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# Performance comparison between standard and magnetically shielded 200 W Hall thrusters with BN-SiO<sub>2</sub> and graphite channel walls

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## Abstract

Magnetic shielding is a specific magnetic topology that has the potential to produce a severalfold increase in the lifespan of Hall thruster. It reduces wall erosion and has been shown to result in similar performances as standard unshielded thrusters in the 5 to 15 kW discharge power range. A direct comparison of the performances of two 200 W shielded and unshielded Hall thrusters is presented here. The effects of replacing the usual BN-SiO<sub>2</sub> walls with graphite are investigated on both type of thrusters. The unshielded ISCT200-US thruster has a peak anode efficiency of 39% and a specific impulse of 1400 s at 250 W with the ceramic discharge channel. It however suffers from the change to graphite wall, the peak efficiency falls down to 31% (1360 s specific impulse) as the discharge current increase by nearly 25%. The magnetically shielded ISCT200-MS performances are significantly lower than its unshielded counterpart. It only reaches 24% anode efficiency and 1020 s specific impulse at 250 W. Interestingly the switch to graphite has little effects on its performances below 300 V. An increase in thrust is observed at 300 V with graphite walls. It raises the anode efficiency to 28% at 320 W (1240 s specific impulse). We propose an explanation as to why the small shielded thruster shows lower performances than an equivalent unshielded one.

*Keywords:* Hall thruster, Electric propulsion, Magnetic Shielding, Wall materials

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## 1. Introduction

Hall thrusters are one of the most widely used electric propulsion system for space applications[1]. They benefit from their high thrust to power ratio and reasonable specific impulse that makes them particularly well suited for missions within earth's sphere of gravitational influence.

One of limiting factor of Hall thruster (HT) usage is their limited lifespan caused by the wall erosion. This erosion is particularly severe in small thrusters ( $\leq 500$  W) where the surface to volume ratio of the discharge channel is high. Such thrusters rarely last more than 3,000 hours[2] while kilowatt class HT often achieve 10,000 hours long lifespan[3].

Increasing the lifespan of HT would enable a number of missions for this technology. On the high power side ( $\geq 5$  kW) the lifespan can be limiting for all electric satellite platform as the electric orbit

raising considerably increase the total firing time. It would also make HT competitive for exploration missions such as the now canceled robotic segment of the Asteroid Redirect Mission[4]. For low power units a longer lifespan would allow the use of HT for very low Earth orbit drag compensation applications. It would also remove a failure mechanism that could prevent end of life disposal of the satellite.

One solution, initially investigated by the Jet Propulsion Laboratory, is to use a “magnetic shielding” (MS) topology[5]. This technique prevents the flow of the high energy ions responsible for erosion toward the walls. This has been shown to effectively reduce erosion by two orders of magnitude. More details on how magnetically shielded thrusters operate will be provided in section 2

Results presented here are a direct comparison between a magnetically shielded (MS) and an unshielded (US) version of the same thruster with a nominal operating power of 200 W. Both thrusters are tested with a BN-SiO<sub>2</sub> and a graphite discharge

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channel. First will be presented the concept of magnetic shielding as well as a short review of the principle of magnetic shielding applied to Hall thrusters and influence of the discharge channel material on their operation. The experimental setup used in this test campaign will be discussed in section 3. Lastly the results will be presented and discussed in section 4.

## 2. Background

### 2.1. Magnetic shielding operating principle

A classical Hall thruster is a  $E \times B$  plasma device. A radial magnetic field is induced in an annular discharge chamber. At the back of the chamber a neutral gas (Xenon in most cases) is injected and an anode is placed. An external cathode is used to produce electrons. Some of these electrons travel toward the anode and are trapped by the magnetic barrier in an azimuthal Hall current. This Hall current ionize the atoms. The low electron diffusion rate in that barrier makes it an area of high (axial) ohmic resistance and thus localizes the potential drop applied between the cathode and the anode. This electric field accelerates the ions. The intensity of the magnetic field is chosen such that only the electrons are magnetized.

Due to the high mobility of the electrons along the magnetic field lines, and the relative radial uniformity of the plasma density, those can be considered equipotential and isotherm as a first order approximation. This has been used for years to shape the electric field in a Hall thruster and focus the ion beam.

In 2010, surprising results were obtained during lifetime testing of the BPT-4000 Hall thruster[6]: after 5600 hours of firing erosion stopped. After investigation the relationship between the magnetic topology and the physical shape of the discharge channel was found to be responsible for this erosionless state. The research teams at the Jet Propulsion Laboratory and Aerojet named that configuration “magnetic shielding” (MS). The difference between a classical unshielded (US) and shielded configuration is illustrated in figure 1. The concept takes advantage of the properties of the magnetic field lines to reduce both the ion energy and ion flux impacting the walls. A field line tangent to the wall is created between the top of the thruster and the anode area at the back of the channel. This lined, called the “grazing line” ensure that the area along

the wall has a layer of cold electrons ( $\sim 5$  eV) originating from the anode region. That lower electron temperature reduces the sheath potential drop at the wall and thus the energy of the ions accelerated through that sheath.

In order to produce that grazing line the maximum of the magnetic field along the center of the discharge channel needs to be pushed downstream. This results in a downstream shift of the ionization and acceleration regions, further reducing the density and average energy of the ions.

### 2.2. Previous work on low power magnetically shielded thruster

Experiments on the H6MS thruster have shown similar performance as the unshielded (US) H6 thruster[7]. The 12.5 kW HERMeS MS-HT also presents very good performances[8].

Low power Hall thruster in the 100 to 400 W range are usually limited to lower efficiencies. An anode efficiency map of number of low power Hall thrusters can be found in the appendix 5.1. Most of the thrusters found in the literature hover around 35 to 40% efficiency in the in the 200 to 300 W range. The BHT-200 and the CAMILA-HT-55 are two notable exceptions with efficiencies approaching 50%.

One of the reasons often put forward to explain the lower efficiency of small thrusters is their higher surface to volume ratio which promotes energy losses to the walls. One of the solution proposed to solve this issue is to increase the relative width of the discharge channel[9, 10, 11]. Since the magnetic shielding topology reduces the interactions between the plasma and the walls it has the potential to also reduce losses in those small thrusters.

This however has not been the case for the first versions of the low power MaSMi-40 and MaSMi-60 magnetically shielded HTs[12]. Their efficiency is markedly lower than equivalent unshielded thrusters (see figure 9). Conversano explains that low efficiency by a combination of low propellant utilization due to inefficient gas injection and weak magnetic field, and high divergence caused by the magnetic shielding topology[13, 14]. Subsequent developments with the MaSMi-60-LM2[15] and MaSMi-DM[16] have raised the performance of this thruster to 45% anode efficiency at 500 W.

The goal of this study is to compare the performance of a traditional unshielded thruster with a

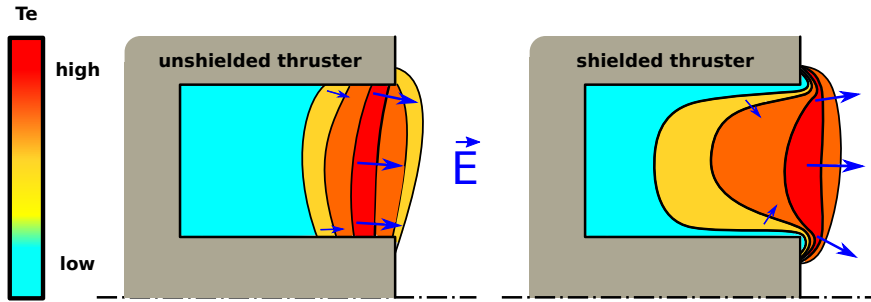


Figure 1: Comparison between classical and magnetic shielding configurations, the black lines represent the magnetic field lines.

140 shielded version as well as with other similarly sized  
Hall thrusters. It should be noted that both those  
thrusters are laboratory prototypes that have not  
145 been optimized for performance.

The results presented here are part of a more  
145 general study on low power magnetically shielded  
thrusters. A 200 W permanent magnets, magne-  
tically shielded Hall thruster named the ISCT200-  
MS was built with the same dimensions and mag-  
150 netic field strength as the ISCT200-US. This was  
done in order to compare the capability of the two  
thrusters. The original ISCT200-US (previously  
called PPI-Mag) was a thruster used to investigate  
155 the effect of the width of the high magnetic field  
area[17].

An initial mapping effort of the discharge enve-  
155 lope was first presented in 2016[18, 19]. The results  
demonstrated that the discharge currents were rea-  
sonably similar in both thrusters for a given dis-  
160 charge voltage and mass flow.

A series of plume measurements conducted in  
160 the NExET vacuum chamber showed that the  
ISCT200-US and ISCT200-MS both have similar  
divergence angle but that the shielded thruster does  
165 not ionize the propellant as well as its unshielded  
counterpart.

The mechanisms of magnetic shielding in a small  
165 thruster were also investigated[20]. Laser induced  
fluorescence spectroscopy revealed that in the MS-  
HT the acceleration region is situated primarily  
170 outside the thruster. The ionization region is also  
shifted downstream which overall reduces the den-  
sity of energetic ions responsible for the erosion of  
the discharge channel.

The ion velocity distribution function near the  
175 walls shows that the ions are not accelerated to-  
ward the walls either. This is presumably due to the  
magnetic field lines parallel to the wall both reduc-

ing the electron temperature (and thus the sheath  
potential) and directing the electric field away from  
180 them.

We also observed some high velocity ions coming  
toward the inner magnetic pole and responsible for  
the tenuous erosion observed there.

### 2.3. Alternative wall materials and magnetic shielding

#### 2.3.1. Motivations for alternative materials

185 More recently we have studied the influence of  
the wall material on the discharge characteristics  
of both thrusters[21]. Since the magnetic shielding  
topology limits the electric field intensity near the  
walls and reduces the ion density in this region[20]  
190 it stands to reason that the thruster should be less  
sensitive to the wall material.

Goebel et al[22] first attempted to replace the  
195 usual boron nitride compound with graphite on the  
6 kW magnetically shielded H6MS Hall thruster.  
Their results show that the discharge current is  
mostly undisturbed by the change of material and  
that the anode efficiency is only a couple of per-  
200 cents lower with this material than with the classi-  
cal boron nitride walls.

This result is remarkable. Graphite seriously de-  
205 teriorates performances in an unshielded thruster.  
Gascon et al[23, 24] showed this when they studied  
the performances of the 1.5 kW SPT-100-ML with  
different wall materials. This study included the  
use of borosil (BN-SiO<sub>2</sub>), alumina, silicon carbide  
and graphite discharge channel walls. While the  
thrust versus discharge voltage behavior was not  
210 perturbed much by the change in material, they  
observed up to 25% increase of the mean discharge  
current as well as an increase in its oscillations.  
This had for effect to reduce the anode efficiency  
from 50% in borosil to 30% with graphite.

Other efforts in using conducting materials in HT discharge channels include a 200 W thruster from the Harbin Institute of Technology[25]. This thruster has a magnetic topology design to push the discharge outside the thruster and is presented as a “no wall loss” thruster[26]. Tests with a titanium discharge channel have demonstrated an anode efficiency of 34%. Earlier tests were also conducted at Princeton with various configurations of short graphite rings[27].

The similarities between our two thrusters allow us to directly compare the influence of the wall material on equivalent US and MS Hall thrusters.

From an engineering point of view graphite is an interesting material for two reasons. Firstly, it has a lower sputter yield than boron nitride compounds[28] by a factor of 2 to 3 at the relevant energies. This means that any residual erosion in magnetic shielding configuration could be mitigated even more by replacing the wall material. The second reason is practical one for thruster ground testing. Back sputtered material from the chamber, usually composed of carbon compounds, tends to deposit on the surfaces of the thruster and change the properties of the walls. In a magnetically shielded thruster this layer is not cleaned by erosion. Since this phenomenon is not present in space, it violates the “test as you fly” philosophy when MS-HT are ground tested. Showing that carbon walls have no influence on the thruster would answer these concerns.

### 2.3.2. Previous results

Our first series of measurements shows no significant difference when the ISCT200-MS is fired with graphite and boron nitride (Saint-Gobain’s BN M26 grade) walls[21]. Both the mean discharge current and its dynamics are similar. The plume is not affected either. Lastly the electric field stays at the same position (ie near the maximum of the magnetic field).

This is a stark contrast with the US-HT. The switch to graphite produces a 20 to 30% higher discharge current at similar voltage and mass flow. The dynamics are also significantly altered with more pronounced oscillations with the conducting graphite. The accelerating electric field is also stretched out and push downstream. Lastly a larger divergence angle and ion current were measured in the graphite configuration.

The results presented here have for objective to conclude this study by measuring the thrust of the

US and MS Hall thrusters with graphite and BN-SiO<sub>2</sub> walls. This will highlight any effect of the wall materials on the specific impulse and anode efficiency of classical and shielded low power thrusters.

## 3. Experimental setup

### 3.1. PIVOINE 2G test facility

The PIVOINE 2G test facility is setup around a 4 m × 2.2 m cylindrical vacuum chamber. It is outfitted with a 220000 l/s cryogenic pumping system sized for Hall thrusters ranging from 1 to 20 kW. This allowed us to maintain a very good vacuum during the whole test campaign. All the measurements presented in this work were performed at a xenon pressure between 5 and 7.5 × 10<sup>-6</sup> mbar. This is below the threshold at which pressure effects become significant[29]. The large chamber relative to the thruster size and power also ensures minimal boundary effects from the grounded chamber.

The thrusters were fired with an oversized 5 A class cathode[30, 31]. Consequently all the figures presented in this article do not take into account neither the heating power of the cathode nor the cathode mass flow.

### 3.2. Plume measurements

Plumes measurements were performed with 15 mm diameter Faraday cup probe. This probe is mounted on a rotating arm 70 cm from the thruster exit plane (approximately 20 thruster diameters). The probe surface is polarized by a Keithley 2410 source meter that also measured the collected ion current. More details on the probe design and utilization can be found in reference [29].

The arm is rotating on a 180 arc in front of the thruster and the ion current is measured over 70 individual points.

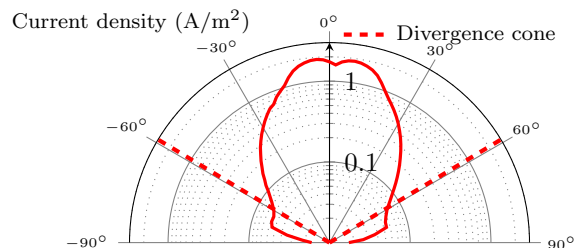


Figure 2: Ion current profile for the US-HT in BN-SiO<sub>2</sub> at 200 V and 1.2 mg/s collected 70 cm from the thruster. The dashed line represent the divergence angle  $\alpha_d$ .

The data collected is not corrected for charge exchange or any other effects. The total ion current is computed by integrating the ion current over the hemisphere facing the thruster. The divergence angle is defined as the half angle of the cone containing 90% of the collected ion current. We define the beam efficiency  $\eta_I$  as the ratio of collected ion current over the total discharge current. The propellant utilization  $\eta_{prop}$  is the ratio of collected ions (assuming those are simply charged) over the number of neutral atoms injected at the anode. It is computed using the equation (1). The mean charge of the ion  $q_{mean}$  is assumed to be 1  $e$  for the results presented in section 4.2. This is a strong assumption, especially on a magnetically shielded thruster. It will be discussed with the results in section 4.3.1.

$$\eta_{prop} = \frac{I_b \cdot M_{Xe} \cdot N_a}{q_{mean} \cdot \dot{m}_a} \quad (1)$$

Measurements were performed for each thruster at 200 V, 1 and 1.2 mg/s anode mass flow.

### 3.3. Thrust stand

The thrust stand in PIVOINE 2G is a simple pendulum design. The thruster is mounted on a titanium structure suspended by three braided steel wires and connected with a flexible PCB. The displacement of the thrust stand is measured by a capacitive sensor with a resolution of 0.2  $\mu\text{m}$ .

The thrust stand is fitted with a system of reference masses for calibration. For each operating conditions, after the thruster's discharge is stabilized the position of the thrust stand is recorded for several minutes. The thruster is then shut down and the two reference masses are hung. For each configurations (no mass, mass 1, mass 1 and mass 2) the position of the thrust stand is measured. These three values are used as calibration points. The thrust stand is not temperature controlled. Calibration after each measurement allows for compensation of thermal drift effects.

The thrust stand, like the rest of the PIVOINE 2G facility was designed for thruster between 1 and 20 kW (ie thrust ranging from 50 to 1000 mN). As such the precision on the thrust is only around  $\pm 0.5$  mN for thrust values between 5 to 15 mN. Uncertainty bounds are computed individually for each measurements.

Thrust measurement were performed for anode mass flows of 0.8, 1 and 1.2 mg/s and discharge voltages of 150, 200, 250 and 300 V.

## 4. Results and discussion

### 4.1. Thrust and efficiency

#### 4.1.1. Unshielded thruster

The thrust versus voltage, and specific impulse versus voltage curves for the different anode mass flows and channel materials are shown in figures 3 b) and 3 c). The thrust ranges between 6 and 16 mN and the ISP between 600 and 1400 seconds at the points tested. The maximum anode efficiency is 39% ( $\pm 3\%$ ).

As described by Gascon et al. on the SPT-100[23] the change in wall material does not significantly affect the thrust vs voltage behavior. The only differences are observed at 200 V and below for a xenon mass flow of 1.2 mg/s. All the other points have similar results within the uncertainty of the measurement. However as seen in figure 3 a) the discharge current is significantly higher in the unshielded HT with graphite walls compared to the boron nitride case. This results in the behavior seen in figure 3 d) where the maximum efficiency is higher with ceramic than with graphite.

Like the thrust, the specific impulse dependence on voltage does not appear to be strongly affected by the change in material. Interestingly the points at a mass flow of 1 mg/s are nearly indistinguishable from the one at 1.2 mg/s while the specific impulse at 0.8 mg/s is significantly lower. This suggests that a higher proportion of the propellant is not ionized at low mass flow.

Figure 9 shows an overview of the anode efficiency achieved with low power Hall thrusters. The ISCT200-US has performances comparable to the CAM200-EM, PlaS-40, T-40 and SPT-30. It outperforms the HT100D by about 5% under 250 W. The BHT-200 and CAMILA-HT-55 are however in a class of their own with an efficiency of more than 45% at 200 W while most other HT only get 35%.

Keeping in mind that the ISCT200-US is a laboratory thruster which has not been optimized for performances we think it adequately compares to commercial thrusters and constitute a good benchmark to assess the performances of the magnetic shielding concept.

#### 4.1.2. Magnetically shielded thruster

As show in figure 4 a), the change of wall material has nearly no effects on the discharge current. This is consistent with the previous results obtained in the small NExET test chamber[21].

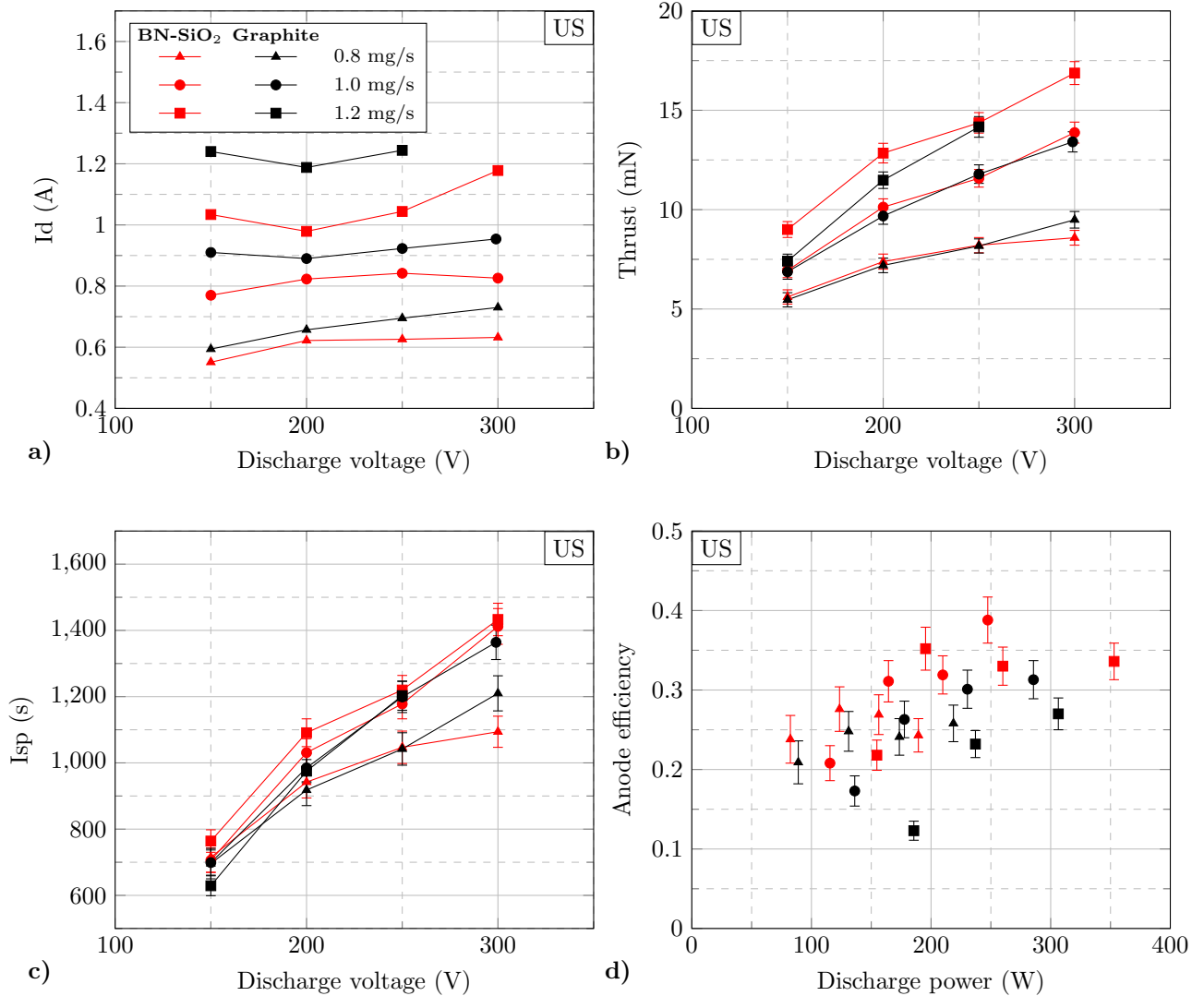


Figure 3: Discharge current (a), thrust (b), anode specific impulse (c) and anode efficiency (d) of the ISCT200-US.

The measured thrust of the magnetically shielded thruster ranges from 4 to 14 mN. As seen in figure 4 b) the thrust of the boron nitride and graphite versions are nearly identical at 250 V and below. A slightly higher thrust is measured with graphite walls but it is within the measurement uncertainty. At 300 V the graphite outperforms the ceramic by a more significant margin.

A similar trend is seen on the specific impulse (figure 4 c). The measured impulse ranges between 550 and 1250 s. The graphite and ceramic versions are fairly similar until the 300 V mark where the graphite has a measured ISP around 10 to 15% higher than the BN-SiO<sub>2</sub>. Contrary to the US-HT

the specific impulse doesn't reach a plateau as the mass flow is increased at constant voltage. This is indicative of a poor propellant ionization.

The magnetically shielded thruster only reaches 25% anode efficiency (figure 4 d). Once again the change of material has little effect on the performances of the MS-HT at lower discharge power. It's only above 300 W that we see a significant advantage for the graphite walls.

While this anode efficiency is rather low compared to classical unshielded Hall thrusters in the same power range (see figure 9), it is comparable to the MaSMi-60-LM1 magnetically shielded Hall thruster built by Conversano[13]. A better com-

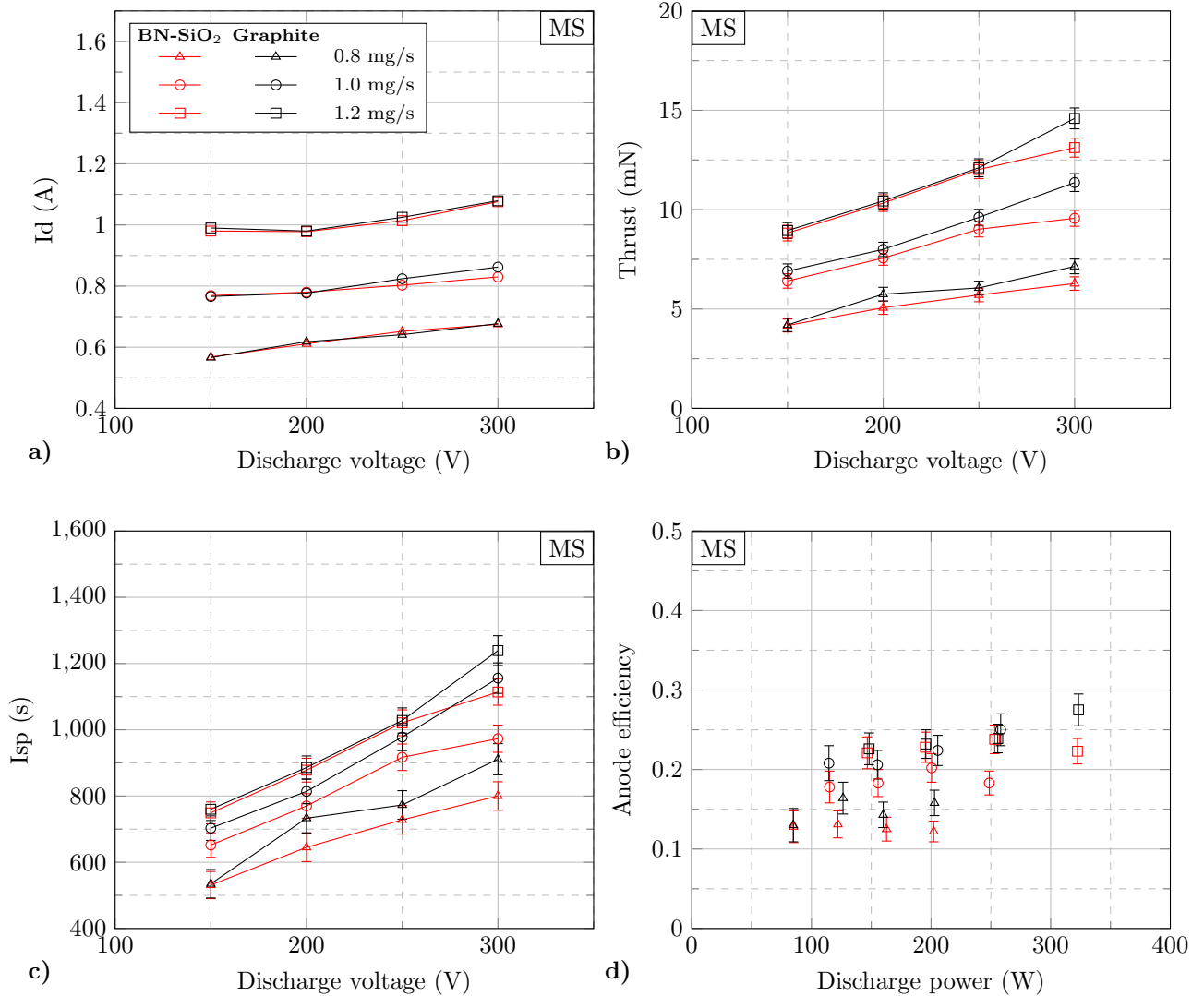


Figure 4: Discharge current (a), thrust (b), anode specific impulse (c) and anode efficiency (d) of the ISCT200-MS.

425 comparison would have been the MaSMi-40 thruster as  
 it is closer in size and intended discharge power, but  
 440 sadly no thrust measurement exists for this MS-HT.  
 This thruster design has also not been optimized for  
 high performance in magnetic shielding.

430 The difference in thrust at higher voltage between  
 the two materials is not explained for now.

#### 4.1.3. Comparison between both thrusters

435 Figure 5 represents the point cloud of all the test  
 cases done during this campaign. It is readily ap-  
 parent that the unshielded thruster has a higher  
 thrust at equivalent discharge power. The differ-  
 450 ence is more pronounced at higher discharge pow-

ers.

This result is reflected in the anode efficiency (fig-  
 ure 6). The US-HT is about 10 points higher than  
 the MS-HT over the whole power range covered in  
 this study.

#### 4.2. Divergence and plume behavior

The divergence angles obtained in the PIVOINE  
 2G chamber show the same tendency as for the pre-  
 vious measurements in the much smaller NExET  
 chamber[21]. With the ceramic walls, the diver-  
 gence of the unshielded thruster is slightly smaller  
 than the MS one. We see here a 3 degrees differ-  
 ence. The divergence angle of the MS-HT is nearly



Table 1: Overview of the data derived from plume measurements. All the cases presented correspond to a 200 V discharge voltage and are not corrected for multiply charged ions.

	$m_a$ (mg/s)	BN-SiO <sub>2</sub>			Graphite		
		$\alpha_d$ (°)	$\eta_I$	$\eta_{prop}$	$\alpha_d$ (°)	$\eta_I$	$\eta_{prop}$
MS	1.0	63	59%	60%	62	59%	63%
	1.2	62	60%	67%	61	60%	68%
US	1.0	60	68%	76%	66	63%	77%
	1.2	59	69%	76%	66	61%	82%

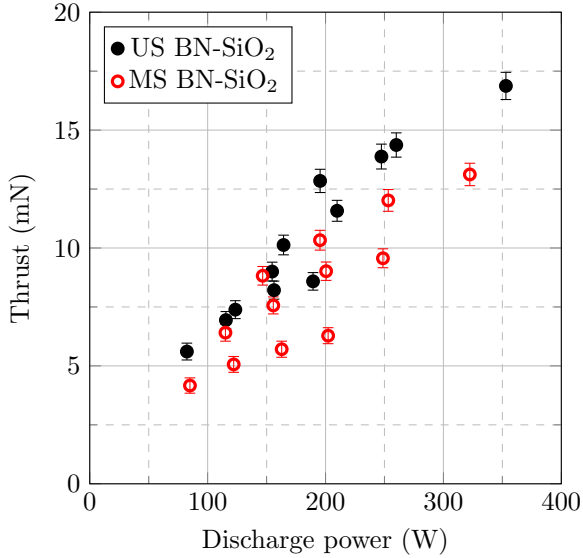


Figure 5: Comparison between the thrust of the US and MS thrusters with ceramic wall

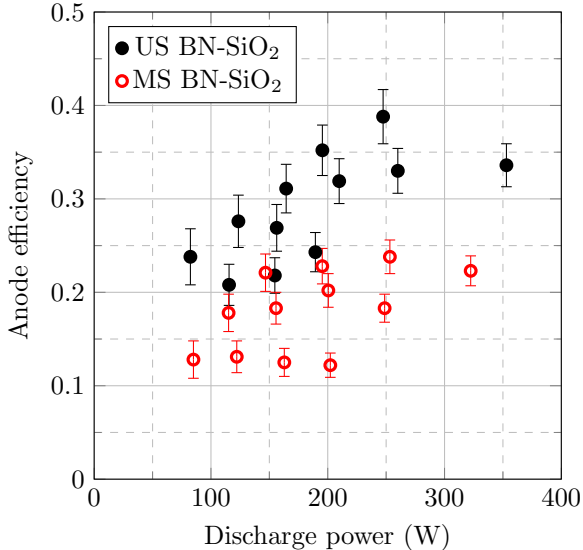


Figure 6: Comparison between the anode efficiency of the US and MS thrusters with ceramic wall

identical with the graphite walls while it increases dramatically in the US case.

Like the previous study[21] the propellant utilization  $\eta_{prop}$  is higher in the US-HT than in the MS-HT. However the difference is more pronounced here (+10 to 15%) than in the other chamber (+7%). This might be due to the factor 10 in background pressure decreasing the smoothing effect of the chamber background plasma. This could also explain the higher divergence angles calculated. A difference is also seen here in the current fraction, a more important electron current is seen in the shielded thruster that was not observed previously.

Comparing the ceramic and the graphite cases, very little variation is seen for the MS-HT. The US-HT on the other hand shows a decrease in the ion current fraction but an increase in the ionized propellant fraction for the 1.2 mg/s case.

#### 4.3. Losses in a shielded thruster

##### 4.3.1. Multiple ionization

As described in section 3.2 we assume that all ions are singly charged to compute the propellant utilization fraction. This approximation is not too far from the truth for traditional US-HT. The beam composition was measured to be 91% Xe<sup>+</sup>, 7% Xe<sup>2+</sup> and 2% Xe<sup>3+</sup> in the plume of the BHT-200[32] which gives a mean ion charge of 1.11  $e$ . In magnetically shielded thrusters such as the H6MS[7] and the MaSMi-60-LM1[13] the proportion of doubly and triply charge ions is much higher. Conversano measured 61% Xe<sup>+</sup>, 25% Xe<sup>2+</sup> and 14% Xe<sup>3+</sup> in the plume of the MaSMi-60 operating at 250 W. This amounts for an average ion charge of 1.53  $e$ .

The high proportion of multiply charged ions in MS-HT is usually explained by the higher electron temperature in this type of thruster due to the reduced electron cooling at the walls[12].

It is tempting to explain the lower performance of the shielded thruster by this overabundance of multiply charged ions. Not only those take more

energy per unit of charge to produce, but they only produce  $\sqrt{2}$  (and  $\sqrt{3}$ ) of the thrust for an equivalent acceleration voltage.

Assuming the ion population described above we can use the ionization energies for the required for the different ionization level to compute the power spent to produce them. This comes out at 13.3 watts per amperes of ion current in the US-HT and 16.3 for the MS-HT. Taking for example the case of the two thrusters at 200 V and 1.2 mg/s xenon mass flow, we can calculate the power spent ionizing the ion current observed. 8.9 W is spent on ionizing the propellant for the ISCT200-US and 9.6 W is used in the ISCT200-MS. The additional energy required to produce those doubly and triply charged ions is clearly not enough to explain the difference in efficiency.

The thrust also depends on the ion charge. Neglecting the divergence and assuming the ions take advantage of 100% of the discharge voltage we can write equations (2) to (5). These equations also assume all the ions are produced at the same location.

As a result for a given ion beam current ( $I_b$ ) a 200 W MS thruster with the ions population described above would produce only 84% of the thrust of an equivalent US thruster. All things being equal this reduces the anode efficiency by 30%. Accounting for the difference in ion beam current for the 200 V, 1.2 mg/s, BN-SiO<sub>2</sub> case the computed thrust for the MS-HT should only be 73% of the US-HT.

At this operating point we measure a thrust of 10.3 mN for the ISCT200-MS and 12.9 mN for the ISCT200-US in the same conditions. This results in a  $80(\pm 4.5)\%$  MS over US thrust ratio. This seems like a reasonable match with the calculation considering the uncertainty in the actual beam composition as well as the beam current.

One might then ask why the H6MS achieves an anode efficiency (0.672) so close to the unshielded H6 (0.682)[7]. First the 6 kW unshielded version of the thruster has a significantly higher fraction of multiply charged ions which adds to a mean charge of 1.27  $e$  while the H6MS version is only at 1.45  $e$ . This means that at equal ion beam current the thrust ratio is 92%. However the ion beam current is actually higher in the MS version (87%) than in the US version (83%). This puts the thrust ratio, only accounting for multi-charged ions and beam current fraction, at 96% which is line with the measured thrust ratio of 95.8%. Of course one should be careful with this kind of approach as it neglects divergence and potential difference in ion energy.

This simple derivation shows that while the thrust of the ISCT200-MS, like other MS thrusters, is penalized by the multiply charged ions, this effect is worsened by the low ion beam current measured in the MS-HT. The main reason for the low ion beam current in the ISCT200-MS seems to be its propellant utilization.

#### 4.3.2. Effect of surface to volume ratio

A striking characteristic of magnetically shielded Hall thrusters is the gap visible between the bulk of the plasma and the walls[33]. Figure 7 highlights those gaps in the ISCT200-MS thruster. This less luminous area is a region of lower plasma density. This was seen with our LIF measurements near the walls[20] where we saw a sharp decrease of the ion density near the walls in the MS-HT. The US-HT on the other hand had a nearly constant ion density. Similarly surface probe measurements in the H6US and H6MS near the exit plane show a decrease of the ions current density from 12 to 5 mA/cm<sup>2</sup>.

We propose that this gap is a path for the neutrals to leak outside the thruster without going through the ionization area. This would explain the poor propellant utilization in the 200 MS thruster compared to the US one. It would also be consistent with the much smaller difference in propellant utilization between the H6MS and H6US.

Assuming a 1 mm gap between the plasma and the walls where no ionization take place, the effective ionization cross section would be reduced by 40% in the ISCT200 case but only by 4% in the H6.

The propellant utilization fraction shown on table 1 are not corrected for multiply charged ions as these fractions are not known for our thruster. Once again we have to resort to figures obtained in the BHT-200[32] for the unshielded case ( $q_{mean} = 1.11e$ ) and the MaSMi-60[12] ( $q_{mean} = 1.53e$ ) for the shielded one. Once corrected for the mean charge, the propellant utilization, in our previously used reference case of 200 V, 1.2 mg/s, is 36% lower in MS than in US. This 36% lower propellant utilization is fairly consistent with the 40% reduction in effective ionization area.

This also fits the the H6MS case. It has a 2% lower propellant utilization than its unshielded counterpart while the effective ionization area is reduced by 4%.

While this assumption of a gap with no ionization is very reductionist, it has the merit of explaining the difference in propellant utilization seen in the

$$T = \dot{m}_I(\eta_{Xe^+} \cdot v_{Xe^+} + \eta_{Xe^{2+}} \cdot v_{Xe^{2+}} + \eta_{Xe^{3+}} \cdot v_{Xe^{3+}}) \quad (2)$$

$$T = \dot{m}_I \times \sqrt{\frac{2e \cdot V_d}{m_{Xe}}} \times (\eta_{Xe^+} + \sqrt{2} \cdot \eta_{Xe^{2+}} + \sqrt{3} \cdot \eta_{Xe^{3+}}) \quad (3)$$

$$T = \frac{I_b}{q_{mean}} \sqrt{2e \cdot V_d \cdot m_{Xe}} \times (\eta_{Xe^+} + \sqrt{2} \cdot \eta_{Xe^{2+}} + \sqrt{3} \cdot \eta_{Xe^{3+}}) \quad (4)$$

$$T = I_b \sqrt{\frac{2 \cdot V_d \cdot m_{Xe}}{e}} \times \frac{\eta_{Xe^+} + \sqrt{2} \cdot \eta_{Xe^{2+}} + \sqrt{3} \cdot \eta_{Xe^{3+}}}{\eta_{Xe^+} + 2 \cdot \eta_{Xe^{2+}} + 3 \cdot \eta_{Xe^{3+}}} \quad (5)$$

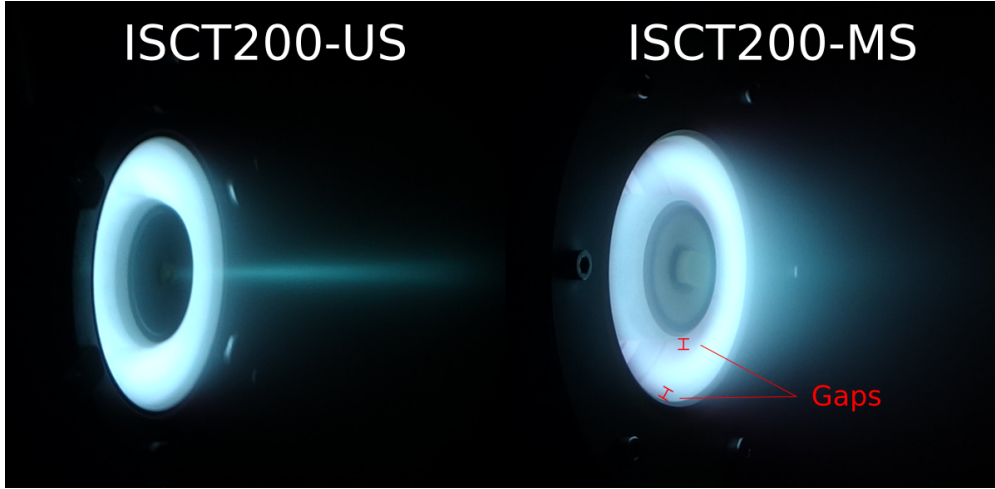


Figure 7: Comparison of the shape of the plasma between the unshielded and shielded thrusters.

smaller thruster but absent in the larger one. It is essentially showing that the reduction in performance in a small MS-HT could be linked to the surface to volume ratio.

Conversano proposed that the poor ionization seen in the MaSMi-60-LM1 was due to non-optimal gas injection design as well as a too weak magnetic barrier[13, 14]. This explanation is unsatisfying in our case as the ISCT200-MS and ISCT200-US have been tested with the same gas injection system, same magnetic field intensity and same magnetic field gradients at the center of the discharge channel. A “leak” of the neutral atoms through the millimeter sized gap between the plasma and the walls has the advantage of providing the right ball-park figure for the dramatic reduction in propellant utilization as well as explaining why this is not seen in larger MS thrusters such as the H6MS, NASA-300MS[34] or HERMeS[8].

#### 4.3.3. Magnetic topology

The last major difference between the MS and US thrusters is the position of the acceleration region. Previous laser induced fluorescence (LIF) spectroscopy measurements have shown that in the MS thruster the electric field is situated a few millimeters outside the discharge channel[20]. This position coincides with the position of maximum magnetic field. As illustrated in figure 8, in a MS-HT in order to get the magnetic field lines going from the exit plane to the anode along the walls (so called “grazing line”) this maximum needs to be pushed downstream. The gap between the exit of the discharge channel and the acceleration region could cause the slow ions to diffuse toward the magnetic poles, thus not contributing to the thrust and causing some of the pole erosion seen on MS-HT[20, 35, 36, 37].

This external electric field can be, as a first approximation, considered to be normal to the magnetic field lines at this position. In a US-HT we take advantage of this effect by creating a “mag-

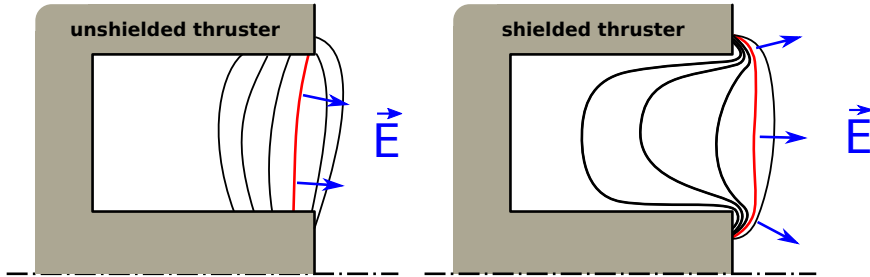


Figure 8: Magnetic field topology and US (left) and MS (right) thrusters. The red line represents the maximum magnetic field intensity as well as the area of maximum electric field. The blue arrows show the direction of the electric field.

netic lens” that focuses the ion beam toward the center axis of the thruster and limits divergence.

The shape of the magnetic field in a MS-HT imposes compromises between beam focusing and wall shielding. This is particularly acute in a small thruster where the magnetic field line curvature must be high in order to reach the anode area.

This highly curved magnetic field with weak magnetic lensing is probably the cause of the higher divergence and hurts performance. This is presumably what Conversano calls “over-shielding” [13, 14]. A compromise “low-erosion” topology, where the grazing lines do not reach as far back toward the anode would probably represent good middle ground between wall shielding and performances. Such a configuration would also certainly reduce the gap between the bulk and the plasma and the walls as well as reduce the curvature of the magnetic field lines near the poles.

## 5. Conclusion

At first glance magnetically shielded Hall thrusters seems to behave the same as classical unshielded thrusters. The change in magnetic field topology has little effect on the discharge current and, as far as kilowatt class thrusters are concerned, have similar performances.

However thrust measurement on the 200 W ISCT200 thrusters shows that the MS-HT has significantly lower thrust and anode efficiency than its US counterpart. Measurements of the plasma plume show that this difference is mainly caused by a poor propellant ionization in the magnetically shielded thruster. The poor ionization is somewhat compensated by the larger fraction of multiply charged ions which results in a similar discharge current.

Poor propellant utilization may be explained by the plasma not filling the entirety of the discharge channel in a MS-HT. Those gaps in the ionization surface create a space for the neutral atoms to escape. Their effects on the thruster performance are all the more important as the thruster is small and they cover a large portion of the discharge channel. They are however negligible in larger thrusters and thus do not impact the performances as dramatically.

This suggests that the full magnetically shielded topology with grazing lines reaching all the way to the anode is probably incompatible with high performances in small low power Hall thrusters. A possible workaround would be to try to direct the neutral atom flow so that they go through the center of the discharge channel.

## Appendix

### 5.1. Low power Hall thrusters efficiency

Table 2: Source of the data presented in figure 9

Thruster	Source
ISCT100 V1	Mazouffre 2018[38]
ISCT100 V2	Unpublished
T-40	Frieman 2015[39]
HT100D	Ducci 2013[40]
PlaS-40	Potapenko 2015[41]
BHT-100	Szabo 2017[42]
BHT-200	Szabo 2012[43]
CAM200-EM	Lev 2016[44]
CAMILA-HT-55	Kapulkin 2011[45]
SPT-20	Loyan 2007[46]
SPT-30	Jacobson 1998[47]
SPT-50	Manzella 1996[48]
MaSMi-60 LM1	Conversano 2017[13]
MaSMi-60 LM2	Conversano 2017[15]

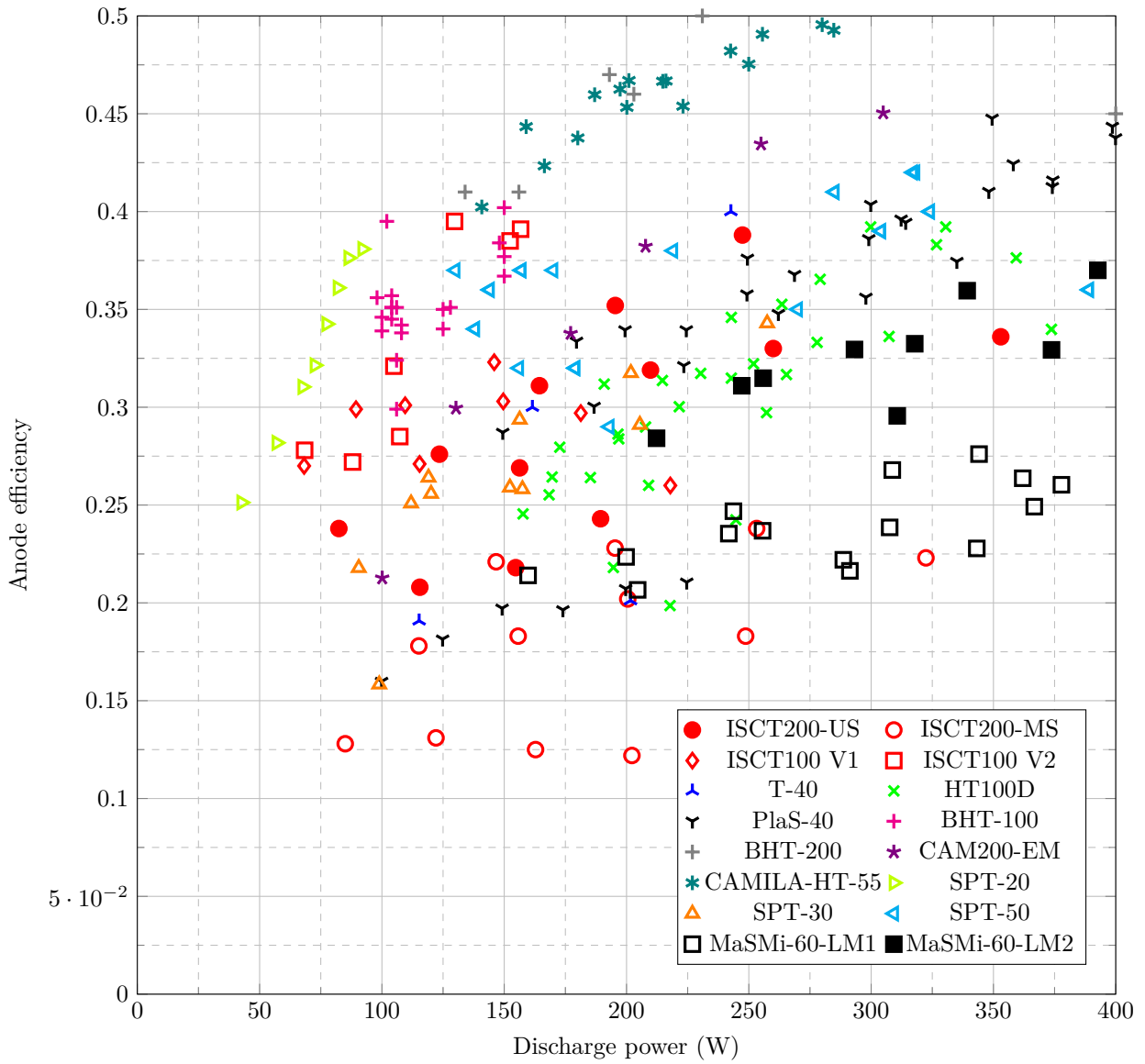


Figure 9: Overview of the anode efficiency of low power Hall thrusters.

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