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mpLBP: A point-based representation for surface pattern description

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ABSTRACT

The Local Binary Pattern (LBP) is a very popular pattern descriptor for images that is widely used to classify repeated pixel arrangements in a query image. Several extensions of the LBP to surfaces exist, for both geometric and colorimetric patterns. These methods mainly differ on the way they code the neighborhood of a point, balancing the quality of the neighborhood approximation with the computational complexity. For instance, using mesh topological neighborhoods as a surrogate for the LBP pixel neighborhood simplifies the computation, but this approach is sensitive to irregular vertex distributions and/or might require an accurate surface re-sampling. On the contrary, building an adaptive neighborhood representation based on geodesic disks is accurate and insensitive to surface bendings but it considerably increases the computational complexity. Our idea is to adopt the kd-tree structure to directly store a surface described by a set of points and to build the LBP directly on the point cloud, without considering any support mesh. Following the LBP paradigm, we define a local descriptor at each point that is further used to define a global statistical Mean Point LBP (mpLBP) descriptor. When used to compare shapes, this descriptor reaches state of the art performances, while keeping a low computational cost. Experiments on benchmarks and datasets from real world objects are provided altogether with the analysis of the algorithm parameters, property and descriptor robustness.

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1. Introduction

In the plethora of distinctive elements of a 3D model, relief and color patterns are crucial aspects for many applications that require a local object characterization. Examples of these applications are the recognition of natural structures, like trees [1], the analysis of artworks styles [2], the classification of fabric patterns [3] or the categorization of objects [4].

Patterns, as meant in this work, are decorative elements that are defined by small corrugations of the surface or simple color arrangements repeated on the surface. We distinguish two types 10 of patterns: geometric patterns that represent small variations 11 on the surface geometry, e.g., repeated, small incisions, chis-12 elings, bumps, etc.; and colorimetric ones, e.g., elements with 13 small painted decorations on the surface. Figure 1 shows exam-14 ples of artworks and design objects characterized by geometric 15 and/or colorimetric patterns. Note that a single element or an el-16 ement repeated only twice (like the nose or the eyes of a statue) 17 do not represent a pattern. Patterns are among the main fac-18 tors when characterizing the type, material and style of natural 19 surfaces and many kinds of object decorations, such as archae-20 ological findings [4]. 21

The analysis of patterns on surfaces is challenging for many reasons, mainly because of the structure of the 3D representation of the object and the difficulty in keeping the computational 24

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Fig. 1. Examples of two surfaces with geometric patterns (a-b) and two surfaces with colorimetric ones (c-d).

cost of the analysis low enough, to be usable in real world cases. The problem of pattern *recognition* on surfaces is still open [5]. 2 In this paper, we tackle the simpler and related problem of Pattern Retrieval: we consider models fully covered by a single 4 pattern and our goal is to identify this pattern. Taking inspiration from the LBP [6, 7], which was introduced to characterize 6 the binary distribution of the intensities on a ring around one pixel of an image, it is possible to extend it to tackle the prob-8 lem of surface pattern retrieval.

To the best of our knowledge, this has been done in recent 10 years by different authors, culminating in three different opera-11 tors: the meshLBP [8, 9], the edgeLBP [10, 11] and the Mean 12 Point Local Binary Patterns (mpLBP for short) [12]. All these 13 methods show that it is possible to tackle the pattern retrieval 14 and classification problem using the LBP, with different degrees 15 of success. Even considering other approaches (e.g., the SIFT + 16 Fisher Vector on circular patches adopted in [13]), these meth-17 ods perform well, marking what is currently the state of the art 18 in this research field. The mpLBP, in particular, yields excel-19 lent performance scores while keeping low the computational 20 cost. The mpLBP operator defines a LBP-based descriptor able 21 to deal with surfaces represented by sets of points. If the sur-22 face is given as a tessellation, this set of points can be the set of 23 vertices, possibly supplemented by additional points sampled 24 on the faces if the number of vertices is low (see Section 3). 25 These points are organized in a kd-tree structure, which makes 26 the navigation in the model representation easier and quicker 27 [14]. 28

This paper extends [12], providing more discussions on the 29 robustness of the mpLBP descriptor, also considering differ-30 ent surface bendings and presenting the mpLBP performance 31 on models obtained from scans of archaeological fragments. 32 33 Moreover, we analyze the efficiency of the descriptor and its characteristics when different neighborhood shapes and sam-34 pling rules are chosen. 35

The remainder of this paper is organized as follows. Sec-36 tion 2 gives an overview of previous research for the retrieval 37 and classification of patterns over surfaces. Section 3 intro-38 duces the punctual operator at the basis of the description, the 39 mpLBP descriptor and presents four possible variants for the 40 ring sampling. Section 4 presents the mpLBP experimental set-41 tings, introducing both the datasets and performance measures 42 and the shape properties adopted for the mpLBP computation. 43 Section 5 presents the results of all the tests performed on the 44 mpLBP. In particular, Section 5.1 shows the retrieval and classi-45 fication performance of the method on two benchmarks [3, 15]

and over a set of scans of archaeological fragments. Section 5.2 focuses on the method robustness with respect to noise and 48 different surface bendings, while Section 5.3 analyzes on the mpLBP performances with different punctual descriptor sampling schemes. Discussions, concluding remarks and feature works are provided in Section 6.

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2. State of the Art

The retrieval and classification of reliefs and textures on surfaces can be seen as an extension to surfaces of the texture image retrieval problem. A large variety of methods for texture image analysis has been proposed in the literature. The main challenge for the detection of specific texture patterns is the recognition of the texture properties robustly to the possible variations [16]. A typical strategy to detect patterns on images is to consider local patches that describe the behavior of the texture around pixels. Examples of statistical descriptions are the Local Binary Patterns (LBP) [6, 7], the Scale Invariant Feature Transform (SIFT) [17] and the Histogram of Oriented Gradients (HOG) [18]. LBP-based methods are very popular and a large number of LBP variants has been proposed [19]. An extended taxonomy of 32 LBP variations and their performance evaluation for texture classification has been proposed in [20] where the LBP variations and 8 convolutional network based features are evaluated over 13 datasets of 2D images. Among the LBP variations considered, the overall best performances are obtained by the so-called Median Robust Extended LBP (MRELBP) that evaluates the descriptor over representative regions instead of single pixels. In terms of absolute performances, the method based on CNN and Fisher Vectors [21] obtains the best results but has a considerably higher computational complexity. In parallel, the aggregation of significant feature points obtained by pooling the point descriptors, e.g. SIFT+Fisher Vectors, was evaluated and obtained significant texture classification performances [16]. Similarly to LBP, the combination of a SIFT-based feature description with Convolutional Neural Networks outperforms the feature-based descriptions on classic benchmarks approximately by 10% at the cost of a higher computational complexity, [21].

For the characterization of patterns over surfaces, two strategies have been adopted so far: (i) a reduction of the problem to an image pattern one, for instance with the projection of the data onto an well chosen plane (image) and the application of an image pattern recognition algorithm to the projected data; (ii) the definition of the pattern description directly on the surface, fact which is not straightforward because it involves handling of three-dimensional data.

As an example of reduction strategy, the method in [1] for tree species classification represents the geometric variations of the tree trunk models with a 3D deviation map over a best fitting cylinder obtained with the Principal Component Analysis (PCA) technique. Then, the cylinder is flattened on a plane and the geometric textures are compared using variations of the complex wavelet transform. Similarly, [2] adopts a height map to project the reliefs and engraves of rock artifacts into an image 10 and classify them. The LBPI and CMC approaches proposed 11 in the SHREC'17 contest [3] adopt, respectively, an image pat-12 tern method over a depth-buffer projection of the surface (LBPI) 13 and the comparison of the principal curvatures in the mesh ver-14 tices using morphological image analysis techniques (CMC). 15 Recently, [13] has proposed to use an opportune parametriza-16 tion around a patch centroid to project the mean curvature val-17 ues into an image and then, to adopt the SIFT + Fisher Vector 18 [16] strategy to compare the parametric images. 19

The Mesh Local Binary Pattern (meshLBP) approach [22, 8, 20 9, 23] proposed the first extension of the LBP description [6] 21 to triangle meshes. The main idea behind the meshLBP is that 22 23 triangles play the role of pixels; there, the 8-neighborhood connectivity of images is ideally substituted by a 6-neighborhood 24 connectivity of the vertices. The role of the gray-scale color is 25 replaced by a function that is meant to capture the main pattern 26 characteristics (usually Gaussian or mean curvatures, shape in-27 dex [24] or mesh color if such information is provided). The 28 edgeLBP [10, 25, 11, 3, 15, 4] performs an LBP evaluation that 29 is based on the rings built over the mesh edges. Adopting a 30 surface-aware characterization the edgeLBP is able to outper-31 form the meshLBP in terms of quality of the query results but 32 it pays a higher computational cost. To overcome the compu-33 tational limitation of the edgeLBP, the mpLBP has been intro-34 duced in [12]. In this case, to speed the extraction of the de-35 scriptor, the mpLBP takes advantage of the kd-tree structure 36 and therefore it deals directly with point clouds. 37

For point clouds, local surface patches can also be con-38 structed by regression using the neighborhood around one point 39 [26, 27, 28, 29] and those patches can be compared in the pa-40 rameter space. In most recent approaches, the surface was lo-41 cally characterized as a digitized height field over the regression 42 surface which may be a plane [30] or a quadric (see [31] for an 43 application to super-resolution). 44

3. mpLBP descriptor 45

This section introduces a statistical descriptor that is global to 46 the shape, that aggregates values of local descriptors computed at a set of positions on the surface. The input surface model can 48 be a point cloud or a triangulation (in the last case, the vertices 49 are input points for the descriptor). 50

The mpLBP procedure can be described by two main steps: 51 the creation of the punctual descriptor (Section 3.1) and LBP 52 evaluations that are further combined to create the mpLBP de-53 scriptor (Section 3.2). In Section 3.3 we discuss the definition 54 and tuning of the parameters of the method. 55

3.1. Punctual descriptor

Let S be a point set embedded in the 3D Euclidean space and a surface property defined on S, $h: S \to \mathbb{R}$, a function defined on S whose values depends on the pattern we want to describe (e.g.: curvature-based values in case of geometric pat-60 terns, a color-based property in case of depicted decorations, 61 etc.). Let us consider the point $\tilde{p} \in S$ and the set $S[\tilde{p}]$ of the 62 points $p_i \in S$ at a distance from \tilde{p} at most equal to R, i.e., $S[\tilde{p}] = \{p_i \in S | d(\tilde{p}, p_i) \le R\}$. We will discuss the choice of the 64 radius R in Section 3.3. Gathering the sets $S[\tilde{p}]$ means visiting the points of S several times. Since 3D models with patterns must be at high resolution (thus described by a high number of points), the way the distance relations between points are com-68 puted must be efficient. In our implementation, these relations are computed using a kd-tree. This structure is computed once per model (with a computational cost of $n \log(n)$).

Points in $S[\tilde{p}]$ are projected on a plane π , obtained using linear regression on $S[\tilde{p}]$. When the density is high enough and if the radius is chosen carefully, that plane may be interpreted as an approximation of the tangent plane. The projected points are sorted in n_{rad} concentric rings based on their distances from \tilde{p} .

The number of rings is given by the parameter n_{rad} , that we call *radial resolution*. Each ring is defined, for $j = 1 \cdots n_{rad}$, as follows:

$$S[\tilde{p}]_j = \left\{ p_i \in S[\tilde{p}] | d(\tilde{p}, p_i) \in [R_{j-1}, R_j] \right\}, \quad R_j = j \frac{R}{n_{rad}}$$

Each $S[\tilde{p}]_i$ is divided in P_i sectors, delimited y some regularly spaced angle values θ_k . Note that P_i may vary along the rings, in order to obtain sectors with similar areas. We call P_i the *spatial resolution*. More formally, we define the sector k of the ring *j* (sector (*j*, *k*) for short) of the point \tilde{p} as:

$$S[\tilde{p}]_{i}^{k} = \left\{ p_{i} \in S | d(\tilde{p}, p_{i}) \in (R_{j-1}, R_{j}], \theta_{i} \in (\theta_{k-1}, \theta_{k}] \right\},\$$

where $\theta_k = k \frac{2\pi}{P_i}, k = 1 \cdot P_j$. Finally, we assign to each sector 77 (j,k) a value $sec(\tilde{p})_{i}^{k}$ as the representative of the function h in 78 that sector. Figure 2 represents the pipeline to build the punctual descriptor. Note that the punctual descriptor can be seen as a 80 feature vector by simply stacking the values of the descriptor 81 on each ring. 82

As it usually happens in the LBP implementations, we ex-83 cluded the computation of the punctual descriptor at points that 84 are close to the boundary of the model (if any). If the boundary of the model is known, it is enough to consider only the 86 points that are at least at distance R from the boundary. In addi-87 tion, if a point punctual descriptor has more than $\frac{1}{4} \sum_{i} P_{i}$ empty 88 sectors, we considered it *invalid* and discard that point. When 89 the intersection of the sphere of radius R with the point cloud 90 generates multiple surface components like those in Figure 3 91 (Right), we consider such a configuration non acceptable and 92 refine the point neighborhood by selecting a smaller value for R. Indeed, for a given model M we assume that the projection 94 onto π is injective and that the surface locally captured by the sphere is locally homeomorphic to a topological disk. More-96 over, we assume the existence of a radius \tilde{R}_{max} , which is the 97 maximum value for the parameter R such that all the points on 98 *M* have an acceptable description. 99

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(a) (b) (c) (d) (e) (f)

Fig. 2. A mpLBP descriptor at point \tilde{p} (marked with a light-blue star in (a)). (b): neighborhood $S[\tilde{p}]$ of \tilde{p} is shown with a dark sphere. (c): point density in $S[\tilde{p}]$. (d): regression plane π , (e): clustering into sectors. (f): resulting punctual descriptor, represented as a 'circular' feature vector.

Fig. 3. Left: illustration of the Gaussian filter adopted to weight the points (in white) in a given sector (in purple). The colors of the Gaussian range from blue (0) to yellow (1). Right: example of a neighborhood that could occur if the radius *R* is larger than \tilde{R}_{max} : points are samples on two discon-



Fig. 4. LBP evaluation for an image. Top-left: in red, the pixel p is highlighted with a dot together with the circle of radius R centered at p. The values of h around p are reported in the bottom-left image.

3.2. Local Binary Pattern evaluation

The punctual descriptor introduced in Section 3.1 is the point
 neighborhood representation to which we apply the LBP encod ing technique.

The LBP paradigm is very popular for images and many ver-5 sions are available [19]. We extend the LBP description to sur-6 faces following closely the image approach [7] which we briefly 7 summarize. For each pixel p, the set of pixels \tilde{p}_i within distance 8 *R* from *p* is called a *ring* of pixels. Visiting each ring from the q top-left pixel in counterclockwise order, a binary array with as 10 many elements as the pixels in the ring is created, adding 0 if 11 $h(\tilde{p}_i) \le h(p)$ and 1 otherwise. Then the LBP value of p is the 12 sum of the numbers in the binary array (it varies from 0 to the 13 number of pixels in the ring). Note that, in this context, it does 14 not matter the order of the comparisons p and all the \tilde{p}_i . The 15 histogram H of the LBP values for all the image pixels is the 16 LBP descriptor of the image. Figure 4 shows this process for a 17 single pixel (Left) and a possible final descriptor (Right). Mul-18 tiple rings can be considered, increasing the size and descriptive 19 capability of the descriptor. 20

In our case we consider \tilde{p} defined as in Section 3.1. If the radius *R* is small enough with respect to the curvature and the

thickness of the object, we can suppose that the rings of the punctual descriptor are locally close to concentric rings using geodesic distance to \tilde{p} . Thus, each sector can be seen as the evaluation of *h* at a sample of the surface. For all the points \tilde{p} in *S*, we define $LBP(\tilde{p})$ the feature vector of n_{rad} elements as follows:

$$LBP(\tilde{p})_{j} = \sum_{k} (str[\tilde{p}]_{j})_{k},$$
$$(str[\tilde{p}]_{j})_{k} = \begin{cases} 0 & if \quad sec(\tilde{p})_{j}^{k} < h(\tilde{p}) \\ 1 & otherwise \end{cases}$$

Then, the mpLBP descriptor of S (mpLBP(S)) is the histogram of the LBP values of the points of S. As a final step, the mpLBP is normalized, i.e., all the entries of mpLBP(S) are divided by the number of points considered in the histogram, enhancing the stability of the descriptor.

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The mpLBP(S) is a $\sum_{j}(P_{j} + 1)$ sized feature vector. Intuitively, we can visualize it as a horizontal concatenation of the rings of the multiple feature vectors in Figure 2(f). In particular, the j-th ring generates a feature vector of $P_{j} + 1$ entries, where $mpLBP(S)_{(j,m)}$ is equal to the number of points \tilde{p} in S such that $LBP(\tilde{p})_{j} = m$ (with $j = 1, ..., n_{rad}$ and $m = 0, ..., P_{j}$).

It is worth mentioning that if the neighborhood of a point is rotated significantly around the normal of the point, its punctual descriptor changes. On the contrary, if the rotation is small, the punctual descriptor is stable; indeed, the Gaussian filter adopted to weight the points is stable under rotations smaller than a fraction of the angular sector. In other words, if the grid of sectors (Figure 2(e)) is slightly rotated, the punctual descriptor does not vary significantly. Moreover, we recall that the LBP value per ring (as intended in this paper) is rotation invariant (because it is a sum of 0 and 1 values on the whole ring), we can conclude that the pattern descriptor of the mpLBP is robust to rotations of the surface. This fact has been verified by applying a random rotation to each point neighborhood: the results indicate almost a perfect stability in this sense. More detail on this fact are provided in Section 5.1.

3.3. Parameter settings

The three parameters of the mpLBP are the radius R (used 48 to set the neighborhood size around each point of S), the radial 49 resolution n_{rad} and the spatial resolution P_i . This is similar to 50 the parameter set of the edgeLBP as described in [10], the main 51 difference being that for the edgeLBP the parameter P is fixed 52 across all the rings. In the following, we present some hints on 53 how these parameters should be tuned. The intuition suggests 54 that the mpLBP ability of detecting a pattern depends on the 55 size of the neighborhood of each point, i.e, the size of the disk

nected parts.

must be related to the pattern size. Moreover, the denser the ring sampling, the more complete information is stored, at the cost of a larger storage size. 3

- R: neighborhood radius shown as a dark bubble in Figure 2(b). R should be set so that neighborhoods contain at least one part of the pattern that we want to describe (e.g.: if the pattern is defined by chiseled circles, the bubble should contain at least one circle entirely).
- n_{rad} : it defines the radial resolution and should be fixed together with P_i (see below). 10

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• P_i : it represents the spatial resolution and varies over the different rings.

Choice of the rings and sampling scheme. The original mpLBP 13 description proposed in [12] adopts as the point description a 14 set of circular rings such that the spatial resolutions P_i guar-15 antee that all the sectors have the same area. For this reason, 16 we selected $P_i = multP(2j-1)$, $multP \in \mathbb{N}_+$. In this case, P_i 17 depends on n_{rad} . This degree of freedom was tuned by the pa-18 rameter *multP* (that replaces the P_i parameters). For instance, 19 in Figure 2(c) the parameters are $n_{rad} = 7$ and multP = 2, which 20 means that $S[\tilde{p}]$ has 7 rings, where $S[\tilde{p}]_1$ has 2 sectors, $S[\tilde{p}]_2$ 21 has 6 sectors and $S[\tilde{p}]_3$ has 10 sectors, etc. 22

However, similarly to the LBP for images, different types of 23 rings may be used. Both the shape (like square, elliptical...) 24 and the sampling scheme (or rather considering only part of the 25 neighborhood) may be changed in order to better suit a given 26 dataset. In general, anisotropic sampling schemes are a valid 27 option in this context. Indeed, the punctual descriptor con-28 verts a patch of a surface into a sort of image. Therefore, it 29 would make sense to straightforwardly adopt a square neigh-30 borhood and its variations, following the image literature on 31 pattern recognition. In general, it is also possible to define var-32 ious scheme variations of the standard punctual descriptor. We 33 focus on different sampling areas of the point neighborhood. In 34 the following, we depict some possible neighborhood and sam-35 pling strategies. In Section 5.3 we quantitatively discuss the 36 performance of these neighborhood choices over a well-known 37 benchmark. 38

• Scheme 1: same concept of the mpLBP punctual descrip-39 tor, but both the descriptor and the sectors are shaped as 40 squares. Figure 5(a) shows how the square neighborhood 41 42 of the points are divided in sectors. The parameters of this descriptor are half the diagonal of the square (a sort of ra-43 dius, thus we still refer to it as R) and the square root of the 44 number of sectors (or rather, the number of sectors along 45 the sides of the square) labelled with pxres. 46

- Scheme 2: same as the mpLBP punctual descriptor, but 47 only alternate sectors are kept on each ring (e.g., sectors 1, 48 3, etc.). In our tests we selected only odd sectors; anyway 49 also even indices could be equally considered. In practice, 50 adopting such a strategy we half the number of samplings. 51
- Scheme 3: similar to Scheme 1, but the first rings are 52 kept in their entirety. The implicit assumption behind this 53 scheme is that smaller rings need a denser sampling. 54

• Scheme 4: same as the mpLBP punctual descriptor, only 55 the sectors with an index *j* such that j = 1 + 4n with $n \in \mathbb{N}$, 56 are considered. Similarly, to the Scheme 1, this strategy 57 aims at decreasing the number of samples. 58

A representation of these variations are showed in Figure 5. The results of these tests are described in Section 4, see Table 5.

4. Experimental settings

The mpLBP was tested on recent benchmarks in order to evaluate its performances. Moreover, with respect to what reported in [12], we run additional tests on the benchmarks considered in the previous word and two additional datasets are considered, extracted from a collection of archaeological fragments.

4.1. Datasets

SHREC17 Benchmark, geometric patterns. The SHREC'17 benchmark dataset [3] on the retrieval of relief patterns is com-71 posed by 720 triangle meshes derived from knitted objects. 72 There are 15 classes of models. Each class was created from the acquisition of the same textile pattern digitized in 12 differ-74 ent embeddings (Figure 6) yielding 180 different models. Then, each model was re-sampled four times (reaching 720 models). Two datasets were derived: the first one is composed by the original 180 models (called *Original Dataset*), while the other is made by all the 720 models (called Complete Dataset). The latter mainly aims at evaluating the overall robustness and stability of methods with respect to different mesh representations.

SHREC18 Benchmark, colorimetric patterns. The SHREC'18 83 benchmark [15] originated from 20 base models without any 84 texture or colorimetric information to which were applied 15 85 gray and white texture each. By combining these, 300 models 86 are obtained [15]. In addition, the luminosity of the textures was 87 modified by using a random value to obtain the same pattern 88 with 20 different shades. Around 30% of the model surfaces 89 are covered by one of the 15 patterns and the remaining part of 90 the surface is only black or only white. The last five patterns 91 are mixed versions of the initial 10 patterns (see Figure 7). Two 92 different datasets are provided: one containing only the models 93 with a single pattern (the set of 200 models characterized by 94 one of the first 10 patterns, called Single pattern dataset) and 95 the other including all the models (all the 300 models, called 96 Complete dataset). 97

GRAVITATE use-case. The GRAVITATE dataset was derived 98 from laser scans of cultural heritage artifacts stored in the Sci-99 ence and Technology in Archaeology Research Center (STARC 100 for short) repository [32]. The fragments came from different 101 collections. They were selected as test beds for the Gravitate 102 EU project [33, 34]. The models are stored as triangulations. 103 Each model is available in several versions, each at a different 104 level of detail, ranging from 50K to millions of vertices. The 105 models are characterized by both colorimetric and geometric 106

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Fig. 5. Various sampling schemes. In (a) we show the grid used to create the the square punctual descriptor (Left) and the final punctual descriptor (Right). In (b,c,d) we highlight the sectors that are considered in Schemes 2,3, and 4.



Fig. 6. The knitted patterns of the SHREC17 contest.

patterns. In case of colorimetric patterns, the RGB values are
stored at each mesh vertex. In addition to the archaeological
documentation, the fragments were grouped by experts and curators according to the types of patterns present on their surface,
thus we use such a classification as a groundtruth to better evaluate our results [4]. By manually cutting out the patterns from
the models that were considered to be significant by the experts,
we created two datasets of patterns on surface [4].

• The *GRAVITATE(geo)* dataset contains 6 classes of geometric patterns, represented in Figure 8. There are 10 models per class, for a total of 60 models. Each patch has around 20*K* vertices.

The *GRAVITATE(col)* dataset contains 10 classes of col orimetric patterns, represented in Figure 8. The number
 of elements per class varied from 4 to 7, for a total of 49
 models. Every patch was made of approximately 40K vertices.

18 4.2. Evaluation Measures

¹⁹ The following evaluation measures are considered to asses ²⁰ our results.

²¹ Nearest Neighbor, First Tier, Second Tier. These measures ²² check the fraction of models in the query's class that appears ²³ within the top k retrievals. By changing the value of k to 1, ²⁴ |C| - 1 and 2(|C| - 1), we consider, respectively, 3 measures: ²⁵ Nearest Neighbor (NN), First Tier (FT) and Second Tier (ST). ²⁶ These values range from 0 (worst result, it means that none of the retrieved elements belong to the class of the query) to 1 (best result, it means that all the retrieved models belonging to the class of the query

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Normalized Discounted Cumulative Gains. The Discounted Cumulative Gain (DCG) derives from the Cumulative Gain, which sums the graded relevance values of all results in the list of retrieved objects of a given query. The DCG assumes that relevant items are more useful if they appear earlier in a query list. Thus, it weights the distances with respect to a relevance value. In the experiments we adopt the nDCG, which is a normalized mean of the DCG computed on each model. We used the implementation proposed in [35].

Average Precision and e-measure. The Precision and Recall are two common measures for evaluating search strategies. Recall is the ratio of the number of relevant records retrieved to the total number of relevant records in the database, while precision is the ratio of the number of relevant records retrieved to the size of the return vector [36]. We consider the mean Average Precision (mAP), which is the area under a precision-recall curve [37]. The e-measure e [38] was also introduced as a quality measure of the first models retrieved for every query. Formally, $e = \frac{2}{Precision^{-1}+Recall^{-1}}$.

4.3. mpLBP settings

The choice of the function h used to build the punctual descriptor is driven by the kind of pattern we want to describe. In the case of geometric patterns, we may consider one of the many existing curvature-based properties, while for colorimetric information we can consider different color embeddings. While the original mpLBP relied on maximum curvature, we test other options: Minimum curvature, Mean curvature, Gaussian curvature and Shape Index. These properties are computed using the Matlab implementation in [39]. This choice was driven by the curvature measure comparisons in [40]. While this implementation works on triangulations, and estimates the curvature on vertices, it is possible to rely on [28, 41, 27] for estimating these quantities for point clouds.

Moreover, we consider the *height-field* (HF for short) as an additional approximation of the surface properties. Indeed, the HF represents a first-order local approximation of the surface. When h = hf, a value is assigned to each point P_i in the neighborhood of P, which is equal to the point-plane distance between the point and the plane π defined in Section 3.1. The



Fig. 7. The 20 base models used in the SHREC'18 benchmark are shown on the left. Each pattern (middle) was applied to all of the base models and changed in terms of their luminosity (examples of the final models are shown on the right).



Fig. 8. One sample per each class of the GRAVITATE datasets. Class labels are given by experts of the field [4].



Fig. 9. Visual representation of how the height-field is computed. Starting from a point P, the plane of linear regression is computed (a) and a scalar value h_f is assigned each point P_j in the neighborhood of P (b). The area represented in (b) is the same as the light blue one on (a), with only P_j represented here for the sake of clearness.

value is negative if $\vec{n}_P \cdot \vec{P_iP} < 0$, where \vec{n}_P is the normal of the point *P*. A point common to the neighborhoods of two different points may have different height values with respect to the two neighborhood regression planes. Figure 9 shows how the HF is computed.

For colorimetric patterns, only the CIELab color-space [42,
43] is considered (the L-channel in particular, which encodes
the luminosity of the colors).

5. Experimental results and discussions

This Section summarizes the mpLB performances over the different datasets with the different settings described in Section 5.1. Then, in Section 5.2 we analyze the robustness of the mpLBP descriptor to surface noise, different bendings a pattern may be embedded in and different neighborhood sampling schema. Finally, Section 5.4 shows the timing comparisons between the mpLBP and the edgeLBP.

5.1. Experimental results

Before discussing the results, it is worth noticing that the evaluation scores of the mpLBP reported in this paper are slightly different than those in [12]: a regression plane alignment bug was found in our previous implementation and it is now corrected.

Performances on the SHREC'17 benchmark. In addition to the23methods of [3] that obtained the best performances, we compare the mpLBP with the edgeLBP [10] and the SIFT-based24method in [13]. Among all the settings tested, the best performing ones are R = 14, $n_{rad} = 7$ and multP = 4. Since most27

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	0	riginal	Dataset			
Method	NN	1-Tier	2-Tier	mAP	e	nDCG
CMC-2	0.633	0.363	0.494	0.390	0.293	0.662
KLBO-FV-IWKS	0.522	0.295	0.412	0.307	0.247	0.603
edgeLBP - run2	0.911	0.689	0.844	0.725	0.590	0.865
T/mC/SIFT/FV	0.872	0.710	0.849	0.741	0.457	0.883
mpLBP - Cmax	0.933	0.706	0.845	0.744	0.449	0.871
mpLBP - Cmin	0.922	0.732	0.861	0.738	0.442	0.862
mpLBP - Cmean	0.911	0.733	0.861	0.763	0.447	0.888
mpLBP - Cmean*	0.917	0.733	0.863	0.761	0.427	0.875
mpLBP - Cmean*	0.922	0.728	0.862	0.763	0.426	0.877
mpLBP - Cgauss	0.939	0.707	0.845	0.744	0.483	0.872
mpLBP - SI	0.911	0.729	0.835	0.749	0.440	0.876
mpLBP - HF	0.672	0.353	0.451	0.431	0.281	0.658
	Co	omplete	Datase	t		
Method	NN	1-Tier	2-Tier	mAP	e	nDCG
CMC-2	0.763	0.272	0.389	0.271	0.261	0.686
KLBO-FV-IWKS	0.986	0.333	0.449	0.339	0.332	0.759
edgeLBP - run2	0.986	0.634	0.780	0.669	0.421	0.902
T/mC/SIFT/FV	0.993	0.712	0.850	0.739	0.647	0.929
mpLBP - Cmax	0.994	0.678	0.820	0.738	0.653	0.931
mpLBP - Cmin	0.997	0.677	0.815	0.733	0.653	0.931
mpLBP - Cmean	0.994	0.702	0.841	0.759	0.665	0.938
mpLBP - Cgauss	0.994	0.678	0.820	0.738	0.653	0.931
mpLBP - SI	0.997	0.688	0.813	0.737	0.650	0.930
mpLBP - HF	0.999	0.383	0.480	0.431	0.419	0.802

Table 1. Results on the SHREC'17 benchmark, both the Original (Top) and the Complete (Bottom) Dataset. Runs marked with * are those which point neighborhood are rotated by a random angle around the normal of the respective point.

of the models in the dataset have a low number of vertices, we resampled them to 40000 vertices using the Remesh tool [44]. Table 1 reports the mpLBP scores together and compares them with the other methods, with respect to NN, FT, ST, e-measure, mAP and nDCG. In this table we also include the results ob-5 tained when testing the independence from the cut of the grid on the neighborhood of the points. We mark with * the runs to which we added to each point neighborhood a small rotation 8 of the tangent parametrization around the point normal (from q 0 to 2π). The results show that adding this rotation does not 10 influence critically the results of our method. 11

The mpLBP scores equivalently or slightly better than the 12 edgeLBP and T/mC/SIFT/FV over the SHREC'17 benchmark 13 on geometric patterns, with small variations depending on the 14 surface property chosen. Overall, over this benchmark, the 15 mpLBP performs well with all the curvature-based properties; 16 in particular, the mean curvature provides slightly better re-17 trieval performances. However, the NN performance over the 18 complete dataset of mpLBP with the height field highlights how 19 this property is able to characterize a model and its re-samplings 20 but it less robust to different surface bendings. 21

Performances on the SHREC'18 benchmark. The performance 22 of mpLBP on this benchmark is compared against those ob-23 tained in [15] and [11]. The parameters settings with the best 24 evaluations are $R = 0.10 n_{rad} = 7 mult P = 1 (set1)$ and 25 $R = 0.14 n_{rad} = 7 mult P = 1 (set2)$. Table 2 summarizes 26 the best scores obtained (more runs and methods are available 27 in [15] and [11]). 28

Over this benchmark, mpLBP and edgeLBP perform equiv-29 alently, even if the time for evaluating the edgeLBP on this 30 dataset is approximately twenty times higher than the mpLBP 31 (details on the computation costs are provided in Section 5.4). 32

	Sin	gle Pat	tern Da	taset		
Run	NN	FT	ST	mAP	e	nDCG
TWB3	0.755	0.502	0.688	0.577	0.455	0.795
V2	0.82	0.51	0.731	0.593	0.481	0.808
edgeLBP-R4	0.915	0.717	0.879	0.766	0.60	0.898
edgeLBP-R5	0.950	0.740	0.892	0.790	0.606	0.911
mpLBP - set1	0.965	0.739	0.862	0.781	0.600	0.910
mpLBP - set2	0.960	0.744	0.864	0.762	0.590	0.900
			•			
	C	Comple	te Data	set		
Run	NN	FT	ST	maP	e	nDCG
TWB3	0.593	0.417	0.564	0.460	0.376	0.711
V2	0.79	0.433	0.594	0.493	0.39	0.753
edgeLBP-R4	0.903	0.673	0.827	0.722	0.557	0.878
edgeLBP-R5	0.923	0.667	0.805	0.727	0.546	0.878
mpLBP - set1	0.903	0.739	0.862	0.668	0.520	0.850
mpI DD cat?	0.007	0 572	0.725	0.620	0.510	0.040

Table 2. Performance scores over the Single pattern dataset and Complete dataset of the SHREC'18 benchmark.

Indeed, to guarantee the decorations were intelligible, the original surfaces were densely sampled (100K vertices, each) and this corresponds to a demanding task for the edgeLBP. On the contrary, this is a good basis for mpLBP because the key issue for its success is that the point cloud is dense enough, i.e., most of the sectors of the descriptors should not be empty.

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Performances on the GRAVITATE dataset. We run the mpLBP on both datasets with 4 different settings. The results are compared with those reported in [4] for edgeLBP on the GRAVI-TATE datasets. In particular, on GRAVITATE(geo) we used the Shape Index as h function, as it is done in [4]. In Table 3, the best mpLBP run we had is compared to the edgeLBP results.

As a general premise, since the dataset classes contain few models (less than 10), even a variation of 0.1 in the scores means that only one model is miss-classified. The performances of the edgeLBP and mpLBP are comparable, with differences that depend on the type of pattern and the quality of the model. This can be observed by the overall performances of the runs. Looking at the single class performances, the NN measures are almost identical, with the edgeLBP being slightly more efficient on the geometric patterns. The opposite is true on the colorimetric ones, where the patterns are more degraded. This may be explained by the fact that since the mpLBP scouts an entire area for each sampling (sector) rather than a single point to code the evolution of the ring properties, it slightly averages the local surface properties simulating a slight smoothing effect. This can be positive in case of noisy colorimetric patterns but it could lead to a confusion between geometric noise and actual small surface variations.

5.2. Robustness of the descriptor

In [12] we already explored the robustness of the mpLBP descriptor to noise. In this work, we also analyzed the robustness of the pattern descriptor of a fixed pattern when the latter lies on surfaces with different bendings. All this robustness analysis are reported in this Section.

Robustness to noise. The popularity of scanning devices that can digitize objects increased the number of acquired 3D mod-69 els available, but not all of them have perfect sensors. Thus,

edgeLBP	settings: n	$n_{rad} = 7, N$	V = 15, R	= 0.6cm		mpLBP s	ettings: n _r	$_{ad} = 5, m$	ultP = 4, I	R = 1 cm	
sidered	NN	FT	ST	e	nDCG	Class Label	NN	FT	ST	e	nDCG
Pattern	1.000	0.722	0.911	0.434	0.934	Feathered Pattern	1.000	0.511	0.767	0.410	0.849
Circles	1.000	0.922	0.978	0.439	0.989	Pattern of Circles	1.000	0.889	0.944	0.439	0.976
als	1.000	0.644	0.756	0.385	0.911	Spirals	1.000	0.544	0.700	0.400	0.870
attern	0.700	0.300	0.367	0.263	0.661	Line Pattern	0.800	0.289	0.444	0.302	0.685
Fringe	1.000	0.467	0.500	0.229	0.804	Smooth Fringe	1.000	0.522	0.533	0.239	0.818
Fringe	1.000	0.400	0.589	0.371	0.773	Hatched Fringe	1.000	0.400	0.500	0.366	0.765
all	0.950	0.576	0.683	0.354	0.845	Overall	0.967	0.526	0.648	0.359	0.827

GRAVITATE(geo) results

GRAVITATE(col) results

edgeLBP	settings: a	$n_{rad} = 5, I$	P = 15, R	= 0.5cm] [mpLBP	settings: n	$_{rad} = 7, P$	= 15, R =	= 0.5cm	
Class Label	NN	FT	ST	e	nDCG] [Class Label	NN	FT	ST	e	nDCG
Guilloche v1	1.000	1.000	1.000	0.171	1.000] [Guilloche v1	1.000	1.000	1.000	0.171	1.000
Six Petals	0.500	0.500	0.767	0.270	0.720		Six Petals	0.500	0.400	0.767	0.270	0.709
Chequer	0.857	0.571	0.738	0.271	0.811		Chequer	1.000	0.714	0.976	0.316	0.924
Striped band	0.800	0.200	0.400	0.222	0.544		Striped band	0.600	0.250	0.500	0.189	0.567
P.o.C. (Painted)	1.000	1.000	1.000	0.171	1.000		P.o.C. (Painted)	1.000	1.000	1.000	0.171	1.000
Lotus and Bud	0.500	0.333	0.583	0.171	0.666		Lotus and Bud	0.500	0.417	0.583	0.143	0.566
Scales v1	0.429	0.310	0.619	0.316	0.579		Scales v1	0.571	0.357	0.643	0.263	0.680
Scales v2	1.000	1.000	1.000	0.171	1.000		Scales v2	0.750	0.333	0.667	0.171	0.673
Guilloche v2	1.000	1.000	1.000	0.171	1.000		Guilloche v2	1.000	1.000	1.000	0.171	1.000
Pattern of Curves	0.500	0.250	0.250	0.086	0.424		Pattern of Curves	0.500	0.167	0.250	0.100	0.427
Overall	0.735	0.582	0.723	0.217	0.758	1 1	Overall	0.742	0.693	0.918	0.211	0.755

Table 3. Results on the GRAVITATE datasets, and comparison with those of the edgeLBP.

acquired data can be corrupted by acquisition noise. Furthermore, objects can be degraded by time or other factors, which can lead to corruption of the patterns that lie on the surface of the object.

Class considered Feathered Pattern

Pattern of Circles

Spirals Line Pattern

Smooth Fringe Hatched Fringe

Overall

Noise in general is an unwanted variation of a signal (the surface, in this case) usually of small scale. Patterns also are usually small, thus the noise is a problem that is worth addressing. We added noise with various amplitudes to some of our test models. Such variations change the h function and as a consequence the whole punctual descriptor. Depending on the 10 pattern nature, we considered different noise addition. The ge-11 ometrical patterns are corrupted with a Gaussian noise on the 12 vertices, based on a parameter λ_{q} , expressed as a percentage of 13 the diameter of the smallest bounding sphere. The values of λ_{ρ} 14 considered are 0.2 and 0.4. See Figure 10 (Top) for an example 15 of mesh degradation. 16

¹⁷ Colorimetric patterns are instead corrupted by adding small ¹⁸ variations to the RGB values stored on the model vertices. Such ¹⁹ variation is bounded to the parameter λ_c , an integer value added ²⁰ to each RGB channel (we assume the three channels to range ²¹ from 0 to 255). For example, $\lambda_c = 5$ added three random offsets ²² in the interval [-5, +5] to each color channel. In our tests, we ²³ used $\lambda_c \in \{5, 7\}$ (see Figure 10 (Bottom)).

The noise tests are run on the SHREC'17 Original dataset 24 for the geometric patterns and on the SHREC'18 Single pattern 25 dataset for the colorimetric one. Results are reported in Ta-26 ble 4. We observe that the performances significantly decrease 27 in presence of heavy noises, while the mpLBP is robust in case 28 of lighter ones. We think that this behaviour derives from the 29 strategy we adopt to evaluate a property in the sectors. Indeed, 30 the use of the weighted mean for each sector balances the small 31 variations of the h function, while it starts being less efficient 32 in case of higher variations (in this case, all the sectors become 33 similar). 34



Fig. 10. Pattern distortion when noise is randomly added. Top row: a geometric pattern is corrupted using increasing Gaussian noise. Bottom row, an increasing random noise is added to each RGB color channel.

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Method	NN	1-Tier	2-Tier	mAP	e	nDCG
mpLBP - set1 Clean	0.917	0.711	0.859	0.743	0.420	0.861
mpLBP - set1, $\lambda_g = 0.2$	0.911	0.693	0.846	0.733	0.380	0.790
mpLBP - set1, $\lambda_g = 0.4$	0.872	0.618	0.769	0.664	0.350	0.753
SHREC'18: Si	ngle Pa	ttern D	ataset,	colorin	netric n	oise
Method	NN	1-Tier	2-Tier	mAP	e	nDCG
mpLBP - set1 Clean	0.965	0.739	0.862	0.781	0.600	0.910

SHREC'17: Original Dataset, geometric noise

Table 4. mpLBP performance for data corrupted with noise. Top: the Original Dataset of the SHREC'17 benchmark, Bottom: Single Pattern Dataset of the SHREC'18 benchmark.

0.653

0.445

0.586

0 4 5 7

0.440

0.355

0.822

0 741

0.514

0.332

0.915

0.75

mpLBP - set1, $\lambda_c = 5$

mpLBP - set1, $\lambda_c = 7$



Fig. 11. Examples of two patterns embedded on surfaces with gradually stronger bendings. The table reports the distances between the pattern descriptor of the pattern embedded on the flat surface and on the bent surfaces. The L^2 norm is used to compute such distances.

Robustness to surface bendings. A very relevant feature of a pattern descriptor on surfaces is its robustness to different bend-2 ings of the underlying surface. To test this, we created a pattern 3 of circlets and applied it to surfaces with more and more severe 4 bendings. These models are reported in Figure 11 (First row). 5 Since they are generated from a synthetic surface and adopting 6 an isotropic bending we are guaranteed that the models possess the same pattern. In the second row of Figure 11, the corre-8 sponding descriptors are showed. A similar test is done using a pattern made up by small crosses (see Figure 11 - Third and 10 Fourth rows). From the results, one can observe that the pattern 11 descriptor changes depending on the embedded pattern. More-12 over, it remains quite close, although not perfectly identical, for 13 the same pattern across the bending changes. This show that 14 the descriptor is more sensible to changes in the patterns it de-15 scribes and far less sensitive to the surface bending. 16

Robustness to different model samplings. In the experiments 17 shown in Section 5.1, the models with a low resolution were 18 re-sampled, increasing the vertex density to reach a reasonably 19 dense representation. Therefore, it is worth exploring the be-20 haviour of the pattern descriptor when it is computed for differ-21 ent sampling density of the same model. We used the SHREC17 22 Original Dataset for this experiment. We selected two of the 23 models of this dataset (one from class 8 and one from class 12) 24 and down-sampled it from 40000 vertices to 3000 vertices, with 25 various steps, using the default sampling scheme implemented 26 in [44]. Figure 12 shows the pattern descriptor computed. It 27 is easy to notice that the pattern descriptor holds its shape and 28 changes when the number of vertices considerably decreases 29 (although in the examples 7000 is still sufficiently stable with 30 respect to the higher samplings we noticed that around 10000 31 vertices is a good quality compromise). This test shows that it 32



Fig. 12. Pattern descriptor robustness to different samplings. The number of vertices of the model is on top of the respective pattern descriptor.

is possible to have similar performances when re-sampling with different vertex resolutions, but it is necessary to have a minimum vertex density in order to have more stable pattern descriptors (in this case, approximately 10000 vertices or more).

Robustness to different choices of the parameters. The choice 37 of the mpLBP parameters $(R, n_{rad} \text{ and } mult P)$ is crucial for the 38 performance of the method because they are related strictly re-39 lated at the resolution a pattern is analysed. Anyway, we noticed 40 that the performance of the mpLBP is quite stable for small 41 variations of the parameters. In other words, slightly chang-42 ing the parameters (all three of them) will not jeopardise the 43 performances of the method. This fact was experimentally con-44 firmed by selecting 27 variations of the best mpLBP run over 45 the SHREC17 original dataset (see Table 1). The performance 46 in terms of NN, FT and ST scores of the mpLBP are reported 47 in Figure 13 for all these 27 settings. On the horizontal axis we 48 report the parameter setting, while the vertical axis represents 49 the performance score (different colours are used for the NN, 50 FT and ST, respectively). The performances are very similar 51 for all the settings. The maximum discrepancy observed across 52 all the evaluation measures is around 0.05, which is very tiny, 53 especially considering that it occurs only once in 27 runs. 54



Fig. 13. The performances of 27 different mpLBP runs on the SHREC17 dataset, with different parameter settings. The dashed lines represent the mean value of the respective evaluation measure.

5.3. Different choices of the ring sampling scheme

We took the four possible variants of the point neighborhood sampling schemes described in Section 3.3 and we evaluated them on the SHREC'17 Original dataset. As shape properties, we considered the height-field as defined in Section 4.3 because of its simplicity and rough shape description and the Mean curvature because it generally performs well over geometric patterns. With reference to the labels defined in Section 3.3. Scheme 1 is computed using R ranging from 7 to 15 and pxres ranging from 10 to 16. To evaluate Schemes 2, 3 and 10 4 we extracted the standard punctual descriptor with parame-11 ters R = 14, $n_{rad} = 7$ and mult P = 4 and we considered only 12 the sectors highlighted in the schemes. In this Section, we re-13 port only the most significant runs. Table 5 summarizes the 14 results of the tests of mpLBP with these settings. In particu-15 lar, when using sampling scheme 1 with h equal to the Mean 16 Curvature, we use R = 10 and pxres = 16, while when using 17 sampling scheme 1 with h = HF, we set R = 7 and pxres = 12. 18 Note that the size of the mpLBP descriptor varies according 19 to the different neighborhood sampling schemes. Looking at 20 the retrieval performances, we notice that mpLBP with scheme 21 1 (with a square-based point neighborhood) performs poorly 22 compared to the other schemes. This is not really surprising 23 because a square-like point neighborhood inserts an orientation 24 and an anisotropic sampling of the model. Unlike images where 25 a square-like neighborhood is compliant with the intrinsic grid 26 structure, for a surface, a circle or a geodesic neighborhood bet-27 28 ter reflect the intrinsic surface metric. Schemes 2 and 3 highlight that other sampling strategies over a circular neighborhood 29 are possible and lead to good performances. On the contrary a 30 too sparse sampling like the one proposed the Scheme 4 jeopar-31 dises the mpLBP performance. These results highlight that the 32 mpLBP technique can be adapted to different schemes and that 33 it is possible to keep limited the size of the descriptor compared 34 to the original mpLBP settings [12] that probably generated a 35 descriptor with redundant information. 36

37 5.4. Computational time

The mpLBP algorithm is implemented in around 200 MAT-LAB lines of code. The most expensive part, in terms of computational cost is the creation of the punctual descriptor, which

SHR	EC'17: O	riginal Dat	taset, scher	ne variant	s	
Parameters	NN	1-Tier	2-Tier	mAP	e	nDCG
Scheme 1 - Mean C.	0.739	0.395	0.534	0.481	0.324	0.705
Scheme 1 - HF	0.794	0.504	0.622	0.560	0.360	0.755
Scheme 2 - Mean C.	0.928	0.707	0.835	0.746	0.447	0.878
Scheme 3 - Mean C.	0.928	0.667	0.804	0.715	0.436	0.861
Scheme 4 - Mean C.	0.856	0.596	0.745	0.658	0.418	0.813

 Table 5. Retrieval results of the various sampling schemes on the SHREC'17 Original Dataset.

is based on a kd-tree. This characteristic allows the mpLBP 41 algorithm to run in a much shorter time if compared, for exam-42 ple, with the edgeLBP, while keeping similarly high evaluation 43 scores. By running both edgeLBP and mpLBP on meshes with 44 different number of vertices (from 5000 gradually to 120000 45 vertices) and different parameter settings, we can see the huge 46 gap between the timings of the two methods (see Table 6). 47 Tests are run on a personal computer Intel Core i7 processor 48 (at 4.2 GHz) with 32Gb RAM. The edgeLBP (as currently im-19 plemented) has the number of sectors per ring constant across 50 all the rings. In order to have a fair comparison, we also set the 51 number of sectors to be constant for mpLBP (i.e., $P_i = P$ with 52 $P \in \mathbb{N}$ fixed). We observed that n_{rad} and P do not affect the com-53 putation times that much. Indeed, the radius size and the num-54 ber of vertices are the biggest bottlenecks. Figure 14 provides another computational time comparison between edgeLBP and 56 mpLBP showing the much more sever increase of the edgeLBP 57 computational cost compared to the cost increase of the mpLBP. 58 These timings are those obtained on the 120k vertices mesh, 59 with R = 4.5, $n_{rad} = 4 P = 15$. We do not report the same trend 60 representation for other mesh and parameters for brevity reasons, but those trends are almost identical to the ones reported 62 (only the time scale (y-axis scale) changes based on the radius).

6. Discussions and concluding remarks

We extended the LBP concept to surfaces represented as point clouds and defined a novel description, called mpLBP. Such a descriptor is able to keep state of the art performance and run more efficiently than its analogous edgeLBP which is based on a surface tessellation, see Section 5.4. Overall, the mpLBP performance is in par or superior (by a thin margin) with the 70



Fig. 14. Computational time trends for the mpLBP and edgeLBP.

5K	R=2.5	R=3.5	R=4.5
p = 4 P = 12	22.04/2.88	16 20/1 22	10.06/1.25
$n_{rad} = 4, F = 12$	15 74/1 50	10.09/1.30	24 54/1 60
$n_{rad} = 7, F = 12$	11.74/1.39	19.91/1.33	24.34/1.00
$n_{rad} = 4, P = 18$	11.40/1.27	15.89/1.48	17.12/1.38
$n_{rad} = 7, F = 18$	10.14/1.95	20.39/1.88	50.18/2.55
10K	R=2,5	R=3,5	R=4,5
$n_{rad} = 4, P = 12$	59.33/4.23	79.09/4.62	92.31/5.09
$n_{rad} = 7, P = 12$	71.69/4.35	95.58/4.93	116.51/5.46
$n_{rad} = 4, P = 18$	52.92/3.95	76.55/4.77	83.54/4.95
$n_{rad} = 7, P = 18$	72.43/5.01	95.86/5.53	140.23/6.25
15K	R=2,5	R=3,5	R=4,5
$n_{rad} = 4, P = 12$	81.13/5.31	118.42/7.48	143.29/8.00
$n_{rad} = 7, P = 12$	107.26/6.63	143.08/7.52	178.01/8.40
$n_{rad} = 4, P = 18$	81.92/5.96	115.85/7.38	128.10/7.49
$n_{rad} = 7, P = 18$	107.83/7.53	143.77/8.19	188.56/9.32
		1	P
30K	R=2,5	R=3,5	R=4,5
30K $n_{rad} = 4, P = 12$	R=2,5	R=3,5	R=4,5 651.99/33.08
30K $n_{rad} = 4, P = 12$ $n_{rad} = 7, P = 12$	R=2,5 341.81/19.90 454.23/23.30	R=3,5 516.53/28.52 618.36/28.36	R=4,5 651.99/33.08 805.07/33.72
30K $n_{rad} = 4, P = 12$ $n_{rad} = 7, P = 12$ $n_{rad} = 4, P = 18$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31
$\begin{array}{c c} 30K \\ \hline n_{rad} = 4, P = 12 \\ n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \end{array}$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25
30K $n_{rad} = 4, P = 12$ $n_{rad} = 7, P = 12$ $n_{rad} = 4, P = 18$ $n_{rad} = 7, P = 18$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25
$30K$ $n_{rad} = 4, P = 12$ $n_{rad} = 7, P = 12$ $n_{rad} = 4, P = 18$ $n_{rad} = 7, P = 18$ 90K	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10 R=2,5	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5
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$\begin{array}{c} \textbf{30K} \\ \hline n_{rad} = 4, P = 12 \\ n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \hline \textbf{90K} \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 7, P = 12 \\ \hline \end{array}$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10 R=2,5 2378.79/109.32 3024.61/122.58	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5 3661.28/158.43 4142.54/157.74	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5 4344.93/196.08 5200.46/194.75
$\begin{array}{c} \textbf{30K} \\ \hline n_{rad} = 4, \ P = 12 \\ \hline n_{rad} = 7, \ P = 12 \\ \hline n_{rad} = 4, \ P = 18 \\ \hline n_{rad} = 7, \ P = 18 \\ \hline \textbf{90K} \\ \hline \hline n_{rad} = 4, \ P = 12 \\ \hline n_{rad} = 7, \ P = 12 \\ \hline n_{rad} = 7, \ P = 12 \\ \hline n_{rad} = 4, \ P = 18 \\ \hline \end{array}$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10 R=2,5 2378.79/109.32 3024.61/122.58 2344.02/110.05	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5 3661.28/158.43 4142.54/157.74 3481.22/160.97	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5 4344.93/196.08 5200.46/194.75 3989.87/179.15
$30K$ $n_{rad} = 4, P = 12$ $n_{rad} = 7, P = 12$ $n_{rad} = 4, P = 18$ $n_{rad} = 7, P = 18$ $90K$ $n_{rad} = 4, P = 12$ $n_{rad} = 7, P = 12$ $n_{rad} = 4, P = 18$ $n_{rad} = 7, P = 18$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10 R=2,5 2378.79/109.32 3024.61/122.58 2344.02/110.05 3034.85/128.34	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5 3661.28/158.43 4142.54/157.74 3481.22/160.97 4145.79/163.19	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5 4344.93/196.08 5200.46/194.75 3989.87/179.15 5704.31/201.03
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$\begin{array}{c} 30K \\ \hline n_{rad} = 4, P = 12 \\ n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \hline \textbf{90K} \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \hline \textbf{120K} \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 4, P = 12 \\ \hline \textbf{120K} \\ \hline n_{rad} = 4, P = 12 \\ \hline \textbf{120K} \\ \hline n_{rad} = 4, P = 12 \\ \hline \textbf{120K} \\ \hline 120K$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10 R=2,5 2378.79/109.32 3024.61/122.58 2344.02/110.05 3034.85/128.34 R=2,5 4314.18/165.65	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5 3661.28/158.43 4142.54/157.74 3481.22/160.97 4145.79/163.19 R=3,5 6612.18/260.30 720123(260.19	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5 4344.93/196.08 5200.46/194.75 3989.87/179.15 5704.31/201.03 R=4,5 8341.62/335.82 0254.40/322.00
$\begin{array}{c} 30K \\ \hline n_{rad} = 4, P = 12 \\ n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \hline 90K \\ \hline n_{rad} = 7, P = 18 \\ \hline n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \hline \hline 120K \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 7, P = 12 \\ $	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 3456.26/25.10 R=2,5 2378.79/109.32 3024.61/122.58 2344.02/110.05 3034.85/128.34 R=2,5 4314.18/165.65 5583.24/189.33 426.02120.22	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5 3661.28/158.43 4142.54/157.74 3481.22/160.97 4145.79/163.19 R=3,5 6612.18/260.30 7812.26/260.18 (596.75/20.25)	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5 4344.93/196.08 5200.46/194.75 3989.87/179.15 5704.31/201.03 R=4,5 8341.62/335.82 9954.04/332.90 725(69)290.25
$\begin{array}{c} 30K \\ \hline n_{rad} = 4, P = 12 \\ n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline n_{rad} = 7, P = 18 \\ \hline \textbf{90K} \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 4, P = 18 \\ \hline \textbf{120K} \\ \hline n_{rad} = 4, P = 12 \\ \hline n_{rad} = 7, P = 12 \\ \hline n_{rad} = 4, P = 14 \\ \hline n_{rad} = 4, P = 1$	R=2,5 341.81/19.90 454.23/23.30 348.93/20.43 456.26/25.10 R=2,5 2378.79/109.32 3024.61/122.58 2344.02/110.05 3034.85/128.34 R=2,5 4314.18/165.65 5583.24/189.33 4236.92/170.22 6502/1409.13	R=3,5 516.53/28.52 618.36/28.36 507.31/28.21 621.50/29.75 R=3,5 3661.28/158.43 4142.54/157.74 3481.22/160.97 4145.79/163.19 R=3,5 6612.18/260.30 7812.26/260.18 6586.75/262.25 700(60/26).21	R=4,5 651.99/33.08 805.07/33.72 583.39/30.31 811.99/35.25 R=4,5 4344.93/196.08 5200.46/194.75 3989.87/179.15 5704.31/201.03 R=4,5 8341.62/335.82 9954.04/332.90 7626.82/309.25

Table 6. Computational times for edgeLBP and mpLBP (in seconds). The top-left cell of each table indicates the number of vertices.

current state of the art, whether these methods are based on engineered and/or learned descriptors. Due to the way the descriptor is evaluated over the rings (the mean of the values of a function on a set of points), the mpLBP remains stable to noise. Indeed, in presence of a small noise intensity that simulates the possible perturbation of a common scanning device, the performances are competitive with the current state of art methods. Moreover, it is robust to different surface bendings and is able to support different sampling schemes, as discussed in Section 5.3.

Other competing methods such as the T/mC/SIFT/FV method in [13] implicitly assumes that the same geodesic 'sphere' centered in every patch is able to parameterize all the models. The sphere radius is unique and can be obtained easily for the SHREC'17 dataset because the patches have comparable size but it is hard to obtain on datasets with models of different size. Moreover, such a single patch parameterization approach is not suitable to deal with datasets containing models with handles and protrusions, like some of SHREC'18 dataset. Indeed, T/mC/SIFT/FV translates the problem into a texture image comparison and requires a resampling with 20K vertices, while mpLBP works directly on the 3D model (mesh or point cloud). From these considerations, T/mC/SIFT/FV can be understood as a global descriptor that down-samples the model vertices as a pre-processing step. On the contrary, the mpLBP descriptor is local and its computation depends on the number of vertices, therefore the time complexities are not directly comparable, while also scoring similar performances.

While most patterns considered in this work are well de-29 scribed by a single scalar function for each point of the model, 30 the possibility of describing patterns based on two or more 31 properties (e.g.: curvature plus color, multiple color channel and so on) is of interest and one of the future research paths. Fu-33 ture reasoning will be devoted to the punctual descriptor used by the mpLBP. Since its resolution can easily be customized 35 and it is not tied to a specific surface property (curvatures, colors, height-fields and so on), the punctual descriptor itself could be used as a feature vector to encode different surface details and/or as the starting point for more advanced local descrip-39 tions. A further extension is the application of the punctual descriptor to the problem of pattern recognition over surfaces. 41 This last is still an open problem, as observed in [5], and a quick and well performing technique such as the mpLBP is a promising contribution towards a possible solution.

7. Acknowledgments

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