

Dispersive effects during long wave run-up on a plane beach

Ahmed Abdalazeez, Ira Didenkulova, Denys Dutykh

▶ **To cite this version:**

Ahmed Abdalazeez, Ira Didenkulova, Denys Dutykh. Dispersive effects during long wave run-up on a plane beach. Fernandes F.; Malheiro A.; Chaminé H. Advances in Natural Hazards and Hydrological Risks: Meeting the Challenge, Springer, pp.143-146, 2020, 978-3-030-34397-2. 10.1007/978-3-030-34397-2_28 . hal-02366937

HAL Id: hal-02366937
https://hal.science/hal-02366937

Submitted on 16 Nov 2019

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution - NonCommercial - ShareAlike 4.0 International License

Springer
SPRINGER NATURE

Dispersive effects during long wave run-up on a plane beach

Ahmed Abdalazeez[1], Ira Didenkulova[1,2*] and Denys Dutykh[3]

[1] Department of Marine Systems, Tallinn University of Technology, Tallinn, Estonia
[2] Nizhny Novgorod Technical University n.a. R.E. Alekseev, Nizhny Novgorod, Russia
[3] Univ. Grenoble Alpes, Univ. Savoie Mont Blanc, CNRS, LAMA, 73000 Chambéry, France
*corresponding author: irina.didenkulova@taltech.ee

Abstract. Dispersive effects during long wave run-up on a plane beach are studied. We take an advantage of experimental data collection of different wave types (single pulses, sinusoidal waves, bi-harmonic waves, and frequency modulated wave trains) and simulate their run-up using two models: (i) non-dispersive nonlinear shallow water theory and (ii) dispersive Boussinesq type model based on the modified Peregrine system. It is shown, that for long positive pulses, dispersive effects are not so important and nonlinear shallow water theory can be used. However, for periodic sinusoidal and bi-harmonic pulses of the same period, the dispersive effects result in significant wave transformation during its propagation, but do not have a strong impact on its maximal run-up height. Overall, for maximum wave run-up height, we could not find a preference of dispersive model against the nondispersive one, and, therefore, suggest using nonlinear shallow water model for long wave run-up height estimation.

Keywords: Long Wave Run-up, Frequency Dispersion, Nonlinear Shallow Water Theory, Modified Peregrine System.

1 Introduction

There are several reasons why the nonlinear shallow water theory (NLSW) is favored for long wave run-up calculations as compared to dispersive wave models, often represented by Boussinesq-type approximations. First of all, wave run-up calculated using dispersive codes is prone to numerical instabilities, which make computations more sensitive to numerical parameters (Bellotti and Brocchini, 2002). Second, the Boussinesq terms in dispersive model tend to zero at the shoreline, so that dispersive equations simplify to NLSW in this region (Madsen et al. 1997).

Horrillo et al. (2006) studied dispersive effects during 2004 Indian Ocean tsunami propagation by comparing NLSW with the fully nonlinear Navier-Stokes equations (FNS). They came to conclusion that, NLSW is more suitable in hazard assessments (e.g. it has a very low computation cost and often it over-predicts the maximum wave run-up height, whereas this property is consider a safety factor). Moreover, Glimsdal et al. (2013) suggested that NLSW is more appropriate for warning purposes. However, dispersive effects become more important in trailing waves, whereas the leading

waves can be well described by NLSW (Løvholt et al. 2014). Note, that maximum wave is often not the first one, at least for tsunamis propagating over a long distance, see, for example, Candella et al. (2008).

Most of the mentioned studies were based on numerical results and were missing the fidelity control mechanism. Therefore, in this paper we take an advantage of available experimental data collection of different wave types (single pulses, sinusoidal waves, bi-harmonic waves, and frequency modulated wave trains) and simulate their run-up using two models: (i) NLSW, and (ii) dispersive model of Boussinesq type based on the modified Peregrine system (mPer).

The paper is organized as follows. In Section 2, we describe the available experimental dataset. The numerical models (NLSW and mPer) are briefly described in Section 3. In Section 4, we compare numerical results of NLSW and mPer models with the experimental data. The main results are summarized in Section 5.

2 Experimental data

The experiments were conducted in the Large Wave Flume (GWK), Hannover, Germany. The experimental set-up consisted of a 251 m long section of constant depth 3.5 m and a plane beach with a slope angle 1:6 (fixed asphalt bed). There were from 16 to 18 wave gauges recording wave propagation along the flume. The wave run-up was measured by capacitance probe, which was supplemented by two regular video cameras. Waves were generated by the piston type wave maker, which showed to be efficient for long wave generation (Schimmels et al. 2016). The generated waves are listed in Table 1. Details of this experiment can be found in Didenkulova et al. (2013).

Table 1. Generated waves and their run-up heights

Type of waves	Wave period (s)	Initial wave amplitude (m)	Experimental run-up (m)	NLSW run-up (m)	mPer run-up (m)
Positive pulse	20	0.10	0.259	0.268	0.254
Positive pulse	20	0.24	0.795	0.840	0.780
Sine wave	20	0.05	0.096	0.13	0.14
Sine wave	20	0.60	2.27	1.80	1.81
Bi-harmonic wave	20	0.12	0.79	0.89	0.85
Bi-harmonic wave	20	0.15	1.3	1.37	1.32
Wake-like train	20→10	0.10	0.46	0.60	0.51
Wake-like train	20→10	0.40	2.14	1.68	2.57

3 Numerical set-up

In the present work, two different numerical models are used: the non-dispersive nonlinear shallow water model (NLSW) and dispersive Bousinessq type model based on the modified Peregrine system (mPer). Both models were set not taking into account

bottom friction and assumed the fluid being perfect and the flow to be incompressible and irrotational.

The model left boundary conditions corresponded to the experimental wave conditions in Table 1. On the right, we placed a sufficiently long plane beach to avoid any interactions with the right boundary.

More precisely, the bathymetry in numerical experiments was set up to reproduce the Large Wave Flume conditions:

$$h(x) = \begin{cases} h_0, & x \in [a,b] \\ h_0 - (x-b)\tan\alpha, & x \in [b,c] \end{cases}, \tag{1}$$

where h_0 = 3.5 m is the constant water depth, α is the bottom slope (tanα = 1:6). The distance $x \in [a,b]$ is the cell interfaces, x_c is the centre of a cell, [a, c] are left and right boundaries of the numerical flume (a = 0 m), and b = 251 m is the point where the slope starts. The distance $x \in [a,b]$ has been divided into number of cells $c_i = (X_{i-1/2}, X_{i+1/2})$, where X_i is the center of cell i, $X_i = 1/2(X_{i-1/2} + X_{i+1/2})$.

The numerical time steps can be calculated as $\Delta t = \left(\frac{t_f - t_i}{M}\right)$, where t_i is the initial time, t_f is the final time and M is the number of time steps.

3.1 Nonlinear shallow water (NLSW) model

The 1D nonlinear shallow water equations are:

$$H_t + (Hu)_x = 0, \tag{2}$$

$$(Hu)_t + \left(Hu^2 + \frac{g}{2}H^2\right)_x = gHh_x, \tag{3}$$

where $H = h + \eta$ is the total water depth, $\eta(x, t)$ is the water elevation with respect to the still water level, $u(x,t)$ is the depth-averaged flow velocity, $h(x)$ is an unperturbed water depth described by Eq. (1), g is the gravitational acceleration, x is the coordinate directed onshore, and t is time. We use the finite volumes method. The numerical scheme is based on the second order UNO2 reconstruction, for more details see (Dutykh et al. 2011).

3.2 Modified Peregrine (mPer) model

The Boussinesq equations for long dispersive wave propagation, derived by Peregrine (1967), are:

$$\eta_t + ((h+\eta)u)_x = 0, \tag{4}$$

$$u_t + uu_x + g\eta_x - \frac{h}{2}(hu)_{xxt} + \frac{h^2}{6}(u_{xxt}) = 0\,. \tag{5}$$

This classical Peregrine system was modified by Durán et al. (2018) in order to recover the conservative form of equations.

Eq. (4) of the mass conservation in new variables becomes:

$$H_t + Q_x = 0\,, \tag{6}$$

where Q is the horizontal momentum, H is the total water depth.

The momentum conservation equation obtained from Eq. (5) becomes (Durán et al. 2018):

$$\left(1+\frac{1}{3}H_x^2 - \frac{1}{6}HH_{xx}\right)Q_t - \frac{1}{3}H^2Q_{xxt} - \frac{1}{3}HH_xQ_{xt} + \left(\frac{Q^2}{H} + \frac{g}{2}H^2\right)_x = gHh_x\,. \tag{7}$$

Eqs. (6) and (7) are called the modified Peregrine equations and are studied in detail in Durán et al. (2018).

4 Results

The two models described above have been used to reproduce the Large Wave Flume experiments listed in Table 1. The water surface elevation has been recorded by different wave gauges at different distances from the wave maker, including wave run-up. The comparison simulated by NLSW and mPer models against measured experiments. The maximum wave run-up heights are shown in Table 1. For periodic waves, the comparison is made for experimentally measured wave with the maximum run-up height. The deviations of computational run-up heights from the measured ones are shown in Table 2.

Table 2. Deviations of computational run-up heights from the measured ones in %

Type of waves	Initial wave amplitude (m)	Experimental run-up (m)	NLSW (%)	mPer (%)
Positive pulse	0.10	0.259	3	-2
Positive pulse	0.24	0.795	6	-2
Sine wave	0.05	0.096	35	45
Sine wave	0.60	2.27	-21	-20
Bi-harmonic wave	0.12	0.79	13	8
Bi-harmonic wave	0.15	1.3	5	2
Wake-like train	0.10	0.46	30	11
Wake-like train	0.40	2.14	-22	20

It can be noticed that for long positive pulses results of both NLSW and mPer models are in a good agreement with experimental data (Fig. 1). In the weak amplitude case NLSW overestimates the experimental result by 3%, while mPer underestimates it by 2%. For the initial wave of higher amplitude, the discrepancy is also higher: 6% for NLSW and 2% for mPer (Table 2). Therefore, one can conclude that the dispersive effects are not so important to predict the run-up height for the class of long single waves of positive polarity and the NLSW can be used.

For dispersive wake-like trains and even for periodic waves (sine waves and bi-harmonic waves) the situation is quite different. Most of the results of both NLSW and mPer have an accuracy of 20-30 % and do not really show the preference of one model against the other. Note, most of wave gauges located along the basin demonstrate the importance of dispersive effects, which are captured by mPer model and ignored by NLSW, but according to Table 2 they do not have principal impact on maximum run-up height. This somehow supports the existing general opinion that for the maximum wave run-up estimation NLSW is enough.

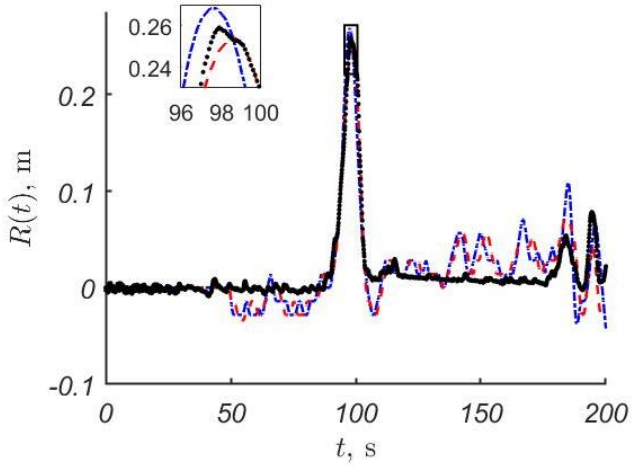


Fig. 1. Run-up height time-series for a positive pulse of A = 0.1 m, T = 20 s, calculated by mPer (red dashed line), NLSW (blue dash-dotted line) and measured experimentally (black dots).

5 Concluding Remarks

We used the nonlinear shallow water model (NLSW) and dispersive Boussinesq type model based on the modified Peregrine system (mPer) to reproduce physical experiments of long wave propagation and run-up. The studied waves were of different shapes and amplitudes and included long single pulses of positive polarity, periodic sine and bi-harmonic waves and dispersive wake-like wave trains.

It is found, that in our wave collection, the single pulses had the best agreement with both models and dispersive effects in this case were negligible. For periodic

waves and dispersive wave trains the dispersive effects were important, and mPer model gave much better fit to the records of tide-gauges, located along the flume. However, for maximum run-up height this better capture of dispersive effects did not play a big role, and both models resulted in 20-30 % deviation from the experimental data.

Acknowledgements

Numerical simulation of wake-like wave trains was carried out with a financial support from Russian Science Foundation grant 16-17-00041, simulation of other wave types was supported by ETAG grant PUT1378. The experimental data were obtained within Hydralab IV Grant HyIV-FZK-03. Authors also thank the PHC PARROT project No 37456YM, which funded the authors' visits to France and Estonia and allowed this collaboration.

References

1. Bellotti G, Brocchini M (2002) On using Boussinesq-type equations near the shoreline: a note of caution. Ocean Engineering 29(12):1569–1575
2. Candella RN, Rabinovich AB, Thomson RE (2008) The 2004 Sumatra tsunami as recorded on the Atlantic coast of South America. Advances in Geosciences 14:117-128
3. Didenkulova I, Denissenko P, Rodin A, Pelinovsky E (2013) Effect of asymmetry of incident wave on the maximum runup height. Journal of Coastal Research 65:207–212
4. Durán A, Dutykh D, Mitsotakis D (2018) Peregrine's System Revisited. In Abcha N, Pelinovsky E, Mutabazi I (eds.) Nonlinear Waves and Pattern Dynamics. p. 3–43, Springer, Cham
5. Dutykh D, Katsaounis T, Mitsotakis D (2011) Finite volume schemes for dispersive wave propagation and runup. Journal of Computational Physics 230(8): 3035–3061
6. Glimsdal S, Pedersen GK, Harbitz CB, Løvholt F (2013) Dispersion of tsunamis: does it really matter? Nat. Hazards Earth Syst. Sci. 13:1507–1526
7. Horrillo J, Kowalik Z, Shigihara Y (2006) Wave dispersion study in the Indian Ocean-tsunami of December 26, 2004. Marine Geodesy 29(3):149–166
8. Løvholt F, Pedersen G, Bazin S, Kühn D, Bredesen RE, Harbitz C (2012) Stochastic analysis of tsunami runup due to heterogeneous coseismic slip and dispersion. Journal of Geophysical Research: Oceans 117: C03047
9. Madsen PA, Banijamali B, Schäffer HA, Sørensen O.R (1997) Boussinesq type equations with high accuracy in dispersion and nonlinearity. In Edge B (ed.) 25th Conference 1996, ASCE, vol. 1, p. 95–108. Coastal Engineering, Hørsholm
10. Peregrine DH (1967) Long waves on a beach. J. Fluid Mech. 27:815–827
11. Schimmels S, Sriram V, Didenkulova I (2016) Tsunami generation in a large scale experimental facility. Coastal Engineering 110:32–41

View publication stats