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Chapter 0

Complete Active Space (CAS)

Wavefunction-Based Analysis of Magnetization and Electronic Structure

Frédéric Gendron, Hélène Bolvin, and Jochen Autschbach

Abstract A theoretical framework for the generation of natural orbitals, natural spin orbitals, as well as orbital- and spin-magnetizations from multi-configurational ab-initio wavefunction calculations including spin-orbit coupling is presented. It is shown how these computational orbital and magnetization tools can be used to interpret and rationalize the magnetic properties of selected complexes containing transition metals, lanthanides, and actinides.

Units, Notation, Acronyms

The reader is assumed to be familiar with basic concepts of quantum mechanics and computational chemistry. SI or Hartree atomic units (au) are employed. Nuclear motion is ignored in the discussion because our focus is on the electronic structure and bonding, and the resulting magnetic properties. The symbols \cdot and \times indicate inner and outer products, respectively, for vectors and matrices or tensors. Bold-italic notation such as \mathbf{r} , $\hat{\mathbf{S}}$, $\boldsymbol{\mu}$ is used for vectors and vector quantum operators. Upright-bold such as \mathbf{a} , \mathbf{G} , $\boldsymbol{\mu}$ is used for matrices and rank-2 tensors. The EPR pseudo-spin operator is denoted as \mathbb{S} .

The following acronyms are used in the text:

AO	atomic orbital (basis function or actual AO)
CAS	complete active space
CF	Crystal-Field
DFT	Density Functional Theory ('pure' and generalized KS variants)
DMRG	Density Matrix Renormalization Group
EM	electro-magnetic
EPR	Electron Paramagnetic Resonance

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0.1 Introduction

In recent years, analysis tools in terms of orbitals that are familiar to chemists have become available to dissect the electron density, as well as spin-densities and magnetization densities that arise from the orbital angular momentum, based on sophisticated SO multi-reference wavefunction calculations. Furthermore, the magne-

tization densities arising from the spin and orbital angular momentum in SO CAS calculations can be visualized. In combination with the orbitals, detailed information can be extracted from ab-initio calculations about how calculated magnetic susceptibilities and electronic magnetic moments (g -factors) are related to the electronic structure, and ultimately to the structure of, and chemical bonding within, a metal complex.

In Section 0.2, some theoretical aspects underlying these analyses are presented. Section 0.3 presents a variety of case studies spanning the range from 3d metals to actinides.

0.2 Theoretical Methods

We assume that the metal complex is oriented within the laboratory coordinate frame such that its principal magnetic axes coincide with the x , y , and z direction. This can be achieved, for instance, by first calculating the magnetic susceptibility tensor in its Cartesian 3×3 matrix representation (components xx , $xy = yx$, $xz = zx$, yy , $yz = zy$, zz). Diagonalization of the tensor gives its principal values (the eigenvalues) and the principal axis system (PAS, the eigenvectors). The complex is then rotated such that the PAS coincides with the unit vectors of the Cartesian laboratory coordinate frame. Furthermore, the components of degenerate states can be chosen to diagonalize the Zeeman operator for the magnetic field along a selected magnetic axis, as described, for instance, in Reference 5.

Static homogeneous external magnetic fields can usually be described well by the corresponding nonrelativistic orbital and spin Zeeman operators, even if the electronic structure calculation of the complex requires a treatment of relativistic effects. The magnetic moment operator that describes the interaction of the electrons with a magnetic field in direction $u \in \{x, y, z\}$ is in the ‘nonrelativistic with spin’ formalism given by

$$\begin{aligned}\hat{\mu}_u &= -\mu_B \hat{M}_u = -\mu_B (\hat{L}_u + g_e \hat{S}_u) \\ \hat{M}_u &= \hat{L}_u + g_e \hat{S}_u\end{aligned}\tag{0.1}$$

Here, $\mu_B = e\hbar/(2m_e)$ is the Bohr magneton, and $g_e = 2.002\,319\,304\,361\,53(53)$ is the free electron g -value [6]. The small deviations of the free electron g -value from two are due to quantum electrodynamics (QED) corrections to the Dirac relativistic treatment. The operators \hat{L}_u and \hat{S}_u are the dimensionless one-electron operators for the u -component of the orbital angular momentum and the spin angular momentum, respectively.

Let ψ be an electronic ground or excited state wavefunction of the complex, or a component of the respective state if it is degenerate. Based on Equation (0.1), orbital and spin magnetizations can be defined as follows:

$$m_u^L(\mathbf{r}) = \int \psi^* \hat{L}_u \psi d\tau' \quad (0.2a)$$

$$m_u^S(\mathbf{r}) = g_e \int \psi^* \hat{S}_u \psi d\tau' \quad (0.2b)$$

The notation $d\tau'$ indicates an integration over all electron spin degrees of freedom, and *all but one* electron position degrees of freedom. The resulting functions therefore depend on a single electron coordinate. The procedure for calculating the magnetizations is similar to how the electron density ρ is defined in terms of the wavefunction:

$$\rho(\mathbf{r}) = N \int \psi^* \psi d\tau' \quad (0.2c)$$

In the equation for the electron density, N is the number of electrons of the system.

The three functions, $m_u^L(\mathbf{r})$, $m_u^S(\mathbf{r})$, and $\rho(\mathbf{r})$, are real functions of 3D space and therefore they can be visualized easily, for example in cut-planes or as 3D isosurfaces. The volume integrals of these functions over 3D space give

$$\int m_u^L(\mathbf{r}) dV = \langle L_u \rangle \quad (0.3)$$

$$\int m_u^S(\mathbf{r}) dV = g_e \langle S_u \rangle \quad (0.4)$$

$$\int \rho(\mathbf{r}) dV = N \quad (0.5)$$

The integral over the electron density gives the electron number. In the other two cases, the integration gives the expectation value of a component of the orbital or spin angular momentum. We write g_e in the equations in this section, but in the calculations of the individual magnetization densities the QED corrections are neglected and $g_e = 2$ is used for the spin magnetization. Per Equation (0.1), the magnetic moment expectation value is obtained from the magnetizations via

$$\langle \mu_u \rangle = -\mu_B \langle M_u \rangle \quad \text{with} \quad \langle M_u \rangle = \int [m_u^L(\mathbf{r}) + m_u^S(\mathbf{r})] dV \quad (0.6)$$

If ψ is a component of a degenerate state of interest in a computational study of a paramagnetic metal complex, then arbitrary unitary transformations among the state components can be applied without loss of generality. However, the functions $m_u^L(\mathbf{r})$ and $m_u^S(\mathbf{r})$ may not be invariant under such transformations. The electron density $\rho(\mathbf{r})$ for the components of orbitally degenerate states may also be subject to symmetry breaking if the full point group of symmetry of the complex is not enforced in the calculations. Many quantum chemistry programs do not support non-abelian symmetry groups. For example, for a non-bonding orbital of a d^1 transition metal or an f^1 f -element configuration with linear metal coordination and a principal rotational symmetry axis of order $> 2\ell$, with $\ell = 2$ or 3 , respectively, m_ℓ is a good

quantum number at the SR level. Accordingly, the calculated electronic structure should reflect the rotational symmetry. The d and f orbitals can then be classified by their symmetry σ , π , δ , $-$ and ϕ , for f orbitals – with respect to the rotational axis, corresponding to $|m_\ell| = 0, 1, 2, 3$. (This notation is often convenient even when the actual symmetry is lower.) The π , δ , and ϕ levels are doubly degenerate. Single (or triple) occupations of these levels correspond to an orbitally degenerate state. In order for each state component to have a rotationally symmetric electron density individually, the degenerate orbitals must be evenly occupied (e.g. 0.5 each for a d^1 or f^1 configuration) if they are the usual real d or f orbitals. However, NR and SR CAS calculations for such a non-bonding degenerate d^1 or f^1 example will likely produce two state components in which one of the real d or f orbitals is occupied and the counterpart of the same symmetry is unoccupied. As a consequence, the rotational symmetry is broken in the individual state components. Well-defined spin and orbital magnetization densities can be generated easily after a subsequent treatment of the SO interaction, which generally requires complex wavefunction coefficients anyway. The components of the degenerate state are then chosen to diagonalize the magnetic moment operator matrix for a given field direction. In the case studies of Section 0.3, we diagonalize the u component of the magnetic moment operator prior to generating $m_u^L(\mathbf{r})$ and $m_u^S(\mathbf{r})$. Unless stated otherwise, the resulting state component with the most positive $\langle S_u \rangle$ is then chosen for further analysis. For axial complexes, the procedure tends to generate linear combinations of the SR states such that, for the d^1 or f^1 example, equal occupations of π , δ , or ϕ metal orbitals are achieved, which corresponds to forming the angular momentum eigenfunctions from the real d or f metal orbitals.

When NR or SR calculations generate spin eigenfunctions with well-defined quantum numbers S and M_S , then $\langle S_u \rangle = M_S$ if u is the chosen projection quantization axis. In quantum chemistry, $u = z$ is the default choice. The function m_z^S is then nothing but the familiar *spin density*. When the magnetic moment operator for a degenerate state is diagonalized, the direction of the magnetic field defines the quantization axis for the spin and the orbital angular momentum. In relativistic calculations where the effects from spin-orbit (SO) coupling are included in the wavefunctions, spin and orbital angular momentum cease to be good quantum numbers. Of course, the corresponding expectation values can still be calculated, and they are meaningful because of their contributions to the magnetic moment.

When an atomic orbital (AO) basis set $\{\chi_\mu\}$ with real functions is used, as it is customary in quantum chemistry, the electron density and the spin magnetization can be expressed in the AO basis in terms of the elements of density matrices:

$$\rho = \sum_{\mu\nu} \chi_\mu \chi_\nu D_{\nu\mu}^\rho \quad (0.7a)$$

$$m_u^S = \sum_{\mu\nu} \chi_\mu \chi_\nu D_{u,\nu\mu}^S \quad (0.7b)$$

It is important to note that the action of the spin operator is fully considered in Equation (0.2b), and that subsequently all spin degrees of freedom are integrated over.

Therefore, there are no spin degrees of freedom explicitly contained in m_u^S anymore, but of course the function implicitly depends on the action of the spin operator because of Equation (0.2b). The matrices \mathbf{D}^ρ and \mathbf{D}_u^S which are formed by the elements $D_{v\mu}^\rho$ and $D_{u,v\mu}^S$, respectively, are real and symmetric, and therefore they can be diagonalized in order to reduce the double sums in Equations (0.7a,0.7b) to single sums:

$$\rho(\mathbf{r}) = \sum_p n_p [\varphi_p(\mathbf{r})]^2 \quad \text{with} \quad \sum_p n_p = N \quad \text{and} \quad \int [\varphi_p(\mathbf{r})]^2 dV = 1 \quad (0.8)$$

$$m_u^S(\mathbf{r}) = \sum_p n_{u,p}^S [\varphi_{u,p}^S(\mathbf{r})]^2 \quad \text{with} \quad \sum_p n_{u,p}^S = g_e \langle S_u \rangle \quad \text{and} \quad \int [\varphi_{u,p}^S(\mathbf{r})]^2 dV = 1 \quad (0.9)$$

The orbitals (one-electron functions) φ_p are the natural orbitals (NOs), and the numbers n_p are the corresponding populations (occupations). We refer to the eigenfunctions $\varphi_{u,p}^S$ of the spin magnetization components as natural spin orbitals (NSOs). The numbers $n_{u,p}^S$ are the corresponding spin populations. The orbitals are chosen to be normalized, such that the populations of the NOs add up to the total number of electrons, and the sum of the spin populations gives $g_e \simeq 2$ times the expectation value for spin component u . Furthermore, the orbitals are chosen to be real such that for metal d and f orbitals they resemble the orbitals familiar from textbooks. We remind the reader that the NO populations are not necessarily integers, because the wavefunctions may be composed of several, or even very many, Slater determinants, due to a combination of static and dynamic correlation, and SO coupling. The spin populations are likewise not necessarily integers. Examples for how the NO and NSO populations can help with the analysis of complicated electronic structures are provided in Section 0.3.

The orbital magnetization requires additional consideration, because of the derivative term in the (dimensionless) one-electron orbital angular momentum component operator

$$\hat{L}_u = -i \sum_{k=1}^N [\mathbf{r}_k \times \nabla_k]_u \quad (0.10)$$

The notation indicates that the component u of the vector $\mathbf{r}_k \times \nabla_k$ is used to construct \hat{L}_u . The operator \hat{L}_u is imaginary, self-adjoint for square integrable functions, and spin-independent. It is possible to construct, from a many-electron wavefunction, a one-particle density matrix \mathbf{D}^J that can be used to calculate the expectation value of an imaginary operator such as \hat{L}_u as follows:

$$\langle L_u \rangle = -i \sum_{\mu\nu} \langle \chi_\mu | [\mathbf{r} \times \nabla]_u | \chi_\nu \rangle D_{\nu\mu}^J \quad (0.11)$$

The matrix formed by the integrals $\langle \chi_\mu | [\mathbf{r} \times \nabla]_u | \chi_\nu \rangle$ over the real AO basis is real and antisymmetric, i.e. upon multiplication with the factor $-i$ one obtains a purely imaginary Hermitean matrix. Likewise the matrix \mathbf{D}^L is imaginary and antisymmetric, such that the expectation value is real. We use a superscript J for this matrix in

order to associate it with the paramagnetic current density defined below, as it is not specific to the orbital angular momentum. The matrix \mathbf{D}^J with elements $D_{\nu\mu}^J$ can be used to calculate expectation values of any spin-independent quantum operator that is imaginary and has an antisymmetric matrix representation in the AO basis. Since the matrix \mathbf{D}^J is Hermitian, it can be diagonalized to give a set of complex eigenfunctions φ_p^J , and real eigenvalues n_p^J , such that the double sum of Equation 0.11 reduces to:

$$\begin{aligned}\langle L_u \rangle &= -i \sum_p n_p^J \int \varphi_p^{J*} [\mathbf{r} \times \nabla]_u \varphi_p^J dV \\ &= -\frac{i}{2} \sum_p n_p^J \int \left(\varphi_p^{J*} [\mathbf{r} \times \nabla]_u \varphi_p^J - \varphi_p^J [\mathbf{r} \times \nabla]_u \varphi_p^{J*} \right) dV\end{aligned}\quad (0.12)$$

The antisymmetrized form in the second line of Equation (0.12) is more commonly used when the orbital magnetization is re-cast in terms of the real-valued paramagnetic current density. The latter is defined in the context of the present discussion as the real-valued vector field

$$\mathbf{j}(\mathbf{r}) = -\frac{i}{2} \sum_p n_p^J \left(\varphi_p^{J*} \nabla \varphi_p^J - \varphi_p^J \nabla \varphi_p^{J*} \right) \quad (0.13)$$

In terms of the paramagnetic current density, the orbital magnetization is given as

$$m_u^L = [\mathbf{r} \times \mathbf{j}]_u = \sum_p n_p^J [\mathbf{r} \times \mathbf{j}_p]_u \quad (0.14)$$

A per-orbital paramagnetic current density can be defined accordingly as

$$\mathbf{j}_p(\mathbf{r}) = -\frac{i}{2} \left(\varphi_p^{J*} \nabla \varphi_p^J - \varphi_p^J \nabla \varphi_p^{J*} \right) \quad (0.15)$$

The numbers n_p^J do not have as specific of a definition as the NO and NSO populations, because they need to be combined with the action of a spin-independent imaginary operator in order to correspond to an expectation value or magnetization density, as in Equations (0.12) or (0.14).

Löwdin [7] defined natural (spin) orbitals as the eigenfunctions of the full one-particle density matrix in the molecular orbital basis. The NOs, NSOs, and the orbitals used to construct the current density, as described in this section, are not the same as Löwdin's, but they are based on related concepts. The restricted active space self consistent field (RASSCF) [8] and restricted active space state-interaction (RASSI) [9] programs of the Molcas suite [10] have for a long time included modules to calculate matrix elements of various kinds of operators in a basis of spin-free (SF) SR many-electron wavefunctions, which are subsequently transformed to the basis of SO wavefunctions. A key feature of this code is that it generates only the necessary SR density matrix information needed for matrix elements of (i) spin-free real operators (e.g. multipole moments, EFGs), (ii) spin-free real operators multi-

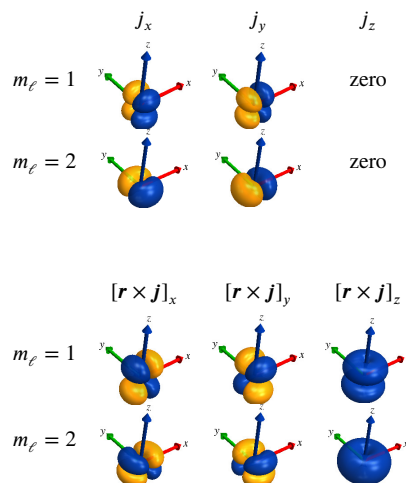


Fig. 0.1 Isosurfaces (± 0.005 au) for the components of the paramagnetic current density \mathbf{j} and the components of the orbital magnetization $\mathbf{m}_\ell^u = [\mathbf{r} \times \mathbf{j}]_u$ generated from analytic expressions of the spherical harmonic angular functions $Y_{\ell}^{m_\ell}$ for d orbitals, i.e. $\ell = 2$ and $m_\ell = 1$ to 2 , multiplied with a normalized $3d$ Slater-type radial function $r^{\ell+2} \exp(-\zeta r)$ with an exponent $\zeta = 2$. There are no contributions from the $m_\ell = 0$ d_σ orbital. The isosurfaces for negative m_ℓ have the same shapes but the functions have the opposite sign patterns. The magnetization quantization axis is z .

plied by \hat{S}_x , \hat{S}_y , or \hat{S}_z and the spin operators themselves, (iii) spin-free imaginary operators (e.g. orbital angular momentum components), or (iv) spin-free imaginary operators multiplied by \hat{S}_x , \hat{S}_y , or \hat{S}_z . We re-arranged this code in such a manner that the corresponding density matrices for cases (i) to (iv) are constructed explicitly for the SO wavefunctions first, while the contraction with the operator AO integral matrices is the very last step of the calculation. This approach gives access both to the operator matrix elements for the SO wavefunctions, and the related (single-state or transition-) density matrices and their eigenfunctions (orbitals). The NOs of this section are related to type (i). The NSOs are related to type (ii), and the eigenfunctions of \mathbf{D}^J are related to type (iii), respectively.

Often, the magnetic properties of a metal complex are intimately tied to formally non-bonding d or f orbitals at the metal center (and magnetic couplings between metal centers, in multi-nuclear complexes or solids). The NOs and NSOs determined from ab-initio calculations then often appear as textbook examples of d or f orbitals, with varying degrees of covalency involving the ligands. In Section 0.3, we will not present individual orbital contributions to m_u^L . However, when the orbital angular momentum magnetization is caused by a single or a few non-bonding metal d or f orbitals, the resulting magnetization m_u^L may easily reveal the underlying contributions from the components of the magnetization density $\mathbf{r} \times \mathbf{j}$ of individual orbitals. For reference, Figures 0.1 and 0.2 display iso-surfaces of the paramagnetic current density components, and the components of the magnetization density, for d and f orbitals with different m_ℓ .

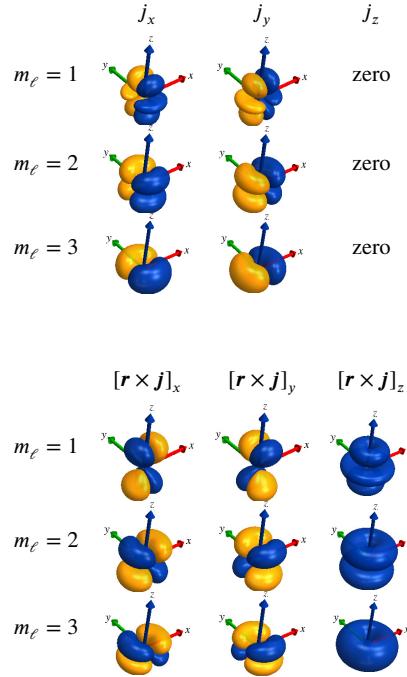


Fig. 0.2 Isosurfaces (± 0.003 au) for the components of the paramagnetic current density \mathbf{j} and the components of the orbital magnetization $\mathbf{m}_u^L = [\mathbf{r} \times \mathbf{j}]_u$ generated from analytic expressions of the spherical harmonic angular functions $Y_\ell^{m_\ell}$ for f orbitals, i.e. $\ell = 3$ and $m_\ell = 1$ to 3 , multiplied with a normalized $4f$ Slater-type radial function $r^{\ell+3} \exp(-\zeta r)$ with an exponent $\zeta = 2$. There are no contributions from the $m_\ell = 0$ f_σ orbital. The isosurfaces for negative m_ℓ have the same shapes but the functions have the opposite sign patterns. The magnetization quantization axis is z .

In the discussion in Section 0.3, the NOs and NSOs correspond to the usual *real* d and f orbitals. For a degenerate pair of these orbitals of π , δ , or ϕ symmetry, an orbitally degenerate rotational symmetry-adapted doublet state arises if there is a single electron or a single hole in the level, i.e. for a combined population of 1 or 3. The real NOs then have occupations of 0.5 or 1.5 each in the two electronic state components. As alluded to above, such an occupation pattern can be viewed as having formed complex linear combinations of the real NOs, with equal weight, to form angular momentum eigenfunctions with a given positive or negative m_ℓ value. (This is the reverse process of the textbook case where real atomic orbitals are formed from the complex eigenfunctions of \hat{L}_z .) In this case, after diagonalizing the magnetic moment operator in the basis of doublet state components, an un-quenched orbital angular momentum is usually obtained. A symmetry lowering that shifts the single occupation or hole dominantly or fully to one of the real NOs and breaks the orbital degeneracy of the state goes along with a quenching of the orbital angular momentum.

0.3 Case Studies: From Transition Metals to Actinides

The magnetic properties of the approximately D_{3d} -symmetric $\text{Co}^{\text{II}}(\text{Tp})_2$ complex (Tp = trispyrazolylborate) were investigated by Tierney *et al.* using EPR and NMR spectroscopies. [21, 22] Due to its interesting magnetic properties, we decided to perform calculations for this complex. The EPR measurements revealed a strong axial magnetic anisotropy characterized by $g_{\parallel} = 8.48$ and $g_{\perp} = 1.02$, with g_{\parallel} being in the direction of the three-fold principal axis of symmetry. The electronic structures of trigonal Co(II) complexes were rationalized theoretically already in the early 1950s by Abragam and Pryce [23], and then revisited by Jesson and McGarvey in 1970s [24, 25]. It is beneficial to consider the (approximate) D_{3d} point group symmetry of the complex as a trigonal distortion from an O_h parent coordination. As

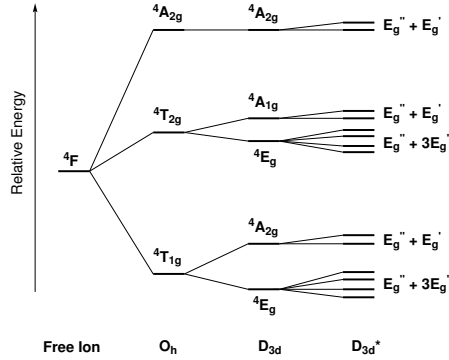


Fig. 0.3 Schematic energy diagram of the lowest electronic states deriving from the splitting of the 4F term of the Co^{2+} ion by an octahedral (O_h) and a trigonal (D_{3d}) crystal-field. D_{3d}^* is the corresponding double group in which the SO states are classified.

seen in Figure 0.3, the $3d^7$ configuration of the Co^{2+} ion leads to the spectroscopic LS -ground term 4F . The excited 4P term is much higher in energy and therefore not discussed here. The seven-fold orbital degeneracy of the ground term is split by an octahedral ligand-field (LF) into the spin quartets $^4T_{1g}$, $^4T_{2g}$ and $^4A_{2g}$. The O_h ground state (GS) $^4T_{1g}$ is then split by the trigonal LF distortion into two spin quartets 4E_g and one spin quartet $^4A_{2g}$. The zero-field splitting (SO interaction) finally breaks the four-fold spin- and two-fold orbitally-degenerate SR GS into four Kramers doublets.

The electronic structure and the EPR g -factors of $\text{Co}(\text{Tp})_2$ were calculated at the CAS level, and the resulting $3d$ NOs for the SO GS are shown in Figure 0.4, along with the orbital and spin magnetizations. At the SCF-SO level, the GS doublet derives almost exclusively from the SR GS 4E_g (98%). It is separated from the first excited state (ES) by 220 cm^{-1} . As the EPR measurements were performed at 3.6 K, only the GS Kramers doublet is thermally populated, and hence, the electronic g -factors can be rationalized with a pseudo-spin $S = 1/2$ and the following spin Hamiltonian:

$$\hat{H}_S = \mu_B [g_{\parallel} B_{\parallel} \hat{S}_{\parallel} + 2g_{\perp} (B_{\perp} \hat{S}_{\perp})] \quad (0.16)$$

The SCF-SO calculation gives for the GS Kramers doublet $g_{\parallel} = 8.72$ and $g_{\perp} = 1.01$. The large magnitude of the magnetic moment along the \parallel magnetic axis results from a large unquenched orbital angular momentum, and from the reinforcement of $\langle L_{\parallel} \rangle$ and $\langle S_{\parallel} \rangle$ (Figure 0.4). One can notice that the calculated spin expectation value of $\langle S_{\parallel} \rangle = 1.44$ is very close to the expected value for a SR spin quartet $\langle S \rangle = 3/2$, which is evidence of the rather weak mixing of SR states in the SO GS. Introduction of the dynamic correlation at the PT2-SO level does not improve the calculated g -factors ($g_{\parallel} = 8.77$ and $g_{\perp} = 0.84$). The deviations from the experimental data are tentatively attributed to the dipolar spin-spin interactions, which are not included in our calculations but are known to contribute to the ZFS in transition metals [26], and

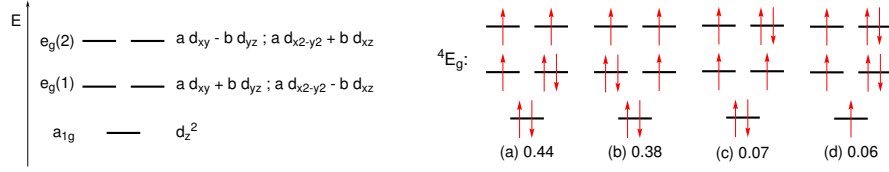


Fig. 0.5 Left: Splitting of the 3d orbitals in the D_{3d} symmetry point group. Right: Composition of the SR ground state wavefunction 4E_g . Only the configurations with a weight larger than 5 % are shown.

to $2\langle S_{\parallel} \rangle$. These contributions from both e_g sets give a tangerine-shaped $m_{\parallel}^S(\mathbf{r})$ iso-surface at the cobalt center. The calculated $\langle S_{\parallel} \rangle = 1.44$ results principally from this description. However, the slight symmetry breaking leads to a SR GS 4E_g with admixtures of additional configurations (c) and (d) of Figure 0.5. These configurations, in combination with the SO interaction, affect the populations of the a_{1g} and $e_g(1)$ NOs and NSOs. Furthermore, sizable spin-magnetization is also seen on the ligand-nitrogen atoms. This effect is associated with the $e_g(2)$ orbitals (see Figure 0.4), which are seen to afford Co – N antibonding interactions. In reference to the orbital diagram of Figure 0.5, the ligands donate electron density to the metal $e_g(2)$ shell, but only with \downarrow spin because the \uparrow spin metal 3d orbitals are filled. This donation is reflected by NO populations of 1.018, slightly larger than the idealized value of 1, and by NSO spin populations slightly below 1 due to the contributions from \downarrow spin in the $e_g(2)$ shell.

$\langle L_{\parallel} \rangle$ and the associated orbital magnetic moment results essentially only from contributions of the $e_g(1)$ orbitals. The a_{1g} orbital with $m_{\ell} = 0$ does not contribute to $\langle L_{\parallel} \rangle$, whereas the contribution from the $e_g(2)$ orbitals to the orbital angular momentum is null. (Due to their single occupations, their contributions to $\langle L_{\parallel} \rangle$ correspond to a sum of two \hat{L}_{\parallel} eigenfunctions, with eigenvalues $+m_{\ell}$ and $-m_{\ell}$.) For the $e_g(1)$ shell, the electronic occupation of ca. 3/2 in each orbital allows to maximize their contributions to \hat{L}_{\parallel} . In this case, one can make a linear combination of the two real orbitals to obtain \hat{L}_{\parallel} eigenfunctions with $\pm m_{\ell}$, one of each being occupied in the two components of the degenerate GS. The composition of the $e_g(1)$ orbitals in terms of the real 3d orbitals calculated for $\text{Co}(\text{Tp})_2$ is the following, with z coinciding with the 3-fold symmetry axis

$$\begin{aligned} e_{1g}(1)_a &= -0.74d_{xy} + 0.35d_{yz} + 0.40d_{xz} + 0.42d_{x^2-y^2} \\ e_{1g}(1)_b &= 0.44d_{xy} + 0.42d_{yz} + 0.33d_{xz} + 0.73d_{x^2-y^2} \end{aligned} \quad (0.17)$$

The presence of the xz and yz contributions reflects the tilting of the two orbitals with respect to the z axis, whereas the mixing of xy and $x^2 - y^2$ mainly simply reflects the arbitrary choice of the ligand azimuth positions. Using $e_g(1)_a$ and $e_g(1)_b$, one can make a linear combination that would lead to an orbital angular momentum expectation value of $\langle L_{\parallel} \rangle = 1.73$. This linear combination is responsible for the oblate $m_{\parallel}^L(\mathbf{r})$ visible in Figure 0.4. Refer to Figure 0.1: The two orbitals in question

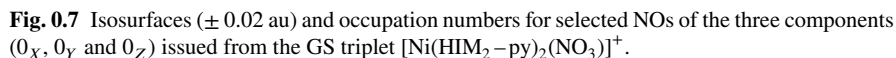
component of the spin quintet is estimated to be higher than 150 cm^{-1} [28]. In a pure spin quintet, the $M_S = \pm 2$ components have a g -factor of 6; the experimental value shows that there is a large orbital contribution due an only partial quenching of the orbital moment and a low lying SR state. This is confirmed by CASPT2 calculations which show that the first excited state lies at 516 cm^{-1} above the GS. With the SO coupling, the spin quintet splits into five components by 0.34 , 118, 132 and 180 cm^{-1} [29]. The spin Hamiltonian is either written for the ground non KD with a small ZFS and a large anisotropic g factor, or by a pseudo-spin $S = 5$ with a large ZFS splitting and a nearly isotropic g tensor. The following analysis is performed based on the non KD perspective.

In a non KD, only one component of the g tensor is non-zero. In the [FeLCI] complex, the magnetic axis of the ground doublet is parallel to the C_2 symmetry axis of the molecule, which is taken to be along the Z direction and coinciding with the quantization axis. The two d_δ orbitals are non-bonding with the chlorine atom and are the lowest in energy while the d_π and d_σ are anti-bonding and destabilized. The two d_δ are split by 300 cm^{-1} due to a differential interaction with the L ligand (cf Figure 0.6). The d_{π_2} orbital is more anti-bonding than the d_σ due to a strong π interaction with the L ligand. The two low lying SR states correspond to configurations $(d_{\delta_1})^2 d_{\delta_2} d_{\pi_1} d_{\pi_2} d_\sigma$ and $d_{\delta_1} (d_{\delta_2})^2 d_{\pi_1} d_{\pi_2} d_\sigma$ respectively, and the orbital moment is quenched. These states are strongly coupled by SO coupling due to the small energy gap, leading to a mixing of 80% and 20 %; this strong mixing leads to the partial un-quenching of the orbital moment, to the large splitting of the spin quintet and to the large magnetic anisotropy of the ground doublet.

NOs and NSOs for the ground doublet are shown in Figure 0.6. While in a non-Kramers doublet NOs' populations might be different, they are almost identical for the two components with 1.8 in d_{δ_1} and 1.2 in d_{δ_2} as expected from the SO coupling mixing. The mixing by SO coupling is much smaller for the other three components and the populations of d_{δ_1} and d_{δ_2} lie in the ranges 1.89-1.98 and 1.08-0.99 respectively. There is one correlation orbital per occupied d orbital and the largest correlation is obtained for the d_{δ_1} orbital which is the most populated one.

In a non-Kramers doublet, NSOs are only defined along the magnetic axis. The spin population follows the electronic configuration: it appears as a complement to 2 to the electron occupancy of the orbitals. The correlation NSOs are shown in the 3rd row of Figure 0.6 and have a spin population of $\approx \pm 0.02$. There is a delocalization of the α spin density in the π and σ symmetries and a spin polarization with the appearance of a β spin density on the ligands in the orbitals of δ symmetry. Finally, as shown in the last row of Figure 0.6, the magnetization is approximately cylindrical, in accordance with Fig. 0.1. Interestingly, the magnetization spreads out onto the lower part of the L ligand and exhibits a sign change, meaning that the covalent interactions between the metal and the ligand induce an orbital magnetization on the ligand that is of opposite sign to that on the metal. The orbital contributing the most to the orbital magnetization is d_{δ_1} .

In this complex, the NOs and NSOs permit a visualization of the strong mixing of two SR states by So coupling which, by partially de-quenching the orbital magnetic moment, leads to a strong magnetic anisotropy. Furthermore, the 'secondary'



0.3.3 Zero-Field Splitting in an octahedral Ni(II) complex

$$\hat{H}_S = \mu_B (g_X B_X \hat{S}_X + g_Y B_Y \hat{S}_Y + g_Z B_Z \hat{S}_Z) + D \left(\hat{S}_Z^2 - \frac{1}{3} S(S+1) \right) + E (\hat{S}_X^2 - \hat{S}_Y^2) \quad (0.18)$$

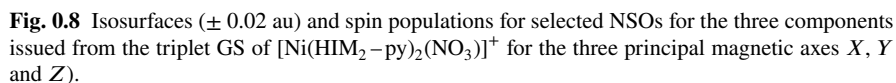
The ZFS parameters D and E and the three g factors have been determined by High-Field High-Frequency spectroscopy. $D = -10.1 \text{ cm}^{-1}$, $E/D = 0.24$, $g_x = g_y =$

2.20 and $g_Z = 2.27$. This is nicely reproduced by CASPT2 calculations using a CAS(13,13) including two bonding e_g orbitals and a second d shell [31].

As it is usually the case in transition metals, the anisotropic magnetic behavior is borne by the ZFS of the ground spin state, and the large negative D value leads to an axial magnetization. The three components of the ground spin triplet are non degenerate and consequently, the expectation value of the magnetic moment vanishes. Magnetic properties arise from the coupling between the three components by the Zeeman operator; the closer the two components are in energy, the more magnetic the corresponding direction is. [29, 31]

The two lowest components, denoted 0_X and 0_Y , are close in energy by 1.8 cm^{-1} while the third one, 0_Z , has a larger energy gap 12.1 cm^{-1} . The NOs of the three components are depicted on Figure 0.7. They are very similar to each other, since the three components arise from the same spin triplet and the SO effects are small, but they differ slightly. The magnetic anisotropy arises precisely from these small differences. The negative D value can be rationalized by the energetic ordering of the d orbitals, and mostly from the splitting of the two e_g orbitals which is due to the difference of σ donation of the ligands to the metal [31]. Referring to Figure 0.7, the three t_{2g} -like orbitals have a population that is slightly smaller than 2 due to the dynamic electron correlation. The two e_g -like orbitals have occupations close to 1, one lower and one larger than 1. e_g^1 is the d_{z^2} orbital and points towards two nitrogens of the $\text{HIM}_2\text{-py}$ ligands while e_g^2 is the d_{xy} and points towards the two other nitrogen atoms and the two oxygen atoms of the nitrate. Since the $\text{HIM}_2\text{-py}$ ligands are better σ donors than the nitrate, e_g^1 is more anti-bonding and more destabilized than e_g^2 . As a consequence, in the two lowest 0_X and 0_Y components, the population of the most stabilized e_g is larger than one while it is less than one for the 0_Z component. The population of the correlation t_{2g}^* NOs is about 0.01 each, which corresponds roughly to the depletion in the t_{2g} shell. The correlation in the e_g shell is less important since the orbitals are singly occupied, and the population of the correlation e_g^* NOs is slightly less than half those of the t_{2g}^* ones.

Magnetic properties arise from the coupling between two components. The coupling between 0_X and 0_Y is the largest since these components are the closest in energy. This coupling defines the direction of the axial magnetization, denoted Z . The NSOs for this quantization direction are shown in Figure 0.8 in comparison to those in directions X and Y obtained from the coupling between 0_Y and 0_Z and between 0_X and 0_Z respectively. The spin density is mostly borne by the e_g orbitals with a spin population close to 1, as expected, but it should be noted that one of the e_g has a larger spin population, namely the d_{U^2} when the axis is along $U = X, Y, Z$. Spin polarization appear with both α and β densities and both through σ (e_g -type orbitals) and π (t_{2g} -like orbitals) bonding schemes. The α and β populations of the t_{2g} NSOs are both 0.038. The β density is more delocalized on the ligands leading to spin polarization through the π bonding. There is a small anisotropy, since the orbital with the lobes perpendicular to the U axis has the lowest β density. For the e_g -like correlation NSOs, the α spin density is slightly larger than the β one (0.015 against 0.01), the α one being more delocalized on the ligands. This spin delocaliza-



The orbital magnetization density and orbital contributions along the three magnetic axes are shown on Figure 0.9. In this complex, the orbital moment is quenched in the GS as long as SO coupling is not considered. The SO coupling with the excited states gives rise to small orbital contributions which play a key role for the anisotropic properties. The largest contribution is along the Z axis. The orbital magnetization in direction U form a ring around this axis which spreads on the ligands perpendicular to this axis. The most contributing orbital is the t_{2g} one with the lobes perpendicular to the axis and to a lesser extend, the e_g along the axis.

In this section, we have shown that when a pure spin triplet is split by the SO coupling with excited states, the NOs permit to quantify the small differences between the three components and to visualize the effects of correlation. The magnetic axes are defined by the coupling between two of the components arising from the triplet

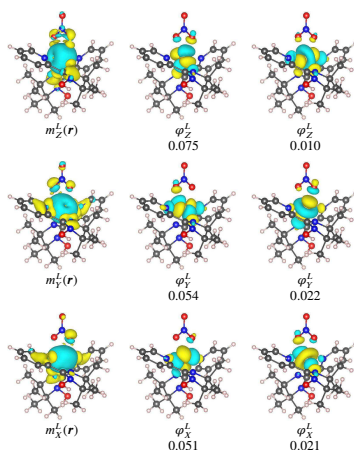


Fig. 0.9 Isosurfaces of the orbital magnetization ($m_u^L(\mathbf{r})$) ($\pm 5 \cdot 10^{-5}$ au) and of their principal current density natural orbitals (φ_u^L) (± 0.02 au) for the three components issued from the triplet GS of $[\text{Ni}(\text{HIM}_2 - \text{py})_2(\text{NO}_3)]^+$ along the three principal magnetic axes X , Y and Z .

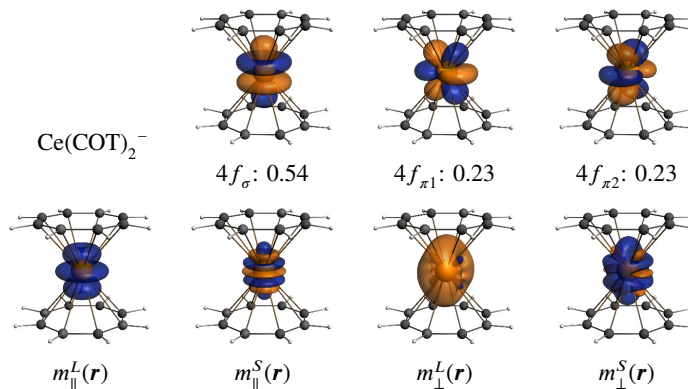


Fig. 0.10 Top row: Isosurfaces (± 0.03 au) and occupations of selected natural orbitals of the SO GS of $\text{Ce}(\text{COT})_2^-$. Bottom row: Isosurfaces (± 0.001 au) of the orbital ($m_u^L(\mathbf{r})$) and spin ($m_u^S(\mathbf{r})$) magnetizations of $\text{Ce}(\text{COT})_2^-$ for the \parallel and \perp magnetic axes. Doublet components with $\langle S_u \rangle > 0$. SCF-SO results.

with their corresponding NSOs and orbital magnetization. It turns out that the spin density is slightly anisotropic and that there is some spin delocalization the σ bonding scheme and spin polarization in the π one. The orbital magnetization is a current around the considered axis and originates mainly from a t_{2g} like orbital.

0.3.4 Linear Ln(III) Complexes: $\text{Ln}(\text{COT})_2^-$

In $\text{Ce}(\text{COT})_2^-$ ($4f^1$ configuration), the linear crystal-field lifts the seven-fold degeneracy of the cerium $4f$ orbitals to give rise to a $\text{SR } ^2\Sigma$ ground state when using labels for rotational symmetry, which is appropriate because M_ℓ for the $4f$ shell is a good quantum number in the presence of an 8-fold symmetry axis. Introduction of the SO interaction mixes the \uparrow and \downarrow spin components of the SR GS and the excited $^2\Pi$ state. The SO GS corresponds then to a KD of $M_J = \pm 1/2$ parentage which originates from the spectroscopic level $^2F_{5/2}$ of the Ce^{3+} ion. The EPR g -factors associated with the GS were characterized experimentally by Walter *et al.* and revealed a planar magnetic anisotropy, with $g_{\parallel} = 1.12$ and $g_{\perp} = 2.27$. [32] These observed g -factors somewhat differ from the idealized values of $g_{\parallel} = 0.86$ and $g_{\perp} = 2.57$ for a $J = 5/2$, $M_J = \pm 1/2$ ion micro-state. The deviations between the observed and CF g -factors result from the different ratios of the $\text{SR } ^2\Sigma$ and $^2\Pi$ states. This ratio is characterized in the GS wavefunction $|\psi\rangle$ by real coefficients A and B , with $|\psi\rangle = A(^2\Sigma) + B(^2\Pi)$. For a Ce^{3+} ion micro-state, values of 0.65 and 0.76 would be expected for A and B , respectively.

The electronic structure of $\text{Ce}(\text{COT})_2^-$ was calculated at the SCF-SO level with a minimal active space containing the seven $4f$ orbitals. [19] The resulting natural orbitals of the SO GS are shown in Figure 0.10. As expected, the unpaired electron is shared between the $4f_{\sigma}$ and the $4f_{\pi}$ orbitals, with the occupation numbers corresponding to 0.74 and 0.68 for the real wavefunction coefficients A and B , respectively. (For this effective one-electron system, the σ and combined π NO occupations are the squares of A and B , respectively.) The calculated $g_{\parallel} = 1.08$ and $g_{\perp} = 2.35$ are in good agreement with the experiment. The planar magnetic anisotropy can be related to the orbital and spin magnetizations shown in Figure 0.10. Using Equations 0.2a and 0.2b, the orbital and spin magnetizations along the parallel magnetic axis of $\text{Ce}(\text{COT})_2^-$ are given as follows

$$\begin{aligned} m_{\parallel}^S(\mathbf{r}) &= \frac{1}{2} [A^2 Y_3^0 Y_3^0 + B^2 Y_3^1 Y_3^{-1}] \\ &= \frac{A^2}{2} f_{\sigma}^2 - \frac{B^2}{4} [f_{\pi+}^2 + f_{\pi-}^2] \end{aligned} \quad (0.19)$$

$$\begin{aligned} m_{\parallel}^L(\mathbf{r}) &= -B^2 Y_3^1 Y_3^{-1} \\ &= \frac{B^2}{2} [f_{\pi+}^2 + f_{\pi-}^2] \end{aligned} \quad (0.20)$$

where $Y_{\ell}^{m_{\ell}}$ are spherical harmonics, and the $f_{|m_{\ell}|\pm}$ correspond to the $\ell = 3$ tesseral harmonics which are real linear combinations of the complex $Y_3^{m_{\ell}}$ with the same $|m_{\ell}|$.

As seen in Eq. 0.19, the spin magnetization corresponds to positive contributions from the f_{σ}^2 density and to negative contributions from the f_{π}^2 densities, giving the alternating blue and orange lobes for $m_{\parallel}^S(\mathbf{r})$ in Figure 0.10. The blue lobes represent the

positive contributions from f_σ and integrate to $A^2/2 = 0.27$, while the orange lobes correspond to the contributions related to f_π and integrate to $-2B^2/4 = -0.23$. Therefore, the two contributions are almost equal and with opposite sign, leading to a very small spin expectation value $\langle S_\parallel \rangle = 0.04$. This value is far from the expected value for a SR spin doublet $\langle S \rangle = 1/2$ and reflects the importance of SO coupling in the $4f$ shell. The orbital magnetization is simpler to analyze. Due to the lack of orbital angular momentum from the $4f_\sigma$ orbital along the \parallel magnetic axis, only the $4f_\pi$ orbitals contribute to $m_\parallel^L(\mathbf{r})$. This is visible in Figure 0.10 where the orbital magnetization corresponds simply to a linear combination of each f_π^2 densities. The isosurface of m_\parallel^L is also essentially identical to the idealized one for $m_\ell = 1$ in Figure 0.2. Integration of the magnetization results an orbital angular momentum expectation value $\langle L_\parallel \rangle = 0.46$. Overall, along the parallel axis the magnitude of the magnetic moment is driven by the orbital contribution from the $4f_\pi$ orbitals. In turn, the occupation of these orbitals is a consequence of the SO interaction, mixing the SR $^2\Sigma$ GS components with the $^2\Pi$ state components of opposite spin projection. Overall, the electronic g_\parallel -factor remains relatively small due to a quenching of the spin magnetic moment.

A similar approach can be used to analyze the magnetization densities along the perpendicular magnetic axis. As already mentioned in Section 0.2, the wavefunction components used for the analysis diagonalize the operator $\hat{L}_\perp + g_e \hat{S}_\perp$. In the model, this is achieved by taking a linear combination of the initial wavefunction $|\psi_\parallel\rangle$ and of its Kramers conjugate $|\bar{\psi}_\parallel\rangle$:

$$\begin{aligned} |\psi_\parallel\rangle &= AY_3^0 - B\bar{Y}_3^1 \\ |\bar{\psi}_\parallel\rangle &= A\bar{Y}_3^0 - BY_3^{-1} \end{aligned}$$

to give

$$|\psi_\perp^\pm\rangle = \frac{1}{\sqrt{2}}(|\psi_\parallel\rangle \pm |\bar{\psi}_\parallel\rangle) \quad (0.21)$$

Substituting Equation 0.21 into Equations 0.2a and 0.2b, the orbital and spin magnetizations along the \perp magnetic axis for the $\langle S_\perp \rangle > 0$ component of the doublet can be written as:

$$\begin{aligned} m_\perp^S(\mathbf{r}) &= \frac{A^2}{2} [Y_3^0 Y_3^0] - \frac{B^2}{4} [Y_3^1 Y_3^1 + Y_3^{-1} Y_3^{-1}] \\ &= \frac{A^2}{2} f_\sigma^2 - \frac{B^2}{4} [f_{\pi-}^2 - f_{\pi+}^2] \end{aligned} \quad (0.22a)$$

$$\begin{aligned} m_\perp^L(\mathbf{r}) &= -AB\sqrt{3} [Y_3^0 Y_3^0] + \frac{AB\sqrt{3}}{2} [2 \cdot Y_3^1 Y_3^{-1} + Y_3^1 Y_3^1 + Y_3^{-1} Y_3^{-1}] \\ &= -AB\sqrt{3} [f_\sigma^2 + f_{\pi+}^2] \end{aligned} \quad (0.22b)$$

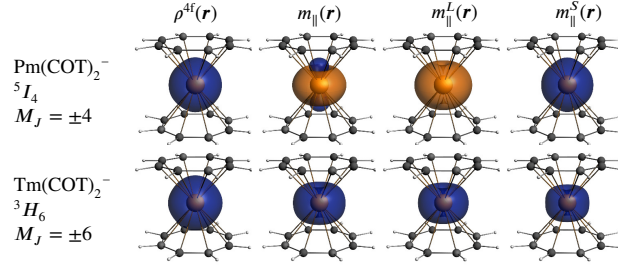


Fig. 0.11 Comparison of the ab-initio $4f$ electron density ($\rho^{4f}(\mathbf{r})$), orbital ($m_{||}^L(\mathbf{r})$), spin ($m_{||}^S(\mathbf{r})$) and total $m_{||}(\mathbf{r})$ magnetizations for the SO GS of $\text{Pm}(\text{COT})_2^-$ and $\text{Tm}(\text{COT})_2^-$. Doublet components with $\langle S_{||} \rangle > 0$. SCF-SO Results. Isosurfaces at ± 0.001 au.

The isosurfaces of the corresponding magnetizations calculated *ab-initio* are shown in Figure 0.10. The spin magnetization corresponds to a dominant positive (blue isosurface) contribution which arises from the addition of the positive contributions of the f_{σ}^2 and $f_{\pi+}^2$ densities, which integrates to $0.38 (A^2/2 + B^2/4)$. This positive contribution is counterbalanced by a smaller negative contribution integrating to -0.11 . The negative contribution is characterized by the orange lobes in $m_{\perp}^S(\mathbf{r})$ and results from the $f_{\pi-}^2$ density. As seen in Eq. in 0.22b, the orbital magnetization results from the reinforcing contributions of the f_{σ}^2 and $f_{\pi+}^2$ densities. This leads to a large calculated expectation value for the orbital angular momentum $\langle L_{\perp} \rangle = -1.72$, characterized in Figure 0.10 by a large orange lobe. Therefore, the origin of the planar magnetic anisotropy in $\text{Ce}(\text{COT})_2^-$ resides in the large magnitude of the orbital magnetization for a field along the perpendicular magnetic axis, which is only to a small extent canceled by the spin magnetization.

Of particular interest are the relationships that may exist between the electron density generated by the $4f$ orbitals ($\rho^{4f}(\mathbf{r})$) and the orbital and spin magnetizations, and hence the magnetic moments. Comparisons of $\rho^{4f}(\mathbf{r})$ and of $m_{||}^{L/S}(\mathbf{r})$ calculated for the SO GSs of $\text{Pm}(\text{COT})_2^-$ and $\text{Tm}(\text{COT})_2^-$ are provided in Figure 0.11. [19]

It is clear that the orbital and spin magnetization are only indirectly related to the $4f$ electron density, because the electron density itself contains no information about the magnetic properties. In the case of $4f^n$ complexes with $n \leq 7$, the spin magnetization tends to resemble the electron density. For instance, in $\text{Pm}(\text{COT})_2^-$ ($4f^4$ configuration), both $\rho^{4f}(\mathbf{r})$ and $m_{||}^S(\mathbf{r})$ have a prolate shape due to similar NO occupations and NSO spin populations, respectively. Here the 4 unpaired electrons are equally shared among the $4f_{\sigma}$, $4f_{\pi}$, $4f_{\delta}$ and $4f_{\phi}$ NOs (or NSOs).

On the other hand, $m_{||}^S(\mathbf{r})$ tends to represent the unpaired electron(s), or the electron hole(s), in the case of $4f^n$ systems with $n > 7$. For example, the electronic occupation of the SO GS of $\text{Tm}(\text{COT})_2^-$ ($4f^{12}$ configuration) is $4f_{\sigma}^2 4f_{\pi}^2 4f_{\delta}^3 4f_{\phi}^3$, which leads to a mainly prolate $4f$ electron density due to the lack of occupations in the δ and ϕ orbitals. The spin magnetization is, however, oblate because the two unpaired spins are associated with the $4f_{\delta}$ and $4f_{\phi}$ orbitals. Similarly to the spin mag-

netization, $\rho^{4f}(\mathbf{r})$ is not directly related to the orbital magnetization. For instance, the very similar $4f$ electron densities calculated for the GS of $\text{Pm}(\text{COT})_2^-$ and $\text{Tm}(\text{COT})_2^-$ lead to drastically different orbital magnetizations. In $\text{Pm}(\text{COT})_2^-$, a relatively large oblate $m_{\parallel}^L(\mathbf{r})$ with opposite sign to $m_{\parallel}^S(\mathbf{r})$ is calculated. The associated expectation values $\langle L_{\parallel} \rangle = -5.73$ and $\langle S_{\parallel} \rangle = 1.73$ leads to a GS with a sizable magnetic anisotropy with $g_{\parallel} = 4.50$ and $g_{\perp} = 0.00$. In $\text{Tm}(\text{COT})_2^-$, a positive oblate $m_{\parallel}^L(\mathbf{r})$ is calculated with $\langle L_{\parallel} \rangle = 5.00$. As for all the complexes of the second half of the series, the orbital and spin magnetization reinforce each other in $\text{Tm}(\text{COT})_2^-$ to give an extremely large magnetic anisotropy with $g_{\parallel} = 13.98$ and $g_{\perp} = 0.00$.

The large orbital angular momenta in $\text{Pm}(\text{COT})_2^-$ and $\text{Tm}(\text{COT})_2^-$ can be rationalized with the help of the electronic occupation of the $4f$ orbitals. As already mentioned, when a single electron or a single hole is equally shared in degenerate orbitals with the same $|m_{\ell}|$, one can generate a linear combination of the two orbitals which is an \hat{L}_{\parallel} eigenfunction with the eigenvalue $\pm m_{\ell}$, and hence maximize the contribution to the orbital angular momentum. For example, the two unpaired electrons in $\text{Tm}(\text{COT})_2^-$ are equally shared in the $4f_{\delta}$ and $4f_{\phi}$ orbitals such that the orbital angular momentum is simply the sum of the two $m_{\ell} = \pm 2$ and ± 3 .

The largest orbital angular momentum for an f -element in an axial environment would therefore be associated with $\sigma^n \pi^1 \delta^1 \phi^1$ and $\sigma^n \pi^3 \delta^3 \phi^3$ configurations. For the former case, the f -shell is less than half filled and the spin and orbital angular momenta would not reinforce each other. Accordingly, the latter case would lead to the overall largest magnetic moment (with σ^1 maximizing the spin magnetic moment). Such configurations are potentially accessible in linear environments with the Dy^{3+} and Er^{3+} ions, leading to a $|J = 15/2, M_J = \pm 15/2\rangle$ Kramers doublet GS, and with the Ho^{3+} ion leading to a non-Kramers doublet $|J = 8, M_J = \pm 8\rangle$. [33] The $|15/2, \pm 15/2\rangle$ doublet was characterized both experimentally and theoretically for the $\text{Er}(\text{COT})_2^-$ complex, [19, 34] whereas the pentagonal-bipyramidal $[\text{Ho}(\text{CyPh}_2\text{PO})_2(\text{H}_2\text{O})_5]\text{I}_3$ complex affords an almost perfect $M_J = \pm 8$ GS, therefore being very close to the ceiling magnetic moment for a single f ion. [35, 36]

To obtain larger magnetic moments, one would need to reach the even larger orbital angular momenta $m_{\ell} = \pm 4$ and ± 5 associated with g - and h -shells, couple orbital angular momenta from different centers, and/or create a large number of strongly coupled unpaired spins. Instead of trying to access exotic elements with partially filled shells of $\ell \geq 4$, [37] one could potentially use small metal clusters to generate magnetic superatoms. [38] For instance, transition metal clusters such as Pb_{12}^{2-} , Sn_{12}^{2-} or the doped versions $[\text{M}@\text{Pb}_{12}^q]$ ($\text{M} = \text{U}, \text{Pu}, \text{Am}, \text{Cm}$), exhibit superatomic molecular orbitals that resemble atomic g and h orbitals. [39] The partial filling of these superatomic orbitals could lead to potentially gigantic orbital angular momenta. However, Hund's rules do not necessarily apply to unsupported metallic clusters because of potentially large Jahn-Teller distortions, which may break the high degeneracy and favor complexes with quenched magnetic moments. [40]

0.3.5 An Octahedral $Np(VI)$ Complex: NpF_6

NpF_6 crystallizes as a molecular crystal; the molecule is octahedral with a $5f^1$ configuration. Its magnetic properties have been characterized by EPR and magnetic susceptibility measurements. [41,42] The ground state is a KD with a negative g factor of -0.604. This is well reproduced by CASPT2 calculations using a CAS(13/13) including the $5f$ of the actinide and six $2p$ orbitals of the ligands. [43]

In O_h symmetry, the seven $5f$ orbitals split in three sets: the non-bonding and non-degenerate f_{xyz} orbital belonging to the irreducible representation (irrep) a_{2u} , the three π antibonding f_{xy} , f_{xz} and f_{yz} orbitals of irrep t_{2u} , and the three σ antibonding f_x , f_y and f_z orbitals of irrep t_{1u} . The ground state of the molecule is a KD of symmetry $E_{5/2}$ corresponding to a single electron in a $e_{5/2}$ spinor, which is a mixture of the a_{2u} and t_{2u} orbitals under the SO coupling interaction. The two components of the KD are, for a quantization axis along z

$$\begin{aligned} |\psi\rangle &= a \left| f_{xyz}; \alpha \right\rangle + b \frac{1}{\sqrt{3}} \left(\left| f_{xy}; \alpha \right\rangle + \left| f_{xz}; \beta \right\rangle + i \left| f_{yz}; \beta \right\rangle \right) \\ |\bar{\psi}\rangle &= a \left| f_{xyz}; \beta \right\rangle + b \frac{1}{\sqrt{3}} \left(\left| f_{xy}; \beta \right\rangle - \left| f_{xz}; \alpha \right\rangle + i \left| f_{yz}; \alpha \right\rangle \right) \end{aligned} \quad (0.23)$$

where a and b are real coefficients depending of on the crystal-field splitting between the a_{2u} and t_{2u} orbitals and the SO coupling. When the quantization axis is along x or y , the Kramers partners are obtained from Equations 0.23 by circular permutation $x \rightarrow y \rightarrow z$ and $x \rightarrow z \rightarrow y$ respectively. Without SO coupling, the ground state is orbitally non-degenerate and the orbital moment is quenched. According to Equation 0.23, there are three contributions to the g factor: i) a spin contribution $2 - 4/3 b^2$; the deviation from 2 arises from the admixture of a β -spin component through SO coupling, ii) a first order orbital angular momentum contribution $-8/\sqrt{3} ab$ due to the partial de-quenching of the angular momentum by SO coupling iii) a second order orbital angular momentum contribution $2/3 b^2$ corresponding to the contribution of the t_{2u} orbitals.

The NOs of the ground KD are shown in Figure 0.12. As expected from Equation 0.23, the f_{xyz} and f_{xy} , f_{xz} and f_{yz} are partially occupied with respective populations of $a^2 = 0.74$ and a combined population of $b^2 = 0.28$. The dynamical correlation occurs equivalently in all the irreps either g or u with a depletion in the bonding orbital in favor of the corresponding antibonding one. The NSOs along z axis with the largest spin population are in accordance with Equation 0.23: an α spin population of a^2 in orbital f_{xyz} and $1/3 b^2$ in orbital f_{xy} and a β population of $1/3 b^2$ in orbitals f_{yz} and f_{zx} . Spin correlation is the largest through t_{1u} orbitals with a α spin population in the metallic t_{1u} orbitals in favor of a β population in the corresponding orbitals t_{1u}^* mostly localized on the ligands. Spin correlation occurs as well in the g orbitals but to a lesser extent. The spin polarization appears clearly on the total spin magnetization with some β spin density on all fluorine atoms. Spin densities for a magnetic field applied along another axis are obtained by circular permutations.

As expected from the analysis of the contributions to the g factor, there is an important contribution from orbital magnetization. The orbital magnetization for the field along z is cylindrical around z and resembles the $m_\ell = 2$ ‘double doughnut’ shape in Figure 0.2, i.e. f_δ with respect to the quantization axis, but there is also a signature of magnetization contributions from f_π ($|m_\ell| = 2$) visible. The orbital magnetization shape isosurface is consistent with the qualitative analysis of the wavefunction, and – like the orbitals contributing to m_z^S – it shows contributions from the fluorine ligands.

In this case, NOs and NSOs permit the visualization of electron and spin densities according to the wave function deduced from crystal field theory. Furthermore, they permit to ‘see’ the spin polarization on the fluorine ligands as well as an extent of magnetic coupling between the metal and the ligands that shows up in the orbital magnetization.

0.3.6 Trigonal $U(IV)$ Complexes: UCp_3-X

The electronic structure of $(C_5Me_4H)_3UNO$ ($5f^2$ configuration) was rationalized with the help of KS-DFT and wavefunction calculations. [44] This complex represents one of the few examples of U^{IV} complexes that exhibit temperature-independent paramagnetism (TIP) at room temperature [45]; usually, the onset of temperature-dependent magnetism occurs at much lower temperatures. For $(C_5Me_4H)_3UNO$, the SR GS corresponds to the non-degenerate singlet state 1A_1 in the C_{3v} symmetry point group, with the lowest SR triplet state lying above the GS at 3746 cm^{-1} . The natural orbitals of the SR GS calculated at the CAS(4,9)SCF-SO level are shown in Figure 0.13. The NOs from the SO calculations are very similar, and therefore not shown, while the occupations for the SO case, also shown in Figure 0.13, differ from the SR calculation.

The electronic structure of $(C_5Me_4H)_3UNO$ results from strong bonding and antibonding interactions between singly occupied $5f_\pi$ orbitals of the $U(C_5Me_4H)_3$ fragment with the two singly occupied π^* orbitals of the nitrosyl ligand. The bonding combinations correspond to the HOMO and HOMO-1 of the complex. As seen in Figure 0.13, the occupations of these bonding π orbitals differ significantly from 2. Indeed, the SR GS is strongly multi-configurational in character and can not be simply described just by the $|\pi_1^2\pi_2^2\pi_1^{*0}\pi_2^{*0}|$ ‘DFT configuration’. In fact, this configuration represents only 14% of the GS wavefunction. The major configuration (20%) corresponds to a double excitation among the π orbitals ($|\pi_1^\uparrow\pi_2^\uparrow\pi_1^{*\downarrow}\pi_2^{*\downarrow}|$), while configurations corresponding to single excitations among the π orbitals also have sizable weights. This strongly correlated wavefunction leads to a GS with an effective U–N bond order (EBO) of 1.3 instead of 2 for the U–NO π bond, as determined qualitatively from the occupations of the bonding vs. antibonding NOs. Introduction of the SO coupling mixes the SR GS with the lowest excited SR triplet states, leading to a non-degenerate GS with ca. 35% of SR spin triplet character. This admixture leads to a sizable decrease in the occupations of the π (and to a lesser degree of the π^*)

NOs. This goes along with an increase of the occupation numbers of the $5f_\delta$ orbitals, which arise formally from the SO coupling between the $5f_\pi$ and the $5f_\delta$ orbitals at the metal center, shifting electron density at the metal from f_π to f_δ . Since the $5f_\delta$ are non-bonding, the EBO is slightly reduced by SO coupling, to below 1.2.

The calculated magnetic susceptibility χ for $(C_5Me_4H)_3UNO$ was calculated using the Van Vleck equation. The result is shown in Figure 0.14-(a). The agreement with the experiment (not shown) is satisfactory. [44] The reader is reminded that the magnitude of χ according to the Van Vleck equation depends on two terms for each electronic state, namely the Curie term and a linear response (LR) term. The former is explicitly temperature dependent ($1/T$) and is present for degenerate magnetic states, whereas the latter is temperature-independent and arises from contributions due to the magnetic coupling between different electronic states. [46] A more complicated behavior of χ may arise via a T -dependent Boltzmann LR and Curie terms average of the low-energy electronic state. The calculated χT for $(C_5Me_4H)_3UNO$ reveals a linear increase with temperature, i.e. the susceptibility itself is constant. This TIP over such a large temperature range is due to the large energy gap (calculated as being over 3000 cm^{-1}) between the non-degenerate SO GS and the first excited magnetic doublets. At room temperature, the lowest magnetic ESs are not populated to a significant degree, and therefore only the LR term for the GS contributes of the magnetic susceptibility.

The replacement of the axial nitrosyl ligand in $(C_5Me_4H)_3UNO$ by a methyl in $(C_5H_5)_3UCH_3$ leads to the formation of a σ bond between a fragment orbital of the CH_3 radical ligand and a (mainly) $6d_\sigma/6p_\sigma$ hybrid orbital of the $(C_5H_5)_3U$ fragment. The bonding combination is formally doubly occupied, whereas the antibonding one is vacant. As seen in the right panel of Figure 0.13, the $5f$ orbitals do not strongly interact with the CH_3 orbitals and remain principally non-bonding. Therefore, the SR GS corresponds to an orbitally degenerate spin triplet 3E in which the two unpaired electrons occupy mainly the $5f_{a1}$ and the $5f_e$ orbitals. The $5f_\pi$ and $5f_\delta$ orbitals of the $C_{\infty h}$ point group belong to the same irreducible representation (e) in the C_{3v} symmetry, leading to $5f_e$ orbitals which are linear combinations of $5f_\pi$ and $5f_\delta$. The SO interaction mixes the SR GS with the lowest excited SR triplet states and gives a non-degenerate GS. Due to the strong mixing of states, the SO GS only contains 14 weight % of the SR GS, and derives principally (42%) from the lowest SR ES 3A_1 . Thus, the SO occupation numbers of the non-bonding NOs differ significantly from the ones calculated for the SR GS. As for the nitrosyl complex, the SR and SO NOs of $(C_5H_5)_3UCH_3$ themselves are very similar, and only the SR set is shown in Figure 0.13.

The calculated χT for $(C_5H_5)_3UCH_3$ is shown in Figure 0.14-(a) and reveals a very different magnetic behavior than $(C_5Me_4H)_3UNO$. At low T , χT increases linearly with T . This is the TIP regime and it is the result of the magnetic coupling that takes place between the non-degenerate GS and the two lowest magnetic ESs. These ESs are calculated lying at 192 and 347 cm^{-1} above the GS and are therefore not populated at low T . Above ca. 60 K , however, the thermal population of the lowest ESs becomes non-negligible. The Curie term contributions to the magnetic susceptibility increase and χ becomes temperature-dependent. This behavior is typical for

U(IV) complexes. [47] The magnetic behavior of $(C_5H_5)_3UCH_3$ was also characterized experimentally with the help of 1H NMR spectroscopy. The NMR spectrum reveals that the proton chemical shifts exhibit strong paramagnetic effects. In reference to tetramethylsilane (TMS), the methyl protons have a paramagnetic NMR shift (δ_{pNMR}^H) of -195 ppm at room temperature. [48] The 1H pNMR shifts were calculated fully ab-initio, using restricted active space self-consistent field (RASSCF) wavefunctions as described in Reference 49. The resulting temperature-dependence of δ_{pNMR}^H is shown in Figure 0.14-(b). If one assumes that the pNMR ligand shifts, with respect to an analogous diamagnetic system, are principally due to contributions that arise from the low-lying paramagnetic metal-centered states, then the isotropic ligand pNMR shifts can be calculated from the metal-centered low-energy states only, using the Soncini and van den Heuvel (SvH) equation. [51, 52] Similar to the van Vleck equation, [50] the SvH equation contains Curie and LR terms to represent the explicitly temperature-dependent and temperature-independent contributions, respectively, to the NMR shifts. As seen in Figure 0.14-(b), the methyl proton pNMR shift in $(C_5H_5)_3UCH_3$ is constant at low T . This behavior arises from the LR term of the non-degenerate GS. Despite the fact that the paramagnetic electronic states are not populated at these temperatures, the very strong magnetic coupling between the GS and the lowest ESs renders the methyl proton shifts highly unusual. At higher T , the thermal population of the excited states causes $1/T$ -dependent contributions to δ_{pNMR}^H from the Curie terms, but they remain relatively small, while the LR contributions to the shift decrease in magnitude with increasing T . At room temperature, a methyl proton shift of -182 ppm is calculated, in quite good agreement with the experiment.

0.3.7 The $[U(Tp^{Me2})_2(bipy)]I$ complex.

$[U(Tp^{Me2})_2(bipy)]I$ where Tp^{Me2} = hydrotris(3,5- dimethylpyrazolyl)borate is a complex of U(III) with a $5f^3$ configuration exhibiting Single Molecule Magnet (SMM) behavior [53]. The ground KD presents a roughly axial magnetization in a direction close to the pseudo C_2 symmetry axis ($g_Z = 3.4$, $g_X = 1.3$, $g_Y = 0.7$). The first excited KD lies at 138 cm^{-1} above the ground state.

NOs for the ground KD are depicted in Figure 0.15. All $5f$ orbitals participate in this state, with an occupation varying from 0.65 to 0.25. For the sake of comparison, the CASSCF canonical orbitals are represented. The whole splitting of the $5f$ orbitals is more than 1000 cm^{-1} ; the more destabilized orbitals show a larger delocalization in the π system of the ligands due to a larger anti-bonding interaction. The trend is the same for the NSOs : the more delocalized orbitals are less populated since higher in energy.

In direction Z with the largest magnetic moment, $g_Z=3.4$ with respective orbital and spin contributions of $g_Z^L = 6.23$ and $g_Z^S = -2.81$. These two contributions have opposite signs, and the orbital one is the largest, as a reminiscence of the free ion where according to the third Hund's rule $J = L - S$ and $L = 6$ and $S = 3/2$.

In this case of an unsymmetrical actinide complex with three ‘magnetic electrons’, wave functions are difficult to analyze since they are strongly multi-determinantal, dynamical correlation plays an important role, and the SO coupling mixes many of the SF states. The visualization tools provide a useful and complementary way in order to gain physical insight and to analyze the magnetic properties of the ground state.

Magnetic molecules tend to have complicated electronic states. Nonetheless, different sets of orbitals and their populations, generated from the complex many-determinant wavefunctions, can provide chemically intuitive insight into the chemical bonding and the resulting magnetic behavior. Additionally, the total spin and orbital magnetizations provide information about the magnetic behavior and, for instance, whether the ligands of an open-shell metal center contribute directly to it.

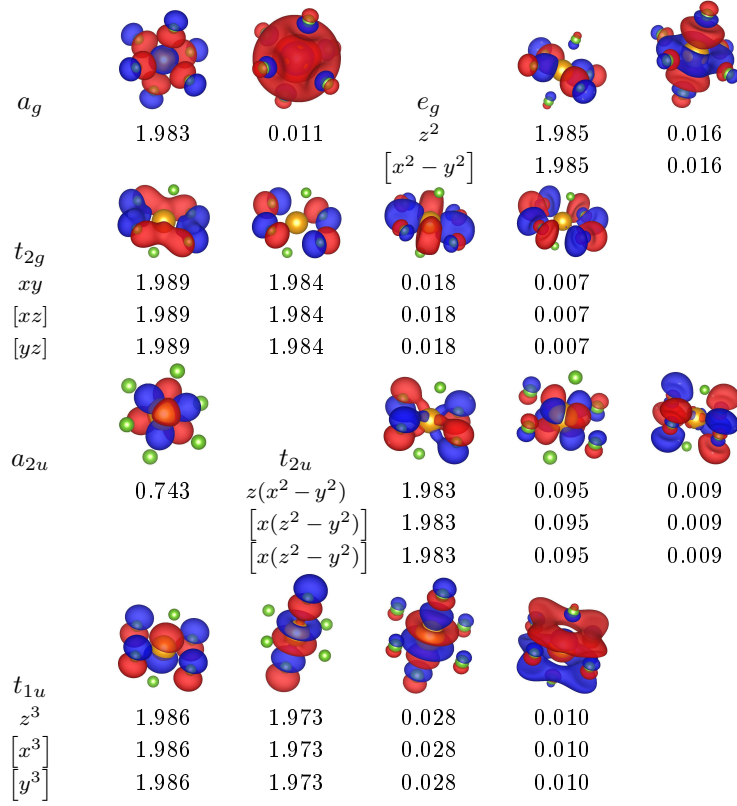
Key words: Electron paramagnetism, electron paramagnetic resonance, spin Hamiltonian, spin orbit coupling, hyperfine coupling, electron g -factor, Zeeman interaction, electron spin, nuclear spin, finite nucleus effects

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NOs



NSOs

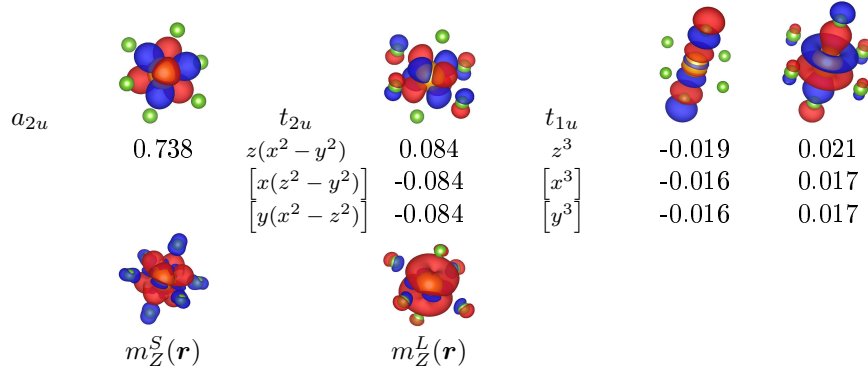
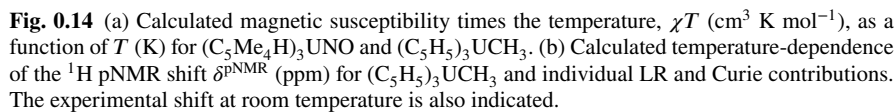
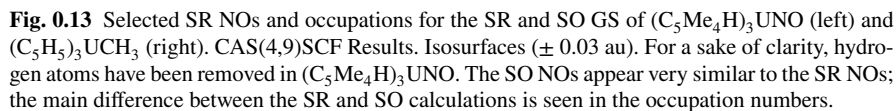


Fig. 0.12 Isosurface of selected NOs and NSOs along the z axis and corresponding populations. One orbital is represented per degenerate irrep, the components in brackets may be deduced by symmetry. The NSOs along X and Y are obtained by circular permutation. Isovalues: ± 0.04 au for orbitals, ± 0.0008 au for magnetization.



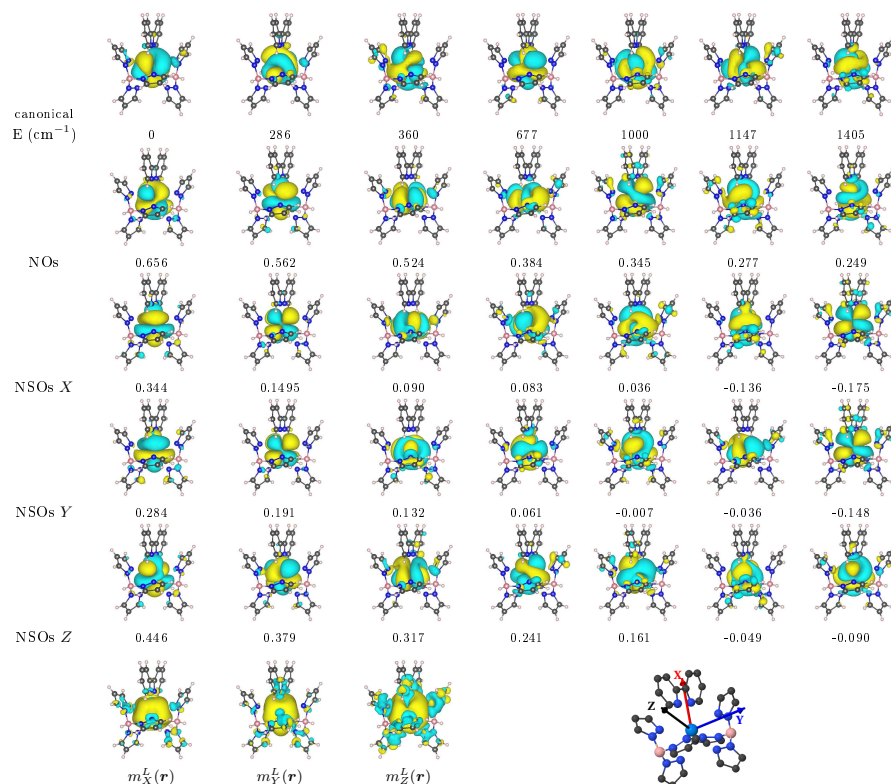


Fig. 0.15 For $[\text{U}(\text{Tp}^{\text{Me}2})_2(\text{bipy})]\text{I}$; Top row: Isosurface and energy (cm⁻¹) of the 5f canonical orbitals. Second row: Isosurface and occupation number of selected NOs. Third to fifth row: Isosurface and spin population of NSOs for the three magnetic axes. Bottom row: Isosurface of the orbital magnetization $m_U^L(r)$ for the three magnetic axes and representation of the magnetic axes. NOs and NSOs are calculated for the component of the ground KD with $\langle S_U \rangle > 0$. Isovalues: ± 0.04 au for orbitals, ± 0.0001 au for magnetization.