

Galactic cartography with SkyMapper – I. Population substructure and the stellar number density of the inner halo

Zhen Wan, Prajwal R Kafle, Geraint F Lewis, Dougal Mackey, Sanjib Sharma,

Rodrigo A Ibata

To cite this version:

Zhen Wan, Prajwal R Kafle, Geraint F Lewis, Dougal Mackey, Sanjib Sharma, et al.. Galactic cartography with SkyMapper – I. Population substructure and the stellar number density of the inner halo. Monthly Notices of the Royal Astronomical Society, 2018, 480 (1), pp.1218-1228. 10.1093/mn $ras/stv1880$. hal-02400866

HAL Id: hal-02400866 <https://hal.science/hal-02400866v1>

Submitted on 9 Dec 2019

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Galactic cartography with SkyMapper: I. Population sub-structure and the stellar number density of the inner halo

Zhen Wan^{1*}, Prajwal R. Kafle², Geraint F. Lewis¹, Dougal Mackey³, Sanjib Sharma¹, and Rodrigo A. Ibata⁴

¹Sydney Institute for Astronomy, School of Physics A28, The University of Sydney, NSW, 2006, Australia

2 ICRAR, The University of Western Australia, 35 Stirling Highway, Crawley, WA 6009, Australia

³Research School of Astronomy & Astrophysics, Australian National University, Canberra, ACT 2611, Australia

 4 Observatoire de Strasbourg, 11, rue de l'Université, F-67000, Strasbourg, France

11 July 2018

ABSTRACT

The stars within our Galactic halo presents a snapshot of its ongoing growth and evolution, probing galaxy formation directly. Here, we present our first analysis of the stellar halo from detailed maps of Blue Horizontal Branch (BHB) stars drawn from the SkyMapper Southern Sky Survey. To isolate candidate BHB stars from the overall population, we develop a machine-learning approach through the application of an Artificial Neural Network (ANN), resulting in a relatively pure sample of target stars. From this, we derive the absolute *u* magnitude for the BHB sample to be ~ 2 mag. varying slightly with $(v - g)_0$ and $(u - v)_0$ colours. We examine the BHB number density distribution from 5272 candidate stars, deriving a double power-law with a break radius of $r_s = 11.8 \pm 0.3$ kpc, and inner and outer slopes of $\alpha_{in} = -2.5 \pm 0.1$ and $\alpha_{out} = -4.5 \pm 0.3$ respectively. Through isochrone fitting of simulated BHB stars, we find a colour-age/metallicity correlation, with older/more metal-poor stars being bluer, and establish a parameter to indicate this age (or metallicity) variation. Using this, we construct the three-dimensional population distribution of BHB stars in the halo and identify significant substructure. Finally, in agreement with previous studies, we also identify a systemic age/metallicity shift spanning ∼ 3 kpc to ∼ 20 kpc in galactocentric distance.

Key words: Survey: SkyMapper – Star: Horizontal Branch – Colour-Magnitude Diagrams – Galaxies: Halo

INTRODUCTION

Our own Milky Way presents us with the most detailed view of a large galaxy structure. In his seminal work, Baade (1954) initially proposed the hierarchical assembly of the Galaxy, picturing that our galaxy has accreted and merged with other galaxies to grow; several key pieces of evidence support this theory, such as the colour gradient in the globular cluster population (e.g. Searle & Zinn 1978). More recently, with high-resolution simulations have revealed the scars that hierarchical merging and accretion will leave on a galaxy, Bullock & Johnston (2005) suggests that our halo should be almost entirely built up from tidally disrupted systems. The different duration and time scale of accretion and merging—in the inner and outer parts of the halos—lead to a picture of younger, discrete substructures superimposed on an older, well-mixed background. Font et al. (2006) suggests that the accretion history of galaxies stands behind the shape of the metallicity distribution of stars in the halo and in surviving satellites: the most-metal rich halo could have accreted a large number of massive satellites, indicating different grow up histories between the metal-rich M31 and the metal-poor Milky Way.

Observations could examine the conclusions from simulations. With the advance of imaging and spectroscopic technologies, a number of extensive surveys of the Galactic stellar halo have been undertaken such as: the Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006); Sloan Digital

[?] E-mail: zwan3791@uni.sydney.edu.au

Sky Survey (SDSS; York et al. 2000); the Sloan Extension of Galactic Understanding and Exploration (SEGUE; Yanny et al. 2009); Large Sky Area Multi-Object Fibre Spectroscopic Telescope (LAMOST; Deng et al. 2012; Zhao et al. 2012) and the Canada-France Imaging Survey (CFIS; Ibata et al. 2017). Among targets in these observations, BHB stars have been proven to effectively indicate Galactic structure (e.g. Sirko et al. 2004a; Clewley & Kinman 2006; Bell et al. 2010; Xue et al. 2011; Deason et al. 2011), kinematics (e.g. Sirko et al. 2004b; Kafle et al. 2012; Kinman et al. 2012; Deason et al. 2012; Kafle et al. 2013; Hattori et al. 2013) and dynamics (e.g. Xue et al. 2008; Kafle et al. 2014). These stars, having evolved off the main-sequence and possessing stable core helium burning, are bright, so that could be seen at large distance; are well-studied in absolute luminosity, so that could be pinned down in 3-dimension space (Fermani & Schönrich 2013). Preston et al. (1991) , an early relative work, found that the average colour of BHB stars shifts on order of ⁰.025 mag within galactocentric distances between 2 kpc to 12 kpc, interpreting this shift as a gradient in age. This shift was examined and extend to ∼ 40 kpc later by Santucci et al. (2015b). A recent research by Carollo et al. (2016) selected ∼ 130,000 BHB stars from SDSS to generate a highresolution chronographic map reaching out to ∼ 50 kpc. This large sample set enables them to identify structures such as the Sagittarius Stream, Cetus Polar Stream, Virgo Over-Density and others, and conclude that these are in good agreement with predictions from ΛCDM cosmology.

With the immense success of the northern hemisphere surveys, a complementary survey of the southern sky become essential. To create a deep, multi-epoch, multi-colour digital survey of the entire southern sky, the SkyMapper project was initiated (Wolf et al. 2018). Recently, the first all-sky data release (DR1)—covering 20, 200 deg² of the sky, with almost 300 million detected sources, including both stellar and non-stellar sources—has been published. In this paper, we make use of the SkyMapper Southern Sky Survey to provide the first detailed population and number distribution maps of BHB stars, exploring and examining the properties of the Galactic halo.

The paper is structured as follows; Sec.2 presents details of the data selection, outlining our approach to the identification of BHB stars from colour-colour relationships drawn from the SkyMapper DR1 Southern Sky Survey. In Sec.3, we present the absolute magnitude calibration of our BHB sample based upon several stellar clusters and parallax separately. We discuss the correlation of BHB stellar ages and metallicity with their SkyMapper colour in Sec.4, and finally, present our southern sky colour/population map and BHB number density distribution in Sec.5. In closing, Sec.6 summarises our results and conclusions.

2 DATA

2.1 Observational Data

The SkyMapper filter set has 6 bands, with its *^r*, *ⁱ* and *^z* bands being similar to corresponding SDSS bands. Its *u* band is relatively bluer than the corresponding SDSS filter, emulating the *Strömgren u* band, while the g band is redder than the SDSS g band. Between these redefined *u* and g bands, SkyMapper has a relatively narrow v band, which is metallicity-sensitive (Bessell et al. 2011). In its DR1, SkyMapper has reached limits of ¹⁷.75, ¹⁷.5, ¹⁸, ¹⁸, ¹⁷.75, ¹⁷.5 mag for its *^u*, ^v, ^g,*r*, *ⁱ* and *^z* band photometry respectively.

The aim is to find the BHB stars in SkyMapper DR1 as much as possible, with the contamination kept as less as possible. Blue Straggler (BS) stars are the primary contamination in BHB sample set selected by colour (e.g. Clewley et al. 2002; Sirko et al. 2004a, and references therein), which cannot be ignored, considering that the ratio of BS stars to BHB stars is $\sim 1.5 - 2.0$ in the inner halo (Santucci et al. 2015a). Additionally, though less significantly, the hot Main Sequence (MS) stars could be mixed up in the selected BHB sample (see later in the colour-colour diagram). To distinguish BHB and BS, as well as MS stars, some earlier works, such as Clewley et al. (2002) and Sirko et al. (2004a), presented a robust method based upon the Balmer H_v and H_δ line profile parameters to cull the contaminants. Though this is not feasible to SkyMapper since it only has the photometric measurement, we applied the method to SEGUE spectrum data and acquired a clean SkyMapper BHB/BS/MS sample by crossmatch in the overlap region of SEGUE and SkyMapper. This sample is then used as a training set to help train an ANN to locate the BHB stars in the SkyMapper colour-colour diagram, which were exerted on the entire SkyMapper DR1 catalogue to isolate candidate BHB stars.

We note that the extinction has been corrected throughout based upon the Schlegel et al. $(1998, \text{ hereafter } S98)^{1}$.

2.2 SEGUE BHB Stars

SEGUE (including SEGUE-1 and SEGUE-2) library contains more than 300,000 spectra, which makes it impossible to profile all stars with limit computational time; hence, before we could select BHB sample from SEGUE, we apply a geometry and a colour cuts to reduce the sample size. In detail, a geometry cut:

$$
Dec. < 15^{\circ} \tag{1}
$$

is applied first, representing the overlap region between SkyMapper and SEGUE. Then we select star within:

$$
0.80 < (u - g)_0 < 1.35
$$
\n
$$
-0.40 < (g - r)_0 < 0.00
$$
\n
$$
\tag{2}
$$

to roughly select BHB stars. These two cuts reduce the SEGUE spectra size to \sim 50,000 stars, on which we exert the line profile selection from Sirko et al. (2004a). We use Sérsic profile to depict H_{γ} and H_{δ} lines by:

$$
y = 1 - A \exp\left[-\left(\frac{|\lambda - \lambda_0|}{b}\right)^c\right] \tag{3}
$$

where A, b and c are three key parameters describe the line shape; y is the normalized line intensity; λ and λ_0 represent

¹ S98 are known to overestimate the amount of reddening, and we exclude the low galactic latitude stars where the extinction is significant. For our sample, the difference of E(B-V) of our sample predicted by the more recent Schlafly et al. (2010, hereafter S10) and S98 is less than ⁰.06 mag (mostly less than ⁰.02 mag) and we employ S98 for consistency with previous studies.

wavelength and central wavelength. Additionally, two more quantities are defined: $D_{0.2}$ is the width of Balmer line at 20% below the local continuum, and $f_m = 1 - A$ is the relative flux at the line core. We extract the H_{γ} and H_{δ} lines profile of all the remained SEGUE stars with Markov Chain Monte Carlo (MCMC; Foreman-Mackey et al. 2013), and apply the cuts:

$$
17 \le D_{0.2}/\text{\AA} \le 28.5
$$

0.1 \le f_m \le 0.3 (4)

on H_{δ} lines profile and:

$$
0.75 \le c_{\gamma} \le 1.25
$$

$$
7.50\text{Å} \le b_{\gamma} \le 10.8 - 26.5 \left(c_{\gamma} - 1.08\right)^{2} \tag{5}
$$

on H_v line profile to select an clean BHB sample set. Figure 1 demonstrates the line profile parameters distribution and the selection we applied, with which we finally end up with 2610 SEGUE BHB stars, as well as 1999 BS stars, and 43281 MS stars.

2.3 Training the ANN to identify BHB stars from SkyMapper

Before we train the ANN and find all the BHB stars in SkyMapper DR1, we crossmatch between SkyMapper and SEGUE with the position difference less than $1.8''$, from
which we find 374 BHB stars 156 BS stars, and 4017 MS which we find 374 BHB stars, 156 BS stars, and 4917 MS stars in SkyMapper. Here in Figure 2, we compare the colour-colour diagrams of BHB/BS/MS stars from SkyMapper and SDSS. SkyMapper colours, $(u - v)_0$ vs $(v - g)_0$ and $(r - i)$ ⁰ vs $(i - z)$ ⁰, are presented; SDSS colours, $(u - g)$ ⁰ vs $(g - r)_0$ and $(r - i)_0$ vs $(i - z)_0$, are shown as comparison. For both SkyMapper and SDSS, we find that BHB stars are indistinguishable from BS stars within red colours diagrams; in the blue colours diagrams, the BHB stars are more clearly isolated from BS stars in SkyMapper than in SDSS—due to the difference between SkyMapper and SDSS filter sets with which we expect to train a reliable ANN.

We randomly select 5% of our sample as a test set, which contains 19 BHB stars, 8 BS stars and 246 MS stars; the training set, with test set excluded, has 355 BHB stars, 148 BS stars, and 4671 MS stars. Then we apply a 2-hiddenlayer ANN with 32 neurons—an algorithm from scikit-learn (Pedregosa et al. 2011) with multi-layer perceptron—with $(u - v)$ ⁰ and $(v - g)$ ⁰ as indicators, which, as in Figure 2, depict the boundary of BHB stars clearly.

When fitting the training set, we assume the probability of a star being BHB star to be zero when the star is located far enough from our sample in colour-colour diagram. The top panel of Figure 3 shows the ANN fitting result, where the probabilities being BHB/BS/MS stars are drawn as contours. We concerned that the selection effect may influence the fitting considering the size of training/test set; to avoid that, we perform the fitting 100 times with randomly selected training/test set. The bottom panel of Figure 3 demonstrates the ratio of successfully identified BHB in each test, which tells us that most tests have the success rate higher than 80%. Later in this study, we select a star if its probability of being a BHB star is larger than 60%, providing good agreement with predicted distributions.

When preparing the SkyMapper data, we select stars

Figure 1. The line profile parameters extracted from SEGUE with the BHB selection criteria (thin dash lines) from Sirko et al. (2004a). In each figure, we colour the BHB stars that meet the criteria blue; colour the BS stars green and the MS star red. Upper: The distribution of $D_{0,2}$ and f_m of H_δ line (see the definition in Sec.2.2). The thick dash lines divide the figure into three parts: BHB, BS and MS regions. We use two thin-dash-line boxes to indicate where BHB and BS stars concentrate. Bottom: The distribution of H_{γ} line profile parameters: c_{γ} and b_{γ} . The dash lines outline the region where BHB stars locate, which is clearly isolated from BS stars. The grey points represent MS stars.

whose latitude $|b|$ is larger than 25° to avoid contamination from the Galactic disk. Additionally, following photometric quality labels are considered:

$$
nima flags = 0,\nflags = 0,\nngood > 1,\nngood-min > 1 and\nnch.max = 1
$$
\n(6)

to ensure a clean and reliable dataset. The photometric uncertainties in the u, v and g bands are shown in Figure 4, which clearly shows that most stars in our sample have photometric uncertainties smaller than ⁰.1 mag.

In total, the ANN selected 16970 BHB stars from SkyMapper DR1. We present their colour distribution in Figure 5, where probabilities of the stars being BHB stars

4 Z. Wan et al

Table 1. An example table of the BHB/BS/MS sample set drawn from SkyMapper. The first column is the SkyMapper object ID, which can be used to locate stars. The second column is the corresponding Spectral ID in SEGUE, in the format of PLATE-MJD-FIBER. The third and fourth columns give the location of the star in J2000 from SkyMapper. The fifth to tenth column presents the SkyMapper u, v and g bands photometric result and uncertainty, which are used as an indicator for classification. The last column is the star type as determined as part of this study.

Object id	SDSS SPECID	R.A.	Dec.	u_{psf}	$e_{u_{psf}}$	v_{psf}	$e_{v_{psf}}$	g_{psf}	$e_{g_{psf}}$	Type
68139182	0513-51989-0528	174.654	3.149	16.602	0.009	15.820	0.005	15.133	0.014	BHB
47695470	2057-53816-0126	124.320	-0.469	15.475	0.003	14.835	0.012	14.222	0.010	BHB
67098280	2716-54628-0474	209.700	-8.977	14.988	0.024	14.064	0.007	13.683	0.006	BHB
47066082	2806-54425-0124	122.583	-8.684	15.014	0.006	14.395	0.027	13.819	0.021	BHB
47066563	2806-54425-0259	122.251	-8.599	15.596	0.026	14.861	0.019	14.199	0.018	BHB
46953790	2806-54425-0378	121.941	-6.800	16.541	0.020	15.744	0.007	15.142	0.009	BHB
100270164	0922-52426-0571	231.901	-1.435	17.774	0.035	16.961	0.078	16.439	0.021	BS
100910930	0924-52409-0281	236.479	-1.223	17.158	0.042	16.527	0.055	15.828	0.005	BS
5347974	0926-52413-0408	335.443	-0.123	18.089	0.243	17.712	0.026	17.092	0.013	BS
48442794	0984-52442-0259	129.310	4.299	16.471	0.029	15.870	0.028	15.156	0.006	BS
48434506	0990-52465-0452	129.713	3.896	16.644	0.014	15.838	0.012	15.294	0.002	BS
65406019	2178-54629-0442	182.693	-0.233	16.254	0.011	15.916	0.011	15.306	0.009	ΜS
65396598	2178-54629-0512	181.608	-0.566	18.110	0.054	17.478	0.052	16.848	0.006	MS
65393432	2186-54327-0437	180.421	-0.652	16.958	0.027	16.628	0.034	15.715	0.004	$\overline{\rm MS}$
68375791	2198-53918-0007	182.443	0.938	16.047	0.017	15.729	0.011	14.945	0.004	MS
65430024	2198-53918-0027	184.064	-0.295	17.640	0.018	17.378	0.078	16.427	0.008	ΜS

are colour coded. The training set and selected BHB stars are available online as supplementary material.

3 DISTANCE CALIBRATION

BHB stars are wildly used as standard candle (see references in Sec.1); the actual absolute magnitude of each BHB star is influenced by the properties of the stellar envelope, particularly the metallicity and temperature (e.g. Wilhelm et al. 1999; Sirko et al. 2004a; Fermani & Schönrich 2013), which also vary the colour of BHB stars. We measure BHB stars absolute magnitude in SkyMapper photometry with two independent methods: calibrate the absolute magnitude with stellar clusters; and with Gaia DR1 parallax (Gaia Collaboration et al. 2016a,b). Following in this section, we present the details of each method.

3.1 Scaling relation from Clusters

The distances to globular clusters are reliable due to many aspects: the globular clusters are compact so that the distance dispersion per system is negligible, and varied distance measurements are feasible to globular clusters like by RR Lyrae stars and isochrone fitting. The trustful distance inspires us to calibrate the absolute magnitude of BHB stars with well studied globular clusters.

For this study, we choose four fiducial globular clusters as distance calibrators: NGC5139 (ω Centauri), M22, NGC6397 and M55. They are all located at roughly ∼ 10 kpc with respect to the Sun, each possessing well-measured distance moduli. Here we adopt four latest work on the distance moduli of the above four clusters: Braga et al. (2018) use RR Lyrae stars to constrain NGC5139's distance and extinction; Kunder et al. (2013) also use RR Lyrae stars for M22; Mc-Namara (2011) takes the mean of the results from RR Lyrae

Table 2. The four globular clusters used as the distance calibrators in this study. The first column presents their name, while the second is their extinction and the last column is their distance modulus. The distance to NGC 5139 (ω Centauri), M22 and M55 are calculated based on RR Lyrae stars where NGC 6397 is based on main sequence fitting. The distance moduli (DM) are extinction corrected.

Name	$E(B-V)_{SFD}$ / mag	DM / mag
NGC5139	0.13	13.67 ± 0.04
M ₂₂	0.32	12.67 ± 0.12
NGC6397	0.19	11.89 ± 0.11
M55	0.14	13.62 ± 0.05

stars and δ Scuti for M55; Brown et al. (2018) calibrates the distance for NGC 6397 through trigonometric parallax. Table 2 presents the resultant extinction and distance moduli of the four clusters used in this study.

We employ the trained ANN to select BHB stars within $1^{\circ} \times 1^{\circ}$ regions that centred at each cluster. The crowding issues could be crucial at the centre of globular clusters, which we avoid by requiring the PSF photometric quality being better than 0.9 so that most stars in the centre of the clusters are ignored. Following this, we applied the adopted distance moduli to each field to calculate the absolute magnitude of our sample and assemble them in Figure 6, where the BHB stars concentrate around $M_u = 2$ mag, with some foreground and background stars dispersed.

The absolute magnitude in Figure 6 varies slowly with colour, which is what we expect for old BHB stars. To describe that, we use a MCMC (Foreman-Mackey et al. 2013) routine (see the parameter probability distribution in Fig-

Figure 2. Comparison of the BHB/BS/MS colour-colour distributions for SDSS and SkyMapper photometry focussing upon $(g - r)_0$ versus $(u-g)_0$ and $(i-z)_0$ versus $(r-i)_0$. The dashed rectangle in the upper-left panel indicates the colour cut that selects BHB stars in the SDSS colour-colour diagram. In the upper panels, we compare two blue colours. BHB stars and BS stars are more clearly separated in SkyMapper colours. The bottom panels present the distribution of BHB/BS/MS stars in two red colours. Clearly, in the red colours, the BHB and BS stars are indistinguishable.

ure 7) to fit the distribution with a simple linear function:

$$
M_u = p_0 + p_1 \times (v - g)_0
$$

\n
$$
p_0 = 2.14^{+0.19}_{-0.19}, \ p_1 = -0.34^{+0.50}_{-0.49}
$$
 (7)
\nHere in this fitting, we exclude foreground and background

stars by selecting stars between $1.5 \leq M_u \leq 2.5$, which is a broad cut to encompass the entire BHB population as shown in Figure 6.

We compare the absolute magnitude inferred from this fitting result with the original value from cluster calibration, and in Figure 8, we present the residual against inferred absolute magnitudes. The rms of the residual is 0.124 mag, corresponding to a distance uncertainty of 5%. We assume the intrinsic uncertainties—like the actual properties and environment of each star, the size of the globular clusters—are included in above 5% distance uncertainty; additionally, we

Figure 3. Upper: The probabilities for each type overplotted on the scattered test set, where BHB stars are in blue. BS stars are in green, and MS stars are in red. We adopt the resulting classification if the probability is larger than 60%. Several BHB stars in the test set reach into the to BS/MS region, but the adopted BHB region is relatively clean. bottom: The success rate of the successful identification of stars as the result of 100 tests with the ANN and different test sets and training sets. This success rate peaks at 0.8.

mulled over the clusters distances uncertainty due to differing approaches and found it beyond the scope of this paper. In considering the potential influence on our the final results, we adopt another 5% systematic distance error (corresponding to ⁰.124 mag, assuming they are at the same scale of the rms) into our final calculations.

Equation 7, as well as the sky position, locate each BHB star in 3-dimensional space. We present the heliocentric radial number distribution of the BHB stars from our sample in Figure 9, where they extend to ∼ 11 kpc.

3.2 Scaling from Gaia DR1 Parallax

Parallax is the most straightforward way to determine distance, which has been part of Gaia project (Gaia Collaboration et al. 2016a,b). Given the overlap between Gaia and

Figure 4. Normalised uncertainty distribution for photometry in the u, v, g bands. Most stars in our data sample have photometric uncertainty smaller than ⁰.1 mag.

Figure 5. BHB stars from SkyMapper selected by our trained ANN. The probability of each stars being BHB star is presented by colour. Stars are concentrated at $((u - v)_0, (v - g)_0)$, where the probability of being BHB stars is the highest.

the SkyMapper footprints, we searched for BHB stars with parallax measured by Gaia DR1, and further determine the absolute magnitude for those BHB stars. This acts as an independent measurement, complementing that from the clusters calibration.

We found 270 BHB stars with parallaxes listed in Gaia DR1, combined SkyMapper photometry, whose absolute magnitudes were calculated with:

$$
M = m + 5\log_{10}(0.01 * \varpi)
$$

$$
\sigma_M = 5\frac{\varpi}{\ln 10} \times \sigma_{\varpi}
$$
 (8)

The distribution of the absolute magnitude of BHB stars calibrated with Gaia parallax and clusters are presented in Figure 10. We find a single peak at ∼ 2 mag for both distributions while the result from Gaia disperses relatively larger due to parallax uncertainties. From Equation 8, we

Figure 6. The CMD of stars in NGC5139 (blue), NGC6397 (green), M22 (orange) and M55 (red) with uncertainties marked. Stars that belong to these clusters concentrate around M_u = 2 mag, and foreground and background stars sit distinct from this sequence.

Figure 7. The colour - absolute magnitude fitting result. The most likely values and their 1 σ ranges are marked in titles.

find the absolute magnitude uncertainty from parallax is σ_{m_0} = 1.46 mag. No prominent second peak means that there is no distinct different population of stars in our select BHB sample set.

4 COLOUR-COLOUR RELATIONSHIP FOR BHB STARS

While their luminosities will be roughly constant, the temperature, and hence the colour of old BHB stars will be

Figure 8. The difference of inferred absolute magnitude from clusters and the fitted absolute magnitude. The majority of the deviations are less than ⁰.2 mag.

Figure 9. The number distribution of BHB stars from our sample in logarithm space. The sample covers heliocentric distance $r <$ 11 kpc.

influenced by their metallicity and envelope mass: metalrich BHB stars will be cooler since it increases the opacity of the stellar envelope; different envelope masses, resulted from processes such as mass loss in the RGB phase, will further vary the temperature of a population of BHB stars.

To investigate how the physical properties of BHB stars influence their photometric properties, previous studies employ stellar-evolution code to derive the correlation between BHB colour and age (e.g. Santucci et al. 2015b, with the MESA isochrone (Paxton et al. 2011, 2013, 2015)). For the work presented here, we generate a series of MIST (MESA Isochrone and Stellar Track, Dotter 2016; Choi et al. 2016) isochrone from $[Fe/H] = -4$ to $[Fe/H] = 0.5$ with Kroupa initial mass function (IMF; Kroupa 2001). We select those stars that are:

- On the core helium burning branch
- Core mass larger than 10% of stellar mass

Figure 10. The distribution of stellar absolute magnitudes derived from Gaia parallaxes (blue) and from the cluster calibration presented in this paper (green). Both distributions peak at ∼ 2 mag, while the results from Gaia possess a larger spread $(\sigma \sim 1 \text{ mag})$ due to parallax uncertainties. The 16th to 84th distribution intervals are indicated with dashed lines.

- Effective temperature of ⁷⁰⁰⁰*^K* < *^T* < ¹³⁰⁰⁰*^K*

These selections exclude massive core helium burning stars and red horizontal branch stars. In Figure 11 we present the selected MIST stars in terms of $(u-v)_0$ vs $(v-g)_0$ colours, colour-coded with metallicity (upper panel) and age (lower panel) respectively. These demonstrate that $(u - v)_0$ colour is sensitive to the properties of the BHB stars, with metal-poor/older stars being bluer in $(u - v)_0$ colour, but clearly age and metallicty are degenerate.

Given that there is not a simple relationship for BHB stars in this colour-colour space, we consider a simple reparametrization of the properties seen in Figure 11. For this, we define the quantity $(u - v)_0 + 5 * ((v - g)_0 - 0.35)^2$, to indicate the different properties with the red line in each indicate the different properties, with the red line in each panel denoting a fiducial case where $(u - v)_0 = -5 * ((v - g)_0 (0.35)^2 + 1.2$. A larger value of this quantity indicates more motel rich/vouncer BHBs, while conversely a smaller value metal-rich/younger BHBs, while conversely a smaller value indicates a metal-poor/older population. This relationship will be used in the discussion of the results of this paper, to show metallicity/age variability through the stellar halo as seen in the southern sky.

5 RESULTS

5.1 Number Density Distribution

The stellar number density distribution of the Galactic halo is thought to trace the accretion history of the Galaxy, and there has been a number of key recently studies using different indicators to depict the profile. For inner Galactic halo, Xue et al. (2015) used RGB stars to find a power-law index $\alpha_{in} = 2.1 \pm 0.3$ and flattening $q_{in} = 0.70 \pm 0.02$, with a break radius $r_s = 18 \pm 1$ kpc; Pila-Díez et al. (2015) found a steeper $\alpha_{in} = 2.5 \pm 0.04$, $q_{in} = 0.79 \pm 0.02$ ($r_s = 19.5 \pm 0.4$ kpc) with MSTO stars; a even steeper stellar halo of $\alpha_{in} = 2.8 \pm 0.4$, $q_{in} = 0.7$ (fixed) ($r_s = 28.5 \pm 5.6$ kpc) were found by Faccioli

Figure 11. The colour-colour distributions of BHB stars drawn from MIST isochrones with $-4 <$ [Fe/H] < 0.5 , colour-coded in terms of metallicity (upper panel) and age (lower panel); these clearly reveal colour-metallicity/colour-age correlations. Metalpoor/old stars are bluer $(u - v)_0$ colour, while metal-rich/young stars are redder. To represent the observed correlation, we define the quantity, $(u - v)_0 + 5 * ((v - g)_0 - 0.35)^2$ represented as a red
line in both panels line in both panels.

et al. (2014) with RR Lyrae Stars; BHB stars were used as a tracer by Deason et al. (2011), which found an intermediate $\alpha_{in} = 2.3 \pm 0.1$, $q_{in} = 0.59 \pm 0.03$ ($r_s = 27.1 \pm 1$ kpc).

It is insightful to examine the BHB halo number density with our sample derived from Figure 9. To do this, we first select stars with Galactic altitude $|Z| > 4$ kpc to avoid contamination from the disk and $u < 17.1$ mag to avoid incompleteness issues. This finally selects 5272 BHB stars, with

Figure 12. The number density of BHB stars as a function of galactocentric distance. Dashed lines represent the best fitting parameters, whereas the grey regions represent the uncertainty of this fit. We identify a break at $r_s = 11.8 \pm 0.3$ kpc, and within the break radius, the power law index is $\alpha_{in} = -2.5 \pm 0.1$. Outside of this radius, the power law index is $\alpha_{out} = -4.5 \pm 0.3$

which we calculate the stellar density by

$$
\rho(r) = N(r)/\epsilon(r)
$$

$$
r^2 = X^2 + Y^2 + \left(\frac{Z}{q}\right)^2
$$
 (9)

where $N(r)$ is the number of stars at r , $\epsilon(r)$ is the surface area at radius *r* covered by our sample, and *X*, *Y* and *Z* are galactocentric coordinates of the stars, and *q* represents a flattening of the distribution.

With Equation 9, we find a break in the number density profile around $r = 11$ kpc; to depict the profile, we run an MCMC routine (Foreman-Mackey et al. 2013) with a double power law and a fixed *^q* ⁼ ⁰.⁷⁶ (consistent with star counts at high galactic latitude (see Sharma et al. 2011, and reference therein)). Figure 12 demonstrates the profile and the MCMC results: the best fit break radius is $r_s = 11.8 \pm 0.3$ kpc; within the break radius, the power law index is $\alpha_{in} = -2.5 \pm 0.1$, while the index beyond the break radius is $\alpha_{out} = -4.5 \pm 0.3$.

5.2 Colour Distribution

In the following, we present the colour (the redefined quantity in section 4) distribution of BHB stars in the Galactic halo as revealed by SkyMapper, in particular focusing upon the large-scale variations and inhomogeneities in the BHB population.

To obtain an overview of the colour distribution, we create a binned map with the bin size of 1kpc^2 , and apply a Gaussian smoothing with kernel $\sigma = 2$ pixel length. In Figure 13 we present the distributions in the X-Z, X-Y and Y-Z Galactic planes: most stars in the centre are relatively blue,

which are either old or metal-poor; superimposed upon this background, colour fluctuations are clear—those substructures are relatively young or metal-rich.

With a rough estimation from Figure 11, a change of 0.1 mag in colour corresponds to a change of \sim 3 − 4 Gyr in age or [∼] ⁰.⁵ *dex* in [Fe/H]. That implies that in the concentration of old/metal-poor stars, there still is an age fluctuation [∼] 1 Gyr or metallicity fluctuation of [∼] ⁰.¹ *dex*, with a scale of \sim 1 kpc.

The lower right panel of Figure 13 presents the distancecolour diagram, where we saw a colour shift of ⁰.05 mag in the distance range 0−15 kpc, indicating a systematic metallicity ([∼] ⁰.2*dex*) or age ([∼] ¹ [−] 2 Gyr) change outwards, and in agreement with the results from Preston et al. (1991).

6 DISCUSSION AND CONCLUSIONS

SkyMapper is providing us with a new view of the southern sky, with which, in this paper, we present a new colour map of the Galactic halo distribution of BHB stars. The BHB stars in the SkyMapper colour-colour diagram are separated from other stars so that it is easier to isolate the target stars with the ANN, which is more straightforward than that applicable to SDSS since SkyMapper has a bluer and narrower filter set. With this, future data releases of SkyMapper offer great promise for providing a precise number density profile and detailed maps of the colour-age/metallicity distribution of the halo. Using the current version of SkyMapper we have reached following conclusions with BHB stars:

We calculate the absolute magnitudes of BHB stars based upon several well measured globular clusters. These span a narrow range $~ M_u = 2$ mag, varying slightly with colour; and the dispersion of the magnitude of BHB stars is ⁰.124 mag. Incorporating our adopted systematic distance uncertainty of 5%, the overall distance uncertainty increases to ∼ 8%. This change does not significantly influence the conclusions of this paper, with very little influence on the colour distributions and other presented properties. We note for completeness that the largest resulting impact is an increase of the uncertainty of the outer power law index by $~\sim 0.1.$

As a comparison, we also derive the absolute magnitude of a subset of BHB stars with a measured parallax from Gaia DR1. Though they have a different dispersion, we find these two methods give the same result within the uncertainties. Since the averaged absolute magnitude of BS stars is ∼ 2 mag fainter than BHB stars (Deason et al. 2011), we expect the absolute magnitude of BS stars from Gaia should peaks at $M_u = 0$. As no such peak is apparent, it is clear that our selection has produced a relatively clean sample of BHB stars.

The BHB properties, in particular, mass, metallicity and age will influence its colour, and to consider the colourcolour properties of BHB stars, we generated synthetic stellar samples using the MIST isochrones. From these, it is clear that the colour influences due to age and/or metallicity cannot be uniquely distinguished from photometric data only. Our conclusions, therefore, reflect potential variation in either, or both, of these quantities.

We estimate the halo stellar number density based on BHB stars; found a break at galactocentric distance r_s

Figure 13. The stellar halo distribution of the quantity $(u - v)_0 + 5 * ((v - g)_0 - 0.35)^2$, taken as indicating age/metallicity variations, with substructures being clearly visible Lower (blue-purple) values of this quantity wh with substructures being clearly visible. Lower (blue-purple) values of this quantity, which represent metal-poor or old populations, are concentrated towards the Galactic Centre with some clusters of younger or metal-rich (coloured red) located at the outskirts. In the lower right panel, we present this age/metallicity population indicator vs galactocentric distance, where green dash line represents the averaged value in corresponding distance range, and red dash lines represent the 16^{th} and 84^{th} percentiles. An upward trajectory is clear from \sim 0.95 at \sim 3 kpc to \sim 1 at 10 kpc.

 11.7 ± 0.3 kpc. Within the break radius, we found a power law index of $\alpha_{in} = -2.5 \pm 0.1$, while the index beyond the break radius is $\alpha_{out} = -4.5 \pm 0.3$. The inner index agrees with previous results, but the break radius is much smaller than previous claims of $r_s = 25 \pm 10$ kpc (e.g. Bland-Hawthorn & Gerhard 2016; Xue et al. 2015; Deason et al. 2011; Pila-Díez et al. 2015). Wolf et al. (2018) suggests the median

point source completeness limits is $u < 17.75$. While we set the magnitude cut at $u < 17.1$ to avoid the impact of incompleteness, the full survey photometric limits and zero-points of the SkyMapper Survey will be investigated in later data releases.

Finally, we present a 3-dimensional colour map of BHB stars in the southern sky, revealing substantial substructures that indicate significant age (∼ 1 *G*y*r*) or metallicity (∼ ⁰.¹ *dex*) variations which are important as they are the potential signatures of the accretion history of the Galaxy (Bullock & Johnston 2005); accompanying those substructures, we find a systematic colour shift from the centre of the Milky Way outwards, suggesting a large-scale metallicity/age variation through the halo. Such variations are natural predictions of an accreted stellar halo in hierarchical cosmological formation models (Bullock & Johnston 2005). This result resembles some previous works' conclusions: most recently, Grady et al. (2018) found a similar age gradient with O-Mira stars; Carollo et al. (2016) and Santucci et al. (2015b) presented the BHB colour distribution in the northern sky based on SDSS, interpreting these substructures as age fluctuations; Ibata et al. (2009) found significant small-scale variations of colour and metallicity in NGC 891, an edge-on galaxy that is an analogue of the Milky Way. Font et al. (2006) suggests that in their simulation, most metal-poor stars in the Galactic halo are buried within the central $~5$ kpc of the Galaxy, indicating that BHB colour substructure could also be resulted from metallicity variation.

It also clear that the SkyMapper DR1 is not yet deep enough for a thorough exploration of the Galactic halo. Assuming that BHB stars possess an absolute magnitude of $M_u = 2$ mag, based on Sec.3, a BHB star with an apparent magnitude $u_0 = 17.75$ mag will be at a distance of 14.12 kpc. However, SkyMapper clearly has the advantage of a narrower filter set to select a better BHB sample and future data releases hold great promise for expanding our understanding of the Galactic halo.

ACKNOWLEDGEMENTS

ZW gratefully acknowledges financial support through a the Dean's International Postgraduate Research Scholarship from the Physics School of the University of Sydney. ADM is grateful for support from an ARC Future Fellowship (FT160100206). GFL thanks the University of Surrey for hosting him as an IAS fellow for the final stages of the preparation of this paper.

The national facility capability for SkyMapper has been funded through ARC LIEF grant LE130100104 from the Australian Research Council, awarded to the University of Sydney, the Australian National University, Swinburne University of Technology, the University of Queensland, the University of Western Australia, the University of Melbourne, Curtin University of Technology, Monash University and the Australian Astronomical Observatory. SkyMapper is owned and operated by The Australian National University's Research School of Astronomy and Astrophysics. The survey data were processed and provided by the SkyMapper Team at ANU. The SkyMapper node of the All-Sky Virtual Observatory (ASVO) is hosted at the National Computational Infrastructure (NCI). Development and support the SkyMapper node of the ASVO has been funded in part by Astronomy Australia Limited (AAL) and the Australian Government through the Commonwealth's Education Investment Fund (EIF) and National Collaborative Research Infrastructure Strategy (NCRIS), particularly the National eResearch Collaboration Tools and Resources (NeCTAR) and the Australian National Data Service Projects (ANDS).

This work has made use of data from the European Space Agency (ESA) mission Gaia ([https://www.cosmos.](https://www.cosmos.esa.int/Gaia) [esa.int/Gaia](https://www.cosmos.esa.int/Gaia)), processed by the Gaia Data Processing and Analysis Consortium (DPAC, [https://www.cosmos.esa.](https://www.cosmos.esa.int/web/Gaia/dpac/consortium) [int/web/Gaia/dpac/consortium](https://www.cosmos.esa.int/web/Gaia/dpac/consortium)). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the Gaia Multilateral Agreement.

Software credit: sklearn (Pedregosa et al. 2011), IPYTHON (Pérez & Granger 2007), MATPLOTLIB (Hunter 2007), numpy (van der Walt et al. 2011), pandas (McKinney 2012), EMCEE (Foreman-Mackey et al. 2013)

REFERENCES

- Baade W., 1954, IAUT, 8, 682
- Bell E. F., Xue X. X., Rix H.-W., Ruhland C., Hogg D. W., 2010, [AJ,](http://dx.doi.org/10.1088/0004-6256/140/6/1850) [140, 1850](http://adsabs.harvard.edu/abs/2010AJ....140.1850B)
- Bessell M., Bloxham G., Schmidt B., Keller S., Tisserand P., Francis P., 2011, [PASP,](http://dx.doi.org/10.1086/660849) [123, 789](http://adsabs.harvard.edu/abs/2011PASP..123..789B)
- Bland-Hawthorn J., Gerhard O., 2016, [Annual Review of Astron](http://dx.doi.org/10.1146/annurev-astro-081915-023441)[omy and Astrophysics,](http://dx.doi.org/10.1146/annurev-astro-081915-023441) 54, 529
- Braga V. F., et al., 2018, [The Astronomical Journal,](http://dx.doi.org/10.3847/1538-3881/aaadab) 155, 137
- Brown T. M., Casertano S., Strader J., Riess A., VandenBerg D. A., Soderblom D. R., Kalirai J., Salinas R., 2018, [The](http://dx.doi.org/10.17909/T9SX1F) [Astrophysical Journal Letters,](http://dx.doi.org/10.17909/T9SX1F) 856, L6
- Bullock J. S., Johnston K. V., 2005, [ApJ,](http://dx.doi.org/10.1086/497422) [635, 931](http://adsabs.harvard.edu/abs/2005ApJ...635..931B)
- Carollo D., et al., 2016, [Nature Physics,](http://dx.doi.org/10.1038/nphys3874) [12, 1170](http://adsabs.harvard.edu/abs/2016NatPh..12.1170C)
- Choi J., Dotter A., Conroy C., Cantiello M., Paxton B., Johnson B. D., 2016, [ApJ,](http://dx.doi.org/10.3847/0004-637X/823/2/102) [823, 102](http://adsabs.harvard.edu/abs/2016ApJ...823..102C)
- Clewley L., Kinman T. D., 2006, [MNRAS,](http://dx.doi.org/10.1111/j.1745-3933.2006.00198.x) [371, L11](http://adsabs.harvard.edu/abs/2006MNRAS.371L..11C)
- Clewley L., Warren S. J., Hewett P. C., Norris J. E., Peterson R. C., Evans N. W., 2002, [MNRAS,](http://dx.doi.org/10.1046/j.1365-8711.2002.05864.x) [337, 87](http://adsabs.harvard.edu/abs/2002MNRAS.337...87C)
- Deason A. J., Belokurov V., Evans N. W., 2011, [MNRAS,](http://dx.doi.org/10.1111/j.1365-2966.2011.19237.x) [416,](http://adsabs.harvard.edu/abs/2011MNRAS.416.2903D) [2903](http://adsabs.harvard.edu/abs/2011MNRAS.416.2903D)
- Deason A. J., et al., 2012, [MNRAS,](http://dx.doi.org/10.1111/j.1365-2966.2012.21639.x) [425, 2840](http://adsabs.harvard.edu/abs/2012MNRAS.425.2840D)
- Deng L.-C., et al., 2012, [Research in Astronomy and Astrophysics,](http://dx.doi.org/10.1088/1674-4527/12/7/003) [12, 735](http://adsabs.harvard.edu/abs/2012RAA....12..735D)
- Dotter A., 2016, [ApJS,](http://dx.doi.org/10.3847/0067-0049/222/1/8) [222, 8](http://adsabs.harvard.edu/abs/2016ApJS..222....8D)
- Faccioli L., Smith M. C., Yuan H.-B., Zhang H.-H., Liu X.-W., Zhao H.-B., Yao J.-S., 2014, [ApJ,](http://dx.doi.org/10.1088/0004-637X/788/2/105) [788, 105](http://adsabs.harvard.edu/abs/2014ApJ...788..105F)
- Fermani F., Schönrich R., 2013, [MNRAS,](http://dx.doi.org/10.1093/mnras/sts703) [430, 1294](http://adsabs.harvard.edu/abs/2013MNRAS.430.1294F)
- Font A. S., Johnston K. V., Bullock J. S., Robertson B. E., 2006, [ApJ,](http://dx.doi.org/10.1086/498970) [638, 585](http://adsabs.harvard.edu/abs/2006ApJ...638..585F)
- Foreman-Mackey D., Hogg D. W., Lang D., Goodman J., 2013, [PASP,](http://dx.doi.org/10.1086/670067) [125, 306](http://adsabs.harvard.edu/abs/2013PASP..125..306F)
- Gaia Collaboration et al., 2016a, [A&A,](http://dx.doi.org/10.1051/0004-6361/201629272) [595, A1](http://adsabs.harvard.edu/abs/2016A%26A...595A...1G)
- Gaia Collaboration et al., 2016b, [A&A,](http://dx.doi.org/10.1051/0004-6361/201629512) [595, A2](http://adsabs.harvard.edu/abs/2016A%26A...595A...2G)
- Grady J., Belokurov V., Evans N. W., 2018, 12, 1
- Hattori K., Yoshii Y., Beers T. C., Carollo D., Lee Y. S., 2013, [ApJ,](http://dx.doi.org/10.1088/2041-8205/763/1/L17) [763, L17](http://adsabs.harvard.edu/abs/2013ApJ...763L..17H)
- Hunter J. D., 2007, Computing In Science & Engineering, 9, 90
- Ibata R., Mouhcine M., Rejkuba M., 2009, [MNRAS,](http://dx.doi.org/10.1111/j.1365-2966.2009.14536.x) [395, 126](http://adsabs.harvard.edu/abs/2009MNRAS.395..126I)
- Ibata R. A., et al., 2017, [ApJ,](http://dx.doi.org/10.3847/1538-4357/aa855c) [848, 128](http://adsabs.harvard.edu/abs/2017ApJ...848..128I)
- Kafle P. R., Sharma S., Lewis G. F., Bland-Hawthorn J., 2012, [ApJ,](http://dx.doi.org/10.1088/0004-637X/761/2/98) [761, 98](http://adsabs.harvard.edu/abs/2012ApJ...761...98K)
- Kafle P. R., Sharma S., Lewis G. F., Bland-Hawthorn J., 2013, [MNRAS,](http://dx.doi.org/10.1093/mnras/stt101) [430, 2973](http://adsabs.harvard.edu/abs/2013MNRAS.430.2973K)
- Kafle P. R., Sharma S., Lewis G. F., Bland-Hawthorn J., 2014, [ApJ,](http://dx.doi.org/10.1088/0004-637X/794/1/59) [794, 59](http://adsabs.harvard.edu/abs/2014ApJ...794...59K)
- Kinman T. D., Cacciari C., Bragaglia A., Smart R., Spagna A., 2012, [MNRAS,](http://dx.doi.org/10.1111/j.1365-2966.2012.20747.x) [422, 2116](http://adsabs.harvard.edu/abs/2012MNRAS.422.2116K)
- Kroupa P., 2001, [MNRAS,](http://dx.doi.org/10.1046/j.1365-8711.2001.04022.x) [322, 231](http://adsabs.harvard.edu/abs/2001MNRAS.322..231K)

12 Z. Wan et al

- Kunder A., et al., 2013, [AJ,](http://dx.doi.org/10.1088/0004-6256/146/5/119) [146, 119](http://adsabs.harvard.edu/abs/2013AJ....146..119K)
- McKinney W., 2012, Python for data analysis: Data wrangling with Pandas, NumPy, and IPython. O'Reilly Media, Inc. McNamara D. H., 2011, [AJ,](http://dx.doi.org/10.1088/0004-6256/142/4/110) [142, 110](http://adsabs.harvard.edu/abs/2011AJ....142..110M)
- Paxton B., Bildsten L., Dotter A., Herwig F., Lesaffre P., Timmes F., 2011, [ApJS,](http://dx.doi.org/10.1088/0067-0049/192/1/3) [192, 3](http://adsabs.harvard.edu/abs/2011ApJS..192....3P)
- Paxton B., et al., 2013, [ApJS,](http://dx.doi.org/10.1088/0067-0049/208/1/4) [208, 4](http://adsabs.harvard.edu/abs/2013ApJS..208....4P)
- Paxton B., et al., 2015, [ApJS,](http://dx.doi.org/10.1088/0067-0049/220/1/15) [220, 15](http://adsabs.harvard.edu/abs/2015ApJS..220...15P)
- Pedregosa F., et al., 2011, Journal of Machine Learning Research, 12, 2825
- Pérez F., Granger B. E., 2007, Comput. Sci. Eng., 9, 21
- Pila-Díez B., de Jong J. T. A., Kuijken K., van der Burg R. F. J., Hoekstra H., 2015, [A&A,](http://dx.doi.org/10.1051/0004-6361/201425457) [579, A38](http://adsabs.harvard.edu/abs/2015A%26A...579A..38P)
- Preston G. W., Shectman S. A., Beers T. C., 1991, [ApJ,](http://dx.doi.org/10.1086/170175) [375, 121](http://adsabs.harvard.edu/abs/1991ApJ...375..121P)
- Santucci R. M., Placco V. M., Rossi S., Beers T. C., Reggiani H. M., Lee Y. S., Xue X.-X., Carollo D., 2015a, [ApJ,](http://dx.doi.org/10.1088/0004-637X/801/2/116) [801, 116](http://adsabs.harvard.edu/abs/2015ApJ...801..116S)
- Santucci R. M., et al., 2015b, [ApJ,](http://dx.doi.org/10.1088/2041-8205/813/1/L16) [813, L16](http://adsabs.harvard.edu/abs/2015ApJ...813L..16S)
- Schlafly E. F., Finkbeiner D. P., Schlegel D. J., Jurić M., Ivezić Ž., Gibson R. R., Knapp G. R., Weaver B. A., 2010, [Astrophysical](http://dx.doi.org/10.1088/0004-637X/725/1/1175) [Journal,](http://dx.doi.org/10.1088/0004-637X/725/1/1175) 725, 1175
- Schlegel D. J., Finkbeiner D. P., Davis M., 1998, [ApJ,](http://dx.doi.org/10.1086/305772) [500, 525](http://adsabs.harvard.edu/abs/1998ApJ...500..525S)
- Searle L., Zinn R., 1978, [ApJ,](http://dx.doi.org/10.1086/156499) [225, 357](http://adsabs.harvard.edu/abs/1978ApJ...225..357S)
- Sharma S., Bland-Hawthorn J., Johnston K. V., Binney J., 2011, [ApJ,](http://dx.doi.org/10.1088/0004-637X/730/1/3) [730, 3](http://adsabs.harvard.edu/abs/2011ApJ...730....3S)
- Sirko E., et al., 2004a, [AJ,](http://dx.doi.org/10.1086/381483) [127, 899](http://adsabs.harvard.edu/abs/2004AJ....127..899S)
- Sirko E., et al., 2004b, [AJ,](http://dx.doi.org/10.1086/381486) [127, 914](http://adsabs.harvard.edu/abs/2004AJ....127..914S)
- Skrutskie M. F., et al., 2006, [AJ,](http://dx.doi.org/10.1086/498708) [131, 1163](http://adsabs.harvard.edu/abs/2006AJ....131.1163S)
- Wilhelm R., Beers T. C., Gray R. O., 1999, [AJ,](http://dx.doi.org/10.1086/300824) [117, 2308](http://adsabs.harvard.edu/abs/1999AJ....117.2308W)
- Wolf C., et al., 2018, preprint, ([arXiv:1801.07834](http://arxiv.org/abs/1801.07834))
- Xue X. X., et al., 2008, [ApJ,](http://dx.doi.org/10.1086/589500) [684, 1143](http://adsabs.harvard.edu/abs/2008ApJ...684.1143X)
- Xue X.-X., et al., 2011, [ApJ,](http://dx.doi.org/10.1088/0004-637X/738/1/79) [738, 79](http://adsabs.harvard.edu/abs/2011ApJ...738...79X)
- Xue X.-X., Rix H.-W., Ma Z., Morrison H., Bovy J., Sesar B., Janesh W., 2015, [ApJ,](http://dx.doi.org/10.1088/0004-637X/809/2/144) [809, 144](http://adsabs.harvard.edu/abs/2015ApJ...809..144X)
- Yanny B., et al., 2009, [AJ,](http://dx.doi.org/10.1088/0004-6256/137/5/4377) [137, 4377](http://adsabs.harvard.edu/abs/2009AJ....137.4377Y)
- York D. G., et al., 2000, [AJ,](http://dx.doi.org/10.1086/301513) [120, 1579](http://adsabs.harvard.edu/abs/2000AJ....120.1579Y)
- Zhao G., Zhao Y.-H., Chu Y.-Q., Jing Y.-P., Deng L.-C., 2012, [Research in Astronomy and Astrophysics,](http://dx.doi.org/10.1088/1674-4527/12/7/002) [12, 723](http://adsabs.harvard.edu/abs/2012RAA....12..723Z)
- van der Walt S., Colbert S. C., Varoquaux G., 2011, [Computing](http://dx.doi.org/10.1109/MCSE.2011.37) [in Science & Engineering,](http://dx.doi.org/10.1109/MCSE.2011.37) 13

This paper has been typeset from a T_EX/LAT_EX file prepared by the author.