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To cite this version:

H Elnaggar, Ph Sainctavit, A. Juhin, S. Lafuerza, F. Wilhelm, et al.. Non-collinear ordering of the orbital magnetic moments in magnetite. Physical Review Letters, 2019 , 123 , $10.1103/Phys \rm\,RevLett.123.207201$. $\rm\,hal-02349259$

HAL Id: hal-02349259 <https://hal.science/hal-02349259>

Submitted on 5 Nov 2019

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¹ Non-collinear ordering of the orbital magnetic moments in magnetite

The magnitude of the orbital magnetic moment $[1-9]$ and its role as a trigger of the Verwey transition $[10-17]$ in the prototypical Mott insulator, magnetite, remain contentious. Using $1s2p$ resonant inelastic X-ray scattering magnetic linear angular distribution (RIXS-MLAD), we prove the existence of non-collinear orbital magnetic ordering and infer the presence of dynamical distortion creating a polaronic precursor for the metal to insulator transition. These conclusions are based on a subtle angular shift of the RIXS-MLAD spectral intensity as a function of the magnetic field orientation. Theoretical simulations show that these results are only consistent with non-collinear magnetic orbital ordering. To further support these claims we perform Fe K-edge X-ray magnetic circular dichroism (XMCD) in order to quantify the iron average orbital magnetic moment.

Magnetite $([Fe^{3+}]_A[Fe^{3+}, Fe^{2+}]_BO_4)$ is the most abun- α insulators [23] ask for a new approach. is dant iron bearing mineral on Earth and it finds many $\bullet\bullet$ In this work we employed a combination of Fe K-edge 16 applications in areas such as palaeomagnetism, medicine, $\bullet\bullet$ XMCD and 1s2p RIXS-MLAD measurements to investi-17 data recording, and engineering [18]. Ever since Verwey's so gate the orbital magnetic moment of Fe in Fe₃O₄. Exper-18 pioneering work [19], an immense amount of research has $\overline{}$ iments at the Fe K-edge $(1s \rightarrow 3d + 4p)$ excitations) have been dedicated to Fe₃O₄ in view of its importance as a ₅₂ a probing depth of few μ m and hence surface effects are 20 reference for systems exhibiting the metal to insulator $\overline{}$ s negligible offering a valuable advantage over $L_{2,3}$ -edge 21 transition [11, 20, 21]. In Fe₃O₄, the Verwey transition $\overline{}$ measurements. We quantified the average orbital mag-22 occurs at $T_V \sim 125 \,\mathrm{K}$ and results in a spontaneous change so netic moment by performing K-edge XMCD. The accu-23 of both, the lattice symmetry and the electric conductiv- ϵ rately measured 1s2p RIXS-MLAD signal was used to 24 ity. Above T_V Fe₃O₄ has a cubic inverse spinel crystal \vert 57 determine the average square orbital magnetic moment 25 structure containing two different Fe sites. Fe^{3+} ions re- $\frac{1}{5}$ which complements the average quantity obtained from 26 side in tetrahedral (T_d) interstices (the A sites) while 50 XMCD. A difference between the orbital magnetic mo-27 both Fe²⁺ and Fe³⁺ ions reside in octahedral (O_h) inter- \bullet ment predicted by both experiments indicates compensa-²⁸ stices (the B sites). The A and B sublattices are anti-⁶¹ tion: the orbital magnetic moments of the Fe ions must ²⁹ ferromagnetically coupled while the Fe ions in the same ⁶² be either antiparallel or non-collinear. ³⁰ sublattice are ferromagnetically coupled (Fig. 1a).

³² bital magnetic moments of the transition metal ions can ⁶⁵ sults is the existence of a non-collinear magnetic orbital 33 be directly quantified by applying the sum rules on the ⁶⁶ ordering that can tilt the orbital magnetic moment as 34 $L_{2,3}$ XMCD signal [22]. In spite of the great success of σ large as 82° away from the spin magnetic moment. We ³⁵ sum rules, the experimental and analysis procedures were ⁶⁸ proposed a model for this non-collinear orbital magnetic ³⁶ shown to be prone to huge uncertainties due to surface $\bullet\bullet$ ordering and inferred the presence of a dynamical distor-³⁷ effects [1]. Orbital magnetic moments as small as $0.01 \mu_{\rm B}$ ⁷⁰ tion related to the X_3 phonon mode in the high tempera- $_{38}$ [2] and as large as $0.33\,\mu_{\rm B}$ [3] were reported for Fe₃O₄. τ_1 ture phase. Our model imposes strong restrictions on the ³⁹ In addition, large orbital magnetic moment contributions ⁷² candidate mechanisms for the Verwey transition [10, 24]. ⁴⁰ that are of equal absolute values but with antiparallel ⁷³ We investigated highly stoichiometric (001), (110) and \bullet coupling between the Fe A and B sublattices were also \bullet (111) Fe₃O₄ single crystals at room temperature. The avas suggested [4] (for a unit formula of Fe₃O₄: Fe_B $\mu_L = \tau_5$ erage orbital magnetic moment projected along the mag-43 1 μ B and Fe_A μ _L = -1 μ B). A summary of the orbital τ netic field direction can be quantified by performing Fe K and spin magnetic moments reported in literature using τ pre-edge XMCD measurements [22]. Three main dichroic 45 various techniques is shown in Fig. S1. These large dis- \rightarrow features can be seen at $E_I = 7112.7 \text{ eV}, E_{II} = 7114 \text{ eV}$ **46** crepancies regarding an essential quantity to many Mott \rightarrow and $E_{III} = 7115.1 \text{ eV}$ with only significant angular de-

In ferromagnets and ferrimagnets, the spin and or- ϵ_4 only possibility to explain both of our experimental re-⁶³ Guided by theoretical calculations, we show that the ⁸⁰ pendence at the first feature (Fig. 1b). The co-existence \bullet 1 of two Fe sites in Fe₃O₄ complicates the direct analysis 82 of the XMCD signal and renders a full calculation impor-83 tant to assign spectral features to the specific Fe species. ⁸⁴ Configuration interaction calculations taking into ac- \bullet s count *i*)- intra-atomic Coulomb interaction, *ii*)- crystal \bullet field, iii)- spin-orbit coupling, and iv)- exchange inter-⁸⁷ action were performed using the quantum many-body \bullet s program Quanty $[25-27]$. Our theoretical simulations \bullet show that the feature at E_I arises mainly from electric \bullet quadrupole transitions (*i.e.* 1s \rightarrow 3d excitations) at the **or** formal Fe²⁺ ions while the features at E_{II} and E_{III} arise mainly from electric dipole transitions (*i.e.* $1s \rightarrow 3d+4p$ excitations) at the Fe³⁺ T_d ions due to onsite $3d - 4p$ orbital mixing as discussed by Westre $et.$ al. [28]. The \bullet quadrupolar signals from the Fe³⁺ A and B sites nearly ⁹⁶ cancel out as shown in Fig. S8.

⁹⁷ The experimental XMCD signal and its angular de-⁹⁸ pendence can be best interpreted to arise from a par-⁹⁹ tially quenched orbital magnetic moment at the formal $Fe²⁺$ ions. An excellent agreement between the calcu-¹⁰¹ lation and the experiment is observed (compare spectra ¹⁰² labelled Exp and Calc 1 in Fig. 1b). This partial quench-¹⁰³ ing is a result of the octahedral symmetry accompanied 104 by a small trigonal distortion $(D_{\sigma} = 67 \pm 10 \,\text{meV})$. The 105 Fe environment is not perfectly O_h since the point group 106 symmetry of the B site is rhombohedral $(D_{3d} \equiv \overline{3}m)$. ¹⁰⁷ We found that the average orbital magnetic moment is 108 $0.26 \pm 0.03 \mu_{\rm B}$ per unit formula of Fe₃O₄. It is impor-109 tant to note that feature I is theoretically predicted to 136 the experimental dichroism signal (Fig. 2b). Theoretical 110 be completely suppressed in the case that $\mu_L = 0 \mu_B$ (see 137 calculation of the RIXS dichroism signal shows that the 111 Fig. 1b Calc 2) strongly supporting the presence of a 138 quadrupolar contributions of the Fe³⁺ T_d and O_h sites $\,$ 112 finite orbital magnetic moment in bulk Fe3O4.

113 To investigate possible non-collinearity of the orbital 140 tures labelled in Fig. 2b are dominantly attributed to the 114 magnetic moment, we performed comprehensive $1s2p$ 141 formal Fe^{2+} ions. This is consistent with the XMCD re-¹¹⁵ RIXS-MLAD measurements. This complements the av-¹⁴² sults, where we found that the angular dependence is only 116 erage projected result obtained from XMCD. The RIXS- 143 visible at the Fe^{2+} ions. The calculated RIXS dichroic 117 MLAD was measured by rotating the sample about the 144 plane of the formal Fe^{2+} ions reproduces the three main 118 incident wave-vector direction (k_{in}) aligned with the 145 spectral features. The calculation only misses a weak fea-110 direction (refer to Fig. 2a). This implies that the 146 ture at incident energy $\sim 7115.1 \text{ eV}$ which is associated 120 RIXS-MLAD includes contributions from both structural 147 with the electric dipole transition at the Fe^{3+} A site due 121 and magnetic dichroism signals. We focus in this work on μ ⁴⁸ to onsite 3d – 4p orbital mixing. 122 the effect of the magnetic dichroism on the linear angular 149 The full 360° experimental (theoretical) angular de-123 distribution of RIXS. We initially measured the RIXS-150 pendence of the three main spectral features can be seen 124 MLAD with the magnetic field *nearly* parallel to k_{in} as $\overline{151}$ in Fig. 2c. The angular dependence is twofold and a 125 a reference measurement. In this case the magnetic field 152 90° angular shift is observed between the first feature ¹²⁶ is oriented along a high symmetry crystallographic direc-¹⁵³ and both the second and third features. A first expla-¹²⁷ tion and the angle between the linear incident polariza-¹⁵⁴ nation of the general angular dependence can be pro-128 tion (ϵ_{in}) and the magnetic field nearly does not change 155 vided by analysing the $1s^13d^7$ intermediate states. Pro-¹²⁹ as a function of the sample rotation. These choices sim-¹⁵⁶ jections of the intermediate states associated with non-¹³⁰ plify the angular dependence and serve as a benchmark ¹⁵⁷ zero transition matrix elements onto cubic crystal field ¹³¹ to analyze the RIXS spectra.

133 the horizontal ($\phi = 0^{\circ}$) and vertical ($\phi = 90^{\circ}$) config-160 nantly from excitations to the t_{2g} orbitals, that are 90° 134 urations show a broad single pre-edge peak (Fig. $S9a$ 161 angular shifted w.r.t. the second and third features cor-135 and b), it is possible to identify three main features in 162 responding to excitations dominantly into the e_g orbitals

FIG. 1. (a) The unit cell of $Fe₃O₄$ and the magnetic coupling between the Fe sites. Octahedral (O_h) Fe³⁺ and Fe²⁺ ions are antiferromagnetically coupled to the tetrahedral (T_d) Fe³⁺ ions. (b) Fe K-edge measurements in $Fe₃O₄$ single crystal. The top panel shows XAS results as a function of the sample azimuthal angle θ . The bottom panel shows the corresponding XMCD experimental (dotted) and theoretical (solid) Fe preedge signal. Two model calculations are presented: i)- Calc 1 is the optimized calculation where a partially quenched orbital magnetic moment of $0.26 \mu_{\rm B}$ per unit formula of Fe₃O₄ was concluded, and ii)- Calc 2 is the theoretically expected XMCD signal for a fully quenched orbital magnetic moment scenario.

139 nearly cancel out (see Fig. S10) and hence the three fea-

132 Although the experimental RIXS planes measured in 150 gram CTM4DOC [29]. The first feature arises domi-158 (*i.e.* O_h) configurations were calculated using the pro [28]. We note that the angular dependence is anisotropic ²¹⁸ An energy shift of ∼ 0.2 eV was found between the two 164 where the intensity of the third feature at $\phi = 180^\circ$ is 219 subclasses.

165 smaller than that at $\phi = 0^{\circ}$. This is related to the 220 We interpret the formation of these two subclasses as anisotropy in the detection in combination to a small ²²¹ a result of a dynamical Jahn-Teller distortion at the Fe $\overline{\text{167}}$ misalignment angle (δ) of the magnetic field relative to $\overline{\text{222}}$ B sites. The magnitude of the static trigonal distortion 168 the rotation axis *i.e.* the detector position relative to $_{223}$ lies close within the phonon energies of Fe₃O₄ [30, 31], the sample as discussed in details in the Supplementary. ²²⁴ the magnetic exchange interaction and spin-orbit cou-170 In addition, our theoretical model assumes that the de- 225 pling, leading to a situation where electron-phonon in-₁₇₁ tection system is a single point while in reality four Ge ₂₂₆ teraction, dynamical Jahn-Teller and Kugel-Khomskii in- (440) analyzer crystals were used. The minor discrep-²²⁷ teractions all play a role in determining the low energy ancy between the experiment and the calculations could ₂₂₈ state. We treat this dynamical variation of the distor-be attributed to this fact.

 We examined the coupling of the spin and orbital degrees of freedom by displacing the magnetic field 50◦ 177 from the high symmetry [001] direction (refer to Fig. 3a). The orientation of the magnetic field corresponds to 179 the $\left[\frac{-\cos(40^{\circ})}{\sqrt{2}}, \frac{\cos(40^{\circ})}{\sqrt{2}}, \sin(40^{\circ})\right]$ direction. Orienting the magnetic field in a low symmetry direction aligns the net spin magnetic moment parallel to the field. If the orbital magnetic moment is not fully quenched, it consequently re-aligns towards the low symmetry direction. The final orientation of the net magnetic moment depends on the strength of the competing interactions such as magnetic exchange, spin-orbit coupling and distortion. Hence, the angular shift of the maximum intensity of the excitations can be used to quantify magnetic-moment-induced dis- tortion of the electron cloud. Based on this concept, we investigated the orbital magnetic moment of the formal Fe^{2+} ions. A careful analysis of the full 360 $^{\circ}$ angular dependence exhibits a peculiar 10◦ angular shift of the maximum intensity between the second and third fea-tures in Fig. 3b.

 presented in Fig. 3c. The model captures the essential ²⁵² our observation. 197 aspects of the angular dependence and in particular the 253 198 10[°] angular shift of the maximum intensity. The an- 254 X-ray spectroscopic measurements on the basis of our 199 gular shift (Ω) quantified by fitting the angular depen-255 model. In particular, we focused on comparing L_3 200 dence to a $cos^2(\phi + \Omega)$ of the three features is reported 256 XMCD [2, 7] and L_3 RIXS [7] measurements to our simu-₂₀₁ in Tab. S4. The anisotropy of the angular dependence is 257 lations. Our model can reproduce the experimental data 202 not well reproduced, likely due to a small misalignment 258 and notably it captures the recently reported L_3 RIXS of the magnetic field that has not been included in the ²⁵⁹ angular dependence well. The existence of this dynam- calculations (see Supplementary). It is now important to ²⁶⁰ ical distortion is furthermore supported by various ex- highlight the key ingredients responsible for this angular ²⁶¹ perimental work such as diffuse scattering experiments shift. The first factor is the static trigonal distortion. ²⁶² using both neutrons [37] and X-rays [38], EXAFS [39], 207 The relative orientation of the exchange interaction with 263 anomalous phonon broadening [40], and pump-probe X- respect to the local trigonal distortion varies between the ²⁶⁴ ray diffraction and optical reflectivity [41]. ₂₀₉ four sites leading to anisotropic effects and generates four ₂₆₅ The presence of four non-equivalent Fe B sites in the non-equivalent Fe B sites. The theoretical RIXS-MLAD ²⁶⁶ high temperature phase has rather interesting implica- ϵ_{211} for the four sites are shown in Fig. S12. The second fac- ϵ_{257} tions. Overall, we find that the average orbital magnetic 212 tor is the effect of dynamical distortion that produces two 268 moment deduced by XMCD and RIXS-MLAD is the 213 subclasses of the Fe B sites, namely, sites 1 and 2 form- 269 same $(0.26 \pm 0.03 \,\mu_B$ per unit formula of Fe₃O₄ as illus- ing one subclass and sites 3 and 4 forming the other (see ²⁷⁰ trated in Fig. 1b and Fig. 4f), however the RIXS-MLAD Fig. 4b). It is only when the dynamical distortion effect ²⁷¹ measurement demonstrates that the average quantity is is taken into consideration that the experimental RIXS-²⁷² not sufficient to describe the orbital magnetic moment $_{217}$ MLAD angular shift can be reproduces (see Fig. S13). $_{273}$ in Fe₃O₄. This is a result of the non-collinear orbital

 Theoretical calculation of the angular dependences are ²⁵¹ sites into two subclasses. This agrees rather well with tion in a first approximation as a small change in the bond lengths over the four sites giving rise to a small en- ergy shift. This is a reasonable approximation because the electronic structure adapts almost instantaneously to the crystallographic structure (*i.e.* the electronic motion is much faster than the nuclear motion). In this case, the effect of phonons could be simulated as a static distribu- tion of bond lengths leading to a shift in energy between the four sites. This is a common practice in XAS theory 238 as can be found in the paper by Nemeusat $et \ al.$ [32] where thermal fluctuations are simulated by a well cho- sen series of configurations. Although theoretical studies that treat simultaneously the electronic and the lattice degrees of freedom are required to comprehend the pre- cise effect of the dynamical distortion, we point out that numerous theoretical works concluded the essential role of the strong electron-phonon coupling in the presence of strong electron correlations leading to dynamical Jahn- $_{247}$ Teller distortion and the creation of polarons $[33-36]$. In 248 particular, Piekarz $et.$ $al.$ $[33, 34]$ identified the highly 249 dispersive X_3 phonon mode as a primary order param-eter of the Verwey transition which splits the four Fe B

We have undergone the task of simulating various

 (a) $[001]$ I (arb. unit) (C) $Φ = 0[°]$ 90o 0.0 135° 45o Experimental: **[-110]** $\Phi(90^\circ$) -Φ(0°) **εin** \mathbf{k}_{in} **[110]** Φ 712 180o 0o δ **B**_{Field} 710 \mathbf{k}_{out} 225° 315° \equiv $\frac{1}{3}$ 708 270° Φ (deg) Norm. I (arb. unit) **[-110]** $Φ = 90°$ 90o 712 135° 45° **εin** \mathbf{k}_{in} 710 Φ **[110]** δ 0o **B**Field **[001]** 708 225° 315° \mathbf{k}_{out} 7112 7114 7116 270 Incident energy (eV) Φ (deg)

FIG. 2. Fe 1s2p RIXS-MLAD measurements. (a) A sketch of the scattering geometry employed. The magnetic field (B_{Field}) is aligned nearly parallel to the incident wave-vector (k_{in}) which corresponds to the [110] direction. (b) Experimental and theoretical dichroism RIXS planes computed as the difference between the RIXS plane at $\phi = 90^\circ$ and at $\phi = 0^\circ$. The full experimental (dotted) and theoretical (solid) 360° RIXS-MLAD signals of the features labelled 1, 2 and 3 in the RIXS dichroic maps are shown in (c) respectively. The angular dependence signal is normalized as: $RIXS - MLAD = \frac{RIXS(\phi) - Min[RIXS(\phi)]}{Max[RIXS(\phi) - Min[RIXS(\phi)]}$.

FIG. 3. Fe 1s2p RIXS-MLAD measurements. (a) A sketch of the scattering geometry employed. The magnetic field (B_{Field}) is aligned to the $\left[\frac{-\cos(40^{\circ})}{\sqrt{2}}, \frac{\cos(40^{\circ})}{\sqrt{2}}, \sin(40^{\circ})\right]$ direc- $(2 + \epsilon a)^2$ is angles to the $\sqrt{2}$, $\sqrt{2}$, $\sqrt{2}$, $\sqrt{2}$, $\sqrt{2}$ is measured by rotating the $\sqrt{2}$ sample about the [110] direction (ϕ rotation). $\phi = 0^{\circ}$ is delated (solid) angular dependence of the three main features (labeled 1, 2 and 3) are shown in panels (b) and (c).

₂₇₄ ordering arising from the interplay between trigonal dis-₃₀₀ ments sensitive to the non-averaged quantity. This or-

 tortion effects (static and dynamical), spin-orbit coupling and exchange interaction at the formal Fe^{2+} ions. The orbital magnetic moment per Fe^{2+} ion is predicted to have a strong dependence on the magnetic field in con- trary to the spin magnetic moment which is collinear to the magnetic field. Fig. 4 illustrates the dependence of the orbital magnetic moments on the orientation of the magnetic field when we rotate it about the [110] direc- tion for the four sites independently. Large non-collinear 284 orbital contributions that tilt as much as 82° away from the magnetic spin moment orientation are present. Fur- thermore, the collinear contribution per site ranges from 0 to 150% of the average quantity as a function of the orientation of the field. Remarkably, the average orbital magnetic moment for the four sites remains nearly con-290 stant (Fig. 4f).

fined when the incident polarization vector (ϵ_{in}) is aligned to $_{294}$ and the magnetic field angular dependence. Experiments the [−110] direction. The experimental (dotted) and calcu-²⁹⁵ sensitive to the effective orbital magnetic moment yield The large discrepancies regarding the orbital magnetic 292 moment of Fe in $Fe₃O₄$ can now be understood in light of the large non-collinear contribution, the site dependency different results to those sensitive to the projected av- erage quantity, or the average of the squared projected quantity. Moreover, variations as a function of the ori-entation of the magnetic field are expected for experi-

FIG. 4. The angular dependence of the orbital momentum (M_L) of the four Fe²⁺ ions as a function of the rotation of the magnetic field (B_{Field}) about the [110] orientation. (a) Sketch of the rotation geometry. The angular dependence of the orbital momentum projected along the direction of B_{Field} and two perpendicular non-collinear contributions are shown in panel (b), (c), (d) and (e). The average orbital magnetic moments of the four Fe^{2+} ions are shown in (f).

301 dering of the orbital magnetic moment is predicted to 357 ³⁰² be short-ranged due to the dynamical distortions at the 303 high temperature phase of Fe₃O₄. The combination of 359 304 1s2p RIXS-MLAD and XMCD provides a powerful tool ³⁶⁰ ³⁰⁵ to quantify site-selectively non-collinear magnetic order-³⁰⁶ ing with bulk sensitivity. Finally, we show that the or-307 bital degree of freedom is an important precursor for the ₃₆₄ 308 Verwey transition in $Fe₃O₄$ given the fact that it is cou-³⁰⁹ pled to a primary order parameter.

310 We acknowledge the staff of beamlines ID12 and ID26³⁶⁷ 311 of the European synchrotron radiation facility for their ³⁶⁸ 312 help in setting up and running the experiments. A. van 313 der Eerden, S. Deelen, P. Theven and H. Vitoux are $\frac{1}{371}$ ³¹⁴ thanked for their efforts in building up the setup. We ³¹⁵ are grateful for P. Zimmerman and A. van der Eerden 316 and A. Ismail for assisting during the synchrotron mea- 374 317 surements at beamline ID26. We are grateful for the ³⁷⁵ 318 fruitful discussions with G. Subías, J. Garcia, J. Blasco ³⁷⁶ ³¹⁹ and V. Vercamer. M. Delgado is thanked for provid-

 ing and assisting us to use the program CTM4DOC. We thank A. Bosak and M. Hussein for their help with the X-ray diffraction measurements and sample characteri- sation. Many thanks to R.-P. Wang for the discussions and suggestions. We acknowledge financial support from COST Action MP1306 (EUSpec). M. Sikora acknowl- edges support from National Science Center of Poland (2014/14/E/ST3/00026). This work was financed by the ERC advanced Grant XRAYonACTIVE No. 340279.

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