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Numerical study of the relationship between the spherulitic microstructure and isothermal crystallization kinetics. Part I. 2-D analyses

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ABSTRACT

In this paper, we proposed a numerical model to study the kinetic properties and the spherulite microstructure of a semi-crystalline polymer under isothermal crystallization, which further exhibits the potential in generating the 2D spherulitic structure according to the observations obtained by experimental techniques. Two characteristic parameters are introduced, namely, characteristic length L_c and characteristic time t_c , which are dependent on the growth rate, G and the nucleation rate, I . In addition, two non-dimensional parameters are introduced to model the nucleation saturation: L_d/L_c and t^*/t_c , which is related to the thickness of nucleation exclusion zone L_d , and the effective nucleation time t^* , respectively. In 2D modeling, the kinetics are confirmed by Avrami fitting, and the effects of the four characteristic parameters on the Avrami parameter n and the crystallization half-time $t_{0.5}$ are presented. The regularity of how the spherulite density or the mean radius of spherulites \bar{R} change along with these parameters are also given, respectively. It shows that L_c is the prominent parameter for the size of the spherulite, and t_c controls $t_{0.5}$ as long as there is no nucleation saturation ($L_d = 0$ and $t^* \rightarrow \infty$). Besides, the existence of the nucleation saturation increases the mean radius of spherulites, but decreases n from 3 to 2 in 2-D modeling. Finally, a relationship between crystallization kinetics and microstructures is provided, giving a new perspective to estimate the nucleation rate.

1. Introduction

The mechanical behavior of semi-crystalline polymers is highly dependent on their microstructure, particularly with regard to plasticity or damage mechanisms (see, e.g. Refs. [1–4]). However, the existing numerical frameworks allow to study independently the influence of each microstructural parameter to enrich our understanding. Nevertheless, the validity of these numerical experiments is based jointly on the relevance of the microstructural model and the constitutive laws. For this reason, it is necessary to develop realistic microstructural models.

The vision adopted in this paper is to generate the spherulitic microstructure of semi-crystalline polymers, based on the physical

processes of crystallization. It should be noted that the spherulitic microstructure we focused on only concerns the radius and the eccentricity of spherulites regardless of the internal properties such as lamellar thickness, branching, etc. Crystallization and its kinetics are controlled by two phenomena: nucleation and growth (see, e.g. Refs. [5–9] for review). There are two main approaches to study the kinetics of spherulite crystallization: one based on direct observation and the other on differential scanning calorimetry (DSC). Direct observation by optical microscopy allows to measure the growth rate of spherulites, G , as well as the nucleation rate, I . This technique makes it possible to follow the evolution of the number of spherulites and the residual area fraction of molten polymer as a function of time, during an isothermal crystallization (see Fig. 1). Nucleation begins slowly and, then, the

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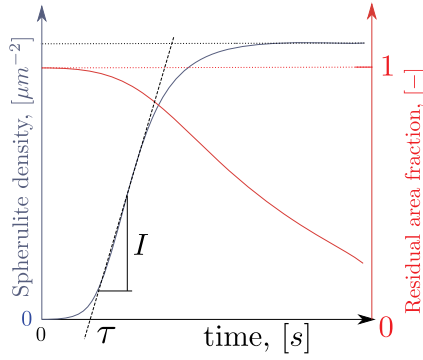


Fig. 1. Scheme of the evolution of the spherulite density versus time during isothermal crystallization as well as the evolution of residual area fraction, which is the ratio of the melt surface over the total surface.

number of spherulites increases linearly with a slope, I , called primary nucleation rate. According to Okada and Hikosaka [10] the onset time, τ , can be defined as the intersection of the extrapolated linear part with the abscissa axis. Finally, the number of spherulites saturates to reach a plateau, which is the final spherulite density. We can emphasize that the nucleation saturates well before the molten polymer is completely crystallized as Okui et al. have observed [11]. Note that the direct observation is limited to 2D observations on thin films. The calorimetric approach, which is easier to carry out, requires the use of Avrami-type models to determine the parameters I and G . There are a large number of studies combining DSC analyses and/or optical microscopy (see, e.g. Refs. [12–22]). However, to the best of our knowledge, there is no study comparing the results obtained from these two techniques, especially for the estimation of nucleation rate, I . In addition, the phenomenon of nucleation saturation is not generally taken into account in the Avrami-type models. Okui et al. suggest two hypotheses to explain this saturation [11]: the presence of nucleating agent or the existence of an excluded nucleation zone [23].

There are numerous papers devoted to the modeling and the analysis of the crystallization kinetics [24–35], most of which are based on the Avrami-type models [36–39] under isothermal condition, or on Nakamura and Ozawa's equation for nonisothermal crystallization [40–42]. Specifically, the modified factors related to mechanical properties [24–27] have also included the effect of flow on the crystallization. The influence of the temperature gradient [29] and the confined volume [31–33,43–46] on the crystallization have also been further discussed. The primary and secondary nucleation of polymer crystals have been studied at the atomistic scale by molecular dynamics or Monte-Carlo methods [47–59]. Kinetic models have been developed for polymer to model thermal and athermal nucleation [60–63]. However, Avrami-type models, atomistic simulations, and kinetic models of nucleation do not take the morphology evolution into account and cannot provide information about the final crystalline structure.

Several computer methods have been proposed to predict the crystallization kinetics and the morphology of semi-crystalline polymers. These include the level set method [64], the front-tracking method [65,66], the phase field method [67–75], the pixel coloring method [30–32,76–84], the cellular automaton method [85–87], the stochastic simulation [88], the Monte-Carlo method, and the ray-tracking method [89–92]. Note that the prediction of spherulitic microstructure is crucial to understand the relationships between properties and the process as evidenced by the number of studies on the topic (see, e.g. Refs. [89–105]).

The aim of this paper is to propose a numerical framework for spherulitic microstructure generation, based on the results of direct observations of crystallization, i.e. able to model growth and nucleation as well as its saturation. At present, we focus on the 2D analyses

Table 1

List of symbols.

Symbol	Description
<i>Geometry description</i>	
L	Side length of the Representative Volume Element (RVE)
$S_0 = L^2$	RVE area
<i>Input parameters</i>	
G	Growth rate of spherulite
I	Nucleation rate
$L_c = G^{\frac{1}{3}}I^{-\frac{1}{3}}$	Characteristic length in 2D
$t_c = G^{-\frac{2}{3}}I^{-\frac{1}{3}}$	Characteristic time in 2D
L_d	Thickness of nucleation excluded zone
t^*	Effective nucleation time
τ	Onset time
<i>Microstructural symbols</i>	
$\theta(\mathbf{x}_k)$	Lamellar orientation inside the k^{th} cell
$S^{(i)}$	Area of the i^{th} spherulite
$R^{(i)} = (S^{(i)}/\pi)^{0.5}$	Equivalent radius of the i^{th} spherulite
\bar{R}	Mean spherulite radius
$e^{(i)}$	Eccentricity of the i^{th} spherulite
<i>Kinetic symbols</i>	
$\chi(t), \chi_\infty$	Degree of crystallinity at time t and at the end
$\alpha(t) = \chi(t)/\chi_\infty$	Degree of transformed material
K_{Av}, n	Avrami's constant and Avrami's exponent
$t_{0.5}$	Crystallization half-time
$N(t), N_\infty$	Number of spherulites at time t and at the end
<i>Numeric parameters</i>	
\mathbf{x}_k	Center coordinate of k^{th} cell
Δx	Side length of cells
Δt	Time step
$\varphi(\mathbf{x}_k)$	State variable of k^{th} cell
$t_0(\mathbf{x}_k)$	Nucleation time of k^{th} cell

regardless of the secondary crystallization, and we only take into account the temperature effect and spherulitic structure with one crystalline phase. Here, the key concept is the concept of nucleation time fields that allows us to model the sporadic nucleation of spherulites. The nucleation time is a random time associated with each space point of our model giving the moment when a stable crystalline seed appears. An analysis of the influence of the model parameters on the isothermal kinetics and the microstructure is conducted. The study originality is based on the introduction of a characteristic length, L_c and a characteristic time, t_c . Indeed, these new parameters opens up new perspectives to describe the relationships between crystallization kinetics and microstructure. In addition, we study the consequences of the two hypotheses previously cited on kinetics and microstructure to explain the nucleation saturation.

The paper is organized as followed: First, in Section 2, we describe the isothermal crystallization model and numerical framework. In Section 3, the simulation results on spherulitic microstructure and kinetics are presented in 3.1 and 3.2. A further discussion is given in Section 4. The symbols used in this paper are listed in the Table 1.

2. Numerical modeling and methodology

In this section, we present the model and the associated numerical framework, to simulate the nucleation and the growth of spherulites at the mesoscale. The area of interest, called the Representative Volume Element (RVE), is discretized into square cells with side length Δx and center coordinate \mathbf{x}_k (see Fig. 2). The cells are characterized in terms of discrete state variables, $\varphi(\mathbf{x}_k)$, such as $\varphi(\mathbf{x}_k) = 0$ for melt and $\varphi(\mathbf{x}_k) = i$ for cells inside the i^{th} spherulite; and crystallite orientation, the polar angle $\theta(\mathbf{x}_k)$.

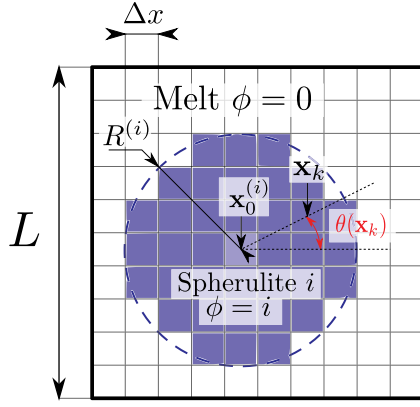


Fig. 2. Representative volume element of the spherulite modeling, where $\mathbf{x}_0^{(i)}$ is the nucleation center of spherulite i and $\theta(\mathbf{x}_k)$ the lamella orientation at point \mathbf{x}_k .

2.1. Concept of nucleation time

We propose to model the spherulite nucleation for isothermal crystallization with the concept of nucleation time, $t_0(\mathbf{x}_k)$. The nucleation time, $t_0(\mathbf{x}_k)$, is a random time associated with the k^{th} cell of coordinates \mathbf{x}_k . It defines the onset time of the first germ for k^{th} cell. It is randomly generated (see Fig. 3(a)) at the beginning of each simulation by the following expression:

$$t_0(\mathbf{x}_k) = \lambda(\mathbf{x}_k)t_0^{\max} + \tau, \quad \text{with } \lambda = \text{rand}(0,1), \quad (1)$$

where τ is the onset time and $t_0^{\max} = I^{-1}(\Delta x)^{-2}$ is the time where the nucleation is certain inside the cell of surface $(\Delta x)^2$ for a given nucleation rate, I .

To model the nucleation saturation, two different ideas are studied (see Fig. 3). Firstly, we propose to introduce an effective nucleation time, $t^* < t_0^{\max}$, which acts as a superior limit of the nucleation time (see Fig. 3(a)), such as:

$$t_0(\mathbf{x}_k) = \begin{cases} \lambda(\mathbf{x}_k)t_0^{\max} + \tau & \text{if } \lambda(\mathbf{x}_k) \leq \lambda_{\max} \\ \infty & \text{if } \lambda(\mathbf{x}_k) > \lambda_{\max} \end{cases} \quad (2)$$

where $0 \leq \lambda(\mathbf{x}_k) < 1$ is a random field and $\lambda_{\max} = t^*/t_0^{\max}$.

Secondly, we also study an excluded nucleation zone around spherulites [23], modeled by a length parameter L_d , which is the layer thickness where the nucleation is inhibited (see Fig. 3(b)).

The effective nucleation time controls the spherulite number (cf. Equation (13)), this concept could be used to model the effect of nucleating agents. The existence of an excluded nucleation zone may be due to thermo-mechanical or diffusional effects around the spherulite that would promote growth over nucleation, such as the depletion zone observed in thin films [8]. Note that it is possible to model the nucleation using the activation frequency and the saturation by introducing the nucleus density [31,32,76,77].

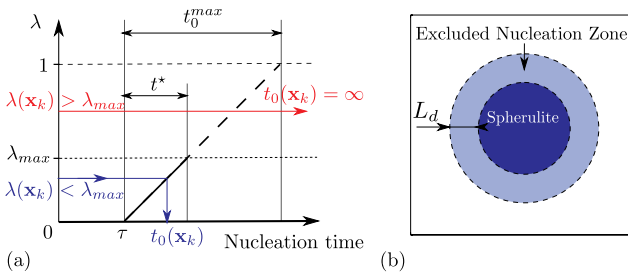


Fig. 3. Scheme of the two strategies to model the nucleation saturation: (a) Introduction of effective nucleation time t^* ; (b) Introduction of the excluded nucleation zone L_d [23].

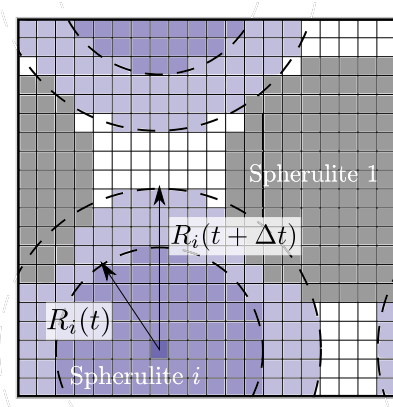


Fig. 4. Schematic representation of the growth step used under periodic boundary conditions.

2.2. Algorithm of growth and nucleation

The pixel coloring algorithm [31,32,76,77] is used to model the spherulite growth. In this method, we take advantage of isotropic growth of spherulites at the microscale for isothermal crystallization. The transformation rule describing the phase change (see Fig. 4) is as follows: if the molten cell \mathbf{x}_k , i.e. $\varphi(\mathbf{x}_k) = 0$, is inside the i^{th} circle, so the cell is transformed into i^{th} spherulite, $\varphi(\mathbf{x}_k) = i$. The i^{th} circle, which represents the shape of the spherulite if it is isolated from other spherulites, is defined by its radius $R_i(t) = G(t - t_0^{(i)})$, where $t_0^{(i)}$ is the nucleation time associated with the i^{th} spherulite and $\mathbf{x}_0^{(i)}$, its nucleation point. Note that periodic boundary conditions (see Fig. 4) are applied to avoid edge effects. The simulation algorithm is as follows:

1. Random generation of nucleation time $t_0(x_k)$ for all cells
2. Time loop for $t \in \{0; \Delta t; 2\Delta t; \dots; N\Delta t\}$
 - (a) Nucleation step: Creation of a new i^{th} spherulite of center, $\mathbf{x}^{(i)} = \mathbf{x}_k$ if $t_0(x_k) < t$ and the cell of x_k is inside the melt area where the nucleation is possible.
 - (b) Growth step: Loop over all i^{th} spherulites
 - Compute $R_i(t) = G(t - t_0^{(i)})$
 - Transform the molten cells inside the i^{th} circle associated with the i^{th} spherulite
3. Post-processing

2.3. Post-processing

At the end of the simulation, all the cells have been assigned to one spherulite. We obtain the final morphology of the spherulite microstructure. We compute two types of information, which are linked to the microstructure and the kinetics. These data are then used to perform our statistical analyses.

2.3.1. Microstructural analysis

The area $S^{(i)}$ of the spherulite i can be obtained by collecting its cells, from which we can directly calculate the equivalent radius of the spherulite, such as:

$$R^{(i)} = \sqrt{\frac{S^{(i)}}{\pi}}. \quad (3)$$

The mean value, \bar{R} is estimated from several simulations.

The growth direction of crystalline lamellae is assumed radial (see Fig. 2). We define the lamella orientation, $\theta(x_k)$, as the angle between the lamella growth direction given by the vector $(x_k^{(i)} - x_0^{(i)})$ and the x -axis for all $x_k^{(i)}$ inside the i^{th} spherulite.

2.3.2. Kinetic analysis

During the simulation, the number of spherulites, $N(t)$, and the degree of transformed material, $\alpha(t)$ are stored at each step time. The degree of transformed material is given by:

$$\alpha(t) = 1 - \frac{n_0(t)}{n_t} \quad (4)$$

where $n_0(t)$ is the number of molten cells at time t and n_t the total number of cells in the simulation box. For isothermal cases, the degree of transformed material is related to the degree of crystallinity, such as $\alpha(t) = \chi(t)/\chi_\infty(T)$ where $\chi_\infty(T)$ is the final degree of crystallinity at the given temperature T .

The Avrami theory is applied to analyze the isothermal crystallization kinetics by fitting the data with the following equation:

$$\alpha(t) = 1 - \exp(-(K_{Av}t)^n) \quad (5)$$

where Avrami's parameters are the exponent n and the Avrami's characteristic time K_{Av} . The exponent n are determined by linear regression of Avrami's plot with $\alpha(t)$ in the range from 0.05 to 0.95. The Avrami's characteristic time K_{Av} is determined by measuring the crystallization half-time $t_{0.5} = \frac{(\ln 2)^{\frac{1}{n}}}{K_{Av}}$.

2.4. Model parameters

There are four parameters that control the crystallization model growth: the nucleation rate, I , the growth rate G , the effective nucleation time, t^* , and the thickness of nucleation exclusion zone, L_d . In our study, we introduce two new parameters instead of G and I : a characteristic length, L_c , and a characteristic time, t_c (see Table 2), defined by:

$$L_c = \left(\frac{G}{I}\right)^{\frac{1}{d+1}}, \quad t_c = (G^d I)^{-\frac{1}{d+1}} \quad (6)$$

where $d = 2$ is the dimension of space. According to the isothermal crystallization properties of various semi-crystalline polymers at different crystallization temperature [11], the characteristic length, L_c , ranges from 10 to $10^2 \mu\text{m}$ and the characteristic time, t_c , ranges from 10^{-3} to 10^5 s. As we will see in Section 3, the parameters L_c and t_c control the size of the microstructure and the kinetics, respectively. It will be shown that the final average spherulite diameter is L_c^2 and that t_c is the time over which nuclei are formed without considering nucleation saturation.

In addition to the parameters of the model, we have the parameters related to the simulation: the size of the simulation box, L ; the space step, Δx and the time step, Δt . The space step is chosen at $\Delta x = 1 \mu\text{m}$ which is of the same order of magnitude as the resolution of an optical microscope. The time step is chosen to guarantee the proper functioning of the algorithm such as $\Delta t = \min(G\Delta x/3, t_{0.5}/50)$.

3. Simulation results

This section presents 2D simulation results of the morphology and the kinetics of the spherulite growth. The influence of four parameters, *i.e.* L_c , t_c , L_d/L_c and t^*/t_c , are analyzed in details. We use the additional parameters L_d/L_c and t^*/t_c because they control the effect of nucleation saturation independently of the values of L_c and t_c . Each simulation is

Table 2
Model parameters.

	Variable	Description
Space variables	$L_c = G^{1/3}I^{-1/3}$	Characteristic length
	L_d	Thickness of excluded nucleation zone
Time variables	$t_c = G^{-2/3}I^{-1/3}$	Characteristic time
	t^*	Effective nucleation time

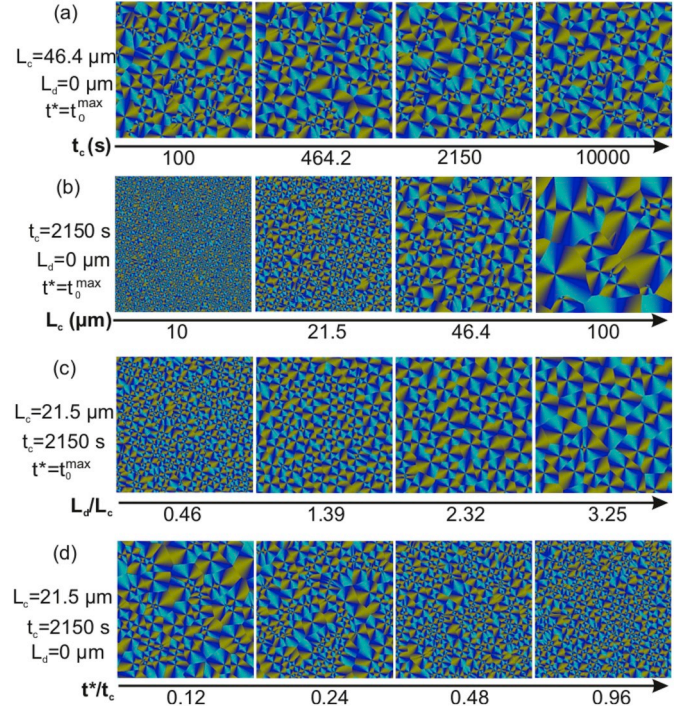


Fig. 5. Examples of final spherulitic morphologies at various cases. The color contrast is due to the lamellar orientation, θ , inside the spherulites. (All results are presented using Paraview software [106]). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

based on the square RVE of $L = 500 \mu\text{m}$, and 500×500 cells with length $\Delta x = 1 \mu\text{m}$ are employed. Besides, the onset time is fixed as $\tau = 0$ s.

3.1. Spherulitic morphology

The influence of the four parameters on the spherulitic morphology is depicted in Fig. 5. In each row, three of the four parameters are fixed, and the evolution of spherulitic microstructure along with the increase of the remaining parameter can be observed. Fig. 6(a–d) represents the spherulite size distribution at the final stage of crystallization in terms

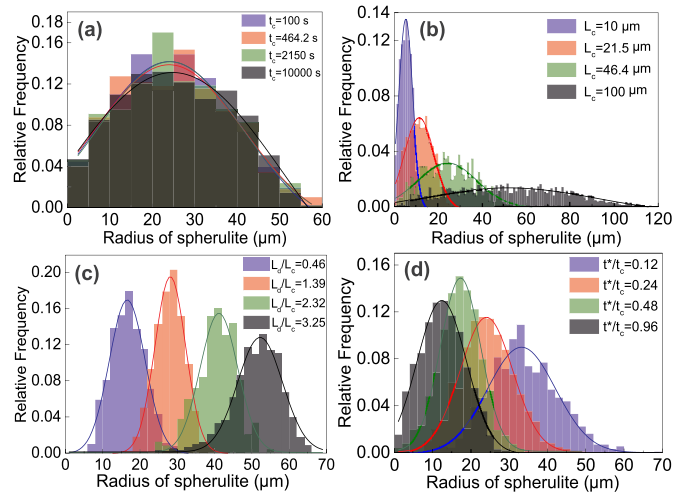


Fig. 6. Simulated spherulite size distributions in terms of spherulite radius. The lines represent curve fits by the use of normal distribution. (a) $L_c = 46.4 \mu\text{m}$, $L_d/L_c = 0$, and $t^* = t_0^{\max}$; (b) $t_c = 2150$ s, $L_d/L_c = 0$, and $t^* = t_0^{\max}$; (c) $t^* = t_0^{\max}$, $L_c = 21.5 \mu\text{m}$, and $t_c = 2.15 \times 10^3$ s; (d) $L_d/L_c = 0$, $L_c = 21.5 \mu\text{m}$, and $t_c = 2.15 \times 10^3$ s.

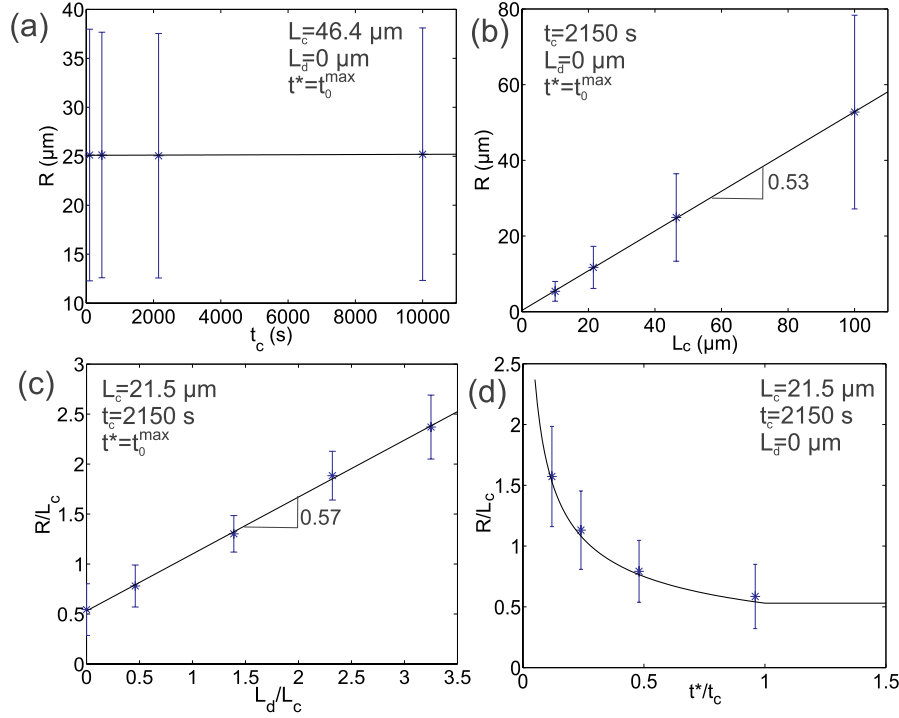


Fig. 7. Mean spherulite radius versus the parameters t_c , L_c , L_d/L_c , and t^*/t_c . Standard deviation is indicated through error bars.

of the spherulite radius for the various cases corresponding to Fig. 5(a–d). The results are fitted by using a normal distribution. Finally, Fig. 7 gives the spherulite radius and its standard deviation versus the four parameters.

Firstly, t_c is increased from 100 s to 10^4 s by fixing $L_c = 46.4 \mu\text{m}$, $L_d = 0$, and $t^* = t_0^{\text{max}}$. The change of t_c while keeping L_c as a constant is obtained by adapting G and I according to Eq. (6). The value of L_c is fixed at higher value to obtain larger spherulites which are easier to observe and the other two parameters are fixed at $L_d = 0 \mu\text{m}$, and $t^* = t_0^{\text{max}}$ to avoid the influence of the nucleation saturation. The spherulitic microstructures are shown in Fig. 5 (a), where it is obvious that the size of spherulite does not change with t_c . Fig. 6 (a) shows the spherulite size distribution at the final stage of crystallization in terms of the spherulite radius over the range of provided t_c , indicating approximately the same average value and distribution. It can also be seen in Fig. 7 (a) that the mean radius and the standard deviation keeps constant at various t_c , which further confirmed the independence of the spherulite size with t_c .

In order to study the influence of L_c , we set $t_c = 2150 \text{ s}$, $L_d = 0 \mu\text{m}$, and $t^* = t_0^{\text{max}}$ (to avoid the influence of nucleation saturation), and we increased L_c from $10 \mu\text{m}$ to $100 \mu\text{m}$. The corresponding morphologies are shown in Fig. 5 (b), demonstrating that the number of spherulites decreases along with increasing L_c , while the size of the spherulites raises. Fig. 6 (b) shows the spherulite size distribution at the final stage of crystallization in terms of the spherulite radius over the range of provided L_c . It can be observed that the final spherulite size shifts tremendously to higher values from the condition of small L_c with a large number of nuclei to the condition of large L_c with a small number of nuclei. Furthermore, we summarized the radius of spherulites for the four conditions. The results are plotted as a function of L_c in Fig. 7 (b), where the mean radius and its standard deviation are presented. It is very interesting to see the mean radius obey a linear increase along with L_c with a tangent of 0.53, and the standard deviation grows simultaneously. As we expected, the characteristic length, L_c , is close to the equivalent diameter of the spherulite. Therefore, we can find that the mean spherulite radius, \bar{R} , is roughly equal to $0.5L_c$.

The nucleation exclusion zone also has a tremendous effect on the

morphology in the numerical model, whose length is introduced by L_d . Thus, we set $t^* = t_0^{\text{max}}$ to neglect the effect of end time of nucleation, $L_c = 21.5 \mu\text{m}$, and $t_c = 2.15 \times 10^3 \text{ s}$, and the non-dimensional parameter L_d/L_c ratio is increased from 0.46 to 3.25 with a step of 0.92 which is associated with the length of nucleation exclusion zone L_d ranging from $10 \mu\text{m}$ to $70 \mu\text{m}$ with a step of $20 \mu\text{m}$. Fig. 5 (c) presents the corresponding morphologies at various L_d/L_c , where the increase of spherulite size can be observed. Fig. 6 (c) gives the simulated spherulite size distributions in terms of the spherulite radii over the range of investigated L_d/L_c values. The size of spherulites presents a gradual shift to larger values from low L_d/L_c to high L_d/L_c ratio, resulting from the decreasing number of nuclei. Moreover, the spherulite radii R are calculated for the four cases respectively, and we plot R/L_c and its standard deviation as a function of L_d/L_c ratio, as shown in Fig. 7 (c). It is shown that the mean value of R/L_c increases linearly along with the L_d/L_c ratio, but the standard deviation remains unchanged. It should be pointed out that the tangent of the curve is independent on L_c and t_c .

Finally, the effect of effective nucleation time t^* on the morphology in the numerical model is studied. We set $L_d/L_c = 0$ to neglect the effect of the nucleation exclusion zone, $L_c = 21.5 \mu\text{m}$, and $t_c = 2.15 \times 10^3 \text{ s}$, and the non-dimensional parameter t^*/t_c ratio, which is associated with the end time of nucleation, is increased from 0.12 to 0.96, produces the corresponding final morphology as presented in Fig. 5 (d). Fig. 6 (d) gives the simulated spherulite size distributions in terms of the spherulite radii over the range of investigated t^*/t_c values, where the size of spherulites presents a gradual shift to lower values from small t^*/t_c to large t^*/t_c , resulting from the increasing number of nuclei. Then, the R/L_c ratio and its standard deviation related to spherulite radius R are plotted for the four cases respectively, showing a decrease in the averaged value along with t^*/t_c . It should be pointed out that the tangent of the curve is independent on L_c and t_c . However, the standard deviation of the spherulite size does not seem to be influenced by t^*/t_c .

3.2. Kinetic properties

Fig. 8 presents the Avrami analysis for the cases with various combination of parameters, where the first column is the Avrami plot

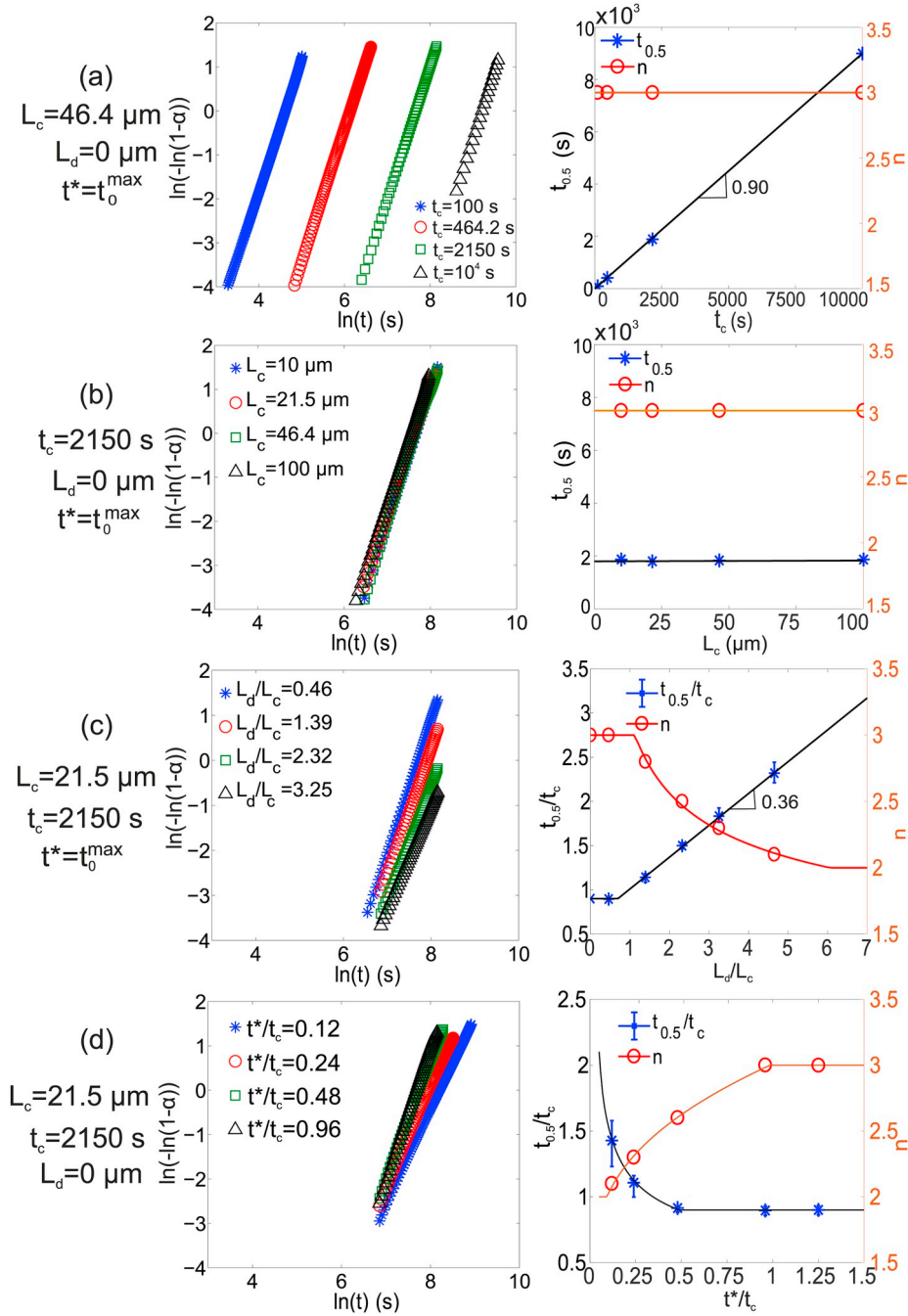


Fig. 8. Kinetic analysis for the various cases. The first column denotes Avrami plots for the isothermal crystallization of the corresponding conditions, and the second column presents Avrami parameters n and crystallization half-time $t_{0.5}$ versus the varying parameters.

and the second column indicates the Avrami parameter n and crystallization half-time $t_{0.5}$ versus the varying parameters, according to the conditions set in Fig. 5. Each curve of the Avrami plot is obtained as an average of 10 random samples. Moreover, the normalized spherulite density, NL_c^2/L^2 , as a function of normalized time, t/t_c , is plotted in Fig. 9 for the corresponding cases, where we can see the normalized spherulite density increases until reaching a plateau. N denotes the number of spherulites. Each curve is calculated by taking the average value of 10 random samples, and the colored region represents the interval of these samples.

Firstly, we set $L_c = 46.4 \mu\text{m}$, $L_d = 0 \mu\text{m}$, and $t^* = t_0^{\text{max}}$, and increased t_c from 100 s to 10^4 s. The Avrami plots are shown on the left in Fig. 8 (a). The crystallization half-time, $t_{0.5}$ and the Avrami exponent, n are plotted as a function of t_c for the four cases correspondingly on the

right. It can be seen that n is constant which is in good agreement with the theoretical value $n = 3$ for the 2D uniform nucleation and growth, and $t_{0.5}$ increases linearly along with t_c . Moreover, the spherulite density as a function of crystallization time is plotted in Fig. 9 (a). Fixing L_c , we can find that the nucleation rate decreases with increasing t_c , but the spherulite density finally reaches the same level.

Then, at fixed $t_c = 2150$ s, $L_d = 0 \mu\text{m}$, and $t^* = t_0^{\text{max}}$, L_c was increased from $10 \mu\text{m}$ to $100 \mu\text{m}$. In Fig. 8 (b), it is noteworthy that n and $t_{0.5}$ remain constant, showing that the crystallization rate is independent of L_c . Fig. 9 (b) presents the spherulite density versus crystallization time for the corresponding four cases, where the curves reach a plateau at the same time.

The Avrami analysis on the kinetic characteristics under various L_d/L_c ratio is given on the left in Fig. 8 (c) by fixing $t^* = t_0^{\text{max}}$, $L_c = 21.5$

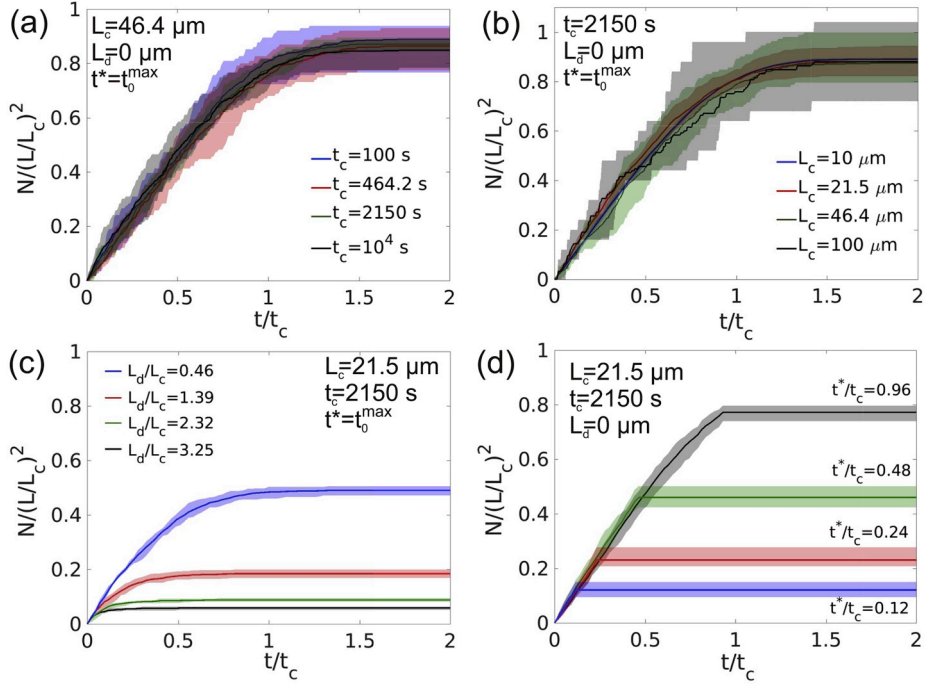


Fig. 9. Normalized number of spherulites as a function of t/t_c for various cases.

μm , and $t_c = 2.15 \times 10^3$ s. The corresponding Avrami exponent n and crystallization half-time $t_{0.5}$ as a function of L_d/L_c are shown on the right in Fig. 8 (c). It can be seen that n decreases from 3.0 to 2.3 for the four increasing L_d/L_c cases. The crystallization half-time $t_{0.5}$ grows with increasing L_d/L_c ratio, indicating a decrease in the kinetics. Besides, the number of spherulites versus crystallization time is provided in Fig. 9 (c). It is obvious that the number of spherulites grows linearly at the initial time with the same nucleation rate, and finally reaches a plateau, which goes up with decreasing L_d/L_c . It indicates that the higher L_d/L_c leads to less nuclei resulting from the large nucleation exclusion zone.

Finally, the Avrami analysis on the kinetic characteristics under various t^*/t_c ratio is presented on the left in Fig. 8 (d) when $L_d/L_c = 0$, $L_c = 21.5 \mu\text{m}$, and $t_c = 2.15 \times 10^3$ s. The corresponding Avrami exponent n and crystallization half-time $t_{0.5}$ as a function of t^*/t_c ratio are also given. It can be seen that n increases from 2.1 to 3.0 for the four increasing t^*/t_c cases. The crystallization half-time $t_{0.5}$ falls with increasing t^*/t_c ratio, indicating an acceleration in the kinetics. Besides, the spherulite density versus crystallization time is provided in Fig. 9 (d), which indicates that the higher t^*/t_c ratio leads to more nuclei due to the larger nucleation time.

4. Further discussion

4.1. Parameter influence

4.1.1. Influence of the characteristic length L_c and the characteristic time t_c

First of all, we note that the microstructure and the crystallization rate depend jointly on the nucleation rate, I , and the growth rate, G . More precisely, the average spherulite area (respectively the number of spherulites, N) is proportional to the square of the characteristic length $L_c = G^{1/3}I^{-1/3}$ (respectively $N \propto 1/L_c^2$), whereas L_c has no effect on the kinetics of crystallization. The characteristic time, $t_c = G^{-2/3}I^{-1/3}$, conversely, controls the kinetics and has no influence on the final morphology. In the case where the nucleation saturation is not considered, the normalized density of spherulites (NL_c^2/L^2) versus the normalized time (t/t_c) curve is universal whatever the values of I and G (Fig. 9(a-b)). We obtain a master curve with an initial slope equal to 1, which saturates for $t > 1.4t_c$ at 0.85. This means that the nucleation rate

in our simulation is indeed $I = 1/(t_c L_c^2)$ and that the average maximum number of spherulites inside a surface $S_0 = L^2$ is equal to $0.85S_0/L_c^2$.

The two parameters, t^* and L_d , are useful to model the nucleation saturation before the crystallization ends (see Fig. 9(c-d)). Both have an influence on the kinetics and the microstructure.

4.1.2. Influence of the effective nucleation time, t^*

At first, we discuss the influence of the effective nucleation time, t^* . For this discussion, it is useful to recall and transpose the Avrami Evans Kolmogorov Johnson Mehl type model. Following the review of Piorkowska and Haudin [107], the degree of transformed material, $\alpha(t)$ is defined by:

$$\alpha(t) = 1 - \exp\left(-\frac{E(t)}{S_0}\right) \quad (7)$$

where $E(t)$ is the 'extended surface' which is equal to the total surface of all domains growing from all nuclei inside the reference surface, without considering the impingement of growing domains. It is defined in 2 dimensions by:

$$E(t) = \int_0^t \pi G^2 (t-u)^2 dN(u) \quad (8)$$

where $dN(u)$ is the number of nuclei created at time u inside S_0 . Here, we assume that $dN(u)$ is proportional to both the nucleation rate, I , and the reference surface, S_0 , for $t < t^*$, so that:

$$dN(u) = \begin{cases} S_0 I du & u < t^* \\ 0 & u \geq t^* \end{cases} \quad (9)$$

After integration, we obtain:

$$E(t) = \begin{cases} S_0 \int_0^t \pi I G^2 (t-u)^2 du = \frac{\pi}{3} S_0 \left(\frac{t}{t_c}\right)^3 & \text{for } t < t^* \\ S_0 \int_0^{t^*} \pi I G^2 (t-u)^2 du & \text{for } t \geq t^* \\ = \frac{\pi}{3} S_0 \frac{t^*}{t_c^3} (3t^2 - 3tt^* + (t^*)^2) & \end{cases} \quad (10)$$

Below t^* , this model is similar to the Avrami model with an exponent $n = 3$, above t^* , the behavior tends to a model of Avrami with

an exponent $n = 2$. It is interesting to note that for sporadic nucleation without nucleation saturation ($t^* \rightarrow \infty$ and $L_d/L_c = 0$), this model predicts an exponent $n = 3$ and the crystallization half-time $t_{0.5} = \left(\frac{\pi}{3} \ln 2\right)^{\frac{1}{3}} t_c \approx 0.90 t_c$. These values are obtained by numerical simulation (see Fig. 8a). The asymptotic approximation of equation (10) suggests the following relationship between n and the ratio t^*/t_c :

$$n \approx \begin{cases} 3 & \frac{t^*}{t_c} > 0.99 \\ \frac{14.2}{4.72 - \ln\left(\frac{t^*}{t_c}\right)} & 0.09 \leq \frac{t^*}{t_c} \leq 0.99 \\ 2 & \frac{t^*}{t_c} < 0.09 \end{cases} \quad (11)$$

Note that the simulation results and this equation provide the range of t^* in which the nucleation is purely sporadic ($n = 3$) or instantaneous ($n = 2$) according to Avrami's approach. The asymptotic approximation suggests also the relationship between $t_{0.5}/t_c$ and t^*/t_c :

$$\frac{t_{0.5}}{t_c} \approx \begin{cases} 0.90 & \frac{t^*}{t_c} > 0.49 \\ 0.37 \left(1 + \left(\frac{t^*}{t_c}\right)^{-\frac{1}{2}}\right) & 0.07 \leq \frac{t^*}{t_c} \leq 0.49 \\ 0.47 \left(\frac{t^*}{t_c}\right)^{-\frac{1}{2}} & \frac{t^*}{t_c} < 0.07 \end{cases} \quad (12)$$

The parameter of these relationships are fitted on the simulation results, except for the law given for $t_{0.5}/t_c$ at very small values of $t^*/t_c < 0.07$. In fact, the 'extended surface' is given by the first order approximation of Equation (10), $E(t) \approx \pi S_0 (t^*/t_c) (t/t_c)^2$, for very small value of $t^*/t_c < 0.07$. For this case, we have $t_{0.5}/t_c = (\ln(2)/\pi)^{\frac{1}{2}} (t^*/t_c)^{-\frac{1}{2}} \approx 0.47 (t^*/t_c)^{-\frac{1}{2}}$.

From the microstructural point of view, Equation (9) gives the final number of spherulites, N_∞ inside the reference surface S_0 :

$$N_\infty = N(t^*) = S_0 I t^* = \frac{S_0 t^*}{L_c^2 t_c} \quad (13)$$

So, the mean value of spherulite area, \bar{S} is given by $\bar{S} = N_\infty/S_0 = L_c^2 t_c/t^*$. Assuming that \bar{S} is proportional to \bar{R}^2 , we obtain the following expression:

$$\frac{\bar{R}}{L_c} \approx \begin{cases} 0.53 & \frac{t^*}{t_c} > 1 \\ 0.53 \left(\frac{t^*}{t_c}\right)^{-\frac{1}{2}} & \frac{t^*}{t_c} \leq 1 \end{cases} \quad (14)$$

Here, the parameters are fitted from the simulation results. A good agreement is observed with the simulation results (see Figs. 7(d) and 8(d)).

4.1.2. Influence of the thickness of the nucleation excluded zone L_d

The simulation results suggest that the following relationship for the mean radius is (see Fig. 7 (c)):

$$\frac{\bar{R}}{L_c} \approx 0.57 \left(0.9 + \frac{L_d}{L_c}\right) \quad (15)$$

From the kinetic point of view, the comparison with Avrami's type model would require the introduction of the nucleation excluded zone concept. This would be possible but it is outside the scope of the present paper as it needs specific numerical methods to solve this kind of problem. Here, we prefer to proceed by analogy by taking inspiration from the simulation results. Indeed, all the kinetic and microstructural parameters vary linearly with the ratio $(t/t_c)^{-\frac{1}{2}}$ (see Equations (11), (12) and (14)). We also find that these parameters vary linearly with the L_d/L_c ratio. This is why we propose the following relationship to fit the simulation data:

$$n \approx \begin{cases} 3 & \frac{L_d}{L_c} < 1.12 \\ \frac{10.1}{\ln\left(\frac{L_d}{L_c}\right) + 3.25} & 1.12 \leq \frac{L_d}{L_c} \leq 6.05 \\ 2 & \frac{L_d}{L_c} > 6.05 \end{cases} \quad (16)$$

$$\frac{t_{0.5}}{t_c} \approx \begin{cases} 0.90 & \frac{L_d}{L_c} \leq 0.69 \\ 0.36 \frac{L_d}{L_c} + 0.65 & \frac{L_d}{L_c} > 0.69 \end{cases} \quad (17)$$

Here, these relationships are fitted from simulation results. A good agreement is observed with the simulation results (see Figs. 7(c) and 8(c)).

4.2. Comparison between the two modeling hypotheses of the nucleation saturation

Two assumptions have been studied in this paper to model the nucleation saturation: the excluded nucleation zone, which is defined by the thickness L_d , and the effective nucleation time, t^* . Although both hypotheses induce changes in the Avrami exponent, n , from 2 to 3, they exhibit significantly different effects on the crystallization half-time, $t_{0.5}$, and the spherulite mean radius, \bar{R} .

For the kinetics, we can see the difference by looking at the evolution of the normalized spherulite density as a function of normalized time (see Fig. 9(c-d)). The transition between the part, where the density increases proportionally with time, and the plateau is smoother for the excluded nucleation zone assumption (Fig. 9(c)).

Furthermore, in case of the excluded nucleation zone assumption, the size distributions of spherulite radii show no spherulite of radius less than L_d (see Fig. 6(c-d)). This assumption also changes the relative position of the nucleus inside the spherulite. We introduce the eccentricity of the i^{th} spherulite, e_i to study this effect (Fig. 10(a)). It is defined by $e_i = d_i/R^{(i)}$; where $d_i = \|x_0^{(i)} - x_g^{(i)}\|$ is the distance between the spherulite nucleus, $x_0^{(i)}$, and its centroid $x_g^{(i)}$. The value of e is presented as a function of the Avrami exponent n in Fig. 10(b). The average eccentricity does not seem affected by the effective nucleation time, whereas the existence of the excluded nucleation zone halves its value. It is noteworthy that for low L_d/L_c that do not affect the kinetics ($n = 3$), there is a significant effect on the average eccentricity. This effect is explained by the fact that the nucleus cannot be at a distance less than L_d from the spherulite boundary.

We believe that the experimental study of the eccentricity of spherulites will make it possible to choose or discriminate against one or the other assumptions used to model nucleation saturation, *i.e.* existence of an effective nucleation time or existence of a nucleation excluded zone. Specifically, at a certain Avrami parameter n , if the eccentricity of the spherulites is obvious, the effective nucleation time assumption algorithm can be employed in the modeling. Otherwise, we rather choose the nucleation excluded zone assumption algorithm.

4.3. Relationships between kinetics and microstructure

The last interesting point is the relationship between kinetics and microstructure. Indeed, if we know the growth rate, G , it is possible to generate an equivalent microstructure from the results of the Avrami analysis. More precisely, the Avrami exponent, n , and the crystallization half-time, $t_{0.5}$, provide us the value of t_c and t^* (or L_d) as shown in Steps 1 and 2 of the previous subsection. Finally, the characteristic length is given by $L_c = G t_c$. It is interesting to note that this approach allows to compute the nucleation rate, $I = L_c^{-2} t_c^{-1}$, from the Avrami parameters and the growth rate G by the following expression:

$$I = \frac{0.051}{G^2 t_{0.5}^3} \left[1 + \exp\left(\frac{7.10}{n} - 2.36\right)\right]^3 \quad (18)$$

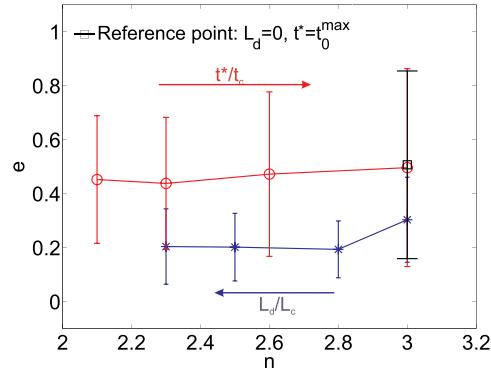
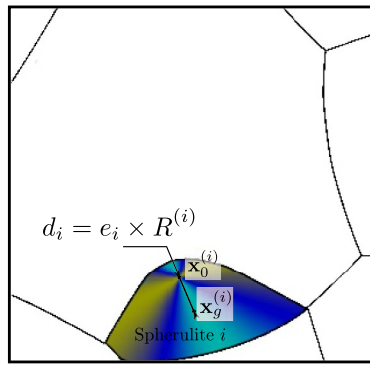


Fig. 10. a) Schematic representation of the algorithm used to generate the microstructure under periodic boundary conditions. b) e versus Avrami parameter n for the two algorithms which introduce nucleation saturation. $L_c = 21.5 \mu\text{m}$, $t_c = 2.15 \times 10^3 \text{ s}$. The red curve denotes the effective nucleation time algorithm, and the blue curve denotes the nucleation excluded zone algorithm. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

this expression is valid for 2D cases and for $2 < n \leq 3$. It should be noted that the surface effects which can lead to transcrystallinity are not taken into account.

Note that Billon and Haudin [108] also provided an algorithm to determine the nucleation rate, I , by combining the isothermal crystallization experiments with the computational simulation.

5. Conclusions

The numerical framework, which is presented in this paper, allows to generate 2D microstructures of isothermal crystallization from physical data such as growth rate, G , and nucleation rate, I . The new concept of nucleation time can well impose the sporadic nucleation or predetermined nucleation (instantaneous nucleation) by introducing the effect of nucleation saturation. Two assumptions have been studied to model the nucleation saturation, namely the existence of an effective nucleation time, t^* , or the existence of a nucleation excluded zone of thickness, L_d .

An analysis was carried out using the characteristic length, $L_c = G^{-1}I^{-\frac{1}{3}}$, and the characteristic time, $t_c = G^{-\frac{2}{3}}I^{-\frac{1}{3}}$, as well as two adimensional parameters (t^*/t_c and L_d/L_c) associated with the two previous assumptions, leading us to the following remarks:

- The mean spherulite radius, \bar{R} is proportional to L_c and independent of t_c ; with a proportionality constant that depends on the dimensionless numbers t^*/t_c and L_d/L_c (cf. Equations (14) and (15)).
- Conversely, the crystallization half-time, $t_{0.5}$ is proportional to t_c and independent of L_c ; with a proportionality constant that depends on the dimensionless numbers t^*/t_c and L_d/L_c (cf. Equations (12) and (17)).
- The nucleation saturation influences the Avrami exponent, n , (cf. Equations 11 and 16), which varies continuously from 3 (no saturation) to 2 (high saturation) for both studied assumptions. In addition, the saturation of the nucleation increases the mean radius of the spherulites and the crystallization half-time according to the laws given by Equations (12) and (14) using the assumption of the existence of an effective nucleation time, and by Equations (15) and (17) using the assumption of the existence of a nucleation excluded zone.
- These simulations allow to highlight a relationship between crystallization kinetics and microstructure. These results suggest that it is possible to generate a microstructure from data from a DSC isothermal analysis, provided that the growth rate G is known (cf. Equation (18)). Nevertheless, a 3D crystallization occurs during DSC experiment. This is the reason why it is necessary to have a 3D numerical framework.

It is interesting to note that the efficiency of our numerical framework offers the possibility to perform 3D simulations containing several hundred spherulites. The extension to 3D cases will be the subject of a further publication [109].

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