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A snapshot of electrified nanodroplets undergoing Coulomb fission

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We investigate the size distribution of electrically charged nanodroplets using atomic force microscopy (AFM). The droplets were generated using nano- and micro-scale silicon tips. A brief voltage pulse results in a “snapshot” of charged nanodroplets on a Cr surface. AFM of the traces left by the nanodroplets revealed that certain droplet diameters are favored suggesting droplet fission due to Rayleigh instability at nanometer length scales. The most occurring droplet diameters are 85.9(4.1) nm and 167.1 nm (9.7 nm) for nano- and micro-scale tips, respectively. © 2012 American Institute of Physics. [doi:10.1063/1.3684979]

In 1882, Lord Rayleigh¹ predicted that a charged droplet will be unstable if the electrical charge q it carries exceeds a value given by

$$q > \sqrt{8\pi^2\gamma\epsilon_0 d^3}, \quad (1)$$

where d is the droplet diameter, γ is the surface tension, and ϵ_0 is the permittivity of free space. Coulomb fission, due to this instability, has recently been observed for micrometer-sized droplets.² We demonstrate, here, a technique to analyze a “snapshot” of charged nanometer-sized droplets under Rayleigh instability. A nanometer-scale silicon tip is used to deposit³ nanodroplets onto a chromium (200 nm) coated silicon wafer. Atomic force microscopy (AFM) of the traces left by the nanodroplets suggests Coulomb fission occurring at these length scales.

The experimental set-up is shown in Fig. 1(a). The tips are composed of two triangular cantilevers attached to a silicon support chip. The two cantilevers define a micrometer capillary slot leading up to a nanometer scale capillary slot at the apex of the tip [Fig. 1(b)]. The tip apex has a nanometer scale channel which was defined using focused ion beam milling.⁴ A nanometer-scale tip was tested which had a channel width of 350 nm (± 10 nm). As a comparison, a micrometer-scale tip⁵ was also tested which had channel width of 1 μm ($\pm 0.1 \mu\text{m}$) [Fig. 1(c)]. The tip is brought into proximity to the Cr coated Si wafer using an xyz positioning stage; the tip-to-plane distance was set to $\sim 100 \mu\text{m}$. The tip is loaded with the liquid ($v \sim 5 \mu\text{l}$) composed of a 75:25 v/v deionized water ($\rho > 10 \text{ M}\Omega \text{ cm}$)-methanol mixture with nitric acid ($c = 0.001 \text{ M}$). A gold wire (diameter = 250 μm) is inserted into the droplet to serve as an electrode. A voltage pulse (0–200 V for 10 ms) is applied to the liquid which causes electrospaying at the apex of the tip.⁶ For a point-to-plane electric field distribution,⁷ the field decreases rapidly in a non-linear fashion in the axial direction away from the point. During the experiments, the electric field at the tip was sufficient to produce electrospaying⁶ and decreases rapidly to $< 4 \text{ kV cm}^{-1}$ at the Cr surface. Arcing behaviour⁸ was

not observed in the current-voltage sweeps but rather a characteristic electrospay current-voltage.⁹ Charged droplets are attracted towards the Cr coated Si wafer which is grounded [Fig. 1(a)]. The time-of-flight of the droplets is calculated to be of the order of tens of microseconds by numerically resolving a point-to-plane electric field model.⁷ Break-up of a cone-jet^{10,11} results in the formation of the electrospay plume as the charged droplets repel each other. During the time-of-flight, the charged droplets which exceed the Rayleigh criterion¹ will undergo Coulomb fission which has been the subject of much research.³ Characterizing the distribution of micrometer-sized charged droplets can be done using optical means.^{2,3,12,13} In contrast, the method

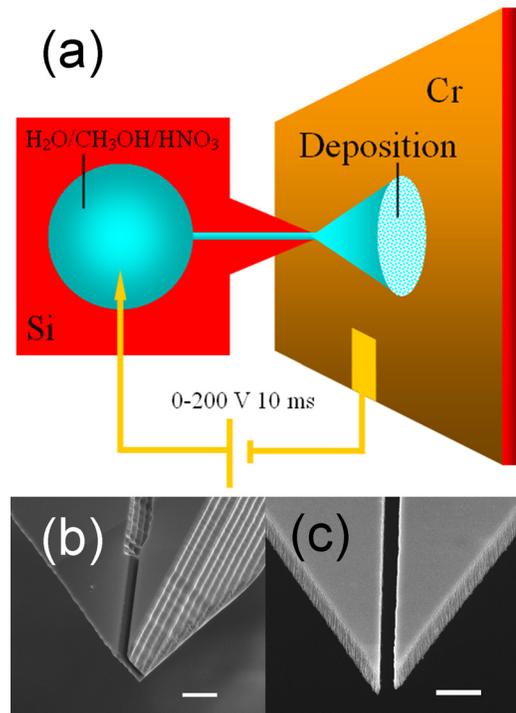


FIG. 1. (Color online) Deposition of nanodroplets onto a metal screen. (a) Experimental set-up showing the nano/micro-machined silicon tip, the liquid (water/methanol/nitric acid), the Cr coated Si wafer, and application of a voltage pulse (0–200 V) between the liquid and the wafer. (b) An SEM image of the nano-scale tip (scale bar = 1 μm). (c) An SEM image of the micro-scale tip (scale bar = 2 μm).

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demonstrated, here, can characterize *individual nanodroplets* according to their size and occurrence. Literature is scarce concerning imaging individual charged nanodroplets originating from an electro spray; scanning electron microscopy and near-field microscopy techniques have been used to characterize nanodroplets deposited onto surfaces.^{14–18} We use near-field microscopy techniques, here, to characterize the traces left by charged nanodroplets after evaporation.

Fig. 2(a) shows an image obtained by tapping-mode AFM imaging (Bioscope, Veeco, USA) of the Cr surface following experiments with the nanotip. The traces are typically composed of a central area $\sim 10\ \mu\text{m}$ in diameter surrounded by a halo⁷ of much smaller sub-micrometer diameter satellite “spots”⁷ characteristic of electrostatic repulsion.¹³ Each satellite spot [Fig. 2(b)] has a central “bump” characteristic of a non-volatile residue¹⁴ possibly due to impurities (rainbow colors in Fig. 2(b), surrounded by a flat “plateau” region [brown in Fig. 2(b)] not reported in the previous studies.^{15–19}

The trace diameters are $\sim 50\ \mu\text{m}$ (inset of Fig. 2(c) which shows that smaller droplets are found towards the periphery of the trace), implying an electro spray plume angle of around 30° ; this is consistent with previous observations.^{7,13}

By analyzing these images we can produce Fig. 2(c) which shows a plot of the normalized spot number (n/N_t ; N_t = total number of spots) versus spot width w for two tips. It is apparent from Fig. 2(c) that certain spot diameters are favored and occur in bunches (see steps in Fig. 2(d) indicated by black arrows). By statistically binning the experimental data presented in Fig. 2(c) using a suitable class interval, we can produce histograms for the spot width w versus droplet occurrence N_{exp} ; the result of this is shown in Figs. 2(e) and 2(f). To explain these results let us recall that a charged droplet distribution has few large droplets (the fissility¹ $X = q^2/8\pi^2\epsilon_0\gamma d^3$ is large) and few small droplets (X is small) but is composed of many droplets of distinct radii in the vicinity of $X \sim 1$; the distributions in Figs. 2(e) and 2(f) are indicative

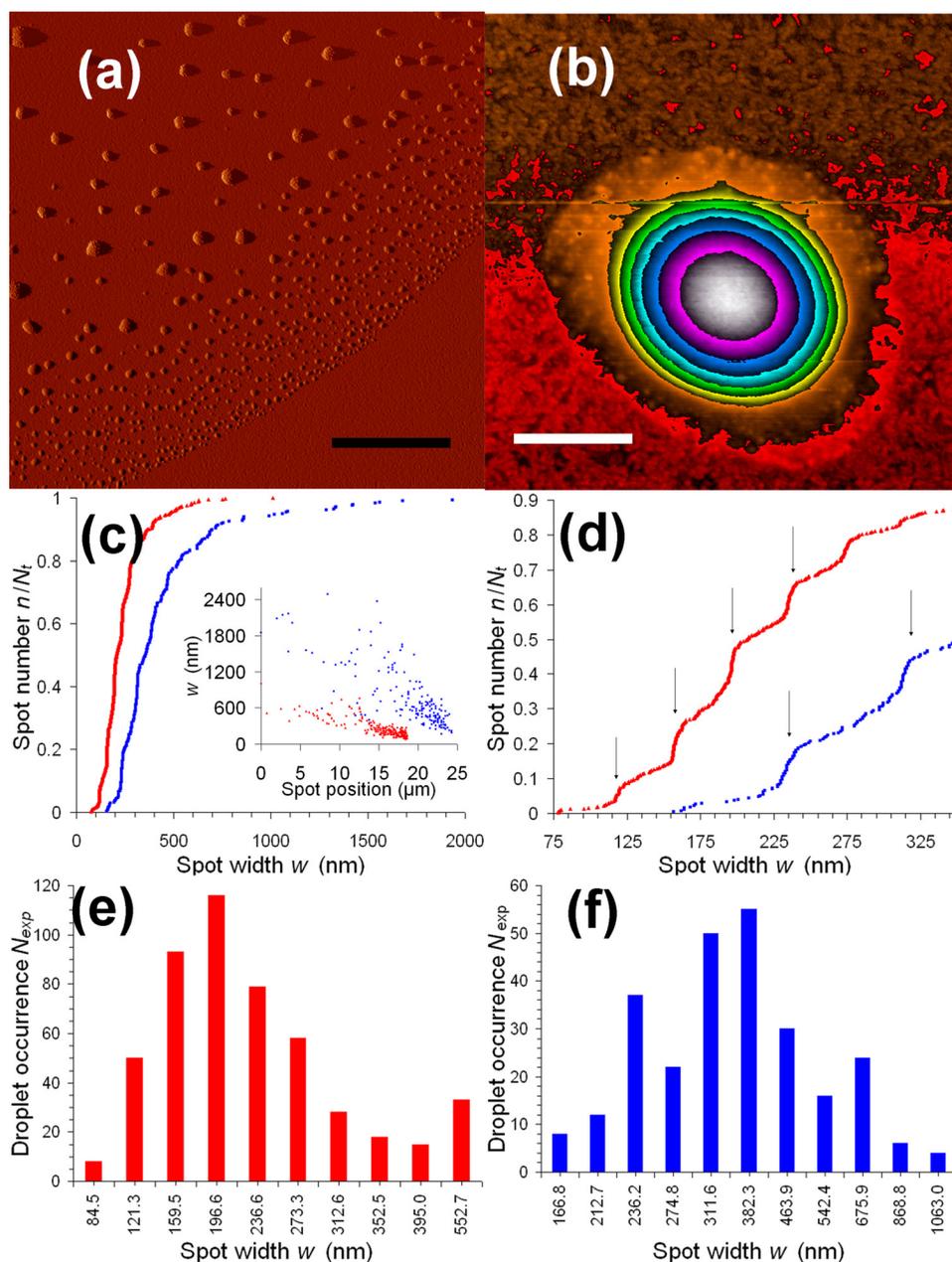


FIG. 2. (Color online) Snapshot of nanodroplets. (a) AFM imaging following experiments using the nano-scale tip (scale bar = $5\ \mu\text{m}$). (b) Zoom on a single spot (scale bar = $500\ \text{nm}$). (c) Plots of the spot number n divided by total number of spots N_t versus the spot width w obtained using the nanotip (red triangles) and the microtip (blue squares) [inset shows spot width versus spot position in trace]. (d) zoom of w versus n/N_t reveals steps in the plots (black arrows). (e) Histogram of spot width distribution using the nano-scale tip (red bars). (f) Histogram of spot width distribution using the micro-scale tip (blue bars).

of this. Traces produced using the nanotip result in a minimum spot width variation of 77.9–1101 nm, whereas microtip results in 157–2578 nm.

In order to interpret our observations, Fig. 3 illustrates a charged droplet impinging on the metal surface where local oxidation²⁰ and desposition²¹ can occur; the result of this is a modification of the surface resulting in a spot having a diameter w . As a first approximation, we can relate w to the original impinging droplet diameter d by using a model based on the macroscopic wetting contact angle θ of the water-methanol-nitric acid mixture on a Cr surface; although it should be noted that a more accurate model would require nanodroplet wetting¹⁵ and charge effects to be taken into account. However, in a first approximation, which ignores droplet deformation due to electric fields,²² as $d = \alpha w$ where $\alpha^3 = (2 - 3\cos\theta + \cos^3\theta)/4\sin^3\theta$ and θ was measured to be $24.7 (\pm 2)^\circ$ using a contact angle meter (Kruss, Germany), we determine the parameter α to be 0.437. This enables a calculation of the experimental droplet diameters (d_{exp}) shown in Tables I and II. The experimental droplet diameters d_{exp} are mean values calculated over the class interval. The observations can be analyzed in terms of (i) droplet size distribution and (ii) volume flow rate.

First, in terms of the droplet size distribution although electrically charged droplet distribution populations are known to be highly complex,²³ a simple fission model based on droplet volume halving can be compared with the experimental results. This simplistic model can check for a signature of droplet break-up at these length scales, presumably due to Rayleigh instability.¹ By choosing an highly occurring droplet diameter d_n (underlined bold values in Tables I and II) observed in the experimental AFM data, we can calculate a set of droplet diameters based on simple volume halving: $V_{n+1} = V_n/2 \Rightarrow d_{n+1} = d_n/\sqrt[3]{2}$; these calculated droplet diameters d_{cal} are shown in Tables I and II along with the experimental droplet diameters d_{exp} . First, the nanotip results in smaller droplets than the microtip). Second, droplet splitting (by halving) is clear from the results both for the nanotip and the microtip. Third, there appears to be two sets of droplet halving happening (single star and double star values for

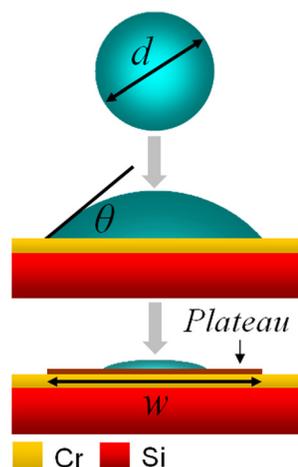


FIG. 3. (Color online) Spot width w and original droplet diameter d : schematic diagram of a droplet impinging a surface having a wetting contact angle of θ .

TABLE I. Experimental (N_{exp} and d_{exp}) and modeling (d_{cal}) results for the nano-scale tip; d_{exp} corresponds to the average experimental original droplet diameter is calculated from w_{exp} (see Figure 3), and the droplet occurrence N_{exp} is the number of spots in the given spot width interval. Droplet diameters corresponding to the $d_{n+1} = d_n/\sqrt[3]{2}$ model are shown starting from the initial bold values. Standard deviations are shown in brackets. Asterisks correspond to related droplet. Asterisks correspond to related droplet.

N_{exp}	d_{exp} (nm)	d_{cal} (nm)
8	36.9(3.4)	34.1*
50	53.0(3.4)	54.1*
93	69.7(3.7)	68.2*
116	85.9(4.1)	85.9*
79	103.4(3.3)	108.2*
58	119.4(3.5)	119.4**
28	136.6(3.7)	136.4*
18	154.0(4.1)	150.5**
15	172.6(2.6)	171.8*
33	241.5(51.3)	238.9**

d_{cal}) which is clear from the simple volume halving model. Two droplet sizes in Tables I and II have large standard deviations due to few data. One can presume that the results indicate a signature of Coulomb fission and gives evidence for nanodroplet splitting due to Rayleigh instability at these length scales, although a full understanding of the droplet distribution population requires more complex models.²³

By making the assumption that the most occurring droplet diameters have $X = 1$, we can calculate the number of unit charges to be 902 droplet⁻¹ ($6.22 \times 10^{-3} \text{ C m}^{-2}$) and 2446 droplet⁻¹ ($4.46 \times 10^{-3} \text{ C m}^{-2}$) for the nano- and microtip, respectively. A volume flow rate Q can be determined from the measurements. The measurement sector angle ψ for the nanotip was equal to 31° (corresponding to 498 spots in this AFM image or ~ 5700 spots in the total trace), whereas ψ for the microtip was 25° (corresponding to 276 spots in this AFM image or ~ 3900 spots in the total trace). Q can be calculated by summing all droplet volumes in the AFM trace and multiplying by a factor which takes into account the measurement sector ψ of the total trace. In this way, we determine Q to be equal to $0.86(\pm 0.1) \text{ nl min}^{-1}$ (nanotip) and $3.72(\pm 0.3) \text{ nl min}^{-1}$ (microtip). By using the physical properties of the water-methanol-nitric acid mixture: surface tension γ ($\sim 47 \text{ mJ m}^{-2}$),²⁴ density ρ ($\sim 844 \text{ kg m}^{-3}$),²⁵ and conductivity σ ($\sim 1.26 \mu\text{S m}^{-1}$); we can compare our findings, here, to

TABLE II. Experimental (N_{exp} and d_{exp}) and modeling (d_{cal}) results for the micro-scale tip (see Table I for explanation). Asterisks correspond to related droplet.

N_{exp}	d_{exp} (nm)	d_{cal} (nm)
8	72.9(2.7)	75.6*
12	92.9(4.5)	95.3*
37	103.2(2.5)	105.3**
22	120.1(4.6)	120.1*
50	136.2(4)	132.6**
55	167.1(9.7)	167.1**
30	202.7(7.8)	—
16	237.0(10)	240.2*
24	295.4(209)	302.6*
6	379.7(29.2)	381.2*
4	464.5(13.5)	480.3*

validated models and experiments in the literature.³ The current I was measured to be 4.5 nA (nanotip) and 9.6 nA (microtip). The scaling law²⁶ $Q = \beta I^2 / \gamma \sigma$, which has been rigorously verified,³ here $\beta = 4.21 \times 10^{-5}$ and 3.98×10^{-5} for the nano- and microtip. For varicose “Rayleigh” break-up,^{27,28} the most likely occurring here, the droplet diameter ($d = 2.27\pi^{-2/3} Q^{1/2} (\rho \epsilon_0 / \gamma \sigma)^{1/6}$) can be calculated²⁷ to be 89.6(± 5.1) nm and 186.4(± 7.4) nm for the nano- and microtips, respectively; these values are comparable with the experimental most occurring values in Tables I and II.

In conclusion, we demonstrate a method which can produce and characterize a snapshot of nanodroplets using nanofabricated silicon tips and AFM. The study provides evidence for Coulomb fission of nanodroplets. This seems the most likely explanation for our observations as the experimental results are not characteristic of arcing,⁸ electrowetting,²⁹ droplet impact,³⁰ or evaporation.³¹ The approach could be useful for testing existing models,^{3,23} characterizing phenomena such as catastrophic droplet breakup.³² Also, the observations have implications for nanotechnology³³ as the tip size is seen to determine the deposition resolution.

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