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Three–wave trapponic solitons for tunable high–repetition rate pulse train generation

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Abstract—We demonstrate that the parametric mixing of an ultra-short Zakharov–Manakov (ZM) soliton pulse with a quasi– continuous wave (CW) signal in a weakly quadratic nonlinear and dispersive medium may lead to the generation of a three–wave soliton with variable speed, or *trappon*. We show that trappons may provide a novel mechanism of cavity–less ultra–short pulse train generation. The time width, the amplitude and the repetition rate of the generated pulse trains may be controlled in a stable manner by adjusting the intensity level of the CW signal and/or the ZM short soliton pulse.

Index Terms—Three wave interaction, Solitons, Pulse train generation.

I. INTRODUCTION

E FFICIENT mechanisms for the generation of high-contrast, ultra-short pulse trains are of interest in a broad range of domains, such as time-resolved spectroscopy and microscopy, selective femtosecond chemistry, quantum coherent control in high-field physics, and optical communications. Relevant application examples include quantumpath control of high-harmonic generation [1]; multi-pulse excitation of atoms, molecules, and solids [2]; multiple-laserpulse excitation of high-gradient plasma accelerators [3]; high-fluence THz wave-train generation for radar, microwave [4] and optical communication systems. Several techniques for generating trains of ultra-short pulses at repetition rates beyond those achievable by active laser mode locking or by means of electrically-controlled modulation have been explored in recent years. For example, linear pulse train generation techniques include the repetition-rate multiplication of a lower rate source by applying amplitude [5], [6] or phasespectral filtering [7], [8], [9]. Moreover, different all-optical techniques that may result in up to THz pulse train rates have also been proposed by using both quadratic and cubic nonlinear media. Consider for example induced modulation instability [10], [11], multiple four-wave-mixing [12], [13], and backward quasi-phase-matched second harmonic generation [14], [15].

In this Paper, we present a novel nonlinear technique for the flexible generation of a train of ultra–short optical pulses

S. Wabnitz was with the Institut Carnot de Bourgogne, UMR 5209 CNRS, Université de Bourgogne, 9 Av. A. Savary BP 46870, 21078 Dijon, France. His present addres is Dipartimento di Elettronica per l'Automazione, Università di Brescia, via Branze 38, Brescia 25123, Italy. with light-controlled time width, amplitude and repetition rate. This technique originates from the interaction of three waves at resonance. Though this process is of interest in various physical contexts, our treatment here is phrased in the language of nonlinear optics where its potential applicability appears to be higher. The physical model describing threewave interactions (TWI) is completely integrable by spectral methods [16], and it exhibits soliton solutions, i.e. particular waveforms that preserve their shapes upon collisions. The simplest of such soliton solutions of the TWI equations was discovered by Zakharov and Manakov (ZM), and it consists of hyperbolic secant pulses. We propose to exploit the parametric interaction of an ultra-short ZM soliton pulse [16] with a quasi-continuous wave signal, which collide in a weakly dispersive and nonlinear quadratic optical crystal. As we shall see, the phase-matched three-wave interaction of the ultrashort pulse with the CW signal may lead to the high-contrast modulation of the CW signal into a sequence of ultra-short pulses. Quite remarkably, the above pulse train generation process is analytically described in terms of the adiabatic reshaping of the initial single-wave ZM soliton into a threewave locked soliton with variable speed, which is also known as the trappon [17]. By exploiting the degrees of freedom of such trapponic soliton solutions, we shall demonstrate here that the time width, amplitude and repetition rate of the generated pulse train may be controlled in a stable manner by simply adjusting the parameters of the two input pulses, namely the intensity level of the CW signal, and/or the intensity level and time width of the short ZM soliton pulse.

II. THREE-WAVE INTERACTION EQUATIONS

The dimensionless equations that describe the quadratic resonant interaction of three waves in a nonlinear optical medium read as

$$\frac{\partial A_1}{\partial \xi} + \delta_1 \frac{\partial A_1}{\partial \tau} = iA_2^*A_3,$$

$$\frac{\partial A_2}{\partial \xi} + \delta_2 \frac{\partial A_2}{\partial \tau} = iA_1^*A_3,$$

$$\frac{\partial A_3}{\partial \xi} + \delta_3 \frac{\partial A_3}{\partial \tau} = iA_1A_2,$$
(1)

with

$$A_j = \pi \chi^{(2)} \sqrt{\frac{n_j \omega_1 \omega_2 \omega_3}{n_1 n_2 n_3 \omega_j}} E_j.$$
⁽²⁾

Here $\tau = t/t_0$, t_0 is an arbitrary time scale; $\xi = z/z_0$, z_0 is an unit space–propagation parameter. E_i is the slowly varying

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electric field envelope of the wave at frequency ω_j , n_j is its refractive index, $\chi^{(2)}$ is the quadratic nonlinear susceptibility, $\delta_j = z_0/(v_j t_0)$ (v_j being the linear group velocity), and j =1,2,3. We assume that the group velocity v_3 of the wave with the highest frequency ($\omega_3 = \omega_1 + \omega_2$) lies between the group velocities of the other waves, i.e. $v_1 > v_3 > v_2$. With no loss of generality, we shall write Eqs. (1) in a coordinate system such that $\delta_1 = 0$, which implies $0 < \delta_3 < \delta_2$. Eqs. (1) exhibit, among others, the conserved quantities

$$U_{13} = U_1 + U_3 = \frac{1}{2} \int_{-\infty}^{+\infty} (|A_1|^2 + |A_3|^2) d\tau, \qquad (3)$$

$$U_{23} = U_2 + U_3 = \frac{1}{2} \int_{-\infty}^{+\infty} (|A_2|^2 + |A_3|^2) d\tau, \qquad (4)$$

which is reported here for future reference, where U_1 , U_2 and $2U_3$ represent the energies of waves at the frequencies ω_1 , ω_2 and ω_3 , respectively.

III. SOLITON-BASED ULTRA-SHORT PULSE TRAIN GENERATION

Let us first present numerical evidence of the train generation process. Figure 1 illustrates the possibility of obtaining an efficient modulation of the input CW signal into a train of ultra-short pulses, as a result of its parametric mixing with an ultra-short ZM soliton pulse at a different carrier wavelength. In particular, in Fig. 1 we numerically solved Eqs. (1), where the initial excitation conditions at $\xi = 0$ were provided by a quasi-CW signal at frequency ω_1 (a standing signal in a coordinate system where $\delta_1 = 0$ and a short ZM soliton pulse at frequency ω_2 (with delay parameter $\delta_2 > 0$). The two input pulses were pre-delayed, so that they could collide at some distance inside the crystal. Figure 1 shows that as soon as the faster ZM soliton pulse starts to overlap in time with the slower quasi-CW signal, their parametric mixing leads to the generation of an idler short pulse at frequency ω_3 . Additionally, Fig. 1 also shows that the TWI leads to a periodic oscillation with distance ξ of the intensity of the two short pulses at carrier frequencies ω_2 and ω_3 . As a result, it turns out [18] that the centre of mass of these two pulses periodically oscillates in time around an average value, which grows larger with distance according to a common average group velocity which is apparently (see Fig. 1) different from the group velocity of the incoming short pulse. As for the incoming CW signal, Fig. 1 also shows that a train of short pulses is carved on the CW background at frequency ω_1 . Finally, Fig. 1 also illustrates that at the end of the threewave interaction process the quasi-CW background at ω_1 is modulated into a sequence of ultra-short pulses, the soliton pulse at ω_2 returns back to its original shape, and the generated sum-frequency pulse at ω_3 vanishes.

Quite remarkably, we shall demonstrate now that the entire three–wave interaction process which is displayed in Fig. 1 may be analytically represented in terms of particular analytical TWI soliton solutions. In the notation of Eqs. (1), the arbitrary input quasi CW signal at frequency ω_1 may be described as



Fig. 1. Sum-frequency parametric interaction of a quasi-CW control at ω_1 and a short pulse at ω_2 . The characteristic delays are $\delta_1 = 0, \delta_2 = 2, \delta_3 = 1$.

$$A_1 = \frac{Ce^{-i\gamma\tau}}{2} [\tanh(\frac{\tau - \tau_i}{\tau_r}) - \tanh(\frac{\tau - \tau_f}{\tau_r})],$$

$$A_2 = 0,$$

$$A_3 = 0,$$
(5)

where C is the complex amplitude and γ is the frequency shift with respect to ω_1 of the quasi-CW signal; τ_i (τ_f) and τ_r are the switch-on (switch-off) time and the rise/fall time of the quasi-CW signal, respectively.

On the other hand, the input ZM single–wave soliton pulse [16] at frequency ω_2 reads as

$$A_{1} = 0,$$

$$A_{2} = 2P\sqrt{\varrho\delta_{2}\delta_{3}}\frac{e^{i\varrho\phi\tau_{2}}}{\cosh(2P\varrho\tau_{2})},$$

$$A_{3} = 0,$$
(6)

where

$$\varrho = \delta_3 / (\delta_2 - \delta_3),$$

$$\tau_2 = -\tau + \delta_2 \xi.$$
(7)

For a given choice of the three linear group velocities, or characteristic delays δ_j , the above ZM soliton is determined in terms of the two real parameters $P > 0, \phi$. The parameter P fixes both the soliton peak amplitude and its temporal width.

Whereas the parameter ϕ corresponds to a phase shift which is linear in both τ and ξ .

After the collision of the ZM pulse with the CW background, we surmise that their parametric interaction generates a three-wave trapponic soliton, which consists of a groupvelocity locked bright-bright-dark triplet. Similar triplet solutions have been already considered in nonlinear optics in the form of simultons [19], [20] or boomerons [21]. Trappon soliton solutions of the TWI Eqs. (1) may be found as discussed in the recent analysis of Ref. [18], [19]. TWI trappons, whose potential impact on nonlinear optics is suggested here for the first time, are characterized by a periodic (or trapped) spatio-temporal evolution of the energy distribution of the three waves, as well as of their locked propagation speed. As a result, the center of mass of a trappon also periodically oscillates within a limited time interval. As far as the potential applications are concerned, the most significant property of the trappon dynamics consists in the carving of a train of short pulses into the CW-background at frequency ω_1 . Indeed, as shown in the next section, the entire three-wave interaction dynamics after the collision of the short pulse with the CW background as shown by Fig. 1 may be analytically described in terms of the trappon solution

$$A_{1}^{T} = ia\sqrt{\delta_{2}\delta_{3}}e^{iq_{1}\tau_{1}} - i\frac{\Delta}{4p}(\frac{\delta_{2}-\delta_{3}}{\delta_{2}\delta_{3}})A_{2}^{*}A_{3},$$

$$A_{2}^{T} = -\frac{2p\delta_{3}}{\Delta}\sqrt{\frac{2\delta_{2}}{\delta_{2}-\delta_{3}}}e^{iq_{2}\tau_{2}}(H_{+}^{*}-H_{-}^{*}),$$

$$A_{3}^{T*} = \frac{2p\delta_{2}}{\Delta}\sqrt{\frac{2\delta_{3}}{\delta_{2}-\delta_{3}}}e^{iq_{3}\tau_{3}}(H_{+}e^{i\beta}-H_{-}e^{-i\beta}), \quad (8)$$

where

$$\begin{split} \Delta &= 1 + |H_{+}|^{2} + |H_{-}|^{2} - 2\cos(\beta)\mathcal{R}e(H_{+}H_{-}^{*}e^{i\beta}), \\ H_{\pm} &= e^{-(B\pm i\chi)\tau} e^{\frac{2\delta_{2}\delta_{3}}{\delta_{2}-\delta_{3}}p\xi}, \\ \chi &= \sqrt{a^{2}-p^{2}}, \\ B &= p(\frac{\delta_{2}+\delta_{3}}{\delta_{2}-\delta_{3}}), \ \tan(\beta) = \sqrt{a^{2}-p^{2}}/p, \\ \delta &= \frac{2\delta_{2}\delta_{3}}{\delta_{2}+\delta_{3}}, \\ q_{n} &= q(\delta_{n+1}-\delta_{n+2}), \ n = 1, 2, 3 \ mod(3), \\ \tau_{n} &= -\tau + \delta_{n}\xi. \end{split}$$
(9)

For a given choice of the characteristic linear velocities in Eqs. (1), the trappon solution of Eqs. (8) is completely determined by just three independent real parameters, namely p, q, a (with the restrictions that p > 0, a > 0 and $a^2 > p^2$). The parameter p is associated with the rescaling of the wave amplitudes, and of coordinates τ and ξ . Whereas a measures the amplitude of the CW background in wave A_1^T . The parameter q adds a phase shift which is linear in both τ and ξ .

The trappon solution (8) extends in time from $\tau = -\infty$ to $\tau = +\infty$ and at large distances (i.e., for $\xi \to +\infty$) it exhibits a time-periodic behavior. Nevertheless, as we shall see in next section, Eqs. (8) exactly describe the mixing of the ZS soliton (6) with the quasi-CW (5) background signal over the finite interval $[\tau_i, \tau_f]$ (which correspond to the times of turning on and off the CW wave at frequency ω_1 , respectively).



Fig. 2. Numerical evolution (continuous lines) and theoretical prediction from Eqs. (8) (dotted lines) of the energy at ω_2 and of the output pulse profile at ω_1 for the case of Fig. 1.

IV. THREE-WAVE ADIABATIC SOLITON SHAPING

Indeed, one may analytically predict the characteristic parameters p, q, a of the generated TWI trappon from the corresponding P, ϕ parameters of the isolated input ZM soliton, and the complex amplitude C and the frequency shift γ of the CW signal. In order to demonstrate this, it is sufficient to suppose that the input ZM soliton adiabatically (i.e., without emission of radiation) reshapes into a trappon soliton after its collision with the quasi-CW background at a given point in time (say, at $\tau = \tau_i$). In the spectral domain [16] this hypothesis is equivalent to imposing that the input ZM soliton, after the collision with the CW background, transfers its discrete eigenvalue to the trappon soliton. In the frame of this basic hypothesis, the conservative nature of the threewave interaction permits us to suppose that: i) the energy U_{23} (4) of the input TWI soliton is conserved in the generated trappon soliton; ii) the phase of the ω_2 frequency components of the input TWI soliton and of the generated TWI soliton varies in a continuous manner across their time interface (i.e., at $\tau = \tau_i$; iii) the amplitude and the phase of the CW background coincide with the corresponding values of the asymptotic plateau of the component at frequency ω_1 of the generated TWI trappon. The above three conditions, after some straightforward calculations, permit us to obtain the following equations that relate the parameters of the incident and of the transmitted solitons (i.e., before and after the collision, respectively)

$$P = p, \quad a = |C|/\sqrt{\delta_2 \delta_3}, \quad q(\delta_2 - \delta_3) = \phi, \tag{10}$$

with the restrictions that $|C|^2 > P^2 \delta_2 \delta_3$ and $\gamma = \phi$. The above conditions define the matching relations among the amplitudes and the phases of both the input ZM soliton and of the CW signal which should be satisfied in order to excite the trapponic soliton. As an example, consider the case of Fig. 1, where the CW background control is described by Eqs. (5) with C = 3, $\gamma = 1$, and the input ZM soliton (6) is obtained from Eqs. (6) with $P = 1.5, \phi = 1$. After the collision with the CW background, Eqs. (10) predict that the generated trappon is obtained from Eqs. (8) with p = 1.5, q = 1, and $a = 3/\sqrt{2}$. We confirmed the accuracy of this prediction by means of extensive comparisons of the analytical expression (8) with numerical solutions of the TWI Eqs. (1). For example, Fig. 2 displays both numerically computed and analytical evolutions



Fig. 3. Output pulse train (11) amplitude (blue line) and its time-average value (red line) for: a) $C = 2.5\sqrt{2}$, P = 1 and b) $C = 2.5\sqrt{2}$, P = 2; Pulse train frequency f = 1/T c) vs. P(C = 10); and d) vs. C(p = 2).

for the energy U_2 (along the crystal length ξ) and for the output transverse profile of wave A_1 (along τ) (these correspond to the same interaction process previously shown in Fig. 1).

V. CONTROLLED PULSE TRAIN GENERATION

The amplitude profile of the generated train of ultrashort pulses at frequency ω_1 may be exactly described by performing the limit for $\xi \to +\infty$ of the first of Eqs. (8), which yields

$$|A_{1\infty}^{T}(\tau)| = |C| \Big| 1 - 4\cos(\beta) \frac{\sin(\pi\tau/T) \sin(\pi\tau/T - \beta)}{1 - \cos(\beta)\cos(2\pi\tau/T - \beta)} \Big|$$
(11)

where $|C| = a\sqrt{\delta_2\delta_3}$ (see (10)), $\tan(\beta) = \sqrt{a^2 - p^2}/p$ (see (9)) and period $T = \pi/\sqrt{a^2 - p^2}$. Two different examples of the generated pulse trains as described by Eqs.(11) are shown in Fig. 3 a)-b).

Equation (11) provides relatively simple expressions that relate the parameters of the injected soliton pulse and CW background to the main features of the generated output pulse train. Indeed, $|A_{1\infty}^T|$ is a time periodic signal (with period T) with average value approximatively equal to |C|. Moreover, from Eqs.(11) one obtains that the peak amplitude of the generated pulses is $M = |C| + 2\sqrt{\delta_2 \delta_3}P$; whereas the minimum amplitude is $m = |C| - 2\sqrt{\delta_2 \delta_3}P$. Hence the maximum intensity contrast for the generated train is obtained for $|C| = 2P\sqrt{\delta_2 \delta_3}$: in this case, the field amplitude at the minima vanishes and the peak amplitudes reads as $M = 4\sqrt{\delta_2 \delta_3}P$.

In Figure 3 c)–d) we illustrate the analytically predicted dependence of the repetition rate of the ultra–short pulse train $\mathbf{R} = \mathbf{1}/\mathbf{T} = \sqrt{|\mathbf{C}|^2/(\delta_2\delta_3) - \mathbf{p}^2}/\pi$, as a function of the amplitudes of the input short pulse and of the CW signal, respectively. As it can be seen in Fig. 3 c), the repetition

rate is the largest whenever the amplitude of the input soliton vanishes. Whereas there is a critical input soliton amplitude, above which the period of the generated pulse train diverges to infinity. On the other hand, Fig. 3 d) shows that when varying the CW background amplitude, a finite repetition rate is only obtained for amplitudes |C| above a certain threshold level, and the rate grows larger with |C| in a linear fashion.

The above results show that the peak amplitude, the time width and the repetition rate of the pulse train which is generated at ω_1 may be controlled in a stable manner by simply adjusting the intensity level of the input CW signal |C| and/or the amplitude level (hence the time width) P of the input short soliton pulse.

It is worth noting the efficiency of the proposed method for generating pulse trains, since theoretically the entire energy of the pump pulse A_1 is converted into the train. Indeed, from the energy conservation relation (3) and the fact that at the end of the interaction $A_3 = 0$, it follows that the energy of the quasi-CW pulse is conserved before and after the collision with the control pulse A_2 .

It should be pointed out that the generation process we have so far described may be thought of as a way of "writing" a pulse train on a quasi CW signal. The opposite process of "erasing" such wave train to go back to a flat, quasi CW, signal is also possible. Indeed, it is easy to realize that this reverse process is well described in a similar way by the formation of the trappon soliton solution of the TWI Eqs. (1) which is obtained from the expression (8) via the invariance transformation $\xi \rightarrow -\xi$, $\tau \rightarrow -\tau$, $A_1 \rightarrow A_1$, $A_2 \rightarrow A_2$, $A_3 \rightarrow -A_3$.

We would like to point out that the observation of the above described three-wave phenomena appears to be readily achievable in nonlinear optical experiments. For instance, let us consider the eee interaction of three-waves with carrier wavelengths of $\lambda_1 = 1.55 \mu m$, $\lambda_2 = 3.4 \mu m$, $\lambda_3 = 1.064 \mu m$ in a 8cm long periodically poled bulk Lithium Tantalate crystal with $28\mu m$ periodicity. In this case, the parametric mixing of a 200 fs incident pulse with a quasi-CW signal (say, with a 3ps time duration) leads to the generation of a train of 250 fspulses with a repetition rate of about 2THz; the corresponding peak power levels of the incident and of the generated fields are of the order of a few hundreds of MW/cm^2 . In practical terms, the upper limit to the maximum repetition rate of the generated pulse train which can be achieved by the present technique will be set by the limit of validity of Eqs. (1), which hold true in three-wave physical systems whenever the presence of group velocity dispersion within each wave can be neglected.

VI. CONCLUSIONS

We revealed that the three–wave parametric interaction of an ultra-short ZM soliton pulse with a quasi–continuous wave (CW) signal in a weakly quadratic nonlinear and dispersive medium may lead to the generation of a trapped soliton, or trappon. Moreover, we predicted that the excitation of trapped solitons may lead to a new class of optically controlled, cavityless sources of ultra-short pulse trains with up to multi–THz repetition rates.

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