



HAL
open science

”When does it work?”: An exploratory analysis of transfer learning for BCI

Pedro Luiz Coelho Rodrigues, Marco Congedo, Christian Jutten

► To cite this version:

Pedro Luiz Coelho Rodrigues, Marco Congedo, Christian Jutten. ”When does it work?”: An exploratory analysis of transfer learning for BCI. BCI 2019 - 8th International Brain-Computer Interface Conference, Sep 2019, Graz, Austria. hal-02321580

HAL Id: hal-02321580

<https://hal.science/hal-02321580>

Submitted on 21 Oct 2019

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

“WHEN DOES IT WORK ?” : AN EXPLORATORY ANALYSIS OF TRANSFER LEARNING FOR BCI

Pedro L. C. Rodrigues¹, Marco Congedo¹, Christian Jutten¹

¹GIPSA-lab, CNRS, University Grenoble Alpes, Grenoble Institute of Technology, Grenoble, France

E-mail: pedro.rodrigues@gipsa-lab.fr

ABSTRACT: Transfer Learning is a critical topic of research in the BCI field. Its goal is to reuse data gathered in a previous session (*source* session) in order to reduce, or completely bypass, calibration in a new session (*target* session). Although many methods have been proposed to tackle this problem, little is known about what characteristics of the datasets should be taken into account in order to ensure good performance. In this paper, we perform an exploratory analysis to study the influence of some simple descriptors of the *source* and *target* datasets over the classification scores obtained with Transfer Learning. We observe that the discriminability of the data points in the *target* session plays an important role in determining how well the Transfer Learning will work, as opposed to that of the *source* session, which has no statistically significant role in most cases.

INTRODUCTION

Reducing calibration time has been an important challenge in Brain-Computer Interface (BCI) research since a long time [1]. Several Transfer Learning (TL) approaches have been proposed in the literature and most are based on the idea of reusing data from a previous recording session of a subject (the *source* session) to classify the data of a new session from the same subject or a different one (the *target* session). However, reusing data directly from previous sessions in general yields poor results. This comes from the fact that the statistical distributions of data from different sessions (same subject or not) are rarely the same [1].

A typical TL approach in BCI is to transform the data points from both the *source* and *target* datasets so that the discrepancy between their statistical distributions is reduced [2–4]. In this paper, we match the statistics of the *source* and *target* datasets via the recently proposed *Riemannian Procrustes Analysis* (RPA) [2], a method that adapts the classical Procrustes analysis to a Riemannian geometry framework.

It is well known that, although any pair of *source–target* subjects can go through a Transfer Learning procedure, some pairs of subjects yield better results in classification than others. Our main goal in this paper is to investigate some factors that might explain this variability and how one might try to predict beforehand (i.e., before doing any matching of the datasets or classifying the data points) the

“compatibility” between the datasets.

Our exploratory analysis relies on the estimation of linear models and the study of the statistical significance of the coefficients estimated for those models. We use as explanatory factors the intra-scores for the *source* and *target* subjects (which is the cross-validated classification score using the subject’s dataset as training and testing dataset), and the MMD between the two datasets. We observe that the intra-score for the *target* subject plays an important role in determining how well the Transfer Learning will work, as opposed to the intra-scores of the *source* subjects, which plays no statistically significant role in most cases. We also observe that before doing any transformation on the data points of the *source* and *target* datasets, the MMD between their statistical distributions plays a statistically significant role over the performance of the Transfer Learning. However, once the RPA is applied, the MMD between the datasets becomes very small and no longer carries statistical information to describe the variability of the cross-subject scores. This confirms the relevance of the RPA method.

MATERIALS AND METHODS

This section begins with a formal definition of the Transfer Learning problem. Then, we give a brief introduction to concepts of Riemannian geometry and describe the RPA method. Finally, we present the statistical tools used in our exploratory analysis of Transfer Learning as well as the dataset chosen for our investigations.

Transfer Learning: We formulate the problem of Transfer Learning by first defining two datasets, the *source* (\mathcal{S}) and the *target* (\mathcal{T}) dataset. They are comprised of couples

$$\begin{aligned} \mathcal{S} &= \left\{ (C_i^{\mathcal{S}}, y_i^{\mathcal{S}}) \text{ for } i = 1, \dots, K_{\mathcal{S}} \right\}, \\ \mathcal{T} &= \left\{ (C_i^{\mathcal{T}}, y_i^{\mathcal{T}}) \text{ for } i = 1, \dots, K_{\mathcal{T}} \right\}, \end{aligned} \quad (1)$$

with $C_i^{\mathcal{S}}$ and $C_i^{\mathcal{T}} \in \mathbb{R}^{n \times n}$ being data points, and $y_i^{\mathcal{S}}$ and $y_i^{\mathcal{T}} \in \{1, \dots, L\}$ their corresponding class labels; $K_{\mathcal{S}}$ and $K_{\mathcal{T}}$ are the number of trials in the *source* and *target* sessions respectively. In this paper, the data points in \mathcal{S} and \mathcal{T} are not Euclidean feature vectors as is usually done, but symmetric positive definite (SPD) matrices, which are used to parametrize the statistics of EEG multivariate time series [6].

Transfer Learning concerns the case when the statistical distributions μ_S and μ_T , describing the *source* and *target* datasets respectively, are different. In this context, one might want to train a classifier h using the information in S and apply it to data points in T (or vice-versa).

A common approach is to define a transformation for the data points in the *target* dataset so that their new statistical distribution is the same as that of the *source* dataset. To do so, most algorithms define an optimization procedure that tries to minimize some notion of distance between the statistical distributions of S and T , such as the Maximum-Mean Discrepancy (MMD) [5]. In [7], a theoretical analysis of the Transfer Learning problem has shown that methods reducing the distance between statistical distributions are mathematically well justified, since they reduce the upper bounds of the classification error of h in T .

Riemannian geometry of SPD matrices: We denote by $X_k \in \mathbb{R}^{n \times T}$ the recording of T samples on n electrodes of the k^{th} trial of a zero-mean time series and y_k the class associated to X_k . The spatial covariance matrix C_k associated to X_k is an $n \times n$ matrix estimated as usual by

$$C_k = \frac{1}{T-1} X_k X_k^T. \quad (2)$$

Covariance matrices are symmetric positive definite (SPD) and form a manifold $\mathcal{P}(n)$. When associated to a metric, one can define fundamental geometric notions in $\mathcal{P}(n)$, such as geodesics (shortest curve joining two points), distance between two points (length of the geodesic connecting them), the center of mass of a set of points, etc. We endow $\mathcal{P}(n)$ with the affine-invariance Riemannian metric, which induces the distance [8]

$$\delta_R^2(C_i, C_j) = \|\log(C_i^{-1/2} C_j C_i^{-1/2})\|_F^2, \quad (3)$$

for $C_i, C_j \in \mathcal{P}(n)$. This distance is more natural for the $\mathcal{P}(n)$ manifold as compared to the Euclidean distance and has been instrumental in several BCI classification algorithms developed in recent years [6]. The geometric mean M according to distance (3) of a set of covariance matrices $\{C_1, \dots, C_K\}$ is defined as [6]

$$M = \operatorname{argmin}_{X \in \mathcal{P}(n)} \sum_{k=1}^K \delta_R^2(X, C_k), \quad (4)$$

where the cost function in (4) is the dispersion of the set of matrices around a matrix X . The above definitions suffice for the intents of this paper. The interested reader will find a thorough treatment of the subject in the monography of R. Bhatia [8] and its applications to BCI in [6].

Riemannian Procrustes Analysis: In this paper, we use the RPA [2] for transforming data points in T so that their new distribution is as close as possible to μ_S . RPA works by considering the distributions of data points in S and T as shapes in a high-dimensional space. It performs rigid geometric operations over the ensemble of data points, such as translation, stretching and rotation, to make their shapes as similar as possible. The transformations are

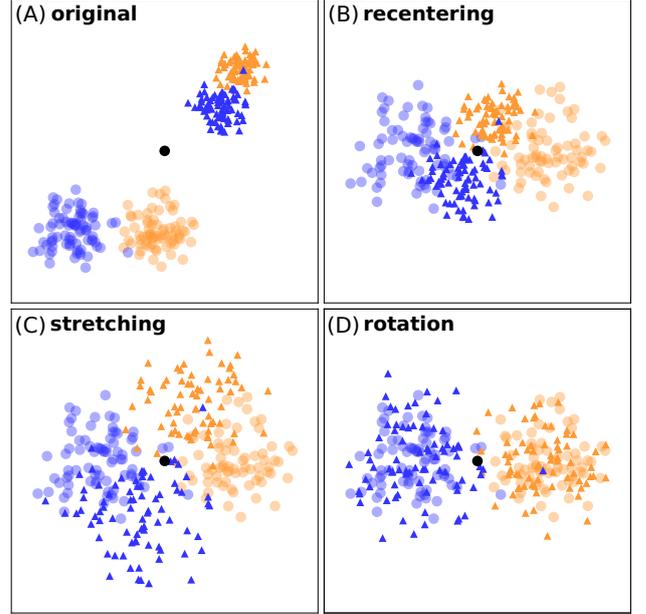


Figure 1: Schematic representation in a 2D Euclidean space of the rigid transformations involved in the classical Procrustes Analysis. The black dot represents the origin of the space and circles in blue and yellow are data points from two classes in a *source* dataset. The triangles are data points of a *target* dataset. The transformations in RPA are analogous to those in Euclidean space but applied to data points in the SPD manifold $\mathcal{P}(n)$.

done respecting the intrinsic geometry of $\mathcal{P}(n)$, which is where the data points of S and T are defined. We represent the transformations in Procrustes analysis in Figure 1 and summarize the steps of the RPA as follows :

1. Estimate the **geometric means** of S and T , denoting them by M_S and M_T , respectively, and the dispersions around the mean of each dataset, denoted by d_S and d_T .
2. **Re-center** the data points in S and T by doing

$$C_i^{S(\text{rect})} = M_S^{-1/2} C_i^S M_S^{-1/2}, \quad (5)$$

$$C_i^{T(\text{rect})} = M_T^{-1/2} C_i^T M_T^{-1/2}, \quad (6)$$

and forming new datasets

$$\mathcal{S}^{(\text{rect})} = \{C_i^{S(\text{rect})}\} \quad \text{and} \quad \mathcal{T}^{(\text{rect})} = \{C_i^{T(\text{rect})}\}.$$

Note that the geometric mean of these two new datasets is the Identity matrix.

3. **Stretch** the dispersion around the mean of the data points in $\mathcal{T}^{(\text{rect})}$ so that it matches the dispersion around the mean of $\mathcal{S}^{(\text{rect})}$ by doing

$$C_i^{T(\text{str})} = \left(C_i^{S(\text{rect})}\right)^s, \quad (7)$$

where we require $s \in \mathbb{R}$ to verify

$$s^2 = d/\tilde{d}. \quad (8)$$

4. The last step consists in **rotating** the matrices from $\mathcal{T}^{(\text{str})}$ around the origin and matching the orientation of its point cloud with that of $\mathcal{S}^{(\text{rct})}$. We have then

$$C_i^{\mathcal{T}(\text{rot})} = U^T C_i^{\mathcal{T}(\text{str})} U, \quad (9)$$

where U is determined via an optimization procedure that minimizes the distance between the class means of each dataset after the rotation. Note that this step is a semi-supervised one, since it requires knowledge of at least a few labels of the *target* dataset for estimating its class means (see [2] for more details).

Transfer Learning classification: In this paper, whenever we want to do a classification task with data points that live in $\mathcal{P}(n)$, we use the Minimum-Distance to Mean classifier (MDM) [6], which is a generalization of the nearest-centroid classifier to the space of SPD matrices. It works by first estimating the geometric mean of the elements of each class in the training dataset (the class means). Then, it assigns to each unlabeled data point the class of the nearest class mean according to the δ_R distance. In the context of transfer learning, we will always consider the *source* dataset \mathcal{S} as the training dataset and the *target* dataset \mathcal{T} as the testing dataset. The classification score is simply the average accuracy of the classifier. In the following analysis, we will consider the results of Transfer Learning classification on three different cases :

DCT : the *source* and *target* datasets are used **DireCTly** as training and testing datasets, without any transformation.

RCT : the *source* and *target* datasets are both **Re-CenTered** and then used as training and testing dataset.

RPA : the *source* and *target* datasets go through the RPA procedure and are then used as training and testing datasets.

For this analysis we will assume that all labels in the *target* dataset are available for the estimation of the class means. In fact, our intent here is not to evaluate the performance of the RPA method in a realistic situation when only a few labels from the *target* dataset are available (this has been done in [2]), but rather to understand under which circumstances it works.

Seriation procedure: Given a dataset, all cross-subject Transfer Learning performance is summarized in a matrix $S^{(m)}$, where the $S_{ij}^{(m)}$ element contains the accuracy of the classification with method $m \in \{\mathbf{DCT}, \mathbf{RCT}, \mathbf{RPA}\}$ using subject i as *target* and subject j as *source*. We use a tool from combinatorial data analysis named *seriation* [9] to sort the lines and columns of $S^{(m)}$ in order to make relevant patterns emerge. The rows and columns of $S^{(m)}$ are sorted in decreasing order of their marginals. The output of this procedure is a new representation where the pairs of *source-target* subjects with the best accuracy are located at the top-left region of the matrix, while the worst pairs are at the bottom-right region.

Statistical analysis procedure: Our quantitative analysis is based on the estimation of linear regression models to describe the variability on the values of $S_{ij}^{(m)}$ as defined in the previous subsection. We estimate a different linear model $\mathcal{L}_i^{(m)}$ for each *target* subject i and method m . We do this because the cross-subject scores for two different *target* subjects and the same *source* subject are statistically dependent, which would undermine the estimation of a full linear model mixing all scores. Moreover, the results after the **RPA** method are related to those for the **RCT** one, since the latter includes the former as a processing step.

We define the linear model $\mathcal{L}_i^{(m)}$ as :

$$S_{ij}^{(m)} = \beta_{1,i}^{(m)} S_i + \beta_{2,i}^{(m)} S_j + \beta_{3,i}^{(m)} \eta_{ij}^{(m)} + \epsilon_i^{(m)}, \quad (10)$$

where

- S_i (S_j) is the intra classification score of *target* (*source*) subject i (j), obtained via cross-validation with training and testing datasets coming from the same subject. Note that since each model $\mathcal{L}_i^{(m)}$ is estimated for one fixed *target* subject i , S_i is a constant in (10) and acts as a scaling for the intercept; thus, it is not considered as an independent variable in the statistical analysis.
- Factor $\eta_{ij}^{(m)}$ is the MMD between datasets \mathcal{S} and \mathcal{T} after the operations of method m , defined as [5]

$$\begin{aligned} \text{MMD}(\mathcal{S}, \mathcal{T}) &= \frac{1}{K_S^2} \sum_{i,j}^{K_S} k(C_i, C_j) \\ &+ \frac{1}{K_T^2} \sum_{i,j}^{K_T} k(\tilde{C}_i, \tilde{C}_j) \\ &- \frac{2}{K_S K_T} \sum_{i,j=1}^{K_S, K_T} k(C_i, \tilde{C}_j) \end{aligned} \quad (11)$$

where

$$k(P, Q) = \exp\left(-\frac{\delta_R^2(P, Q)}{2\sigma^2}\right), \quad (12)$$

for $P, Q \in \mathcal{P}(n)$ and σ is taken as the median value of all pairwise distances of elements in \mathcal{S} and \mathcal{T} .

- The variable $\epsilon_i^{(m)}$ stands for all residual factors that are not explained by the linear regression model.

Once the linear models are all estimated, we perform a set of hypothesis tests for each *target* subject i . The goal is to assess the statistical significance of the coefficients of each model. The first kind of test is a F -test for the omnibus null hypothesis :

$$\begin{aligned} \mathcal{H}_0 : & \quad \beta_{2,i}^{(m)} = \beta_{3,i}^{(m)} = 0, \\ \mathcal{H}_1 : & \quad \beta_{k,i}^{(m)} \neq 0 \text{ for at least one } k \text{ in } \{2, 3\}. \end{aligned} \quad (13)$$

This is a standard test used for inspecting whether the set of independent variables of a linear regression model,

S_j and δ_{ij} in (10), is statistically significant for explaining at least part of the variability of the dependent variable, $S_{ij}^{(m)}$ in (10). When the null hypothesis is rejected, we say that there is enough statistical evidence for considering that the slope of at least one of the independent variables is different than zero. In this case, we perform t -tests for checking which explanatory variable in $\mathcal{L}_i^{(m)}$ is statistically significant. We have :

$$\begin{aligned} \mathcal{H}_0 &: \beta_{\ell,i}^{(m)} = 0, \\ \mathcal{H}_1 &: \beta_{\ell,i}^{(m)} \neq 0, \end{aligned} \quad (14)$$

for $\ell \in \{2, 3\}$. When the null hypothesis of (14) is rejected for $\beta_{\ell,i}^{(m)}$, we say that there is statistical evidence for considering it different than zero and so the independent variable related to it contributes for explaining the dependent variable $S_{ij}^{(m)}$.

The statistical procedure explained above yields two sets of p -values for each method $m \in \{\mathbf{DCT}, \mathbf{RCT}, \mathbf{RPA}\}$. The first set contains the p -values for each F -test on each *target* subject i , whereas the second set gathers the p -values of the t -tests. The results presented in the next section are based on the analysis of these sets of p -values and how they are distributed along different *source* subjects for each method.

Dataset: We carried out our analysis on a publicly available dataset [10] which we will refer as *Cho2017* from now on. The dataset contains recordings of subjects performing BCI trials following a MI paradigm with 64 EEG electrodes (sampling frequency 512 Hz) from 52 subjects, each one performing 200 trials (100 of each class). We filtered the EEG signals in the 8-30 Hz band and each trial was considered as a segment from 0.5 to 2.5 seconds after the trial onset. We estimated the spatial covariance matrices using (2). Not all subjects in *Cho2017* have data which can be well discriminated, so we kept only those whose the intra-score in terms of AUC (Area Under the ROC-curve) is above chance level; this keeps 40 subjects out of the 52 in total.

RESULTS AND DISCUSSION

In this section, we present the results of our analysis of Transfer Learning via RPA on the *Cho2017* dataset. We begin with a qualitative analysis of the output of the seriation procedure applied to the cross-subject scores. Then, we study the correlation of each factor defined in (10) with the cross-subject scores. Finally, we analyse the results of the statistical hypothesis tests for each one of the linear models \mathcal{L}_i and discuss the patterns observed for the whole dataset (from now on, we will indicate the superscript specifying which method m only when necessary).

Cross-subject classification accuracy: Figure 2 shows the output of the seriation procedure on the cross-subject Transfer Learning scores for the *Cho2017* dataset on three classification methods: **DCT**, **RCT**, and **RPA**. We observe that with **RCT** and **RPA** there are more pairs of subjects with high values of cross-subject classification

than with **DCT**. In particular, we note that for **RCT** and **RPA** there are many *target* subjects for which the classification accuracy is high for almost all possible *source* subjects. To investigate the possible explanations for this behavior, we perform a *Spearman* correlation test between the average cross-subject score for each target (given by the average value along the rows of matrix S) and the intra-subject accuracy of the corresponding *target* subject. For the **RPA** method, we obtain a correlation of 0.58 ($p < 10^{-3}$), whereas for **RCT** it is 0.44 ($p < 10^{-2}$) and **DCT** is 0.45 ($p < 10^{-2}$). We interpret these results as : subjects that are “good” for classifying their own data can better receive information from other *source* subjects. We also provide a quantitative analysis of the results. Figure 3 portrays the histograms of all cross-subject Transfer Learning scores S_{ij} (rows and columns confounded) for each method and their means are displayed in Table 1. These results show that the transformations over the *source* and *target* datasets do improve the cross-subject classification scores on the average.

Table 1: Average values of the cross-subject Transfer Learning scores and the MMD distance between *source* and *target* datasets for each method.

Method	$(\delta_{ij})_{\text{avg}}$	$(S_{ij})_{\text{avg}}$
DCT	0.63	0.53
RCT	0.01	0.58
RPA	0.01	0.76

Changes in MMD after each RPA step: We evaluate how the MMD between each pair of *source-target* subjects changes after the re-centering step and the full RPA procedure. Table 1 gives the average values of the MMD distances for each method and shows that there is a clear decrease after each transformation. This result is not surprising, since each step of the RPA procedure was conceived exactly to make the distributions of \mathcal{S} and \mathcal{T} closer in some sense and the MMD allows for a quantitative assessment of it.

Study of the linear models \mathcal{L}_i : After exploring the grand averages of the cross-subject Transfer Learning scores and how they relate to a few explanatory factors, we analyse the linear models \mathcal{L}_i defined in (10) and estimated on each *target* subject i for the three methods of interest : **DCT**, **RCT**, and **RPA**.

We first plot the p -values of the F -test for each model sorted in ascending order. Under the omnibus null hypothesis for *target* subjects, the p -values follow a uniform distribution and, thus, when sorted they will lie on a straight line. The leftmost plot in Figure 4 shows that for almost all subjects the variability of the cross-subject performance is well explained by the linear model estimated for the **DCT** method and, in a lesser extent, for the **RCT** method. It is worth remembering that the statistical significance of the coefficient for the intercept, and, therefore, the influence of the intra-score S_i on describing the

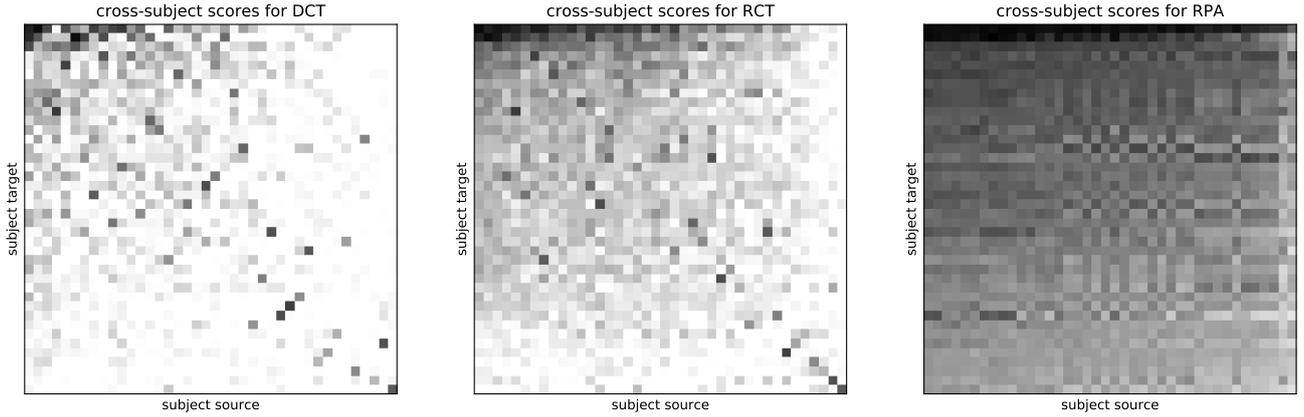


Figure 2: Accuracies of the cross-subject classification for three different Transfer Learning procedures on the *Cho2017* database. The rows and columns of each subplot were reordered using the *seriation* procedure explained in the text. The colormap varies from white (accuracy 0.5) to black (accuracy 1.0).

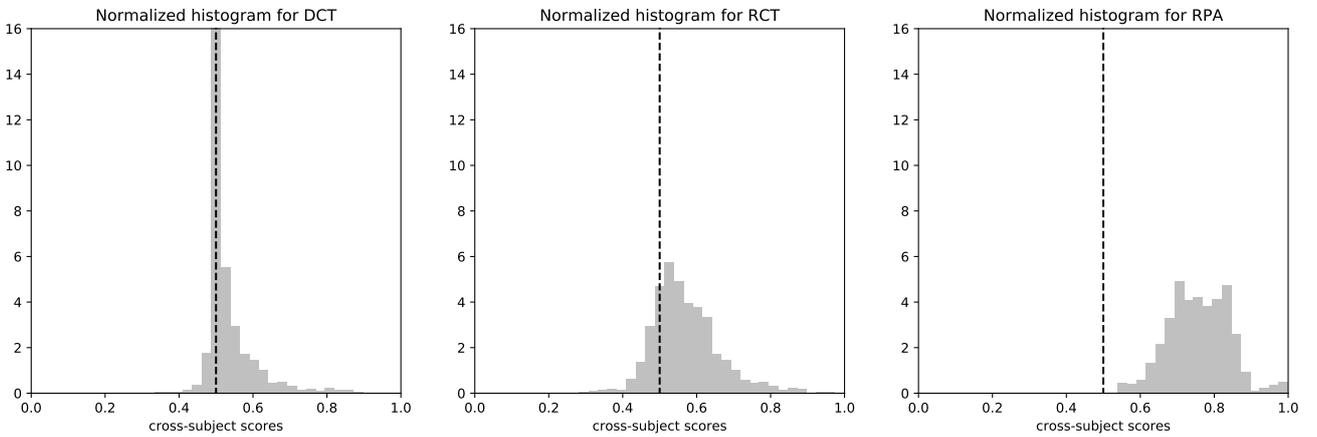


Figure 3: Normalized histograms of the cross-subject Transfer Learning scores for the three methods described in the text. The vertical dashed line indicates chance level.

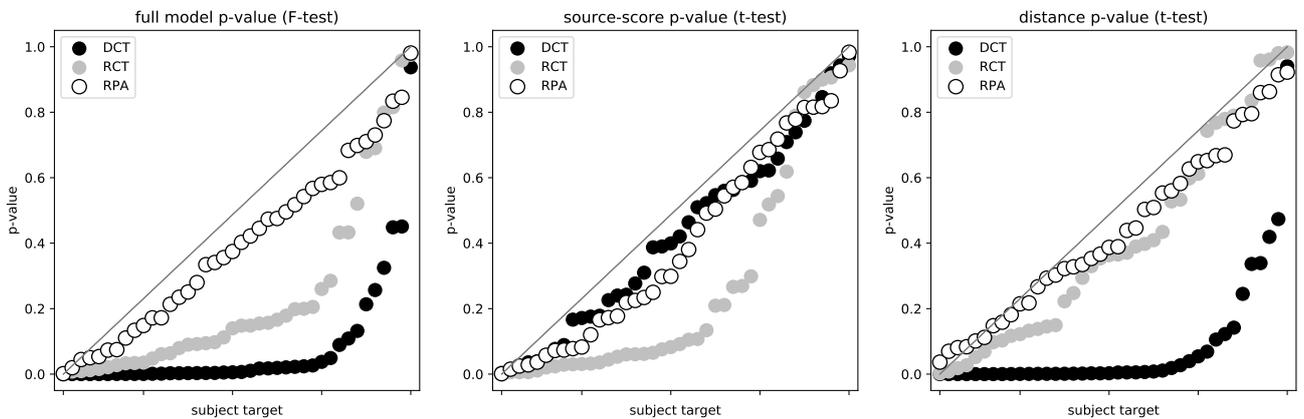


Figure 4: p -values of different statistical tests over the linear models \mathcal{L}_i (each one associated to a *target* subject i). Each circle represents the p -value of a given test on a given *target* subject and the x -axis has been rearranged so that all the p -values are in increasing order. The leftmost plot represents the results of the F -test of the full linear model \mathcal{L}_i , whereas the center plot illustrates the p -values for the t -test of the coefficient $\beta_{2,i}$ in \mathcal{L}_i (related to the intra-score of the *source* subject), and the rightmost plot displays the p -values for the t -test on the coefficient $\beta_{3,i}$ in \mathcal{L}_i (related to the MMD between the *source* and *target* datasets).

values of S_{ij} , is not assessed via the F -test. This is why we have calculated the *Spearman* correlation between the row-averaged S_{ij} and the S_i in the previous sub-section.

The distribution of the p -values in the center plot of Figure 4 shows that $\beta_{2,i}$ has no statistical significance in the linear model \mathcal{L}_i for any of the *target* subjects in the **DCT** and **RPA** methods. However, for **RCT** it does seem to play a role for some *target* subjects. What we can conclude from these observations is that **RPA** is able to make the cross-subject Transfer Learning score independent of the choice of *source* subject (at least in terms of its intra score). As a consequence, it makes it easier to find “good” source subjects for each *target* subject, as it was already observed during our qualitative analysis of Figure 2.

Finally, the rightmost plot in Figure 4 shows that the MMD between *source* and *target* datasets plays a role in describing the cross-subject Transfer Learning scores only for the **DCT** method. This result is comforting, since it brings evidence to the fact that the operations in the RPA procedure are capable of factoring out most of the differences between the statistical distributions of \mathcal{S} and \mathcal{T} . As a consequence, we may say that any further improvement that one might want to do on the Transfer Learning procedure should take into account other aspects of the mismatch between datasets besides the MMD between them.

CONCLUSION

In this paper, we have investigated the influence of different factors on the variability of cross-subject Transfer Learning scores. Our goal has been to assess whether some basic explanatory variables, such as the intra-score of the *source* and *target* subjects, play any role for determining the scores obtained in the cross-subject classification. A simple, and yet important, application of this study is being able to predict beforehand (i.e., before doing all transformations and then classifying the trials) which *source* subject would be the most appropriate for doing classification on a given *target* subject.

We have observed that the discriminability of the trials of the *target* subjects (i.e. its intra-score) plays a fundamental role in determining how the cross-subject Transfer Learning will perform. On the other hand, the influence of the intra-scores for the *source* subjects have proven to be rather limited. We have also observed that the influence of the MMD between \mathcal{S} and \mathcal{T} is not statistically significant after using RPA to match the two datasets. What we can conclude from this is that the RPA procedure is capable of factoring out most of the influence of the discrepancy between statistical distributions of the *source* and *target* datasets.

It is our opinion that investigating the factors determining the success of Transfer Learning is instrumental for devising new and more powerful strategies for doing it. The present study is a little step in this direction. Future works shall include the search for richer models for describing

the cross-subject Transfer Learning scores. Some approaches would be to consider non-linear relations between the explanatory variables as well as adding new factors related to other features of the *source* and *target* subjects.

REFERENCES

- [1] F Lotte, L Bougrain, A Cichocki, *et al.*, “A review of classification algorithms for EEG-based brain–computer interfaces: A 10 year update”, *Journal of Neural Engineering*, vol. 15, no. 3, p. 031 005, 2018.
- [2] P. L. C. Rodrigues, C. Jutten, and M. Congedo, “Riemannian procrustes analysis: Transfer learning for brain-computer interfaces”, *IEEE Trans. on Biomedical Engineering*, pp. 1–1, 2018.
- [3] P. Zanini, M. Congedo, C. Jutten, S. Said, and Y. Berthoumieu, “Transfer learning: A Riemannian geometry framework with applications to brain-computer interfaces”, *IEEE Trans. on Biomedical Engineering*, pp. 1–1, 2017.
- [4] N. T. H. Gayraud, A. Rakotomamonjy, and M. Clerc, “Optimal Transport Applied to Transfer Learning For P300 Detection”, in *7th Graz Conference*, Graz, Austria, 2017, p. 6.
- [5] A. Gretton, K. M. Borgwardt, M. J. Rasch, B. Schölkopf, and A. Smola, “A kernel two-sample test”, *Journal of Machine Learning Research*, vol. 13, no. 1, pp. 723–773, Mar. 2012.
- [6] M. Congedo, A. Barachant, and R. Bhatia, “Riemannian geometry for EEG-based brain-computer interfaces; a primer and a review”, *Brain-Computer Interfaces*, pp. 1–20, 2017.
- [7] S. Ben-David, J. Blitzer, K. Crammer, A. Kulesza, F. Pereira, and J. W. Vaughan, “A theory of learning from different domains”, *Machine Learning*, vol. 79, no. 1-2, pp. 151–175, 2009.
- [8] R. Bhatia, *Positive Definite Matrices*. Princeton university press, 2009.
- [9] I. Liiv, “Seriation and matrix reordering methods: An historical overview”, *Stat. Anal. Data Min.*, vol. 3, no. 2, pp. 70–91, Apr. 2010.
- [10] H. Cho, M. Ahn, S. Ahn, M. Kwon, and S. C. Jun, “EEG datasets for motor imagery brain–computer interface”, *GigaScience*, vol. 6, no. 7, pp. 1–8, 2017.