

Design, operation and performance of the PAON4 prototype transit interferometer

R. Ansari, J.E Campagne, D. Charlet, M. Moniez, C. Pailler, O. Perdereau, M. Taurigna, J.M. Martin, F. Rigaud, P. Colom, et al.

▶ To cite this version:

R. Ansari, J.E Campagne, D. Charlet, M. Moniez, C. Pailler, et al.. Design, operation and performance of the PAON4 prototype transit interferometer. Monthly Notices of the Royal Astronomical Society, 2020, 493 (2), pp.2965-2980. 10.1093/mnras/staa345 . hal-02418270

HAL Id: hal-02418270

https://hal.science/hal-02418270

Submitted on 12 Jun 2020

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Downloaded from https://academic.oup.com/mnras/article-abstract/493/2/2965/5799007 by INFU BIBLIO PLANETS user on 12 June 2020

Design, operation and performance of the PAON4 prototype transit interferometer

R. Ansari,^{1,2} J. E. Campagne,^{1,2} D. Charlet,^{1,2} M. Moniez,^{1,2} C. Pailler,^{1,2} O. Perdereau,^{1,2} M. Taurigna,^{1,2} J. M. Martin,³ F. Rigaud,³ P. Colom,⁴ Ph. Abbon,⁵ Ch. Magneville,⁵ J. Pezzani,⁶ C. Viou [©],⁶ S. A. Torchinsky,⁷ Q. Huang^{1,8} and J. Zhang^{1,8,9}

Accepted 2020 February 3. Received 2020 February 3; in original form 2019 October 11

ABSTRACT

PAON4 is an L-band (1250–1500 MHz) small interferometer operating in transit mode deployed at the Nançay observatory in France, designed as a prototype instrument for intensity mapping. It features four 5 m diameter dishes in a compact triangular configuration, with a total geometric collecting area of \sim 75 m², and is equipped with dual polarization receivers. A total of 36 visibilities are computed from the eight independent RF signals by the software correlator over the full 250 MHz RF band. The array operates in transit mode, with the dishes pointed toward a fixed declination, while the sky drifts across the instrument. Sky maps for each frequency channel are then reconstructed by combining the time-dependent visibilities from the different baselines observed at different declinations. This paper presents an overview of the PAON4 instrument design and goals, as a prototype for dish arrays to map the large-scale structure in radio, using intensity mapping of the atomic hydrogen 21 cm line. We operated PAON4 over several years and use data from observations at different periods to assess the array performance. We present a preliminary analysis of a large fraction of these data and discuss crucial issues for this type of instrument, such as the calibration strategy, instrument response stability and noise behaviour.

Key words: cosmology: observations, large-scale structure of Universe – instrumentation: interferometers – methods: observational – techniques: interferometric – radio continuum: general – radio lines: galaxies.

1 INTRODUCTION

Despite the tremendous success of the Λ CDM cosmological model and the wealth of information provided by the analysis of CMB anisotropies (Hinshaw et al. 2013; Planck Collaboration 2016, 2018), SNIa luminosities (Betoule et al. 2014) and optical surveys (see e.g. Salazar-Albornoz et al. 2017; Abbott et al. 2018; DES Collaboration 2018), the nature of dark matter and dark energy

remains elusive (Bull et al. 2016) and a number of fundamental physics questions still need clarification. The large-scale structure (LSS) and its baryon acoustic oscillation (BAO) feature are among the most powerful probes to constrain the cosmological model and dark energy and modified gravity models (Amendola et al. 2013). The matter distribution on the large scale in the universe is usually mapped through optical photometric and spectroscopic surveys.

The 21 cm line emission/absorption at 1.42 GHz due to the hyperfine transition of neutral atomic hydrogen (H I) is a unique spectral feature in the L/UHF band that can be used to trace matter distribution from the vicinity of the Milky Way at very low redshifts,

¹LAL, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, 91405 Orsay, France

²Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France

³GEPI, UMR 8111, Observatoire de Paris, 61 Av. de l'Observatoire, 75014 Paris, France

⁴LESIA, UMR 8109, Observatoire de Paris, 5 place Jules Janssen, 92195 Meudon Cedex, France

⁵CEA, DSM/IRFU, Centre d'Etudes de Saclay, 91191 Gif-sur-Yvette, France

⁶Station de Radioastronomie de Nançay, Observatoire de Paris, PSL Research University, CNRS, Université d'Orléans, 18330 Nançay, France

⁷APC, Université Paris Diderot, CNRS/IN2P3, CEA/Irfu, Observatoire de Paris, Sorbonne Paris Cité, 75205 Paris Cedex 13, France

⁸National Astronomical Observatories, Chinese Academy of Sciences, Beijing 100012, China

⁹College of Physics and Electronic Engineering, Shanxi University, Shanxi 030006, China

^{*} E-mail: campagne@lal.in2p3.fr

up to cosmological distances at $z\sim 1$ –3, and into the epoch of Reionization (EoR) at redshifts well above 10. Using the 21 cm line to study the dark ages and the EoR has been considered for more than 20 yr (see e.g. Furlanetto, Oh & Briggs 2006; Pritchard & Loeb 2008) and several experiments have been carried out or are ongoing to detect the 21 cm signal from the EoR. LOFAR (van Haarlem et al. 2013), MWA (Tingay et al. 2013), PAPER (Parsons et al. 2010), HERA (Pober et al. 2014), NenUFAR (Zarka et al. 2015) are among the main dedicated instruments targeting EoR signal detection.

As already noted more than a decade ago (Abdalla & Rawlings 2005; Peterson, Bandura & Pen 2006), mapping the 3D distribution of matter using H I as a tracer is an elegant and complementary approach to optical surveys to constrain cosmological parameters and dark energy through the study of LSS and BAO. The early proposals considered the observation of individual galaxies at $\lambda = 21$ cm, requiring very large collecting areas and sensitivities, which is expected for SKA¹ (Braun et al. 2015).

However, it was soon realized that the study of LSS with the 21 cm emission could be carried out through the intensity mapping technique, without the need to resolve individual H1 sources, and with less-stringent requirements on instrument sensitivity. To perform such a survey, a wide-band instrument with a wide field of view is required, operating in the L/UHF band, from a few hundred MHz to 1400 MHz ($\nu = 1420.4/(1+z)$ MHz). A modest angular resolution of a fraction of a degree (\sim 10') is enough to determine the matter power spectrum on the scales most useful for cosmology (Chang et al. 2008; Ansari et al. 2008; Wyithe, Loeb & Geil 2008; Peterson et al. 2009).

This approach has a major drawback even without considering the instrument noise and radio frequency interference (RFI). The foreground emission in the radio spectrum, around 1 GHz, has brightness temperatures above 10 K, and is dominated by the Milky Way synchrotron emission and radio sources. The foregrounds are thus a few thousand times brighter than the cosmological signal, which is of the order of, or below, 1 mK. This huge level of foreground emission makes the component separation a challenging task, much more difficult compared to CMB observations. The smooth frequency dependence of the synchrotron emission is the key to solving this daunting task. The problem is similar for experiments looking for the 21 cm signal from the EoR and has been studied by a number of authors (e.g. Wang et al. 2006).

The detectability of the cosmological 21 cm signal at lower redshifts ($z \lesssim 3$) in the presence of foregrounds has been subsequently studied (e.g. Ansari et al. 2012b; Wolz et al. 2014). The advantages of the m-mode analysis for map making and foreground subtraction, applicable for a transit-type interferometer, is discussed in Shaw et al. (2014) and extended to the polarization case in Shaw et al. (2015).

The interest in intensity mapping (IM) as a tool for cosmological and dark energy surveys has grown over the last decade, with broadened science reach (Bull et al. 2015b; Cosmic Visions 21 cm Collaboration 2018). A number of groups have engaged in exploiting existing instruments to carry out intensity mapping surveys, for example using GBT (Chang et al. 2010; Masui et al. 2013) or plan to do so with SKA and its pathfinders (Bull et al. 2015a), or with single-dish telescopes (Bigot-Sazy et al. 2015) such as FAST (Bigot-Sazy et al. 2016).

Other groups are building specifically designed instruments for such surveys. Most groups plan to use dense interferometric arrays, associated with high-throughput digital beam-forming and digital correlators that can fulfil the instrumental requirements for IM surveys. Single-dish instruments combined with multi-feed receivers provide an alternative instrumental design. A seven-beam receiver covering the frequency band 700–900 MHz was envisaged for the GBT (Chang & GBT-HIM Team 2016) and a ~50-feed receiver will be built and placed at the focal plane of an off-axis reflector by the BINGO team (Battye et al. 2013; Wuensche & the BINGO Collaboration 2018).

Dedicated IM instruments share a number of common features and problems with wide-field arrays built or under development to search for the EoR signal, such as LOFAR, MWA, PAPER, HERA, and NenUFAR, although the latter observe at much lower frequencies ($\nu \sim 100$ MHz, $z \sim 10$). Two main options are considered for IM interferometric arrays. Either cylindrical reflectors, oriented north-south, possibly with fast Fourier transform (FFT) beamforming along the cylinder axis, or an array of dishes, with pointing capability in declination. FFT beam-forming is also possible using a regular grid of antennas, including dishes, as mentioned by Tegmark & Zaldarriaga (2009). Such a strategy has already been implemented on a modest scale in individual LOFAR stations for the High Band Array, and at around 1 GHz frequencies in EMBRACE (Torchinsky et al. 2016). This was the ultimate goal of the SKA mid-frequency array with an early demonstrator called 2-PAD (Armstrong et al. 2009).

In addition to the cosmological 21 cm signal detectors, such dedicated instruments will be powerful machines for time-domain radio astronomy. Indeed, the large mapping speed of transit interferometers would make them suitable to search for rare transient phenomena, such as fast radio bursts (FRB) or pulsars. FRBs correspond to bright broad-band radio flashes,² discovered in recent years (Thornton et al. 2013). High values of dispersion measures (DM) suggest an extragalactic origin, confirmed by the host identification for at least one FRB (Chatterjee et al. 2017). Pulsars can be considered as astrophysical clocks, and high precision timing measurements of a large number of millisecond pulsars (MSP) is being carried out in pulsar timing array (PTA) programs (Perera et al. 2019), to search for low-frequency gravitational waves. Dedicated searches are also being carried out, such as (Stovall et al. 2014) to increase the MSP population. Wide-band transit interferometers could also carry out FRB and pulsar searches in parallel to the intensity mapping survey, if equipped with dedicated digital backends.

CHIME (Bandura et al. 2014), which is among the most advanced IM projects, uses an array of cylinders, as pioneered by the Pittsburgh Cylindrical Telescope (PCT) prototype (Bandura 2011). The HIRAX project (Newburgh et al. 2016) plans to build a large array of 6 m dishes, in South Africa, close to the SKA site, and larger arrays, such as the proposed PUMA, are being considered (Bandura et al. 2019).

Development of the PAON4 array and the data analysis procedures is closely linked with Tianlai. Tianlai is an NAOC-led project (Chen 2012; Das et al. 2018) that is currently operating two pathfinder instruments in a radio-quiet site in the Xinjiang province of western China. The first Tianlai instrument is composed of three cylinders, each 40 m long and 15 m wide, equipped with a total of 96 dual polarization receivers. Following initial evaluation

¹SKA organization: https://www.skatelescope.org/

²The FRB catalogue: http://frbcat.org



Figure 1. PAON4 dish array interferometer at Nançay, viewed from the south-west.

and design work for PAON4, the Tianlai instrument concept was extended by including a second array (Tianlai16D) composed of 16 steerable 6 m diameter dishes, in a dense circular configuration. We carried out studies to optimize the PAON4 and Tianlai16D array configurations and evaluate the performance (Zhang et al. 2016a, b).

This paper is organized as follows. The PAON4 instrument design and project history are presented in Section 2. Section 3 presents an overview of the electronics chain, the software correlator and the acquisition system. The instrument operation and the survey are described in Section 4, while the data analysis pipeline is discussed in Section 5. Section 6 presents the instrument performance and some preliminary results from the ongoing survey. The paper concludes with an outline of our future plans for PAON4 followed by concluding remarks.

2 PAON4 INSTRUMENT DESCRIPTION

Preliminary design of a small dish interferometer at Nançay began in 2010. The project, subsequently named Paraboles à l'Observatoire de Nançay (PAON – Paraboloids at the Nançay Observatory), was approved in 2012 spring by the partner institutes: LAL-CNRS/IN2P3, Observatoire de Paris, and Irfu/SPP (CEA). The goal is to evaluate specific issues of dense interferometric arrays operating in transit mode. In particular, the project investigates:

- (i) electromagnetic coupling between neighbouring receivers at close distance and the impact on the correlated noise;
- (ii) array stability and the gain and phase calibration using bright sky sources;
- (iii) data analysis and sky map reconstruction from timedependent visibilities.

During a short test period from 2012 autumn to 2013 summer, two 3 m diameter dishes were used for observation at Nançay. Meanwhile, the PAON4 reflectors were designed and manufactured. The mount and reflectors were assembled on site during the end of 2014 spring/summer and then equipped with the receivers and electronic modules in 2014 autumn. First observations were carried out in 2015 winter, and the instrument was formally inaugurated in

2015 April. The four reflectors are visible in the photograph shown in Fig. 1, taken from a point south-west of the array.

2.1 Array configuration

The PAON4 interferometer is composed of four 5 m diameter parabolic F/D=0.4 reflectors and has a combined geometric collecting area of $\sim 78~\text{m}^2~(\sim 60~\text{m}^2~\text{effective}$ area for $D_{\rm eff}\sim 4.4~\text{m})$. It is hosted at the Nançay radio observatory³ in France, about 200 km south of Paris. The array (central antenna) is located at latitude $47^{\circ}22'55.1''$ N and $2^{\circ}11'58.7''$ E longitude.

The PAON4 compact triangular configuration was selected after comparison of several possibilities. The chosen configuration provides six independent baselines, which is the maximum possible with four antennas, compared to four baselines for a rectangular 2×2 configuration. Moreover, the beam of the triangular configuration has a much more circular shape than the 2×2 , and its resolution is also slightly better than a single dish of 14 m diameter (Zhang et al. 2016b). Three dishes are positioned at the three vertices of an equilateral triangle with 12 m sides, while the fourth dish is located close to the centre of the triangle. In addition to the four autocorrelation signals (zero length baseline), there are six independent baselines, as shown in the array layout schematic of Fig. 2. One baseline (1–2) is aligned with the east—west direction, one baseline (3–4) lies along the north—south direction, and the four other baselines have both EW and NS components.

The receiver on each reflector is made of a cylindrical feed with two probes sensitive to two polarizations. The *H* probe is sensitive to the electric field parallel to the EW direction, and the *V* probe is sensitive to the field in the meridian plane. There are thus a total of eight RF signals from the four feeds: four *H*-polarization signals and four *V*-polarization ones. These are amplified, filtered and frequency shifted to the VHF band before being digitized. The digitized signals are processed in real time by a small cluster of acquisition computers that calculate all correlations. Two additional RF signals pass through identical analogue and digital electronic

³Nançay radio observatory, https://www.obs-nancay.fr/

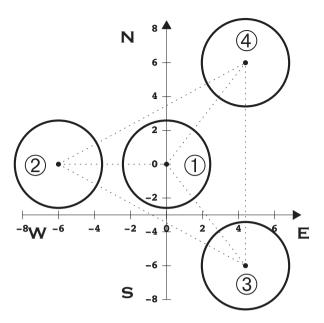


Figure 2. PAON4 array layout (coordinates are in metres).

chains before being fed to the acquisition computer. The first one, called RFIMON, carries an RF signal from a simple dipole antenna and is used to monitor the RFI environment in the PAON4 band. The second RF signal comes from a 50 Ω resistor connected to the input of an LNA, identical to the one that equips the H and V probes. This RF signal, referred to as THERMON, is used to monitor the temperature-dependent gain variations of the analogue electronic chain and correct for it. This is discussed further in Section 5. PAON4 also includes a standard temperature probe that is read every few minutes, providing temperature variations of the antenna environment. The mount, reflector and feed design is discussed hereafter, and the electronic chain and the software correlator are described in Section 3.

2.2 Reflector and feed design

The antennas were designed and built at the Observatoire de Paris GEPI laboratory and by industry subcontractors. The design has been chosen in order to fulfil the following requirements:

- (i) build four prototype antennas with 5 m diameter with a parabolic reflector;
- (ii) build a robust antenna architecture to be able to sustain historical storm conditions in the region of Nançay (i.e. wind speed of $\sim\!130~km\,h^{-1})$ as well as snow and ice during severe winter conditions;
- (iii) permit the dish motor to orient in a broad range of elevation (declination) angles;
- (iv) limit the cost as much as possible while ensuring reliable operations for 10 yr or more.

Some design parameters are summarized in Table 1 and the whole array is shown in Fig. 1.

The mechanical structures of the antennas are standard steel structure elements that have undergone anti-corrosion treatment by hot-dip galvanizing, and were prepared (cut, drilled) by numerically controlled machines by the subcontractor. Each parabola is made of 12 petals for logistical reasons. Each petal is made of a laser-cut stainless steel sheet with a carefully hand-installed reflector mesh.

Table 1. Main design parameters of the PAON4 dish and feed.

Dish				
Diameter reflector	5 m			
f/D	0.4			
$L \times W \times H$	$6 \times 5 \times 5.4 \text{ m}$			
Roughness (design)	$\lambda/50$ at 21 cm			
Zenith angle	15 °N to 38 °S			
Total weight	2200 kg			
Feed, choke	and probes			
Diameter 'choke'	360 mm			
Height 'choke'	80 mm			
Distance from entrance	10 mm			
Thickness	1.5 mm			
Diam. internal 'feed'	158 mm			
$\Delta D/D$	$5.10^{-3} (0.8 \text{ mm})$			
Thickness	4.5 mm			
Height (total)	377 mm			
Probes	2 (linear)			
Probe (diam./length)	6.2 mm/50.2 mm			
Conic part of the probe	2.5 mm			
Distance probe-end cap	79.2 mm			
Base	N std. Radiall R 161 404			
Gain (meas./sim.)	9.5 dB/10.34 dB			

About 600 h were required to install the mesh at the GEPI laboratory. The surface deviations of the mesh were kept as low as possible, and they were measured after mounting at a level of $\lambda/70$ r.m.s. This design is well adapted for a project on the scale of PAON4, but for a larger array a more automated process would be required since non-negligible manpower on site was required for the mounting of the 48 petals.

Asynchronous motors with reduction gears and non-reversible trapezoidal screws are used for the declination axis pointing. The rotation of the motor is selected by embedded software, and takes into account the stop phase duration for better pointing precision. The position of the parabola is controlled by an accelerometer that is installed in a sealed control command box and is therefore fully protected against the weather conditions, unlike the position encoders. In addition to performing pointing measurements, the accelerometer can monitor any small angular displacement of the antennas such as those due to possible ground instabilities. A running mean of 2000 samples is performed in order to measure the position of each parabola. The pointing of the antennas is controlled by scripts or by an embedded web server accessible through the internet. A precision of $\sim 0.1^{\circ}$ has been measured on site.

The PAON4 antennas are installed near the EMBRACE prototype (Torchinsky et al. 2016), and could therefore be easily connected to the electric mains and Ethernet network. At this place, the ground is particularly loose and, in order to avoid having to build expensive and fixed concrete foundations, the antenna structures are slightly flexible with respect to horizontal stability, and are equipped with four legs in a statically undetermined configuration. In addition, the rotation axis bearings include kneecaps.

The feed design was adapted to the dish diameter, taking into account the needs of two orthogonal linear polarizations and the total bandwidth [1250, 1500] MHz. It uses a classical circular wave guide with a choke. The geometric parameters are listed in Table 1. The guide has a diameter of 158 mm and a length of 377 mm machined inside a aluminium guide 4.5 mm thick. The cut-off frequencies are 1110 MHz for the TE11 mode and 1460 MHz for the TM01 mode,



Figure 3. Photograph of a feed: The two amplifiers for the H and V probes are located in the two boxes at the top.

Radiation diagram (feed & choke only) at 1400 MHz (dBi)

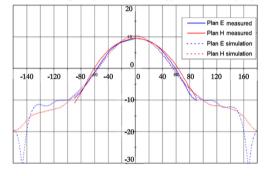


Figure 4. Radiation diagram of the feed and choke: measurement (solid lines) and simulation (dashed lines).

making the feed system single moded throughout the bandwidth except in the upper 40 MHz. The guide wavelength is $\lambda=543$, 341, 299 mm at 1250, 1420, 1500 MHz. The machining guarantees a circular tolerance of $\Delta D/D=5\times 10^{-3}$ (0.8 mm) for a cross-polarization isolation of -30 dB. This feed is suitable for the PAON4 bandwidth but could not be easily adapted to a larger bandwidth. The probes are made with brass rods of relatively large diameter to have the possibility of larger bandwidth in the future. The conic shape of the rod minimizes the impedance mismatch with the base. The exact locations of the probes inside the circular guide have been optimized by simulation and verified by measurement a posteriori. The choke design has also been optimized by simulation to reduce side lobes as much as possible.

Fig. 3 shows the manufactured feed. The feed is maintained at the focal location by three fibreglass hollow bars to optimize the electromagnetic transparency of the supports while ensuring robustness during high wind conditions. The radiation diagram of the feed alone has been simulated and then measured with good agreement, as shown in Fig. 4.

3 ELECTRONIC AND ACQUISITION SYSTEM

PAON4 is equipped with the analogue and digital electronic modules developed in the BAORadio project, begun in 2007, mostly as digital components for a 21 cm H I intensity mapping survey (Ansari et al. 2012a). The ADC boards are based on FPGA technology.

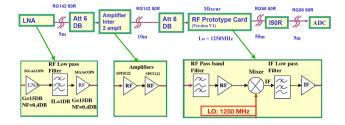


Figure 5. Schematic view of the PAON4 analogue electronics chain.

Each is capable of digitizing four RF signals at 500 MHz sampling rate, and performing an FFT in real time with 61 kHz frequency resolution (Charlet et al. 2011).

An analogue RF amplification, filtering, local oscillator and mixer were designed and realized for testing the digital component boards with the PCT (Pittsburgh cylindrical reflectors). The LNA was specifically designed and made for PAON4. The electronic chain, and in particular the analogue components, were designed primarily for testing purposes and the performance does not equal the current state-of-the-art.

The BAORadio electronics and the associated data acquisition software were used several times on the PCT at Pittsburgh (Bandura 2011). In 2010, 32 signals were processed from the PCT feeds, including the computation of the full set of 512 correlations, over a reduced band of $\sim 50\,\mathrm{MHz}$. The same system was also used on the FAN project (Deschamps et al. 2013) and successfully deployed at the NRT (Nançay Radio Telescope) for the HICluster program, searching for H I in nearby clusters (Ansari et al. 2016).

3.1 Analogue and digital electronics

An overall schematic view of the PAON4 analogue electronics chain is shown in Fig. 5.

The amplifier circuit consists of two LNAs interconnected through a low pass filter. The amplifiers are installed at the feed. They are connected to the probes through 10 cm cables. An Avago/Broadcom MGA633 GaAs MMIC ultra-low-noise amplifier is followed by a Ooryo SPF5122 LNA, and a low pass filter is inserted between the two LNAs to lower the power at the input of the second one. The total gain is 30 dB and the noise factor NF \sim 0.6 dB, leading to a noise temperature of $T_a \sim$ 50 K for the the first stage amplifier ($F=1+\frac{T_a}{290\,\mathrm{K}}$; NF = $10\log_{10}(F)$). An 8 mRG142 cable connects the feed amplifiers to the second stage amplifier on the antenna. This stage consists of two SPF5122 LNAs and provides an additional gain of 30 dB, which is connected to the frequency shifter in the main analogue electronics cabinet on the central antenna with a second 8 m RG142 cable. After an RF filter, the signal is amplified before down conversion. An ADF4360-5 PLL and VCO frequency synthesizer delivers a 1250 MHz signal to a JMS-11X frequency mixer. The signal is down-converted to the [0-250 MHz] VHF band. Additional VHF amplification is performed and a low pass filter (20 dB at 1500 MHz) eliminates the high-frequency part of the signal. The RF card output is connected to the ADC board in the EMBRACE (Torchinsky et al. 2016) container by two 50 Ω RG58 cables. A first 40 m cable brings the signal to the feedthrough panel at the container wall, followed by a 10 m cable from the feedthrough panel to the PAON4 digital electronics.

Each BAORadio ADC board includes two (ADC+FPGA) blocks sharing common control electronics. Each block handles two analogue inputs that are sampled at 500 Msample s⁻¹ with

Table 2. PAON4 datasets.

Dataset	Period	Declination (deg)	No. scans	Duration	Comment
CygA-Sep16	2016 autumn	37–44	10	2 wk	FFT firmware
CasA-Sep16	2016 autumn	56-60	5	2 wk	FFT firmware
CygA-Nov16	2016 autumn	35-46	11	2 wk	FFT firmware
Scan_2018 A	2018 summer	40-60	20	\sim 2 mth	$\delta_{step} = 1 \deg$
Scan_2018 B	2018 autumn	40-60	20	\sim 2 mth	$\delta_{step} = 1 \deg$
LD ₋ 1	2019 January	25, 30, 42, 58	4	\sim 10 d	CasA, CygA, M1, VirA
LD_2	2019 April/May	12-24	7	2 wk	M1, Sun
LD_3	2019 June, July	35	1	10 d	CygA, stability checks
LD_4	2019 July	12, 22, 58	3	$\gtrsim 2 \text{ wk}$	CasA, M1, VirA

8-bit dynamic range. Each block transmits data through high-speed optical links to dedicated PCIExpress reception boards in the acquisition computers. The eight PAON4 RF signals (4 H-pol + 4 V-pol) are thus digitized by two ADC boards, and data is transmitted via four optical fibres to the acquisition computers located a few hundred metres away. A third ADC board handles the RFIMON and THERMON channels, which are treated separately by the acquisition computer and do not go through the correlator. The ADC boards are configured and controlled through USB links and they receive a common master clock and trigger signals through dedicated connectors. Two different versions of the firmware can be loaded on the ADC board FPGAs. The first one, called the RAW firmware, is used to digitize signal and transmit waveforms to the acquisition computers. The RAW firmware can handle a maximum of 48k samples corresponding to 96 µs long digitization frames. The second firmware, called the FFT firmware, performs waveform sampling, Fourier transform (FFT), clipping, and then transmits the Fourier coefficients (2-byte complex numbers) for 8k sample digitization frames corresponding to 16 µs in time and 4096 Fourier coefficients with 61 kHz frequency resolution. Each digitization frame is time-tagged with the 125 MHz FPGA clocks and the digitization frames on different FPGAs are synchronized by the external trigger signal. The BAORadio ADC boards can cope with a maximum trigger rate of ~30 kHz, corresponding to \sim 50 per cent on-sky time. However, the current acquisition computer system and software correlator can only cope with a trigger rate of ≤5 kHz, corresponding to ≤10 per cent on-sky time. We carried out observations with the FFT firmware in 2016 September and November (see Table 2), but the results discussed in this paper are mostly based on data taken with the RAW firmware. The digital data stream, either waveform or Fourier components, is transferred over optical fibres to the software correlator-acquisition computer cluster located 300 m away, in the Nançay computer building.

3.2 Data acquisition and software correlator

The data acquisition system is composed of a cluster of computers located in a dedicated room in Nançay. They are interconnected through a private 10 Gbit s⁻¹ Ethernet network. Communication to the outside world is done through the external 1 Gbit s⁻¹ Ethernet network. An additional computer connected through the Nançay private network is located in the EMBRACE container. It is also on another dedicated network and controls a number of subsystems including power supplies, local oscillator (LO), as well as the thermometer readout. The same computer handles the control of the ADC boards through USB communication with the pointing controllers of the four antennas.

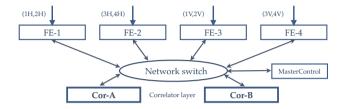


Figure 6. Schematic view of the PAON4 acquisition and correlator system.

The acquisition/software correlator system itself is composed of six computing nodes and an additional machine acting as the acquisition controller and supervisor. The computing nodes are arranged in two layers: four of them form the first layer (frontend machines), which receive data from the two ADC boards, through four optical links. The two nodes forming the second layer perform the correlation computations. Fig. 6 shows a schematic view of the system configuration. The acquisition and processing of the two ancillary RFIMON and THERMON signals is done by an independent computer running the same software.

The front-end machines perform FFT on the received data streams, except when the FFT firmware is used, and then divide the frequency bands into a number of sub-bands corresponding to the number of computing nodes in the correlator layer. Each front-end machine receives the data corresponding to two RF signals, currently arranged as a pair of polarization signals, *H*–*H* or *V*–*V*. Fourier components for each sub-band are sent to the corresponding compute node in the correlator layer, which has two nodes, each computing 36 correlations for 2048 frequency channels over the 125 MHz band, which is half of the full ADC board Nyquist sampling limit of 250 MHz. The 36 computed correlations correspond to the following pairs:

- (i) eight autocorrelations, four corresponding to the H signals and four to the V signals;
- (ii) 12 correlations corresponding to the cross-correlations between the same polarization signals. There are $\sin H H$ and $\sin V V$ cross-correlations between H-polar and V-polar signals from the four feeds;
- (iii) 16 correlations corresponding to H–V cross-correlations between the H-polarization signal from one feed and the V-polarization signal from the second feed.

The total data rate ingested by the front-end machines at \sim 10 per cent on-sky time corresponds to \sim 400 MB s⁻¹, with a factor of 4 higher rate exchanged between the two layers, as the FFT computation is carried out with 4-byte floating point numbers. Correlations are taken typically at a sampling rate of one or a few seconds. Most data discussed here were taken with a correlation

sampling rate of 3 or 6 s. Computed correlations (also called 'visibilities') are saved into permanent storage (disc) every few seconds, and a number of visibility matrices, defined again by input parameters, are grouped into a single file. A typical 24 h observation run with 3 s visibility sampling rate produces around 70 GB of data, split into ~ 100 MB size files.

The data acquisition and correlator software, TACQ, was developed for the BAORadio project starting in 2007 and has been enhanced over the years. It is a flexible high-performance C++ software package, which uses the SOPHYA⁴ class library for standard numerical algorithms and I/O. The flexibility and various operation modes allows TACQ to be used at different stages of the project, from final tests of the electronic system boards to the routine operation of the interferometer, as well as during commissioning.

The TACQ package defines a simple and very efficient multithreaded architecture, where different threads communicate through a central memory manager hub. The number of running threads is also dynamically determined through the parameters that are tuned to a given hardware configuration. A description of the software architecture, the different classes and system operation modes is beyond the scope of this paper and will be discussed in a separate forthcoming publication.

In practice, a main program called MFACQ with different operation modes, controlled by an extended set of parameters, handles the acquisition and correlation computation tasks. The control node spawns one MFACQ process in each of the compute nodes, the four front-end nodes and the two nodes in the correlator layer for PAON4, and provides each process with their specific set of parameters. The complete system operates in streaming mode, with data packets exchanged between MFACQ processes through the network layer. The time synchronization for visibility computation is ensured by the hardware time tags that are propagated through the data packet streaming protocol.

4 OPERATIONS AND OBSERVATIONS

After the completion of its construction (mid-2015), the PAON4 observations served several aims in successive periods, with few minor hardware or software changes. Observations carried out in 2015 were mostly dedicated to hardware debugging, from finding faulty cables and electronic modules to identifying some RFI sources. For example, an Ethernet switch was initially installed in the central antenna electronic cabinet, to ensure the readout of a temperature sensor, and was generating RFI. We also spent some time measuring correlated noise, both on the instrument and in the lab, in 2015 and 2016. Correlated noise measurements in the lab showed that the main source was by coupling through the power supply. The overall system was subsequently improved with better shielding, more careful ground wiring, and an improved power supply system. The correlated noise level was reduced by a factor of 10 in this process. Gain variations and some randomly occurring perturbations were observed. Clarifying their sources and curing or correcting these effects consumed significant time and effort in 2017 and early 2018, as discussed in Section 5.

In 2016 May, the 4V channel was terminated by connecting its front-end LNA to a 50 Ω resistor. This was done as a diagnostic for understanding the source of perturbations (see Section 5.1) and gain variations (see Section 5.2). The 4V channel was reconnected to the antenna and the additional THERMON signal was added to

⁴SOPHYA C++ class library: http://www.sophya.org/

the system in 2018 July, after the identification of the perturbation source. In 2015 and 2016, we were operating PAON4 with the FFT firmware loaded on the ADC boards. The ADC boards were then sending FFT coefficients to the software correlator. We switched to the RAW firmware in 2017 February, in order to investigate some problems with the FFT firmware, including possible saturation by satellite signals because of the limited dynamic range of the FFT firmware. We also added two front-end nodes to handle FFT computation by the acquisition/correlator software.

Data taking is automatic once all acquisition parameters are set, and can be remotely initiated and monitored. After each acquisition run, data are transferred to the IN2P3 computing centre for analysis and archival. An SSH connection to the acquisition cluster is used for launching the data taking. It sets up the antenna and configures the digitization boards, and checks or modifies the acquisition parameters such as the visibility sampling rate, the observation ID and the dataset path on the master control node. The acquisition is started or scheduled to begin at a later time.

The PAON4 instrument has been designed to survey a significant fraction of the northern sky, 3000-5000 deg², with full right ascension coverage, through a set of 24 h constant declination scans. In 2016 autumn, we carried out three mini-surveys, observing declination ranges around the Cygnus A and Cassiopeia A bright radio sources with the FFT firmware. Details can be found in Table 2 and a more in-depth analysis can be found in Huang (2019). As mentioned above, observations from the beginning of 2017 until mid-2018 were motivated by the necessity to identify the source of perturbations. We started the first extended PAON4 survey in 2018 July, covering about 20 degrees in declination, between the declinations of Cas A and Cyg A. More than 40 24 h constant declination scans with 0.5 degree step were done from 2018 July-December. The observations were split into two interleaved independent sets, labelled Scan_2018_A and Scan_2018_B. In each set, scans are separated by 1 degree step and the scans in B are shifted by 0.5 degrees with respect to the corresponding A scan. The scan pattern for Scan_2018 (A & B) datasets is shown in Fig. 7. A number of additional problems have been identified by analysis of the Scan_2018 data, in particular imperfect packet synchronization by the ADC boards in some cases. The 2019 observation strategy was then targeted to further investigate these problems and to precisely characterize the instrument (pointing, lobe, etc.) through long-duration (LD) uninterrupted observations over several days. Table 2 summarizes the characteristics of the different PAON4

5 DATA PROCESSING

The data processing pipeline is composed of a set of C++ programs and PYTHON scripts that perform the tasks listed below. The visibility files are the input of the processing pipeline. They contain $N_{\rm vis} \times N_{\rm freq}$ matrices, one matrix per visibility sampling time, where $N_{\rm vis}$ is the number of visibilities, and $N_{\rm freq}$ the number of frequency channels, which are respectively $N_{\rm vis} = 36$ and $N_{\rm freq} = 4096$ for PAON4. Most of the data analysed here have a visibility sampling rate of 3 or 6 s. The pipeline includes the following components:

- (i) data-quality monitoring and noise characterization;
- (ii) determination and correction for time-dependent electronic gain variations G(t) as well as frequency-dependent gain g(v);
- (iii) production of time-frequency binned (TFM) or right ascension-frequency binned (RAFM) maps for the different visibilities;

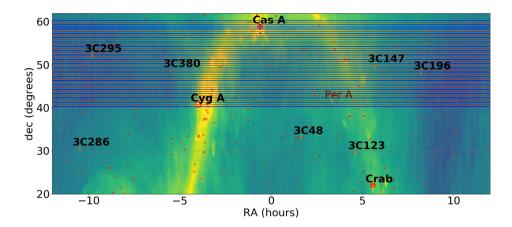


Figure 7. PAON4 acquisitions in 2018 summer and autumn, in the (RA, Dec.) sphere with equatorial projection. Each acquisition is represented by a horizontal line, blue or red for the two halves (see text). The position of bright sources from NVSS (with the addition of Perseus A) is shown by open circles. The diameter of the circle represents the source brightness. The underlying image is a projection of the Haslam 408 MHz synchrotron map, prior to source subtraction, as retrieved from the LAMBDA archive.

- (iv) phase and gain calibration using known sky sources, and determination of instrument parameters such as system temperature $T_{\rm sys}$ and beam response;
 - (v) RFI flagging and cleaning, mostly performed on TFM maps;
- (vi) production of fully cleaned and calibrated time-frequency binned (TFM) or right ascension-frequency binned (RAFM) maps for the different visibilities, which are then used by the subsequent analysis stages, in particular by the map making;
- (vii) map making through different methods, including *m*-mode decomposition (see e.g. Zhang et al. 2016b).

The mathematical formalism for radio interferometer measurement equations and the calibration methods have been studied by many authors, including polarimetry issues (e.g. Hamaker, Bregman & Sault 1996; Sault, Hamaker & Bregman 1996; Smirnov 2011). The numerical optimization problem has also been studied (e.g. Salvini & Wijnholds 2014; Smirnov & Tasse 2015) as well as their application to the calibration of large arrays such as LOFAR, MWA or HERA (Kazemi et al. 2011; van Weeren et al. 2016; Byrne et al. 2019). However, specificities of mid-frequency arrays operating in transit mode have not yet been fully investigated.

In this paper, we focus on the first four stages of the pipeline, listed above. The discussion of subsequent stages and the maps produced from PAON4 observations is beyond the scope of this paper, and will be the subject of forthcoming publications.

Typical time-frequency maps (TFM) spanning 24 h, obtained after a basic processing of PAON4 visibility data, are shown in Fig. 8. These maps were obtained from data taken on 2018 October 13, with antennas pointed toward the Cyg A declination at $\delta = 42^{\circ}$. The left-hand panel shows the autocorrelation signal from the 1Hchannel. The strong pollution of the lower part of the frequency band, below ~1300 MHz by RFI, mostly from satellites, is clearly visible. The transit of bright sources, here Cyg A and the galactic plane, can be seen on the autocorrelation map. The galactic 21 cm emission around 1420 MHz is also visible, with the zoom around this frequency in the lower panel showing the galactic frequencydependent emission pattern. The right-hand panel shows the crosscorrelation signal from the $(1H \times 3H)$ feed pair. In addition to gain correction, an average frequency template corresponding to the correlated noise has been subtracted from the cross-correlation time-frequency map. The transit of the bright source is clearly

visible with high signal to noise. Satellites are also visible in the lower frequency range.

5.1 External perturbations

Before 2018 July, PAON4 data were perturbed by a persistent artefact. Finding its origin occupied a major fraction of PAON4 observing time in 2017 as well as during the first semester of 2018. Sudden changes in the signal level were observed on a few of the PAON4 signals. Fig. 9 shows the variations of signal levels at four frequencies, for the 3H signal on the left, with normal behaviour, and the 4H signal on the right, exhibiting sudden level changes or jumps, at all four frequencies. On the normal 3H autocorrelation signal, one may observe a slowly varying trend, which is due to temperatureinduced gain variations, following day-night temperature changes. The transit of Cygnus A, at about 36 h (i.e. 12:00 UT), is visible at all frequencies except at 1420.44 MHz where 21 cm galactic emission dominates. In contrast with this normal behaviour, the perturbed 4H signal exhibits erratic variations, starting from a sharp rise at about 17 h and ending after a sharp fall at about 32 h (8:00 UT next day), with several intermediate positive or negative steps, at all frequencies. These perturbations were already seen on early PAON4 data, in 2015, but were more frequent during 2017-2018. Investigating this effect during that year, we noted that:

- (i) the perturbation occurrence rate was \sim 80 per cent (i.e. 8 d out of 10);
 - (ii) only one antenna was affected at a time;
- (iii) the most affected antenna was antenna 4, with a rate of about 80 per cent. However, in 2015, whenever the effect was observed it affected only antenna 3;
- (iv) in the rare occurrences where one of the another antennas was affected, both polarizations were affected by similar (but not identical) perturbations, in exactly the same time interval. In the case of antenna 4, one of the two polarization probes on the feed, the 4V channel, was terminated from mid-2016 to mid-2018 by a 50 Ω resistor connected to the LNA input. No significant perturbation was ever observed on this terminated channel.

This last fact, combined with other checks through electronic modules and cable permutations, showed that the perturbation had an external origin. Accumulating more data during the year brought

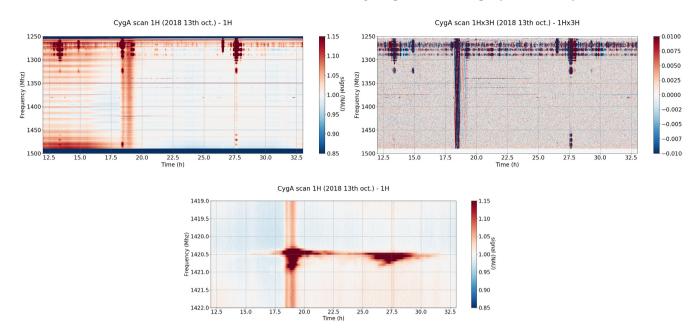


Figure 8. Top row: Examples of time–frequency maps in normalized units (NAU) obtained from processing PAON4 visibility data (after gain correction). Time (UT) is along the horizontal axis, spanning about 24 h, starting from 00:00 UT on the starting day (October 13 in this example). The vertical axis corresponds to frequency, varying from 1250 MHz to 1500 MHz, from top to bottom. The autocorrelation signal 1H is shown on the left, while the cross-correlation signal $1H \times 3H$ is shown on the right. The transit of Cyg A can be seen at about 18:30 UT followed by bright galactic emission. Several satellite transits are also clearly visible, including one just before the Cyg A transit. Residual RFI and time variation of the stationary wave pattern in g(v) before Cyg A transit in the autocorrelation map are also visible. Bottom row: zoom of the autocorrelation of the 1H channel arround the 21 cm frequency.

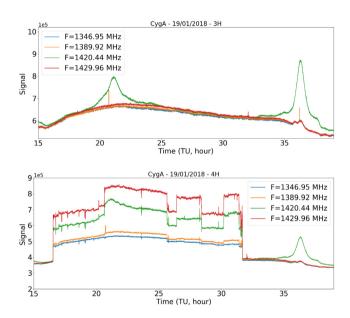


Figure 9. Example of variations of autocorrelation levels as a function of time measured on PAON4 for two channels (top: 3*H*, bottom: 4*H*) on 2018 January 19 at four frequencies (blue: 1347 MHz, orange: 1390 MHz, green: 1420.5 MHz, red: 1430 MHz) over a duration of about 24 h. Antennas were set at the elevation of the transit of Cygnus A. During this observation, channel 4*H* was perturbed.

another intriguing piece of evidence, displayed in Fig. 10. The start and end times of the perturbation seemed to correlate quite well with the hour of the dawn and sunset in Nançay, although with some dispersion. After a long investigation campaign, in 2018 May we finally spotted a small bird spending its nights in the shielded

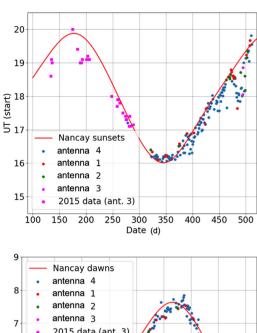
environment of the chokes surrounding our feed. We concluded that the thermal radiation produced by the bird was the source of an additional signal during the night. We placed anti-bird nets around the chokes at the end of 2018 May, which solved the problem.

5.2 Spectral response and time-dependent gain

The PAON4 channel response varies both with time and frequency. We use in our analysis a simplified gain correction model by considering these two effects independently of each other, giving $G(t, v) = G(t) \times g(v)$.

As a result of the combination of the various stages of frequency filtering, and signal transmission cables, the frequency response is complex (Fig. 11). The gain g(v) shape is primarily determined by the LNA and pre-amplifier spectral response, but in the current design of the DAQ, the 50 m coax cables between the central dish and the digitization boards located in the EMBRACE container are responsible for the dramatic gain decrease above 1300 MHz. For each channel, the gain also shows wiggles that are attributed to standing waves in the 9 m cable between the LNA and the preamplifier and the 10 m cables between the pre-amplifier and the local oscillator electronics. The characteristics of these standing waves are time variable. The peak-to-peak wave separation, of the order of 12.5 MHz, is inversely proportional to the cable length, which motivated the shortening of cables as much as possible. The R&D programme began at this time with the aim of performing the analogue to digital conversion as close as possible to the LNA on the feed. This R&D programme will result in the installation of new electronic boards called IDROGEN (see Section 7).

As mentioned above in Section 5.1, and shown in Fig. 9 (top panel), the raw PAON4 autocorrelation signals in each channel show a systematic drift in time with a day–night pattern. This is caused by the gain variations due to ambient temperature variations experi-



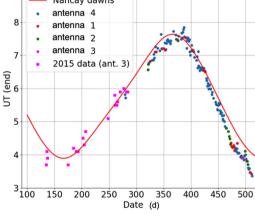


Figure 10. Variation of the start time (top) and end time (bottom) of the perturbation with date. The abscissa shows the date, reported as a number of days since January 1, and the ordinate corresponds to the time in hours. The colour of the symbols corresponds to the antenna that was perturbed at each date. Early PAON4 data, in 2015 April–May, when only antenna 3 was perturbed, are shown as squares.

enced by the analogue electronics chain. The analogue electronics are located outside without any environmental control system. The temperature stability of the PAON4 electronics chain was measured in the lab. There is $4\,\mathrm{dB}$ ($\sim\!60\,\mathrm{per}$ cent) gain variation for temperature varying between 0 and 55°C. In the PAON4 setup, a 15°C range is expected and, with the sunshine effect, the daily amplitude of the temperature variation could easily reach and exceed 30°C, leading to $\sim\!30\,\mathrm{per}$ cent gain variations. The analogue electronics were not designed to be deployed without a temperature-controlled environment and this is an issue that will be improved in the next-generation electronics design (see Section 7).

Using data taken in 2017 and 2018 with the resistor terminated 4V channel, we demonstrated that the time variation of the signal of each channel, outside bright sky source transit times, was tightly correlated with the terminated channel. A gain variation model based on this correlation was then created and the terminated channel signal used to compute and correct for the time varying gain term $G_i(t)$ of all other channels. The effect of gain variations decreased from \sim 25–30 per cent to \pm 3–5 per cent using this simple scheme. The 4V channel was reconnected in 2018 July, and an additional resistor terminated channel, THERMON, was added to PAON4. This is now used to correct for gain variations. The gain-

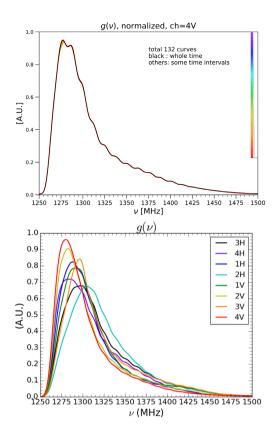


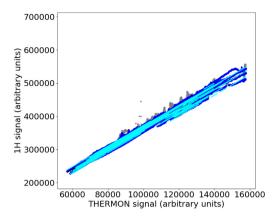
Figure 11. Frequency-dependent gain determination from 2016 November data. Top: Stability of the frequency-dependent gain $g(\nu)$ over time. The 4V channel gain is shown, with the total time interval split into 131 intervals. The black curve shows the $g(\nu)$ for the whole period, while gains for the 131 intervals are shown in different colours. Bottom: The normalized frequency-dependent gains $g(\nu)$ for the eight PAON4 RF signals.

corrected visibilities are expressed in NAU (normalized arbitrary units), with autocorrelation levels close to unity outside bright sources or sky transits.

We determined for each channel the parameter of a linear correlation with the median of the signal (after satellite and source removal) and the THERMON signal (in the same time frame). We show in Fig. 12 examples of this reconstruction for the 1H channel when analysing data from the Scan_2018 A and B parts simultaneously. A unique slope was fitted with different intercepts for each observation run. Once correcting for the linear variations, outlined in cyan, the signal variation amplitudes are reduced from \sim 25-30 per cent to $\pm 3-5$ per cent. The THERMON and the antenna channels are both correlated with a direct temperature measurement. This correlation has a large dispersion and shows hysteresis as a result of the different mechanical structures and the positioning of the temperature sensor (on top of the EMBRACE hut). Fig. 12 shows that the THERMON signal provides a better template for correcting the temperatureinduced signal variations than a direct temperature measurement. Evidence of a residual hysteresis may be seen in the bottom panel, which could be explained by the thermo-mechanical differences between the LNAs on the feeds and the lighter THERMON set-up, leading to faster temperature variations for the latter.

5.3 On-sky calibration

Point sources on-sky are used to determine the instrumental phases, as well as the antenna beam and overall radiometric calibration.



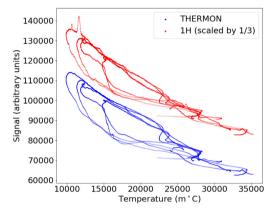


Figure 12. Top: Time-dependent gain G(t) correction, for channels 1H, for good data from Scan_2018 A and B. Grey dots are excluded from the fits (due to source transit, satellites or RFI). Only the blue ones are used. The thin cyan lines represent the results of the global fit, with one slope for all datasets and one intercept for each of the observation runs. Bottom: Variations of the THERMON and 1H channels as a function of the measured ambient temperature over a few days in 2018 July.

The PAON4 survey strategy includes regular observation of bright sky sources, such as Cassiopeia A (Cas A) and Cygnus A (Cyg A), every few days to obtain gain and phase calibration parameters that are then used for the subsequent scans and to update the instrument model.

The primary calibration source is Cas A, which can be considered a point source for PAON4. A simple model is used to represent expected autocorrelation and cross-correlation signals from Cas A, and we fit instrumental phases and amplitudes as well as beam shape parameters. Also fitted is the effect on the auto- and crosspolarizations for H and V due to changing the pointing direction along the east-west direction. For each polarization, H or V, independently from each other, the parameters are adjusted on the set of four autocorrelations and six cross-correlations signals, for each binned frequency channel. The cross-correlations between two orthogonal probes $H \times V$ are not included, ignoring source polarization. After fitting the autocorrelations that notably fix the beam shape parameters, the six cross-correlations signals are used to determine relative phases between the feed on antenna 1 taken as reference and the three other feeds (i.e. $\Delta \Phi_i = \Phi_i - \Phi_1$ with i = 2, 3, 4). There are degeneracies between the instrumental phases and the relative phases induced by the array geometry, which is fixed at this stage. We have refined the PAON4 antenna positions, determined

from geometrical measurements during PAON4 deployment, using the satellite transits as described below.

The lower part of the PAON4 band below 1300 MHz is heavily polluted by satellite emissions and is dominated by positioning satellites from the GPS (USA), Galileo (EU) and Beidou (China) constellations. In particular, PAON4 sees a strong signal from the Galileo E6 band, centred at 1278.75 MHz, as well as from Beidou in the same band. Although GPS does not have direct emission in the PAON4 band (1250-1500 MHz), we do see the GPS L2 signal centred around 1227 MHz, at a symmetric frequency of \sim 1273 MHz, with respect to the LO frequency at 1250 MHz. These satellite signals are used for determining PAON4 geometry, beam shape and instrumental phases. Several satellite tracks are usually present in our daily (24 h) observations. We developed an additional software module included in our pipeline, which uses satellite tracks computed using the SGP45 library from NORAD6 TLEs (two-line elements) available from CELESTrak,7 as well as tracks of celestial objects at different frequencies, separately for each polarization. The module performs the following operations:

- (i) determination of the pointing directions, as well as parametrized beam shape for each PAON4 antenna, using autocorrelation signals and the satellite tracks. It should be noted that the satellite signals are very strong. Galileo satellites are a few hundred times brighter than Cas A;
- (ii) using the parameters determined above, the phases are determined for each baseline separately. It is also possible to determine the phases from a combined fit over the six baselines and multiple frequencies using a linear frequency-dependent phase model $\Phi_{ii}(\nu)$;
- (iii) the derived instrumental phase variations as a function of pointing directions are used to refine PAON4 antenna positions along the vertical direction (Oz) and the north–south direction, as discussed in Section 6. The positions along the east–west direction changes the fringe rate and a combined fit, using visibility data from different declinations and many sources, is used to obtain precise array geometry;
- (iv) among the fitted parameters are the source amplitudes. The source amplitudes for Cas A and Cyg A are used to determine PAON4 radiometric calibration factors (K $\rm NAU^{-1}$), to convert gain-corrected visibilities to temperature. Instrument gain stability is also discussed in Section 6.

6 INSTRUMENT PERFORMANCE

The analysis presented here is based on data taken in 2016 autumn, 2018 autumn, and 2019 winter and spring. The precision of calibration parameters, stability, and overall instrument performance are discussed here.

6.1 System temperature and radiometric calibration stability

The transit of Cas A, Cyg A and satellites is used to determine the antenna temperature of the eight polarizations (H and V for each antenna). Two procedures are used. The first one, (a), uses satellite tracks and Cas A and Cyg A transits and is applied to data from the 2019 long-duration (LD) observations. The dish diameter in this procedure is determined from the autocorrelation signals using satellite transits, while the bright source maximum amplitude N_{ij} is

⁵https://www.danrw.com/sgp4/

⁶https://www.norad.mil

⁷http://www.celestrak.com/NORAD/elements

Table 3. System temperature determined for each of the eight polarizations using two different procedures (a) and (b) described in the text.

Polar.	T_a^{CasA} (K)	$T_a^{\text{CygA}}(K)$ (a)	T_a^{CasA} (K)
1 <i>H</i>	116	147	144
2H	127	129	133
3H	130	122	138
4H	161	152	185
1V	113	100	103
2V	108	92	100
3V	103	111	98
4V	143	151	180

obtained by fitting the cross-correlation signal between two signals of the same polarization (i.e. H–H or V–V cross-correlation only). In the second procedure, (b), the autocorrelation signals during the Cas A transit are used to derive the maximum signal amplitude N_i and the effective dish diameter D_i for a given dish and polarization. This second procedure is applied to the Cas A transits during the Scan2018 (A,B) periods (Table 2). A Gaussian beam approximation is used in the procedures. Time–frequency maps produced after the gain $g(v) \times G(t)$ correction lead to gain-corrected autocorrelation signal levels very close to 1 NAU, except during source or satellite transits.

The fit coefficients are converted into radiometric calibration coefficients $C^{\rm Jy}$ in units of Jy NAU⁻¹ and $C^{\rm K}$ in units of K NAU⁻¹. This is done using the Cas A and Cyg A spectral flux reported in Perley & Butler (2017). Cas A has an intensity of $I_{\rm s}=1730$ Jy and $I_{\rm s}=1772$ Jy at 1440 MHz and 1396 MHz respectively. Cyg A has an intensity of $I_{\rm s}=1585$ Jy at 1396 MHz. The radiometric calibration coefficient $C^{\rm K}$ in normalized units (NAU) is related to temperature in kelvin using the source intensity $I_{\rm s}$ according to

$$C_i^{\text{K}} = \frac{I_s}{2N_i} \frac{\pi}{4k_{\text{B}}} D_i^2 \quad \text{K NAU}^{-1}.$$
 (1)

With no strong sources in the field, signal levels are around 1 NAU. The value of the calibration coefficient is then equal to the system temperature $T_{\rm sys}$ reported in Table 3. We have used two procedures applied to different datasets to determine effective dish diameters and radiometric calibration.

Procedure (a) operates at 1396 MHz to determine the system temperature. It uses the satellite tracks at 1278.75 MHz to fit the effective dish diameters and pointing parameters with the assumption that they do not vary too much over the bandwidth. The radiometric calibration is then determined from fitting the 12 cross-correlation maximum intensities during bright source transits. This procedure is applied to Cas A and Cyg A transits separately, during a single, albeit long, period of observation.

Procedure (b) is applied independently to visibilities at different frequencies, with results at 1440 MHz reported in Table 3. It fits at the same time the maximum intensity, the effective diameter and the azimuth misalignment of the dishes using the eight autocorrelations during the eight Cas A transits, with observations scattered over several months. With method (b) we note that the effective diameter exhibits sinusoidal variations around $D \sim 4.5$ m as a function of frequency due to standing waves between the reflector and the feed. These variations represent a 180° phase shift between the H and V polarizations.

Table 3 summarizes the different values of the antenna temperatures. We estimate a relative uncertainty of 10 per cent mainly due to the maximum intensity and the effective diameter errors. The stability level is better than 10 per cent based on measurements performed over several months.

The results show a tendency for dish number 4 to be noisier, which may be due to the fact that this dish is the closest to the surrounding trees. The H-polarization feeds are about 20 per cent noisier than the V-polarization feeds (H: $T_{\rm sys} \sim 130~{\rm K}$, V: $T_{\rm sys} \sim 110~{\rm K}$). The origin of this difference between the H and V feeds is not yet understood.

The total noise temperature is \sim 120 K. Electronic noise contributes \sim 60–70 K (see Section 3.1). Inefficiency of the mesh reflector adds noise since it permits some ground thermal emission through. Further studies will be done to clarify the source of the additional noise contributions.

6.2 Noise characterization

Given the $\sim \! 10^5$ ratio between the noise level and the expected cosmological 21 cm signal, which is essentially stochastic, characterizing the noise and the way fluctuations decrease with integration time is a central question for IM instruments. Interferometry has the intrinsic advantage of being rather immune to variations of individual receiver noise levels. However, correlated noise would limit the theoretical sensitivity expected from a combination of visibility signals with long integration time. Moreover, interferometric arrays designed for IM surveys are closely packed, which increases the concern for the correlated noise between receivers due to electromagnetic coupling between feeds. We have studied the noise behaviour of our complete electronic chain, including the digitizer boards in the laboratory, and identified some coupling sources responsible for correlated noise, such as the coupling through the power supplies.

For more than a year up to 2018 July, data were taken with a terminated 4V signal, where the input of the amplifier on the 4V feed was connected to a 50 Ω resistor (see Section 5). These data were used to help identify the sources of various perturbations, including the one subsequently identified as being due to a bird. They were also used to study the correlated noise, comparing visibilities involving the 4V signal with other signal pairs.

Our conclusions, from a preliminary study of the correlated noise, are summarized below.

We analysed data from the 2018 January observations and computed time–frequency maps with $\delta\nu\simeq 500\,\mathrm{kHz}$ frequency resolution and 12 min time bins, corresponding to an effective per pixel integration time of $\Delta t\sim 50~\mathrm{s}$. Dispersions on the visibility signals (real/imaginary parts) were then computed over clean sections of the TFM maps, covering $\sim\!6$ h in time and $\sim\!35~\mathrm{MHz}$, excluding bright regions of the sky. A noise reduction factor $\sqrt{\Delta t\times\delta\nu}\sim 5000$ is expected. The r.m.s. (σ) values quoted below assume that the signals have been normalized to get autocorrelation levels equal to unity (for fields without bright sources).

- (i) The noise levels observed for signal pairs involving the terminated 4V signal (1V–4V, 1H–4V, etc.) are compatible with the levels expected given the integration time and frequency bandwidth, leading to $\sigma_{\rm re,\,im}\sim 2\times 10^{-4}$. The correlated noise contribution can be considered negligible, at least for the integration times of the current analysis.
- (ii) For the same polarization signal pairs between two different dishes, such as (1H-3H) or (1V-3V), the observed noise level

is higher compared to the expected level, assuming Gaussian uncorrelated noise. We measure dispersions up to four–five times higher, $\sigma_{\rm re.\,im} \sim 8 \times 10^{-4}$.

(iii) For two cross-polarization probes located in the same feed/dish such as (1H-1V) or (3H-3V), the dispersion level increases to more than $\sigma_{\rm re,\,im}\sim 2\times 10^{-3}$.

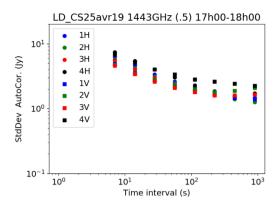
The extra noise observed on the same polarization probes in two different feeds, or two probes within the same feed, shows up as frequency-dependent patterns, quite stable in time over a few hours. This can be interpreted as noise generated in the analogue electronic chain, cross-fed through electromagnetic couplings between feeds on two different dishes, or between probes in the same feed, and then amplified in a way analogous to the Larsen effect. Fortunately, it can be efficiently subtracted due to its stability in time. Further studies are needed to determine the noise floor due to this correlated noise.

We have also analysed how the noise level decreases with integration time. Here, time–frequency maps with different effective per pixel integration times are computed, with a fixed frequency bin width $\delta \nu = 500\,\mathrm{kHz}$, from the 2019 April–May data. Maps with different averaging time window sizes, equal to (1, 2, 4, 8, 16, 32, 64, 128) in units of visibility sampling time are built and then used to compute signal dispersions (in the absence of bright source transits or RFI). Data from 2019 spring were taken with a visibility sampling time of 6 s leading to a maximum visibility averaging time of 768 s. PAON4 was operated with ~10 per cent on-sky efficiency so the maximum effective integration time is slightly above 1 min.

Fig. 13 shows the evolution of dispersion levels computed as the r.m.s. of the different time-frequency maps, excluding bright sources, satellites and RFI. The correlated noise is subtracted from the cross-correlation time-frequency maps, using the frequency template obtained by the time-averaged signal, computed separately for each cross-correlation. The top panel shows the evolution of the dispersion with the integration time, for the eight PAON4 autocorrelation signals. The r.m.s. decreases with integration time, following a $1/\sqrt{\Delta t}$ trend. A noise floor or saturation starts to appear at long integration times, more or less strongly dependent on the dataset and the autocorrelation signal. However, it should be kept in mind that the r.m.s. of the autocorrelation signals is sensitive to gain variations with time, as well to the variation of the diffuse sky brightness. The presence of this apparent noise floor for the autocorrelation signals does not imply that the underlying noise is not white. The bottom panel shows the evolution of the r.m.s. values computed on the cross-correlation visibilities (real part) for the 12 H-H and V-V correlations. Here, the r.m.s. values are compatible with the expected levels, and decrease with integration time following the expected white noise law $1/\sqrt{\Delta t}$, without significant contribution from correlated noise, once the average level at each frequency has been subtracted.

6.3 Phase calibration and array geometry

As mentioned in Section 5.3, Galileo satellites are used to perform phase calibration and determine instrumental phases for a large fraction of PAON4 observations carried out in 2018 autumn, 2019 winter and spring. Instrumental phase values are determined for each constant declination scan. Fig. 14 shows the antenna-2 phase $\Delta\Phi_2 = \Phi_{12} = \Phi_2 - \Phi_1$ values, determined at 1278.5 MHz for 17 scans and the *H*-polarization feeds, as a function of the common nominal antenna direction in the meridian plane, referred to as the zenith angle ($Z = 90^{\circ}$ – elevation). This angle corresponds



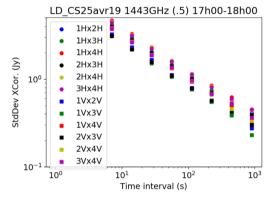


Figure 13. Evolution of noise level with integration time. Top: Dispersion level for the eight PAON4 autocorrelation signals as a function of the integration time. Bottom: Dispersion level for the real parts of the six H-H and six V-V cross-correlation signals as a function of integration time in seconds.

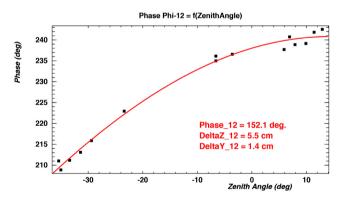


Figure 14. Phase calibration and array geometry corrections. Instrumental phase values Φ_{12} determined for different scans, plotted as a function of the zenith angle (black squares). The red line represents a model fit, including corrections to the baseline and the residuals are within $\pm 2^{\circ}$.

to the angle between the antenna axis and the local vertical, or the difference between the observed declination and the instrument latitude. Negative zenith angles correspond to the antenna being tilted toward the south. One can see that the phase Φ_{12} varies over more than 30°, with a smooth variation as a function of the zenith angle. The variation is well explained by a shift in theoretical antenna position, along the north–south Oy and vertical Oz directions. The best-fitting model, taking into account the baseline shift, is shown by the red curve. The fitting result shows that the two feed heights differ by about \sim 55 mm for this (1H-2H)

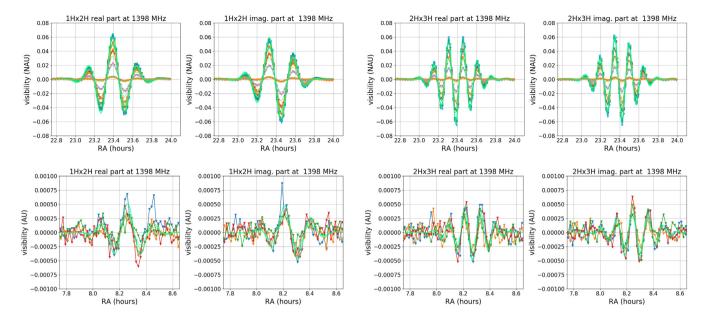


Figure 15. Comparisons of observed and expected (with a simplified model, see text) visibility variations with right ascension for scans near Cas A (top) and 3C 196 (bottom) declinations, from the Scan_2018 A and B data, for the 1*H*–2*H* (left) and 2*H*–3*H* (right) cross-correlations. Each colour corresponds to a different date, and the expected visibilities are shown in cyan.

baseline, while the north–south component of this baseline should be corrected by \sim 14 mm. Using the six baselines, we determined the corrections to the array geometry, using the zenith dependence of the instrumental phases. We obtain a precision of \sim 2 mm using these 17 scans. A shift in the east–west baseline component would not show as a zenith angle phase dependence, but rather as a change in the fringe rate. We have not yet determined baseline corrections along the east–west Ox direction using the fringe rates, but higher precision is expected for the determination of the east–west baseline corrections. The instrumental phases do not change by more than \pm 2 $^{\circ}$ despite the fact that the observations were done over a period spanning more than eight months. Similar phase stability is observed for the other baselines.

6.4 Comparison of observed and expected signals

Fig. 15 shows a comparison of observed and expected visibilities for a few scans close to two bright sky sources, Cas A (~1700 Jy) and 3C 196 (\sim 15 Jy) for the cross-correlation of two pairs of feeds, 1H– 2H and 2H–3H. We gathered data from scans at several declinations around the source, represented by different colours. The visibility amplitude decreases for scans at more distant declinations with respect to the source declination. This effect is clearly visible for Cas A, but also for 3C 196. The expected signal was rescaled using a single conversion coefficient per feed, used for both sources, computed by adjusting the amplitudes of the expected Cas A on-source scan of 2018 July 17. This simplified computation of expected signals does not take into account pointing uncertainties, whereas a $\sim 0.5 \, \text{deg}$ shift is suggested by our satellite fits. Nor does it take into account the non-Gaussian secondary lobes in the beam pattern. The full signal level for Cas A is expected to be about $\sim 6000 \,\mathrm{mK}$, and $\sim 60 \,\mathrm{mK}$ for 3C 196, while the noise level is about ~20 mK given the time and frequency binning used here.

Fig. 16 shows a region of the reconstructed map at 1400 MHz using PAON4 observations from 2016 November 16–December 1.

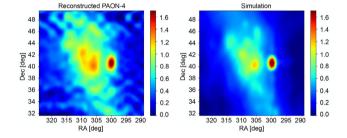


Figure 16. Example of a reconstructed map in a $\sim 35 \times 18^\circ$ region around Cyg A, covering the area $(32^\circ < \delta < 50^\circ)$ in declination and $(290^\circ < \alpha < 325^\circ)$ in right ascension, from 2016 November data (left). The right-hand panel shows the simulated map. (Huang 2019).

A map making applying the *m*-mode decomposition in harmonic space from the transit visibility code is used (Huang 2019). A sky map covering the full 24 h right ascension, and the declination range $35^{\circ} \lesssim \delta \lesssim 46^{\circ}$ is computed from 11 24 h constant declination scans around the Cyg A declination. The extracted map covers $\sim\!18^{\circ}$ in declination (32° $<\delta<50^{\circ}$) and $\sim\!35^{\circ}$ in right ascension (290° $<\alpha<325^{\circ}$) around the nearby radio galaxy Cyg A. The emission from Cyg A and the Milky Way synchrotron emission, as well as from the Cygnus X star-forming region, is clearly visible.

7 FUTURE PROSPECTS

Time-variable systematics in the frequency response led us to develop a new generation of sampling and signal processing board, IDROGEN/NEBuLA, to perform digitization as close to the feeds as possible (see Section 5.2). The IDROGEN board is designed to equip interferometers with several hundred feeds, scattered over a few hundred metres. Clock synchronization is managed by the implementation of the White Rabbit⁸ technol-

⁸https://white-rabbit.web.cern.ch

ogy. A first version of this new board, called NEBuLA (*NumEriseur a Bande Large pour l'Astronomie*) was designed and produced in 2016–2017. The second version, called IDROGEN, is developed as part of the CNRS/IN2P3 DAQGEN project. This project began in 2017 with the goal of developing generic modules for rapid acquisition systems for particle and astroparticle projects.

IDROGEN boards will be located in the electronic boxes on each antenna, sampling the RF signals, relieving the need for frequency shifting and transmitting the digital streams over optical fibres all the way to the computer cluster a few hundred metres away. The deployment of IDROGEN boards on PAON4 is foreseen in 2020 spring, after more in-depth characterization of PAON4 in its present configuration. A reduction of the amplitude of the temperature-dependent gain variations is also expected because the analogue chain is simplified and does not have the down-conversion stage. It has also improved passive cooling.

Upgrades of the acquisition system hardware and software are also planned with the deployment of IDROGEN boards and should enable PAON4 to reach ~25 per cent to 30 per cent on-sky time, which is a significant improvement compared to the current performance of ≤10 per cent (see Section 3). In particular, GPU support will be added to the TACQ package for the correlation computing software processor and also to the FFT processor to increase the system throughput. First tests will be performed in the current operation mode of PAON4. At a later stage, the new digitizer boards will be operated and qualified in the FFT mode. After those tests, we expect to release a stable version of the TACQ software, with full support for IDROGEN boards.

8 CONCLUSIONS

A densely packed dish array interferometer is a cost-effective option to build radio instruments to survey large sky areas in the L band. We have built and operated the PAON4 dish array transit interferometer under very tight budget constraints. Preliminary results indicate that this type of instrument together with its associated observing strategy are effective both in terms of scientific analysis and cost effectiveness. The study presented here will progress further to longer integration times in order to demonstrate that the expected sensitivities at the few mK level can be achieved. In-depth studies with more data and PAON4 maps will be published in the coming year. PAON4 does not have redundant baselines, and the additional possibilities offered by the combination of nearly identical baselines will be explored with larger instruments. Such studies are being pursued in parallel with the Tianlai dish array. The next-generation IDROGEN digitizer/signal processor boards are in the final stage of development and will be suited for a dish interferometer consisting of a few hundred feeds and ~km baselines. IDROGEN will be deployed for qualification on PAON4 in 2020 and we plan to carry out a higher-sensitivity survey in the declination range 30-60° in 2021. The resulting 3D maps will be useful to characterize the spectral behaviour of the galactic foregrounds, including a determination of its smoothness on the few MHz scale.

ACKNOWLEDGEMENTS

The deployment of PAON4 and observations at Nançay would not have been possible without the help and support of the technical staff of the Nançay Radio Observatory, which is the Unité scientifique de Nançay (USN) of the Observatoire de Paris, associated as Unité de

Service et de Recherche (USR704) to the French Centre National de la Recherche Scientifique (CNRS). The Nançay Observatory also gratefully acknowledges the financial support of the Conseil régional of the Région Centre in France. We acknowledge financial support from 'Programme National de Cosmologie and Galaxies' (PNCG) of CNRS/INSU, France.

REFERENCES

Abbott T. M. C. et al., 2018, MNRAS, 480, 3879

Abdalla F. B., Rawlings S., 2005, MNRAS, 360, 27

Amendola L., Kunz M., Motta M., Saltas I. D., Sawicki I., 2013, Phys. Rev. D, 87, 023501

Ansari R., Le Goff J., Magneville C., Moniez M., Palanque-Delabrouille N., Rich J., Ruhlmann-Kleider V., Yèche C., 2008, preprint (arXiv: 0807.3614)

Ansari R., Campagne J.-E., Colom P., Magneville C., Martin J.-M., Moniez M., Rich J., Yèche C., 2012a, Comptes Rendus Phys., 13, 46

Ansari R. et al., 2012b, A&A, 540, A129

Ansari R., Campagne J. E., Colom P., Ferrari C., Magneville C., Martin J. M., Moniez M., Torrentó A. S., 2016, Exp. Astron., 41, 117

Armstrong R., Hickish J., Zarb Adami K., Jones M. E., 2009, Proc. Sci., A Digital Broadband Beamforming Architecture for 2-PAD. SISSA, Trieste, PoS#45

Bandura K., 2011, PhD thesis. Carnegie Mellon Univ.

Bandura K. et al., 2014, in Larry M. S., Roberto G., Helen J. H., eds, Proc. SPIE Conf. Ser. Vol. 9145, Ground-based and Airborne Telescopes V. SPIE, Bellingham, p. 914522

Bandura K. et al., 2019, BAAS, 51, 53

Battye R. A., Browne I. W. A., Dickinson C., Heron G., Maffei B., Pourtsidou A., 2013, MNRAS, 434, 1239

Betoule M. et al., 2014, A&A, 568, A22

Bigot-Sazy M. A. et al., 2015, MNRAS, 454, 3240

Bigot-Sazy M.-A. et al., 2016, in Qain L., Li D., eds, ASP Conf. Ser. Vol. 502, Frontiers in Radio Astronomy and FAST Early Sciences Symposium 2015. Astron. Soc. Pac., San Francisco, p. 41

Braun R., Bourke T., Green J. A., Keane E., Wagg J., 2015, Proc. Sci., Advancing Astrophysics with the Square Kilometre Array. SISSA, Trieste, PoS#174

Bull P., Camera S., Raccanelli A., Blake C., Ferreira P., Santos M., Schwarz D. J., 2015a, Proc. Sci., Measuring baryon acoustic oscillations with future SKA surveys. SISSA, Trieste, PoS#24

Bull P., Ferreira P. G., Patel P., Santos M. G., 2015b, ApJ, 803, 21

Bull P. et al., 2016, Phys. Dark Univ., 12, 56

Byrne R. et al., 2019, ApJ, 875, 70

Chang T.-C., GBT-HIM Team, 2016, American Astronomical Society Meeting Abstracts #227. p. 426.01

Chang T.-C., Pen U.-L., Peterson J. B., McDonald P., 2008, Phys. Rev. Lett., 100, 091303

Chang T.-C., Pen U.-L., Bandura K., Peterson J. B., 2010, Nature, 466, 463 Charlet D. et al., 2011, IEEE Trans. Nuclear Sci., 58, 1833

Chatterjee S. et al., 2017, Nature, 541, 58

Chen X., 2012, Int. J. Modern Phys. Conf. Series, 12, 256

Cosmic Visions 21 cm Collaboration et al., 2018, preprint (arXiv:1810.095 72)

Das S. et al., 2018, in Zmuidzinas J., Gao J.-R., eds, Proc. SPIE Conf. Ser. Vol. 10708, Millimeter, Submillimeter, and Far-Infrared Detectors and Instrumentation for Astronomy IX. SPIE, Bellingham, p. 1070836

DES Collaboration, 2018, Phys. Rev. Lett., 122, 171301

Deschamps H. et al., 2013, IEEE Trans. Nuclear Sci., 60, 3620

Furlanetto S. R., Oh S. P., Briggs F. H., 2006, Phys. Rep., 433, 181

Hamaker J. P., Bregman J. D., Sault R. J., 1996, A&AS, 117, 137

Hinshaw G. et al., 2013, ApJS, 208, 19

Huang Q., 2019, PhD thesis. Paris-Saclay Univ. and Univ. Chinese Academy of Science

Kazemi S., Yatawatta S., Zaroubi S., Lampropoulos P., de Bruyn A. G., Koopmans L. V. E., Noordam J., 2011, MNRAS, 414, 1656

2980 R. Ansari et al.

Masui K. W. et al., 2013, ApJ, 763, L20

Newburgh L. B. et al., 2016, in Hall H. J., Gilmozzi R., Marshall H. K., eds, Proc. SPIE Conf. Ser. Vol. 9906, Ground-based and Airborne Telescopes VI. SPIE, Bellingham, p. 99065X

Parsons A. R. et al., 2010, AJ, 139, 1468

Perera B. B. P. et al., 2019, MNRAS, 490, 4666

Perley R. A., Butler B. J., 2017, ApJS, 230, 7

Peterson J. B., Bandura K., Pen U. L., 2006, preprint (arXiv:astro-ph/060 6104)

Peterson J. B. et al., 2009, Astro2010: The Astronomy and Astrophysics Decadal Survey, Science White Papers, No. 234.

Planck Collaboration, 2016, A&A, 594, A13

Planck Collaboration, 2018, preprint (arXiv:1807.06209)

Pober J. C. et al., 2014, ApJ, 782, 66

Pritchard J. R., Loeb A., 2008, Phys. Rev. D, 78, 103511

Salazar-Albornoz S. et al., 2017, MNRAS, 468, 2938

Salvini S., Wijnholds S. J., 2014, A&A, 571, A97

Sault R. J., Hamaker J. P., Bregman J. D., 1996, A&AS, 117, 149

Shaw J. R., Sigurdson K., Pen U.-L., Stebbins A., Sitwell M., 2014, ApJ, 781, 57

Shaw J. R., Sigurdson K., Sitwell M., Stebbins A., Pen U.-L., 2015, Phys. Rev. D, 91, 083514

Smirnov O. M., 2011, A&A, 527, A106

Smirnov O. M., Tasse C., 2015, MNRAS, 449, 2668

Stovall K. et al., 2014, ApJ, 791, 67

Tegmark M., Zaldarriaga M., 2009, Phys. Rev. D, 79, 083530

Thornton D. et al., 2013, Science, 341, 53

Tingay S. J. et al., 2013, Publ. Astron. Soc. Aust., 30, e007

Torchinsky S. A., Olofsson A. O. H., Censier B., Karastergiou A., Serylak M., Picard P., Renaud P., Taffoureau C., 2016, A&A, 589, A77

van Haarlem M. P. et al., 2013, A&A, 556, A2

van Weeren R. J. et al., 2016, ApJS, 223, 2

Wang X., Tegmark M., Santos M. G., Knox L., 2006, ApJ, 650, 529

Wolz L., Abdalla F. B., Blake C., Shaw J. R., Chapman E., Rawlings S., 2014, MNRAS, 441, 3271

Wuensche C. A., BINGO Collaboration, 2018, J. Phys.: Conf. Ser., 1269, 012002

Wyithe J. S. B., Loeb A., Geil P. M., 2008, MNRAS, 383, 1195

Zarka P. et al., 2015, International Conference on Antenna Theory and Techniques (ICATT). IEEE, Kharkiv, Ukraine

Zhang J., Zuo S.-F., Ansari R., Chen X., Li Y.-C., Wu F.-Q., Campagne J.-E., Magneville C., 2016a, Res. Astron. Astrophys., 16, 158

Zhang J., Ansari R., Chen X., Campagne J.-E., Magneville C., Wu F., 2016b, MNRAS, 461, 1950

This paper has been typeset from a $T_EX/I \Delta T_EX$ file prepared by the author.