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Neutron imaging of liquid-liquid systems containing paramagnetic salt solutions

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The method of neutron imaging was adopted to map the concentration evolution of aqueous paramagnetic $Gd(NO_3)_3$ solutions. Magnetic manipulation of the paramagnetic liquid within a miscible nonmagnetic liquid is possible by countering density-difference driven convection. The formation of salt fingers caused by double-diffusive convection in a liquid-liquid system of $Gd(NO_3)_3$ and $Y(NO_3)_3$ solutions can be prevented by the magnetic field gradient force.

I. INTRODUCTION

Paramagnetic liquids are created by dissolving salts containing transition-metal or rare-earth ions in a solvent¹. Magnetic levitation of objects immersed in paramagnetic liquids has been used for magnetohydrostatic separation since the 1960s² and nowadays finds application in biotechnology³. Exposing a paramagnetic solution to an inhomogeneous magnetic field gives rise to the magnetic field gradient force⁴:

$$\mathbf{F}_{\nabla B} = \frac{\chi}{2\mu_0} \nabla \mathbf{B}^2. \tag{1}$$

This expression relates the force density to the magnetic susceptibility of the solution χ , the magnetic flux density B, and the permeability of free space μ_0 .

It is possible to trap aqueous paramagnetic salt solutions in the magnetic field gradient of a magnetized iron wire⁵. Convection from these paramagnetic liquid tubes is inhibited by the magnetic field gradient force, although mixing by diffusion still prevails on a long time scale. A magnetic field gradient can also initiate magnetothermal convection in a paramagnetic fluid^{6,7}.

At present, the possibility of extracting paramagnetic ions from a homogeneous aqueous solution with an inhomogeneous magnetic field is garnering significant research interest $^{8-14}$. In response to the recent rare-earth crisis, this activity has been spurred by the idea of magnetically separating rare-earth ions, which was originally explored by Noddack et al. in the $1950s^{15-17}$. Recent studies used Mach-Zehnder interferometers to relate changes in the refractive index to an enrichment of magnetic ions underneath a permanent magnet⁸⁻¹¹. The two most recent of these showed that the observed magnetic enrichment is evaporation-assisted 10,11 . According to Lei et al.¹¹, the heightened ion concentration ($\leq 2\%$ bulk concentration) in the evaporation layer is maintained by the magnetic field gradient. This results in a modest longlived paramagnetic ion enrichment underneath the magnet. The magnetic field gradient force pales in comparison with the force governing diffusion and is unable to appreciably influence the motion of individual ions on these grounds $(RT\nabla c \approx 10^{10} \,\mathrm{N/m^3} \gg F_{\nabla B} \approx 10^4 \,\mathrm{N/m^3};$

R: gas constant, T: room temperature, and ∇c : concentration gradient)⁷.

In this study, we use neutron imaging to track the concentration distribution of aqueous paramagnetic gadolinium(III) nitrate (Gd(NO₃)₃) solutions in a liquid-liquid system with a miscible nonmagnetic counterpart. This direct method consists of measuring the attenuation of a white neutron beam on passing through a liquid sample. Neutrons interact with the nuclei of the sample, which makes the measurement element-specific, allowing the direct study of liquids that are both miscible and visually indistinguishable under normal conditions. Gd is the element with the highest neutron absorption cross section ($\sigma_a = 49,700$ barn for thermal neutrons¹⁸). In addition, Gd³⁺ possesses a large magnetic moment of $7 \mu_B$ by virtue of unpaired 4f electrons. Consequently, solutions of $Gd(NO_3)_3$ are ideal candidates for neutron imaging of paramagnetic solutions, enabling the direct observation of their response to magnetic fields. Recent advances in detector systems have provided the means for neutron imaging with both high spatial and temporal resolutions $^{19-21}$. Here, we monitor the interplay of convection, magnetic field gradient force, and diffusion by variations in the neutron transmission profile.

II. MATERIALS AND METHODS

Neutron imaging experiments were carried out at the IMAGINE station²² located in the neutron guide hall of the Orphée reactor at the Laboratoire Léon Brillouin just before its final shutdown. The spectrum of the white neutron beam contained cold neutrons ($\lambda = 2-20$ Å), which emerged from a pinhole and travelled 4 m to the detector where the neutron flux was 2×10^7 cm⁻² s⁻¹. The detection system consisted of a LiF scintillator, with a resolution of 18 µm/pixel, coupled to an sCMOS camera. Recorded images of 2560×2160 pixels correspond to a field of view of 46 × 39 mm². All images shown here were obtained with an acquisition time of 60 s. The spatial resolution is on the order of 50 µm.

Quartz cuvettes with path lengths of 1 mm were filled with the liquid solutions and placed in front of the detector (see sketch in Fig. 1(a)). Incoherent scatter-



FIG. 1. (a) Sketch of the experimental setup (top view). (b) Calculated magnetic field gradient force distribution in the cuvette for a 1 M aqueous $Gd(NO_3)_3$ solution in the field of a uniformly magnetized 20 mm Nd-Fe-B cube.

ing by water molecules ($\sigma_{inc} = 160.5$ barn) was minimized by dissolving salts in D₂O ($\sigma_{inc} = 4.1$ barn). For maximum contrast, the analyzed paramagnetic salt solutions were restricted to colorless and transparent Gd(NO₃)₃ solutions. The neutron absorption cross section of Gd dwarfs the scattering cross section of D₂O ($\sigma_s = 19.5$ barn). Thus, effects of parasitic scattering on the final signal are expected to be comparatively weak. For the study of magnetic effects, cube-shaped Nd-Fe-B permanent magnets of side length 20 mm were placed adjacent to the cuvettes (2 mm from the solution within) and shielded from the neutron beam with boron carbide sheets.

An empty beam was recorded during each measurement session. This was necessary for normalization to the intensity of the white beam I_0 . Furthermore, the electronic noise I_{df} was subtracted from the image to obtain the transmittance:

$$T = \frac{I - I_{df}}{I_0 - I_{df}}.$$
 (2)

The final step of the image processing was the removal of noisy pixels by using an outlier filter.

III. RESULTS AND DISCUSSION

The Beer-Lambert law describes the attenuation of the neutron beam by the Gd^{3+} ions in D_2O :

$$I = I_0 e^{-\epsilon cl},\tag{3}$$

with the molar neutron absorption coefficient ϵ , the Gd³⁺ concentration c and the sample thickness l. Strictly speaking, ϵ depends on the neutron energy and the assumption of a single value for a polychromatic neutron beam is a simplification. This approximation is not a concern, considering the fact that the neutron wavelengths constituting the beam (2-20 Å) lie within one order of



FIG. 2. Gd^{3+} concentration calibration curve in 1 mm quartz cuvette. Transmittance values were normalized to that of a D₂O filled cuvette and follow the Beer-Lambert law (broken line) up to 0.4 M. An offset b = 0.07 (solid line) is needed at higher concentration.

magnitude of each other. A calibration of the transmitted intensity to the Gd^{3+} concentration was performed by recording images of solutions in 1 mm path length cuvettes (see Fig. 2). The attenuation follows the Beer-Lambert law up to a concentration of about 0.4 M, when the beam is almost completely absorbed and the transmitted intensity originates predominately from incoherent scattering. An offset exponential fit with an extra variable (b = 0.07) captures the behavior, but quantitative statements cannot be readily made at concentrations higher than 0.5 M.

The magnetic susceptibility of a 1 M Gd(NO₃)₃ heavy water solution ($\chi_{1M} = 322 \times 10^{-6}$) is a sum of the diamagnetic D₂O contribution ($\chi_{D_2O} = -8 \times 10^{-6}$) and the paramagnetic Curie-law contribution of the Gd³⁺ ions⁵. This value and the magnetic field distribution of the Nd-Fe-B magnet allow the computation of the magnetic field gradient force in the vicinity of the magnet (see Fig. 1(b)). The magnetic field was calculated by approximating the magnet as two uniform sheets of magnetic charge²³.

In the case of an inhomogeneous solution comprising a paramagnetic and nonmagnetic component, a magnetic field gradient orthogonal to the concentration gradient alters the equilibrium state²⁴. The $Gd(NO_3)_3$ solution climbs up the side of the cuvette until the balance between buoyancy $(F_q = \Delta \rho g)$ and magnetic field gradient forces is re-established. This can be seen in Fig. 3. Here, $100 \,\mu L$ of 0.4 M Gd(NO₃)₃ solution ($\rho = 1180 \,\mathrm{kg \, m^{-3}}$)at the bottom of a 1 mm path length cuvette was covered with 400 µL D₂O ($\rho = 1110 \text{ kg m}^{-3}$). A magnet was placed at the side and the diffusion of the $Gd(NO_3)_3$ was monitored for 3 h. The magnetic field gradient draws the $Gd(NO_3)_3$ solution towards the magnet, although homogenization by diffusion continues in its presence. An estimate for the diffusion coefficient D of $0.4 \,\mathrm{M}$ $Gd(NO_3)_3$ in D_2O can be obtained from the vertical concentration profile by a fit with the solution of the one-



FIG. 3. Neutron image of a 1 mm path length quartz cuvette with 100 µL 0.4 M Gd(NO₃)₃ solution overlain with 400 µL of D₂O. A 20 mm magnet cube to the right skews the Gd³⁺ concentration profile. (a) After 3 min (b) after 3 h. (c) Fits of Eq. (4) to the vertical cross sections (broken lines in neutron images) of the concentration profiles 3 mm ($\nabla B \neq 0$) and 19 mm ($\nabla B = 0$) away from the magnet show good agreement and the diffusion coefficient *D* can be obtained.

dimensional diffusion equation (see Fig. 3(c)):

$$c(z,t) = \frac{c_0}{2} \operatorname{erf}\left(\frac{z}{\sqrt{4Dt}}\right),\tag{4}$$

with Gd³⁺ starting concentration c_0 . The value of $D = 1.2 \times 10^{-9} \,\mathrm{m}^2/\mathrm{s}$ obtained for the nonmagnetized region after 3 h is reasonable for rare-earth ions in water²⁵. However, this value should be treated with caution, as the initial interface was smeared by introducing the liquids into the cuvette before the onset of diffusion. The diffusion coefficient from the fit for the magnetized region is higher at $D = 1.5 \times 10^{-9} \,\mathrm{m}^2/\mathrm{s}$, but the one-dimensional expression does not account for horizontal diffusion from the warped concentration profile.

The density difference between the Gd(NO₃)₃ solution and the nonmagnetic liquid can be adjusted by addition of Yttrium(III) nitrate (Y(NO₃)₃), which is transparent to neutrons ($\sigma_a = 7.0 \text{ barn}^{18}$), to the D₂O. Decreasing the density difference leads to more vigorous magnetically induced migration and facilitates magnetic confinement. If the density of the Gd solution is higher than that of the Y solution, the removal of the magnet before homogenization has taken place prompts a



FIG. 4. (a)-(f) Neutron images of 100 µL 0.4 M $Gd(NO_3)_3$ above 300 µL 1.3 M Y(NO_3)_3 solution ($\Delta \rho$ = 140 kg m^{-3}) in a 1 mm path length quartz cuvette. The view is restricted to the area below the surface in the vicinity of the liquid-liquid interface. (a) 2 min after the $Gd(NO_3)_3$ solution is suspended above the $Y(NO_3)_3$ surface. (b)-(c) Doublediffusion imposes Gd salt fingers which protrude into the $Y(NO_3)_3$ solution after 90 min and begin to sink due to the loss of buoyancy. The fingers have diameter of 1.2 mm and persist for over 8h (Multimedia view). (d) A cubic 20mm magnet at the side of the cuvette halts the instability growth and destroys the stratification instantly $(t_2: \text{ time since mag-}$ netization; Multimedia view). (e)-(f) Once the magnet is removed, the control over the $Gd(NO_3)_3$ is relinquished and it fans out. The system snaps back into the stratified state in less than 10 min and the cascading salt fingers homogenize the mixture after 2 h (t_3 : time since removal of magnet; Multimedia view). (g) Horizontal cross sections (broken lines in the neutron images) of the salt fingers in (b), (c), and (e) show a width of $\approx 1.2 \text{ mm}$ and a periodic variation of the Gd³⁺ concentration by $\approx 0.02 \text{ mol/L}$. The plotted data was smoothed with a Savitzky-Golay filter.

buoyancy-driven Rayleigh-Taylor instability^{26,27} and the Gd solution plunges to the bottom of the cuvette in a matter of seconds. A different situation arises when the density difference is inverted and the Gd solution floats above the Y solution. To investigate this, 100µL $0.4 \,\mathrm{M}$ Gd(NO₃)₃ solution was injected on top of 300 µL $1.3 \text{ M Y(NO_3)_3 solution}$ ($\rho = 1320 \text{ kg m}^{-3}$) in a cuvette (see Fig. 4(a)). After 1 h the system was beset by a salt-fingering instability due to double diffusive convection^{28,29} (see Fig. 4 (b)-(c)). This phenomenon is encountered at the interface of solutions that diffuse into each other at unequal rates. The diffusivity of Y^{3+} in the 1.3 M solution exceeds that of the Gd in the 0.4 M solution. It follows that $Y(NO_3)_3$ will diffuse laterally into small portions of $Gd(NO_3)_3$ solution that cross the interface. The increase in density due to the gained $Y(NO_3)_3$ makes the $Gd(NO_3)_3$ solution plummet in form of $1.2 \,\mathrm{mm}$ diameter fingers (see cross sections in Fig. 4(g)), which continue to leech $Y(NO_3)_3$ from their surroundings during their descent. These transport the $Gd(NO_3)_3$ advectively, two orders of magnitude faster than regular diffusion and trigger a stratification with neighboring fingers that rise thanks to the buoyancy acquired by the loss of $Y(NO_3)_3$. The stratification persists for over 8 h (see Fig. 4(c) and animations in supplementary material). Hence, the usually stabilizing factor of diffusion can destabilize a system in which the density decreases upwards. A magnet next to the cuvette erases the stratification and restabilizes the system by capturing the paramagnetic solution (see Fig. 4(d)). This does not reverse the mixing that has occurred and the Gd^{3+} ions can be seen to continuously diffuse into the $Y(NO_3)_3$ solution. The magnetic field gradient merely prevents the collapse of the liquid-liquid interface. Nonetheless, the system undergoes an immediate change upon its withdrawal (see Fig. 4(e)). Bereft of the confining magnetic field gradient force, the boundary between the solutions is once again disrupted. The ensuing release of the paramagnetic liquid is accompanied by convective mixing of the solutions amidst which the salt fingering instability can be witnessed anew. After two hours the system equilibrates as homogenization sets in (see Fig. 4(f)).

Neutron imaging is a viable method for capturing quasi two-dimensional convective and diffusive processes in solutions containing Gd³⁺ ions. A pre-existing concentration of paramagnetic fluid in some region can be redistributed within a miscible liquid by the magnetic field gradient force, which counteracts density-difference driven convection. Furthermore, double-diffusive convection in the system of magnetic $Gd(NO_3)_3$ and nonmagnetic $Y(NO_3)_3$ salt solutions is suppressed. This manifests itself in the stratification by salt fingers when the magnet is absent. The implication of this is of great importance for the development of the magnetic separation of rare-earth ions, as even minor differences in diffusivity can precipitate salt fingering instabilities. If left unchecked, these will mix the separated solutions. A prerequisite for the generation of the liquid-liquid interface is a driving force that creates and preserves the concentration gradient of the paramagnetic ions. The magnetic field gradient is then able to bestow stability upon the system. Driving forces can range from the weak factor of evaporation to the more substantial injection of electrochemical energy, which can drive convection²⁴. In view of improvements in both imaging instrumentation and available neutron flux, higher resolution and frame rates are expected to improve the neutron imaging of hydrodynamic processes in the future. This may prove valuable for the analysis of ions in solutions.

IV.

SUPPLEMENTARY MATERIAL

Time sequenced images of liquid-liquid systems containing $Gd(NO_3)_3$ and $Y(NO_3)_3$ solutions: undisturbed double-diffusive convection and magnetic confinement of a $Gd(NO_3)_3$ drop. See supplementary material for details.

V. ACKNOWLEDGMENTS

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Supplementary Material:

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S1. ADDITIONAL TIME SEQUENCED NEUTRON IMAGES



1. Unhindered mixing by salt fingering

FIG. S1. Two 1 mm path length quartz cuvettes with 75 μ L 0.4 M Gd(NO₃)₃ (left) and 100 μ L 0.5 M Gd(NO₃)₃ (right) above 300 μ L of 1.3 M Y(NO₃)₃. Gd(NO₃)₃ solutions were injected above the Y(NO₃)₃ solution surface in the left cuvette and below it in the right cuvette. Salt fingers form in both systems and mix the solutions within 7 h. Left cuvette: The surface profile is caused by capillary forces. The salt fingers begin to form at the side of the cuvette and propagate inwards. (Multimedia view)

2. Magnetic confinement of a drop of $Gd(NO_3)_3$ solution



FIG. S2. $50 \,\mu\text{L} \ 0.5 \,\text{M} \,\text{Gd}(\text{NO}_3)_3$ solution ($\rho = 1200 \,\text{kg m}^{-3}$) above $800 \,\mu\text{L} \ 1.3 \,\text{M} \,\text{Y}(\text{NO}_3)_3$ solution ($\rho = 1320 \,\text{kg m}^{-3}$) in a 2 mm path length quartz cuvette. The acquisition time was 80 s for this measurement. The calibration from Fig 2 is not valid for path lengths above 1 mm. Therefore, the negative logarithm of the transmittance is shown. (a) The $\text{Gd}(\text{NO}_3)_3$ drop migrates to the cubic 20 mm magnet at the side of the cuvette within 2 min. (b) The trapped drop in the magnetic field gradient (see (Fig. 1(b))) gradually diffuses into the $Y(\text{NO}_3)_3$ solution over the course of 5 h. (c) Salt fingers appear immediately after removal of the magnet at $t = 4 \,\text{h} \, 30 \,\text{min}$. (d) At $t = 6 \,\text{h} \, 10 \,\text{min}$, the stratification disappears after placing the magnet next to the cuvette again. (Multimedia view)