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Models of interacting supernovae and their spectral diversity

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ABSTRACT

Using radiation hydrodynamics and radiative transfer simulations, we explore the origin of the spectral diversity of interacting supernovae (SNe) of Type II_n. We revisit SN 1994W and investigate the dynamical configurations that can give rise to spectra with narrow lines at all times. We find that a standard $\sim 10 M_{\odot} 10^{51}$ erg SN ejecta ramming into a $0.4 M_{\odot}$ dense circumstellar material is inadequate for SN 1994W, as it leads to the appearance of broad lines at late times. This structure, however, generates spectra that exhibit the key morphological changes seen in SN 1998S. For SN 1994W, we consider a completely different configuration, which involves the interaction at a large radius of a low-mass inner shell with a high-mass outer shell. Such a structure may arise in an 8–12 M_{\odot} star from a nuclear flash (e.g. of Ne) followed within a few years by core collapse. Our simulations show that the large mass of the outer shell leads to the complete braking of the inner shell material, the formation of a slow dense shell, and the powering of a luminous SN II_n, even for a low inner shell energy. Early on, our model line profiles are typical of SNe II_n, exhibiting narrow cores and broad electron-scattering wings. As observed in SN 1994W, they also remain narrow at late times. Our SN 1994W model invokes two low-energy ejections, both atypical of observed massive stars, and illustrates the diversity of configurations leading to SNe II_n. These results also highlight the importance of spectra to constrain the dynamical properties and understand the origin of SNe II_n.

Key words: hydrodynamics – radiative transfer – supernovae: general – supernovae: individual: 1994W – supernovae: individual: 1998S – supernovae: individual: 2011ht.

1 INTRODUCTION

Interacting supernovae (SNe) exhibit a wide range of radiative properties, covering extremes that include both superluminous events and ‘impostors’. This diversity of bolometric displays reflects variations in the power source, and in the context of interacting SNe, this is controlled by the outer shell mass and the inner shell energy (we will loosely refer to the outer shell as circumstellar material, CSM). More perplexing is the diversity of spectra associated with interacting SNe. Multidimensional effects acting both on small scale (e.g. to produce clumping) and large scale (e.g. an asymmetric CSM) may play a role. However, a large variation of both inner and outer shell properties in spherically symmetric interactions can alone produce a wealth of peculiar spectral signatures. Multiple regions are likely to contribute simultaneously to the escaping radiation, including the unshocked cool CSM, the ionized unshocked CSM, the interacting region between the reverse and the forward shocks (which contains both shocked CSM and shocked ejecta material,

and bounds the cold dense shell, CDS), as well as the inner ejecta in homologous expansion. These distinct regions generally have different temperatures, density, velocity, and they may also possess a different composition. Because of the evolving structure of the interaction, the emitting regions at early times may be very distinct from those that contribute at late times. Consequently, one expects significant spectral evolution from SNe II_n.

Interacting SNe are notoriously known for their spectral line profiles which exhibit narrow cores and broad wings. This is the specific signature seen at early times when the SN is discovered and the classification as II_n stems from that observation alone (Dopita et al. 1984; Niemela, Ruiz & Phillips 1985; Schlegel 1990). A few well known and recent examples are SN 1998S (Fassia et al. 2000; Leonard et al. 2000), SN 1994W (Sollerman, Cumming & Lundqvist 1998), SN 2006tf (Smith et al. 2008), SN 2009kn (Kankare et al. 2012), SN 2010jl (Stoll et al. 2011; Zhang et al. 2012), or SN 2011ht (Humphreys et al. 2012; Roming et al. 2012; Mauerhan et al. 2013). This special line profile morphology is controlled by the low velocity of the CSM which gives rise to the narrow component, and by scattering with thermal electrons. In SNe II_n the

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importance of electron scattering as a line broadening mechanism is enhanced by the large electron scattering optical depth, the larger Sobolev lengths (since the velocities are smaller), and the smaller bulk velocities which can be smaller than the characteristic speed of thermal electrons (of the order of $550 \sqrt{T/10^4 \text{ K}} \text{ km s}^{-1}$).¹ Modelling of this process in the SN context gives support to this interpretation (Chugai 2001; Dessart et al. 2009).

However, the relative spectral uniformity of SNe IIn (with line profiles showing narrow cores and broad symmetric wings) holds only at early times. Eventually their spectra start showing very diverse line profiles, in some cases unique. So far, the modelling of SNe IIn spectra has been focused on the early epochs when the spectra show the distinct ‘IIn’ signature. But to build a consistent picture of interacting SNe it is crucial to understand the entire evolution, from early to late times. As we discuss here, the late-time line profiles offer key constraints, not available at early times when the optical depth is large and frequency redistribution through electron scattering is strong.

Here, we focus on the behaviour of line-profile widths after maximum light and demonstrate how line-profile morphology can be used to distinguish interacting models, thereby lifting the degeneracy inherent to SN light curves. Specifically, we want to understand what distinguishes events like SN 1998S or SN 2010jl, which show broad emission lines at late times – and in particular $H\alpha$, from events like SNe 1994W, 2009kn, or 2011ht which show narrow line profiles that become systematically narrower with time.

This issue emerged in Dessart et al. (2009) when modelling SN 1994W. Although our models were not based on hydrodynamical simulations, we reproduced the spectral evolution of the event by invoking slow emitting material at *all times* and we noted the remarkable absence of broad lines. This suggested that while fast material may have been present early on, it must have been quickly decelerated to a low velocity, or that this fast material was somehow dark (i.e. had a low emissivity), or that at all times all emission from the fast-moving material was reprocessed by the slowly moving CSM (i.e. because of an optical depth effect).

In the model proposed by Chugai et al. (2004), a SN ejecta of $7\text{--}12 M_{\odot}$ rams into a $0.4 M_{\odot}$ extended shell, producing a light curve similar to SN 1994W. In this model, the energy/momentum is stored primarily in the inner shell. The moderate deceleration of the inner shell by the outer shell leads to a moderate luminosity boost compared to standard non-interacting SNe. It also leads to the formation of a CDS moving at $\sim 4000 \text{ km s}^{-1}$, which implies that a lot of fast moving material survives the interaction with the CSM. In contrast, the model of Chugai et al. (2004) predicts an $H\alpha$ line width of the order of 1000 km s^{-1} throughout the high-brightness phase of SN 1994W, including late times when the CSM optical depth in their model is below unity. This result is surprising, because their hydrodynamical model predicts a fast moving CDS: photons emitted from the CDS are Doppler shifted and this should eventually become noticeable in the emerging radiation as Doppler-broadened line profiles. Doppler-broadened profiles are seen (and explained) at late times in some SNe IIn, for example 2010jl (Dessart, Audit & Hillier 2015), so this mechanism is not unexpected in interacting SNe.

Since SN 1994W was discovered, other SNe have been identified with similar properties, in particular SN 2009kn (Kankare et al.

2012) and SN 2011ht (Humphreys et al. 2012; Roming et al. 2012; Mauerhan et al. 2013). SN 2011A seems to be analogous to these events too (de Jaeger et al. 2015). A separate SN IIn-P classification has been proposed for these events (Mauerhan et al. 2013). Here, we wish to explore what hydrodynamical configurations can produce this distinct class of events. Besides modelling light curves, which offer ambiguous constraints when used alone, we also study the spectral evolution of our radiation hydrodynamical models. We use the same numerical approach as in Dessart et al. (2015) for the study of superluminous interacting SNe like SN 2010jl. Starting from various initial configurations, we perform multigroup radiation hydrodynamics simulations of the interaction between an inner shell and an outer shell. We then post-process these radiation hydrodynamical simulations (reading off the radius, velocity, temperature, and density of the simulated domain at a given epoch) with the non-local thermodynamic equilibrium (nLTE) code `CMFGEN`. As in Dessart et al. (2015), the radiative transfer works for an arbitrary velocity field and can therefore retain the complex dynamical properties of the interaction region. Because the simulation with `CMFGEN` assumes steady state, we repeat the calculation for multiple epochs to capture the spectral evolution of the interacting SN model.

In the next section we provide a brief summary of the numerical procedure, in particular the small improvements over the approach presented in Dessart et al. (2015). In Section 3, we give the sources of observational data we use, as well as the adopted distance, reddening, and explosion time. In Section 4, we start by revisiting the model of Chugai et al. (2004), which involves an energetic massive inner shell ramming into a low-mass extended CSM. We show how that model is more suitable to explain events like SN 1998S. We then present, in Section 5, a grid of simulations in which we vary the inner and outer shell properties to identify a configuration compatible with the observations of SN 1994W. In Section 6, we propose a scenario for SN 1994W. It involves an energetic low-mass inner shell that is much less massive than the slow moving massive outer shell. The reversed mass balance between inner/outer shells gives rise to a number of interesting properties that can help explain the light curve and spectra of events like SN 1994W. As discussed by Woosley & Heger (2015), various aspects of this scenario may be encountered in the final stages of evolution of $9\text{--}11 M_{\odot}$ stars.

While we were finalizing this paper and preparing for submission, a study of SN 2011ht by Chugai (2015) came out. His approach is very different from ours but our respective conclusions agree – the simulations and results presented here have been obtained over the past year and our conclusions have not been influenced by Chugai (2015).

2 NUMERICAL APPROACH

The simulations presented in this paper are performed with a variety of numerical tools, including `HERACLES` (González, Audit & Huynh 2007; Vaytet et al. 2011), `MESA` (Paxton et al. 2011, 2013, 2015), `VLD` (Livne 1993; Dessart, Livne & Waldman 2010a,b), and `CMFGEN` (Hillier & Miller 1998; Dessart & Hillier 2005, 2008, 2010; Hillier & Dessart 2012).

`HERACLES` is a Eulerian multidimensional radiation hydrodynamics code (González et al. 2007), with the possibility for multigroup radiation transport (Vaytet et al. 2011). The hydrodynamics is treated using a standard second-order Godunov scheme. For the radiation transfer, the multigroup M1 moment model (Dubroca & Feugeas 1999) is used. In all `HERACLES` simulations, we adopt a uniform H-rich composition suitable for the study of SNe IIn. In practice, we use an H mass fraction of 0.633, He

¹ Spectral line broadening by thermal electrons is seen not just in SNe, but also in partially ionized dense slowly moving outflows of stars (e.g. η Car; Hillier et al. 2001).

mass fraction of 0.36564, and an iron mass fraction of 0.00136. Instead of assuming an ideal gas, we use a general equation of state that accounts for the contributions from atoms, ions, and electrons, including the contribution from ionization energy. We have done comparison tests with simulations that adopt an ideal gas equation of state and we find small differences only, probably because the shocked low-density plasmas studied here are radiation dominated – the thermal energy is a small fraction of the energies (radiation or kinetic) involved. Thermodynamic quantities (energy, pressure, sound speed, heat capacity, temperature) are tabulated in density–temperature and density–energy space for convenient use in HERACLES. As in Dessart et al. (2015), we supply the code with an opacity table for our adopted composition. We compute our opacities as a function of density, temperature, and energy group. Energy groups are positioned at strategic locations to capture the strong variation in absorptive opacity with wavelength. We use one group for the entire Lyman continuum (including the X-ray range), two groups for the Balmer continuum, two for the Paschen continuum, and three groups for the Brackett continuum and beyond.

Our HERACLES simulations are 1D and use a uniform radial grid with 1200–2400 cells (more grid cells are employed when the radial coverage is larger). Such a resolution is sufficient to model adequately the overall dynamics and energetics of the interaction and study the spectral properties with CMFGEN.²

The initial configuration of the interaction is produced in various ways. In all cases, we consider interactions between two shells at large distances – the junction between the inner and outer shells is far beyond the initial radius of the progenitor star, and typically in the range $0.2\text{--}1.8 \times 10^{15}$ cm. The parameter space is large so other configurations will be considered later.

The internal energy budget at the onset of interaction will differ whether we consider eruptions/explosions from blue supergiant (BSG) or red supergiant (RSG) stars because of the different magnitude of expansion cooling. In Dessart et al. (2015), we ignored such considerations because we focused on superluminous SNe IIn, events in which the power released by the interaction completely overwhelms the internal energy of the inner and outer shells at the onset of interaction. This may no longer hold when considering SNe IIn with a luminosity closer to non-interacting SNe. As we ignore any radiation from the system emitted prior to the onset of interaction our results underestimate the true luminosity from the system at early times. This matters if one is concerned with the quantitative aspects of the problem; here we are more focused on understanding the fundamental qualitative differences between SNe IIn. One can recall for example the strong offset in bolometric light curve between SN 1994W and SN 2011ht, while the two events show a similar spectral evolution.

In practice, we use two different approaches for the initial set-up. The first one, also used in Dessart et al. (2015), is simplistic since we set analytically the values for the fluid quantities (our choices are guided by simulations of core collapse SNe; e.g. Dessart & Hillier 2011). This approach is used in Section 4. One drawback is that we have to guess the initial temperature. If the outer shell arises from a pre-SN wind located at large distances, its age is old, and

its temperature is low – how low is irrelevant and we just adopt our floor temperature of 2000 K. If the outer shell arises instead from a recent ejection, the temperature may still be high, i.e. well above the recombination temperature of hydrogen. Further, the structure of the outer shell may also be significantly affected by radiation arising from the inner shell emitted prior to the onset of interaction. For the inner shell, a proper account of the ejecta energy/temperature is relevant because the interaction may start when the ejecta is still hot and optically thick.

In Sections 5 and 6, we use a more physical approach for the initial set-up. We prepare initial conditions for the HERACLES simulations using MESA (Paxton et al. 2011, 2013, 2015) and v1D (Livne 1993; Dessart et al. 2010a,b). In practice, we evolve a massive star from the main sequence until the BSG phase, the RSG phase, or until core collapse. We then trigger an explosion/eruption as desired, by depositing a prescribed energy at a prescribed radius/mass cut and on a very small time-scale. We then let the resulting ejecta evolve until it reaches the desired radius for our interaction set-up. The approach is still artificial in the sense that we do not model the explosion mechanism, but given that trigger, the model is energetically and dynamically consistent.

In the present simulations, we ignore ⁵⁶Ni and any contribution from radioactive decay, so that radiation originates from the release of internal (i.e. primarily radiation) energy originally present in the inner/outer shell and from direct (or re-processed) emission from the shock.

To post-process the HERACLES simulations, we perform steady state nLTE radiative transfer simulations with CMFGEN, with allowance for arbitrary velocity fields. At multiple epochs, we remap the radius, velocity, temperature, and density computed by HERACLES for a wide range of interaction configurations and solve for the radiative transfer by holding the temperature fixed. The rate equations are solved using the Sobolev approximation. More quantitative calculations will require the inclusion of line blanketing, and the adoption a more realistic nLTE cooling function in the hydrodynamic simulations. The assumption of steady state in CMFGEN implies that we ignore the light-travel time to the outer boundary and any explicit delay associated with optical depth effects. However, because CMFGEN uses the temperature structure from HERACLES, time delays associated with the diffusion of radiation through the optically thick ejecta/CSM are taken into account. Because HERACLES explicitly allows for time dependence, there is an inherent time offset, of the order of a few days around bolometric maximum, between the escaping radiation at a given time in HERACLES and its computation with CMFGEN based on the HERACLES snapshot at that time.

In contrast to Dessart et al. (2015), we employ a more complex model atom, including H I, He I, He II, C I–C III, N I–III, O I, O II, Na I, Si II, Ca II, Sc II, Ti II, and Fe II–V. We use a modest number of levels for each atom/ion (comparable to the simulations reported in Dessart & Hillier 2011) because our focus is on the spectral evolution – we search for signatures of the interaction dynamics on the H α profile morphology so that the exact magnitude of line blanketing, for example, does not need to be known accurately for our purposes.

3 OBSERVATIONAL DATA

We compare our models to SN 1994W, SN 1998S, and SN 2001ht.

For SN 1994W, the photometry is from Sollerman et al. (1998), combined with spectra from Chugai et al. (2004). We use a distance

² With a higher resolution, we resolve better the velocity jumps, for example associated with the weak reverse shock. The Zeldovich spike ahead of the forward shock also peaks at a higher temperature. But the global energetics (e.g. the bolometric light curve, the conversion efficiency) and dynamics (shock propagation speed) are only weakly altered. See Dessart et al. (2015) for discussion.

of 25.4 Mpc, a reddening $E(B - V) = 0.15$ mag, and adopt the same time reference (i.e. 1994 July 14) as in Sollerman et al. (1998).

For SN 2011ht, the photometry is from Roming et al. (2012). We use a distance of 19.2 Mpc, neglect reddening, and use JD 245 5833.0 for the time origin (Roming et al. 2012).

For SN 1998S, the photometry is from Fassia et al. (2000), and the spectra are from Fassia et al. (2001) and Leonard et al. (2000). We use a distance of 17.0 Mpc, a reddening $E(B - V) = 0.22$ mag, and adopt the same time reference (i.e. JD 245 0875.2) as in Fassia et al. (2000).

4 MODEL A: A MASSIVE ENERGETIC EJECTA RAMMING INTO A $0.4 M_{\odot}$ EXTENDED CSM

In this first section, we discuss our model A, which corresponds to an interaction configuration similar to that proposed for SN 1994W by Chugai et al. (2004).

4.1 Interaction configuration

The inner shell is massive ($\sim 10 M_{\odot}$) and energetic (10^{51} erg kinetic energy), quite typical of a standard Type II SN ejecta. The outer shell is assumed to have formed through a wind, with a mass-loss rate of $0.1 M_{\odot} \text{ yr}^{-1}$ which lasted 3.5 yr and abated ~ 3 yr before the inner shell exploded. With a speed of 100 km s^{-1} , it stretches from 1.0 to 2.1×10^{15} cm. Beyond that (in the outer CSM region produced before the phase of intense mass loss), the density drops by four orders of magnitude. At the onset of interaction, the inner shell

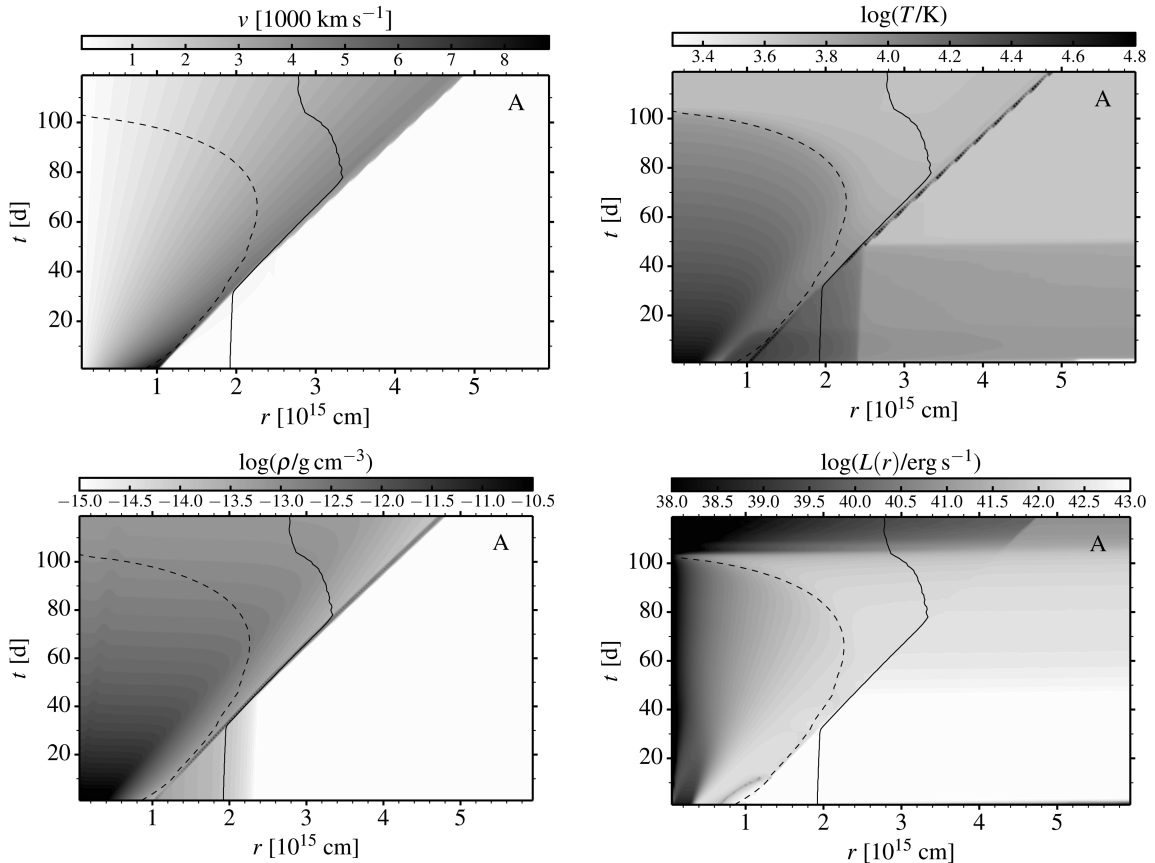


Figure 1. Grey-scale images showing the velocity, temperature, density, and local luminosity versus radius and time, as computed by HERACLES for model A. The solid line traces the photosphere (we refer here to the location where the electron scattering optical depth integrated inwards from r_{max} is equal to $2/3$) and the dashed line the location where the optical depth is 10 (for both quantities, we use the opacity from electron scattering only).

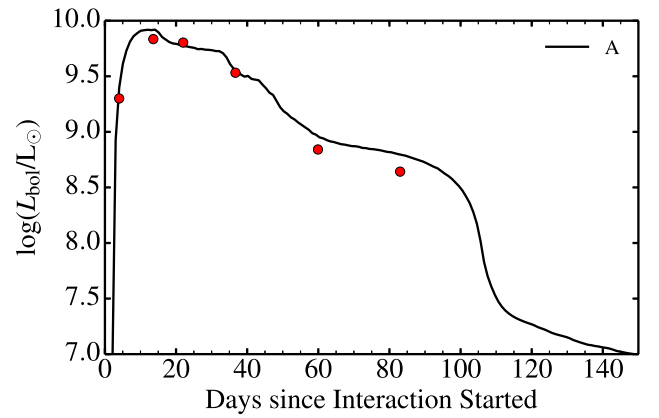


Figure 2. Bolometric light curve for model A. The dots correspond to the luminosity computed at a few epochs with CMFGEN.

age is ~ 12.0 d. A figure showing the initial configuration of this interaction is given in Appendix A (Fig. A1).

4.2 Dynamical properties

The evolution of the properties of the radiation hydrodynamics simulations of model A with HERACLES is shown in three sets of illustrations. Fig. 1 shows grey-scale images of the velocity, temperature, density, and radiative luminosity versus radius and time. Fig. 2 shows the HERACLES bolometric light curve for model A (the

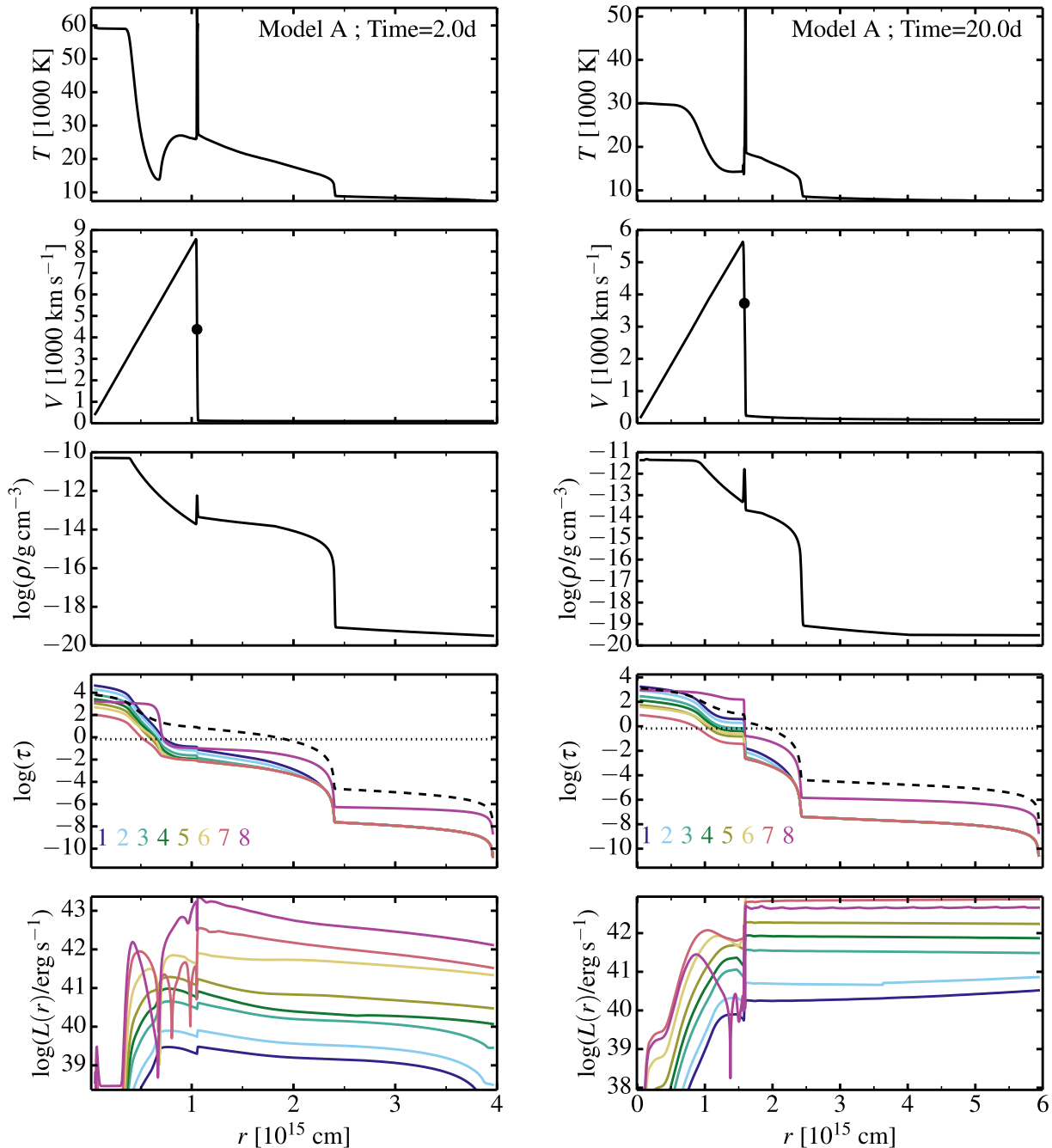


Figure 3. Left: properties of the interaction model A computed with HERACLES at 2.0 d after the start of the interaction. We show the gas temperature, the velocity (the dot corresponds to the velocity of the CDS), the mass density, the optical depth, and the radiative luminosity versus radius. For the optical depth panel, we show that quantity for each energy group (coloured line; the group energy increases with the group number; see Section 2 for details) and for electron scattering (dashed line) – the dotted line corresponds to an optical depth of $2/3$. At this time, the CSM is optically thick. The photosphere is located at $\sim 2.0 \times 10^{15}$ cm. The bolometric luminosity is rising to maximum as radiation diffuses through the CSM. Right: same as left, but now at 20.0 d after the onset of the interaction. The CSM is still optically thick but the CDS is closer to the photosphere.

dots correspond to the luminosity computed at various epochs with CMFGEN – see Section 4.3). Figs 3 and 4 show results from the HERACLES simulation at selected epochs. Each figure contains five panels illustrating the gas temperature, the velocity, the mass density, the optical depth, and the radiative luminosity versus radius.

The early evolution is quite typical of interacting SNe (Chugai et al. 2004; Moriya et al. 2013; Whalen et al. 2013; Dessart et al. 2015). The initial shock luminosity gives rise to a burst of radiation

at the ejecta/CSM interface, which propagates through the cold and dense CSM on a free-flight time. Radiation raises the ionization of the CSM, enhancing its electron scattering optical depth. By 2.0 d after the onset of the interaction, the CSM is optically thick out to $\lesssim 2.0 \times 10^{15}$ cm (this is where the electron scattering optical depth integrated inwards from r_{\max} is equal to $2/3$ – we define this location as the photosphere), and the total CSM electron scattering optical depth is of the order of 10 (these different regions are clearly

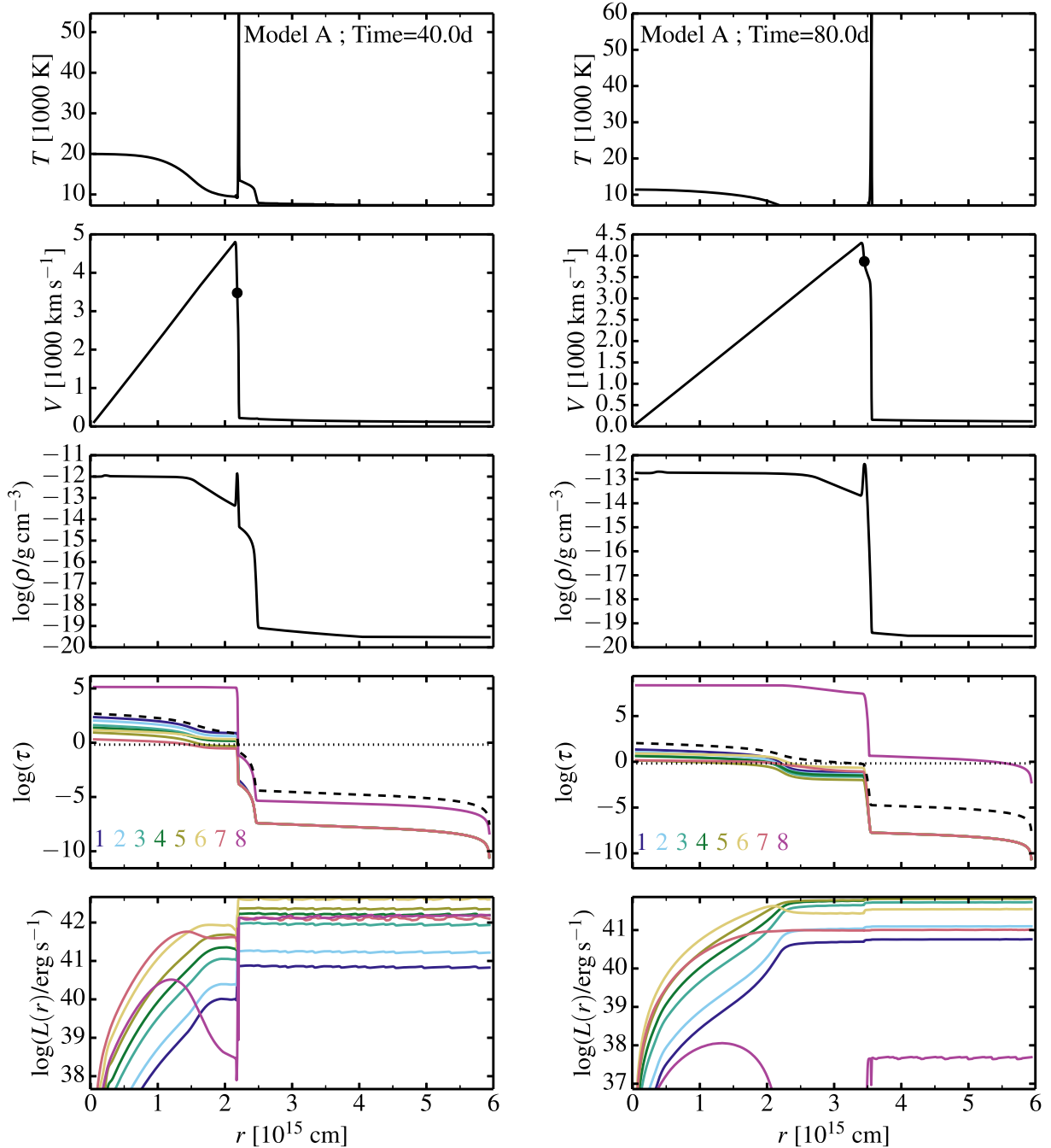


Figure 4. Left: same as for Fig. 3, but now at 40.0 d after the onset of the interaction. The photosphere is now within the CDS – the CSM above the CDS is optically thin. Right: same as left, but now at 80.0 d after the onset of the interaction. The CDS is becoming optically thin and the bulk of the radiation stems from the optically thick ejecta located at smaller radii.

identified in Fig. 1). Subsequently, radiation injected at the shock has to diffuse through the CSM. The emergent bolometric luminosity thus rises to maximum after about a diffusion time of 10 d, and then drops. A dense shell has formed and contains about 5 per cent of the swept-up CSM mass (left-hand column of Fig. 3).

At 20.0 d after the onset of interaction (right-hand column of Fig. 3), the ejecta/CSM interface has reached $\sim 1.6 \times 10^{15}$ cm. This shocked region is bounded by a reverse shock and a forward shock and is confined within a CDS of about 15 000 K, significantly cooler than the temperature spike just exterior to the CDS (at 50 000 K). This CDS is moving at ~ 3500 km s $^{-1}$. In contrast, the photosphere

has essentially not moved because it resides in the slowly moving CSM, but the CDS is now much closer to that photosphere. Indeed, the CSM electron scattering optical depth (between the photosphere and the CDS) is only of a few. All the energy is emitted from the CDS region so that the luminosity is constant beyond it, in particular between the CDS and the photosphere.

At 40.0 d after the onset of the interaction (left-hand column of Fig. 4), the CDS has reached $\sim 2.1 \times 10^{15}$ cm and has overtaken the former location of the photosphere within the CSM. The photosphere is at that time within the CDS. Its temperature is about 10 000 K, and it is characterized by a very steep density profile. For

an external observer, the SN would look like a radiating sphere with no extension, i.e. with a very sharp edge. Up until that time, the luminosity of all energy groups shows a pronounced jump across the CDS, implying that the bulk of the radiation emerges from the CDS – the emitting region is moving outwards with a typical velocity of 3500 km s^{-1} .

At 80.0 d after the onset of the interaction (right-hand column of Fig. 4), the CDS has reached $\sim 3.5 \times 10^{15} \text{ cm}$ and is progressing unimpeded through the low-density outer CSM. Its speed has remained essentially constant throughout and is of the order of 3500 km s^{-1} . The CDS is now cooler, with a temperature of $\sim 6000 \text{ K}$, and its electron scattering optical depth is $\lesssim 1$. The CDS is optically thick to Lyman continuum photons but is transparent to Balmer continuum photons. From 50 to 60 d onwards, the luminosity shows only a modest jump across the CDS, implying that the bulk of the radiation now comes from the inner ejecta, which has not taken part (and will not take part) in the interaction. These emitting layers are moving at a few 1000 km s^{-1} .

The bolometric light curve therefore shows two distinct phases (Fig. 2). The first phase, up until about 40–50 d, is dominated by the interaction as the shock is making its way through the dense CSM. During this phase, the CDS is optically thick. After that, the bolometric luminosity comes from the CDS as well as the inner ejecta, which is no longer obscured. This second phase corresponds to the plateau light curve that this model would have had in the absence of the interaction³ – the contribution from the CDS and the interaction during that second phase is modest (it depends on the wind mass-loss rate for the outer CSM, which is chosen here to be small).

4.3 Spectral evolution

The second part of our study is to post-process these HERACLES simulations with CMFGEN, following the procedure discussed in Dessart et al. (2015) and outlined in Section 2. We choose representative epochs. We compute CMFGEN models at 2.0 d (CDS hardly formed, CSM optically thick, source of radiation deeply embedded within this CSM), at 11.6 d (around maximum light; CSM still optically thick), at 20.0 and 34.7 d (as the CDS gets close to the photosphere located at $2.1 \times 10^{15} \text{ cm}$), and at 57.9 and 81.0 d (when the bulk of the radiation comes from ‘unshocked’ ejecta, below the CDS; CSM optically thin). Great care is taken when remapping the HERACLES model on to the CMFGEN grid to resolve the strong variations in density, temperature, and velocity of the dynamical model.

The resulting spectral evolution is shown in the top panel of Fig. 5. The first two epochs show the typical IIn spectral morphology. Line profiles are centred at the rest wavelength. They show a strong and narrow central peak with extended wings. The line broadening mechanism is dominated by electron scattering (Chugai 2001; Dessart et al. 2009). This is well understood since the bulk of the radiation is injected deep within the CSM. The slow expansion of the CSM in this model (100 km s^{-1}) is much smaller than the electron thermal speed of $\sim 500 \text{ km s}^{-1}$, and its optical depth of about 10 makes electron scattering an important process for frequency redistribution. The spectra are quite blue at those epochs, with lines of He I and H I primarily. There is also a large number of very narrow lines, primarily from Fe II, which are formed in the cool part of the

unshocked CSM. This is a clear signature that the spectrum forms in two distinct regions, one hot and partially ionized (associated with H I and He I lines in particular), and the other cool and recombined (associated with very narrow lines of H I or Fe II).

However, the spectra do not retain this IIn morphology long. At 20.0 and 34.7 d, the IIn signature is gone and we observe instead line profiles with blueshifted absorption and weak emission. The bulk of the radiation is now coming from the outer edge of the fast moving optically thick CDS, which has a steep density profile. The emission part of the line is therefore dwarfed and the absorption is blueshifted. The CDS temperature is still of the order of $10\,000 \text{ K}$, so He I lines continue to be seen (primarily as blueshifted absorption). As for previous epochs, narrow H I and Fe II lines are predicted.

At the last two epochs shown in Fig. 5, the morphology has drastically changed. The spectra are now analogous to SNe II-P during the late plateau phase, but H α and the Ca II triplet at 8500 \AA show strong and broad emission with weak or no associated absorption.⁴ We are now seeing a hybrid source of emission, with a dominant contribution from the inner ejecta and a more modest contribution from the more optically thin CDS. The dense and fast CDS contributes most notably through strong and broad H α and Ca II emission, with little associated absorption. It is emission from the CDS that fills in the inner ejecta absorption associated with H α and Ca II (Figs B3 and B4).

To facilitate the line identification we have calculated synthetic spectra with selected species excluded from the calculation, and then coloured the offset between the resulting flux and the total flux (top panel of Fig. 5). This exercise reveals the dominance of H I and He I at early times (up until epoch 34.7 d) when the spectrum is relatively blue (e.g. there is a large flux shortward of the Balmer edge). As the colour temperature drops and the material recombines in the spectrum formation region, lines of Ti II, Sc II, and Fe II appear and strengthen. The drastic evolution in line profile shapes, especially for H α , is evident. We also note the presence of Si II 6347–6371 \AA . This doublet is present at 34.7 d as two weak absorptions, displaced from rest wavelength by $\sim 2500 \text{ km s}^{-1}$. At the next two epochs, this Si II doublet appears as one broad and strong absorption, with its maximum still around -2500 km s^{-1} from rest wavelength.

The left-hand panel of Fig. 6 shows the H α region at multiple epochs spanning the high-brightness phase of model A (same epochs as for Fig. 5), in both velocity (bottom x-axis) and wavelength (top x-axis) space. It illustrates the narrow-core broad-wing symmetric line-profile shape at early times (2.0 and 11.6 d); the transition to a P-Cygni profile with weak emission and little sign of broadening from electron scattering (20.0 and 34.7 d); the appearance of a blueshifted and strong emission line, dominated by Doppler broadening (57.9 and 81.0 d). The emission blueshift decreases as the CDS optical depth drops (Dessart et al. 2015). The first four spectra show the clear presence of narrow components in H α and He I 6678 \AA , which arise from the cool unshocked slow ($\sim 100 \text{ km s}^{-1}$) CSM – these features are absent at later times because the dense part of the CSM has been completely swept up by the fast-moving CDS (the only slow CSM left has a very low density in our set-up – see Fig. A1).

³ As noted earlier we have ignored the energy contribution arising from radioactive decay, and this may affect the light curve.

⁴ At late times, a treatment of the radiative transfer with time-dependent terms would probably yield a stronger H α line, both in absorption and emission (Utrobin & Chugai 2005; Dessart & Hillier 2008).

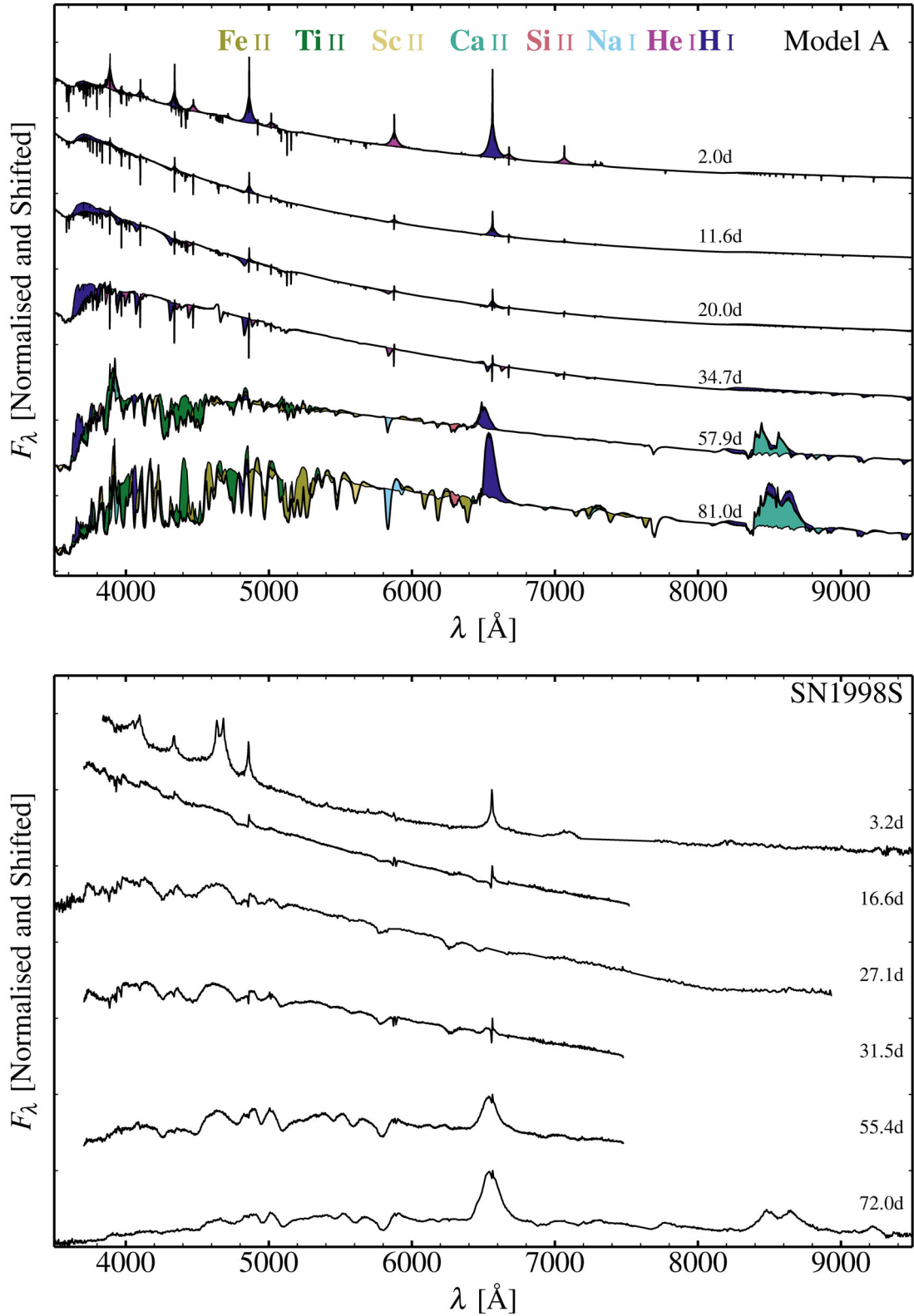


Figure 5. Top: multi-epoch spectra for model A during the high-brightness phase (time is since the onset of interaction). Bottom: multi-epoch spectra of SN 1998S (corrected for redshift but not for extinction) covering the early phase with narrow lines and broad wings (3.2 d), pure absorption spectrum (16.6, 27.1, and 31.5 d), absorption spectrum with strong and broad emission lines (55.4 and 72.0 d). The axis range for the top and bottom panels is the same so one can compare the models and observations line by line.

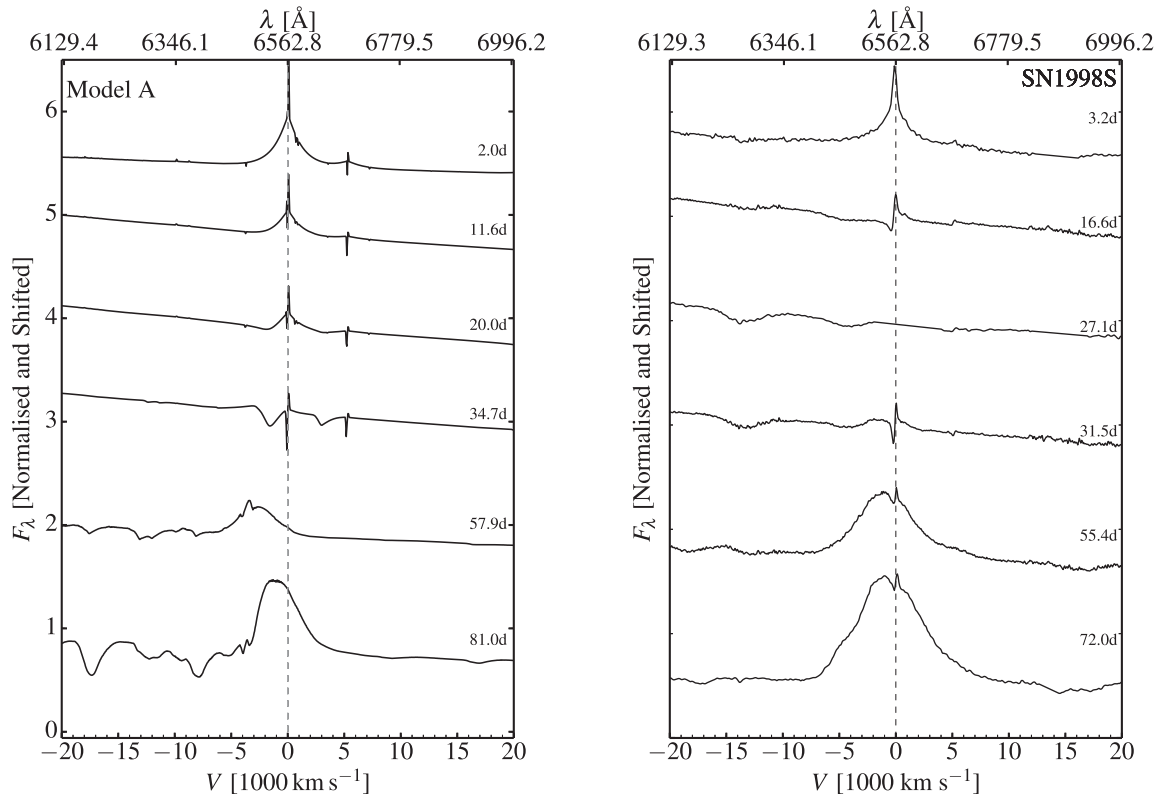


Figure 6. On the left we illustrate multi-epoch H α spectra for model A during the high-brightness phase where the time is measured relative to the onset of interaction. On the right we show data for SN 1998S. Notice the drastic evolution in the profiles of H α , and the striking qualitative similarity in the temporal evolution for the model and SN 1998S.

In the appendix, we provide additional figures describing the origin of the flux versus wavelength and radius, and at multiple epochs (Figs B1–B4). Viewed this way in two-dimensional space, one gets a better sense of the complicated spectrum formation process, with the distinct contribution each region makes to the emergent light.

4.4 Comparison to observations

In Fig. 2, we showed the bolometric luminosity computed by CMFGEN at multiple epochs (dots). There is a good agreement between the results from HERACLES and CMFGEN despite the different numerics and physics of each code. We can therefore use the CMFGEN models to compute the V-band magnitude and compare to observations.

Fig. 7 shows the good agreement between model A and the observed V-band light curve of SN 1994W, as also found by Chugai et al. (2004). This is expected since the interaction configuration of our model A corresponds to the model of Chugai et al. (2004), and our predictions for the dynamics and energetics of that model are comparable to theirs.

But spectroscopically, model A is not compatible with the multi-epoch spectral observations of SN1994W. While model A shows narrow lines at early times, when the II η morphology prevails, it evolves to a broad line spectrum at later epochs during the high-brightness phase. In contrast, SN 1994W shows line profiles that are initially narrow and become increasingly narrower as time progresses (Chugai et al. 2004).

Interestingly, model A reproduces the evolution of SN 1998S. Model A matches roughly the V-band light curve of SN 1998S

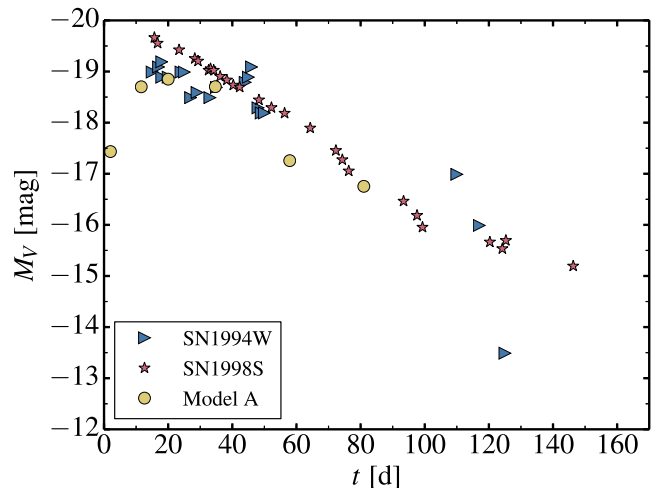


Figure 7. Absolute V-band light curve for SN 1994W and SN 1998S compared to our model A. See Section 3 for details on the source of observations, distances, reddening, and inferred time of explosion. For the model, the time is given with respect to the onset of interaction.

(Fig. 7) – SN 1998S and SN 1994W have comparable light curves.⁵ But more importantly, model A reproduces the overall spectral

⁵ The ambiguous information conveyed by light curves in this case is striking because SN 1998S and SN 1994W have a completely different spectral evolution.

evolution of SN 1998S (compare the two panels in Fig. 5), as well as the morphological changes in the line profiles (e.g. for H α ; Fig. 6).

In our model A the absorptions blueward of H α are due to Fe II and Si II (see above). In the observations of SN 1998S, a sizeable dip in the spectrum coincides with the location of Si II in our model (see also Leonard et al. 2000; Fassia et al. 2001) – the feature is not caused by high-velocity H α absorption.⁶

Quantitatively, model A shows some offsets with the observations of SN 1998S. The model light curve is too faint initially, but this could be remedied by adjusting the location of the CSM (closer to the progenitor star, as in Shivvers et al. 2015) as well as accounting for the ejecta radiation released since shock break out (we only start accounting for radiative losses at the onset of the interaction). The model light curve is also too faint at late times, but this could be remedied by adopting a higher mass-loss rate for the distant CSM (or invoking some power from radioactive decay). So, both offsets could be cured by simple adjustments to the adopted interaction configuration.

Spectroscopically, there are also some discrepancies. The earliest spectrum of SN 1998S shows lines of more ionized species than predicted in our models. This should be cured by moving the CSM closer to the exploding star, as in Shivvers et al. (2015). Indeed, given a radiation energy δE_{rad} stored in the optically thick CSM volume V the gas temperature (which equates roughly the radiation temperature) will scale as $(\delta E_{\text{rad}}/aV)^{1/4}$. So, the closer the interaction site is to the progenitor surface, the higher the CSM temperature and ionization, all else being the same. In the future, we will design a more suitable model to match the observed properties of SN 1998S, by adjusting the velocity and density structure of the adopted CSM, as well as the properties of the underlying ejecta (in the absence of interaction, SN 1998S would have been a II-L, not a II-P).

These discrepancies are merely small quantitative offsets and we conclude that the model of Chugai et al. (2004), or our model A, is more suitable to explain events like SN 1998S. The fundamental conflict between this model and the observations of SN1994W is that it systematically leads to the production of broad lines at late times, something that we already emphasized, without proof, in Dessart et al. (2009).

In their modelling of H α for SN 1994W, Chugai et al. (2004) adopted free expansion for the CSM with a value of 1100 km s^{-1} at $5.4 \times 10^{15} \text{ cm}$ (any emission occurring at smaller radii arises from slower regions). They do not seem to consider emission from the fast moving CDS at $\sim 3500 \text{ km s}^{-1}$ (all emission seems to arise from within the slow moving CSM) and the strongly non-monotonic velocity structure of this configuration. This likely explains the origin of the relatively narrow H α profiles they produce, even at 89 d when the CSM optical depth is merely 0.54. At such a low optical depth, the CSM material cannot efficiently absorb and re-emit the photons arising from the CDS. In our simulations, we include the whole system (i.e. unshocked ejecta, shocked ejecta, shocked CSM, unshocked CSM), and find that the contribution from the ejecta and/or CDS eventually dominates in this configuration when the CSM optical depth drops below a few. The associated signature is

⁶ The fundamental impact of interaction is the deceleration of fast material. Any fast material from the SN ejecta piles up in the CDS (and the fastest material is the first to disappear). The fastest material emitting/absorbing H α photons is tied to the CDS and it thus carries a maximum Doppler shift corresponding to the CDS velocity.

the production of broad lines at late times. Such broad lines are seen at late times in SN 1998S. For the same physical reason, they are seen (and explained) in SN 2010jl (Dessart et al. 2015).

5 GRID OF MODELS WITH DIFFERENT INNER/OUTER SHELL MASS AND ENERGY

To determine the key inner/outer shell properties that influence the light curves and spectra of interacting SNe, we perform a grid of simulations. One important goal of these simulations is to identify configurations that can produce bright displays even for low CDS velocities, since we anticipate this type of configuration is warranted for SNe like 1994W (Dessart et al. 2009).

5.1 Interaction configurations

For the inner shell, we consider explosions taking place in BSG and RSG stars. For the outer shell, we consider a dense CSM produced by wind mass loss. Because expansion cooling has a stronger effect in more compact stars, ejecta from BSG star explosions will be cooler than their RSG counterparts when they reach a distance of $\sim 10^{15} \text{ cm}$ (this is a rough estimate of the interaction radius for SN 1994W). So, to start with a suitable ejecta temperature for the inner shell, we construct BSG and RSG star models with MESA and explode them with v1D.

We use MESA to evolve a star with a zero-age main-sequence mass of $20 M_{\odot}$. The code is stopped when the surface radius increases to $100 R_{\odot}$ (BSG) and again when it reaches $1000 R_{\odot}$ (RSG). One MESA model is saved for each stage. We then use v1D to trigger explosions in these progenitors and evolve the resulting ejecta until they reach a desired radius where we wish them to encounter some CSM. In all cases, the energy is deposited within the H-rich envelope ($1\text{--}10 M_{\odot}$ below the surface) and leads to no explosive nucleosynthesis – the ejected material retains its original (H-rich) composition.

To generate a diversity of interactions we consider various combinations of mass-loss rates, wind velocity, ejecta mass, and ejecta kinetic energy. For the wind phase we adopt mass-loss rates of 0.1 and $1.0 M_{\odot} \text{ yr}^{-1}$ that last for 1 yr, and which generate CSM masses of 0.1 and $1 M_{\odot}$. For RSG progenitors we use a wind velocity of 60 km s^{-1} , while for BSG progenitors we use a wind velocity of 600 km s^{-1} . Because of the larger wind velocity, and the fixed duration of the mass loss, the outer shell thickness for the BSG case is 10 times that of the RSG shell. For the inner shell, we simulate explosions with v1D to eject approximately 1 or $10 M_{\odot}$ with an energy of about 0.05 , 0.1 , or $1.0 \times 10^{51} \text{ erg}$. The corresponding models are named B1, B2, B3 (BSG progenitors) and R1, R2, and R3 (RSG progenitors) – see Table 1 for a summary of properties.

5.2 Dynamical properties

The left-hand panel of Fig. 8 shows the bolometric luminosity computed with HERACLES for these six interaction models. Considerable diversity is exhibited by the light curves.

When the inner shell has a large energy (models R3 and B3), the high-brightness phase is very luminous. Initially, the power stems from the interaction, but at later times, it can stem from the large stored energy in the inner shell. For model R3, the explosion is from a RSG star and, as expected, we see a normal SN II-P luminosity of about $10^9 L_{\odot}$ after the initial interaction-powered peak (which lasts about 30 d). For model B3, the smaller progenitor star leads to a much smaller luminosity contribution at late times (in these models of shell explosion and interaction, no ^{56}Ni is produced so radioactive

Table 1. Summary of initial properties for the interaction models, separating those for the inner shell (which may be SN ejecta or not) and for the outer shell (produced dynamically in an explosion or secularly through a long-lived superwind phase). For both shells, we give its kinematic age when reaching the initial interaction radius R_i . The quantity V_m represents the mean mass-weighted shell velocity. Numbers in parenthesis correspond to powers of 10.

Model	Type	Age (d)	Inner shell				R_i (10^{15} cm)	Type	Age (d)	Outer shell			
			E_{kin} (erg)	M_{tot} (M_{\odot})	V_m [km s^{-1}]					E_{kin} (erg)	M_{tot} (M_{\odot})	\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	V_m (km s^{-1})
A	Ejecta	12.0	1.00(51)	9.96	3000	1.00	Wind	1157.4	3.49(46)	0.35	0.1	100	
B1	Ejecta	11.5	4.95(49)	0.98	2189	0.85	Wind	167.2	3.56(48)	1.0	1.0	600	
B2	Ejecta	22.9	9.57(49)	9.20	970	1.29	Wind	253.3	3.56(47)	0.1	0.1	600	
B3	Ejecta	6.9	9.56(50)	9.50	3042	1.18	Wind	233.4	3.56(47)	0.1	0.1	600	
R1	Ejecta	36.2	4.70(49)	1.0	2150	1.00	Wind	1971.1	3.39(46)	1.0	1.0	60	
R2	Ejecta	55.1	8.90(49)	9.54	937	0.97	Wind	1889.0	3.42(45)	0.1	0.1	60	
R3	Ejecta	22.2	9.28(50)	9.54	3027	1.33	Wind	2598.8	3.42(45)	0.1	0.1	60	
C	Ejecta	2.3	8.56(49)	0.31	4755	0.20	Ejecta	127.9	1.19(49)	6.3	...	396	
D	Ejecta	23.4	6.77(49)	0.29	4730	1.80	Ejecta	941.7	0.94(49)	6.1	...	377	

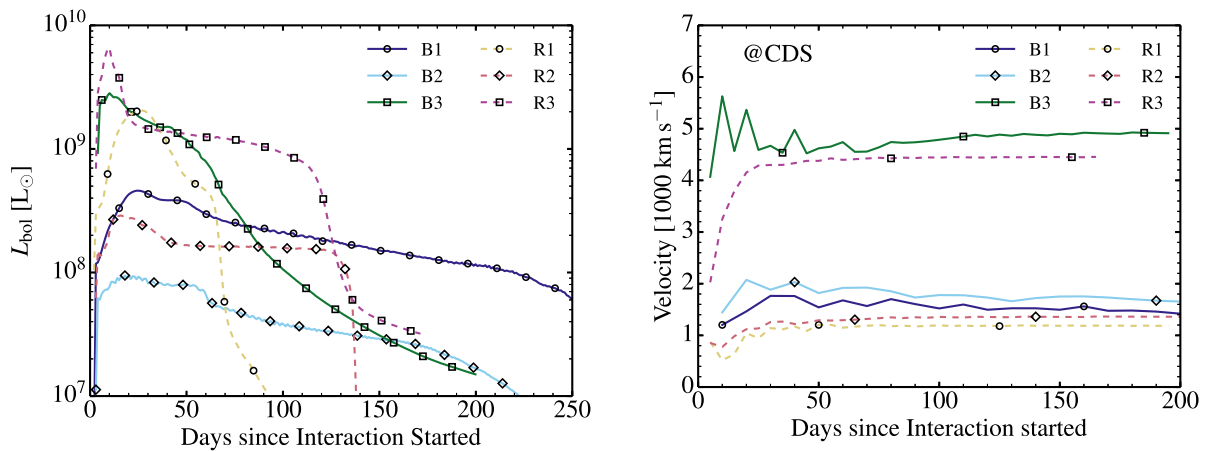


Figure 8. Left: bolometric light curves for models B1, B2, B3, R1, R2, and R3 computed with HERACLES. Right: evolution of the CDS velocity for the same set of simulations (see Section 5 for discussion).

decay is not a power source at any time), so the late-time light curve drops faster and is powered exclusively by the interaction.

Models B2 and R2 have similar ejecta masses to those of R3 and B3, but the ejecta energy is a factor of 10 lower. As a consequence of the smaller kinetic energy the shock luminosity is much reduced and this leads to a much lower peak luminosity. The internal energy (i.e. left over by the original shock that produced the inner shell) is much lower than in the R3/B3 model counterparts. This leads to a smaller contribution to the light curve, although because of the lower expansion/evolution of the whole system, the material stays optically thick longer and can be brighter at very late times (few 100 d) than the R3/B3 model counterparts. Overall though, the lower energy models R2/B2 radiate a much lower time-integrated bolometric luminosity than models R3/B3.

In weak explosions, it is nonetheless possible to power a bright light curve. One way is to increase the CSM mass because this enhances the conversion efficiency from kinetic energy of the inner shell into radiation. Another way to boost the luminosity further is by reducing the mass of the inner shell (i.e. increasing the E/M at fixed E). The reduced inertia of the inner shell facilitates its deceleration and thus enhances the conversion efficiency. This is precisely what is achieved with models R1 and B1.

The inner shell of R1 has a kinetic energy a factor of 2 lower than R2, and a factor of 20 lower than R3. However, model R1 reaches a peak bolometric luminosity of $2 \times 10^9 L_{\odot}$, which is

a factor of about 10 larger than R2, and only a factor of 3 lower than R3. This occurs because in R1, $1 M_{\odot}$ of ejecta is ramming into $1 M_{\odot}$ of CSM, and so the conversion of kinetic energy into radiative energy is very efficient. In models R2 and R3, a $9.54 M_{\odot}$ ejecta rams into a CSM mass of only $0.1 M_{\odot}$. Model B1 reaches a much fainter maximum than R1 because the CSM wind speed is 10 times larger (weaker shock) and the wind density is 10 times smaller (this is because we adopt the same wind mass-loss rate as model R1). However, the interaction through the more extended CSM persists for longer and powers a luminosity $\gtrsim 10^8 L_{\odot}$ out to 250 d (the luminosity from model R1 drops below $10^7 L_{\odot}$ at $\lesssim 100$ d). Compared to model B2, model B1 has a peak luminosity a factor of 5 higher despite having a kinetic energy almost a factor of 2 lower.

Thus it is straightforward to produce a very luminous interacting SN with a low-energy inner shell simply by invoking a CSM mass that is comparable or larger than the inner shell mass. The conversion efficiency is higher so that a larger fraction of the kinetic energy of the inner shell is extracted. The influence on the luminosity is large because a typical SN radiates a total of 10^{49} erg, so extracting 50 per cent of the 5×10^{49} erg kinetic energy of the inner shell can more than double the luminosity compared to a standard SN.

Another consequence of having an interaction between a low-mass inner shell and a high-mass outer shell is that fast material will not survive the interaction – the interaction will die out if the

fast material in the inner shell is entirely braked. As can be seen in the right-hand panel of Fig. 8, models R3 and B3 show a CDS speed of 4000–5000 km s⁻¹ (comparable to the 3500 km s⁻¹ of our model A), while the CDS speed for models R1 and B1 is only ~1000 km s⁻¹. Thus interactions between a low-mass inner shell and a high-mass outer shell, like those associated with R1 and B1, may be able to explain events like SN 1994W.

Finally, as can be seen in Fig. 8, the power from most of our interaction simulations is of the order of a few 10⁷ L_⊙ at ~200 d (with no contribution from ⁵⁶Ni), and thus can alone explain the late-time luminosity of a SN IIn like 2009kn (Kankare et al. 2012).

5.3 Spectral properties

We now discuss the spectral properties of these models at different epochs with the goal of illustrating the diversity of spectral morphologies arising from different configurations. To expedite the CMFGEN simulations for this section, we only include model atoms for H I, He I–II, and Fe II–V.

Fig. 9 shows a montage of spectra for models B1, B2, B3, R1, R2, and R3 computed with CMFGEN and based on HERACLES simulations at early (top half) and late (bottom half) times after the onset of interaction. The spectra are quite disparate. At early times, all models except R3 and B3 show the distinctive IIn line profiles with a narrow core and extended symmetric wings. In model R3 at 5 d and B3 at 10 d, the CSM optical depth is already low (this can be indirectly inferred by the 10 d rise time to bolometric maximum;

Fig. 8). Emission from the optically thick CDS is thus weakly affected by the CSM and the spectra show the nearly unadulterated CDS radiation. Some line profiles (e.g. H α , H β , He I 5875 Å) exhibit weak emission and blueshifted absorption (the spectrum resembles that of model A at 20.0 and 34.7 d), while He II 4686 Å forms within the CDS and appears as broad and blueshifted emission. This line was not predicted in our calculations for model A because the emitting region was too cool. Its presence in model B3/R3 is not surprising, as it is observed in SNe like 1998S (Fassia et al. 2000; Leonard et al. 2000; Shivvers et al. 2015). Other models show the distinctive IIn properties. Combined with the presence of lines from the hot CSM (broadened by electron scattering) or from the hot CDS (broadened by Doppler effect), all six models show narrow lines arising from the cool outer CSM.

At late times model B3 shows broad line profiles, in particular H α , with a blueshifted peak and emission skewed to the red. Model R3 at 75 d exhibits a spectrum more typical of a non-interacting SN II late in the plateau phase. The skewness of the H α profile is much reduced (i.e. the emission is more symmetric), although the peak emission is blueshifted by about -1500 km s⁻¹. For model R3, the emission is primarily from the inner ejecta (unaffected by the interaction), as obtained for model A at corresponding epochs.

In model B2 at 80 d, the emission is primarily from the CDS and gives rise to double-peaked line profiles (probably because of an optical depth effect similar to limb darkening) for H I and He I lines, with peaks at about ± 1000 km s⁻¹. The blue component is stronger, which suggests a continuum optical depth effect acting on

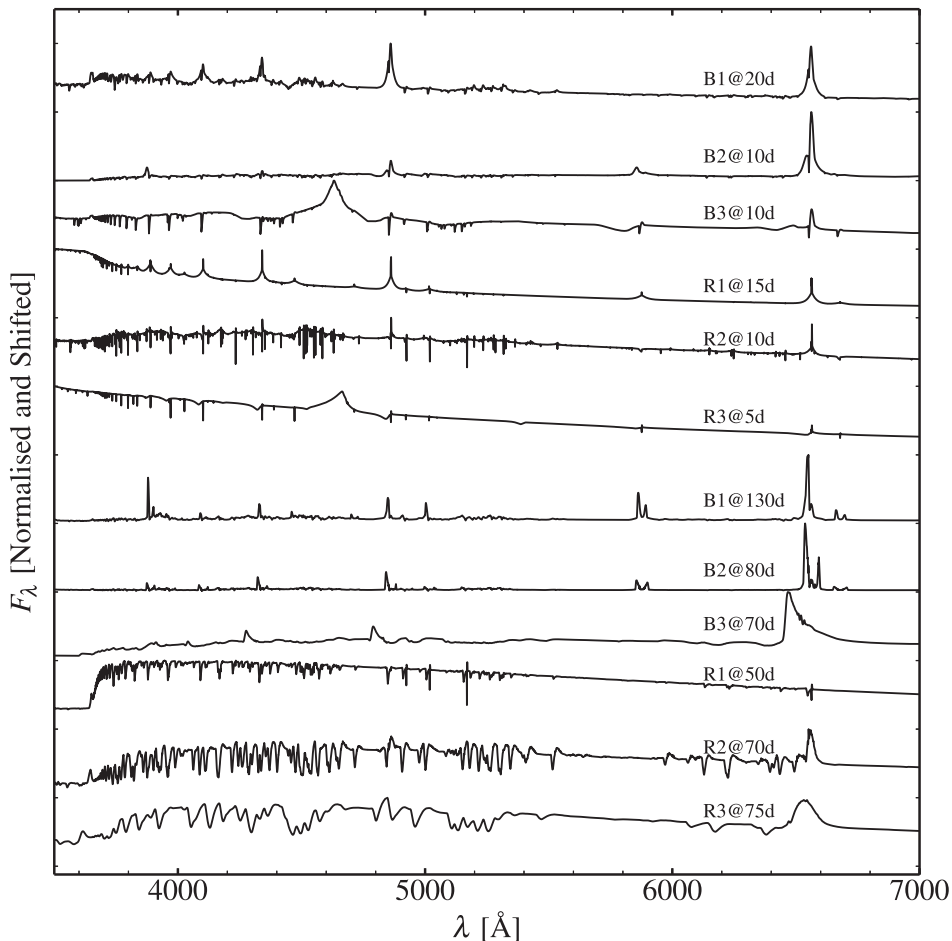


Figure 9. Early and late time spectra for models B1, B2, B3, R1, R2, and R3 computed with CMFGEN and based on HERACLES simulations.

line photons. Lower energy models show narrower lines. In model R1 at 50 d, the spectrum forms in the optically thick slow-moving CDS and only absorption lines are seen (this is similar to model A at 34.7 d). In model B1, only narrow emission lines are seen.

This diversity of early/late time line profiles conveys a wealth of information on the interaction configuration. We defer to a subsequent paper the study of all these profile properties. What we take from this study is that model R1 can produce a bright display while showing broad lines neither at early times nor at late times. In the next section, we will elaborate a more suitable model that shares these properties and reflects those observed for SN 1994W.

6 SN 1994W: A LOW-MASS ENERGETIC INNER SHELL RAMMING INTO A SLOW MASSIVE OUTER SHELL

6.1 Preamble

In this final modelling section, we setup a more physical model to explain events like SN 1994W. Building upon the results from the preceding sections, the configuration we are after is a massive slow outer shell and a low/moderate mass inner shell with a modest kinetic energy (by SN standards).

Stars in the range 8–12 M_{\odot} sit at the junction between two completely different fates. The lower mass ones may ultimately produce a bare white dwarf, while the more massive ones will form a degenerate core (made of ONeMg or Fe-group elements) that collapses to a neutron star (Poelarends et al. 2008). For stars just above that mass cut, O, Ne, or Si may ignite off-centre, under degenerate conditions. If/when this occurs, burning is dynamical and leads to a nuclear flash (Weaver & Woosley 1979; Woosley & Heger 2015). Because the phenomenon is only encountered in the late stages of evolution, when these low-mass massive stars are in a RSG phase, even a very small energy release from nuclear burning is sufficient to eject the loosely bound envelope (Dessart et al. 2010a). If the delay until core collapse is weeks to months, the subsequent explosion will lead to an interaction between two detached shells. If the delay is short (say, of the order of days), only one explosion may be seen because the SN shock will overtake the first shock before it reaches the stellar surface (Woosley & Heger 2015).

Such nuclear flashes have been proposed as a potential mechanism leading to interacting SNe such as SN 1994W (Chugai et al. 2004; Dessart et al. 2009). Our simulations of Sections 4–5 show that interactions in which the inner shell is more energetic than, but less or as massive as, the outer shell can lead to a luminous SN II event. Here, we compute light curves and spectra for such configurations, and confront them with the observations of SN 1994W.

6.2 Interaction configurations

The possible parameter space is large since we do not know the final star mass, the energy of each explosion, nor the delay between them – significant variations are to be expected for these quantities. So, our model is one realization out of many possibilities, but it is chosen to match roughly what was inferred for SN 1994W. In particular the interaction must take place at a large distance from the progenitor star (Chugai et al. 2004; Dessart et al. 2009). We need the inner shell to be less massive than the outer shell and to have a larger kinetic energy (Sections 4–5).

Because of off-centre ignition (in particular of Ne), we could not evolve any MESA model for a $<12 M_{\odot}$ star until core collapse. So, we use instead a higher mass model of $12 M_{\odot}$ and enhance the

mass loss during the RSG phase to compensate for the higher initial mass. Our $12 M_{\odot}$ MESA model has then a final mass of $9.87 M_{\odot}$ and a final radius of $520 R_{\odot}$ (our conclusions would hold if these values were changed by few 10 per cent). Using v1D and starting from this model, we first trigger a 10^{49} erg explosion at the base of the H-rich envelope (outer edge of the He core), at a mass cut of $3.5 M_{\odot}$ and let this ejecta evolve to late times. We then trigger a 10^{50} erg explosion in this H-deficient remnant. We use a mass cut of $3.1 M_{\odot}$ (and not 1.4 – $1.5 M_{\odot}$) because this second explosion is meant to mimic core collapse of a lower mass star, which would have a lower He-core mass than the $12 M_{\odot}$ model we use. This second ejecta is then evolved to late times.

We set up the interaction using both ejecta calculated with v1D. To test the influence of the initial interaction radius R_t , which is connected to the timing of the two explosions, we set up a model C with $R_t = 2 \times 10^{14}$ cm, and a model D with $R_t = 1.8 \times 10^{15}$ cm.

For the outer shell, we use the structure of the first exploded shell when its base reaches R_t . For the inner shell, we use the structure of the second exploded shell when its outer part reaches R_t . We join the two shells at that radius R_t . Because each shell was exploded and evolved with the radiation hydrodynamics code v1D, the fluid variables (radius, velocity, density, temperature) are physically consistent.

The properties of the initial configuration for models C and D are given in Table 1. The initial velocity, density, and temperature structures are illustrated in Figs A2 and A3 in Appendix A. When setting up the interaction configuration, some grid zones are trimmed in the outer parts of the inner shell and the inner parts of the outer shell in order to avoid creating a gap. This explains the slight differences in mass/energy for each shell of models C and D. The inner shell is $\approx 0.3 M_{\odot}$ and expands very fast, with a mean mass-weighted velocity of ≈ 4750 km s^{-1} . In model C, it is only 2.3 d old at the start of the interaction so the inner shell is initially hot and mostly optically thick. In model D, the inner shell is 23.4 d old, cold and optically thin. The outer shell of models C/D is $\approx 6.3 M_{\odot}$ (20 times more massive than the inner shell), with a mean mass-weighted velocity of ≈ 380 km s^{-1} . Its age at the start of the interaction is 127.9 d in model C, and 941.7 d in model D. Because of its slow expansion, the inner parts of that shell are still optically thick and hot (about 20 000 K) in model C. In model D, the outer shell is much older, and therefore cold and optically thin. In the absence of interaction, the outer shell alone would exhibit a very long and faint plateau (with a bolometric luminosity of the order of $10^7 L_{\odot}$; see the low-energy explosions of RSG stars discussed in Dessart et al. 2010a).

In model A and the grid of models presented in Section 5, the outer shell was formed through a phase of intense mass loss. So, the CSM in that case was pre-SN wind material. Here, the outer shell is a very different type of CSM (described by an homologous expansion, a complex density structure, etc). It is explosively formed by a nuclear flash and subsequently affected, within days to months, by the terminal collapse of the remaining star (which in this case can only produce a very low mass ejecta made of the fraction of the He core that does not collapse into the remnant, so $\lesssim 1 M_{\odot}$ in such progenitors).

6.3 Results for model C

6.3.1 Dynamical properties

The dynamical evolution for model C is very different from standard interacting SNe – in particular the strong interaction generating the shock has ceased before the peak brightness is reached. We

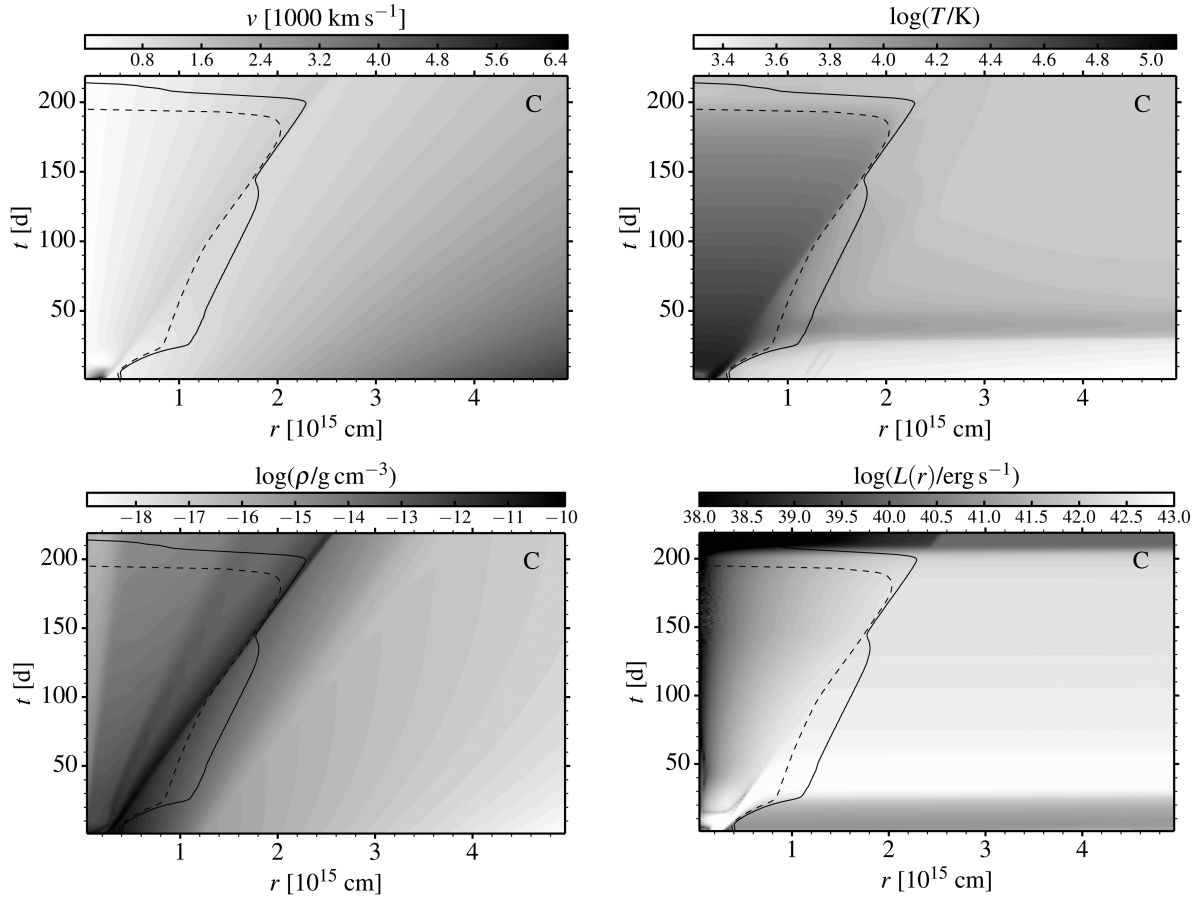


Figure 10. Grey-scale images showing the evolution of the velocity, temperature, density, and local luminosity for model C. The solid line traces the photosphere and the dashed line the location where the optical depth is 10 (for both quantities, we use the opacity from electron scattering only).

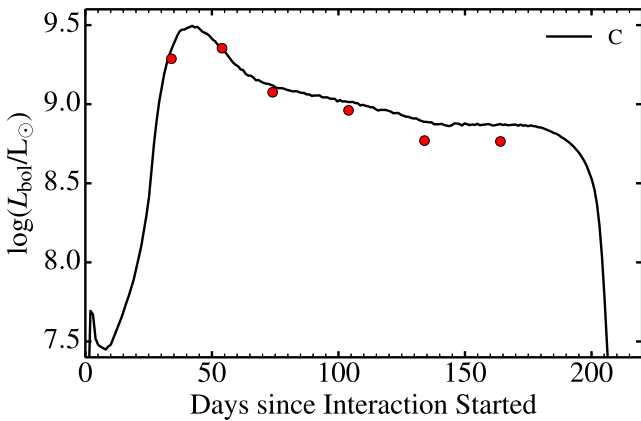


Figure 11. Bolometric light curve for model C (the dots correspond to the luminosity computed at corresponding epochs with CMFGEN).

illustrate these differences in a series of grey-scale images and snapshots. Fig. 10 shows grey-scale images of the velocity, temperature, density, and radiative luminosity versus radius and time computed with HERACLES for our model C. Fig. 11 shows the bolometric light curve of model C computed with HERACLES. Figs 12 and 13 show this evolution at selected snapshots, from 1.0 to 150.0 d after the onset of the interaction.

The interaction is very strong initially because the density at the base of the outer shell is $\sim 10^{-11}$ g cm $^{-3}$ and the velocity of the fast

material in the inner shell is $\sim 10\,000$ km s $^{-1}$. The outer shell being optically thick, the radiation generated by the shock cannot escape. All the energy is trapped. The temperature at the base of the outer shell rises from 20 000 to $\gtrsim 100\,000$ K. As time progresses, the shock continues to progress through the outer shell, sweeping up more material and building a hot optically thick dense shell, but the deceleration is severe. By 10 d, no material in the inner shell moves faster than 1000 km s $^{-1}$ – the shock is essentially gone by then (Fig. 12). This implies that the rest of the outer shell will not be shocked, and also that the inner parts of the inner shell will not be decelerated further. The effect of the shock has been to pile up a lot of material around 1000 km s $^{-1}$, leaving slower and faster material (dynamically) unaffected.

Within 10 d, the interaction as a power source for the SN has vanished (the shock is already weak). The bulk of the kinetic energy in the inner shell has been transformed into internal energy, which is primarily radiation. Most of this radiation energy is trapped within the dense shell, so the subsequent radiation is the slow release of radiation energy from this optically thick ejecta. At 10.0 d, the flux emerging from the dense shell is huge, much in excess of the flux radiated at the photosphere: the two will become comparable after a diffusion time of about 30 d (see e.g. the bottom right-hand panel of Figs 10 and 13).

Before the interaction starts, the photosphere in the outer shell is at $\lesssim 4 \times 10^{14}$ cm. Once the interaction starts, the energy deposited by the shock heats up the ejecta, shifting the spectral energy distribution to the blue, facilitating the reionization of the outer shell

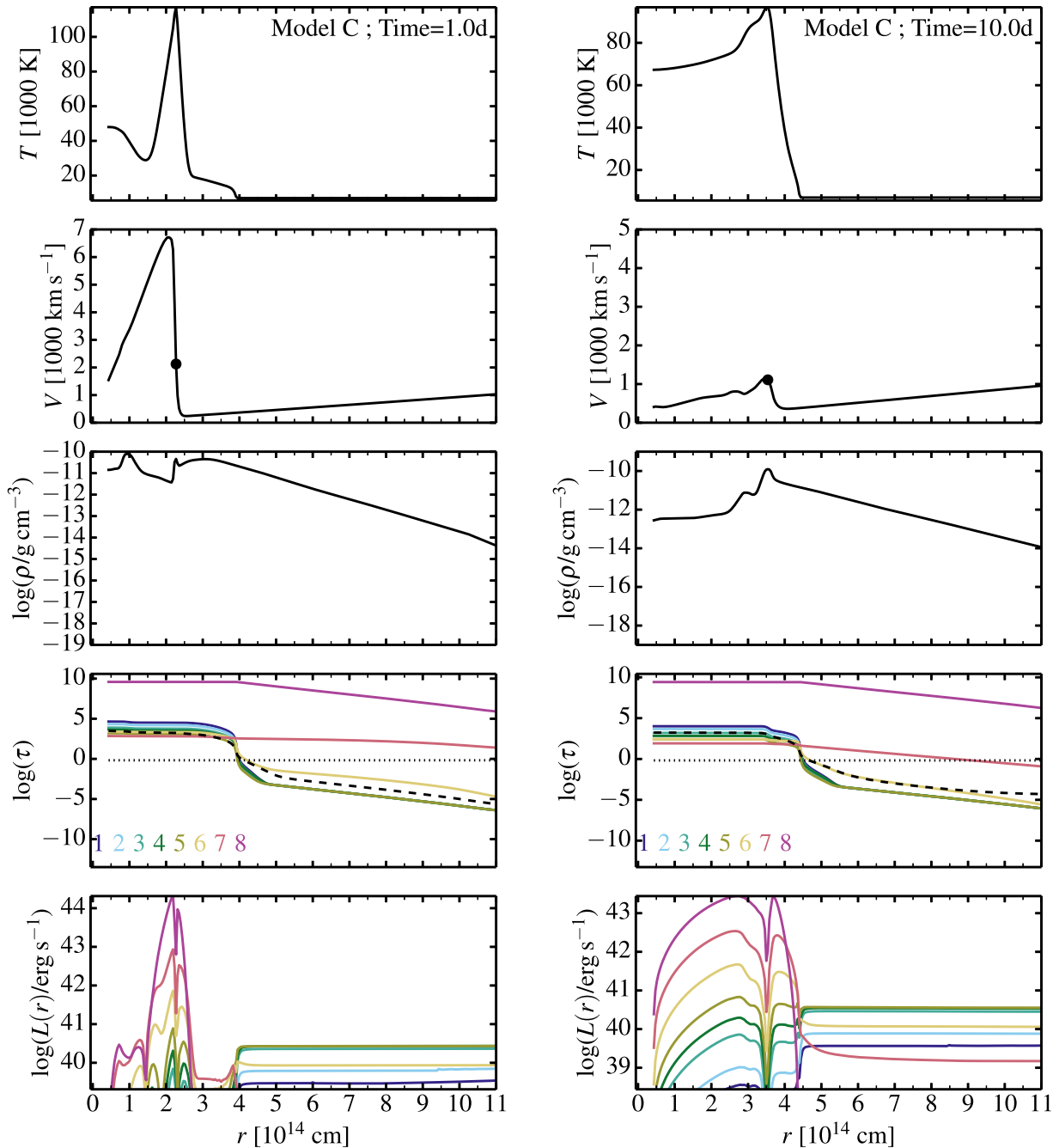


Figure 12. Left: properties of the interaction model C computed with HERACLES at 1.0 d after the start of the interaction. We show the gas temperature, the velocity (the dot corresponds to the velocity of the CDS), the mass density, the optical depth, and the radiative luminosity versus radius. For the optical depth panel, we show that quantity for each energy group (coloured line; the group energy increases with the group number; see Section 2 for details) and for electron scattering (dashed line) – the dotted line corresponds to an optical depth of 2/3. At this time, the outer shell is optically thick out to 4×10^{14} cm. The radiation emerging through the photosphere is very small compared to the luminosity injected at the shock. Right: same as left, but now at 10.0 d after the onset of the interaction.

material, and pushing the photosphere out to larger radii. At 10.0 d, the photosphere has moved out to $\sim 4.2 \times 10^{14}$ cm, and following the (slow) ejecta expansion, it keeps moving out to reach $\sim 1.1 \times 10^{15}$ cm at 30 d, and $\sim 1.6 \times 10^{15}$ cm at 100 d. The thickness of the ionized material in the outer shell (or, equivalently, the size of the region between the photosphere and the CDS) is fairly constant between 30.0 and 150.0 d (Fig. 10) – this region is comoving with the ejecta. So, this situation is analogous to a low energy faint SN II-P, but here energy is freshly supplied once the ejecta has expanded to

a large radius, in this case beyond 2×10^{14} cm. The fresh supply of energy boosts the SN luminosity, transforming this originally faint transient into a very luminous Type II SN. The ejecta retains its low velocity and thus, unlike a typical SN II-P, the event is very luminous but has a low expansion rate.

The very slow and dense material at the base of the outer shell has been swept up into a dense shell, undergoing an acceleration from ~ 200 to ~ 1000 km s $^{-1}$. This corresponds to about half the total kinetic energy of the inner shell initially. The other half,

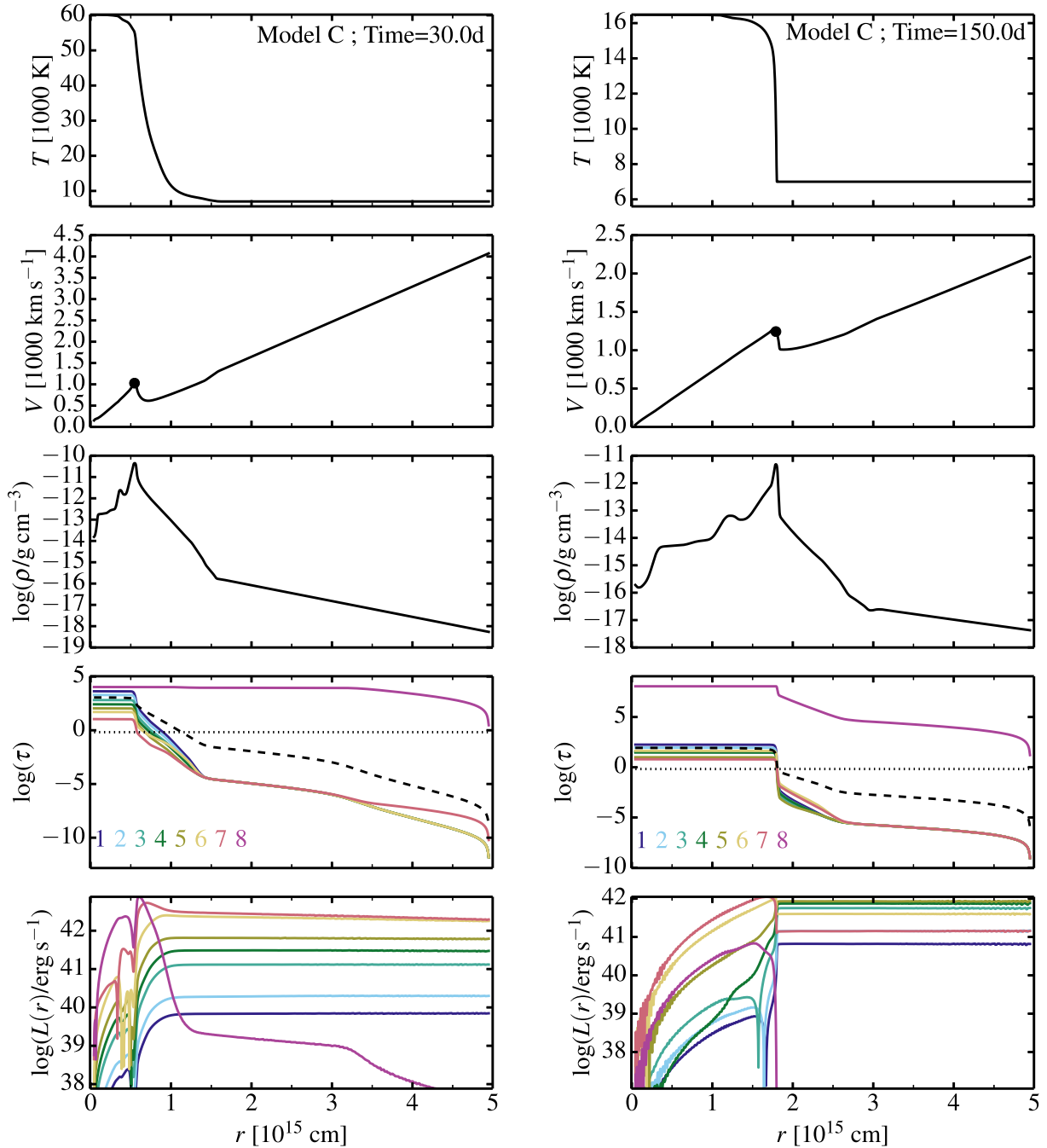


Figure 13. Same as for Fig. 12, but now at 30.0 d (left) and 150.0 d (right) after the onset of the interaction.

$\sim 5 \times 10^{49}$ erg, is radiated away, producing a very luminous event, typically with five times the total integrated luminosity of a standard SN.

6.3.2 Spectral simulations for model C and comparison to SN 1994W

Using the same procedure as in Section 4, we have post-processed the HERACLES simulations of model C with CMFGEN to compute the emergent spectra at 30, 50, 70, 100, 130, and 160 d after the onset of interaction. For each epoch, we obtain a good correspondence

between the bolometric luminosity computed by HERACLES (line) and CMFGEN (Fig. 11).

Fig. 14 shows the CMFGEN spectral sequence for our model C (top panel) as well as the multi-epoch spectral observations of SN 1994W (bottom panel). The model C shows the distinctive IIn line profile signatures at 30, 50, 70, and 100 d on H I and He I lines, as well as the presence of very narrow lines associated with Fe II. The spectrum forms within the outer shell, in a region not affected dynamically by the interaction. This outer shell shows a steep declining density (comparable to a power-law density profile with an exponent -8), is partially ionized, and moves with a velocity of $500\text{--}1000 \text{ km s}^{-1}$ (Fig. 10). It is the scattering with free electrons in these photospheric

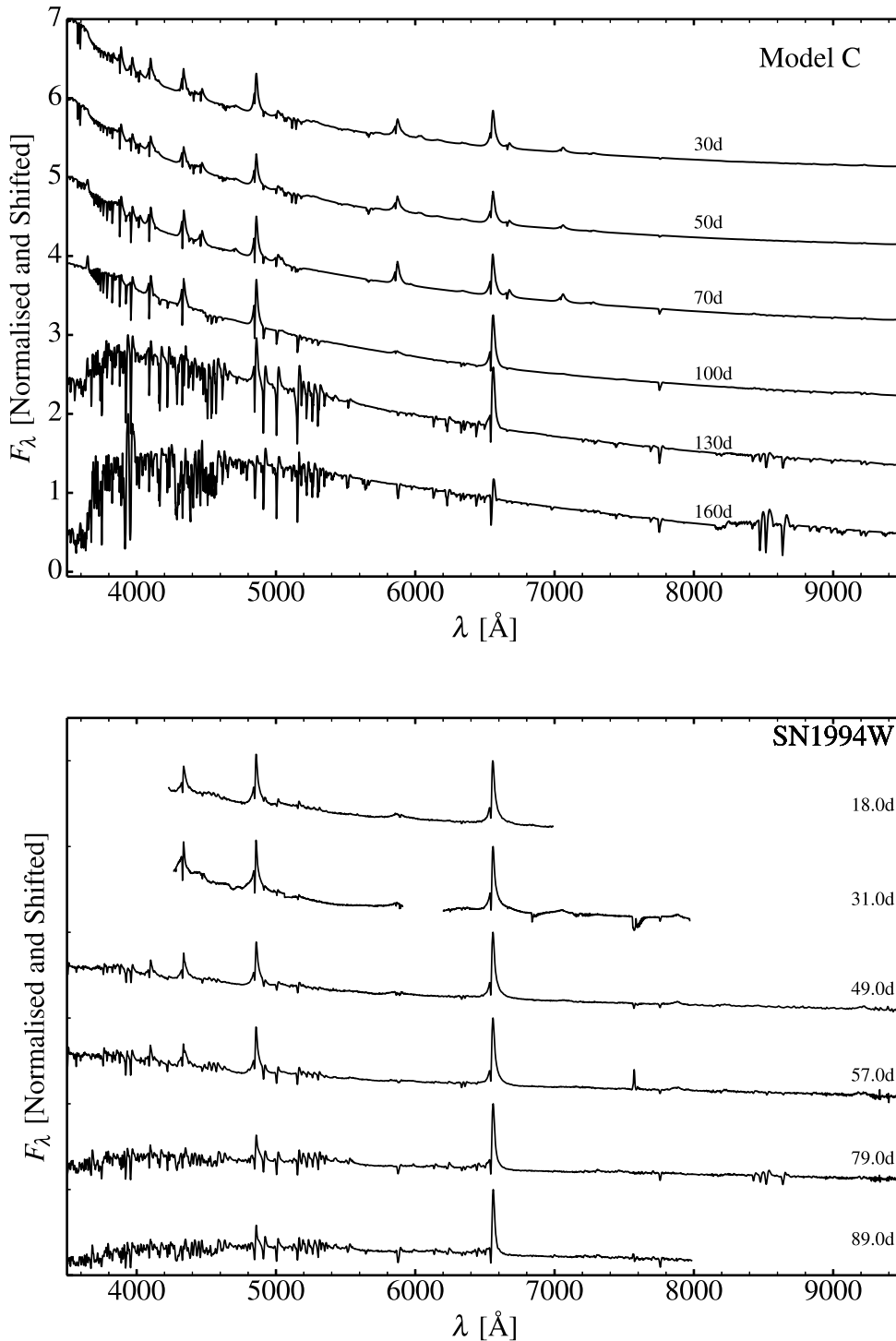


Figure 14. Top: spectral evolution of the double explosion model (C). Bottom: multi-epoch spectra of SN 1994W, corrected for redshift but not for extinction. The spectrum shows narrow lines with broad wings early on, but, unlike SN 1998S, never develops broad lines at late times.

layers that cause the presence at early times of the broad symmetric wings on H I and He I lines. This configuration, which is based on a radiation hydrodynamics model, is physically equivalent to the heuristic set-up of Dessart et al. (2009) for SN 1994W.

As time progresses, the line profiles lose their extended wings and become narrower (see e.g. H α ; Fig. 15). This arises because the spectrum formation region is more confined to the recombination front, with hot/ionized material below and cool/neutral material

above (Fig. 13). The spectral energy distribution becomes redder, and lines from Ca II, Na I, Sc II, Ti II, and Fe II strengthen. Broad lines are absent at all times because the bulk of the radiation arises from slow moving material (shocked material from the interaction but also unshocked material in the outer shell) – the representative expansion rate is $\sim 1000 \text{ km s}^{-1}$. This is also the origin of the absorption in all line profiles at a Doppler velocity $\sim -1000 \text{ km s}^{-1}$ (see e.g. H α ; Fig. 15). Initially, the absorption is partially filled-in

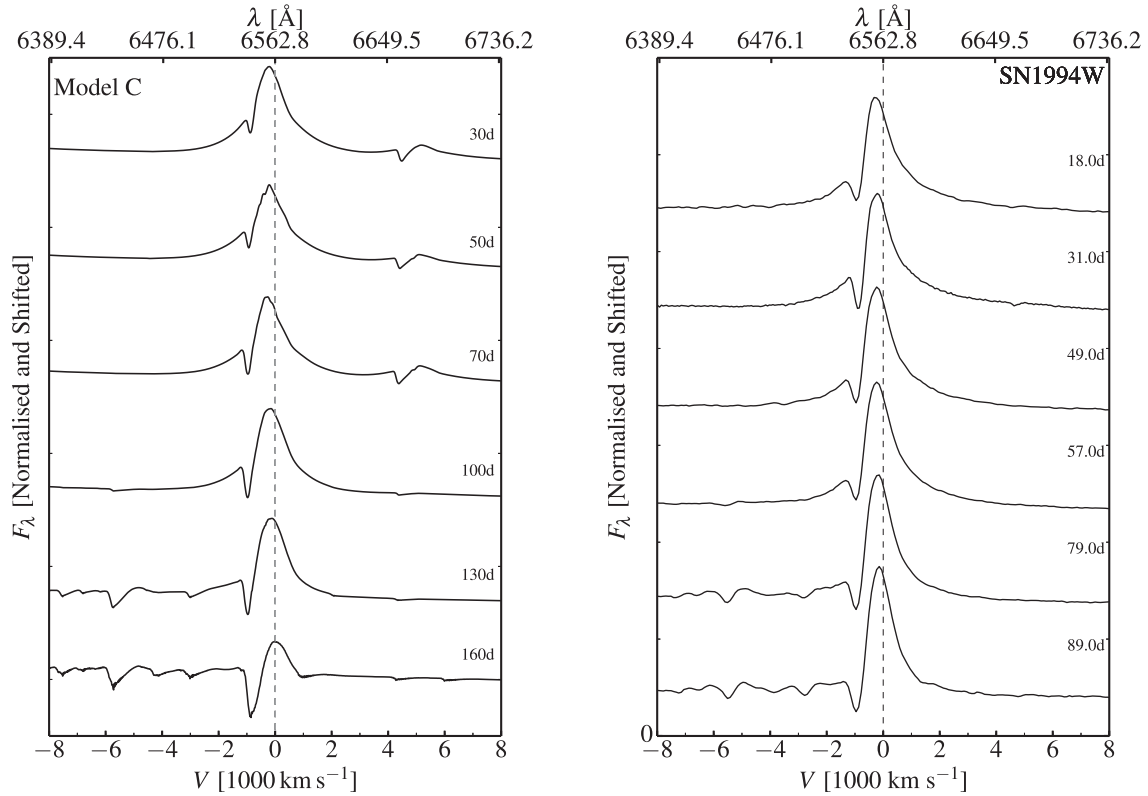


Figure 15. Left: spectral evolution of the double explosion model C. Right: multi-epoch spectra of SN 1994W. The spectrum shows narrow lines with broad wings early on, but, unlike SN 1998S, never develops broad lines at late times.

(the residual flux is above the continuum level) because of photon frequency redistribution by scattering with thermal electrons. At later times (spectra for days 130 and 160), this absorption appears as a standard P-Cygni absorption (with a minimum flux below the continuum level). All these properties match the spectral evolution of SN 1994W (bottom panel), and are in stark contrast with model A (and SN 1998S).

Despite the good agreement between the synthetic spectra of model C and the observations of SN 1994W, the model light curve is somewhat discrepant. While model C predicts a sustained bolometric luminosity for up to 200 d, the high-brightness phase of SN 1994W lasts for about 100 d (Fig. 16). As mentioned earlier, the parameter space covered by interacting SNe is likely very large. Nuclear flashes in 8–12 M_{\odot} stars are an attractive scenario for interacting SNe because they offer a natural explanation for the short delay between the ejection of the H-rich envelope and the terminal explosion following core collapse. So, rather than considering alternate scenarios (different progenitor mass, shell eruptions, etc.), we have slightly modulated the initial configuration of model C to test how we could reconcile the light curve of model C with the observations of SN 1994W, while retaining the same spectral evolution properties. We find that the discrepancy is reduced if we shift the interaction to larger radii. In the next section, we illustrate the results for one such model, named model D.

6.4 Results for model D

The initial configuration of model D is very similar to that of model C except for the initial interaction radius R_i , which we increase from 2×10^{14} to 1.8×10^{15} cm. Compared to model D, the interaction region in model C is initially much more compact so the inner/outer

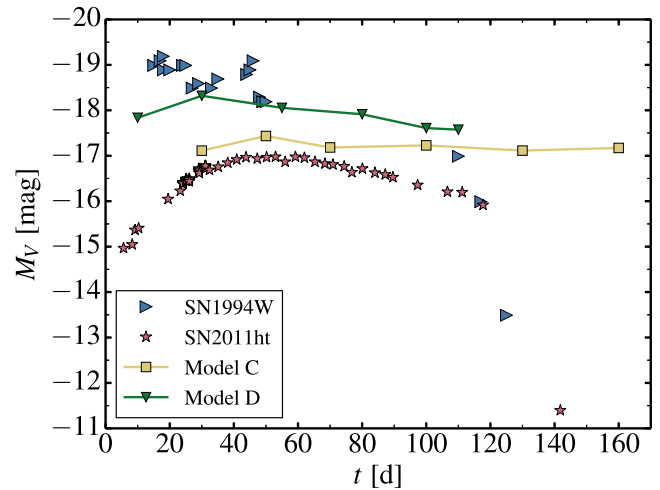


Figure 16. Absolute V-band light curve for SN 1994W and SN 2011ht compared to our models C and D. See Section 3 for details on the source of observations, distances, reddening, and inferred time of explosion. For the models, the time is with respect to the onset of interaction.

shell densities and temperatures are higher. Interaction starts when the outer shell is still optically thick. The length scales are smaller so the deceleration of the inner shell is very rapid – the shock in model C dies within 10 d of the onset of interaction. In model D, the interaction region is much more extended. The outer shell age is $\gtrsim 7$ times greater than in model C, so its density is about 400 times lower (each shell is explosively produced and in homologous expansion at the onset of interaction). Were it not cold and recombined,

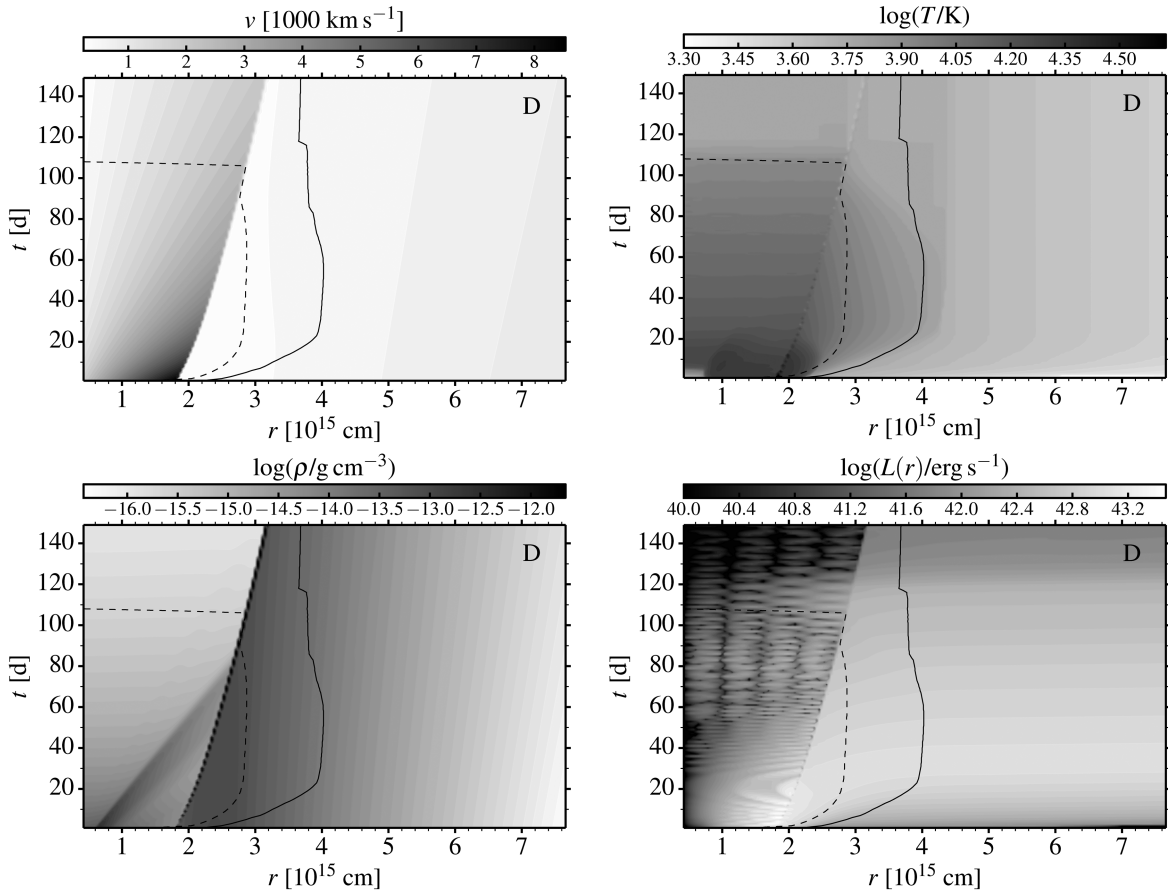


Figure 17. Grey-scale images showing the evolution of the velocity, temperature, density, and local luminosity for model D. The solid line traces the photosphere and the dashed line the location where the optical depth is 10 (for both quantities, we use the opacity from electron scattering only).

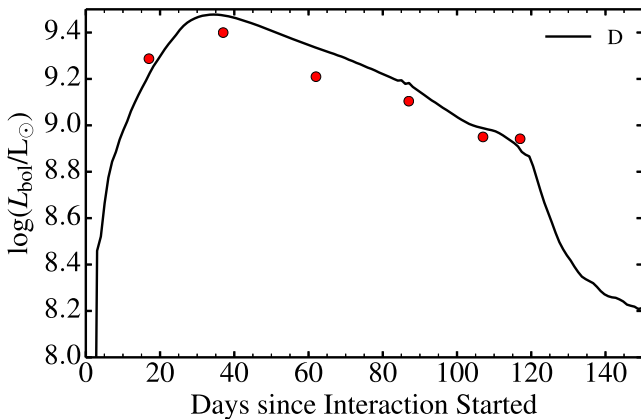


Figure 18. Bolometric light curve for model D (the dots correspond to the luminosity computed at corresponding epochs with CMFGEN).

the outer shell optical depth would be $\gtrsim 50$ times lower than in model C. The characteristic time for the CDS to sweep up a given mass of CSM is also $\gtrsim 7$ longer. So, even though the shell masses and energies are comparable in models C and D, the dynamics and radiative properties of the interaction are distinct.

We show in Fig. 17 a set of grey-scale images for the velocity, temperature, density, and luminosity versus radius and time for model D. Fig. 18 shows the bolometric light curve of model D com-

puted with HERACLES. We also show snapshots of these interaction properties at 10.0 and 100.0 d (Fig. 19).

Compared to model C, the shock is still present at the end of the simulation at 150 d. But just like in model C, the inner shell material is strongly decelerated. Because of the contrast in inner/outer shell mass, the fast material in the inner shell at late times has a very low density.⁷ At 150.0 d, the CDS mass is about $3 M_{\odot}$ and the residual fast inner shell material contains $\lesssim 0.01 M_{\odot}$.

Because the shock persists for the entire duration of the simulation, the shock luminosity is a continuous power source for the light curve. Initially, about half of the outer shell mass is quickly ionized, not directly by Lyman photons because they suffer a large optical depth, but indirectly through absorption of lower energy photons. Within 20 d, the photosphere has migrated out to 4×10^{15} cm in the outer shell and will remain at that location until the CDS overtakes that radius at $\gtrsim 150$ d. Relative to model C, the volume of ionized material is larger and the energy from the shock is released for longer so the temperature in the interaction region is lower (it peaks at $\sim 30\,000$ K, rather than $\gtrsim 100\,000$ K).

Because of the slow expansion of the outer shell (in both models C and D), the densities are large enough to make the material optically thick to electron scattering. The limiting factor is the ionization. In

⁷ Recall here that the HERACLES code is Eulerian so we actually inject low-density material at the ‘inflow’ inner boundary. The innermost point of the inner shell is initially at 1500 km s^{-1} . At 150.0 d, the only part of the original inner shell that remains is between 1500 and 2000 km s^{-1} .

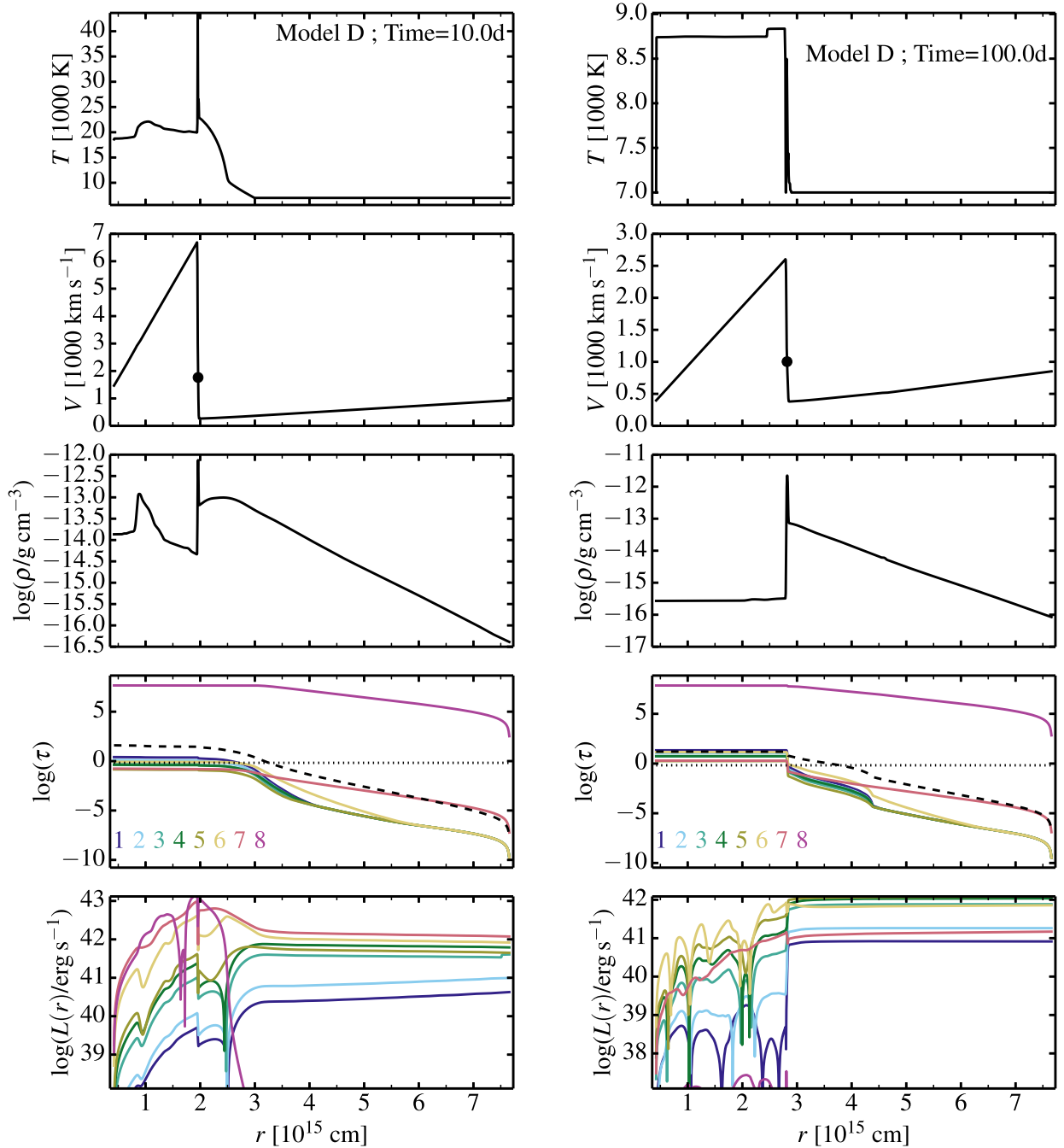


Figure 19. Same as for Fig. 12, but now for model D at 10.0 d (left) and 100.0 d (right) after the onset of the interaction. At late times, the unshocked inner shell mass is $\lesssim 0.01 M_{\odot}$ while the CDS mass is $\approx 3 M_{\odot}$. The dot in the velocity panel (second row from top) corresponds to the velocity of the CDS.

model D, the balance between heating by the shock and cooling from radiation and expansion permits the ionization of a sizeable fraction of the outer shell. This ionized layer is present during the entire high-brightness phase of model D. So, we expect to see persistent signatures of electron scattering. Furthermore, by 60 d after the onset of the interaction, the CDS velocity is down to $\approx 1000 \text{ km s}^{-1}$ while its optical depth is about 25. So, just like in model C, this configuration should not give rise to broad spectral lines at any time.

The lower optical depths achieved in model D produce a faster rising light curve, a brighter peak, and a shorter high-brightness phase than in model C. The correspondence with the observed light

curve of SN 1994W is now satisfactory (Fig. 16). Besides kinetic energy, the transition radius seems an important tuning parameter controlling the light curve of this type of interactions and it may be in part responsible for the observed diversity of SNe IIn (the light curves of SN 1994W and SN 2011ht differ sizeably, yet they exhibit a very similar spectral evolution; Humphreys et al. 2012).

Fig. 20 shows the spectral evolution for model D, which is very analogous to that of model C. Because of the larger radius for interaction, the temperature of the ionized outer shell and of the CDS is lower. This causes the spectral energy distribution to be redder than for model C early on. Importantly, broad lines are never seen, as typified by $H\alpha$ (Fig. 21). Before light-curve maximum, the

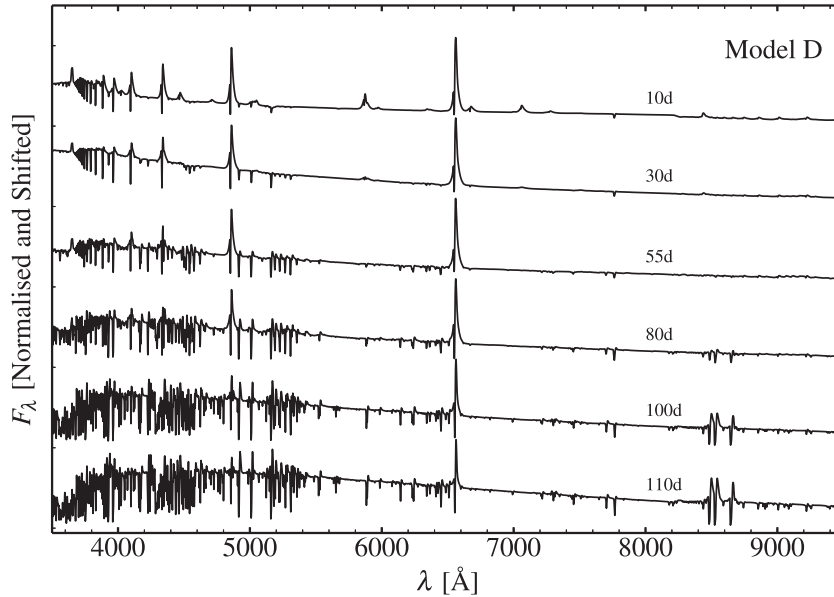


Figure 20. Spectral evolution of the double explosion model D. For each spectrum, the label indicates the time since the onset of interaction.

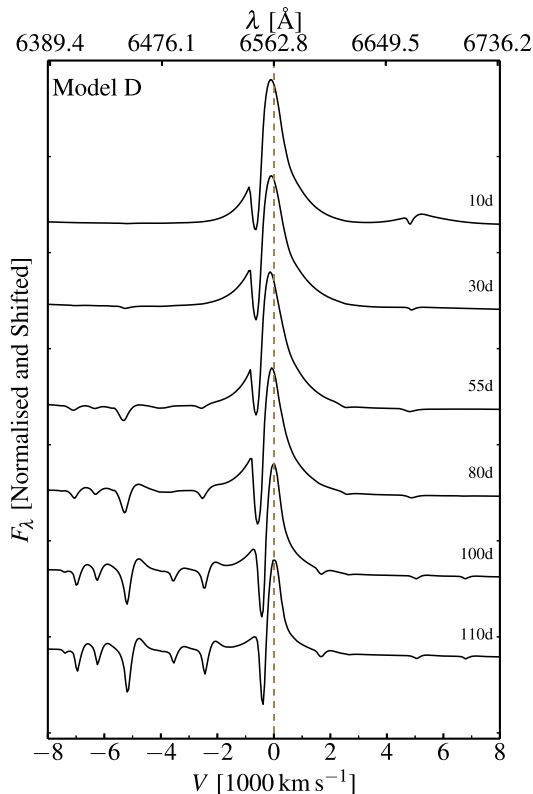


Figure 21. Evolution of the H α region for the double explosion model D. For each spectrum, the label indicates the time since the onset of interaction.

rate at which radiation escapes the CSM is lower than the rate at which it is released at the shock because of optical depth effects. Consequently, the temperature rises in the optically thick CSM until a maximum around bolometric maximum. Afterwards, as long as the optical depth remains sizeable, the rate at which radiation escapes the CSM is greater than the rate at which it is released at the shock and the temperature decreases (Fig. 22). This effect,

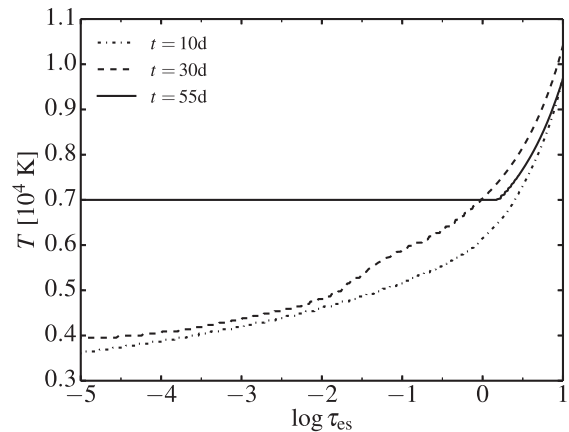


Figure 22. Temperature profile versus electron scattering optical depth in model D at 10, 30, and 55 d after the onset of interaction. Notice the higher gas temperature in the spectrum formation region (at optical depth between 1 and 10) at the time of maximum ($t \sim 30$ d), which is also when the spectrum is bluer.

characteristic of the diffusion process here, is seen in model D (and also in model X of D15) and is also observed in SN 1994W (Sollerman et al. 1998; Chugai et al. 2004). Indeed, the spectra progress towards higher colour temperatures until maximum and towards lower colour temperatures afterwards (they increasingly redden with time), showing signs of recombination and increasing line blanketing. All these properties reproduce satisfactorily the observations of SN 1994W.

7 CONCLUSIONS

In this paper, we have presented a series of radiation hydrodynamics and radiative transfer simulations in order to explore the origin of the spectral diversity of interacting SNe. The study is not exhaustive but it captures the salient features seen in events like SN 1998S on the one hand, and SN 1994W on the other hand.

The main impetus for this work was the perplexing absence of broad lines at all times in the spectra of SN 1994W. In Dessart et al. (2009), we obtained a very good match to the spectral observations of SN 1994W by invoking a hydrogen-rich slow optically thick shell, in which the bulk of the radiation is emitted. We also proposed that the electron scattering wings were formed internally to this thick shell, rather than externally into some CSM. Our proposed scenario was not easily adaptable to the results of Chugai et al. (2004), who argued for an interaction between a $7\text{--}12 M_{\odot} \sim 10^{51}$ erg inner shell with a $0.4 M_{\odot}$ dense wind CSM. The difficulty with that model is to explain the lack of broad lines at late times. In a recent study on superluminous SNe like 2010jl (Dessart et al. 2015), we found that the emission from the dense shell eventually appears, even with a massive and dense CSM, and the associated line profiles are Doppler broadened, with a velocity representative of the velocity of the dense shell. For SN 1994W, the Chugai et al. model predicts a dense shell moving at $\sim 4000 \text{ km s}^{-1}$, which is in tension with the $\sim 1000 \text{ km s}^{-1}$ width of spectral lines observed at late times.

Here, we resolve this issue. Revisiting the model of Chugai et al. we find that it is more suitable to explain events like SN 1998S. At early times, when the CSM optical depth is large, the CDS and the SN ejecta are all obscured. Some spectral lines appear with a distinct IIn morphology, with a narrow core and extended wings, all arising from photons re-processed within the slow unshocked CSM. Most lines show a second and narrower component, associated with the more distant and cool CSM. However, as time progresses and the CSM optical depth becomes only a few, a large fraction of the photons emitted by the CDS is no longer re-processed by the CSM. For a CDS velocity of a few 1000 km s^{-1} , the Doppler effect dominates line broadening. In our model A (and by extension the corresponding model of Chugai), the SN spectrum evolves from a IIn morphology to a pure absorption spectrum, where the flux forms within the CDS. The lack of an emission component stems from the very steep density profile at the (outer) edge of the CDS. The SN enters a third phase when the CDS becomes optically thin. The SN radiation then comes primarily from the inner slower unshocked ejecta, while the CDS located further out contributes primarily through broad emission in $H\alpha$ and the Ca II triplet at 8500 \AA .

These three phases predicted by our model A are observed in SN 1998S (with slight temporal offsets). Our analysis demonstrates that the CDS is not obscured at late times. More generally, the CDS is likely seen in all interacting SNe at late times. But the implication is that SNe like 1994W, which never show broad lines, cannot be explained by an interaction involving a massive energetic ejecta ramming into a less massive CSM since it would produce a fast moving CDS. As our grid of explosions has shown, configurations involving an inner shell of moderate mass and energy interacting with a massive slow outer shell (e.g. models R1 and B1) produce a CDS with a low velocity, compatible with the observations of SN 1994W.

Such a configuration can probably arise in many different ways in nature. Here, we invoke the context of nuclear flashes in low-mass massive stars (Weaver & Woosley 1979; Woosley & Heger 2015). We produce two subsequent explosions in a low-mass RSG star of $12 M_{\odot}$ on the main sequence. The first explosion, which mimics the effect of a nuclear flash, ejects the loosely bound H-rich envelope, producing a $\approx 6 M_{\odot}$ ejecta with a mean mass-weighted velocity of $\approx 400 \text{ km s}^{-1}$. The second explosion corresponds to the terminal gravitational collapse of the star left behind, producing a $0.3 M_{\odot}$ ejecta with a kinetic energy of the order of $7\text{--}8 \times 10^{49}$ erg

ejecta with a mean mass-weighted velocity of 4740 km s^{-1} . We perform two simulations (models C and D) with an initial radius of interaction at 0.2 and $1.8 \times 10^{15} \text{ cm}$.

This mass/energy configuration leads to a very different type of interaction compared to model A, while the differing interaction radius between models C and D introduce more subtle differences. In model C, the low-mass inner shell is completely decelerated within 10 d of the onset of the interaction. About 50 per cent of its kinetic energy is converted to internal energy, trapped in the interaction region. Without this interaction, the first exploded shell would appear as a very faint ($\sim 10^7 L_{\odot}$) narrow-line SN II-P (such events likely exist and are missed by current surveys). With the interaction the internal energy of the outer shell is boosted, causing its temperature to increase. A sizeable part of the outer shell material that had recombined is then reionized, pushing the photosphere out in both mass and radius. The combination of low velocity, large radii, and partial ionization above the photosphere lead to a IIn spectral morphology at early times. Importantly, as the ejecta cools and recombines, the spectrum reddens, the electron scattering wings weaken, the photosphere recedes, and the line profiles narrow. All these properties are observed in SN 1994W and shown by model C. Model C is, however, somewhat discrepant because it underestimates the bolometric luminosity of SN 1994W, and then overestimates it at late times: model C remains luminous for 200 d after the onset of interaction. This discrepancy is cured with model D by invoking a larger initial interaction radius.

In model D, the length scales are much larger so the deceleration of the inner shell takes longer. The interaction region has a lower optical depth, producing a light curve that now matches satisfactorily the observations of SN 1994W. Although the shock survives throughout the high-brightness phase, the CDS velocity is never large, and quickly drops to $\sim 1000 \text{ km s}^{-1}$, as in model C. The spectral evolution of models C and D is therefore comparable, and compatible to that of SN 1994W (because of a lower gas temperature in the CSM, the spectral evolution of model D reproduces better the observations of SN 1994W than model C, for example with weaker and shorter lived He I lines, like $\text{He I } 6678 \text{ \AA}$). The spectral simulations of Dessart et al. (2009), which were not based on a radiation hydrodynamical model, correspond to a configuration similar to model D.

While we were finalizing this paper and preparing for submission, a study of SN 2011ht by Chugai (2015) came out. Chugai's work has a lot of overlap with the present work but it uses an independent and very different approach. Still, the conclusions by and large agree and give further support to the notion that SNe like 1994W or 2011ht result from the interaction of a low-mass ejecta with an extended, slow, and massive outer shell. One distinction is that Chugai argues for fragmentation to explain the ~ 100 d high-brightness phase of SN 2011ht while we argue that the duration of the high-brightness phase can be modulated simply by invoking a different interaction radius (model D versus model C).

Models that invoke an interaction of two shells can produce large luminosities. This is because SNe generally have a huge kinetic energy reservoir, which exceeds by a factor of about 100 the time-integrated luminosity of a standard SN. Interaction with CSM is an efficient process to tap into this energy reservoir. The norm in an interacting SN is therefore to be superluminous. In the model of Chugai et al., the CSM is much less massive than the inner shell, so the deceleration is weak and the high energy available in the inner shell is hardly tapped. But the consequence is the formation of a fast moving CDS, which we demonstrated is incompatible with the observations of SN 1994W. Both SN 2011ht and SN 2011A (de

Jaeger et al. 2015) show a similar spectral evolution to SN 1994W but are characterized by even lower peak visual magnitudes (of the order of -16 mag). Our models C and D, and possible incarnations of that scenario that retain the principle of a low/moderate-mass energetic inner shell exploding within a massive slow moving outer shell, seem much more suited to explain these events than models in which a massive inner shell rams into a CSM of much lower mass. One plausible circumstance for this type of interaction is a nuclear flash shortly before core collapse in a low-mass massive star (Woosley & Heger 2015).

The designation of SN 1994W-like events as SN IIn-P (Mauerhan et al. 2013) aims to distinguish them from the broader diversity of SNe IIn. But the designation is somewhat controversial, in part because light curves tend to be degenerate – distinct models can produce identical light curves. The nebular flux of SN 1994W may be explained by invoking a low amount of ^{56}Ni , but it can also be explained by invoking an interaction with a lower density CSM and no ^{56}Ni at all. The origin of the nebular flux is ambiguous, especially in an object that showed strong signs of interaction early on, and therefore it cannot be decisive. The ‘P’ might suggest a connection to SNe II-P, but these result from a point explosion in a RSG star and are thus distinct. In our SN IIn simulations (and in observations), the post-maximum brightness can show a range of decline rates, often incompatible with a plateau designation. Interestingly, the light curves of SN 1998S and SN 1994W are somewhat similar. What is strikingly different between the two types of events is the spectral evolution. SN 1994W-like events differ from all other SNe by the presence of narrow lines *at all times* – SN 1998S shows narrow lines at early times but broad lines (reminiscent of a SN II-P/II-L) at late times. This feature is missed in the IIn classification since many SNe IIn exhibit narrow lines only for a short time. So, perhaps a better designation for SN 1994W-like events would be as Type IInn, to emphasize the persistence of narrow lines at all times.

What distinguishes narrow line SNe II-P from SNe IIn like 1994W are their low luminosity: a fresh supply of energy to a low-energy SN II-P boosts its luminosity but hardly affects its expansion rate. So SNe IIn that would form through the scenario of model C should be characterized by a large brightness for their inferred expansion rate, which would go against the correlation between optical brightness and expansion velocity seen in SNe II-P (Hamuy & Pinto 2002). LSQ13fn is a SN that exhibits such peculiar properties, including evidence for ejecta/CSM interaction at early times (Polshaw et al. 2015).

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APPENDIX A: INITIAL INTERACTION CONFIGURATIONS FOR MODELS A AND C

This section contains figures describing the initial conditions for the HERACLES simulations for models A, C, and D.

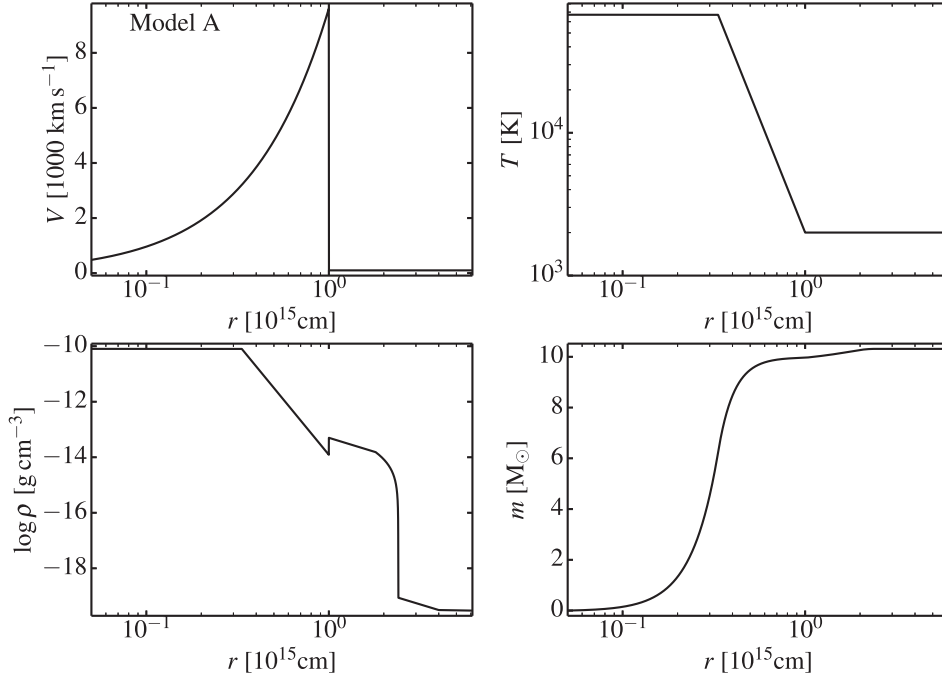


Figure A1. Interaction configuration of model A used as initial conditions for the HERACLES simulations.

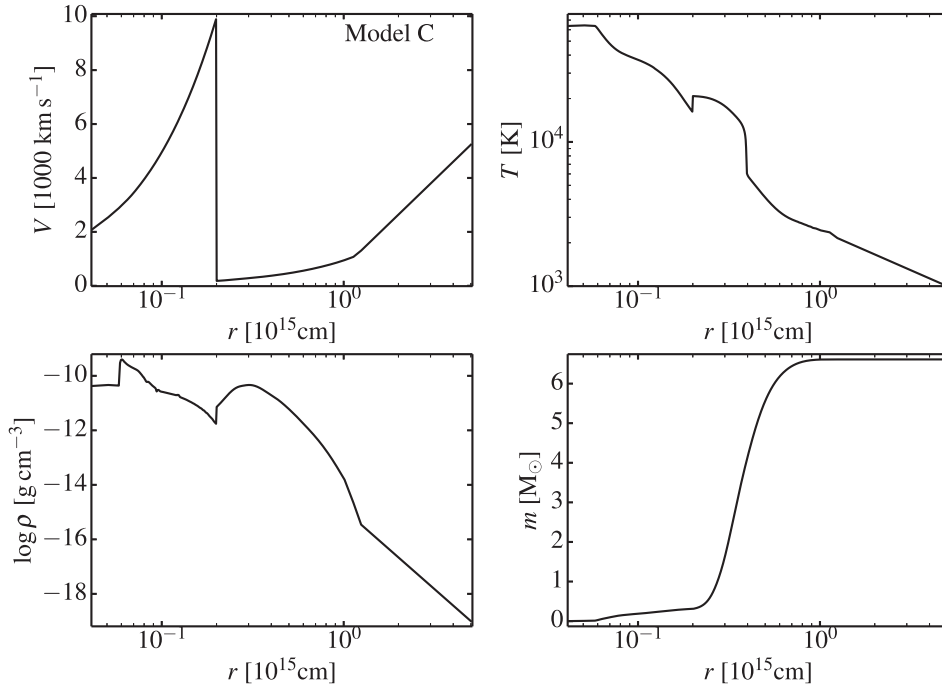


Figure A2. Interaction configuration of model C used as initial conditions for the HERACLES simulations. The outer shell and the inner shell were simulated separately with v1D to mimic a nuclear flash at the base of the H-rich envelope and the final core collapse, respectively.

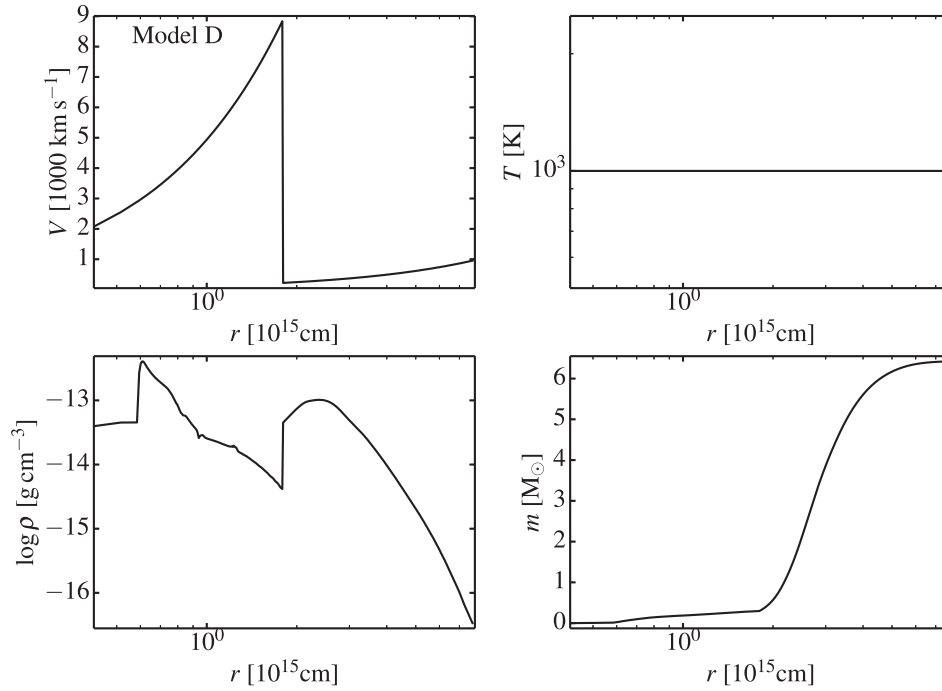


Figure A3. Interaction configuration of model D used as initial conditions for the HERACLES simulations. The outer shell and the inner shell were simulated separately with `v1D` to mimic a nuclear flash at the base of the H-rich envelope and the final core collapse, respectively. This model is similar to model C, but the radius where the two shells start interacting is located further out, at about 1.8×10^{15} cm. Both shells are optically thin and cold initially – for convenience we reset the initial temperature to a floor value of 1000 K.

APPENDIX B: DFR PLOTS FOR MODELS A

This section provides additional information on the spectrum formation computed by `CMFGEN` for the interaction configuration of model A simulated with `HERACLES`. Details on how to interpret these figures can be found in Dessart et al. (2015).

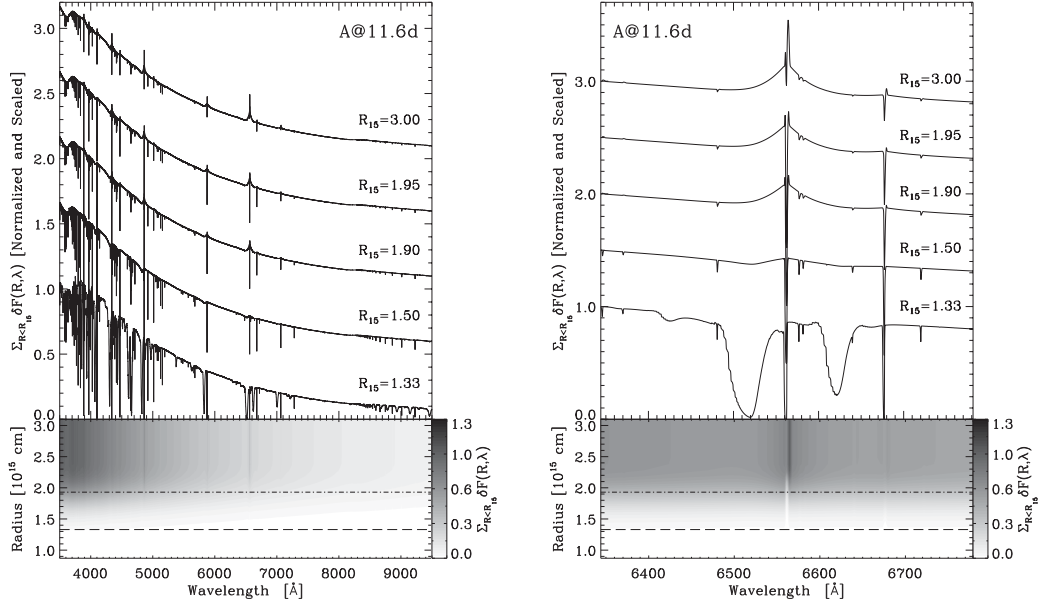


Figure B1. Illustration of the wavelength (λ) and depth (R) dependence of the quantity $\sum_{R<R_{15}} \delta F(R, \lambda)$ for model A at 11.6 d after the onset of interaction. Here, $\delta F(R, \lambda)$ represents the contribution to the observer's flux at wavelength λ originating in a shell of width ΔR at radius R . It is defined by $\delta F(R, \lambda) = (2\pi/D^2) \int_{\Delta R} \Delta z \eta(p, z, \lambda) e^{-\tau(p, z, \lambda)} p dp$; R_{15} is R in units of 10^{15} cm; D is the distance; ΔR and Δz are the shell thickness in the radial direction and along the ray with impact parameter p , respectively; $\eta(p, z, \lambda)$ and $\tau(p, z, \lambda)$ are the emissivity and the ray optical depth at location (p, z) and wavelength λ . The grey-scale in the bottom panel shows how $\sum_{R<R_{15}} \delta F(R, \lambda)$ varies as we progress outwards from the inner boundary, indicating the relative flux contributions of different regions. If we choose R_{15} as the maximum radius on the `CMFGEN` grid, we recover the total flux. The dash-dotted line corresponds to the radius of the electron scattering photosphere, and the dashed line corresponds to the CDS radius. The top panel shows selected cuts (see right-hand label) of the quantity $\sum_{R<R_{15}} \delta F(R, \lambda)$. From top to bottom ($R_{15} = 3.0, 1.95, 1.90, 1.50$, and 1.33), $\sum_{R<R_{15}} \delta F(R, \lambda)$ represents 1, 0.83, 0.73, 0.19, and 0.003 of the total emergent flux at 6800 \AA . Right: same as left, but now zooming in on the $H\alpha$ region. At this epoch, the bulk of the observed radiation originates in the CSM.

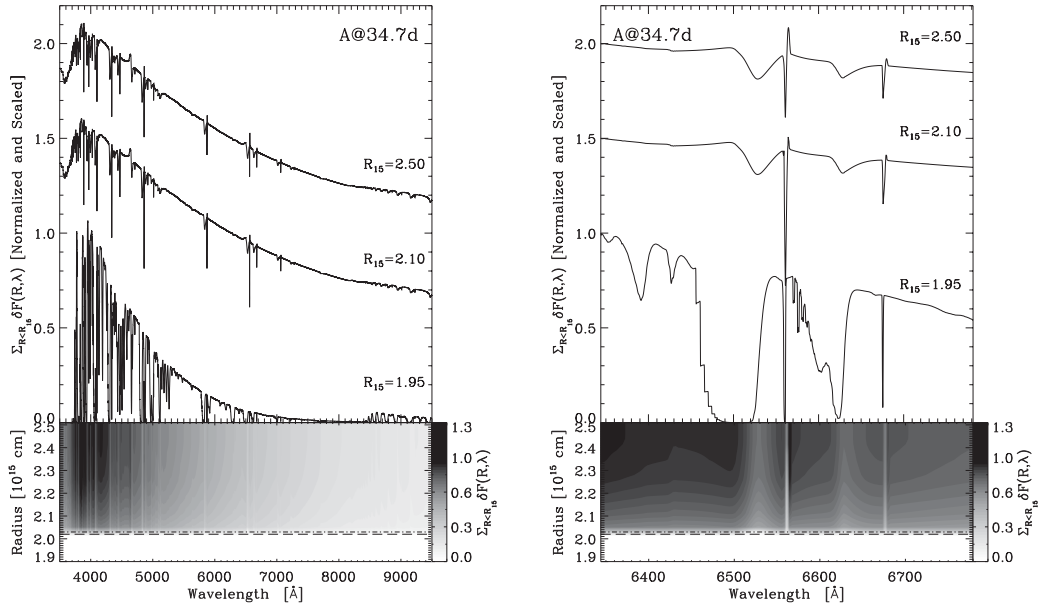


Figure B2. Same as Fig. B1, but now at 34.7 d after the onset of interaction. In the bottom panel and from top to bottom ($R_{15} = 2.5, 2.1$, and 1.95), $\sum_{R<R_{15}} \delta F(R, \lambda)$ represents 1, 0.95, and 0.0001 of the total emergent flux at 6800 \AA . The CDS is optically thick, and most of the observed radiation originates in the CDS. The electron scattering photosphere (i.e. where $\tau_{\text{es}} = 2/3$) now lies within the CDS.

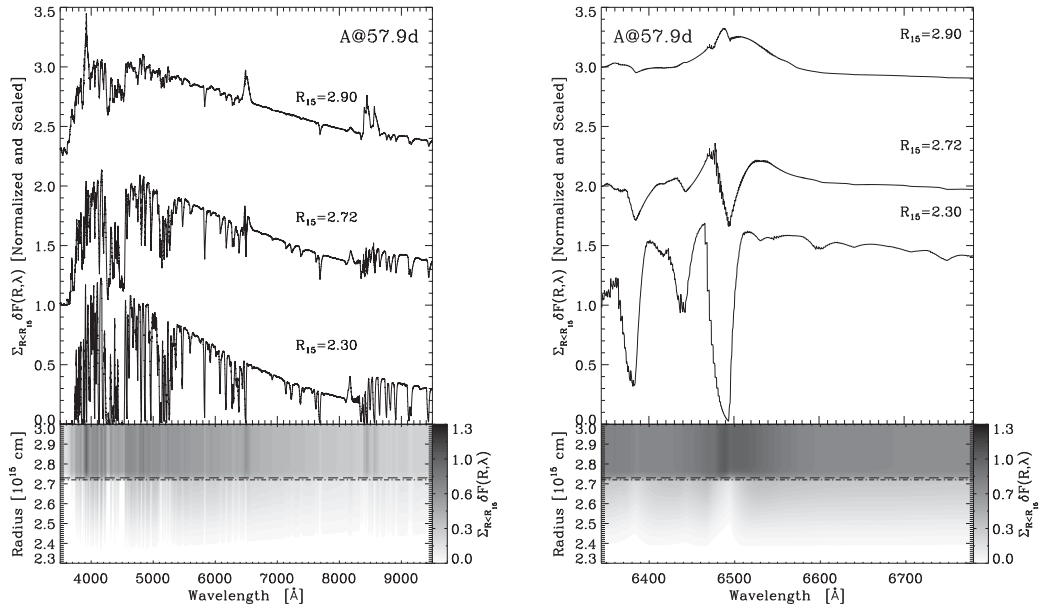


Figure B3. Same as Fig. B1, but now at 57.9 d after the onset of interaction. In the bottom panel and from top to bottom ($R_{15} = 2.9, 2.72,$ and 2.3), $\sum_{R < R_{15}} \delta F(R, \lambda)$ represents 1, 0.52, and 0.0007 of the total emergent flux at 4010 Å. The CDS is becoming transparent, and emission from the inner shell is starting to directly escape to the observer. However, at this epoch, the observed emission is still dominated by the CDS.

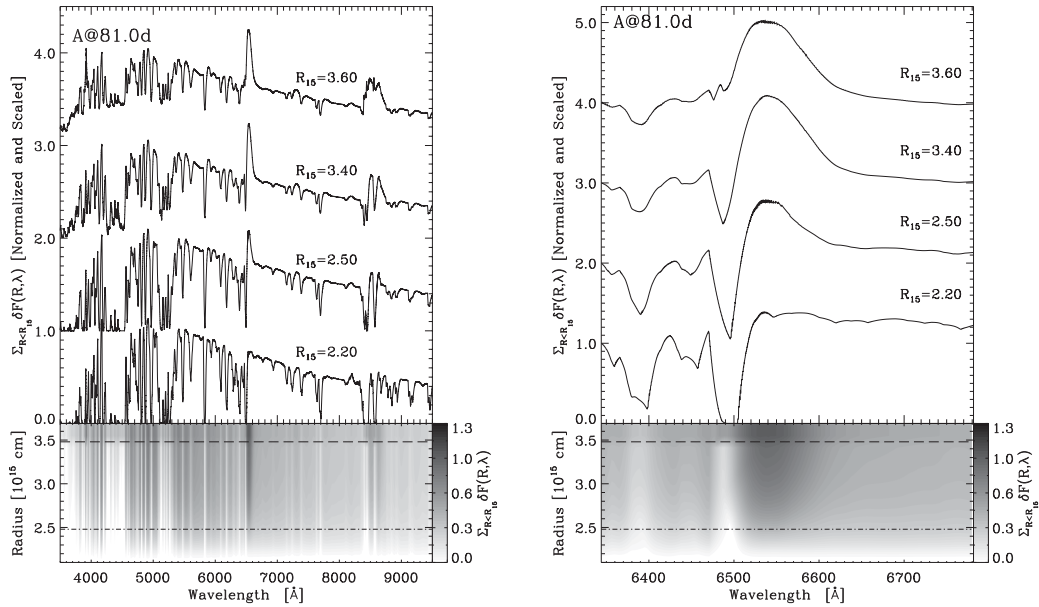


Figure B4. Same as Fig. B1, but now at 81.0 d after the onset of interaction. In the bottom panel and from top to bottom ($R_{15} = 3.6, 3.4, 2.5,$ and 2.2), $\sum_{R < R_{15}} \delta F(R, \lambda)$ represents 1.0, 0.93, 0.58, and 0.16 of the total emergent flux at 4930 Å. At this epoch, the CDS is almost fully transparent and most of the emission arises from the inner ejecta (shell). Emission from the CDS fills in many of the absorption features normally associated with a Type II SN.

APPENDIX C: DFR PLOTS FOR MODELS C

This section provides additional information on the spectrum formation computed by CMFGEN for the interaction configuration of model C simulated with HERACLES. Details on how to interpret these figures can be found in Dessart et al. (2015).

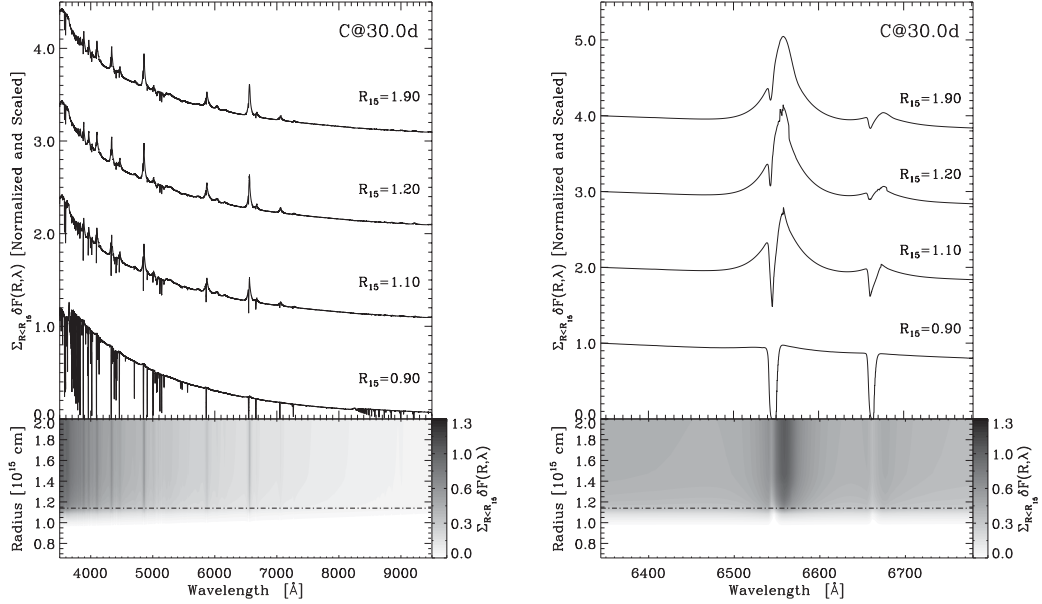


Figure C1. Same as Fig. B1, but now for model C at 30.0 d after the onset of interaction. In the bottom panel and from top to bottom ($R_{15} = 1.9, 1.2, 1.1,$ and 0.9), $\sum_{R < R_{15}} \delta F(R, \lambda)$ represents 1.0, 1.07, 0.72, and 0.002 of the total emergent flux at 3950 Å. At this epoch, the CDS is located deep within the optically thick CSM.

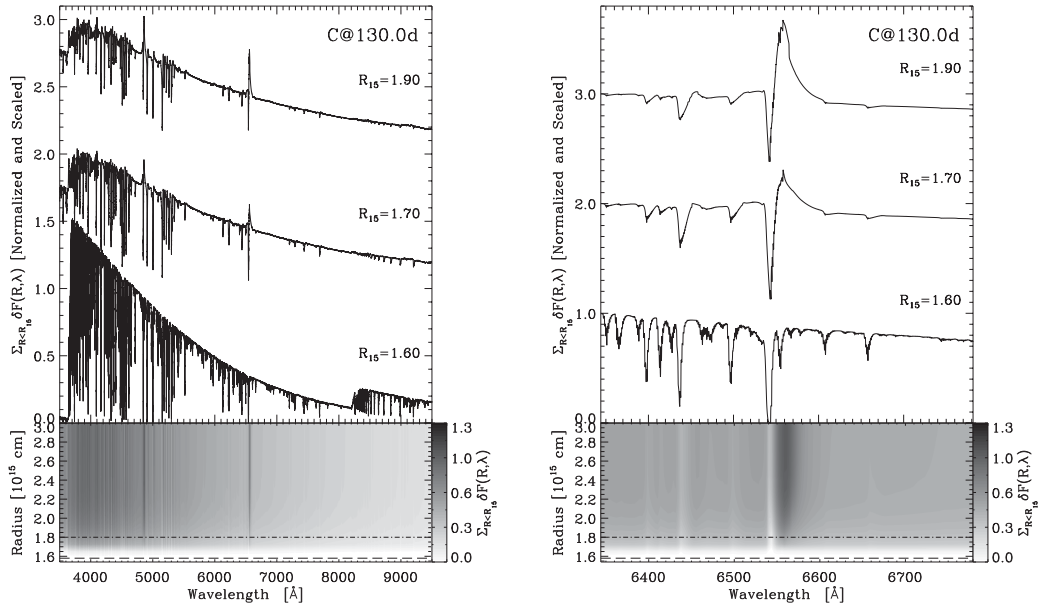


Figure C2. Same as Fig. C1, but now at 130.0 d after the onset of interaction. In the bottom panel and from top to bottom ($R_{15} = 1.9, 1.7,$ and 1.6), $\sum_{R < R_{15}} \delta F(R, \lambda)$ represents 0.99, 0.81, and 0.006 of the total emergent flux at 4100 Å. At this epoch, the CDS is located deep within the optically thick CSM.

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