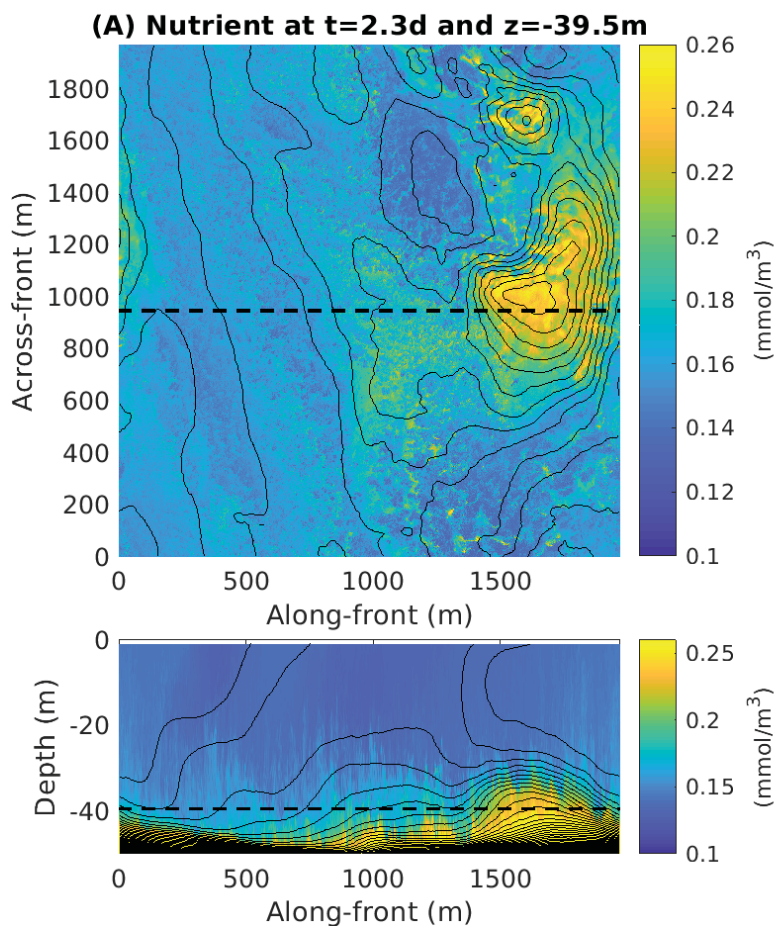


Figure 8.



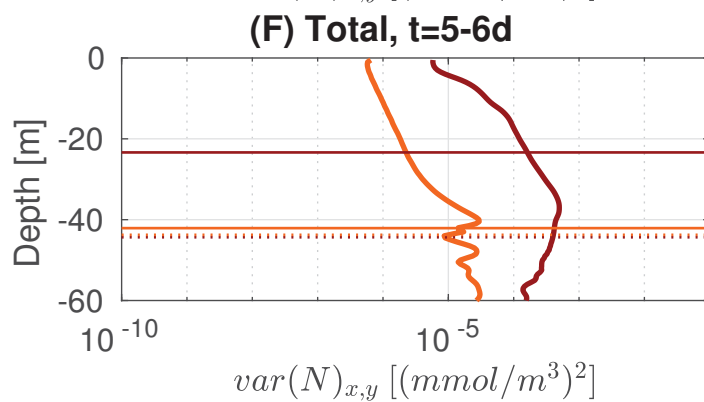
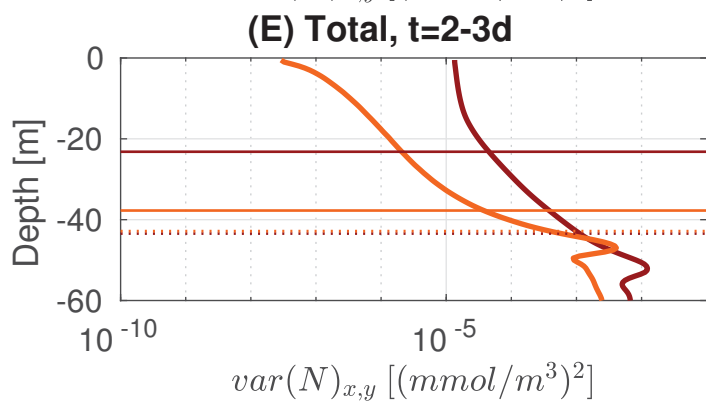
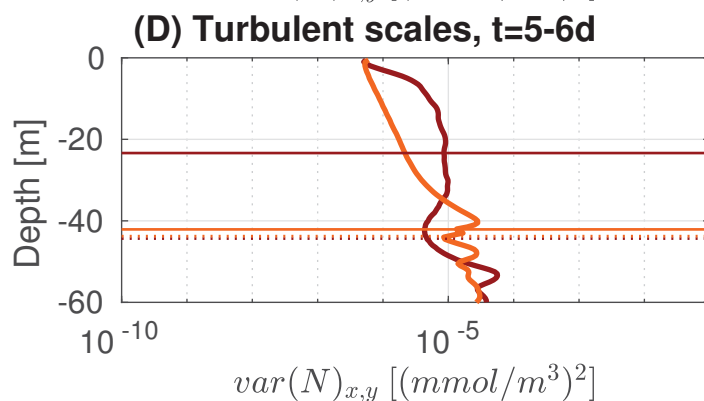
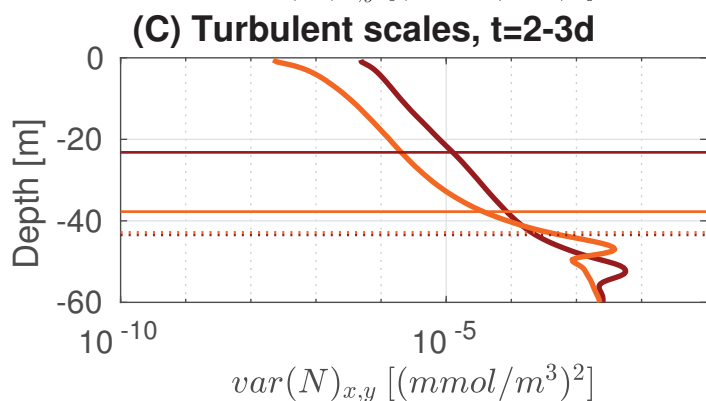
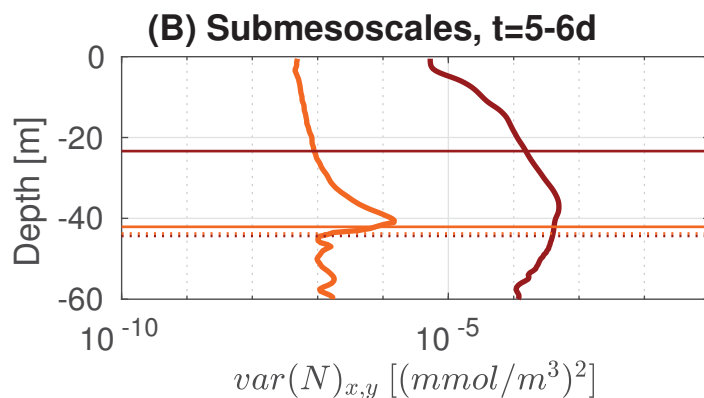
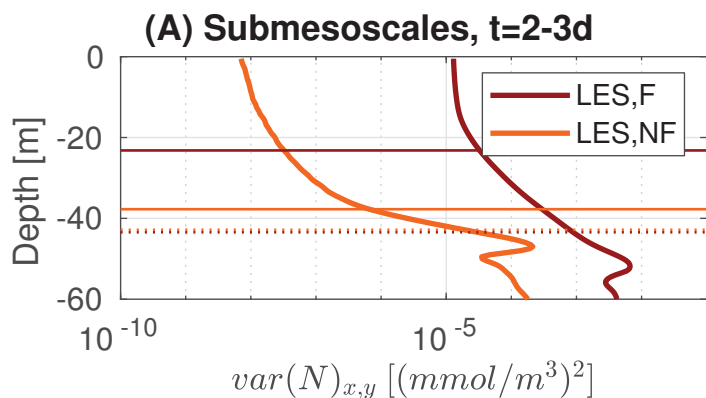


Figure 9.

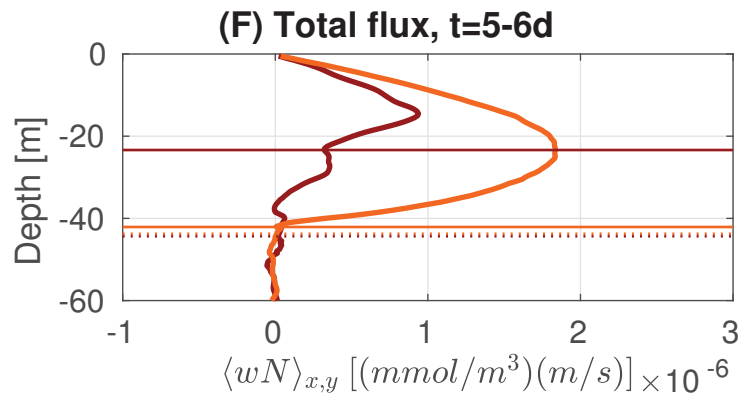
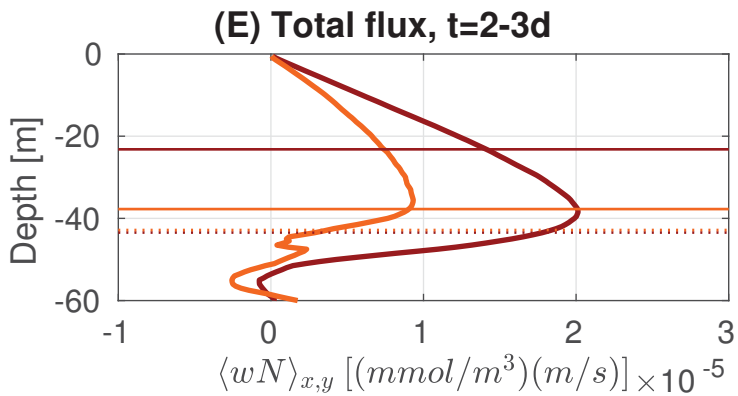
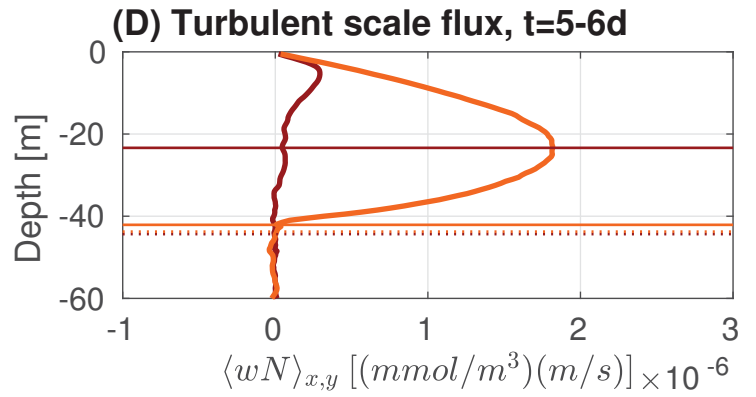
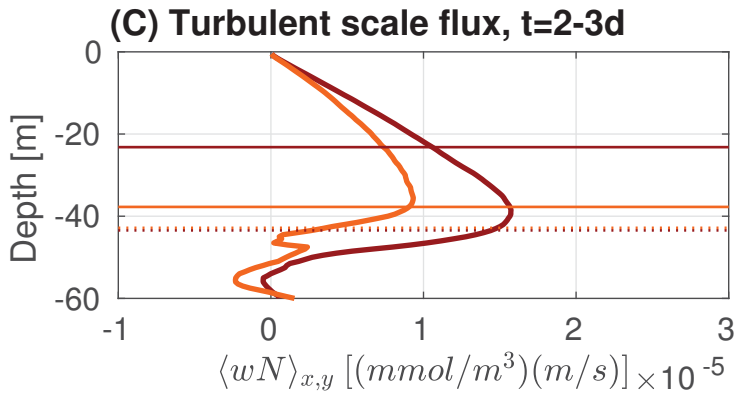
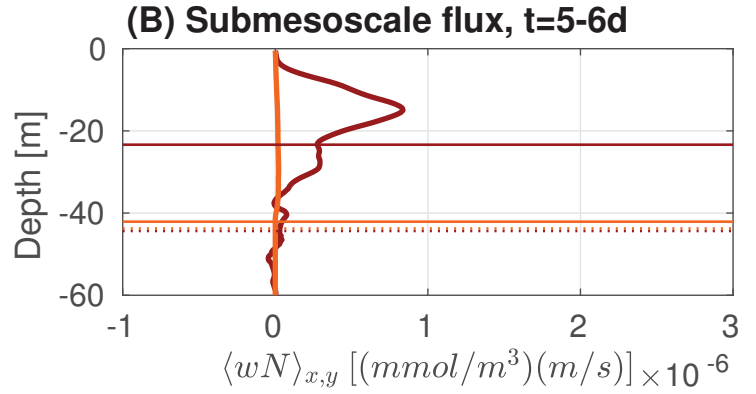
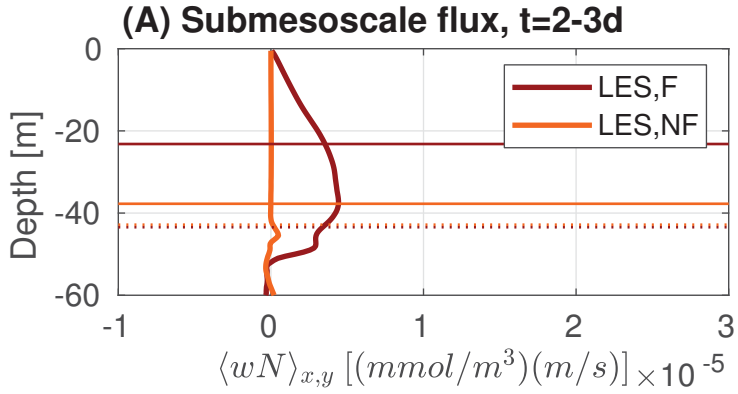
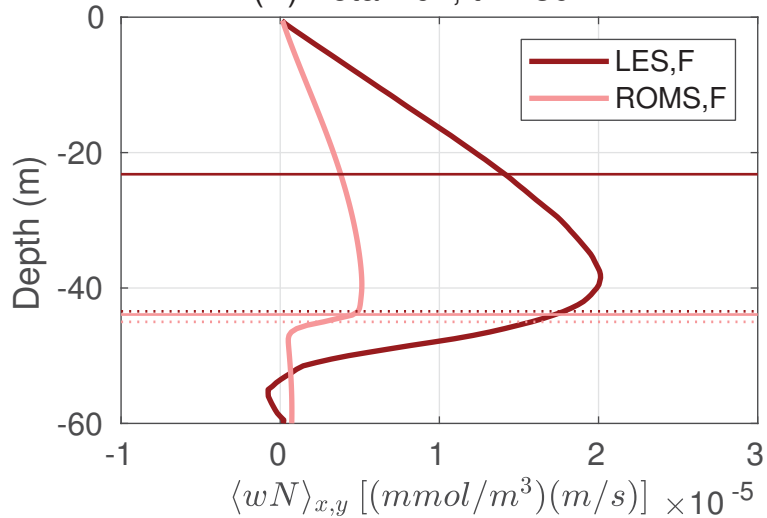
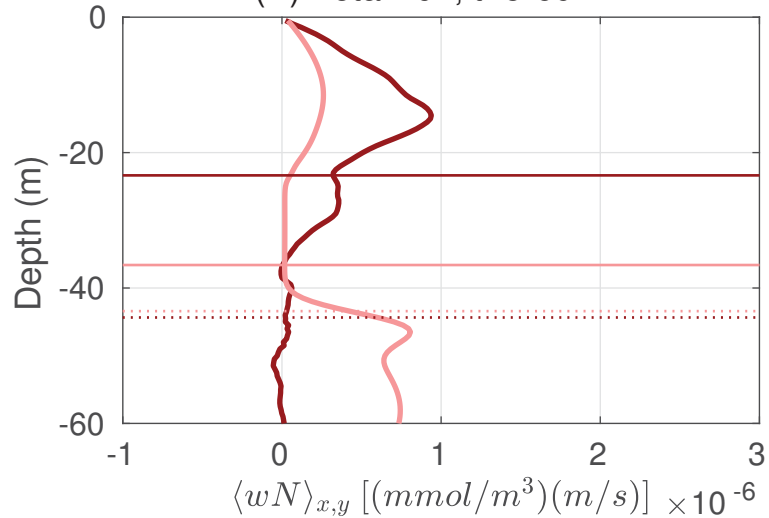


Figure 10.

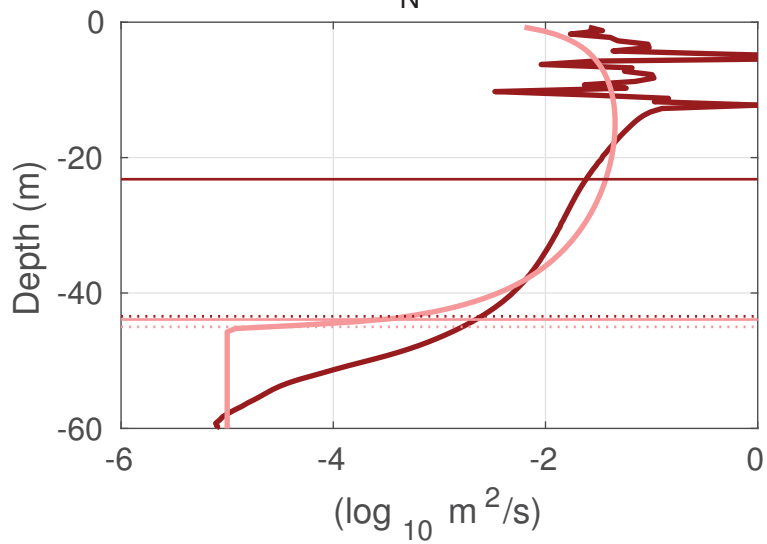
(A) Total flux, t=2-3d



(B) Total flux, t=5-6d



(C)  $\kappa_N$ , t=2-3d



(D)  $\kappa_N$ , t=5-6d

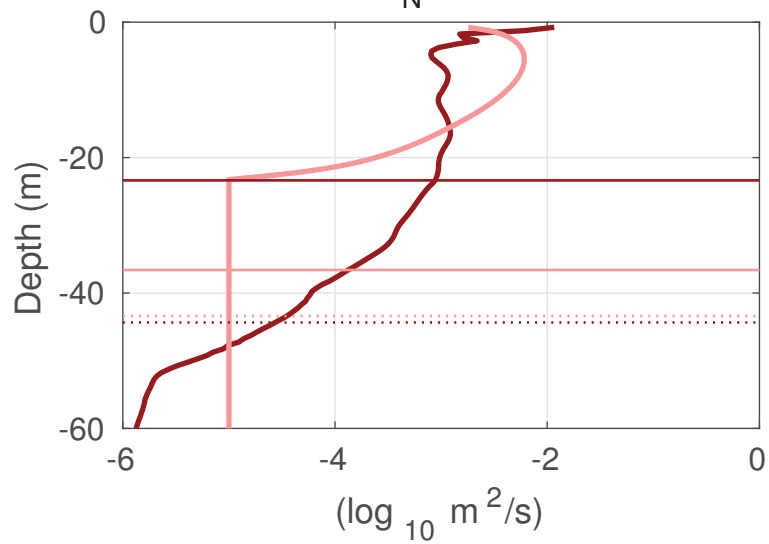
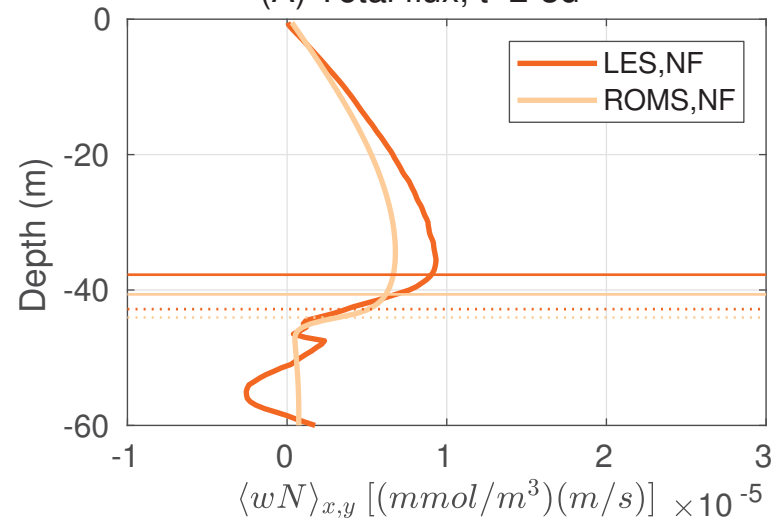
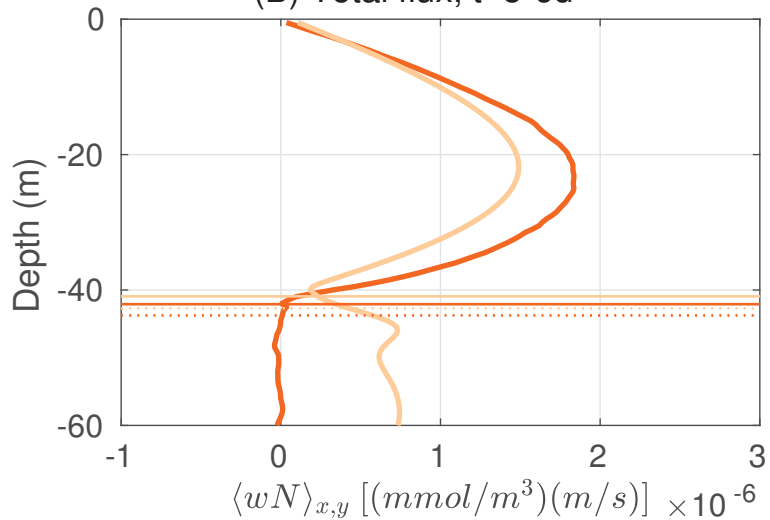


Figure 11.

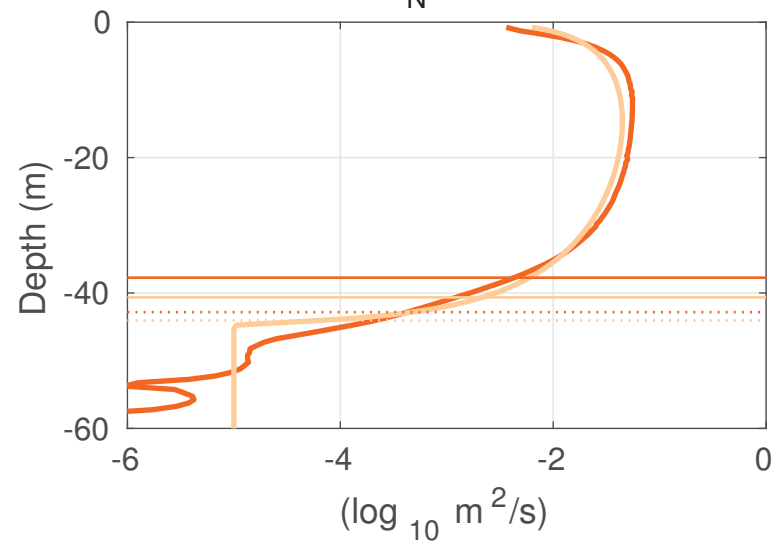
(A) Total flux, t=2-3d



(B) Total flux, t=5-6d



(C)  $\kappa_N$ , t=2-3d



(D)  $\kappa_N$ , t=5-6d

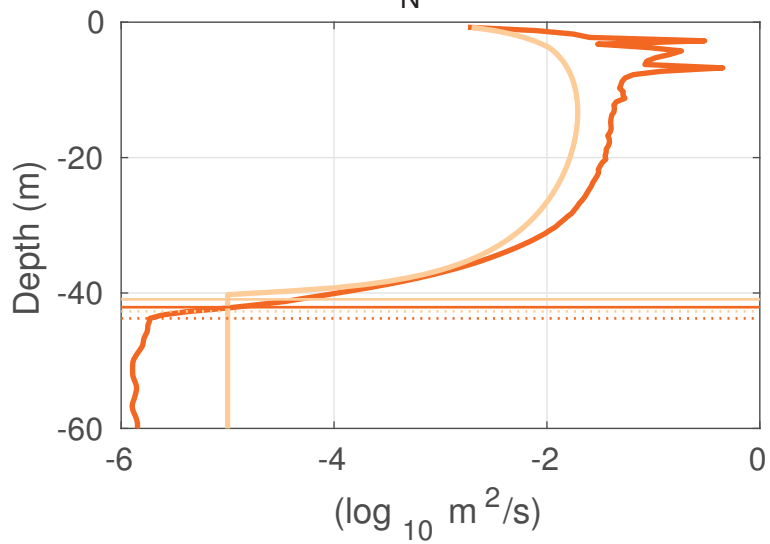


Figure 12.



