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Evaporation, diffusion and self-assembly at drying interfaces†

K. Roger, ^a E. Sparr ^{*b} and H. Wennerström ^b

Water evaporation from complex aqueous solutions leads to the build-up of structure and composition gradients at their interface with air. We recently introduced an experimental setup for quantitatively studying such gradients and discussed how structure formation can lead to a self-regulation mechanism for controlling water evaporation through self-assembly. Here, we provide a detailed theoretical analysis using an advection/diffusion transport equation that takes into account thermodynamically non-ideal conditions and we directly relate the theoretical description to quantitative experimental data. We derive that the concentration profile develops according to a general square root of time scaling law, which fully agrees with experimental observations. The evaporation rate notably decreases with time as $t^{-1/2}$, which shows that diffusion in the liquid phase is the rate limiting step for this system, in contrast to pure water evaporation. For the particular binary system that was investigated experimentally, which is composed of water and a sugar-based surfactant (α -dodecylmaltoside), the interfacial layer consists in a sequence of liquid crystalline phases of different mesostructures. We extract values for mutual diffusion coefficients of lamellar, hexagonal and micellar cubic phases, which are consistent with previously reported values and simple models. We thus provide a method to estimate the transport properties of oriented mesophases. The macroscopic humidity-independence of the evaporation rate up to 85% relative humidities is shown to result from both an extremely low mutual diffusion coefficient and the large range of water activities corresponding to relative humidities below 85%, at which the lamellar phase exists. Such a humidity self-regulation mechanism is expected for a large variety of complex system.

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Introduction

Water evaporation is a phenomenon we all witness from an early age, although its apparent simplicity quickly dissipates as we are taught science basics. Indeed, liquid water is stable between 0 °C and 100 °C and yet it can convert to its gaseous form at ambient temperatures. This apparent paradox is explained by the necessity to consider the full system, including both liquid water and the gas phase surrounding it. Only when this gas phase is saturated with water vapor, at 100% relative humidity, will evaporation stop. Predicting the evaporation rate of pure water remains a challenging task since a collection of different limiting steps can be encountered, such as diffusion or convection in the gas phase and thermal transfer to the interface. Aqueous systems often contain solutes that exhibit

negligible evaporation rates. Water evaporation then results in an increased concentration of the solute close to the air–liquid interface, which often makes diffusion in the liquid phase the rate limiting transport process. Interestingly, an increased number of components in the system can thus lead to a simplified description of the evaporation phenomenon. The concentration gradient can significantly impact the properties of the system. For example, Kabalnov and Wennerström² showed that dispersed colloidal particles diffuse away from the air–liquid interface in the gradient created by water evaporation in a mixed solvent. An application of this effect is found in the prevention of the drying out at the tip of ink-pens, when not in use. More dramatic effects can occur when the gradient gives rise to the appearance of new phases close to the air–liquid interface.^{1,3–6} These structures have a strong influence on diffusion and other transport properties.^{6,7} The control of drying processes thus crucially depends on the understanding of the physico-chemical processes giving rise to structure and composition gradients at the air–liquid interface of multi-component solutions. Such an understanding also impacts the description of filtration and centrifugation processes as well as that of transport across out-of-equilibrium biological membranes

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as, for example, found in the skin and the liquid tear film on our eyes.^{8–11}

A challenge in the description of the transport processes during evaporation is that the systems are highly non-ideal and they can show a rich phase behavior. A detailed experimental characterization of the interfacial region is a prerequisite for obtaining a relevant understanding of the phenomena. In a recent publication,¹ we presented experimental investigations showing the formation of interfacial multilayer structures on drying aqueous solutions, using a capillary setup that allows for detailed mapping of gradients in composition and structure. In the present paper, we focus on providing a theoretical description of evaporation from non-ideal solutions, using additional experimental results and theoretical analysis. Section 1 contains a report of experimental results that are particularly relevant for the theoretical analysis. Section 2 describes a general scaling law that analytically follows from Fick's second law for diffusion in non-ideal systems. Section 3 consists in a quantitative evaluation of mutual diffusion coefficients for aligned mesophases. Section 4 contains a discussion of a humidity self-regulation mechanism exhibited in amphiphile/water solution and its extension to complex systems.

Results and discussion

1. Experimental findings

1.1 Drying cell to study interfacial phase separation in a water gradient. In order to quantitatively monitor water evaporation and characterize the drying interfaces, we have designed a drying cell as previously described.¹ The set-up consists of a glass capillary with a rectangular cross-section 0.1×1 mm, which connects in one end to a large reservoir filled with an aqueous solution, while its other end is exposed to an air flux of controlled humidity (see Fig. 1A). The relative humidity (RH) of this air flux can be varied from 1% to 99% relative humidity by mixing dry and water-saturated air through a humidity generator (HumiSys LF, InstruQuest). The aqueous solution is placed in the reservoir and

flows by capillarity to the tip of the capillary, where water evaporation occurs in an environment at controlled relative humidity. This cell can be used together with microscopy (Zeiss Axioplan optical microscope with crossed polarizers) and scattering (cSAXS, PSI, Switzerland) characterizations, while a modified version consisting of 9 capillaries attached to the same reservoir of rectangular cross-section 0.2×2 mm was used to monitor mass loss through evaporation of water (multi-capillary cell). The dimensions of the capillary ensure very low Reynolds numbers and thus creeping flow, also called Stokes flow. For pure water, the fluid velocity was determined by monitoring the position of an air–water meniscus and yields a Reynolds number of 9×10^{-4} at a relative humidity of 0.7%. Since the surface of evaporation is orthogonal to the walls of the capillary, the fluid will undergo a simple unidirectional advection in this cell, in contrast to other setups such as polydimethylsiloxane (PDMS) microfluidic chips.¹²

1.2 Pure water versus aqueous solutions of amphiphilic molecules. If water is the only volatile compound in the solution, one can simply quantify the evaporation of water by measuring the mass loss over time. We set the multi-capillary drying cell on a balance, which was placed in air of tunable relative humidity. The solution was poured in the bulk reservoir, which was then capped to ensure that evaporation occurs only at the tip of the capillaries. As soon as the liquid reached the tip of the capillary, water evaporation can be measured as a decrease of the overall mass. The time variation of the mass loss is displayed in Fig. 2A for pure water and for a water/surfactant binary solution (α -dodecylmaltoside, DDM), at a relative humidity of 1%. The logarithmic scale highlights that evaporation in these different systems gives rise to different power law variations of the mass loss with time. For pure water, an exponent of unity is obtained, which means that the evaporation rate is constant over time. For the binary amphiphile–water system, an exponent of 1/2 is obtained, which means that the evaporation rate decreases with increasing time with an inverse square root dependence. Given the power law, the pre-factor determines the rate of evaporation at all times. The pre-factors were thus determined for both systems over a large

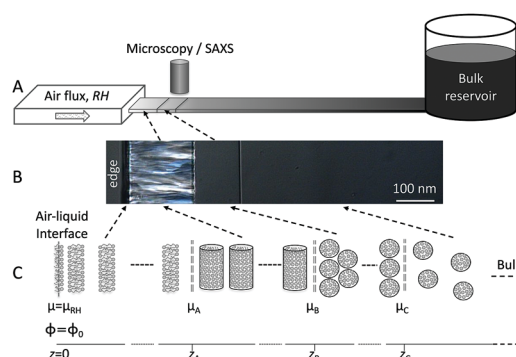


Fig. 1 (A) Schematic representation of the drying setup consisting of a rectangular capillary connected to a large reservoir containing the aqueous solution and placed in front of an air flux of controlled relative humidity, as previously described.¹ (B) Top view of the capillary under drying placed in between crossed polarizers under an optical microscope. (C) Associated microstructures and chemical potential gradients.

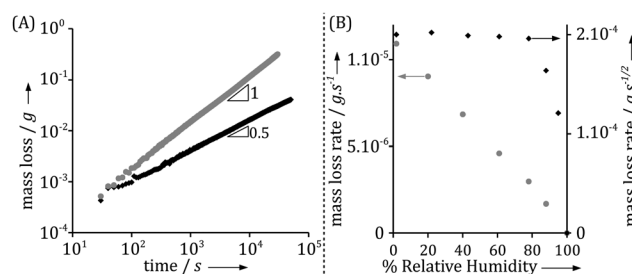


Fig. 2 (A) Mass of water evaporated with time from a multi-capillary cell for pure water (grey circles) and a 15 wt% α -dodecylmaltoside surfactant/water solution (black diamonds). As evidenced by the log/log scale, the mass loss follows a power law for each system, but the exponent is 1 for pure water and 1/2 for the surfactant solution. (B) Mass loss rate with relative humidity for both systems. For pure water, the variation is linear with relative humidity, while for the surfactant solution a highly non-linear behavior is observed, corresponding to a nearly constant value for most of the humidity range. This supports a change in the transport limiting step when RH changes.



range in relative humidity, as displayed in Fig. 2B. For pure water, the evaporation rate scales linearly with relative humidity, while for the binary solution, it is nearly independent of the relative humidity for $RH < 85\%$. The macroscopic observations displayed in Fig. 1B clearly imply that there is a difference in the rate limiting transport process between these two systems. This qualitative difference is also illustrated by the observation that pre-factors depend on the external flow rate in the gas phase for the pure water system, while they do not for the surfactant solution in the present experimental conditions.

1.3 Experimental observations of self-assembly at drying interfaces. One main advantage of the drying cell illustrated in Fig. 1A resides in the possibility for multiple characterizations at an adequate length scale. This can be used to unveil the microscopic cause of the difference in the macroscopic behavior illustrated in Fig. 1C. Observations under a light microscope, between crossed polarizers, revealed the presence of several different lyotropic mesophases in the interfacial layer, separated by sharp boundaries that are parallel to the air–liquid interface and thus orthogonal to the advective flux (see Fig. 1B). High-resolution Small-Angle X-ray scattering (SAXS) was performed using a coherent synchrotron beam to characterize the mesostructure of each phase (see Fig. S2, ESI†).¹ The same sequence of phases was observed from the reservoir towards the tip as displayed in the equilibrium bulk phase diagram with decreasing water concentration.¹³ We observe lamellar, hexagonal and micellar cubic phases. Infra-red (IR) microscopy measurements confirmed the build-up of a water concentration gradient coinciding with the structural gradient evidenced by optical microscopy and SAXS.¹ Water concentration varied approximately linearly within each phase and showed abrupt changes at the phase boundaries. Additionally, SAXS yields the swelling profile of each mesostructure between the phase boundaries. All these observations support the assumption of a local thermodynamic equilibrium despite the overall non-equilibrium character of the system.

Time resolved SAXS and IR microscopy measurements show that while both the positions of the phase boundaries and composition at a given position vary with time, the observations could always be rescaled to the same profiles within each phase between the phase boundaries.¹ Optical microscopy enables an easy monitoring of the growth of the mesophases with time, and thus provides rescaling factors. Fig. 3A displays the thickness increase over time of the different phases observed in the interfacial layer formed in the surfactant/water system. Remarkably, the thickness of all phases increases linearly with the square root of time, for all relative humidities. This is consistent with the measured macroscopic mass loss due to evaporation (Fig. 2A). The thickness of the outer phase in contact with air varies with the relative humidity at the boundary, while the thicknesses of all inner phases are seemingly independent of boundary conditions. At relative humidities above 85%, the outer lamellar phase disappears and the hexagonal phase becomes the outer phase. The relative humidity of this phase transition coincides with the analogous phase transition in equilibrium conditions, as confirmed by sorption calorimetry measurements.¹ Fig. 3B shows that the ratio between the thicknesses of two inner

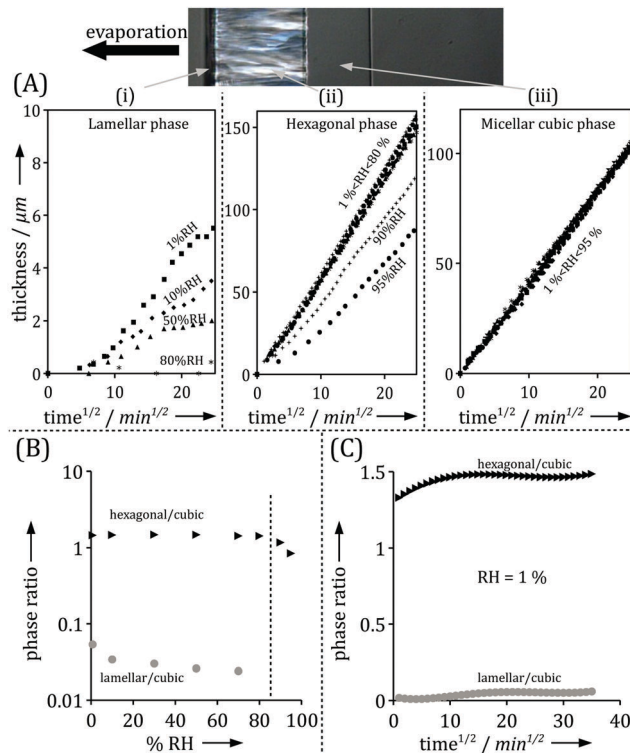


Fig. 3 (A) Thickness variations with time of the lamellar phase (i), hexagonal phase (ii) and micellar cubic phase (iii), which scale with the square root of time (adapted from ref. 1). (B) Ratio of thicknesses between the hexagonal and cubic phases (black) is constant over most of the humidity range, while the ratio of thicknesses between the lamellar and hexagonal phases (grey) varies with RH until the lamellar phase disappears at 85% RH. (C) Ratio of thicknesses between the hexagonal and cubic phases (black), and the lamellar and cubic phases (grey) over time at a given RH. The ratios are constant after a transition regime. Experiments were performed using the milli-fluidic drying cell in Fig. 1A where the bulk solution contained 15 wt% α -dodecylmaltoside surfactant/water solution.

(hexagonal and micellar cubic) phases is independent of variations in RH at $RH < 85\%$, while the ratio between the thickness of the outer phase, which is in contact with air, and the thickness of an inner phase varies with the RH boundary condition. Interestingly, the profile in Fig. 3B is very similar to the one extracted from the macroscopic measurements for evaporation rates from the same system (Fig. 2B). Fig. 3C shows that, at a given relative humidity, the ratio between two phases is almost constant over time. It is also noticed that the outer lamellar phase is much thinner compared to the inner phases with higher water contents, which decreases the precision of its thickness determination compared to the inner phases. Similar observations have also been made for other binary and ternary water–surfactant and water–lipid systems.¹

To further investigate the role of the boundary condition we monitored the response to an abrupt relative humidity change in the gas phase. Fig. 4 shows how the different phase boundaries move in response to an instantaneous change in RH from 1% to 95%. There is momentarily a condensation of water at the interface and a change in the direction of diffusional flow. The lamellar phase disappears and the hexagonal phase responds and becomes



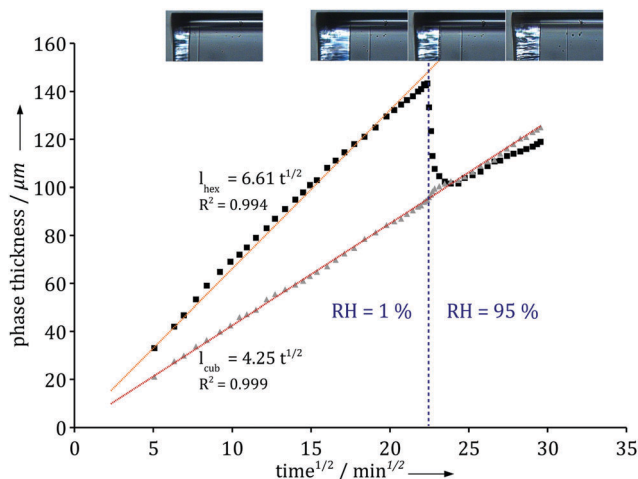


Fig. 4 Thickness variation with time of the hexagonal phase (black squares) and the micellar cubic phase (grey triangles) upon a change in the air relative humidity. The hexagonal phase responds and reaches a slower increase as expected from Fig. 3, while the micellar cubic phase is completely insensitive to the change. Experiments were performed using the milli-fluidic drying cell in Fig. 1A where the bulk solution contained 15 wt% α -dodecylmaltoside surfactant/water solution.

thinner as its inner boundary moves towards the air/liquid interface. Within an hour, the system has fully adjusted to the new boundary condition and the diffusional flow reverts to its original direction throughout the system. Note that the thickness of the inner micellar cubic remains virtually unaffected by the change in the boundary condition. The relatively fast response indicates that the majority of molecular degrees of freedom are in, or close to, equilibrium and respond quickly to the changes caused by the dynamic processes.

The experimental observations summarized in Fig. 2–4, as well as those reported in ref. 1 clearly demonstrate a remarkable consistency between experimental observations of microscopic and macroscopic properties of the drying interfaces in the amphiphile–water systems. There are clear trends in the experimental data that calls for explanations. The observed $t^{1/2}$ time dependence in Fig. 2B, 3A and 4 is notably indicative of a diffusion controlled rate-limiting process. In the following section, we explore theoretically what predictions follow from Fick's first and second laws for both ideal and non-ideal systems.

2. Scaling law for ideal and non-ideal systems

Our aim is now to provide a theoretical description of water evaporation from non-ideal solutions, limited by diffusion in the liquid and under unidirectional advection, which corresponds to our experimental conditions.

2.1 Evaporation in simple aqueous systems. Before describing the more realistic system with self-assembly processes, it is useful to examine the simple case of an ideal solution of a very dilute volatile solute in a non-volatile solvent. For this case, advection is negligible compared to diffusion. Using Fick's first law, the diffusion flux of solute per area $J_{\text{diff}}^{\text{solute}}$ is

$$J_{\text{diff}}^{\text{solute}} = -D_0 \frac{\partial \phi}{\partial z} \quad (1)$$

Combined with the equation of continuity, one arrives at Fick's second law

$$\frac{\partial \phi}{\partial t} = D_0 \frac{\partial^2 \phi}{\partial z^2} \quad (2)$$

Here we use the volume fraction ϕ to denote concentrations and D_0 is the diffusion coefficient of the pure solvent. As an example, consider the example in which a solution of the volatile solute at the concentration $\phi_{\text{diff}}^{\text{solute}}$ in a non-volatile solvent is exposed to a flowing gas. The volatile solute will evaporate at the surface, triggering a diffusion of solute molecules towards this surface. At the air–liquid interface ($z = 0$), the concentration of the solute is zero and it grows towards the bulk value $\phi_{\text{diff}}^{\text{solute}}$ away from the surface ($z > 0$). The partial differential eqn (2) can be transformed into an ordinary differential equation by introducing the variable transformation to a dimensionless parameter x ;

$$x = z / \sqrt{D_0 t} \quad (t \neq 0) \quad (3)$$

as first shown by Boltzmann.¹⁴ Using the boundary conditions $\phi^{\text{solute}} = 0$ at $z = 0$ and $\phi^{\text{solute}} = \phi_{\text{bulk}}^{\text{solute}}$ at $z = \infty$, the solution of eqn (2) is

$$\phi^{\text{solute}}(z, t) = \phi_{\text{bulk}}^{\text{solute}} \operatorname{erf} \left(\frac{z}{2\sqrt{D_0 t}} \right) \quad (4)$$

where erf is the error function. Eqn (4) shows that the concentration profile has the same functional form at all times, with a length scale that increases as $(D_0 t)^{-1/2}$, which is typical of a diffusion-limited process.

The evaporation rate, which is defined as the mass of the evaporated solute per unit time, $dm(t)/dt$, can be written using either a local or an integral approach:

$$\begin{aligned} \frac{1}{\text{Area} \cdot \rho} \frac{dm(t)}{dt} &= -J_{\text{diff}}(0) = \frac{d}{dt} \left[\int_0^\infty (\phi_{\text{bulk}} - \phi(z, t)) dz \right] \\ &= D_0^{1/2} \phi_{\text{bulk}} (\pi t)^{-1/2} \end{aligned} \quad (5)$$

Interestingly, this simple model yields a diffusion-limited signature that is very similar to what is observed in all our experiments, even though such a model lacks several crucial elements. Firstly, in the system that we study experimentally the solvent, water, evaporates rather than the solute. An advective term must thus be included in the model to take into account the liquid flow from the reservoir, which compensates the evaporated volume of water. Secondly, amphiphiles/water solutions are strongly deviating from ideality. Thirdly, the diffusion coefficient is not a constant and it depends on the concentration in each position. Fourthly, the gradient in chemical potential allows for the formation of other phases in addition to the bulk homogeneous solution. Despite these considerable additional difficulties, some major qualitative features of eqn (4) remain relevant for the complex case, as will be discussed in the following section.

2.2 Gradient and flow in an evaporating system. Fig. 1A shows a schematic representation of the capillary set-up to study interfacial phase separation in a water gradient.¹ Water evaporates



at the gas liquid interface but the position of this interface is kept fixed by controlling the hydrostatic pressure. Water evaporation thus gives rise to a liquid flow $v(t)$, which for an incompressible system is independent of the position in the capillary, z . Due to water evaporation, the solute becomes more concentrated close to the interface, which in turn triggers a diffusive flow J_{diff} of the non-volatile solute in the opposite direction. For the incompressible binary system, the diffusive flows of solute and solvent will exactly cancel out in order to keep the volume constant.¹⁵ The diffusion of one component in one direction is necessarily compensated by the diffusion of the other component in the opposite direction. Thus, the process can be characterized by a single diffusion constant, D . The net flow of the solute is then

$$\begin{aligned} J(z, t) &= -v(t)\phi(z, t) + J_{\text{diff}}(z, t) \\ &= -v(t)\phi(z, t) - \frac{D(\phi)}{RT}\phi \frac{\partial \mu}{\partial z} \end{aligned} \quad (6)$$

In the second equality, we have introduced a generalization of Fick's first law, which accounts for non-ideality in the thermodynamics by specifying the driving force as the gradient in chemical potential, μ , rather than the gradient in concentration, ϕ . The chemical potential of water (μ_w) is directly related to the water activity (a_w) and the relative humidity (RH) as

$$\Delta\mu_w = RT \ln(\text{RH}/100) = RT \ln(a_w) \quad (7)$$

In eqn (6), we also allow for a concentration dependence of the diffusion coefficient. The equation of continuity results in

$$\frac{\partial \phi}{\partial t} = -\frac{\partial J(z, t)}{\partial z} = v \frac{\partial \phi}{\partial z} + \frac{\partial \left\{ \frac{D(\phi)}{RT} \phi \frac{\partial \mu}{\partial \phi} \frac{\partial \phi}{\partial z} \right\}}{\partial z} \quad (8)$$

Boundary conditions are set by $\phi(z = \infty) = \phi_{\text{bulk}}$ and $\phi(0) = \phi_0$, where the second boundary condition is determined by the condition that the solvent water is in equilibrium with the gas phase with controlled RH. In addition, the net solute flow is zero at the air-liquid interface, $J(0, t) = 0$, so that the transport due to the advective flow is cancelled by the diffusive flow at this position. It follows from eqn (6) that

$$v(t) = -D(\phi_0) \left\{ \frac{d\mu}{d\phi} \frac{\partial \phi}{\partial z} \right\}_{z=0} / RT \quad (9)$$

It is a formidable task to solve eqn (8) for a typical non-ideal system. However, it is possible to obtain a substantial simplification of the problem by making the variable transformation of eqn (3). Similar to the simple example of eqn (4), the partial differential eqn (8) can be transformed into an ordinary differential equation by introducing the variable transformation to a dimensionless parameter x , expressed in eqn (3):

$$x = z / \sqrt{D_0 t}$$

where D_0 is the diffusion coefficient of pure water, which we introduce to make x non-dimensional. This leads to:

$$-\frac{1}{2}x \frac{d\phi}{dx} = -\frac{1}{C_0} \left\{ \frac{d\phi}{dx} \right\}_{x=0} \frac{d\phi}{dx} + \left(\frac{d\phi}{dx} \right)^2 \frac{df_S}{d\phi} + f_S(\phi) \frac{d^2\phi}{dx^2} \quad (10)$$

$$f_S(\phi) \stackrel{\text{def}}{=} \frac{D(\phi)}{D_0 RT} \phi \frac{d\mu}{d\phi}; \quad 1/C_0 \stackrel{\text{def}}{=} \frac{D(\phi_0)}{D_0 RT} \left\{ \frac{d\mu}{d\phi} \right\}_{\phi=\phi_0}$$

with the boundary conditions at $x = 0$ and $x = \infty$ preserved. The condition in eqn (9) has been used to eliminate $v(t)$ in eqn (8), a full derivation is presented in ESI.† Even though it is difficult to obtain an explicit solution of eqn (10), there exists a specific solution $\phi(x)$ satisfying the time independent boundary conditions at both ends of the capillary. This solution describes the functional form of the concentration profile. The profile at a given time, t_1 , is then obtained by the using the coordinate transformation of eqn (3) so that $x = z / \sqrt{D_0 t_1}$. This leads to the significant prediction that the shape of the concentration profile is preserved during the process, while the length scale increases proportionally to the square root of time. Even without explicitly solving the diffusion equations, we can conclude that all properties that are proportional to the length-scale increase linearly with the square root of time. The fundamental reason for a scaling behavior is that there is no external length-scale in the problem.

In deriving eqn (10) we have assumed that $\phi(z)$ is a continuous function that is differentiable for all values of z . This condition is not fulfilled for the case where there is a phase change in the interfacial layer, which indeed may occur in the concentration gradient in, for example, amphiphile-water systems. If we assume local equilibrium in the gradient, the position of the phase change is determined by the local thermodynamic conditions. When such a change occurs at some position, z_1 , the chemical potential, $\mu(z)$, is still a continuous function, while there are discontinuities in the function describing the concentration profile, $\phi(z)$, as well as the function describing the variation in the diffusion coefficient at various positions in the interfacial film, $D(z)$. For the formal solution of eqn (10) it is then necessary to treat the different single-phase regions separately and then join them by boundary conditions determined by thermodynamic conditions at the phase boundaries (Fig. 1C). There is again no introduction of an external length-scale. Thus, there is a unique solution in the variable x (eqn (3)), and one preserves the property of a unique concentration profile with a real space length-scale that increases as the square root of time.

We have arrived at some specific predictions about the concentration profile without explicitly solving the diffusion equation. These predictions are based on three assumptions. The first is the validity of the generalized form of Fick's second law. The second assumption is that the state of the system is determined by the local thermodynamic variables so that phase boundaries occur at the same local chemical potentials in the gradient as in the equilibrium bulk systems. The third and more specific assumption is that the rate limiting transport



process for the evaporation is the diffusion in the condensed phase.

Under the assumption of local thermodynamic equilibrium, phase transitions occur at given volume fractions $\{\Phi_{ij}\}$, which are determined by bulk thermodynamics. A given phase thus exists within a composition range $\{\Phi_a, \Phi_b\}$ (Fig. 1C). For a given relative humidity at the air–liquid interface, eqn (10) yields a given concentration profile $\Phi^{\text{RH}}(x)$. The stability region of a given phase characterized by $\{\Phi_a, \Phi_b\}$ corresponds to a constant value of $(x_a - x_b)$. The distance between these phase boundaries is then:

$$z_a - z_b = \sqrt{D_0}(x_b - x_a) \cdot \sqrt{t} = \text{constant} \cdot \sqrt{t} \quad (11)$$

The experimental data in Fig. 3 clearly demonstrate such $t^{1/2}$ dependence with high accuracy. The slope of the curve is proportional to $\sqrt{D_0}(x_b - x_a)$, which depends on the relative humidity only for the phase in contact with air. It follows from eqn (11) that the ratio between the thicknesses of two such phases should be constant in time, which is also shown in the experimental data displayed in Fig. 3B.

The magnitude of the advective flow, v , is given by eqn (9), which can be rewritten using the variable transformation of eqn (3):

$$v = -D(\phi_0) \left\{ \frac{d\mu}{dx} \right\}_{x=0} (RT)^{-1} (D_0 t)^{-1/2} \quad (12)$$

This shows that v decreases with the inverse square root of time. The mass evaporation rate is then given by:

$$\frac{dm}{dt} = v(t) \text{Area} \cdot \rho \quad (13)$$

and the mass loss through evaporation, $m(t)$, thus scales with the square root of time, which fully agrees with experimental measurements displayed in Fig. 2A.

Overall, theoretical and experimental scaling behavior are in excellent agreement, without making any specific assumptions on the characteristics of the systems in terms of how diffusion coefficient and chemical potential vary in the gradient. This agreement supports the main assumption of the model, which is that diffusion in the condensed phase is the rate-limiting process for water evaporation in the present systems.

3. Quantitative evaluation of mutual diffusion coefficients in mesophases

The scaling law derived in the previous section provides a generic description of evaporation, but it remains to interpret the specific quantitative parameters such as pre-factors and proportionality constants. Mathematically, the characteristics of the system are contained in the function $f_s(\Phi)$ and the constant C_0 in eqn (10). In principle, these two quantities can be calculated if the concentration profile in the layer and the activity–concentration isotherm are known. It would then be possible to obtain values of the diffusion coefficient at all concentrations, $D(\Phi)$. In practice, this procedure will be limited mainly by the spatial resolution of the concentration measurement, in particular, for the thin outer phase that is in

contact with air.¹ Another limitation in precision is the activity–concentration isotherm determination at high relative humidity (RH) based on sorption techniques. In this section, we use a simpler approach based on an approximation supported by experimental observations and theoretical scaling in order to extract the order of magnitudes of mutual diffusion coefficients of the different phases.

Using infra-red microscopy, we have monitored the concentration gradient in the capillary. Within experimental error, the concentration gradient is observed to linearly vary with z within a given phase.¹ Furthermore, the IR data show that the concentrations at the boundaries between two phases in the non-equilibrium gradient correspond to their equilibrium counterparts. A drastic change in the boundary conditions at the air–liquid interface result in a rapid response of the system as illustrated in Fig. 4. This shows that the self-assembly reorganization time is much shorter than the time needed for the build-up of the gradient, which is consistent with the local equilibrium hypothesis. The rapid reorganization time and the fact that the concentration gradients are approximately linear suggest that a quantitative evaluation of the parameters characterizing the system can be obtained within a quasi steady-state approximation.

The essence of the quasi steady-state approximation is to assume that at a given moment in time the flow in the system is the same as for a system at steady state with the same thickness and the same concentration at the boundaries. The scaling law ensures that the final result does not depend on the choice of the specific time. Using this approximation one can estimate mutual diffusion coefficients in this system, neglecting the effect of non-equilibrium dynamics.

At steady state, $\frac{\partial \phi}{\partial t} = 0 = -\frac{\partial(-v\phi + J_{\text{diff}})}{\partial z}$. Therefore, the net flux $-v\phi + J_{\text{diff}}$ is constant over the whole capillary. Since the net flux is zero at the evaporation boundary, it is thus zero everywhere. It follows from eqn (6) that:

$$v_{\text{ss}} = \frac{D(\phi)}{RT} \frac{\partial \mu}{\partial z} = \frac{D(\phi)}{RT} \frac{d\mu}{d\phi} \frac{d\phi}{dz} \quad (14)$$

We assume a constant average diffusion coefficient within a phase, since the main concentration dependence of D is caused by a change in the mesostructure. Integrating eqn (14) between the corresponding phase boundaries Φ_2 and Φ_1 yields:

$$v_{\text{ss}} = \frac{D_{\text{ab}}}{z_b - z_a} \int_{\phi_a}^{\phi_b} \frac{1}{RT} \frac{d\mu}{d\phi} d\phi \quad (15)$$

where $D_{\text{ab}}/(z_b - z_a) = P_{\text{ab}}$ is the permeability of the phase between the boundaries a and b (Fig. 1C).

Eqn (15) allows a quantitative evaluation of the mutual diffusion coefficient under the quasi-steady-state approximation:

$$D_{\text{ab}} = v_{\text{ss}}(z_b - z_a)/(\mu_b - \mu_a) \quad (16')$$

This equation can be alternatively expressed with time-independent quantities using the scaling law:

$$D_{\text{ab}} = v_0(x_b - x_a)/(\mu_b - \mu_a) \quad (16'')$$

with $v(t) = v_0 t^{-1/2}$.



We can extract v_0 values from gravimetric measurements of water evaporation under the conditions of quasi steady-state, thicknesses through optical microscopy images, and the activity–composition isotherm through sorption calorimetry measurements.¹ We can thus evaluate the mutual diffusion coefficients for the different phases using eqn (16). For the present system, the average constant diffusion coefficient for the lamellar phase is estimated to $(1.2 \pm 0.2) \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$, for the hexagonal phase the estimated diffusion coefficient is $(3.4 \pm 1.0) \times 10^{-11} \text{ m}^2 \text{ s}^{-1}$ and for the micellar cubic phase we obtain $D = (8.0 \pm 2.0) \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$. Strikingly, the mutual diffusion coefficient varies roughly by an order of magnitude between the different phases, and is always at least one order of magnitudes lower than the self-diffusion coefficient of water in a pure aqueous solution. In addition, taking explicitly the non-ideality of the system through the activity–composition relationship was found to be crucial in the quantitative evaluation.

We now turn towards a comparison of these mutual diffusion coefficients values with simple models and other published values. The lamellar phase is a one-dimensional liquid crystalline structure, which can be described as an alternating stack of hydrophobic layers, the hydrocarbon chains, and hydrophilic layers, the hydrophilic heads and water. If we consider a repetition unit consisting of one hydrophobic layer and one hydrophilic layer, we can estimate the effective diffusion coefficient of water through this repetition unit¹⁶ (see ESI†). This effective coefficient will strongly depend on the orientation of the stack with respect to the flux. In the capillary, stacks are orthogonal to the water flux, as evidenced by the anisotropic SAXS patterns. This is the alignment that most efficiently hinders water evaporation at the surface as water molecules must cross the hydrophobic layers in which they have a low solubility. The rate-limiting step is thus water diffusion through hydrophobic layer for self-diffusion and most likely also for the mutual diffusion. For such an oriented lamellar structure, the perpendicular diffusion coefficient can be estimated simply based on the structure dimensions, local diffusion coefficients in water and in hydrocarbon and the oil/water partition coefficient¹⁶ to $(2.1 \pm 0.6) \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$ (for more details, see ESI†). This value is in close agreement with the value obtained from our experiments, which is consistent with the modelling of the structure/transport relationship for the lamellar phase. If the lamellar phase was instead oriented with lamellae parallel to the flux, a larger diffusion coefficient would be expected, although the activity–composition relationship would be unchanged. This highlights the predominant role of mesostructure orientation in this transport problem. There exists a large collection of permeability measurements for phospholipid bilayers in the literature. For liquid crystalline bilayers composed of dioleoyl phosphatidylcholine (C18:1 chains), permeability values ranging between $P = 3\text{--}13 \times 10^{-4} \text{ m s}^{-1}$ have been reported,^{20–23} which corresponds to specific resistances to diffusive transport of $\rho = P \cdot d_{\text{bilayer}}/2 = 0.72\text{--}3.1 \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$, where d_{bilayer} is the bilayer thickness taken as 4.8 nm. This range of values is compatible with the mutual diffusion coefficient we evaluated for the DDM (12C:0). Our method is thus an alternate

mean to evaluate water transport across bilayers in of oriented lamellar phases rather than monitoring release from unilamellar vesicles.

In the hexagonal and micellar cubic phase, there exists continuous pathways for water to diffuse through hydrophilic regions, which gives rise to faster self-diffusion compared to the lamellar phase. In the water gradient, the channels between the rods in the hexagonal phase become narrower. At the phase boundary towards the lamellar phase, the hexagonal phase contains around 12 wt% water, while at the other phase boundary towards the micellar cubic phase, the hexagonal phase contains around 47 wt% water.^{1,13} This difference in water content explains the difference in diffusion coefficients for the micellar cubic and hexagonal phases. The hydrophilic layers are constituted of water and maltoside chains. Nilsson and Söderman¹⁷ showed that the water self-diffusion in such systems is similar to water self-diffusion in the corresponding aqueous sugar solutions. In our system, the diffusion coefficient values obtained for the hexagonal and the micellar cubic phases indeed fall within the expected range for the corresponding sucrose/water solutions.^{18,19}

A direct consequence of the low diffusion coefficient of the outer oriented lamellar phase at the air–liquid interface is the low value of the evaporation rate, given by eqn (15). The system spontaneously forms an efficient barrier against evaporation, which is sufficient to induce a change in the transport limiting step compared to pure water.

4. Evaporation rate and humidity self-regulation

Fig. 2 demonstrates that there are qualitative differences in the behavior of the evaporation rate between pure water and the surfactant system. For the latter system, the rate decreases in time as $t^{-1/2}$, which signifies the rate-limiting step is the diffusion in the liquid phase. The rate is thus determined by the magnitude of the diffusion coefficient in the condensed phase. During evaporation, there appears a sequence of phases in the interfacial region and it follows from the results of the previous section that the thicknesses of the respective phases adjust to give (nearly) the same diffusional flow in the different phases. The observation that the lamellar phase is much thinner than the hexagonal and cubic ones shows that it has a much lower mutual diffusion coefficient.

We now turn to a practical consequence of the step in the diffusion coefficient profile occurring at the phase boundary. As shown in Fig. 2B, the evaporation rate is virtually constant up to 85% RH in the air. This qualitative behavior is very similar to what is found for *stratum corneum*, the outer layer of our skin,^{10,24–26} and the non-linear transport behavior strongly contrasts with the evaporation rate from a pure water solution (Fig. 2B). In this section, we want to unveil the microscopic origin of such a behavior and discuss its generality. The mass evaporation rate writes as:

$$\frac{dm(t)}{dt} = \text{Area} \cdot \rho \frac{d}{dt} \int_0^\infty (\Phi_{\text{bulk}} - \Phi(z, t)) dz \quad (17)$$

This integral formulation can be rewritten to explicit the various phases of the system, lamellar (0,a), hexagonal (a,b),



micellar cubic (b,c) and micellar (c,∞):

$$\frac{dm(t)}{dt} = \text{Area} \cdot \rho \left(\frac{d}{dt} \left(\int_0^{z_a} (\Phi_{\text{bulk}} - \Phi(z,t)) dz + \int_{z_a}^{z_b} (\Phi_{\text{bulk}} - \Phi(z,t)) dz + \int_{z_b}^{z_c} (\Phi_{\text{bulk}} - \Phi(z,t)) dz + \int_{z_c}^{\infty} (\Phi_{\text{bulk}} - \Phi(z,t)) dz \right) \right) \quad (18)$$

The experimental data suggests that the concentration gradient within a phase is approximately linear, which is consistent with quasi-steady-state and leads to:

$$\frac{dm(t)}{dt} = \text{Area} \cdot \rho \left[\frac{dz_a}{dt} (\Phi_{0,\text{RH}} + \Phi_a) + \frac{d(z_b - z_a)}{dt} (\Phi_a + \Phi_b) + \frac{d(z_c - z_b)}{dt} (\Phi_b + \Phi_c) + \frac{d}{dt} \left(\int_c^{\infty} (\Phi_{\text{bulk}} - \Phi(z,t)) dz \right) \right] \quad (19)$$

Eqn (14) shows that the thickness growth rate of a given phase is determined by the product of its mutual diffusion coefficient and activity range. The lamellar phase has a much lower mutual diffusion coefficient than the other phases and a comparable activity range. As a result, the thickness growth rate of this phase is much smaller than the growth rates of the other phases, and it can therefore be neglected in eqn (19). Following eqn (11), the growth rates of the other phases has no explicit dependence on the air relative humidity but may exhibit an indirect dependence through the concentration gradient. However, we have observed through infra-red and SAXS microscopy that the concentration gradient in the inner phases is unchanged upon varying the relative humidity.¹ Consistently, the experimentally measured growth rates of these phases are independent of the relative humidity. Therefore, the evaporation mass rate is itself independent of the boundary condition $\Phi_{0,\text{RH}}$ up to the thermodynamic disappearance of the lamellar phase at the air-liquid interface at 85% RH (Fig. 2B). This macroscopic self-regulation behavior thus rests on a structure with low water mutual diffusion coefficient at the air-liquid interface, which exists over a large range of water activity. This phase will respond to humidity changes by adapting its thickness so that its overall permeability remains practically constant as the chemical potential at the air-liquid interface changes.²⁷

In practice, this behavior should be common in complex aqueous solutions, containing amphiphiles, polymers and colloids. Indeed, in the vicinity of the air-liquid interface, water is scarce. Therefore, the water activity rapidly changes with concentration, which ensures an extended range of existence for the driest phase formed by the system. Furthermore, structures formed in the water poor region tend to optimize the hydration of the solute, which will lead to low mutual diffusion coefficients. Nonetheless, the quality of this evaporation self-regulation will depend on the exact values of the diffusion coefficient and the activity range at which the least permeable structure exists. In the experimental system presented, an extremely low diffusion coefficient is achieved in the

driest phase where the lamellae are oriented perpendicularly to the evaporation flow. If the lamellae were oriented parallel to the evaporation flow, which would correspond to the same activity profile, the self-regulation behavior would be weaker as the lamellar phase would exhibit a similar growth rate as the hexagonal phase.

Conclusions

In this article, we presented an experimental and theoretical investigation of water evaporation from aqueous solutions of amphiphilic molecules. Using milli-fluidic drying cells, we monitored the build-up of interfacial structure composed of several liquid crystalline phases at the air-liquid interface. This interphase corresponds to a gradient in both composition and mesostructure, which spontaneously forms in response to the non-equilibrium conditions imposed by evaporation. Several mesophases of distinct structures and thus transport properties are formed within this interphase. All time-dependent quantities exhibit a square root of time scaling. Analyzing the advection/diffusion transport equation for non-ideal solutions we demonstrate that this scaling law is a general consequence of diffusion limited transport in the liquid phase. The scaling law is valid independently of the characteristics of the system, such as diffusion coefficient and activity profiles as long as the evaporation is diffusion controlled.

We extracted values of mutual diffusion coefficients for the different mesophases encountered along the gradients. The driest phase possesses a lamellar structure with lamellae oriented perpendicularly to the water flow and exists over a large range of relative humidities below 85% RH. The mutual diffusion coefficient was measured as $(1.2 \pm 0.2) \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$, which agrees with a simple structure model and literature data for lamellar bilayers.¹⁶ Our method thus enables the measurement of mutual diffusion coefficients in aligned structures.

We discussed a striking macroscopic behavior observed in such systems, but also in biological systems such as *stratum corneum*, which is the independence of the evaporated mass with relative humidity. This macroscopic behavior rests on a structure with low water mutual diffusion coefficient at the air-liquid interface, which exists over a large range of water activity. In practice, this behavior is expected to be general to complex aqueous solutions, containing amphiphiles, polymers and colloids.

To conclude, our results suggest that in order to describe drying, filtration and centrifugation of complex aqueous systems, a non-ideal and non-equilibrium thermodynamic description based on activity and diffusion coefficient profiles is required.

Conflicts of interest

There are no conflicts to declare.

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Evaporation, diffusion and self-assembly at drying interfaces: Supporting Information

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S1. Calculation of the effective diffusion coefficient of water in a lamellar phase oriented perpendicularly to the evaporation flux

Assuming that the lamellar phase can be described as a stack of alternating homogeneous hydrophobic and hydrophilic layers, we can calculate the effective mutual diffusion coefficient of water perpendicular to a repetition unit of the lamellar phase as:¹

$$D_{\text{perpendicular}} = \frac{D_1(d_1+d_2)^2}{(d_1+Kd_2)\left(d_1+\left(\frac{D_1}{KD_2}\right)d_2\right)} \quad (\text{S1})$$

where d_1 is the thickness of the hydrophobic layer (hydrocarbons tails), d_2 is the thickness of the hydrophilic layer (water + sugar headgroups), D_1 the diffusion coefficient of water in the hydrophobic layer, and D_2 the diffusion coefficient of water in the hydrophilic layer. The equilibrium partition coefficient of water between the hydrophilic layer and hydrophobic layer is defined as $K = \frac{c_{\text{sugar}}^{\text{water}}}{c_{\text{tail}}^{\text{water}}}$. Here, $c_{\text{sugar}}^{\text{water}}$ is directly calculated from the experimentally known amount of water in the lamellar phase. The solubility of water in dodecane, which is an adequate model for the hydrophobic layer consisting of C_{12} tails, is reported as $c_{\text{dodecane}}^{\text{water}} = 2.69 \text{ mmol/L}$ dodecane.² This value corresponds to the solubility of water in dodecane that is in equilibrium with water. To calculate the solubility of water in dodecane that is in equilibrium with a water/sugar solution, the hydrated hydrophilic heads, we need the chemical potential variation of water between pure water this water/sugar solution. This leads to the expression of the water concentration in the tail region:

$$c_{\text{tail}}^{\text{water}} = c_{\text{dodecane}}^{\text{water}} \cdot \exp\left(\frac{\Delta\mu_{\text{lamellar}}^{\text{water}}}{RT}\right) \quad (\text{S2})$$

From the measured activity/composition isotherm (Figure S1), we read $-1.5 < \Delta\mu_{\text{lamellar}}^{\text{water}} < -0.2$, which then leads to: $0.6 \text{ mmol/L} < c_{\text{tail}}^{\text{water}} < 2.2 \text{ mmol/L}$ and thus $3350 < K < 550$. Since the lamellar phase composition range is $0.018 < \phi_{\text{lamellar}}^{\text{water}} < 0.12$, and the surfactant head accounts for 49% of the surfactant volume,³ we can estimate $0.8 < d_1/d_2 < 1$ for the lamellar phase. The diffusion coefficient of water in the tail, D_1 , is taken as the self-diffusion coefficient of water in water, $2.3 \cdot 10^{-9} \text{ m}^2/\text{s}$, the diffusion coefficient of water in the hydrophilic layer, D_2 , is taken as the diffusion coefficient of water in a concentrated sugar solution, $3 \cdot 10^{-11} \text{ m}^2/\text{s}$ (the precise value of D_2 has in practice no quantitative consequences on the outcome of the calculations). Together, this leads to an estimate of the diffusion coefficient according to Eqn (S1):

$$1.6 \cdot 10^{-12} \text{ m}^2/\text{s} < D_{\text{perpendicular}} < 2.6 \cdot 10^{-12} \text{ m}^2/\text{s} \quad (\text{S3})$$

S2. Activity/Composition isotherm of water and surfactant

We measured the activity/composition isotherm for water at 23°C using sorption calorimetry (Figure S1, top),⁴ where the water activity, a_w , is directly related to the chemical potential of water, $\Delta\mu_w$, as

$$\Delta\mu_w = RT \ln a_w \quad (S4)$$

Since this is a purely binary system, the surfactant activity/composition isotherm can be recalculated from the water activity/composition isotherm using the Gibbs-Duhem relationship. The result is shown (Figure S1) below together with an extrapolation to conditions with low surfactant concentration. The sorption calorimetry method does not provide accurate measurements for high water activities (low surfactant concentration), which limits the precision of the calculations for this concentration regime (determination of the effective mutual diffusion coefficient in the micellar cubic phase, for instance).

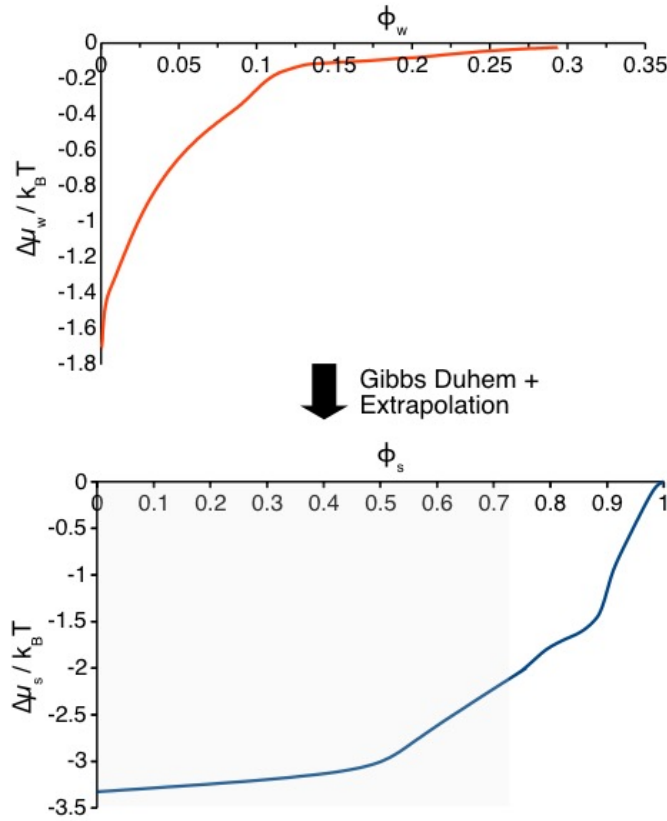


Figure S1 : Top: Activity/Composition isotherm of water in the binary system water/alpha-dodecylmaltoside measured through sorption calorimetry. Bottom: activity/composition isotherm of the surfactant in this binary system calculated from the water isotherm using Gibbs-Duhem relationship and extrapolating at low surfactant fractions.

S3. Derivation of eqn 10 using a variable transformation

The equation of continuity results in

$$\frac{\partial \phi}{\partial t} = -\frac{\partial J(z,t)}{\partial z} = -v \frac{\partial \phi}{\partial z} + \frac{\partial \left\{ \frac{D(\phi)}{RT} \phi \frac{\partial \mu}{\partial \phi} \frac{\partial \phi}{\partial z} \right\}}{\partial z} \quad (8)$$

where the net flow of the solute, $J(z, t)$, is then given by eqn (6), and the advective liquid flow is

$$v(t) = -D(\phi_0) \left\{ \frac{d\mu}{d\phi} \frac{\partial \phi}{\partial z} \right\}_{z=0} / RT \quad (9)$$

The partial differential eqn (8) can be transformed into an ordinary differential equation by introducing the variable transformation to a dimensionless parameter x ,

$$x = z/\sqrt{D_0 t} \quad (t \neq 0) \quad (3)$$

where D_0 is the diffusion coefficient of pure water. The partial derivatives of x with respect to z and t are expressed as

$$\frac{\partial x}{\partial t} = \frac{-z}{2t\sqrt{D_0 t}} = -\frac{x}{2t} \quad (S5)$$

and

$$\frac{\partial x}{\partial z} = \frac{1}{\sqrt{D_0 t}} \quad (S6)$$

The left hand side of eqn (8) can be rewritten using the variable transformation (3 and S5), giving

$$\frac{\partial \Phi}{\partial t} = \frac{\partial \Phi}{\partial x} \frac{\partial x}{\partial t} = -\frac{x}{2} \frac{\partial \Phi}{\partial x} \cdot \frac{1}{t} \quad (S7)$$

Using the same variable transformation (3 and S6), the first term of the right hand side of eqn (8) can be written as

$$v \frac{\partial \Phi}{\partial z} = -\frac{D(\Phi_0)}{RT} \left\{ \frac{\partial \mu}{\partial \Phi} \frac{\partial \Phi}{\partial z} \right\}_{z=0} \cdot \frac{\partial \Phi}{\partial z} = -\frac{D(\Phi_0)}{RT} \frac{1}{\sqrt{D_0 t}} \left\{ \frac{\partial \mu}{\partial \Phi} \frac{\partial \Phi}{\partial x} \right\}_{x=0} \cdot \frac{1}{\sqrt{D_0 t}} \frac{\partial \Phi}{\partial x} = -\frac{1}{C_0} \cdot \left\{ \frac{\partial \Phi}{\partial x} \right\}_{x=0} \cdot \frac{\partial \Phi}{\partial x} \cdot \frac{1}{t} \quad (S8)$$

where C_0 is defined as

$$1/C_0 \stackrel{\text{def}}{=} \frac{D(\Phi_0)}{D_0 RT} \left\{ \frac{d\mu}{d\phi} \right\}_{\phi=\phi_0} \quad (S9)$$

and the second term at the right hand in eq 8 can be written as

$$\begin{aligned} \frac{\partial}{\partial z} \left\{ \frac{D(\Phi)}{RT} \Phi \frac{\partial \mu}{\partial \Phi} \frac{\partial \Phi}{\partial z} \right\} &= \frac{\partial}{\partial z} \left\{ \frac{D(\Phi)}{\sqrt{D_0 t} RT} \Phi \frac{\partial \mu}{\partial \Phi} \frac{\partial \Phi}{\partial x} \right\} = \frac{\partial}{\partial x} \left\{ \frac{D(\Phi)}{D_0 RT} \Phi \frac{\partial \mu}{\partial \Phi} \frac{\partial \Phi}{\partial x} \right\} \cdot \frac{1}{t} = \frac{\partial}{\partial x} \left\{ f_s(\Phi) \frac{\partial \Phi}{\partial x} \right\} \cdot \frac{1}{t} = \\ &\left\{ \frac{\partial f_s}{\partial x} \left(\frac{\partial \Phi}{\partial x} \right)^2 + f_s(\Phi) \frac{\partial^2 \Phi}{\partial x^2} \right\} \cdot \frac{1}{t} \end{aligned} \quad (S10)$$

where $f_s(\Phi)$ is defined as

$$f_s(\phi) \stackrel{\text{def}}{=} \frac{D(\phi)}{D_0 RT} \phi \frac{d\mu}{d\phi} \quad (S11)$$

Combining eqn 8, S7, S8, and S10 finally gives

$$-\frac{x}{2} \frac{\partial \Phi}{\partial x} = -\frac{1}{C_0} \cdot \left\{ \frac{\partial \Phi}{\partial x} \right\}_{x=0} \cdot \frac{\partial \Phi}{\partial x} + \left(\frac{\partial \Phi}{\partial x} \right)^2 \frac{\partial f_s}{\partial x} + f_s(\Phi) \frac{\partial^2 \Phi}{\partial x^2} \quad (10)$$

S4. Mesostructure characterization using SAXS

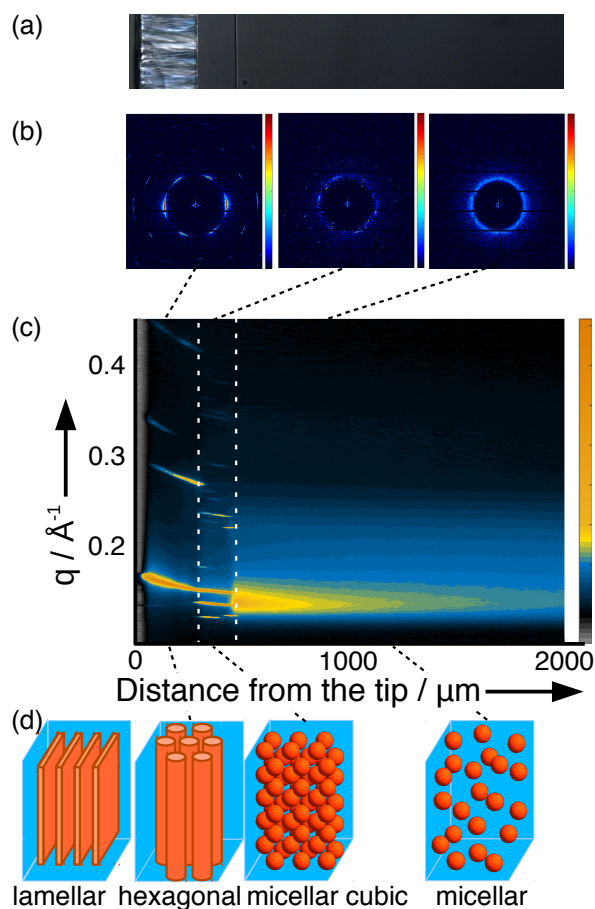


Figure S2 : Several mesophases are observed along the concentration gradient extending from the capillary's tip to the reservoir (a). We characterized these mesostructures using SAXS. Two dimensional pattern were observed and displayed anisotropy for the lamellar and hexagonal phases, which shows that these phases are oriented in the capillary setup (b). Azimuthal integration was performed to obtain structure maps, which give the peak positions for the different mesophases (c). From the peak sequence, we can deduce the mesostructure (d).

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