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Blind Signal Detection Under Synchronization Errors for FSO Links with High Mobility

M. T. Dabiri, S. M. S. Sadough, M. A. Khalighi

Abstract—We consider the use of free-space optical communication for fast moving platforms such as high-speed trains where the sampling clock offset is randomly changing and, in addition, the receiver does not have any information on the instantaneous channel fading coefficient. By employing multiple samplers at the receiver, we propose a class of sequence detection methods for the case of OOK signaling without using any training sequence. First, we study maximum likelihood based detection, which has a relatively high computational complexity. Second, by employing generalized likelihood ratio test, we propose a more practical blind sequence detection method of reduced complexity. To further reduce the computational complexity, third, we propose a novel scheme that uses two wavelengths at the transmitter and differential blind detection at the receiver. Fourth, to benefit from diversity gain with this differential scheme, we consider the use of sufficiently different wavelengths, where we propose an efficient blind detection method. The pros and cons of each proposed detection method are contrasted through numerical results and their processing load are compared as well.

Index Terms—Free-space optics; blind data detection; differential signaling; synchronization; atmospheric turbulence.

I. Introduction

Free-space optical (FSO) communication is well known as a promising wireless access technology thanks to its features of huge available license-free spectrum, low-cost implementation, and robustness to electromagnetic interference [2]. Due to the relatively low implementation complexity, intensity modulation with direct detection (IM/DD) based on On-Off keying (OOK) is used in most current commercial FSO systems. Nevertheless, for optimal signal demodulation, adaptive threshold setting is required at the receiver (Rx), which needs, in turn, accurate channel estimation [3]. Channel estimation is classically done through the transmission of multiple pilot symbols per frame. However, this pilot overhead results in a spectral efficiency loss, in particular for the case of fast-varying channels [4], [5]. To avoid transmitting pilot symbols, a few earlier works have investigated maximumlikelihood (ML) sequence detection and its generalization [6], [7]. However, the proposed methods generally suffer from high computational complexity which may be of critical concern for practical implementation of FSO systems. Therefore, some more recent works, such as [8]-[16], have tried to design

Parts of this work have been presented at the 11th International Symposium on Communication Systems, Networks, and Digital Signal Processing (CSNDSP), Budapest, Hungary, July 2018, Reference [1].

lower complexity signal detection methods. However, in [8]–[16] it i assumed that the transceiver is perfectly synchronized. Although, such assumption is a valid for the fixed FSO links, this is not the case for mobile FSO link scenarios.

A. FSO for high-mobility platforms

In this paper we consider the use of the FSO technology for providing high data-rate wireless access for high-speed trains, which has attracted a great deal of attention in the past few years. Indeed, the demand of passengers to access broadband services with high quality in high-speed trains is exponentially increasing. Current radio-frequency wireless technologies such as the 4G (LTE, Long Term Evolution) and 4G+ (LTE-Advanced) networks can offer unreliable handovers and limited data rate, resulting in unsatisfying quality-ofexperience for users [17], [18]. Within this context, FSO has been recognized as a promising connectivity solution [18]-[20]. However, apart from the requirement of highly accurate and agile beam tracking, one of the most important challenges in such systems is time synchronization between the transmitter (Tx) and the Rx. This is, of course, in addition to the need to channel estimation, explained above. In fact, in most related literature, OOK modulation is considered assuming signal detection under the assumption of perfectly synchronized (PSY) Tx and Rx, which is practically not valid for FSO links with high mobility. To clarify better this point, consider a train with speed of 360 Km/h or 100 m/s. Given the speed of light $c = 3 \times 10^8 \,\mathrm{m/s}$, only after 1 ms, the propagation delay of considered ground-to-train link changes equal to $\Delta_{\tau_p}=\frac{100\text{m/s}\times 1\text{ms}}{3\times 10^8\text{m/s}}=0.33\times 10^{-9}$. Now, consider a ground-to-train FSO link with a bit-rate of $R_b = 1$ Gbps. For OOK modulation, $R_b = 1 \,\text{Gbps}$ is obtained when bit duration $T_b = 1/R_b = 1 \text{ ns.}$ Hence, only after 1 ms, the sampling time at the Rx is deviated by at least $\tau = \Delta_{\tau_n} =$ $0.33 \times 10^{-9} = 0.33 T_b$. This can result in a significant link performance degradation. Moreover, due to the Doppler effect, the coherence time of the underlying channel is reduced significantly. Hence, for reliable communication we would need to adjust the synchronization and the channel estimate at intervals much shorter than 1 ms, which requires the insertion of several pilot bits inside each data frame. Obviously, this results in a considerable spectral efficiency loss and increased system complexity. These considerations suggest the practical interest of blind signal detection for such FSO links.

B. Contributions

In this work, we assume that the sampling clock offset is randomly changing and, in addition, the Rx does not have

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access to the instantaneous channel fading coefficient. First, by using N_s samplers at the Rx, we propose a blind sequence detection method over an observation window of length L. This method, which relies on the knowledge of the distribution of the channel attenuation, can achieve a performance close to the Rx with PSY and perfect channel state information (PCSI).

Second, based on the generalized likelihood ratio test (GLRT) criterion, we propose a suboptimal and more practical blind sequence detection method. Despite the need to larger values of L to achieve performance comparable to the ideal Rx, the proposed method can significantly reduce the computational complexity of conventional ML-based method.

Third, by employing differential OOK signaling with the expense of using two optical sources (emitting on two different wavelengths) and two photo-detectors, we propose a more efficient blind data detection scheme. Differential signaling is an innovative method that was firsty introduced in [21] to suppress the effect of background noise, and later proposed in [22], [23] to resolve the problem of detection threshold adjustment for OOK demodulation. It was also used in [24] to mitigate pointing errors effects, and in [25] to explore a one-bit channel information scheme for a 2×1 FSO link. When the two wavelengths are sufficiently different, differential signaling can benefit from a diversity gain against channel fading [25]. As the *fourth* contribution, we propose an efficient blind detection scheme for such a scheme, albeit accepting an increased detection complexity.

The performances of the proposed methods are investigated through numerical results. We also compare the processing load of the four proposed detection methods.

C. Paper structure

The reminder of this paper is organized as follows. In Section II, we describe our system model and main assumptions. Our proposed signal detection schemes for the case of using a single wavelength are described in Section III along with the related simulation results and analyses. Next, in Section IV, we propose blind signal detection methods under differential signaling, and investigate their performance. Lastly, Section V concludes the paper.

II. SYSTEM MODEL

As mentioned in the introduction, we consider an IM/DD FSO link using OOK modulation. As explained, due to high mobility of the Tx/Rx and high data rate, the sampling clock offset τ is randomly changing. At the Rx, we use N_s samplers that we denote by $\mathrm{SP_i},\ i\in\{1,2,...,N_s\},$ see from Fig. 1 for $N_s=3$. Let τ be the sampling clock offset between the Tx and $\mathrm{SP_1}.$ We assume that τ is an unknown parameter and has a uniform distribution in $(-T_b,T_b).$ As shown in Fig. 1, $\mathrm{SP_i}$ samples the i-th integrator output at time instants $t=\tau_i'+kT_b,$ where $\tau_i'=\tau+(i-1)T_b/N_s$ with k denoting the k-th bit interval. Prior to each sampler, an optical delay-line is inserted to apply a time shift of $(i-1)T_b/N_s$, for the i-th sampler. In practice, precise and stable adjustment of the amount of the

delay is possible using small-size fiber-based delay-lines.¹

A. Signal model for a simple link using a single wavelength

We consider here the use of an APD at the Rx. As explained and as depicted in Fig. 2, due to the sampling clock offset τ , at the Rx, $(1 - \tau_i/T_b)$ of $(k + k_i')$ th transmitted signal along with the τ_i/T_b of $(k + k_i' + 1)$ th transmitted signal are placed at the kth pulse duration interval of receiver. Hence, for OOK modulation, the photo-current output of SP_i corresponding to the k-th bit interval can be written as

$$r_k^{\prime(i)} = \eta h \left(1 - \frac{\tau_i}{T_b} \right) s_{k+k_i'} + \eta h \frac{\tau_i}{T_b} s_{k+k_i'+1} + n_{k+k_i'}^{(i)}, \quad (1)$$

where $\tau_i = \tau_i' - k_i' T_b$, $\tau_i \in \{0, T_b\}$; $k_i' = \lfloor \tau_i' / T_b \rfloor$ with $\lfloor z \rfloor$ being the floor function; h denotes the instantaneous channel coefficient assumed to be constant over a large number of transmitted bits; and $s_k \in \{0,1\}$ denotes the transmitted OOK symbols. Also, $\eta = 2\xi \, P_t$, where P_t is the average transmitted power, $\xi = e G \mu / \tilde{h}_p \nu$, G is the APD gain, e denotes the electron charge, μ is the APD quantum efficiency, ν is the optical frequency, and \tilde{h}_p stands for the Planck constant. Lastly, $n_k^{(i)}$ is the zero mean Gaussian noise with variance $\sigma_{n,k}^2$ that includes thermal and shot noises, and can be accurately modeled by a Gaussian distribution [26]. We have:

$$\sigma_{n,k}^2 = \sigma_s^2 h s_k'' + \sigma_0^2,$$
 (2)

where $s_k''=(1-\tau_i/T_b)s_k+\tau_i\,s_{k+1}$, and σ_s^2 and σ_0^2 denote the variances of shot noise and signal-independent (thermal and background) noises, respectively. This model can be simplified to the case of a PIN photo-detector by setting G=1 and $\sigma_s^2\approx 0$ [26]. According to (1), the output of the sampler SP_i at the time sample k depends on the transmitted signals at time samples $k+k_i'$ and $k+k_i'+1$. In this paper, we assume that k_i' is perfectly known at the Rx.² Let us define $r_k^{(i)}$ as $r_k^{(i)}=r_{k-k_i'}^{(i)}$. For simplicity and without loss of generality, in the sequel, we assume $T_b=1$. Accordingly, see Figs. 1 and 2,

$$r_k^{(i)} = \eta h (1 - \tau_i) s_k + \eta h \tau_i s_{k+1} + n_k^{(i)}.$$
 (3)

For signal detection, we should reasonably use the output of the sampler (say, the *i*-th), for which $0 \le \tau_i < 1/N_s$. More precisely, we have:

$$\tau_{i} = \tau + (i - 1)/N_{s} - k'_{i}$$

= $\tau + (i - 1)/N_{s} - \lfloor \tau + (i - 1)/N_{s} \rfloor.$ (4)

From (4) and as shown in Fig. 2, for any given τ , only one of the τ_i s falls in the interval $[0,1/N_s)$. This allows us to simplify the detector's structure, as we will see in the next section. For instance, for $N_s=5$, we are sure that the synchronization error between transmitter and the considered ith sampler is

¹Such a fiber-based optical delay-line consists of an input and output fiber collimator to project the light into free space and collect it back into the fiber. The distance the light travels (and hence, the delay) can be accurately controlled, e.g., by fixing the separation between the input and output optics.

²Note that k_i' only takes three values of $\{-1,0,1\}$, depending on τ . Also, it changes much slower than τ , which makes it possible to estimate it with high accuracy. The estimation of k_i' is the beyond the scope of this paper and we assume it is perfectly known at the Rx.

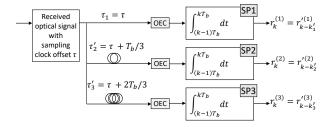
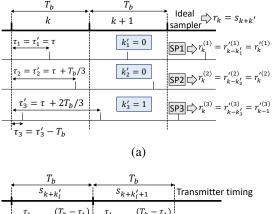


Fig. 1. Block diagram of sampler for $N_{\rm s}=3$. OEC stands for optical to electrical conversion.



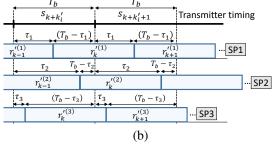


Fig. 2. Illustration of samplers' outputs corresponding to Fig. 1 for the case where the offset clock between the Tx and the first sampler (SP₁) is τ : (a) showing the relationship between τ_i and τ_i' , and also $r_k^{(i)}$ and $r_k'^{(i)}$; (b) showing the relationship between $r_k'^{(i)}$ and s_k .

lower than 0.2, or $0 \le \tau_i < 0.2$ and by increasing N_s , we expect the synchronization error decreases. Hence, for data detection, we first estimate i for which $\tau_i \in [0, 1/N_s)$. Then, we use the outputs of this sampler (which changes over time due to link mobility) for data detection.

Finally, from (3) and due to the one-to-one relationship between τ and τ_i , we have

$$p\left[r_{k}^{(i)}|h,\tau,s_{k},s_{k+1}\right] = p\left[r_{k}^{(i)}|h,\tau_{i},s_{k},s_{k+1}\right]$$

$$= \frac{1}{\sqrt{2\pi\left(h\left((1-\tau_{i})s_{k}+\tau_{i}\,s_{k+1}\right)\sigma_{s}^{2}+\sigma_{0}^{2}\right)}}$$

$$\times \exp\left(-\frac{\left|r_{k}^{(i)}-\eta\,h(1-\tau_{i})s_{k}-\eta\,h\,\tau_{i}\,s_{k+1}\right|^{2}}{2\,h\left((1-\tau_{i})s_{k}+\tau_{i}\,s_{k+1}\right)\sigma_{s}^{2}+2\,\sigma_{0}^{2}}\right).$$
(5)

B. Signal Model for OOK with Differential Signaling

By differential signaling, at the Tx, at time sample k, the OOK signal s_k and its complement $\overline{s}_k = 1 - s_k$ are used to drive two distinct optical sources (OSs) working on

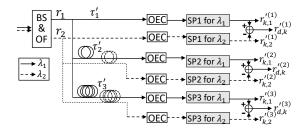


Fig. 3. Proposed block diagram of sampler for the case of differential signaling.

wavelengths λ_1 and λ_2 [21]. The outputs of the OSs are passed through a beam combiner (BC) before sending over the FSO channel. To keep the same average transmitted power of P_t as in the previous case, we set $\eta = \xi P_t$.

At the Rx, the optical signal is passed through a beam splitter (BS) whose outputs are fed into two optical filters (OFs) with center wavelengths on λ_1 and λ_2 in order to separate the received optical signals from the two lasers. Then, after optical-to-electrical conversion (OEC), signals r_1 and r_2 are time-sampled to get $r_{k,1}^{\prime(i)}$ and $r_{k,2}^{\prime(i)}$, respectively. Then, $r_{k,2}^{\prime(i)}$ is subtracted from $r_{k,1}^{\prime(i)}$ to get $r_{d,k}^{\prime(i)}$ (see Fig. 3).

Let h_1 and h_2 be the channel fading coefficients corresponding to λ_1 and λ_2 , respectively. Similar to the formulation of $r_k^{(i)} = r_{k-k_i'}^{\prime(i)}$, here $r_{k,1}^{(i)} = r_{k-k_i',1}^{\prime(i)}$, $r_{k,2}^{(i)} = r_{k-k_i',2}^{\prime(i)}$ and $r_{d,k}^{(i)} = r_{d,k-k_i'}^{\prime(i)}$. Hence, the photo-current outputs of SP_i corresponding to the k-th bit interval are given by:

$$\begin{cases}
r_{d,k}^{(i)} = r_{k,1}^{(i)} - r_{k,2}^{(i)}, \\
r_{k,1}^{(i)} = \eta(1 - \tau_i)h_1s_k + \eta \tau_i h_1 s_{k+1} + n_{k,1}^{(i)}, \\
r_{k,2}^{(i)} = \eta(1 - \tau_i)h_2 \overline{s}_k + \eta \tau_i h_2 \overline{s}_{k+1} + n_{k,2}^{(i)},
\end{cases} (6)$$

where $n_{k,1}^{(i)}$ and $n_{k,2}^{(i)}$ are zero-mean Gaussian noises with variances:

$$\begin{cases} \sigma_{n,1}^{2} = \sigma_{s}^{2} h_{1} s_{k}^{"} + \sigma_{0}^{2} \\ \sigma_{n,2}^{2} = \sigma_{s}^{2} h_{2} \overline{s}_{k}^{"} + \sigma_{0}^{2}, \end{cases}$$
(7)

and

$$\overline{s}_k'' = (1 - \tau_i) \,\overline{s}_k + \tau_i \,\overline{s}_{k+1}. \tag{8}$$

Also, the variance of $n_{d,k}^{(i)} = n_{k,1}^{(i)} - n_{k,2}^{(i)}$ is:

$$\sigma_{d,n}^2 = \sigma_s^2 (h_1 \, s_k'' + h_2 \, \overline{s}_k'') + 2\sigma_0^2. \tag{9}$$

For the case of close λ_1 and λ_2 , we have $h_1 \approx h_2$ [21]. Otherwise, when these wavelengths are sufficiently apart, we can assume that h_1 and h_2 are almost independent.

C. Channel Model

In our channel model, we consider the joint effect of deterministic propagation loss, denoted by h_a , and the random intensity fluctuation due to atmospheric turbulence, denoted by h_l , while neglecting the effect of pointing errors. In fact, in order to compensate pointing errors, recent FSO systems employ efficient tracking mechanisms based on electro-optic

or acousto-optic devices [27], [28], which is particularly applicable to the case of fast moving platforms [29]. In the sequel, we do not consider the effect of pointing errors by assuming that an efficient automatic beam pointing, acquisition and tracking system is employed [30]. The channel attenuation is then considered as $h = h_l h_a$. To model h_a we use the gamma-gamma (G-G) distribution that is accepted as a general model describing all turbulence regimes, with the following probability density function (PDF) [31]:

$$f_{GG}(h_a) = \frac{2(\alpha\beta)^{\frac{\alpha+\beta}{2}}}{\Gamma(\alpha)\Gamma(\beta)} h_a^{\frac{\alpha+\beta}{2}-1} k_{\alpha-\beta} (2\sqrt{\alpha\beta h_a}).$$
 (10)

where, $\Gamma(.)$ is the gamma function, $k_m(.)$ is the modified Bessel function of order m and second kind, and parameters α and β are related to turbulence conditions.

III. SIGNAL DETECTION FOR SINGLE-WAVELENGTH TRANSMISSION

Under PCSI and PSY at the Rx, given the received signal $r_k = \eta \, h \, s_k + n_k$, the transmitted signal $s_k \in \{0,1\}$ can be detected easily as: $r_k \stackrel{\hat{s}_k=1}{\geq} \frac{\eta \, h}{2}$. In general sense, blind signal detection may involve ambiguity on the instantaneous channel fading coefficient and synchronization (i.e., the correct sampling time). In the proposed blind methods, we avoid ambiguity on the instantaneous channel fading coefficient by exploiting the slow fading property of the FSO channel through sequence symbol detection. In addition, we avoid ambiguity in the synchronization by using N_s samplers.

We assume here that we do not have any information on τ or h; our goal being to detect OOK signals without requiring any pilot symbol. We propose two detection methods for this purpose. The first method detects the sequence of OOK signals under the assumption that the Rx knows the channel fading distribution $f_h(h)$, whereas the second proposed method does not require this PDF. It is worth mentioning that although for a static FSO link the channel distribution parameters typically change very slowly over time and we do not estimate them frequently, in the high mobility context that we consider in this paper, their estimation may be an important issue.

For sequence data detection, we arrange the outputs of all samplers in "observation windows" composed of L intervals. Let us denote by $\mathbf{r}_i(L) = \{r_1^{(i)}, r_2^{(i)}, ..., r_L^{(i)}\}$ the vector of outputs of the sampler SP_i corresponding to the transmitted signals $\mathbf{s}(L+1) = \{s_1, s_2, ..., s_{L+1}\}$. Based on (2) and (3), the PDF of $\mathbf{r}_i(L)$ conditioned on h, τ_i , and $\mathbf{s}(L+1)$ is:

$$p[\mathbf{r}_{i}(L)|h, \tau_{i}, \mathbf{s}(L+1)] = \prod_{k=1}^{L} p[r_{k}^{(i)}|h, \tau_{i}, s_{k}, s_{k+1}],$$
 (11)

where
$$p\left[r_k^{(i)}\big|h,\tau_i,s_k,s_{k+1}\right]$$
 is given in (5).

 3 Note that, from (3), a received sequence with length L includes the contribution of L+1 transmitted symbols. Therefore, we limit the samplers' outputs to L samples.

A. Optimal ML-based Sequence Detection Method

Based on ML criterion, signal detection is performed as:

$$\hat{\mathbf{s}}(L) = \underset{\mathbf{s}(L+1)}{\arg \max} \ \mathcal{M}_{\mathrm{ML}}(\mathbf{s}(L+1)), \tag{12}$$

where

$$\mathcal{M}_{\mathrm{ML}}(\mathbf{s}(L+1)) = \int_{0}^{\infty} \mathcal{M}'_{\mathrm{ML}}(\tau) f_{h}(h) dh, \qquad (13)$$

and

$$\mathcal{M}'_{\mathrm{ML}}(\tau) = \int_{0}^{1} \prod_{i=1}^{N_{s}} p\left[\mathbf{r}_{i}(L) \middle| h, \tau, \mathbf{s}(L+1)\right] d\tau,$$

$$= \int_{0}^{1} \prod_{i=1}^{N_{s}} \prod_{k=1}^{L} p\left[r_{k}^{(i)} \middle| h, \tau, s_{k}, s_{k+1}\right] d\tau. \quad (14)$$

Given (5), finding a general closed-form expression for the integral in (14) is quite difficult.

As we can see, the proposed method detects $\hat{\mathbf{s}}(L)$ by searching over 2^{L+1} possible states of the metric (13), each one involving the calculation of a two-dimensional integral. In addition, this method requires the knowledge of the parameters α and β of the channel PDF $f_h(h)$. A simple method for estimating the parameters of a G-G PDF was recently proposed in [32]. This method relies on the estimation of the moments of h of orders k, (k+1), l, and (l+1), that should be calculated over a sufficiently large sample size.

Overall, as explained above, this method suffers from relatively high computational complexity for a practical and real-time implementation.

B. Suboptimal GLRT-based Sequence Detection Method

We propose here a sub-optimal detector based on the GLRT criterion, which has a lower computational complexity and does not require the channel PDF. From [33], [34], the GLRT method jointly decides on h and $\mathbf{s}(L) = \{s_1, ..., s_L\}$ as:

$$\hat{h}, \hat{\mathbf{s}}(L) = \underset{h, \mathbf{s}(L+1)}{\operatorname{arg max}} \prod_{i=1}^{N_s} p[\mathbf{r}_i(L) | h, \mathbf{s}(L+1)]$$

$$= \underset{h, \mathbf{s}(L+1)}{\operatorname{arg max}} \int \prod_{i=1}^{N_s} p[\mathbf{r}_i(L) | h, \tau, \mathbf{s}(L+1)] d\tau. \quad (15)$$

To reduce the computational complexity of (15), we propose a detection method which is inspired by GLRT that we refer to it as GLRT-based detection method. This detector jointly decides on h, i, and $\mathbf{s}(L) = \{s_1, ..., s_L\}$:

$$\hat{i}, \hat{h}, \hat{\mathbf{s}}(L) = \underset{i,h,\mathbf{s}(L+1)}{\arg\max} p[\mathbf{r}_i(L)|h, \mathbf{s}(L+1)].$$
 (16)

When τ_i is known, we have $p[\mathbf{r}_i(L)|h,\mathbf{s}(L+1)] = p[\mathbf{r}_i(L)|\tau_i,h,\mathbf{s}(L+1)]$. As mentioned previously, one τ_i , corresponding to an ith min, $i \in \{1,...,N_s\}$, falls in the interval $[0,1/N_s)$. For this special τ_i , the mean and the variance are equal to $\overline{\tau}_i = 1/2N_s$ and $\sigma_{\tau_i}^2 = T_b^2/12N_s^2 = 1/12N_s^2$, respectively. Given that $\sigma_{\tau_i}^2$ decreases by increasing

$$\hat{i}, \hat{h}, \hat{\mathbf{s}}(L) = \underset{i,h,\mathbf{s}(L+1)}{\arg\max} p\left[\mathbf{r}_i(L)\middle| \tau_i = \frac{1}{2N_s}, h, \mathbf{s}(L+1)\right].$$
(17)

Equivalently,

$$\hat{i}, \hat{h}, \hat{\mathbf{s}}(L) = \underset{i,h,\mathbf{s}(L+1)}{\arg\max} \log p \left[\mathbf{r}_i(L) \middle| \tau_i = \frac{1}{2N_s}, h, \mathbf{s}(L+1) \right]$$

$$= \underset{i,h,\mathbf{s}(L+1)}{\arg\min} \sum_{k=1}^{L} \frac{\left| r_k^{(i)} - \eta h \left(1 - \frac{1}{2N_s} \right) s_k - \frac{\eta h}{2N_s} s_{k+1} \right|^2}{h \left(\left(1 - \frac{1}{2N_s} \right) s_k + \frac{1}{2N_s} s_{k+1} \right) \sigma_s^2 + \sigma_0^2} + \log \left(h \left(\left(1 - \frac{1}{2N_s} \right) s_k + \frac{1}{2N_s} s_{k+1} \right) \sigma_s^2 + \sigma_0^2 \right). \tag{18}$$

For notation simplicity, we define

$$s_k' = \left(1 - \frac{1}{2N_s}\right)s_k + \frac{1}{2N_s}s_{k+1}.\tag{19}$$

We have then,

$$\hat{i}, \hat{h}, \hat{\mathbf{s}}(L) = \underset{i, h, \mathbf{s}(L+1)}{\operatorname{arg min}} \sum_{k=1}^{L} \frac{\left| r_k^{(i)} - \eta \, h \, s_k' \right|^2}{h \, s_k' \, \sigma_s^2 + \sigma_0^2} + \log \left(h \, s_k' \, \sigma_s^2 + \sigma_0^2 \right)$$
(20)

For the given i and s(L+1), by differentiating (20) with respect to h and setting it to zero, we obtain,

$$\hat{h} = -\frac{\left(2\eta^{2}\sigma_{0}^{2} + \sigma_{s}^{2}\right)\mathcal{S}_{2}'}{2\eta^{2}\sigma_{s}^{2}\mathcal{S}_{3}'}
+ \left[\frac{2\sigma_{0}^{2}}{\eta\sigma_{s}^{2}\mathcal{S}_{3}'}\left(\left(1 - \frac{1}{2N_{s}}\right)\left(\mathcal{R}_{on,1}^{(i)} + r_{L}^{(i)}s_{L}\right)\right)
+ \frac{1}{2N_{s}}\left(\mathcal{R}_{on,1}'^{(i)} + r_{L}^{(i)}s_{L+1}\right)\right)
+ \frac{1}{\eta^{2}\mathcal{S}_{3}'}\left(\left(1 - \frac{1}{2N_{s}}\right)\left(\mathcal{R}_{on,2}^{(i)} + \left(r_{L}^{(i)}\right)^{2}s_{L}\right)
+ \frac{1}{2N_{s}}\left(\mathcal{R}_{on,2}'^{(i)} + \left(r_{L}^{(i)}\right)^{2}s_{L+1}\right)\right)
+ \frac{\left(2\eta^{2}\sigma_{0}^{2} + \sigma_{s}^{2}\right)^{2}\left(\mathcal{S}_{2}'\right)^{2} - 2\eta^{2}\sigma_{0}^{2}\sigma_{s}^{4}\mathcal{S}_{1}'\mathcal{S}_{3}'}{\left(2\eta^{2}\sigma_{s}^{2}\mathcal{S}_{3}'\right)^{2}}\right]^{1/2}, (21)$$

where

$$\begin{cases}
S_1' = \sum_{k=1}^{L} s_k' = \left(1 - \frac{1}{2N_s}\right) s_1 + \frac{1}{2N_s} s_{L+1} + N_{on} \\
S_2' = \sum_{k=1}^{L} s_k'^2 \\
S_3' = \sum_{k=1}^{L} s_k'^3
\end{cases} \tag{22}$$

 4 We will see in the numerical results that $N_s \geq 4$ is large enough to provide a good Rx performance.

 N_s , assuming sufficiently large⁴ N_s , we estimate τ_i by its and also, $N_{on} = \sum_{k=2}^L s_k$ is the number of bits '1' in the mean $\overline{\tau}_i$. Then, we can simplify (16) as vector $\mathbf{s}'(L-1) = \{s_2, s_3, ..., s_L\}$, and

$$\begin{cases}
\mathcal{R}_{on,1}^{(i)} = \sum_{k=1}^{L-1} r_k^{(i)} s_k \\
\mathcal{R}_{on,1}^{\prime(i)} = \sum_{k=1}^{L-1} r_k^{(i)} s_{k+1} \\
\mathcal{R}_{on,2}^{(i)} = \sum_{k=1}^{L-1} \left(r_k^{(i)} \right)^2 s_k \\
\mathcal{R}_{on,2}^{\prime(i)} = \sum_{k=1}^{L-1} \left(r_k^{(i)} \right)^2 s_{k+1}.
\end{cases} (23)$$

Now, the detection method in (20) is simplified as

$$\hat{i}, \hat{\mathbf{s}}(L) = \underset{i, \mathbf{s}(L+1)}{\arg \min} \sum_{k=1}^{L} \frac{\left| r_k^{(i)} - \eta \,\hat{h} \, s_k' \right|^2}{\hat{h} \, s_k' \, \sigma_s^2 + \sigma_0^2} + \log \left(\hat{h} \, s_k' \, \sigma_s^2 + \sigma_0^2 \right), \tag{24}$$

where \hat{h} is calculated from (21). Note that for the case of an all-zero transmitted sequence, i.e., s(L+1) = 0, the proposed estimator in (21) does not work correctly. In such a case, from $\hat{i}, \hat{h}, \hat{\mathbf{s}}(L) = \underset{\hat{i}, \hat{k}, \sigma(L+1)}{\operatorname{arg min}} \sum_{k=\sigma(L+1)}^{L} \frac{\left|r_k^{(i)} - \eta \, h \, s_k'\right|^2}{h \, s_k' \, \sigma_s^2 + \sigma_0^2} + \log \left(h \, s_k' \, \sigma_s^2 + \sigma_0^2\right). \quad \mathcal{S}_2' = 0 \text{ and } \mathcal{S}_3' = 0 \text{ from (22). As a result, we can not use (21)}$ to calculate \hat{h} . To resolve this issue, we propose an alternative to (24) as follows:

$$\hat{i}, \hat{\mathbf{s}}(L) = \underset{i, \mathbf{s}(L+1)}{\operatorname{arg min}} \left\{ \begin{array}{c} \mathcal{A}_1 & \text{for } \mathbf{s}(L+1) \neq 0 \\ \mathcal{A}_0 & \text{for } \mathbf{s}(L+1) = 0 \end{array} \right., \quad (25)$$

where

$$\begin{cases}
\mathcal{A}_{1} = \sum_{k=1}^{L} \frac{\left| r_{k}^{(i)} - \eta \hat{h} s_{k}' \right|^{2}}{\hat{h} s_{k}' \sigma_{s}^{2} + \sigma_{0}^{2}} + \log \left(\hat{h} s_{k}' \sigma_{s}^{2} + \sigma_{0}^{2} \right), \\
\mathcal{A}_{0} = L \log \left(\sigma_{0}^{2} \right) + \mathcal{R}_{tot,2}^{(i)} / \sigma_{0}^{2},
\end{cases} (26)$$

$$\mathcal{R}_{tot,2}^{(i)} = \sum_{k=1}^{L} \left(r_k^{(i)} \right)^2.$$

Lastly, in the case of a thermal noise limited Rx, metrics of A_1 and A_0 are simplified as follows:

$$\begin{cases}
A_{1} = \mathcal{R}_{tot,2}^{(i)} - \frac{\left(\left(1 - \frac{1}{2N_{s}}\right)\mathcal{R}_{on,1}^{(i)} + \frac{1}{2N_{s}}\mathcal{R}_{on,1}^{\prime(i)}\right)^{2}}{S_{2}^{\prime}} \\
- \frac{\left(\left(1 - \frac{1}{2N_{s}}\right)r_{1}^{(i)}s_{1} + \frac{1}{2N_{s}}r_{L}^{(i)}s_{L+1}\right)^{2}}{S_{2}^{\prime}}, (27)
\end{cases}$$

$$A_{0} = \mathcal{R}_{tot,2}^{(i)}.$$

Note that, unlike the metric of (13) which requires the calculation of a two-dimensional integral, the metric in (25),(26) only needs a series of simple additions and multiplications and also does not require the knowledge of $f_h(h)$. Here, the Rx searches among $N_s \times 2^{L+1}$ possible received sequences (i.e., 2^{L+1} possible bit sequences for each sampler output) to find the sequence that minimizes (25). To avoid this exhaustive search and to further reduce the Rx complexity, we have developed a fast search algorithm for implementing (25), which reduces the search space to $4N_sL$ states. Details of this algorithm are presented in Appendix.

TABLE I SYSTEM PARAMETERS FOR SIMULATIONS

Description	Parameter	Setting	
APD Gain	G	100	
APD Quantum Efficiency	μ	0.9	
Plank's Constant	$ ilde{h}_p$	$6.6 \times 10^{-34}~\mathrm{m^2Kg/s}$	
Wavelength	λ	1550 nm	
Receiver Load	R_l	$100~\Omega$	
Receiver Temperature	T_r	$300^{\circ}~K$	
Channel Loss	h_l	30 dB	
Background Noise Power	P_b	10 nW	
Weak turbulence	σ_R^2	0.4	
channel parameters	α	6.9	
	β	5.3	
Strong turbulence	σ_R^2	2	
channel parameters	α	3.9	
	β	1.7	

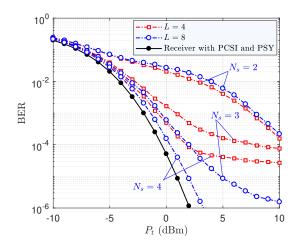


Fig. 4. BER of ML-based detection method for for $\sigma_R^2=0.4$ and different values of L and N_s , compared to the case of PCSI and PSY.

C. Simulation Results

We present here a set of numerical results to study the system performance for the proposed detection methods. The main considered parameters for the simulation results are summarized in Table I, mostly adopted from recent literature, e.g. [13], [35]. Unless otherwise specified, we consider the case of the weak turbulence regime. Link performance is mainly evaluated in terms of the average bit-error-rate (BER) where the case of the Rx with PCSI and PSY is considered as a lower bound benchmark.

To investigate the impact of the number of samplers and the observation window length on the performance of the first (ML-based) proposed detection method, we have presented in Fig. 4 BER plots versus P_t for different values of N_s and L, assuming that $f_h(h)$ is known at the Rx. As expected, the link performance improves by increasing N_s and L, with a strong dependence on the former; the improvement is especially

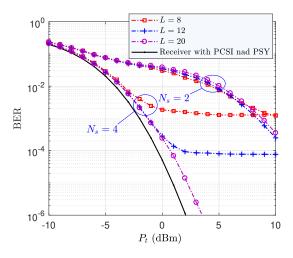


Fig. 5. BER of GLRT-based detector for $\sigma_R^2=0.4$ and different values of L and N_s , compared to the case of PCSI and PSY.

significant when N_s increases from two to three. In fact, for relatively small N_s , the system performance is limited by inter-symbol interference resulting from synchronization errors. As N_s increases, the standard deviation of timing jitter decreases, and hence, the resulting inter symbol interference. From these results, we can suggest L=8 and $N_s=4$ as suitable choices for the proposed detector, where we can achieve a performance close to the PSCI and PSY case; e.g. with a gap of smaller than 2 dB at a target BER of 10^{-6} . Let us now investigate the performance of the second (GLRTbased) proposed detector. We have presented in Fig. 5 the BER plots, where as expected, by increasing N_s and L, the BER approaches that of the Rx with PCSI and PSY. Here, $N_s = 4$ and L = 20 appear to be a suitable choice. It is worth mentioning that this larger L does not mean a higher computational complexity, compared with the ML-based one (for which L = 8 was a suitable choice, see above). To clarify this, for L=8 and $N_s=4$, to detect a sequence of 8 bits, for instance, the ML-based detector requires to compute 28+1 metrics of (13), involving the calculation of an two-dimensional integral, while in addition, requiring the knowledge of $f_h(h)$. The GLRT-based detector, on the other hand, needs to compute $2 \times 4 \times (20 + 1)$ metrics of (26) for $N_s = 4$ and L = 20.

IV. SEQUENCE DETECTION OF DIFFERENTIAL OOK MODULATION

We consider now the case of employing differential OOK signaling (see Subsection II-B and Fig. 3) in two special cases where the corresponding channel fading coefficients have very high or otherwise very low correlation. These correspond to the cases where λ_1 and λ_2 are selected as very close or very different, respectively. The former is suitable when working in relatively weak turbulence, whereas the latter offers diversity benefit under relatively strong turbulence conditions.

Before describing the blind detection methods, we present in the following the BER calculation for the case of PCSI (i.e., perfectly known h_1 and h_2) and PSY (i.e., $\tau_i = 0$) at the Rx.

For PSY receiver, (6) is simplified as

$$r_{d,k} = \eta(h_1 s_k - h_2 \overline{s}_k) + n_{d,k},$$
 (28)

where $n_{d,k}$ is a zero mean Gaussian noise with variance $\sigma_{d,n}^2 = \sigma_s^2 h_1 s_k + \sigma_s^2 h_2 \overline{s}_k + \sigma_0^2$.

A. BER Analysis Under PCSI and PSY

For the case of highly correlated h_1 and h_2 , i.e., $h_1 \approx h_2$, the average BER, denoted by P_e is given by

$$P_e = \int_0^\infty P_{e|h}(h) f_h(h) dh, \tag{29}$$

where

$$\begin{split} P_{e|h}(h) &= \frac{1}{2} \operatorname{Prob}\{r_{d,k} < \gamma_{th} | s_k = 1\} \\ &+ \frac{1}{2} \operatorname{Prob}\{r_{d,k} > \gamma_{th} | s_k = 0\} \\ &= \frac{1}{2} Q \left(\frac{\gamma_{th} + \eta h}{\sqrt{\sigma_s^2 h + \sigma_0^2}} \right) + \frac{1}{2} Q \left(\frac{\eta h - \gamma_{th}}{\sqrt{\sigma_s^2 h + \sigma_0^2}} \right), (30) \end{split}$$

and Q(.) is the well known Q-function and γ_{th} denotes the detection threshold. By differentiating (30) and setting the result to zero, the optimal detection threshold is obtained as $\gamma_{th,opt} = 0$, as expected. Then, (29) is simplified as

$$P_e = \int_0^\infty Q\left(\frac{\eta h}{\sqrt{\sigma_s^2 h + \sigma_0^2}}\right) f_h(h) dh. \tag{31}$$

For the case of independent h_1 and h_2 , we have:

$$P_e = \int_0^\infty \int_0^\infty P_{e|h_1,h_2}(h_1,h_2) f_{h_1}(h_1) f_{h_2}(h_2) dh_1 dh_2.$$
(32)

Based on (6), we can write:

$$P_{e|h_1,h_2}(h_1,h_2) = \frac{1}{2}Q\left(\frac{\gamma_{\text{th}} + \eta h_2}{\sqrt{\sigma_s^2 h_2 + \sigma_0^2}}\right) + \frac{1}{2}Q\left(\frac{\eta h_1 - \gamma_{\text{th}}}{\sqrt{\sigma_s^2 h_1 + \sigma_0^2}}\right). \tag{33}$$

To obtain the optimal detection threshold, by differentiating (33) and setting the result to zero, we get:

$$\gamma_{\text{th,opt}} = -\frac{\eta h_2(\sigma_s^2 h_1 + \sigma_0^2) + \eta h_1(\sigma_s^2 h_2 + \sigma_0^2)}{\sigma_s^2 (h_1 - h_2)}
+ \frac{1}{\sigma_s^2 (h_1 - h_2)} \left[\left(\eta h_2(\sigma_s^2 h_1 + \sigma_0^2) + \eta h_1(\sigma_s^2 h_2 + \sigma_0^2) \right)^2
- \sigma_s^2 (h_1 - h_2) \left(\eta^2 h_2^2(\sigma_s^2 h_1 + \sigma_0^2) - \eta^2 h_1^2(\sigma_s^2 h_2 + \sigma_0^2) \right)
- (\sigma_s^2 h_1 + \sigma_0^2) (\sigma_s^2 h_2 + \sigma_0^2) \ln \left(\frac{\sigma_s^2 h_1 + \sigma_0^2}{\sigma_s^2 h_2 + \sigma_0^2} \right) \right].$$
(34)

From (7), in differential signaling case, for $h_1=h_2=h$, the mean of received signal from bits '0' and '1' are $-\eta h$ and ηh , respectively, and have the same variances. Hence, for differential signaling with $h_1=h_2$, due to the symmetry of the received signals around zero, when h_1 tends to h_2 , $\gamma_{\text{th,opt}} \to 0$, as expected. Also, for the case of signal-independent noise

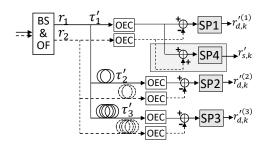


Fig. 6. Simplified Rx block diagram from Fig. 3 for differential signaling with highly correlated h_1 and h_2 .

at the Rx, this optimal value reduces to $(h_1 + h_2)/2$, as considered in [25], [36].

In the sequel, we propose blind signal detection methods for the case of differential signaling. We consider signal detection based on the GLRT criterion due to the high computationally complexity of the ML detector, as explained in the previous section for the case of single-wavelength transmission.

B. Differential Sequence Detection Method for the Case of Highly-Correlated Channels

Consider first the case where λ_1 and λ_2 are very close, resulting in $h_1 \approx h_2 = h$, with the benefit of suppressing the effect of background noise [21]. For this case, the block diagram of the Rx structure in Fig. 3 is simplified to that given in Fig. 6 (the block SP_4 will be explained later). Here, (6) can be simplified as

$$r_{d,k}^{(i)} = \eta h(1 - \tau_i) s_{d,k} + \eta h \tau_i s_{d,k+1} + n_{d,k}^{(i)},$$
 (35)

where $s_{d,k}=s_{k,1}-s_{k,2}\in\{-1,1\}$. In this case, unlike $n_k^{(i)}$ in (3), the variance of $n_{d,k}^{(i)}$ is independent from both the transmitted symbols and τ_i . As a result, we have

$$\sigma_{d,n}^2 = \sigma_{s,n}^2 = \sigma_s^2 h + \sigma_{d,0}^2$$
, with $\sigma_{d,0}^2 = 2\sigma_0^2$. (36)

Using (35), we can write

$$p\left[r_{d,k}^{(i)}|h,\tau_{i},s_{k},s_{k+1}\right] = \frac{1}{\sqrt{2\pi\left(\sigma_{s}^{2}h + \sigma_{d,0}^{2}\right)}} \times \exp\left(-\frac{\left|r_{d,k}^{(i)} - \eta h (1 - \tau_{i}) s_{d,k} - \eta h \tau_{i} s_{d,k+1}\right|^{2}}{2\left(\sigma_{s}^{2} h + \sigma_{d,0}^{2}\right)}\right).$$
(37)

Let $\mathbf{r}_{d,i}(L) = \{r_{d,1}^{(i)}, r_{d,2}^{(i)}, ..., r_{d,L}^{(i)}\}$ denote the output sequence of SP_i sampler. Using (37), and assuming h is known at the Rx, the GLRT detection (see (16)) gives:

$$\hat{i}, \hat{\mathbf{s}}(L) = \underset{i, \mathbf{s}(L+1)}{\arg \max} p \Big[\mathbf{r}_{d,i}(L) \Big| h, \tau_i \in [0, 1/N_s), \mathbf{s}(L+1) \Big],$$
(38)

where

$$p\left[\mathbf{r}_{d,i}(L)\middle|h,\tau_{i}\in\left[0,1/N_{s}\right),\mathbf{s}(L+1)\right]$$

$$=N_{s}\int_{0}^{\frac{1}{N_{s}}}p\left[\mathbf{r}_{d,i}(L)\middle|h,\tau_{i},\mathbf{s}(L+1)\right]d\tau_{i}$$

$$=\frac{\mathcal{D}'_{1}}{\sqrt{\mathcal{D}'_{3}}}Q\left(\frac{N_{s}\sqrt{\mathcal{D}'_{3}}}{\sqrt{\sigma_{s}^{2}h+\sigma_{d,0}^{2}}}-\frac{\mathcal{D}'_{2}}{\mathcal{D}'_{3}}\right), \quad (39)$$

$$\begin{cases}
\mathcal{D}'_{1} = \frac{N_{s} \exp\left(\frac{\mathcal{D}'_{2}^{2/2}/\mathcal{D}'_{3} - \sum_{k=1}^{L} \left(r_{d,k}^{(i)} - \eta h s_{d,k}\right)^{2}}{2\left(\sigma_{s}^{2}h + \sigma_{d,0}^{2}\right)}\right)}{\left(2\pi\left(\sigma_{s}^{2}h + \sigma_{d,0}^{2}\right)\right)^{L/2 - 1}} \\
\mathcal{D}'_{2} = \eta h \sum_{k=1}^{L} \left(r_{d,k}^{(i)} - \eta h s_{d,k}\right) s_{d,k}'' \\
\mathcal{D}'_{3} = \eta^{2}h^{2} \sum_{k=1}^{L} s_{d,k}''^{2}
\end{cases} (40)$$

and $s''_{d,k} = s_{d,k+1} - s_{d,k}$. Since $s_k + \overline{s}_k = 1$, in order to estimate h, we pass $r_1 + r_2$ through an additional sampler, e.g. SP₄ as shown in Fig. 6. At the output of this latter, we have:

$$r_{s,k}^{\prime(i)} = \eta h + n_{s,k},\tag{41}$$

where $n_{s,k}$ is an additive Gaussian noise with zero mean and variance $\sigma_s^2 h + 2\sigma_0^2$. Now, using (41), we can obtain an ML estimate of h as

$$\hat{h} = \frac{1}{\eta L} \sum_{k=1}^{L} r_{s,k}^{(i)} = h + n_h^{(i)}, \tag{42}$$

where $n_h^{(i)}=\frac{1}{\eta L}\sum_{k=1}^L n_{s,k}'^{(i)}$ is a Gaussian noise with zero mean and variance $\sigma_{n,h}^2=(\sigma_s^2h+2\sigma_0^2)/\eta^2L$. So, we can easily estimate h even without any information on s_k and τ_i . By substituting h by \hat{h} in (39), s(L) detection is done by searching over $N_s \times 2^{L+1}$ possible states of metric (39). It is worth mentioning that, unlike metric (13), (39) consists of a closed-form expression.

Note that, to detect data from (38), the detector requires to calculate and compare $N_s imes 2^{L+1}$ possible states of the metric (39) which increases exponentially by increasing L. The proposed detection method of (38) can be considerably simplified in the high SNR regime where the effect of noise can be ignored compared with the sampling clock offset. Remember that we should find which τ_i , $i \in \{1, ..., N_s\}$, gets its value in the interval $[0, 1/N_s)$. For a given i, if $s_k = 1$, $r_{d,k}^{(i)}$ takes the positive values ηh or $\eta(1-\tau_i)$. Likewise, if $s_k=0$, $r_{d,k}^{(i)}$ takes the negative values $-\eta h$ or $-\eta(1-\tau_i)$. Now, for the specific i where τ_i falls in the interval $[0,1/N_s)$, we have with a high probability $r_{d,k}^{(i)}>0$ for $s_k=1$ and $r_{d,k}^{(i)}<0$ otherwise. Using this and following the method developed in Appendix, it can be shown that the metric (38) is maximized when N_d positive values of $\mathbf{r}_{d,i}(L)$ are chosen as bit "1" and $L-N_d$ negative values as bit "0". Hence, the search space is reduced from $N_s \times 2^{L+1}$ to $2N_s$ where the factor 2 is related to the two possible states (0 or 1) of s_{L+1} .

C. Differential Sequence Detection Method for the Case of Independent Channels

Consider now the special case where λ_1 and λ_2 are sufficiently different so that we can assume almost independent h_1 and h_2 . Under such conditions, we can potentially benefit from a diversity gain [25], which makes this scheme interesting for moderate to strong turbulence regimes. However, we need almost twice number of samplers, compared to the correlated case (see Figs. 3 and 6), resulting in a more complex Rx. Here, $p\left[r_{d,k}^{(i)}\middle|h_1,h_2,\tau_i,s_k,s_{k+1}\right]$ can be expressed as in (43) on the top of the next page. Notice that in contrast to the correlated scenario, here we have to detect the received signals in the presence of three unknown parameters, i.e., h_1 , h_2 , and τ . For this, we propose a two-step detection method as described in the following.

1) First Step: An initial estimate for h_1 and h_2 is obtained

$$\hat{h}_m = \eta^{-1} \max\{r_{1,m}^{(i)}, r_{2,m}^{(i)}, ..., r_{L,m}^{(i)}\}, \text{ for } m \in \{1, 2\}.$$
 (44)

Now, similar to the GLRT methodology, by substituting (6) and (44) in (20), the first decision step is expressed as

$$\hat{m}, \hat{i}, \hat{\mathbf{s}}(L) = \underset{m, i, \mathbf{s}(L+1)}{\arg \min} \mathcal{A}_2, \tag{45}$$

where

$$\mathcal{A}_{2} = \sum_{k=1}^{L} \frac{\left| r_{k,m}^{(i)} - \eta \, \hat{h}_{m} \, s_{k,m}' \right|^{2}}{\hat{h}_{m} \, s_{k,m}' \sigma_{s}^{2} + \sigma_{0}^{2}} + \log \left(\hat{h}_{m} \, s_{k,m}' \sigma_{s}^{2} + \sigma_{0}^{2} \right), \tag{46}$$

 $m \in \{1, 2\}, s_{k,1} = s_k, s_{k,2} = \bar{s}_k, \text{ and }$

$$s'_{k,m} = \left(1 - \frac{1}{2N_s}\right) s_{k,m} + \frac{1}{2N_s} s_{k+1,m}.$$
 (47)

Using the same approach we proposed in Appendix to reduce the complexity of calculation of (26), here we can reduce the search space of (45) to $8N_sL$, which is twice that of the GLRT-based method for the case of single wavelength transmission (see Appendix for more details).

2) Second Step: Now, assuming error-free signal detection in the first step, we use ML-based estimation of h_m to improve the accuracy of the initial estimate in (45):

$$\hat{h}_{m} = \frac{\sum_{k=1}^{L-1} r_{k,m}^{(i)} ((1 - \tau_{i}) s_{k} + \tau_{i} s_{k+1})}{\eta \sum_{k=1}^{L-1} ((1 - \tau_{i}) s_{k} + \tau_{i} s_{k+1})^{2}}.$$
 (48)

where we replace $\mathbf{s}(L) = \{s_1, s_2, ..., s_L\}$ by $\hat{\mathbf{s}}(L)$ from the first detection step and τ_i by $\overline{\tau}_i = 1/2N_s$. Using the improved h_m from (48), and similar to (20), we can formulate the second step of data detection as

$$\hat{i}, \hat{\mathbf{s}}(L) = \underset{i, \mathbf{s}(L+1)}{\operatorname{arg min}} \,\mathcal{A}_3,\tag{49}$$

$$p\left[r_{d,k}^{(i)}|h_{1},h_{2},\tau_{i},s_{k},s_{k+1}\right] = \frac{\exp\left(-\frac{\left|r_{d,k}^{(i)}-\eta(1-\tau_{i})(h_{1}\,s_{k}-h_{2}\,\overline{s}_{k})-\eta\,\tau_{i}(h_{1}\,s_{k+1}-h_{2}\,\overline{s}_{k+1})\right|^{2}}{2\left[(1-\tau_{i})(h_{1}\,s_{k}+h_{2}\,\overline{s}_{k})+\tau_{i}(h_{1}\,s_{k+1}+h_{2}\,\overline{s}_{k+1})\right]\sigma_{s}^{2}+2\sigma_{0}^{2}}}{\sqrt{2\pi\left(\left[(1-\tau_{i})(h_{1}\,s_{k}+h_{2}\,\overline{s}_{k})+\tau_{i}(h_{1}\,s_{k+1}+h_{2}\,\overline{s}_{k+1})\right]\sigma_{s}^{2}+\sigma_{0}^{2}}}.$$
(43)

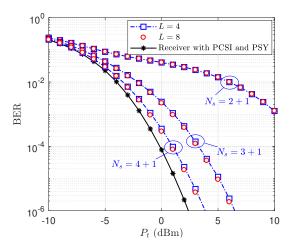


Fig. 7. BER Performance of scheme C for $\sigma_R^2=0.4$ and different values of L and N_s , compared to the BER achieved with PCSI and PSY.

where

$$\mathcal{A}_{3} = \sum_{k=1}^{L} \log \left(p \left[r_{d,k}^{(i)} \middle| \hat{h}_{1}, \hat{h}_{2}, \tau_{i} = \overline{\tau}, s_{k}, s_{k+1} \right] \right). \tag{50}$$

As explained in Appendix, the minimum of \mathcal{A}_3 is obtained when N_d positive values of $\mathbf{r}_{d,i}(L) - \gamma_{\text{th,opt}}$ are detected as bit '1' and $L - N_d$ negative values of $\mathbf{r}_{d,i}(L) - \gamma_{\text{th,opt}}$ are detected as bit '0', with $\gamma_{\text{th,opt}}$ given in (34), which is calculated by substituting h_1 and h_2 by their estimates from (48). This way, the search space for finding the minimum of \mathcal{A}_3 is reduced from $N_s \times 2^{L+1}$ to $2N_s$. The total search space associated with the first and the second steps is hence $2N_s(1+4L)$, which is much smaller than the initial search space of 2^L .

D. Simulation Results

To study the performance of the proposed blind detectors, consider first the case of highly correlated channels. In Fig. 7, we have presented the BER plots for different values of N_s and L. Here, L=4 and $N_s=5$ can be considered as appropriate choices since the obtained performance is quite close to the detector with PSY and PCSI, with an SNR gap of less than 2 dB at a target BER of 10^{-6} . This requirement to relatively small N_s and L makes this scheme interesting from a computational complexity point of view. Let us now investigate the case of independent h_1 and h_2 . We focus on the strong turbulence regime where having independent h_1 and h_2 allows to benefit from a diversity gain here. We have contrasted in Fig. 8 the BER performance of the proposed detector for different L and N_s . For the sake of presentation clarity, the cases of $N_s=4$, 6, and 8, are presented separately,

where we again notice the significant impact of N_s on the Rx performance. For instance, from Fig. 8a, for a relatively small value of $N_s=4$ (i.e., using two samplers on each wavelength), we do not obtain any performance improvement by increasing L and/or P_t . From Fig. 8 for $N_s=8$ and L=16, a BER performance close to the ideal receiver is achieved, with an SNR gap of less than 2 dB at a target BER of 10^{-6} . The requirement to larger N_s and L, compared with the correlated case, and the resulting higher computational complexity can be justified for the strong turbulence regime by the significant performance improvement obtained due to the link diversity.

E. Complexity Comparison

Besides the presented simulation results, in order to draw general conclusions on the advantage of the proposed blind detectors, we have compared them from an implementation complexity point of view in Table II.

V. CONCLUSION AND FUTURE WORK

In this work, we investigated optimal signal detection for an FSO link with high mobility under practical conditions where the Rx does not have any knowledge about the instantaneous channel fading coefficients and, in addition, it experiences sampling clock offset. The main idea behind the proposed schemes was to use multiple samplers at the Rx and to perform blind sequence detection on the resulting signal samples. First, we proposed two sequence data detectors based on ML and GLRT criteria for conventional OOK signaling where a single wavelength is used for signal transmission. Due to the relatively high computational complexity of these detectors, in a second step, we proposed a differential signaling structure based on the transmission of two wavelengths that can be selected as too close or otherwise very different. The former scheme is interesting under weak turbulence conditions, allowing to suppress the background noise effect, whereas the latter offers link diversity and, as a result, a significant performance improvement under relatively strong turbulence conditions. We proposed efficient blind signal detection methods for these two schemes and illustrated their efficiency through numerical results. Also, we discussed and contrasted the computational complexity of the proposed detectors, in particular, regarding the choice of the number of samplers and the frame length. It is worth mentioning that the suitable choice of these parameters does not depend on channel conditions.

In our work we assumed that the mobile transceiver are perfectly aligned. One way to align the mobile transceiver is by using an array of photodetector at the receiver to track the transmitter beam which may be associated with error. Future work will focus on studying and designing the receiver that

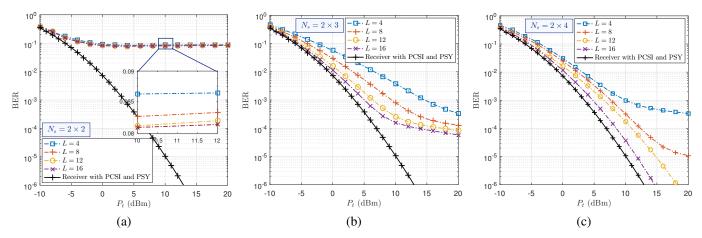


Fig. 8. BER Performance of scheme D for $\sigma_R^2=2$ and different values of L and N_s , compared to the BER achieved with PCSI and PSY for: (a) $N_s=2\times 2=4$; (b) $N_s=2\times 3=6$; (c) $N_s=2\times 4=8$.

TABLE II

COMPUTATIONAL COMPLEXITY COMPARISON OF PROPOSED DATA DETECTION SCHEMES.

Methods	Required	Required	Search	Comments	Computational
	N_s	L_s	Space		Complexity
ML,	4	8	2^{L+1}	ML-based detector, conventional OOK signaling; requires to know	Very high
Single			=512	$f_h(h)$ and solving two-dimensional integrations for each metric.	
Wavelength				Search space is too large.	
GLRT,	4	20	$4N_sL$	GLRT-based detector, conventional OOK signaling; does not require to know	Medium
Single			=320	$f_h(h)$; each metric consists of a series of additions and	
Wavelength				multiplications. Search space is relatively large.	
Differential	4+1	4	$2N_s$	GLRT-based detector, differential OOK signaling; does not require to know	Low
Signaling,	=5		=8	$f_h(h)$; each metric consists of a series of additions and	
Correlated				multiplications. Search space is very small. Closed-form formulation	
Channels				was derived for the metric. Suitable for weak turbulence conditions.	
Differential	2×4	16	$2N_s (4L+1)$	GLRT-based detector, differential OOK signaling; does not require to know	Relatively
Signaling,	=8		=1040	$f_h(h)$; each metric calculation consists of a series of additions and multiplications.	high
Independent				Search space is relatively large.	
Channels				Suitable for strong turbulence conditions.	

jointly synchronize and track the received optical signal before data detection.

APPENDIX

To avoid the exhaustive search in the GLRT detector, we develop here a fast search algorithm to implement (25). Let us show that for a fixed $N_1 = \sum_{k=1}^{L-1} s_k$, the minimum value of metric \mathcal{A}_1 is obtained when $\mathcal{R}_{on,1} = \sum_{k=1}^{L-1} r_k^{(i)} s_k$ takes its maximum value. The maximum value of $\mathcal{R}_{on,1}$ is achieved when N_1 observations among L-1 observations $\mathbf{r}_i(L-1) = \{r_1^{(i)},...,r_{L-1}^{(i)}\}$ are detected as bit one. As $N_1 \in \{0,1,...,L-1\}$ takes L different values, the search space is reduced from $N_s \times 2^{L+1}$ possible states to $4N_sL$, where N_s stands for the number of samplers, coefficient 4 characterizes the four possible states of $\{s_L,s_{L+1}\}$ and L stands for the number of possible states of N_1 .

In the sequel, we prove that the metric \mathcal{A}_1 is a decreasing function of $\mathcal{R}_{on,1}$. According to (27), in the case of signal independent noise, it is obvious that \mathcal{A}_1 is a decreasing function of $\mathcal{R}_{on,1}$. So, we consider the general shot noise and thermal noise scenario characterized by (26). We consider the worst case where $N_1 < L/2$ and for $k \in \{1, 2, ..., L-1\}$ if $s_k = 1$, then s_{k+1} and s_{k-1} are equal to zero. In other words, the worst case here is when the received sequence does not

contain two consecutive bits "1". In this worst case, A_1 can be rewritten as

$$\mathcal{A}_{1} = -\frac{2\eta}{\sigma_{s}^{2}} \underbrace{\left(\mathcal{B}_{1} \mathcal{R}_{on,1}^{(i)} + \mathcal{B}_{2} \mathcal{R}_{on,1}^{\prime(i)}\right)}_{I_{1}} + N_{1} \log \mathcal{B}_{1}^{\prime}$$
$$-\frac{1}{\sigma_{0}^{2}} \underbrace{\left(\mathcal{B}_{1} \mathcal{R}_{on,2}^{(i)} + \mathcal{B}_{2} \mathcal{R}_{on,2}^{\prime(i)}\right)}_{I_{1}} + N_{1} \log \mathcal{B}_{2}^{\prime} + C_{1}, \quad (51)$$

where $\mathcal{B}_1 = \frac{\mathcal{B}_1'}{\mathcal{B}_1' + \sigma_0^2}$, $\mathcal{B}_2 = \frac{\mathcal{B}_2'}{\mathcal{B}_2' + \sigma_0^2}$, $\mathcal{B}_1' = \hat{h}\sigma_s^2 \left(1 - \frac{1}{2N_s}\right)$, $\mathcal{B}_2' = \hat{h}\sigma_s^2 \frac{1}{2N_s}$, and C_1 is independent from both $\mathbf{s}'(L-1)$ and $\mathbf{r}_i(L-1)$. Note that, y = x/(x+a) is an increasing function of x where a is a constant term. As \hat{h} is an increasing function of $\mathcal{R}_{on,1}^{(i)}$, \mathcal{B}_1' and \mathcal{B}_2' and consequently \mathcal{B}_1 and \mathcal{B}_2 are an increasing function of $\mathcal{R}_{on,1}^{(i)}$, $\mathcal{B}_{on,1}^{(i)}$. Considering the relationships between $\mathcal{R}_{on,1}^{(i)}$, $\mathcal{R}_{on,1}^{(i)}$, $\mathcal{R}_{on,2}^{(i)}$ and $\mathcal{R}_{on,2}^{(i)}$, it is easily verified that the terms I_1 and I_2 increase by increasing $\mathcal{R}_{on,1}^{(i)}$. On the other hand, at high SNR regime, we have $\mathbb{E}\left[\mathcal{R}_{on,1}^{(i)}\right]/\sigma_s^2 \gg 1$ and $\mathbb{E}\left[\mathcal{R}_{on,2}^{(i)}\right]/\sigma_0^2 \gg 1$, where $\mathbb{E}[.]$ denotes expectation. So, we have $\frac{2\eta}{\sigma_s^2}I_1 \gg N_1\log\mathcal{B}_1'$ and $\frac{I_2}{\sigma_0^2} \gg N_1\log\mathcal{B}_2'$. This confirms that for the worst case, the metric \mathcal{A}_1 is a decreasing function of $\mathcal{R}_{on,1}^{(i)}$. Hence, for a given N_1 , instead of searching

over $N_s \times {L-1 \choose N_1}$ possible states, we can compute metric \mathcal{A}_1 for N_s cases in which the N_1 maximum values of $\mathbf{r}_i(L-1)$ s are considered as bit "1". This proves that the total search space is reduced from $N_s \times 2^{L+1}$ to $4N_sL$. For instance, for $N_s = 3$ and L = 10 and 20, the fast search method reduces the search space from 6144 and 6291456 to 120 and 240, respectively.

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