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1	The helical motions of roots are linked to avoidance of particle forces in soil
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24 Abstract

- Limitation to root growth results from forces required to overcome soil
 resistance to deformation. The variations in individual particle forces affects
 root development and often deflects the growth trajectory.
- We have developed Transparent Soil and Optical Projection Tomography
 microscopy systems where measurements of growth trajectory and particle
 forces can be acquired in a granular medium at a range of confining pressures.
 We developed image processing pipelines to analyse patterns in root
 trajectories and a stochastic-mechanical theory to establish how root
 deflections relate to particle forces and thickening of the root.
- Root thickening compensates for the increase in mean particle forces but does
 not prevent deflections from 5% of most extreme individual particle forces
 causing root deflection. The magnitude of deflections increases with pressure
 but assemble into helices of conserved wavelength in a response linked to
 gravitropism.
- The study revealed mechanisms for the understanding of root growth in
 mechanically impeding soil conditions and provides insights relevant to
 breeding of drought-resistant crops.

42 Keywords

43 Biophysics, root, granular, mechanical stress, deflection, Transparent Soil

45 Introduction

To improve crop water and nutrient efficiency of crops, significant plant breeding interest is now focused on modifying the architecture of the root system to improve rooting depth (Lynch, 2011). Much of the attention is given to genetically controlling rooting angles to enhance drought resistance (Uga *et al.*, 2013) or to enhance nutrient acquisition (Liao *et al.*, 2001). While most crop research takes molecular genetics approaches to study the development of root system architectures, limitations arise because suitable traits for deep rooting are difficult to identify.

53 There is consequently a growing interest in understanding the biomechanical factors 54 that limit root growth through soil (Colombi et al., 2017b). Physical limitations to tissue expansion are linked to the physiology of the cell, in particular the cells ability 55 56 to sustain turgor pressure and to soften the properties of cell walls (Mirabet et al., 57 2011). Turgor pressure results in the build-up of tension forces within cell walls and growth occurs because the network of cellulose microfibrils permit extension and 58 rearrangement (Braidwood et al., 2014) through a mechanism termed polymer creep. 59 Although the extensibility of primary cell walls is biochemically controlled (through 60 pH, production of enzymes and free radicals, Cosgrove, 2005), growth can be 61 mechanically arrested because external pressure exceeds turgor pressure, as initially 62 shown by early biophysicists (Green et al., 1971) and later studies (Geitmann & 63 Ortega, 2009). 64

This view of the biophysics of growth is challenged in soils where plant roots grow 65 66 under considerable levels of external pressure from an inhomogeneous soil medium. 67 Turgor pressure in plant cells is rarely measured above 1 MPa, even when growth has 68 been arrested (Meshcheryakov et al., 1992; Clark et al., 1996). This level of pressure 69 corresponds well to the maximum axial pressure a root can exert on a rigid obstacle 70 (Misra et al., 1986) but not to the soil penetrometer pressure at which growth is arrested (5 MPa). Differences are attributed to lubrication by border cells, or flexibility 71 of the root tissue (Bengough & Mullins, 1990). Still, turgor pressure within root cells 72 is an order of magnitude less than known physiological limits of turgor, for example 73 in fungal appressoria where turgor pressure can exceed 10 MPa (Howard et al., 1991). 74 75 Turgor pressure itself may not be the basis for limitation to deep rooting, and it is reasonable to question why plants are not generating larger growth forces to penetratehard soils.

78 The inhomogeneity of soil makes it difficult to understand the forces experienced by roots. Soils are comprised of particles held together by forces at the contact points 79 80 between adjacent particles (repulsion, friction, cohesion). Even when dry and monodisperse, packings of particles are disordered (Majmudar & Behringer, 2005). 81 Large variations in particle forces arise because of the heterogeneous distribution of 82 contact points between particles, with the tail of the probability distribution of particle 83 forces following an exponential distribution (Radjai et al., 1998). It is not clear how 84 such a stochastic distribution of forces will affect the growth of a root. The mechanics 85 86 of root penetration has been the subject of recent computational studies (Fakih et al., 87 2019), but conceptual frameworks to understand the nature of root responses to granular forces are still lacking. 88

We report here an analysis of microscale deflections of growth due to interactions with the soil granular structure. We develop an experimental system that captures the statistical distribution of particle forces exerted on the root and analyse growth responses to these forces. We propose a theory that links root elongation to particle force and show that root responses to mechanical interactions with particles are linked to the statistical distribution of these forces.

95 Materials and methods

Transparent Soils. Transparent Soil is a soil surrogate made of Nafion[™], a 96 transparent low refractive index polymer. It was prepared as described in (Downie et 97 al., 2012). Nafion pellets (4 mm×3 mm NR50 1100, Ion Power Inc., USA) were 98 freezer milled and sieved with 1250 µm and 250 µm mesh size and polydispersity 99 further characterised by image analysis (Methods S1-1). Particles were immersed in 100 101 stock solutions of Hoagland No 2 basal solution (H2395, Sigma, USA) to adjust the 102 pH and titrate the particles with mineral ions. These were shaken at 30°C for 30 minutes before replacing the nutrient solution (Downie et al., 2012), and the operation 103 104 was repeated until the pH was 6.5. The particles were rinsed with dH₂O to remove excess Hoagland media and autoclaved in dH₂O at 30% water content. The resulting 105 106 particles had sizes ranging from 0.20 to 2.21 mm (Figure 1A).

Pressure chambers. Chambers were made of SterilinTM Quickstart Universal 107 Polystyrene 30mL tubes, and the piston applying the force at the surface of the soil 108 was made of SterilinTM Polystyrene 7 mL tubes (Methods S1-2). The piston was 109 transparent to allow penetration of light and fitted with negligible friction with the 110 inner wall of the chamber. A 3 mm hole was drilled in the cap of the inner tube (piston) 111 to introduce the seed or the penetrometer needle for measuring penetration resistance 112 113 forces. Compression in the chamber was applied by moving the base of the stage 114 (Methods S1-2) and monitoring soil confining pressure with a 20 N load cell (Applied Measurements Ltd). The intensities of the compression applied to the soil were 0 N (0 115 kPa, control), 10 N (25 kPa) and 20 N (50 kPa). 116

Resistance to penetration. Penetrometer resistance was measured within chambers 117 under confining pressure of 0 kPa, 25 kPa and 50 kPa (n=6). Penetrometer resistance 118 was measured using an Instron 5544 universal test frame (Instron, MA, USA) fitted 119 with a 50 N load cell accurate to ± 2 mN (Methods S1-3). The penetrometer needle 120 used was a cone shaped tip of 30° semiangle with a base of 1.72 mm in diameter and 121 a cross-sectional area of 2.32 mm² and a 20% rebated shaft to minimise shaft friction. 122 Shaft cones of 30° semiangle are commonly used as root analogues because they 123 compromise well between cone friction and formation of soil bodies (Bengough & 124 Mullins, 1990). Crosshead displacement for penetrometer testing was performed at a 125 rate of 2 mm min⁻¹ to maintain quasi-static conditions (Methods S1-2). It has been 126 shown experimentally that dynamic effects are observed for penetration rates that are 127 128 one or two orders of magnitude larger (Bengough & Mullins, 1990). Depths of 20 to 40 mm were tested because the mean force was approximately constant over this range 129 and shaft friction negligible. We define the particle force F_i as the ith peak of force 130 recorded in this experiment. Mean force $\langle F \rangle$, third quartile $F_{75\%}$, and probability 131 distribution of particle forces were characterised. 132

Root biomechanics. The mechanical resistance of seedling roots (n=7) was tested under compression. Seeds were germinated using germination paper until the roots were approximately 2 cm long. Seedling primary roots were then anchored in plaster of Paris and tested under axial compression (Methods S1-3) using an Instron 5544 universal test frame as described above.

Plant growth. Lentil (Lens culinaris) cv. Peridot seeds were sterilised in 10% solution 138 of sodium hypochlorite for 20 minutes. Seeds were pre-germinated on germination 139 paper at 25°C and photoperiod of 16 h. After root protrusion (36 h), the seeds were 140 transferred to a cylindrical chamber containing Transparent Soil held at 30% 141 volumetric water content. The germinated seeds grew for 3 days at 25°C in soil 142 maintained at 0 kPa, 25 kPa and 50 kPa of confining pressure (n=5). Roots were then 143 144 washed and digitally scanned with root diameter measured along the first 2 cm of the 145 root from the apical meristem.

3D Microscopy. After 3 days of growth, a solution of 20% trehalose was added for 146 refractive index matching with the soil particles. A vacuum pump (RelChron PPROB-147 10398) was used to remove air bubbles present in the samples. Images were collected 148 15 hours after the addition of trehalose under laboratory conditions with an Optical 149 Projection Tomography microscope (Sharpe et al., 2002). The microscope was made 150 from a Leica MZ16 FA stereomicroscope fitted with a 0.5X plan achromatic objective 151 152 for long working distance (135 mm) and a Leica DFC350FX camera (Figure 1B). Each scan consisted of 720 projections taken every 0.5 degree. Scans were obtained at three 153 different depths and achieved 13 to 20 µm resolution and 3 cm field of view out of 5 154 cm of soil depth. The image data obtained from three different depths were combined 155 using Fiji sequence stitching (Schindelin et al., 2012), and 3D reconstructions were 156 157 performed in Matlab (MathWorks Inc.) using the filtered backprojection algorithm. Confocal laser scanning imaging was done on a Nikon A1R microscope. Roots were 158 stained with calcofluor (fluorescent brightener 28; Sigma F3543) and imaged using 159 either x4 or x10 magnification. 160

Signal processing. We developed a pipeline to reconstruct the root centreline with 161 precision (Figure 2A). First, a 3D vessel tracing algorithm was used to obtain a coarse 162 representation of the root centreline (Friman et al., 2010). To improve the accuracy 163 and precision of the root centreline a multiplane tracing approach was developed 164 (Methods S2-1) by generalisation of bi-plane snakes (Canero et al., 2000). Root 165 166 centrelines were subsequently centred along the z-axis. This was achieved using a spline regression with 3 anchor points and fitted values were subtracted from the 167 original signal. Centred signals f(t) were then analysed for helical patterns. The 168 analysis was based on a modification of the Fourier transform to include orthonormal 169 170 helix forming basis functions (Figure 2B),

$$\psi_0(t) = (0, 0, \sqrt{3}t) \text{ and } \psi_k(t) = (e^{i2\pi kt}, e^{i(2\pi kt - \pi/2)}, 0),$$
(1)
 $k \in [-N, N].$

171 *t* represents the rooting depth and *k* the spatial frequency. The sign of *k* indicates 172 clockwise or anti-clockwise helices. The coefficients of the transform C_k are then 173 obtained by projection on the set of basis functions,

$$C_k = \int_0^T (f_x; f_y; f_z/T^2) \cdot \overline{\psi_k} dt.$$
⁽²⁾

174 The wavelength of the helix is $\lambda_k = |1/k|$. $\tilde{\lambda}_k$ is the length of root contained in a helix 175 of one period is therefore

$$\tilde{\lambda}_k = \sqrt{1 + (2\pi k r_k)^2} \lambda_k,\tag{3}$$

176 where $r_k = \sqrt{C_k \overline{C_k}} + \sqrt{C_{-k} \overline{C_{-k}}}$ is the radius of the waveform of frequency *k*. We also 177 introduce the asymmetry ratio R_a ,

$$R_a = \frac{C_{-j}\overline{C_{-j}}}{C_k\overline{C_k}} \tag{4}$$

where k>0 and j>0 are respectively the clockwise and anticlockwise dominant 178 frequencies of opposite sense of rotation. The asymmetry ratio $0 \le R_a \le 1$ indicates 179 180 whether the helix change its sense of rotation during growth. When clockwise and anticlockwise spectra have identical peaks, R_a is equal to 1, and in the case of a perfect 181 182 helix of infinite length, it is equal to 0. When analysing real data, extremal values are not reached but relative values of R_a indicate the degree of consistency of the sense 183 of rotation of a root helical trajectory. Changes in root directions were identified as 184 local maxima in the root curvature. A custom software RootHix was developed to 185 perform the analyses (www.archiroot.org.uk/tools.html). Full mathematical derivation 186 of the analysis can be found in Methods S2-2. The data generated in this study is 187 for Zenodo available download the following repository 188 on https://zenodo.org/record/889946#.WbgwrsiGO-4. 189

190 Theory for root-particle interactions. Root deflection occurs when the energy of 191 axial elongation U_e becomes larger than the energy U_b required for bending and lateral 192 displacement of particles (Figure 2C),

$$U_b(E, I, \langle F \rangle, d, \delta) < U_e(F, \delta).$$
⁽⁵⁾

- 193 F (N) is the force required to displace the particle in front of the root, E (Pa) is the 194 Young's modulus of the root tissue, I (m⁴) is the second moment of area of the root, 195 $\langle F \rangle$ is the mean particle force, δ is the mean displacement between two peak forces in 196 a penetrometer test, and d is the distance between particles determined as the mean 197 particle diameter (Methods S3).
- 198 Since U_e is a growing function of F, it is possible to calculate from equation 5 a 199 critical force F_{crit} above which the deflection of the root will occur,

$$F_{crit} = A(EI)^{1/4} \langle F \rangle^{3/4} d^{1/2} \delta^{-1}, \tag{6}$$

with a bending constant $A \approx 0.237$. A similar calculation can be made if the tissue has viscoelastic properties. In this case, *E* is replaced with a time-dependent coefficient $E^*(t)$, termed creep function, which we obtain from the Kelvin Voigt viscoelastic model,

$$\frac{1}{E^*(t)} = \frac{1}{E} \left(1 - \exp\left(-\frac{E}{\eta}t\right) \right). \tag{7}$$

t here refers to the time required for the root growth to overcome a particle and is determined as d/v where v is the root tip velocity (m s⁻¹). The probability of a deflection occurring can then be expressed from the distribution of particle forces obtained from penetrometer test. Because deflections are rare, they must be caused by large particle forces which occurrence is described by the tail of the distributions of particle forces. These follow an exponential law,

$$q = \frac{1}{4} \exp[-b(F_{crit} - F_{75\%})].$$
(8)

The theory then provides the probability distribution (pdf) σ and κ of the occurrence of deflections and curvature of the root respectively,

$$\sigma(x) = \frac{q}{\delta} \exp\left(-\frac{xq}{\delta}\right),\tag{9}$$

$$\kappa(x) = \frac{q^2 d^2}{\langle l \rangle^2 \delta^2 x^3} \exp\left(-\frac{q d}{\langle l \rangle \delta x}\right).$$
(10)

212 $\langle l \rangle = B(d^2 E I / \langle F \rangle)^{\frac{1}{4}}$ is the expected bending length with $B \approx 2.06$. The pdf of root 213 curvature follows an inverse gamma distribution with shape parameter 2 and scale 214 parameter $qd/\langle l\rangle\delta$. Full mathematical derivation for models can be found in Methods 215 S3.

When the tissue is anisotropic, root reorientation occurs preferentially along a given 216 axis of rotation (blue cone, Figure 2D). The axis of rotation defines two equally 217 probable bending directions V_1 and V_2 . Because the anisotropy is helical, V_1 and V_2 218 are not constant but rotate along the roots (red arrow, Figure 2D). To test whether 219 deflections occur preferentially in certain directions, we assign the probability q_1 for 220 direction V_1 and $q_2 = 1 - q_1$ for V_2 . We used equations 5-8 to simulate the 221 occurrence of deflections in an elongating root based on experimental data and 222 assumed three scenarios for the direction of deflection. If the deflection has no 223 predefined direction (random deflection) then $q_1 = q_2 = 0.5$. If there is an intrinsic 224 sense of rotation then $q_1 = 1$ or $q_2 = 1$. If the direction of deflection occurs 225 226 preferentially towards gravity (gravitropic deflection), the probability is

$$q_1 = \frac{\tanh(-G\Delta\alpha) + 1}{2} \tag{11}$$

227 $\Delta \alpha = \alpha_1 - \alpha_2$ is the difference in verticality between V_1 and V_2 , i.e. α_1 (respectively 228 α_2) is the positive angle between V_1 (respectively V_2) and the downward vertical. *G* 229 defines the sensitivity of the response to gravity.

230 **Results**

231 **Resistance to penetration.** Penetrometer tests produced stochastic data (Figure 3A). Analysis of the data showed soil confining pressure (0 kPa, 25 kPa, and 50 kPa, 232 generated by loads of 0 N, 10 N and 20 N respectively) increased the mean penetration 233 234 force. In soils that were not held under compression, the mechanical resistance to penetration was the lowest with $\langle F \rangle = 0.15$ N (±0.01), $F_{75\%} = 0.19$ N. In soils held 235 under a confining pressure of 25 kPa, the resistance to penetration increased to $\langle F \rangle =$ 236 1.11 N (\pm 0.03), $F_{75\%} = 1.18$ N. The highest resistance to penetration, $\langle F \rangle =$ 237 2.14 N (\pm 0.03), $F_{75\%}$ = 2.26 N, was obtained in soils held at a confining pressure of 238 239 50 kPa (Figure 3B).

We analysed the sequence of forces recorded during penetration (Figure 3C&D). The tail of the statistical distribution of transformed particle forces (Figure 3C) showed an exponential decline, with characteristic force values (1/*b*) measured as 36.3 mN, 75.9 mN and 95.3 mN for respectively 0 kPa, 25 kPa and 50 kPa of soil confining pressure.
Permutation tests showed the exponential tail of the distribution was not affected by
the increase in confining pressure from 25 kPa to 50 kPa (p=0.88), but there was a
statistical difference between uncompressed and compressed soils (p<0.001).

We also studied the distances δ between peak forces (Figure 3D). The probability density of δ followed an exponential decline with a characteristic distance of 0.13 mm. No statistical differences were found between soils under compression (p=0.94) nor between compressed and uncompressed soil (p=0.12). The distance between the peaks of force was substantially smaller than the size of the particle diameter (1 mm on average).

- Roots helical response to mechanical forces. Plant roots grew healthily in all 253 254 experiments (Figure 4A). Soil confining pressure reduced root elongation rates and increased root diameters. Roots growing in soil without confining pressure exhibited 255 the fastest elongation rate of 1.99 cm.d⁻¹ (± 0.40) and had diameters of 0.64 mm (± 0.04) 256 at 2 cm from the root tip. Roots growing in soil under 25 kPa of confining pressure 257 exhibited an elongation rate of 1.60 cm.d⁻¹ (± 0.42) and had diameters of 0.69 mm 258 (±0.03). Roots growing in soil under 50 kPa of confining pressure exhibited an 259 elongation rate of 1.36 cm.d⁻¹ (± 0.28) and had diameters of 0.75 mm (± 0.07). 260
- Root centrelines exhibited helical morphologies (Figure 4A) which could be detected 261 by helical transformation (Figure 4B). The analysis identified a dominant wavelength 262 that is not affected by soil confining pressure. Wavelength values ($\tilde{\lambda}$) were 13.7 mm 263 (±1.4), 12.1 mm (±0.5) and 12.8 mm (±0.6) for pressures of 0 kPa, 25 kPa and 50 kPa 264 respectively (Figure 4C). However, the radius of the helix $r_k r_k$ significantly increased 265 from 0.17 mm (± 0.03), to 0.24 mm (± 0.03) and 0.30 mm (± 0.04) for pressures of 0 266 kPa, 25 kPa and 50 kPa. These helical shapes had curvatures of respectively 0.034 267 mm⁻¹, 0.063 mm⁻¹ and 0.071 mm⁻¹. Helices were clockwise, anti-clockwise and 268 occasionally changed direction of rotation along the same root axis. 269
- Compression tests were used to characterise the mechanical properties of roots (Figure 4D). All roots tested deformed into a helical shape at an average force of 20.0 mN (\pm 1.5). Helical shapes were more pronounced near the tip where the root was thinner. Roots retained their helical shape after removal of the axial forces. The wavelength of the helix ($\tilde{\lambda} = 12.2 \text{ mm} \pm 2.0$) closely matched those measured in Transparent Soil, but

the radius of the helix (0.9 mm \pm 0.1) was about three times as large as the value measured under 50 kPa of confining pressure. The mechanical test was interrupted before roots were visibly fractured. Roots were subsequently moved into water and recovered their shape within 20 minutes.

279 Soil particles influence root deflections. Roots curvatures at deflections exceeded those of fitted helices by an order of magnitude (Figure 5A). The distance between the 280 sites of deflections was not influenced by the pressure acting on the soil. The 281 distribution of the distance between the sites of two successive deflections was 282 approximately uniform, with distances spanning between 500 µm and 6 mm with an 283 284 average of 2.5 mm (Figure 5B). Since the characteristic distance between peaks of forces produced by soil particles is $\delta = 0.13$ mm and one deflection occurs every 2.5 285 mm of root growth in average, thus 5% of particle force events produced root 286 deflections. 287

The curvature of the root where deflection occurs was influenced by soil confining 288 pressure (Figure 5C). In the absence of confining pressure, curvatures were below 0.2 289 290 mm⁻¹. When 25 kPa of pressure was applied, curvatures measured were below 0.3 mm⁻¹ ¹, whereas when 50 kPa of pressure was applied, curvatures above 0.4 mm⁻¹ were 291 292 measured. Confocal laser scanning microscopy observations showed sharp deflections 293 extending over a length of root of around 700 µm. The curvature of these deflections 294 increased with increases in confining pressure. There was little evidence of tissue torsion. Angle in the files of epidermal cells relative to the local longitudinal root axis 295 296 was rarely observed and did not correlate with the sites of deflection (Figure 5C Inset).

Linking root gravitropism and deflections to helix formation. The model described 297 298 the overall root responses to confining pressure for the distribution of curvatures (Figure 6A Top) but overestimated the deflection in the high frequency domain 299 (Figure 6A Middle). The Young's modulus required to predict the range of curvatures 300 varied between 1.5 and 5.0 MPa (3.7 MPa ±1.4, 1.64 MPa ±0.62 and 2.05 MPa ±0.78 301 for respectively 0 kPa, 25 kPa and 50 kPa of confining pressure) and declined with 302 303 confining pressure (Figure 6A Bottom). Apparent variations in the Young's modulus 304 may be due to the viscoelasticity of the tissue, with Kelvin Voigt model best fitting data with E = 21.5 kPa and $\eta = 1.7$ GPa. s. 305

There was strong evidence of the role of gravitropism in the maintenance of helical 306 shapes. Experimental results showed the 307 asymmetry ratio R_a is decreasing linearly with root deviation from verticality (black 308 curves, Figure 6B top right). Roots that grew more horizontally had therefore a greater 309 310 tendency to maintain a consistent helix and conserved sense of rotation. Simulations demonstrated this is caused by a bias in the direction of growth when a deflection 311 312 occurs. When random deflections were imposed in the simulations (red curves, Figure 6B), roots lost their ability to maintain helical forms due to the sense of rotation of the 313 314 helix changing randomly when hitting an obstacle: R_a was larger than in all other cases and also independent of the deviation from verticality. Roots which deflected 315 following a fixed direction V_1 or V_2 (green curves, Figure 6B) naturally produced helix 316 317 with unchanged sense of rotation (asymmetry ratio ≈ 0.3). Here too, the model could not predict the experimental effect of deviation from verticality on the asymmetry 318 319 ratio. Roots which direction of deflection was influenced by root verticality (gravitropic simulation, Figure 6B, blue curve) produced more realistic growth 320 321 patterns and induced the formation of helices with occasional switches in the sense of rotation, but these switches were less frequent. 322

323 Discussion

324 Linking root responses to soil structure. Biophysical theories link growth response to soil pressure, cell wall rheology, and water potential (Greacen & Oh, 1972; Dexter, 325 1987). If the soil pressure on the root and the tensile stresses in the cell walls exceed 326 turgor pressure, then growth must be arrested (Plant, 1982; Dexter, 1987). Our 327 328 approach departs from this view and links root physical limitations to the mechanical 329 stability and deflections of the root tip due to surrounding particle forces. Therefore, critical root elongation forces define the ability of a root to remain mechanically stable, 330 and this ability is linked to the rigidity of the tissue and the distribution of particle 331 forces. 332

The emergence of theories for the prediction of critical elongation forces has been largely limited by the ability to characterise the mechanical environment of a growing root. Experimental systems using compression chambers of various sorts have been extensively used in the 1960's and later (Barley, 1962; Materechera *et al.*, 1991; Abdalla A *et al.*, 1969), but simultaneous measurements of particle forces were not

made. The first attempts of Whiteley and Dexter (1982) showed measuring the drag 338 force of a particle of known size and traction speed is possible but precise control of 339 particle displacement is not. More recently, research on the physics of granular media 340 has characterised interparticle mechanics using planar force sensors or computational 341 methods (Mueth et al., 1998; Hurley et al., 2016), but application of such techniques 342 within biological systems remains difficult. Use of photo-elastic materials has been 343 successful (Kolb et al., 2012; Wendell et al., 2012) but current materials do not allow 344 345 fabrication of realistic soil-like substrate, and for this reason, penetrometer resistance tests remain the preferred approach to characterise the resistance to root elongation 346 (Clark et al., 2003). Root responses to particle forces are equally difficult to monitor. 347 Particle displacements have been measured alongside root deflections in glass bead 348 substrates using tracking algorithms (Bengough et al., 2009). More recently X-ray 349 350 computed tomography has achieved similar results in 3D (Keyes et al., 2017). Deriving measurements of forces from such data is not currently possible because it 351 352 would require detection of the deformation of individual particles (Brodu *et al.*, 2015).

353 In this study we have addressed some of these challenges and characterised how root deflections occur in relation to the distribution of particle forces in the growth medium. 354 355 Our pressure chamber shares similarity with the system used by (Materechera *et al.*, 1991), but we additionally monitored 3D growth trajectories and measured 356 357 penetrometer resistance. More importantly, we have developed signal processing technologies to retrieve the wavelength and radius of root helices and to study the 358 359 frequency and magnitude of root deflections, e.g. using multiplane tracing and helical transform (Figure 2 A&B). Previously, few studies have utilised the variations 360 361 observed in penetration resistance. Geostatistical tools were used to analyse periodic variation in penetration resistance in relation to changes in soil structure (Grant et al., 362 1985; Hadas & Shmulewich, 1990), but none of these studies linked variations in 363 particle forces to growth trajectories and root responses to mechanical stress. 364

Theory for growth in confined soil environments. Using our experimental system,
it was possible to identify factors that heavily influence root responses to interactions
with soil particles.

Granular media appear to cause frequent deflections of the root trajectory. Growth
response to soil heterogeneity has been widely documented (Goss & Russell, 1980),

and can be commonly observed in the form of tortuous morphologies, for example in 370 compacted soil (Popova et al., 2016). Our results showed the presence of root 371 deflections appears to be independent of soil mechanical resistance and may prevail 372 in granular media. Deflections occur by bending at the root tip as observed on other 373 root species (Bizet et al., 2016), and it is predominantly the magnitude of deflection, 374 not the frequency, that is affected by soil confining pressure (Figure 5). The study was 375 376 limited to roots and particles within a narrow range of sizes. It is unclear how the 377 mechanisms described here translate across spatial scales. Root behaviours in finer or cohesive soils are notable. Arguably, some degree of homogenisation of particle forces 378 would apply (Kolb et al., 2017), but granular media are also known to exhibit 379 380 macroscopic behaviour such as arching or clustering (Delenne et al., 2004; Aranson & Tsimring, 2006). Therefore, root trajectories in these conditions may also exhibit 381 sequences of deflections that are similar to those observed in our study. 382

Root deflections are linked to a mechanical process controlled by the fluctuations of 383 384 particle forces acting at the root tip. We have characterised the nature of particle forces and found patterns that confirm this hypothesis. The distance between peak particle 385 forces (δ) is conserved across a range of confining pressures, and the tail of the 386 387 statistical distribution of particle forces experienced by a root is exponential, as is commonly found in granular media (Figure 3C, Radjai et al., 1998). Because the 388 389 distance between the sites of deflections is larger than δ and larger than the size of particles (Figure 5B), we conclude that in our experimental set-up, a root can often 390 displace soil particles axially, but that on rare occasions the growth trajectory is 391 deflected. Deflection also requires mechanical energy to bend the root and displace 392 particles laterally (Gordon et al., 1992), and therefore it is both the distribution of axial 393 394 and lateral particle forces that determine if a deflection will take place.

395 Root deflections are mechanically viscoelastic and anisotropic, and may be influenced 396 by gravitropism. Results show roots did not fully recover their shape following mechanical tests (Figure 4D). Also, there was time dependence of the apparent 397 Young's modulus determined experimentally from the model (Figure 6A). This 398 behaviour is typical of viscoelastic materials (Findley & Davis, 2013). Since the time 399 400 required to overcome a soil particle (between 9 and 14 minutes) exceeds the duration of mechanical testing, visco-elastic deformation must affect the nature of the 401 402 deflection. This is also consistent with the requirements for tissues to elongate

(Braidwood et al., 2014) and for fluids to move across cells (Nonami et al., 1997). We 403 observed the formation of helices with wavelengths similar to those observed during 404 the waving phenomenon observed at the surface of agar (Rutherford et al., 1998). The 405 curvature of helices is an order of magnitude smaller than the curvature at the sites of 406 a deflection and we conclude helical shapes are due to the combined anisotropy of the 407 tissue (Lloyd & Chan, 2002) and the frequency of deflections. Unlike what was 408 proposed by Silverberg et al. (2012), torsion pre-stress is not required for helices to 409 410 form.

We have formalised the conditions for the occurrence of a deflection. Our theory 411 predicts how roots respond to soil confining pressure in granular media, and it shows 412 that roots deflect at frequencies that are maintained across increasing levels of soil 413 confining pressure (Figure 5B). This is counterintuitive because the forces required to 414 415 displace soil particles are increasing too. However, root thickening and subsequent stiffening of the tissue (Materechera et al., 1991; Bengough et al., 2006) prevent the 416 417 increase in frequency of deflections. The thickening is not sufficient to limit the magnitude of deflections which, as predicted by the mechanics of embedded structures 418 (Mojdehi et al., 2016), results in shorter bending length and increased curvature 419 420 (Popova *et al.*, 2016).

Our theory also showed limitations. The mean field approximation used to establish 421 422 the critical particle force led to oversimplified predictions of distances between 423 deflections (Figure 6A). The model itself did not address either how the soil structure or the displacement of particles affects the stochasticity of forces. However, various 424 experimental and theoretical studies are now addressing these limitations. The 425 stochasticity of soil penetrometer resistance is now being linked to soil structure (Ruiz 426 et al., 2017). Theoretical work on snow mechanics has also successfully demonstrated 427 how understanding the microstructure of a granular media can lead to improved 428 429 predictions of forces applied on a penetrating structure (Schneebeli et al., 1999; Löwe & van Herwijnen, 2012). In the future, our theory could therefore be improved by 430 better accounting for variations in particle forces, and this could allow prediction of 431 root growth and morphology to be made directly from the knowledge of soil structure. 432

Root navigation through paths of least resistance in soil. Roots are known to
mobilise various sensing mechanisms in response to obstacles. For example, response

to touching an obstacle has been found to mobilise also gravity sensing (Massa & 435 Gilroy, 2003) and the root cap is believed to play a key role in the reorientation of the 436 tip. Skewing and waving patterns observed during growth on gels are also thought to 437 result from gravitropism and touch stimuli (Migliaccio & Piconese, 2001; Oliva & 438 Dunand, 2007). Similar mechanisms also prevail in the field where roots are known 439 for example to grow in macropores (Moran et al., 2000; White & Kirkegaard, 2010). 440 The phenomenon was recently found, for example, to compensate for the effects of 441 442 soil compaction (Colombi et al., 2017a).

In this study we found evidence that root responses to soil pressure results from 443 444 interactions taking place at the level of the soil particle. Helical shapes were formed 445 more consistently when roots deviated from verticality (Figure 6B), and this was due to gravitropic effects during deflections from particles. Simulations predicted smaller 446 447 asymmetry ratio than those measured experimentally (Figure 6B), which indicates that simulated root morphologies are more helical. This could be explained by 448 449 constraints imposed in the model on the direction of deflections. The model did not include biological responses linked to the anisotropy of the tissue either. For example, 450 we did not include changes in the mechanical properties of the tissue in response to 451 452 gravitropic stimulation. Such responses were not studied experimentally here, but work on Arabidopsis thaliana have shown that a number of biomechanical factors can 453 454 affect the waving mechanism observed in roots (Buer et al., 2003). Mechanical properties of root tissues are also known to vary in response to mechanical stresses 455 and consequently to confining pressure (Loades et al., 2013). 456

The conservation of the root deflection frequency also hints at a potential mechanism for growth through paths of least resistance in soil. Because deflections limit exposure to large particle forces, they reduce the overall resistance opposed to elongation. Deflections have also undesirable consequences on root foraging dynamics. For example, models predict that stochastic deflections result in a transition from a convective to a dispersive propagation through soil (Dupuy *et al.*, 2018), and a subsequent reduction in rooting depth.

The development of deep roots requires mechanical stability of elongating tissues.
Extreme pressures, deformations, or deflections of the root apex are known to affect
the cellular organisation of the meristem (Jackson *et al.*, 2017). In such conditions, the

467 developmental functions of the meristem may be affected, and the ability to explore 468 new regions of soil or access resources may become limited. Some control of the 469 morphological and structural properties of tissues in response to soil mechanical 470 properties must therefore prevail. The way sensing of and response to the 471 micromechanical environment operate, however, requires additional study.

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Figure 1. Experimental system for the study of root trajectories in response to soil 662 particle forces. A) Transparent Soils are used as soil analogue. Stained particles can 663 be used for visualisation and here also to quantify particle size distribution. The 664 histogram of particle size distribution (below) shows particles have an average 665 diameter of 1.07 mm ±0.32. B) Biomechanical analysis of root soil interactions is 666 based on three experiments. First the buckling of root tips in compression was 667 characterised on living root tips using a universal test frame (left). Measurements and 668 control of particle forces were obtained from plants growing in a cylindrical chamber 669 670 with the Transparent Soil maintained under controlled mechanical pressure using a piston fitted with a load cell (Methods S1). The transparent piston has a 3 mm opening 671 to (i) monitor changes in particle forces using a penetrometer needle (middle) and (ii) 672 to allow for emergence of the shoot (right). B) An optical projection tomography 673 system with two degrees of freedom (rotation and vertical translation) is used to image 674 675 the roots over large fields of view. The microscope assembles 720 projections of a root taken every 0.5 degree and at three depths. 676





Figure 2. Pipeline for mechanistic understanding of root growth trajectories. A) The 678 morphology of the root is characterised using a 3D image processing pipeline. (left) 679 680 projection data are assembled by stitching followed by 3D reconstruction using the filtered back projection algorithm. A coarse representation of the centreline is first 681 obtained using automated tracing (centre) and fine mapping of the root centreline is 682 683 then obtained using multiplane tracing (right). B) Signal processing tools were developed to mine for local deflection of the root and detect helical waveforms. Here 684 685 the root trajectory is projected in the XZ (top) and YZ (middle). The helical transform then provides the power spectrum of spatial frequency of the helical waveforms 686 687 (bottom). The curve in red indicates the dominant wavelength waveform extracted by the study. A theory is also developed to understand root responses to soil particle 688 689 forces. C) The theory considers two response modes. First, the root may overcome the resistance F of the particle resisting straight elongation (left). When F reaches a critical 690 value, bending $\langle M \rangle$ and lateral displacement of particles $\langle F \rangle$ offer less resistance and 691 692 a deflection occurs. D) Because a root has inherent helical anisotropy (principal axis of rotation as blue arrows, minor axis of rotations shown as red arrows), deflection 693 694 occurs in the 3-dimensional space where two directions of deflections of least resistance V_1 and V_2 are equally probable. The sense of direction of the deflection is 695 696 then determined by other biological factors.



Figure 3. Granular physics of Transparent Soil. A) Variation in the force F(N) resisted 698 699 by a penetrometer cone of similar size to a root (1.72 mm diameter) for different levels of confining pressure and measured at depths between 20 mm and 30 mm. The forces 700 have been normalized by the averaged force $\langle F \rangle$ obtained over a travelled distance of 701 702 20 mm. The averaged force increases with confining pressure P. The markers indicate 703 local maxima of the forces at different confining pressure (red triangle 0 kPa, green circle 25 kPa and blue square 50 kPa). To avoid sensitivity to sensor noise, only 704 705 maxima that are absolute on a neighbourhood of 30 µm are identified. B) Probability density distribution of the forces (red triangle 0 kPa, green circle 25 kPa and blue 706 square 50 kPa). C) Tail of the probability distribution of particle forces shows 707 exponential decline, where $F_{75\%}$ is the third quartile. D) Probability density 708 distribution of the distance between identified of forces F (markers in A) with red 709 triangle 0 kPa, green circle 25 kPa and blue square 50 kPa. 710



713 Figure 4. A) Lentil seedlings grown at increasing levels of confining pressure (from left). Typical centrelines (black curves) of roots grown under increased confining 714 715 pressure (right). The horizontal X-Y coordinates are multiplied by 4 to enhance visibility. Markers indicate the sites of local maxima in root curvature and red lines 716 show the dominant helix obtained by helical transform. B) The power spectrum of the 717 helical transform from roots grown at respectively 0 kPa (red), 25 kPa (green) and 50 718 kPa (blue) shows helices can be both clockwise and anti-clockwise. C) Radius of the 719 helical waveforms is influenced by the pressure from the soil respectively (same 720 colour code as above) but the wavelength $\tilde{\lambda}$ is conserved at approximately 13 mm of 721 722 root length. D) Root deformations in response to compression forces and buckling also exhibit helical patterns. The wavelength of the helix observed in these roots (12 mm) 723 724 closely matched those grown in soil and is shown in cyan in figure (C) as a vertical line and a surrounding shadow indicating the confidence interval. 725



728 Figure 5. Development in granular media induces microscale deflections of the growth trajectory. A) The profile of root curvature along the root (shaded area) shows that the 729 overall growth trajectory of the root is dominated by a sequence of local changes in 730 direction. The sites of deflections (markers) have high curvature with comparison to 731 the expected curvature from the global helix (vertical lines). B) The frequency of 732 deflections expressed as the distribution of the distance between the sites of two 733 consecutive deflections. The frequency follows an approximate uniform distribution 734 and is not influenced by soil confining pressure. C) The curvature at the site of the 735 deflection is increased with the soil confining pressure. Observations made with a 736 737 Confocal Laser Scanning Microscope shows localised bending of the root, here under 738 25 kPa and 50 kPa (bottom left, scale bar 500 µm). Red, green, and blue markers indicate confining pressures of the Transparent Soil, respectively 0 kPa, 25 kPa and 739 740 50 kPa.



Figure 6. Predictions of root responses to particle forces. A) The theory predicts 743 occurrence and magnitude of deflections, linking the distribution of root curvatures 744 (top) and the frequency of occurrence of deflections (middle) to critical particle force, 745 particle size and mean particle force. Suitable prediction can only be achieved with 746 747 relaxation of the root stiffness with time, here modelled with the Kelvin Voigt viscoelastic model (bottom). Experimental data is plotted with dotted lines and 748 theoretical predictions are plotted with plain lines. Red, green, and blue markers 749 indicate confining pressures of respectively 0 kPa, 25 kPa and 50 kPa. B) Experiments 750 and simulations showed gravitropic response is also required to obtain realistic 3-751 752 dimensional root trajectories, with both helical transform analysis (top) and visualisation (bottom) showing the effect of gravitropism in the formation of helices. 753 Experimental data (black) shows the asymmetry ratio is influenced by deviation from 754 verticality which confirms the role of gravitropism in the formation of helical patterns. 755 Simulations of trajectory with random deflection ($q_2=0.5$, red) leads to large deviation 756 757 from verticality and do not form dominant helical waveforms. When the sense of 758 rotation is fixed ($q_2=1$, green), helical patterns are formed but deviations from verticality are observed. When root deflection is gravitropic (equation 11, blue) helices 759 760 are formed with switches from clockwise to anticlockwise rotations. Plain lines were 761 obtained by linear regression and shaded areas indicate the prediction intervals.