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## Dip coating with colloids and evaporation.

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**Abstract:** We investigate the coating of a glass plate with silica colloids by a dip coating method in presence of evaporation. We show experimentally that the deposed quantity plotted versus plate velocity V exhibit a minimum, in agreement with a simple argument developed by us in a previous, theoretical paper. This minimum corresponds to a crossover between the well-known Landau-Levich regime observed at higher plate velocity and a less well-known regime at lower plate velocity where the deposit is formed directly at the contact line. This very general result is consistent with experiments and calculations made by other teams with different compounds or under different wetting geometries. Modifying our initial argument by taking into account the particle density gradient, we show that a simple modelling of each regime in terms of scaling laws is possible, the deposed mean thickness scaling respectively as  $V^{-1}$  and  $V^{2/3}$  in the lower and higher velocity limits, which is consistent with our data and with available literature.

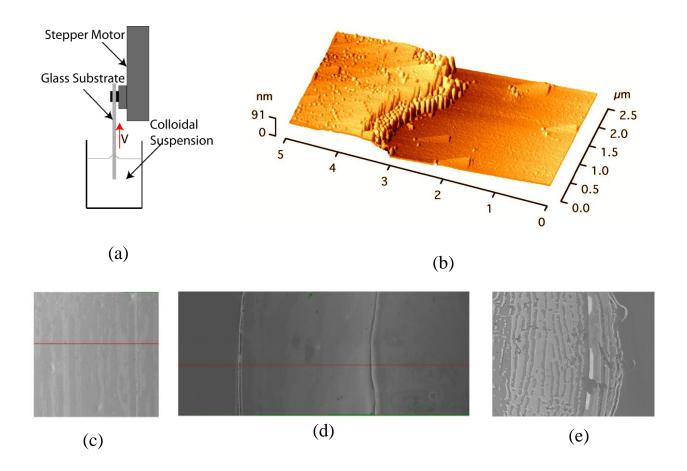
Keywords: coating, colloids, moving contact line, wetting and evaporation, drying.

## 1 – Introduction

There is a growing interest in coating hard and soft substrates with colloids, because of numerous applications to optics and microelectronics [1-2]. A possibility to realize these substrates is to use dip coating under evaporation [3], i.e. to remove at constant speed a plate from a bath of colloidal suspension while drying occurs. This leads to several undesired effects: defects, heterogeneous deposition, cracks and delamination [1,4]. The problem is also difficult to model as three singularities may coexist at the contact line (CL) receding on the substrate [5-6] (and even in a advancing case [6]) : (1) divergence of viscous stresses, (2) divergence of evaporation as in the well known "coffee stain" effect [8-10], (3) and divergence of colloid concentration.

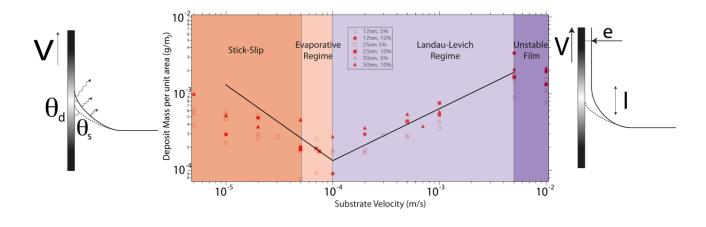
In a recent paper we modelled the hydrodynamics in the vicinity of a moving, evaporating, contact line [5], and we found that there should exist two different regimes at respectively low and high plate velocity, in which the deposed mean thickness e should respectively decrease and increase with the plate velocity V. This should lead to a minimum of the deposit thickness for a critical intermediate velocity. If we except a very recent study performed with complex compounds on silicium substrates [11], this effect has been scarcely evidenced in a dip coating experiment with colloids, though similar behaviours were found for deposition of phospholipids [12], and in a rather specific two-plate geometry (meniscus receding in a Hele-Shaw cell) [13-14].

We present here evidences in favour of this effect in the case of silica colloids deposited on glass from water solutions with dip coating [6]. Our experimental conditions are described in section 2, and the results presented in section 3. To summarize, we found that the deposition is perturbed by complex behaviours (stick-slip and instability) that strongly alter the uniformity of the deposit, but despite this additional complexity the two predicted regimes indeed appear with this minimum of deposed thickness at their crossover. In section 4, we reconsider our qualitative modelling of ref. [5], including the effect initially neglected of the particle concentration gradient. We show that this additional term modifies the predictions in the limit of low plate velocity, for which the deposed thickness scales as  $e \sim V^{-1}$  instead of  $e \sim V^{-2}$  (as initially suggested in [5-6]), while in the limit of high velocity one finds  $e \sim V^{2/3}$  as expected from the classical Landau-Levich film entrainment description. These predictions are in good agreement with our data and with others obtained on different systems [11-16]. Let us note here that the  $V^{-1}$  law has been proposed very early by Dimitrov and Nagayama [15] and rediscovered later independently by Diao and Xia [16], and by Jing et al. [14] who interpreted it on the basis of a balance of solvent at the scale of the meniscus. As we shall see both arguments (our's and the solvent balance at the meniscus level) are equivalent, the interest of our approach being that scaling laws are also provided for the spatial dependency of particle concentration during deposition. This could allow one to build future extensions to situations involving several independent length scales, or to prepare further experimental investigations of these spatial effects with - for instance - fluorescent microscopy.



**Fig. 1**: (a) Experimental set up. (b) A typical AFM visualization of the deposit. (c-e): deposit left on the plate after drying, observed by optical profilometry, for increasing plate velocity: (a) V=50  $\mu$ m/s, (b) V=1 mm/s, (c) V=5 cm/s. The motion of the plate took place along the horizontal direction. The suspension concentration was equal to 10%, and the particle size (not visible here) was equal to 50 nm. The horizontal scale of these pictures is respectively equal to 1.5 mm, 8 mm and 1.5 mm (total extent of the pictures).

#### 2 – Experimental conditions.

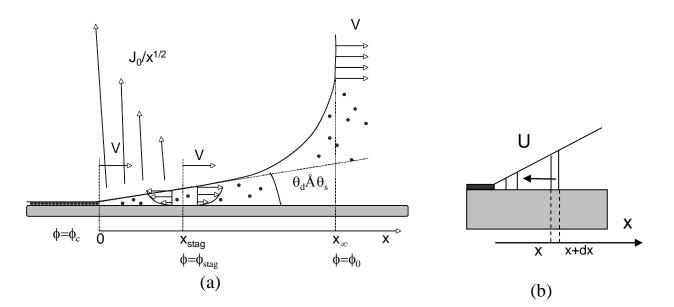
A sketch of the experimental set-up is suggested on Fig.(1-a). A clean glass plate is plunged inside a colloidal suspension and removed from this bath at constant speed (*V* ranging between 50  $\mu$ m/s and 5 cm/s), while deposition and evaporation takes place on the glass. We used silica suspensions (Klebosol silica slurries 50R50, 30R25 and 30R12) with three different particle diameters (*12 nm*, 25 nm and 50 nm), and two different volume concentrations ( $\phi_0$ =5% and 10%). The glass plate is cleaned and prepared before each experiment by the following protocol. First the glass surface is rub with an abrasive cerium oxide suspension (concentration 20%), cleaned with pure water, ethanol, and again pure water, and then let to dry. A plasma treatment is then imposed to the glass. After drying completion, the deposit has been observed with an atomic force microscopy (AFM), and by optical profilometry. 

**Fig. 2**: Mean thickness of silica colloids deposed on a glass plate by dip coating. Roughly, two regimes of deposition appear, the one on the right being linked to the entrainment of a landau-Levich film at high plate velocity, the other on the left with deposition and evaporation directly at the contact line (the continuous lines, of respective slope -1 and 2/3 are guides for the eyes).

A typical example of an AFM visualisation is reproduced on Fig. (1-b), and several views with optical profilometry on Figs.(1-c) to (1-e). The particles are deposed in a random way, with many defects at small scale, and the spatial distribution at large scale is also scarcely uniform, perturbed by a disordered patterning linked to stick-slip and instabilities of the contact line.

#### – Experimental results.

Most of our investigations were performed with optical profilometry, which has the advantage to provide a deposit cartography at large scale. Typical "maps" obtained with this method, are reproduced on Figs. (1-c) to (1-e) for increasing plate velocities. At low velocity (Fig. 1-c), the deposit is perturbed by a stick-slip effect, similar to the one observed by Rio et al [7] or Ghosh et al. [17] respectively for advancing and receding contact lines of colloidal suspensions, or to the one identified between two plates by Bodiguel et al. [13]. At intermediate velocities (Fig. 1-d), the deposit is reasonably uniform, before to be again perturbed by film flow instabilities at high plate velocity (Fig. 1-e) of unknown origin. We have measured the mean thickness of the deposit, using these profilometry records, versus plate velocity for the different particle sizes and concentrations. While this methods gives us a first idea of the shape of the deposit it has two significant drawbacks: a reference point is needed (i.e. we need to have naked glass on the image to have a reliable measurement) and the field of view is limited to a few millimetres (while the coated surface of the substrates were 15cm x 8cm). These two combined constraints leads to measurements in the vicinity of the initial contact line, where transitional regimes are most likely to happen. We then relied on a more averaged methods consisting on weighing the substrates before and after the experiment. The results are displayed too on Fig. 2, where two distinct regimes separated by a minimum of the thickness are clearly visible, in good agreement with our theory [5-6].



**Fig. 3**: (a) Sketch of the low velocity problem in the framework of the plate, treated here as static, the liquid receding to the right. (b) During its motion towards contact line, the volume of a slide of liquid is changing because of evaporation, which introduces a change of particle concentration.

The continuous lines on the same figures are guide for the eyes of slope -1 and 2/3. Clearly, the behaviour at high velocity is in agreement with the exponent 2/3 deduced in [5] from Landau-Levich result, while things are less obvious at low velocity, but clearly indicate a continuous decrease of thickness with V. Note also the existence in each of the two domains of two more specific zones : just between the stick-slip region and the minimum of thickness there seems to exist a narrow region of deposition ("Evaporative regime"), in which the mean deposit thickness still decreases but without spatial modulations, and at large substrate velocity the thick film entrained by the plate undergoes complex instabilities which perturb the deposit distribution ("Unstable film").

## 3 – Theoretical discussion.

We now remind the physical origin of the two very different behaviours, suggested by the two sketches on the same figure, and provide the reader with a qualitative modelling of both regimes. In the higher velocity range, the plate entrains a continuous film of liquid out of the bath, that dries later on the whole extent of the plate. As well known from available literature [3], the thickness of the liquid film *e* is equal to that calculated long ago by Landau, Levich and Derjaguin, and should scale as  $e \propto l_c C_a^{2/3}$  where  $Ca = \eta V/\gamma$  designates the Capillary Number built upon liquid viscosity  $\eta$ , plate velocity V, surface tension  $\gamma$ , and where  $l_c = \sqrt{\gamma/(\rho g)}$  is the capillary length (g acceleration of gravity,  $\rho$  mass density of the liquid). During drying, the volume fraction occupied by the particles in the liquid increases from the initial volume fraction  $\phi_0$  to a critical value close to the maximal packing concentration  $\phi_c$ , which implies that the deposit thickness should scale as

$$e_{HV} \propto \frac{\phi_0}{\phi_c} l_c \left(\frac{\eta V}{\gamma}\right)^{2/3} \tag{1}$$

in the limit of high velocities. As said above, a line of slope 2/3 has been indicated on the Log-Log plot of Fig. 2. As one can check, this slope is consistent with the obtained data. At low velocity (see the sketch on Fig. 3-a), the situation is very different. There is now a contact line, from which the deposit directly emerges, evaporation being now mainly localized at the contact line itself. Following Deegan et al. [8-9], the evaporating flux diverges there, following a law of the kind (see Fig. 3-a):

$$J = J_0 / x^{1/2} \tag{2}$$

where  $J_0$  can be estimated here by noting that at the scale of the meniscus size  $x_{\infty}$ , the mean evaporating velocity should be given by:

$$\frac{J_0}{\sqrt{x_\infty}} \propto \frac{D}{x_\infty} \frac{c_{sat}}{\rho_w}$$
(3)

where *D* is the diffusivity of water in air,  $c_{sat}$  the saturation mass concentration of water vapour in air, supposed to be reached at the free surface of the liquid (and to vanish at infinity), and  $\rho_w$  the mass density of water. In the framework attached to the plate, the liquid motion should obey the following mass conservation equation:

$$-V\frac{\partial h}{\partial x} + \frac{\partial}{\partial x}\left[h < u_x > \right] = -\frac{J_0}{\sqrt{x}} \tag{4}$$

where  $\langle u_x \rangle$  designates the mean velocity averaged on the liquid thickness h(x), given in the lubrication approximation by:  $\langle u_x \rangle = -(h^2/3\eta)(\partial P/\partial x)$ , with  $P = P_{atm} - \gamma (\partial^2 h/\partial x^2)$ ,  $P_{atm}$  being the reference atmospheric pressure. Integrating one time this equation leads to a mean velocity

$$\langle u_x \rangle = V - \frac{J_0}{2h(x)}\sqrt{x} \tag{5}$$

that exhibits a stagnation surface located at a distance of the contact line equal to:

$$x_{stag} = \left(\frac{J_0}{2\theta_d V}\right)^2 \tag{6}$$

where  $\theta_d$  is the dynamic contact angle, supposed to be rather close to the static angle  $\theta_s$  in this low velocity limit. The structure of the flow is suggested on Fig. 3-a. For scales x<x<sub>stag</sub> evaporation drives everything to the contact line, and in particular all the colloids trapped in this region. We thus guess that  $x_{stag}$  will play the role of a capture length ruling the thickness deposited on the plate in the low velocity limit  $e_{LV}$ . To estimate

it, a balance of solute can be written as follows: the plate is withdrawing from the liquid a volume per unit of length and unit of time of solute equal to  $Ve_{LV}\phi_c$ , while the stagnation surface crosses a volume of solute equal to  $V\theta_S x_{stag}\phi_{stag}$  where  $\phi_{stag}$  is the colloid concentration that holds at the stagnation line. If, as in ref. [5] one identifies  $\phi_{stag}$  to the colloid concentration  $\phi$  that holds in the bulk of the liquid, this balance leads finally to a deposit thickness that reads [5]:

$$e_{LV} \propto \frac{\phi}{\phi_c} \frac{J_0^2}{4\theta_s V^2} \tag{7}$$

As anounced at the begining of the present paper, unlike  $e_{HV}$  this thickness *decreases* with the plate velocity, which, combined to (1) leeds indead to a minimum of the deposed thickness. This description is enough to explain our results, but if one looks more carefully to the data at low velocity on Fig.2, the exponent predicted by this model (equal here to 2) overestimates the observed decrease of  $e_{LV}$  upon V, an exponent close to 1 (suggested by the line added to the graph) would be more reasonable. This observation is consistent with results obtained with other compounds by Faustini [11], Le Berre [12] and Jing et al. [13], the three groups reporting an exponent close to 1. This presumably results from the too rough nature of the approximate  $\phi_{stag} \approx \phi$  used above. Obviously, the concentration of solute increases as the liquid becomes closer and closer to the contact line. A simple scaling argument can be built on a slide of liquid, of thickness dx (see Fig. 3-b), moving inside a wedge of angle  $\theta_S$ , at a velocity U towards the contact line, and whose variation of volume per unit length of contact line reads:

$$\delta[hdx] = -\theta U \delta t - \theta x \frac{\partial U}{\partial x} \delta t = -\theta \delta t \frac{\partial (xU)}{\partial x}$$
(8)

After combining this with the estimated velocity of the liquid close to contact line,  $U \approx J_0/(2\theta\sqrt{x})$ , one is led to the conclusion that the slide volume scales as  $\sqrt{x(t)}$ , and thus that the particle concentration near contact line should in turn scale as:

$$\phi(x) = \phi_0 \sqrt{\frac{x_\infty}{x}} \tag{9}$$

where the concentration  $\phi_0$  holds at the scale of the meniscus (matching with the bulk of the reservoir). Using this expression in the estimate of  $\phi_{stag} \approx \phi_0 (x_{\alpha}/x_{stag})^{1/2}$  leads finally to the following law ruling the "true"  $e_{LV}$ :

$$e_{LV} \propto \frac{\phi_0}{\phi_c} \frac{J_0}{\sqrt{x_\infty}} \frac{x_\infty}{V}$$
(10)

in which the new exponent -1, smaller than the previous value -2 is in better agreement with all available data [6-16]. Note that this expression, as noticed by Doumenc [13], can be reached independently by a balance of solute at the level of the whole meniscus: while the meniscus deposits on the plate of volume of the coated film equal to  $Ve_{LV}\phi_c dt$ , there is, at the scale of the whole meniscus, a volume of solvant that

evaporates equal to  $x_{\infty} (J_0 / \sqrt{x_{\infty}}) dt$ , and which creates an excess of solute of quantity  $\phi_0 x_{\infty} (J_0 / \sqrt{x_{\infty}}) dt$ . Balancing this excess of particles with the quantity deposited on the plate leads directly to (10).

### 4 – Conclusion.

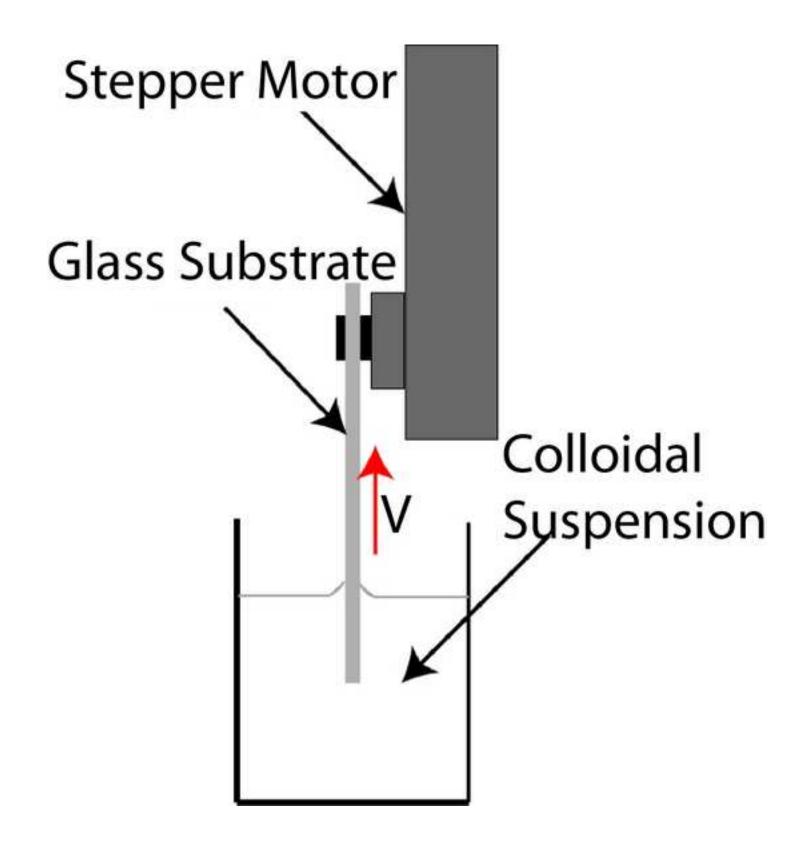
In summary, we have checked experimentaly with silica particles deposed on glass our prediction proposed in [5] of the existence of a minimal thickness of colloids deposited on a plate by dip coating, and corrected our model by including the increase of colloid concentration when the liquid reaches the vicinity of the contact line in the low velocity limit. We insist on the fact that this simple approach avoids any use of complicated partial differential equations, and allows one to get a simple understanding of the mechanisms at play here. The behavior that we found, experimentally as well as by a simple modeling, is in agreement with the observations of other groups on different systems [11-13], and with their own interpretations. It would be interesting to explore experimentally in more details the spatial distribution of colloid concentration in the liquid near the deposition front, to see to what extent a scaling law of the kind (9) could hold. To our knowledge, this has never been done and we are perhaps the first to propose this law. Also, it would be interesting to relate the present transition with the classical Landau-Levich threshold of film entrainment [18], and to see if evaporation and deposition introduces a completely different phenomenon, or simply shifts this threshold, for instance via modifications of the reference contact angle due to evaporation [5].

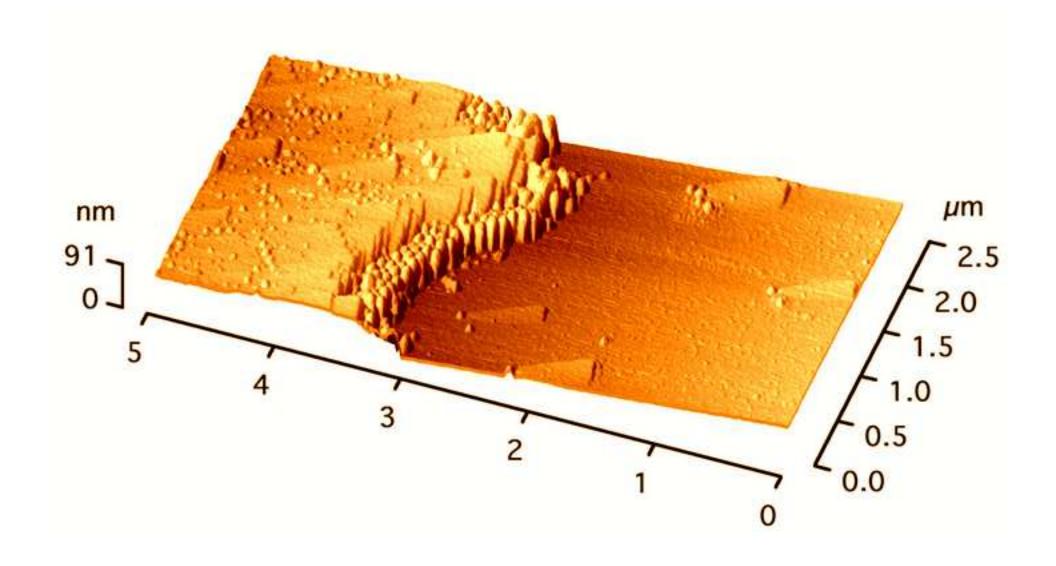
**Aknowledgments:** We are indebted to discussions with C.-T. Pham, H. Bodiguel, F. Doumenc and B. Guerrier. One of us (G.B.) has benefited from a DGA grant, and this work has been supported by the ANR funding DEPSEC.

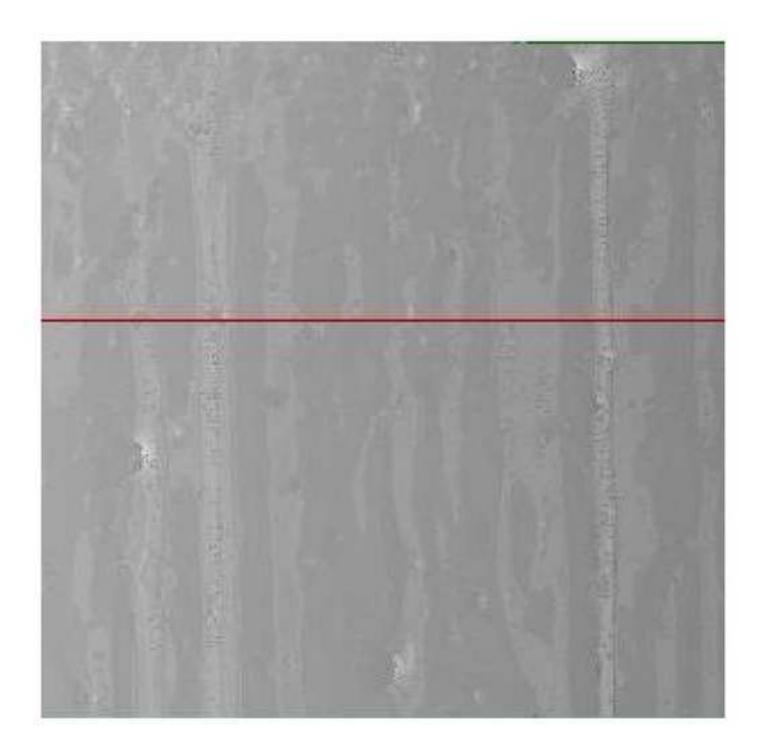
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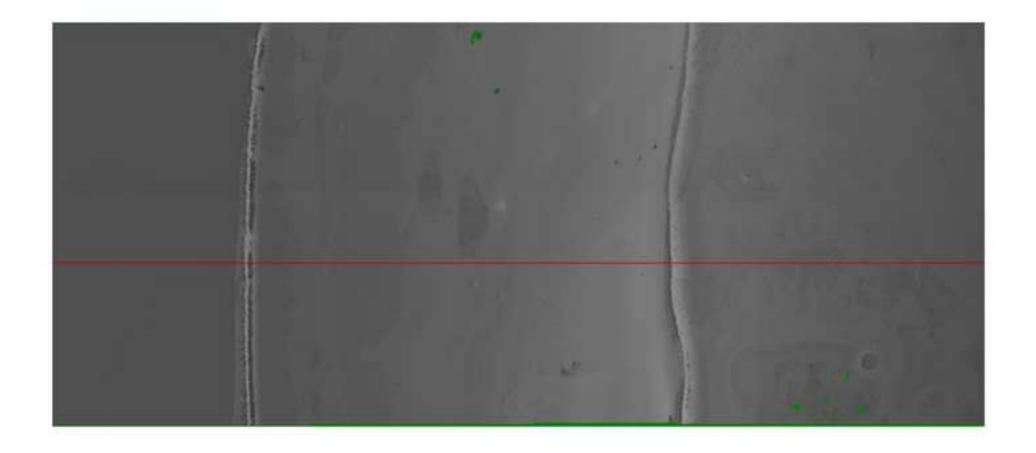
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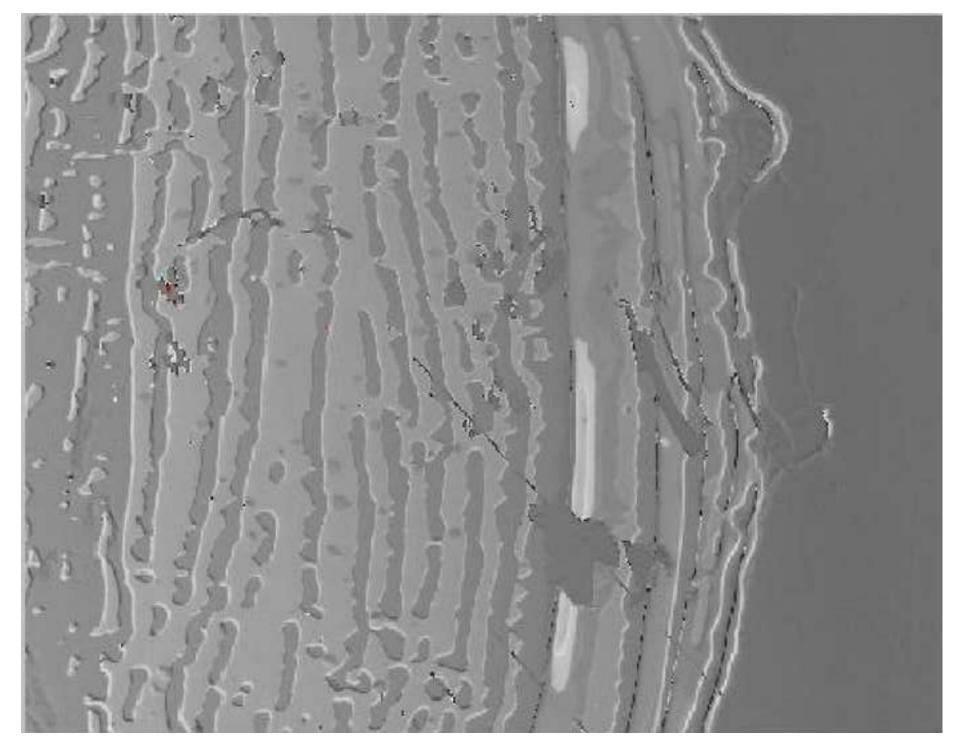
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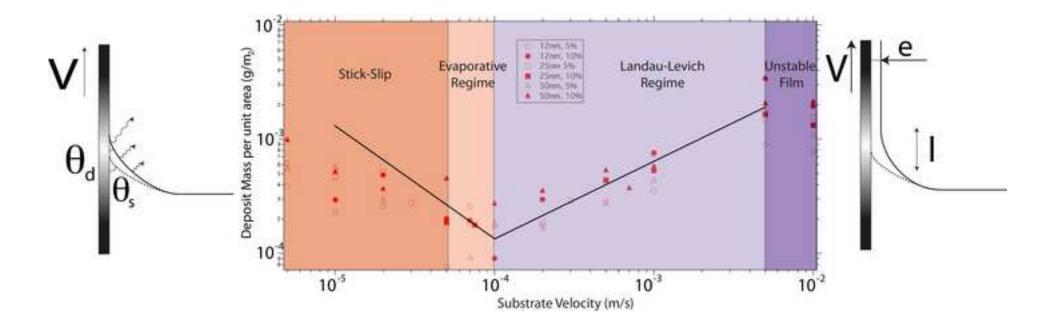












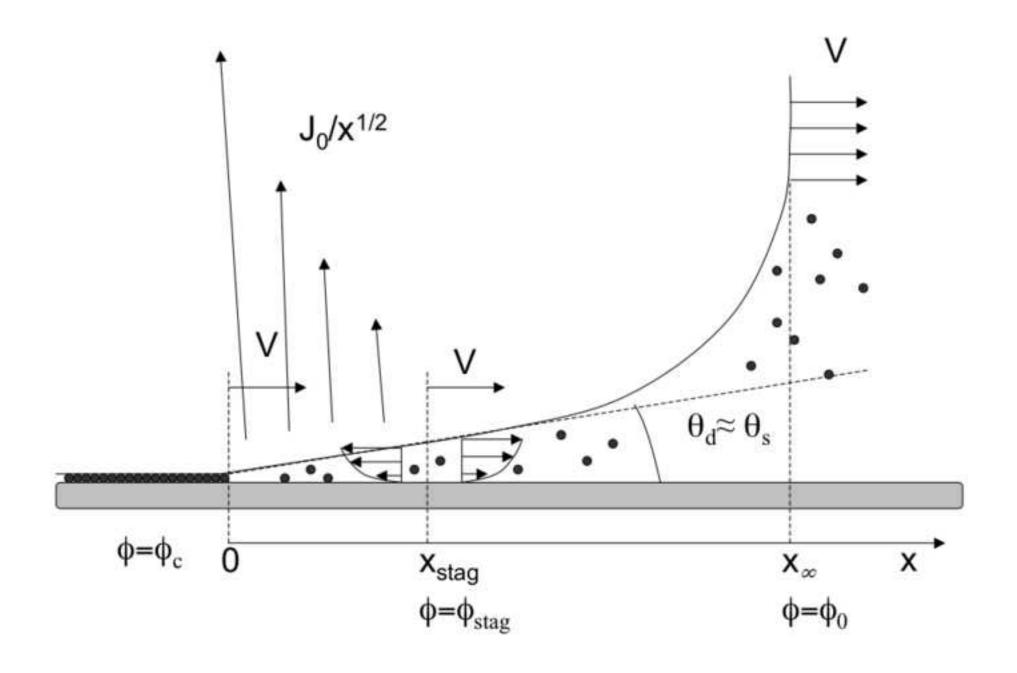


Figure 3-b Click here to download high resolution image

