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► To cite this version:

Olivier François, Séverine Liégeois, Benjamin Demaille, Flora Jay. Inference of population genetic structure from temporal samples of DNA. 2019. hal-02413974

HAL Id: hal-02413974 https://hal.science/hal-02413974v1

Preprint submitted on 16 Dec 2019

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Inference of population genetic structure from temporal samples of DNA

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1

Abstract

The recent years have seen a growing number of studies investigating evolutionary 2 questions using ancient DNA techniques and temporal samples of DNA. To address 3 these questions, one of the most frequently-used algorithm is based on principal com-4 ponent analysis (PCA). When PCA is applied to temporal samples, the sample dates 5 are, however, ignored during analysis, which could lead to some misinterpretations of 6 the results. Here we introduce a new factor analysis (FA) method for which individ-7 ual scores are corrected for the effect of allele frequency drift through time. Based 8 on a diffusion approximation, our approach approximates allele frequency drift in 9 a random mating population by a Brownian process. Exact solutions for estimates 10 of corrected factors are obtained, and a fast estimation algorithm is presented. We 11 compared data representations obtained from the FA method with PCA and with PC 12 projections in simulations of divergence and admixture scenarios. Then we applied 13 FA with correction for temporal drift to study the evolution of hepatitis C virus in 14 a patient infected by multiple strains, and to describe the population structure of 15 ancient European samples. 16

17 **1** Introduction

In recent years, the number of studies analyzing temporal samples of DNA or ancient 18 DNA has increased dramatically, both for humans and for other organisms (Lazaridis 19 et al., 2014; Haak et al., 2015; Mathieson et al., 2015; Carroll et al., 2015; Skoglund 20 and Mathieson, 2018). In such studies, a central question concerns the inference of 21 ancestral relationships between sampled populations (Slatkin, 2016). Evolutionary 22 biologists and population geneticists have devised many methods for addressing this 23 question. One of the most frequently-used method is based on principal component 24 analysis (PCA) and projections of ancient samples on axes built from present-day 25 samples (Patterson et al., 2006, 2012). In population genetics, PCA is performed 26 by finding the eigenvalues and eigenvectors, or axes, of the covariance matrix of al-27 lele frequencies. The highest order eigenvectors indicate the directions in the high 28 dimensional allele-frequency space which account for most of the covariance. Indi-29 vidual samples are then plotted on the plane spanned by the first axes, offering a 30 visual representation of the structure hidden in the data obtained with short com-31 puting time. Relative distances in the reduced space indicate their similarity and 32 their ancestral relationships (McVean, 2009). When PCA or PC projections are ap-33 plied to analyze temporal samples, information on sample dates is, however, usually 34 omitted in the computation of eigenvalues and eigenvectors (Slatkin, 2016; Slatkin 35 and Racimo, 2016; Harris and DeGiorgio, 2017). 36

Previous studies have reported that time differences in samples are reflected in the principal axes of a PCA (Skoglund *et al.*, 2014), creating sinusoidal shapes similar to those observed with geographic samples (Novembre and Stephens, 2008). The combination of both time and spatial heterogeneity in sampling further modify the patterns

observed in PCA. Local dispersal through time causes ancient samples to be shrunk 41 toward the center of the PC plot and not to cluster with their present-day counter-42 part despite no major discontinuity in the demographic process (Duforet-Frebourg 43 and Slatkin, 2016). Sinusoidal distortions linked to gradients and longitudinal data 44 also occur in various fields, and are called *horseshoes* or *arches*. Those distortions 45 complicate the interpretation of multidimensional scaling, local kernel methods and 46 ordination analysis (Hill and Gauch, 1980; Diaconis et al., 2008). Supervised methods 47 that combine ancient and modern samples by using PC projections on present-day 48 samples also suffer from some statistical issues. PC projections exhibit a shrinkage 40 bias toward the center of the principal axes, and this bias could increase in analyses 50 of temporal samples (Lee *et al.*, 2010). Since those biases could lead to misinterpre-51 tations or to incorrect estimates of individual ancestry, it is important to propose 52 methods that correct principal components when temporal samples are analyzed for 53 descriptive purposes. 54

Corrections of sinusoidal patterns arising in principal components have been pro-55 posed when distortions are caused by spatial auto-correlation in geographic samples 56 (Frichot et al., 2012). Similarly, Kalaitzis and Lawrence (2012) have proposed to 57 remove temporal correlations leaving residual variance with residual component anal-58 vsis. Modified versions of the STRUCTURE algorithm – which is closely related to 59 PCA – were also developed to integrate corrections based on spatial or temporal diffu-60 sion models (Pritchard et al., 2000; Caye et al., 2018; Joseph and Pe'er, 2018). In this 61 study, we introduce a new factor analysis (FA) method for visualizing hidden struc-62 ture and for describing ancestral relationships among samples collected at distinct 63 time points in the past. Based on a diffusion approximation, our approach approxi-

mates allele frequency drift in a random mating population by a Brownian process. 65 Using the Karhunen-Loève theorem, we propose a representation of the factor model 66 in which additional covariates, representing temporal eigenvectors, are introduced 67 in the model. Our model assumes informative Gaussian prior distributions for the 68 effect sizes of the temporal covariates. Exact solutions for time-corrected factors 69 are obtained, and a fast algorithm based on singular value decomposition (SVD) is 70 proposed. We compare corrections for temporal drift in FA with PCA in coalescent 71 and generative simulations of divergence and admixture scenarios. We eventually 72 apply corrections for temporal drift to study the evolution of hepatitis C virus in a 73 patient infected by multiple viral strains, and to describe population structure for 74 DNA samples from ancient Europeans and Eurasians. 75

76 2 New Method

This section introduces a new factor analysis method for describing ancestry among samples taken at distinct time points in the past. The objective is to propose a factorial decomposition of the data matrix similar to a PCA, in which the individual scores are corrected for the effect of allele frequency drift through time. The scores, called factors, will be obtained as maximum-a-posteriori estimates in a Bayesian model.

⁸³ Model. Let Y be an $n \times p$ matrix of genotypic data, where n is the number of ⁸⁴ individual samples and p is the number of markers, typically represented as single ⁸⁵ nucleotide polymorphisms (SNPs). We suppose that the data are centered, so that ⁸⁶ the mean value for each column (or marker) is null. We also suppose that each sample,

 i_{i} , is associated with a sampling date, t_{i} , corresponding to the age of the sample. The dates are normalized to span the unit interval $0 < t_{1} \leq \cdots \leq t_{n} \leq 1$. Here, time has a forward representation. The date t_{1} corresponds to the most ancient sample, and t = 1 represents samples at present time. Our FA model takes the following form

$$\mathbf{Y} = \mathbf{U}\mathbf{V}^T + \boldsymbol{\epsilon},\tag{1}$$

where **U** is an $n \times K$ matrix of scores, \mathbf{V}^T is a $K \times p$ matrix of loadings. The 91 number of factors, K, can be set to any number smaller that n and p depending 92 on how drastically one wants to reduce the dimension of the data (and approximate 93 the data matrix). It can be set to the number of ancestral groups minus one when 94 this information is known. The individual scores contained in the K column vectors, 95 $\mathbf{u}_1, \ldots, \mathbf{u}_K$, of the matrix U reflect the ancestral relationships among samples (Pat-96 terson et al., 2006). To incorporate corrections for temporal drift, we model the error 97 term, ϵ , as follows 98

$$\epsilon \sim \mathbf{N}(0, \alpha^{-1}\mathbf{C} + \sigma^2 \mathbf{I}), \qquad (2)$$

⁹⁹ where $\mathbf{N}(0, \alpha^{-1}\mathbf{C} + \sigma^{2}\mathbf{I})$ is the multidimensional Gaussian distribution with mean 0 and covariance matrix $\alpha^{-1}\mathbf{C} + \sigma^{2}\mathbf{I}$, α is a precision (scale) parameter for temporal drift, σ^{2} is the variance of the residual error, and \mathbf{I} is the $n \times n$ identity matrix. We suppose that \mathbf{C} is an $n \times n$ covariance matrix given by

$$c_{ij} = \min(t_i, t_j) \quad i, j = 1, \dots, n.$$
(3)

The definition of the covariance matrix, \mathbf{C} , is related to the covariance function of the Brownian process. This model assumption corresponds to the diffusion approximation of allele frequency drift in a random mating population conditional on

¹⁰⁶ non-fixation of alleles in the population (Kimura, 1964, 1983). The diffusion approx-¹⁰⁷ imation underlies the development of several recent methods of ancestry estimation ¹⁰⁸ similar to our model (Patterson *et al.*, 2012; Pickrell and Pritchard, 2012; Peter, 2016; ¹⁰⁹ Joseph and Pe'er, 2018). As a consequence of the definition, the variance of allele ¹¹⁰ frequencies is proportional to time. In applications, we normalized the sample dates ¹¹¹ so that t_1 corresponds to the variance of allele frequencies in the oldest sample.

Factor estimates. To compute the factor matrix, **U**, in the model equation (1), we turned to an equivalent formulation of this equation

$$\mathbf{Y} = \mathbf{W} + \mathbf{Z}\mathbf{B}^T + \epsilon',\tag{4}$$

¹¹⁴ where the residual noise is described by

$$\epsilon' \sim \mathbf{N}(0, \sigma^2 \mathbf{I}) \,. \tag{5}$$

In this formula, effect sizes, B_j , $j = 1, \dots, p$, are introduced, and considered as i.i.d. random variables with univariate Gaussian prior distribution $N(0, \alpha^{-1})$. A latent matrix, $\mathbf{W} = \mathbf{U}\mathbf{V}^T$, has a non-informative prior distribution. After a spectral decomposition of the covariance matrix \mathbf{C} , we define

$$\mathbf{Z} = \mathbf{P}\sqrt{\Lambda} \tag{6}$$

where P is a unitary matrix of eigenvectors, and Λ is the diagonal matrix containing the eigenvalues of C

$$\mathbf{C} = \mathbf{Z}\mathbf{Z}^T = (\mathbf{P}\sqrt{\Lambda})(\mathbf{P}\sqrt{\Lambda})^T.$$
(7)

¹²¹ Based on the Karhunen-Loève theorem (Loève, 1948), the diagonal terms of Λ can ¹²² be approximated as

$$\lambda_i \approx \frac{n}{(i-1/2)^2 \pi^2}, \quad i = 1, \dots, n,$$
(8)

123 and we have

$$Z_{ij} \approx f_i(t_j) \sqrt{\lambda_i/n}, \quad i, j = 1, \dots, n,$$
(9)

where $f_i(t)$ is defined as $f_i(t) = \sqrt{2} \sin((i - 1/2)\pi t)$ for all t in the interval [0, 1]. According to these results, the eigenvectors of the covariance matrix have sinusoidal shapes, and a diffusion model is consistent with the arch effect observed in principal components of genetic variation (Skoglund *et al.*, 2014).

Statistical estimates of the matrices **U**, **V** and **B** can be obtained by maximizing a posterior distribution in a Bayesian framework. This approach amounts to finding the minimum of the following loss function

$$\mathcal{L}(\mathbf{W}, \mathbf{B}) = \frac{1}{2} \|\mathbf{Y} - \mathbf{W} - \mathbf{Z}\mathbf{B}^T\|_F^2 + \frac{1}{2}\lambda \|\mathbf{B}\|^2, \qquad (10)$$

where we have set λ equal to the inverse of the temporal signal-to-noise ratio, $\lambda = \alpha\sigma^2$. Finding the matrices **W** and **B** that minimize the loss function $\mathcal{L}(\mathbf{W}, \mathbf{B})$ is equivalent to computing their estimates in a latent factor regression model with ridge penalty (Frichot *et al.*, 2013). According to Caye *et al.* (2019), the latent matrix, **W**, minimizes the following loss function

$$\mathcal{L}(\mathbf{W}) = \frac{1}{2} \|\mathbf{D}_{\lambda} \mathbf{P}^{T} (\mathbf{Y} - \mathbf{W})\|_{F}^{2}, \qquad (11)$$

¹³⁶ where \mathbf{D}_{λ} is a diagonal matrix with coefficients equal to

$$\mathbf{D}_{\lambda}(i,i) = \left(\frac{\lambda}{\lambda + \lambda_i}\right)^{1/2}, \quad i = 1, \dots, n.$$
(12)

¹³⁷ The estimate of **W** is provided by the best approximation of rank K of the matrix ¹³⁸ **Y**, where "best approximation" is related to the following matrix norm

$$\|\mathbf{Y}\|_{A}^{2} = \operatorname{Tr}(\mathbf{Y}^{T}\mathbf{A}\mathbf{Y}), \quad \mathbf{A} = \mathbf{P}\mathbf{D}_{\lambda}^{2}\mathbf{P}^{T}.$$
(13)

¹³⁹ In closed form, the optimal solution is equal to

$$\mathbf{W} = \mathbf{P} \mathbf{D}_{\lambda}^{-1} \operatorname{svd}_{K}(\mathbf{D}_{\lambda} \mathbf{P}^{T} \mathbf{Y}).$$
(14)

The K corrected factors forming U and their associated loadings, V, can be obtained from the SVD of the matrix W (see Table S1). For very large data sets, a modification of the SVD based on random projections could provide an accelerated version of the algorithm (Halko *et al.*, 2011).

Software availability. A short working R code presenting the algorithm in a selfcontained way is provided in Table S1. The method described in this section is
currently implemented as an R package temporalFA.

147 **3** Results

Horseshoe effect. To provide an example of distortion arising in PCA due to 148 uncorrected temporal drift, we performed a simulation of a coalescent model for 149 forty-one samples with ages ranging from 0 to 4,000 generations in a population 150 with effective size $N_{\rm e} = 10,000$. The sample dates in the simulation corresponded 151 to an interval of 100 generations. Covariance among samples was smaller for the 152 most ancient samples than for the most recent samples, and it increased linearly 153 with time (Figure 1A). The patterns observed in the sample covariance matrix were 154 highly similar to those obtained in a theoretical covariance function corresponding 155 to a Brownian process (Figure 1C). The PC plots of individual samples exhibited 156 sinusoidal patterns, in which the most ancient and recent samples were placed at 157 both extremes of a horseshoe (Figure 1B). Correcting for temporal drift, the factor 158



Figure 1. Horseshoe effect. Coalescent simulation of allele frequencies drifting through time in a single population ($N_e = 10,000$). Forty-one samples with ages ranging from 0 (present, grey color) to 4,000 generations (past, dark blue color) were simulated. A) Covariance matrix for observed samples B) PC plot for individual samples, C) Brownian covariance matrix used as a correction model, D) Factor analysis plot showing correction for temporal drift. In covariance matrices, the blue color indicates lower values whereas the yellow and grey colors indicate higher values.

analysis plot displayed a single cluster grouping all samples without any apparent
structure among samples (Figure 1D). This last result showed that distortion due to
temporal drift was correctly removed in a factor analysis using a Brownian model of
genetic drift.

Divergence model. In a second series of experiments, we simulated models of 163 divergence of two populations. In coalescent simulations, twenty-four samples with 164 ages ranging from 0 to 1,000 generations were simulated, corresponding to a sampling 165 interval of 100 generations and four present-day individuals. In a PCA of simulated 166 samples, PC1 reflected the level of divergence between populations while PC2 repre-167 sented temporal drift (Figure 2A). Correcting for temporal drift, the factor analysis 168 plot exhibited two clusters without any apparent structure within each group (Figure 169 2B). The Davies-Bouldin clustering index reached higher values in the FA plots than 170 in the PC plots, meaning that the clusters were better characterized and better rep-171 resented populations of origin in FA than in PCA (Figure 3C). In generative model 172 simulations, factor 1 in FA better explained the hidden factor than did the first PC 173 in PCA (Figure 3D). The results provided evidence that correcting for temporal drift 174 in FA revealed population structure hidden in the noisy data. 175

Admixture models. In another series of experiments, we considered admixture models in which an ancestral population splits into two sister populations 1,300 generations ago. The two divergent populations came into contact 500 generations ago, giving rise to descendants having 75% ancestry in the first ancestral population and 25% ancestry in the second ancestral population. One hundred present-day individuals were sampled from the admixed population, and fifty individuals were sampled



Figure 2. Simulation of two-population models. Twenty-four samples with ages ranging from 0 (present, grey color) to 1,000 generations (past, dark blue color) were simulated. A) Typical PC plot for observed samples, B) Factor analysis plot showing correction for temporal drift, C) Clustering index for PCA and FA results (100 coalescent simulations), D) Squared correlation between PC1 - Factor 1 and a true factor having two modes (100 generative model simulations).



Figure 3. Simulation of admixture models. One hundred samples were simulated for present-day admixed individuals (admixture rate 25 and 75%, grey color) and samples from two ancestral populations (age 1,000 generations, orange and blue colors). A) Typical plot for PC projection of ancient samples onto the admixed population showing a shrinkage effect, B) Factor analysis plot showing correction for shrinkage, C) Mean square error for estimates of admixture proportions from PC projections and FA plots (100 generative model simulations), D) Mean squared error for estimates of admixture proportions). Green crosses represent population centers, from which admixture estimates were computed.

from each ancestral population before the admixture event (1,000 generations ago). 182 Artificial genotypes generated according to a Brownian model were also used to simu-183 late levels of admixture similar to those observed in coalescent models (see Methods). 184 The objective of the experiments was to compare the results of PC projections of an-185 cient samples onto the present-day population with those obtained in factor analysis 186 with correction for temporal drift. Typical plots for PC projections exhibited a 187 shrinkage effect in which the projected samples were shifted toward zero, and closer 188 to the admixed population than expected (Figure 3A). The shrinkage effect was even 189 more pronounced in coalescent simulations than in generative model simulations (Fig-190 ure S1 and Figure 3C-D). Correction for temporal drift in factor analysis removed 191 the shrinkage effect, and, in the FA plot, the locations of centers of ancestral clusters 192 reflected admixture levels more precisely than in PC plots (Figure 3B). The mean 193 squared errors for estimates of admixture proportions were higher in PC projections 194 than in FA plots both in generative and in coalescent simulations (Figure 3C-D). The 195 results showed that correcting for temporal drift in FA improved the representation 196 of admixed individuals and their source populations compared with projections on 197 present-day individual PCs. 198

Hepatitis C virus infection. To follow chronic infection in a non-responder hepatitis C patient treated in the 2000's, we studied n = 1,934 samples of viral RNA sequences over a period of thirteen years (Caporossi *et al.*, 2019). The patient was coinfected by viral strains from two HCV genotypes, 4k and 1b. Height serum samples were available from years 2002 to 2014. Treatment with dual therapy had been administered for six months after the beginning of the follow-up period. A PC plot



Figure 4. Hepatitis C virus infection. Longitudinal study of a single nonresponder patient infected by two viral strains (HCV genotypes 1b and 4k). A total of n = 1,934 viral samples were collected from years 2002 to 2014. Dark blue color corresponds to the oldest samples, while yellow and grey colors correspond to the most recent samples. A) PC plot of viral samples, B) factor analysis with correction for temporal drift. A few outlier individuals detected in the FA plot are not shown in the plot.

of viral samples displayed a pattern similar to those observed in simulations of di-205 vergence models (Figure 4A and Figure 2A). PC1 reflected divergence among the 206 samples classified in distinct viral types, and PC2 was influenced by the ages of the 207 samples. After correction for temporal drift in a FA plot, viral particles were grouped 208 according to their phylogenetic classification (Figure 4B). In the FA plot, a first clus-209 ter consisted of 1b strains from year 2003 to 2014. A second cluster consisting of 4k 210 strains exhibited some degree of substructure, separating samples taken during treat-211 ment (year 2003) to the other samples. An interpretation of this result was that 1b 212 strains had mainly evolved through drift after treatment, whereas 4k strains might 213 had experienced other evolutionary changes, suggesting selection on this genotype 214 during the evolution of the disease (Caporossi *et al.*, 2019). 215

Ancient European genomes. We used PC projections and a Brownian model of 216 factor analysis to study a merged data set consisting of 155k SNP genotypes for 249 217 present-day European individuals and 386 ancient samples from Eurasia. The ages of 218 ancient individuals were less than 12,080 years cal BP, and individuals were selected 219 to be close to present-day Europeans in a preliminary FA analysis to leverage the 220 effect of low genomic coverage on factor one. The data set contained ancient samples 221 mainly from (Olalde et al., 2018; Mathieson et al., 2015; Haak et al., 2015; Mathieson 222 et al., 2018). First, we computed principal components on present-day samples, and 223 projected the ancient samples on the first two PCs (Figure S2). We also computed 224 factors with temporal correction for present-day and ancient samples, choosing the 225 hyper-parameter so that the factors correlate with principal components on present-226 day individuals ($\lambda = 2 \times 10^{-6}$, Multiple $R^2 = 0.97$ for factor 1, $R^2 = 0.75$ for factor 227

228 2, $P < 10^{-10}$, Figure S3). Both analyses revealed a similar pattern, in which most 229 ancient samples from Ukraine and all samples from Scandinavia, including hunter-230 gatherers from Latvia, were close to present-day Finnish samples, ancient samples 231 from Great Britain were close to present-day British samples, and ancient samples 232 from Anatolia and Israel were close to present-day southern Europeans. Ancient 233 samples from Iran, Armenia and Iraq formed a distinct group.

Next, we performed an unsupervised time-corrected factor analysis considering 234 ancient samples only. In this analysis, sample ages explained 0.2% of the variance 235 in factor 1 and 5.4% of the variance in factor 2, showing that temporal bias was 236 correctly removed from the first two factors ($\lambda = 10^{-3}$). The FA plot exhibited 237 four main clusters and a pattern of variation strongly consistent with the geographic 238 origin of samples (Figure 5, see Figure S4 for a definition of clusters). A first cluster 239 grouped ancient samples from Ukraine, Latvia and Sweden (Figure 5, green color). 240 Ages in the Scandinavian cluster 1 were around 7,671 years BP (mean value, SD 241 = 1,710 years). A second cluster grouped ancient samples from Russia, including 242 samples from Samara of the Yamnaya culture, Central Europe and Great Britain 243 (Figure 5, dark blue stars to golden points). Ages in cluster 2 were around 3,832 244 years cal BP (SD = 1,570 years). A third cluster grouped individuals from Anatolia 245 and Israel, Southern Europe and Great Britain (Figure 5, brown stars to golden 246 points). Ages in the southeastern cluster 3 were around 6,079 years cal BP (SD = 247 1,311 years). A fourth cluster grouped samples from Central Asia (salmon triangles). 248 Samples from Bronze age Great Britain (4,300 years BP) were grouped in cluster 2, 249 whereas samples from the neolithic period and from the same region were found in 250 cluster 3 representing Southeastern Europe. More generally, samples with ages older 251



Figure 5. Ancient European genomes. Factor analysis of 386 ancient Eurasian individuals with ages ranging between 400 and 12,000 years BP. Four main groups represent individuals from 1) Northern Europe and Ukraine (green color), 2) Russia, Steppe, Central Europe and the British Isles (average dates around 4k years BP, blue color), 2) Near East, Southern Europe and the British Isles (average dates around 6k years BP, brown color), and 4) Central Asia (Salmon color).

than around 4,500 years BP were grouped in the southeastern cluster, while more recent samples from the bronze age clustered with ancient North Eurasian, Russian and Steppe samples in the central cluster 2. Discontinuities in ancestry reflected in factor 1 were observed for samples from Great Britain, Germany and Hungary (Figure 6). In Hungarian samples, a linear trend was observed for the period 4,500 -8,000 years BP, consistent with levels of hunter-gatherer ancestry detected in (Lipson *et al.*, 2017).

To assess the genetic ancestry of samples from Great Britain, a second FA was 259 performed. This analysis isolated British samples from ancient North Eurasians 260 and ancient Near Easterners, considered as putative source populations (Figure 7). 261 British samples with dates earlier than 4,300 years cal BP clustered with samples 262 from the Near East. Samples with dates around 4,300 years cal BP (early bronze 263 age) were close to samples from Russia, and a genetic discontinuity was observed with 264 more ancient samples from Anatolia. Estimating admixture coefficients from factor 265 1, the early bronze age samples shared around 64% of their ancestry with the North 266 Eurasian samples and 36% with the Neolithic Easterners. Samples from the middle 267 bronze age (around 3,300 BP) formed a distinct group, suggesting a more complex 268 history than two waves of invasions in the British Isles. 269

Finally, a larger set of 697 ancient samples was considered for replication of PC projection and unsupervised FA results. PCA and FA plots yielded similar descriptions of the data when a larger set of ancient samples was considered (Figure S5-S6).



Figure 6. Factor 1 as a function of age (years cal BP). Factor 1 of a temporal FA displayed as a function of age for samples from Great Britain, Germany, Hungary and Bulgaria. The data support a major change in genetic mixture of individuals from Great Britain, Germany, Hungary around 4,500 years BP (dashed line).



Figure 7. Ancestry of ancient samples from Great Britain. FA plot for samples from ancient North Eurasians (Russia and Samara with Yamnaya Culture, dark blue color), from ancient Near East (Neolithic Anatolia and Israel, brown color), and from Great Britain (grey color). The samples from Great Britain cluster in three groups: Neolithic (N), Early Bronze Age (EBA), Middle Bronze Age (MBA).

273 4 Discussion

We introduced a new factor analysis method for describing ancestral relationships 274 among DNA samples collected at distinct time points in the past. Like in PCA, the 275 method is based on a factorial decomposition of the data matrix into a product of 276 score and loading matrices. The most important difference with the PCA approach 277 is that individual scores in FA were corrected for the effect of temporal drift in allele 278 frequency. Based on a diffusion approximation, we approximated allele frequency 279 drift by a Brownian process, and an efficient algorithm based on the singular value 280 decomposition computed the factor estimates. 281

Using a Brownian model of genetic drift, we compared the results of FA with 282 those of PCA and PC projections in simulations of divergence and admixture. In 283 divergence scenarios, distortions due to temporal drift were removed in FA. Correct-284 ing for temporal drift revealed hidden population structure better than did a PCA. 285 In admixture scenarios, estimates of ancestry coefficients were more accurate in FA 286 than those inferred from principal components. In those simulations, correcting for 287 temporal drift allowed a better representation of admixed individuals than PC pro-288 jections. 289

Next, we applied temporal corrections to study the evolution of hepatitis C virus in a patient infected by multiple strains. After correction for temporal drift, viral strains clustered according to their phylogenetic classification. In agreement with the fact that the patient did not respond to treatment, FA suggested that 1b strains had mainly evolved through drift after treatment. Evidence for substructure within 4k samples suggested an action for other evolutionary processes among those strains. Caporossi *et al.* (2019) reported that nucleotide diversity was higher in 1b time sam-

ples than in 4k time samples, which might indicate that drift was more important in the 4k population. With the FA result, this suggests that distinct corrections should be applied to 4k and 1b samples. We performed a separate FA with 4k samples only (not shown), and the observed substructure persisted. Overall, the FA plot supported the hypothesis that drift was not the only process acting on the genetic diversity of 4k genotypes, and that those strains might have experienced some form of selection during the course of disease evolution Caporossi *et al.* (2019).

In a re-analysis of a merged data set of ancient DNA filtering out SNPs with high 304 levels of missing data and genomes of low coverage, we implemented correction for 305 temporal drift to describe ancestry in samples from ancient Europeans and Eurasians. 306 After correction, the patterns observed in FA plots were consistent with those ob-307 served in projections of ancient samples on axes built on the 1,000 Genomes data. 308 The factor analysis supported the hypothesis that a major change in genetic mixture 309 of individuals occurred in Great Britain and in continental populations around 4,300 310 years BP (Olalde et al., 2018). Observed FA patterns were more consistent with 311 geography in than those in PC projections, suggesting a role of localized gene flow 312 unseen in previous analyses at the continental scale. Our analysis provided a visual 313 representation of Bronze age British samples consistent with the proportion of North 314 Eurasian and steppe ancestry of the original (Olalde *et al.*, 2018). 315

In conclusion, including corrections for temporal drift resulted in an algorithm with a computational cost similar to a PCA. Determining the model hyper-parameter was based on simple approaches, computing a correlation between sample dates and first FA scores. Our study showed that the FA method corrected biases observed in PC plots successfully. A useful and important feature of the new approach was to

³²¹ avoid supervised analyses in which unbalanced samples over-representing present-day
³²² individuals are utilized. The unsupervised approach based on FA revealed details of
³²³ population structure masked in PC projections, and was generally more accurate
³²⁴ than principal component analysis of population structure for ancient samples.

5 Materials and Methods

Coalescent simulations. We used the computer program *msprime* to simulate 326 temporal samples for individuals at distinct time points in the past (Kelleher et al., 327 2016). Firstly, a single population of $N_e = 10,000$ individuals was simulated during 328 4,000 generations. An individual was sampled every 100 generations, resulting in 41 329 samples with ages ranging between 0 (present-day) and 4,000 generations. A total of 330 around 9,000 SNPs were simulated for each individual. Secondly, a divergence model 331 was considered in which an ancestral population of effective size $N_e = 10,000$ split 332 into two sister populations of equal sizes 1,500 generations ago. Twenty-four individ-333 uals with ages ranging from 0 to 1000 generations were sampled every 100 generations 334 (four present-day individuals were simulated), and around 8,800 SNPs were simulated 335 for each individual. One hundred replicate data sets were created with the same de-336 mographic parameters. For each simulation, the Davies-Bouldin index was computed 337 (Davies and Bouldin, 1979). The Davies-Bouldin index is a metric for evaluating the 338 degree of clustering in multidimensional data, and ranges between zero and one. Cor-339 rections for temporal drift in allele frequency are expected to provide index values 340 closer to one than those for principal components. Thirdly, an admixture model was 341 considered in which an ancestral population of effective size $N_e = 10,000$ split into 342 two sister populations of equal sizes 1,300 generations ago. The two divergent pop-343

ulations came into contact 500 generations ago, and this event gave rise to a third 344 population. Individuals in the admixed population shared 75% ancestry with the 345 first ancestral population, and 25% ancestry with the second ancestral population. 346 One hundred individuals were sampled from the admixed present-day population, 347 and fifty individuals were sampled from each ancestral population, 1,000 generations 348 ago. A total of around 9,600 SNPs were simulated for each individual. One hundred 349 replicate data sets were created with the same demographic parameters. For each 350 simulation, we computed the centers of the ancestral and admixed population on the 351 first axis, and we estimated admixture proportion based on the ratio of distances 352 between population centers. We also did this for the first factor with correction for 353 temporal drift. We eventually computed mean squared estimation errors both for 354 PCA and for FA estimates. 355

Generative model simulations. Since the correction method is not restricted application to ancient DNA, we performed a series of experiments using the generative model defined in equation (1)

$$\mathbf{Y} = \mathbf{U}\mathbf{V}^T + \epsilon, \quad \epsilon \sim \mathbf{N}(0, \alpha^{-1}\mathbf{C} + \sigma^2 \mathbf{I}).$$

The objective was to evaluate statistical errors for latent factor estimates in a general context. The generative model simulations have the advantage of creating artificial data for which the ground truth is available. Based on a genealogical interpretation of principal components, we devised two series of simulations (McVean, 2009). The first scenario considered a divergence model in which two populations evolved without gene flow. In this case, populations were grouped separately along the first factor, and their divergence time was represented by the distance separating the group means.

The samples were taken at random times in the past and correlated noise was included in the data matrix. The second scenario considered an admixture model in which two populations diverged in the distant past and an admixture event occurred recently. Half of the samples were ancient, taken from the ancestral populations at random times in the past, and the other half of the samples were collected from the admixed population in present time.

For the divergence model, the factor matrix U contained K = 3 factors, simulated 369 as Gaussian independent random variables. The standard deviation for first factor, 370 s_1 , measured divergence between the two ancestral populations, and was varied in the 371 range from to 2 to 10. Factors 2 and 3 had lower standard deviations, respectively 372 equal to $s_2 = 1.5$ and $s_3 = 0.5$, so that \mathbf{u}_1 contained the largest genomic information. 373 The λ parameter, representing an inverse temporal signal-to-noise ratio, was chosen 374 in the range $[10^{-1}, 10^{-6}]$. The number of samples, n, was equal to 200, and the 375 number of markers was kept to p = 1,000. Loadings were simulated as independent 376 standard Gaussian random variables, and the residual variance was set to $\sigma^2 = 1$. 377 For each simulation the squared correlation between the true \mathbf{u}_1 and estimated factor 378 $\hat{\mathbf{u}}_1$ was computed. 379

For the admixture model, the factor matrix U contained K = 3 factors. In the first factor, the two ancestral populations were positioned (with a standard deviation of 1) so that the distance separating their centers, d_1 , measuring divergence between them, was varied in the interval [10,12]. Factors 2 and 3 had standard deviations equal to $s_2 = 1.2$ and $s_3 = 1$. Admixed individuals were positioned so that center was at relative distance *a* from ancestral population 1, and 1-a from ancestral population 2, where *a* represents the ancestry contribution of population 1 to modern samples. The

simulated ancestry coefficients ranged between a = 0.2 and a = 0.4. The λ parameter 387 was set to $\lambda = 5.10^{-2}$. The number of samples was set to n = 200, and the number 388 of markers was kept to p = 5,000. The loadings were simulated as independent 380 Gaussian, N(0,0.2), random variables, and the residual error was set to $\sigma = 0.1$. We 390 performed a total of 100 simulations. For each simulation, the squared correlation 391 between the true \mathbf{u}_1 and estimated factor $\hat{\mathbf{u}}_1$ was computed, and an estimate of the 392 ancestry coefficient was provided, based on the relative positions of cluster means in 393 $\hat{\mathbf{u}}_1$. 394

Hepatitis C virus data. To understand chronic infection in non-responder hep-395 atitis C virus (HCV) patients treated with dual therapy in the 2000's, Caporossi et al. 396 (2019) performed deep sequencing on the NS5B (381 bp) region of the viral genome 397 for a patient followed at Grenoble-Alpes University Hospital. The patient had a 398 known date of infection because of an identified transmission event due to transfu-399 sion. The patient was treated with dual therapies based on pegylated interferon and 400 ribavirin. The treatment had been administered for six months from January to June 401 2003, and a total of height serum samples were available for a follow-up period of 13 402 vears. Co-infection by viral genotypes 4k and 1b was detected, and n = 1,934 RNA 403 samples from years 2002 to 2014 were studied. 404

Ancient Human DNA samples. A merged data set consisting of genotypes for 1,820 ancient and present-day individuals compiled from published papers was downloaded from David Reich's repository (https://reich.hms.harvard.edu/). The downloaded data matrix contained up to 1.23 million positions in the genome. Considering age defined as average of 95.4% date with range in cal BP computed as 1950

CE, Eurasian samples with age less than 12,080 years were retained. The data matrix was filtered out for samples falling far outside of the present-day Europeans in a preliminary FA analysis, leading to a median genomic coverage of 3.35x and a minimum coverage of 0.51x in the final data set. Only genomic positions with less than 25% of missing genotypes were analyzed. Missing genotypes were imputed by using a matrix completion algorithm based on sparse non-negative matrix factorization (Frichot and François, 2015; Frichot *et al.*, 2014).

The resulting data set contained 155,682 genotypes for 249 present-day European 417 individuals from the 1,000 Genomes project (phase 3) and 386 ancient samples from 418 Eurasia studied in previous works (The 1000 Genomes Project Consortium, 2015) 419 (Supplementary File 1). The most important contributions to samples included in 420 our data set were 1) 137 ancient individuals in (Olalde et al., 2018) including 72 421 individuals from Great Britain, 30 from Czech Republic, 24 from Hungary, 14 from 422 Germany and 13 from Russia, 2) 74 ancient individuals in (Mathieson et al., 2015) (31 423 same samples with 390k in (Haak et al., 2015)), including 49 individuals from Great 424 Britain, 15 from Turkey, 35 from Finland, 8 from Russia, 3) 57 ancient individuals 425 from (Mathieson et al., 2018), including 18 individuals from Great Britain, 11 from 426 Hungary, 7 from Germany, 6 from Finland, 11 from Russia, 5 from Ukraine, 4) 40 427 ancient individuals in (Lipson et al., 2017), including 6 individuals from Great Britain, 428 9 from Hungary, 14 from Finland, 4 from Ukraine. For a full list of individuals 420 studied see Table S2. A larger set of genotypes with 5,081 ancient and present-day 430 individuals from the same repository was also considered in analyses. Following the 431 same filtering and imputation procedures as for the first data set, the resulting data 432 contained 123,763 genotypes for 477 present-day European individuals from the 1k 433

Genomes project and 697 ancient samples from previous studies (Supplementary File
2). The data were imputed from genotypes with 20% missing SNPs.

Acknowledgements. We thank the Paris-Saclay Center for Data Science 2.0 (IRS)
and LRI for funding BD and SL salaries and supporting FJ's mobility. We also thank
Cyril Furtlehner for discussions. This article was developed in the framework of the
Grenoble Alpes Data Institute, supported by the French National Research Agency
under the "Investissements d'avenir" program (ANR-15-IDEX-02).

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545 Supplementary Materials

- 546 Supplementary tables and figures for "Inference of Population Genetic Structure
- ⁵⁴⁷ from Temporal Samples using Bayesian Factor Analysis" by François et al.

Table S1. R code for temporal factor analysis

```
temporal_fa = function(sample_ages, Y, k = 2, lambda = 1e-3){
 # sample_ages: Ages of samples (year BP/BCE or generations)
 # Y: Matrix of fully imputed genotypes
 # k: Number of factors
 # lambda: Hyper-parameter (range: 1e-1 to 1e-6)
 # conversion of ages as elapsed times between 0 and 1
    Y <- t(scale(t(Y), center = TRUE, scale = FALSE))</pre>
    var_Y <- apply(Y, 1, FUN = var)</pre>
    range_ages <- max(sample_ages) - min(sample_ages)</pre>
    t_n <- 1 - (sample_ages - min(sample_ages))/range_ages</pre>
    t_n \leftarrow min(var_Y) + (max(var_Y) - min(var_Y)) * t_n
 # Brownian covariance model
    n <- length(t_n)</pre>
    C <- matrix(NA, n, n)
    for (i in 1:n){
        for (j in 1:n)
            C[i,j] <- min(t_n[i], t_n[j])}</pre>
 # Eigenvectors and eigenvalues
    ec <- eigen(C)</pre>
    P_n <- ec
    lambda_n <- ec$values</pre>
 # New factors
    D <- diag(sqrt(lambda/(lambda_n + lambda)))</pre>
    D_inv <- diag(sqrt((lambda_n + lambda))</pre>
    sv <- svd(D %*% t(P_n) %*% Y, nu = k)
    U_n <- P_n %*% D_inv %*% sv$u %*% diag(sv$d[1:k])
    W_n <- U_n %*% t(sv$v[,1:k])
 # Returns corrected factors U and latent matrix W
    return(list(u = U_n, w = W_n))
}
```



Figure S1. Admixture model simulation. Shrinkage in PC projections. Simulation of two-population admixture models (25-75 % proportions). Two hundred samples with ages equal to 0 (present-day admixed individuals, grey color) and 1,000 generations (ancestors, orange and blue colors) were simulated. A) Plot for PC projection of ancient samples onto the admixed population, with a strong shrinkage effect (coalescent simulation), B) Factor analysis plot showing correction for shrinkage, C) Mean square error for estimates of admixture proportions from PC projections and FA plots (100 generative model simulations), D) Mean square error for estimates of admixture proportions (100 coalescent simulations). Green crosses represent population centers, from which admixture estimates were computed.



Figure S2. Ancient Humans - PC projections. Projections of 386 ancient Eurasian genomes with age ranging between 400 and 12,000 years BP on principal components of 249 European genomes from the 1,000 Genomes data. Present-day individuals are represented as colored full dots. Smaller light grey dots and other types of dots are ancient genomes.



Figure S3. Ancient Humans - Supervised factor analysis. Factor analysis of 386 ancient Eurasian genomes with age ranging between 400 and 12,000 years BP and 249 European genomes from the 1,000 Genomes data. Present-day individuals are represented as colored dots. Smaller light grey dots and other types of dots are ancient genomes.



Figure S4. Ancient Europeans - Clusters in factor analysis. Definition of clusters for computing estimates of average ages per factor region. Cluster 1 consists of individuals from Ukraine and Scandinavia, not represented in the plot. Cluster 2 is formed of North Eurasian individuals (Russia, Samara, red color) and central and western Europeans (green color). Cluster 3 is formed of Near Eastern individuals, southern and western Europeans (Neolithic, black and blue colors). Cluster 4 is formed of central Asians (Neolithic, light-blue color). Clustering was performed with a k-means algorithm.



Figure S5. Extended ancient genome data set - PC projections on 1k Genomes data. Projections of 697 ancient genomes on the principal components of 477 genomes from the 1k Genomes data. Only ancient individuals are displayed with some populations emphasized (dates more recent than 12 ky cal BP).



Figure S6. Extended ancient genome data set - Factor Analysis. Factor analysis of 697 ancient genomes with some populations emphasized (dates more recent than 12 ky cal BP). The observed pattern similar to PC projections, but more consistent with geography.