

# **A nonlinear time-series analysis approach to identify thresholds in associations between population antibiotic use and rates of resistance**

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### A non-linear time-series analysis approach to identify thresholds in associations between population antibiotic use and rates of resistance

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### **Abstract**

52 Balancing access to antibiotics with control of antibiotic resistance is a global public health 53 priority. Currently, antibiotic stewardship is informed by a 'use it and lose it' principle, in 54 which population antibiotic use is linearly related to resistance rates. However, theoretical 55 and mathematical models suggest use-resistance relationships are non-linear. One explanation 56 is that resistance genes are commonly associated with 'fitness costs', impairing pathogen 57 replication or transmissibility. Therefore, resistant genes and pathogens may only gain a 58 survival advantage where antibiotic selection pressures exceed critical thresholds. These 59 thresholds may provide quantitative targets for stewardship: optimising control of resistance 60 while avoiding over-restriction of antibiotics. We evaluated the generalisability of a non-61 linear time-series analysis approach for identifying thresholds using historical prescribing and 62 microbiological data from five populations in Europe. We identified minimum thresholds in 63 temporal relationships between use of selected antibiotics and rates of carbapenem-resistant *Acinetobacter baumannii* (in Hungary), extended spectrum β-lactamase producing *Escherichia coli* (Spain), cefepime-resistant *Escherichia coli* (Spain), gentamicin-resistant *Pseudomonas aeruginosa* (France), and methicillin-resistant *Staphylococcus aureus*  67 (Northern Ireland) in different epidemiological phases. Using routinely generated data, our 68 approach can identify context-specific quantitative targets for rationalising population 69 antibiotic use and controlling resistance. Prospective intervention studies restricting antibiotic 70 consumption are needed to validate thresholds. 

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## <sup>99</sup>**Introduction**

100 Antimicrobials have facilitated improvements in health and food-security worldwide. 101 However, excessive use has promoted antimicrobial resistance (AMR), undermining many 102 aspects of healthcare and generating new disease burdens.<sup>1-4</sup> While decisions around 103 antimicrobial use are made by individual prescribers and patients, consequences of over-use 104 are only fully apparent across populations.<sup>5</sup> Competing needs and non-exclusivity lead to a 105 'tragedy of the commons'.<sup>1,2</sup> The Global Action Plan on AMR therefore emphasises cross- $106$  societal efforts to conserve the current stock of effective antimicrobials.<sup>6</sup> Antimicrobial 107 stewardship aims to control AMR by reducing inappropriate use, while ensuring access to 108 effective therapy.<sup>2</sup> There is growing evidence that reducing population use of antimicrobials 109 selecting for resistance, can effectively reduce  $AMR$ <sup>7</sup>. However, over-restriction may be 110 counter-productive: use of alternative antimicrobials may increase in response, leading to 111 new selection pressures or resistance problems.<sup>8</sup> Balancing the benefits and risks of 112 antimicrobials in healthcare requires understanding of their effects on AMR at population 113 scales. $9-11$ 

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115 Most empirical evidence has considered linear use-resistance relationships.<sup>12-16</sup> Although 116 useful for identifying the most salient selection pressures in a population,<sup>12</sup> theoretical and 117 mathematical models suggest non-linear relationships are more likely.<sup>9-11,17</sup> In particular, 118 selection pressures may only impact on resistance rates, where volumes of antibiotic use in 119 the population are above minimum thresholds. Potential explanations for minimum 120 thresholds, include: antibiotic substitution with changes in use;<sup>8</sup> associations between the 121 strength of selection pressure and induction of co-resistance;<sup>18</sup> differential effects on sub-122 populations within bacterial species, $19$  or ecological niches; $20$  and the 'total use thresholds' 123 hypothesis.<sup>9</sup> The latter concept arises from the observation that resistance genes are 124 commonly associated with fitness costs impairing pathogen replication or transmissibility.<sup>21</sup> 125 Resistant pathogens may therefore only gain a survival advantage over susceptible organisms, 126 where selection pressures from antibiotic use outweigh fitness costs.<sup>9</sup> If identified, minimum 127 thresholds may offer important targets for antibiotic stewardship, indicating an upper limit of 128 safe population antibiotic use which does not increase resistance within populations.

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130 Non-linear relationships between fluoroquinolone use and resistant *E.coli* and *Staphylococcus*  131 *aureus* have been reported.<sup>20,22</sup> We have shown that reducing antibiotic use to below 132 minimum thresholds predicted shifts in the molecular and clinical epidemiology of *S. aureus* 133 and *Clostridium difficile*.<sup>23-25</sup> However, early findings suggest antibiotic use-resistance 134 relationships are likely to depend upon the clinical population,  $9,23,25$  pathogen genotypes,  $24$ 135 intensity of infection control,<sup>23</sup> and transmission dynamics.<sup>11</sup> Moreover, fitness costs 136 associated with different resistance genes are variable.<sup>21</sup> If fitness costs are low, or attenuated 137 through epistasis<sup>26</sup> or compensatory mutations,<sup>27</sup> resistance may persist despite removing 138 previously important antibiotic selection pressures.<sup>28</sup> A generalisable method for finding 139 minimum thresholds should therefore provide context-specific results, have relatively low-140 informational demands, and allow for iteration.

141

142 Here, we examined the generalisability of a non-linear time-series analysis methodology for 143 identifying minimum threshold in use-resistance associations. Using routinely generated data 144 from five European centres, we show this pragmatic approach can provide population-145 specific quantitative targets for antimicrobial stewardship for a variety of resistance 146 outcomes, epidemiological phases, transmission dynamics, and clinical populations.

## <sup>148</sup>**Results**

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### 150 **Identifying non-linear temporal relationships: from experiment to application**

151 In a Monte Carlo experiment we compared the ability of linear and non-linear time-series 152 analysis (Multivariate Adaptive Regression Splines, MARS) to identify pre-defined 153 relationships between simulated explanatory and outcome time-series (Supplementary Figure 154 1). Non-linear time-series analysis (NL-TSA) accurately identified both truly linear and non-155 linear associations. However, linear time-series analysis provided biased estimations and 156 overall poorer data-fit if relationships were non-linear.

157

158 NL-TSA models applied to retrospective time-series data from five European study 159 populations (examples 1-5), frequently identified minimum thresholds in antibiotic use-160 resistance relationships, (figures 1-5 and Supplementary Table 1). 'Ceiling effects', in which 161 further increases in explanatory variables did not affect resistance rates, were found at high-162 levels of use of some antibiotics and hand hygiene. Non-linearities in autoregression and 163 population interaction terms further indicated the complexity of transmission dynamics within and between clinical populations.<br>165 within and between clinical populations.

### 166 **Example 1: Carbapenem-resistant** *Acinetobacter baumannii* **(Debrecen, Hungary)**

167 We examined ecological determinants of carbapenem-resistant *A. baumannii* (CRAb) in a 168 tertiary hospital population in Debrecen, Hungary (figure 1). Between Oct 2004 and Aug 169 2016 (n=143 months), incidence density of CRAb increased from a 12-month average of 0.14 170 to 9.43 cases per 10 000 OBDs, while that of carbapenem-susceptible *A. baumannii* (CSAb) 171 remained relatively constant. There were no planned antibiotic stewardship interventions in 172 the study period. We observed increasing use of broad-spectrum antibiotics, including a 173 tripling in carbapenem use, and more recent escalation in colistin use.

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175 Carbapenem resistance in this setting was conferred predominantly by  $bla_{\text{OXA-23-like}}$  carbapenemases, while  $bla_{\text{OXA-24-like}}$  genes occurred sporadically.<sup>29</sup> CRAb were significantly carbapenemases, while *bla*<sub>OXA-24-like</sub> genes occurred sporadically.<sup>29</sup> CRAb were significantly<br>177 more likely to be resistant to ciprofloxacin, gentamicin, amikacin, piperacillin-tazobactam more likely to be resistant to ciprofloxacin, gentamicin, amikacin, piperacillin-tazobactam 178 and ceftazidime than CSAb (Supplementary Table 2), although susceptibility testing for the 179 latter two agents was discontinued in 2013 as recommended by EUCAST. Vector 180 autoregression models found that colistin use followed, rather than predicted, variation in 181 CRAb incidence density. Use of carbapenems, fluoroquinolones, piperacillin-tazobactam, 182 third generation cephalosporins (3GC), and aminoglycosides were considered potential 183 explanatory variables.

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185 Previous CRAb incidence density and recent hospital use of carbapenems, piperacillin-186 tazobactam, and fluoroquinolones were explanatory variables in the best-fit  $(R<sup>2</sup>=0.86)$  non-187 linear TSA model (Supplementary Table 1). In an almost identical model with poorer trade-188 off of data fit and model complexity (higher Modified Generalised Cross Validation statistic), 189 fluoroquinolone use was replaced by the effect of 3GC use above a threshold of 36 (95% CI, 190 30 to 41) DDDs per 1000 OBDs (coefficient, 95% CI: 0.111, 0.018 to 0.203; p=0.019; lag 3).

191

192 In this setting increases in CRAb added to, rather than replaced, CSAb, suggesting CRAb 193 occupied new ecological niches. Strong autoregression in the CRAb time-series was 194 consistent with substantial within-hospital transmission.<sup>29</sup> CRAb incidence density increased 195 when population use of carbapenems, piperacillin-tazobactam, fluoroquinolones, and 3GC 196 exceeded minimum thresholds. By the end of the study period, use of fluoroquinolones had 197 reduced to below threshold. However, CRAb could be further controlled by reducing use of 198 carbapenems, 3GC, and piperacillin-tazobactam, from present levels to respective thresholds 199 (table 1).

### 200 **Example 2: Extended spectrum β-lactamase producing** *E. coli* **(Orihuela, Spain)**

201 We examined variables temporal associated with the percentage of *E. coli* producing ESBL 202 (%Ec-ESBL+) in connected district general hospital and community populations of Orihuela, 203 Spain, between Jul 1991 and Oct 2016 (n=304 months, figure 2). Limited outbreaks of 204 ESBL-producing *E. coli* were noted from 1998, but from 2002 the %Ec-ESBL+ increased 205 rapidly alongside escalating use of fluoroquinolones and co-amoxiclav. While use of these 206 agents later stabilised or declined, hospital use of third-generation cephalosporins continued 207 to increase.

208

209 Over the study period, *bla*<sub>CTX-M</sub> genes were common in *E. coli* across Spain, with 210 dissemination of the CTX-M-15-producing O25b-ST131 clone and clonally unrelated CTX-211 M-14-producing strains identified.<sup>30,31</sup>. Acquisition of fluoroquinolone resistance was a key 212 step in the evolution of dominant  $bla_{CTX-M-15}$  containing sub-clones of O25b-ST131.<sup>32</sup> 213 Consistent with this, 81% of ESBL-producing *E. coli* in Orihuela were non-susceptible to 214 ciprofloxacin. They were also significantly more likely to be resistant to co-trimoxazole, co-215 amoxiclav and aminoglycosides compared to non-ESBL *E. coli* (Supplemental Table 3). 216 Vector autoregression models demonstrated bidirectional interactions between community 217 and hospital %Ec-ESBL+ and that use of piperacillin-tazobactam and carbapenems followed, 218 rather than predicted, changes in %Ec-ESBL+. In separate hospital and community models, 219 %Ec-ESBL in the other population was considered as an explanatory variable.

220

221 In the best-fit model  $(R^2=0.62)$  hospital %Ec-ESBL+ was predicted by prior %EcESBL in 222 hospital and community, and hospital use of 3GC, and fluoroquinolones exceeding minimum 223 thresholds (Supplementary Table 1). A potential 'ceiling' effect was noted at high-levels of 224 fluoroquinolone use, meaning that when use exceeded a second upper threshold, further 225 increases in %Ec-ESBL+ were small. An initial decrease in %Ec-ESBL+ where 226 fluoroquinolone use was between 151 and 161 DDDs per 1000 OBDs reflected uncertainty 227 around this ceiling threshold, which may be resolvable with additional data. In the model for 228 community %Ec-ESBL+  $(R^2 0.767)$ , associations were identified with hospital %Ec-ESBL+, 229 and community use of fluoroquinolones and co-amoxiclav above minimum thresholds.

230

231 Autoregressive and population interaction effects suggested the importance of horizontal 232 transmission of ESBLs, with predominant influence of community on hospital epidemiology. 233 Population use of broad-spectrum beta-lactams and fluoroquinolones were important 234 explanatory variables in both settings. In the community, use of fluoroquinolones had fallen 235 below threshold levels and %Ec-ESBL+ had started to decrease by the end of the study. 236 However, translating thresholds into antibiotic stewardship targets (table 1) suggested further 237 restricting community co-amoxiclav use by 31% and hospital use of fluoroquinolones (-41%) 238 and 3GC (-21%).

239

240 From best-fit models, we created 24-month projections for %Ec-ESBL+ in the hospital and 241 community under different antibiotic stewardship options, and compared these to expected 242 %Ec-ESBL+ under a 'business as usual' scenario of antibiotic use (Supplementary Figure 2). 243 Immediate restriction of hospital use of fluoroquinolones and 3GCs to thresholds was 244 predicted to cause an abrupt and sustained reduction in hospital %Ec-ESBL+ from 9.89% to 245 2.35% (p<0.0001) and, due to population interactions, a gradual reduction in community 246 %Ec-ESBL+ from 7.11% to 3.69% ( $p<0.0001$ ). Limiting community co-amoxiclav use to 247 threshold levels was predicted to cause a small reduction in community %Ec-ESBL+ but not 248 to affect hospital epidemiology.

249

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### 251 **Example 3: Cefepime-resistant** *Escherichia coli* **(Seville, Spain)**

252 We examined ecological variables explaining cefepime resistance among urinary or invasive 253 *E.coli* infections (%Ec-FepR) in a tertiary hospital in Seville, Spain. Between March 2008 254 and December 2016 (n=108 months) %Ec-FepR fell from 12.6% to 7.9% (figure 3). 255 Cefepime use was low, declining from 4.4 to 1.6 DDDs per 1000 OBDs with thrice-weekly 256 (Jan 2012, audit1) and daily (Jan 2014, audit2) prescription audits. By contrast, previously 257 declining use of 3GC increased from January 2013 when they replaced co-amoxiclav and 258 ciprofloxacin as first-line empirical therapy for intra-abdominal or urinary infections.

259

260 Resistance to cefepime in *E. coli* is mostly conferred by ESBLs with high affinity for 261 cefepime (TEM-, SHV- and CTX-M-types). In addition to those agents hypothesised to 262 predict ESBL-producing *E. coli* (see example 2), we considered the role of piperacillin-263 tazobactam.<sup>13</sup> Due to low rates of cefepime prescribing, we grouped this with 3GC use. We 264 introduced variables for antibiotic auditing interventions and for revised susceptibility 265 breakpoints (Oct 2014).<sup>33</sup>

266

267 The final non-linear model  $(R^2 0.30)$  identified associations with %Ec-FepR 12 months prior 268 (seasonal effect) and use of third- or fourth-generation cephalosporins and fluoroquinolones 269 above minimum thresholds (Supplementary Table 1). A significant interaction term between 270 %Ec-FepR in the previous month (autoregression, lag 1) and the second antibiotic auditing 271 intervention suggested a gradual effect of the audit in reducing %Ec-FepR.

272<br>273

Reductions in third- and fourth-generation cephalosporins and fluoroquinolone use to below 274 minimum thresholds explained modest declines in %Ec-FepR between 2008 and 2012. Partial 275 reversal in this trend was consistent with increasing use of 3GC towards the end of the study 276 period. %Ec-FepR could be controlled further by reducing third- and fourth-generation 277 cephalosporin use by 41% (table 1).

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### 279 **Example 4: Gentamicin-resistant** *Pseudomonas aeruginosa* **(Besançon, France)**

280 We examined ecological variables explaining rates of gentamicin-resistant *P. aeruginosa*  281 (GRPa) among adult and paediatric admissions to a tertiary hospital in Besançon, France 282 (figure 4). Between Jan 1999 and Dec 2014 (n=192 months), incidence density of GRPa 283 decreased from 14.0 to 3.4 cases per 1000 OBDs, and the proportion of *P. aeruginosa*  284 isolates resistant to gentamicin declined from 63% to 16%.

285

286 Aminoglycoside modifying enzymes (AMEs) are the most common mediators of 287 aminoglycoside resistance in *P. aeruginosa*; with acetyltransferases (e.g. *aac(6')-Ib*) and 288 nucleotidyltransferases (e.g *ant*(2")-*Ia*) most frequent in Europe.<sup>34</sup> Since related genes in 289 mobile genetic elements encode AMEs and β-lactamases, β-lactam use may also predict 290 aminoglycoside resistance.<sup>35</sup> In previous analyses from Besançon, aminoglycosides, cefepime and fluoroquinolones were predictors of MexXY-OprM overproduction in *P. aeruginosa*. <sup>36</sup> 291 292 GRPa isolates were also more likely to overproduce the chromosomally-encoded AmpC 293 cephalosporinase (56% *vs.* 20%; p<0.001) and be multi-drug resistant (65% *vs.* 13%; 294 p<0.001). We hypothesized that GRPa incidence density may be predicted by use of 295 aminoglycosides, fluoroquinolones, extended-spectrum penicillins with β-lactamase 296 inhibitors, carbapenems, monobactams, and third- and fourth-generation cephalosporins.

297 Given potential intra-class differences in promoting resistance, we grouped use of gentamicin 298 and tobramycin separately from that of amikacin.

299

300 In the best-fit model ( $R^2$ =0.86), GRPa incidence density was strongly predicted by incidence 301 density in the previous month, and hospital use of gentamicin/tobramycin and 302 fluoroquinolones above minimum thresholds (Supplementary Table 1). No independent 303 association with Amikacin use was identified.

304

305 Declining GRPa was largely explained by falling inpatient use of gentamicin/tobramycin, 306 and, to a lesser extent, fluoroquinolones. Use of both drug groups was maintained below 307 minimum thresholds from around 2007. Continuing decreases in GRPa incidence density 308 were at least partially explained by autocorrelation at lower incidence densities. Reciprocal 309 increases in gentamicin-susceptible *P. aeruginosa* over the same period, and moderate 310 inverse correlation (r=-0.55), suggest competition for the same niche as GRPa. 311 Gentamicin/tobramycin and fluoroquinolone use should be maintained below thresholds to 312 control GRPa.

313

### 314 **Example 5: Methicillin-resistant** *Staphylococcus aureus* **(Antrim, Northern Ireland)**

315 We evaluated ecological variables explaining incidence density of MRSA clinical isolates in 316 adult admissions to a district general hospital in Antrim (Jan 2005 to Sep 2013,  $n=105$ ) 317 months). Between 2005 and mid-2008, incidence density of MRSA clinical isolates remained 318 stable at c.3.0 per 1000 OBDs (figure 5). Following restrictiong fluoroquinolones (January 319 2008) and intensification of hand-hygiene, burdens fell to 1.64 cases per 1000 OBDs by 320 2013.

321

322 The epidemic hospital MRSA clonal complex CC22, predominated in Northern Ireland 323 during the study period: its success attributed to an ability to acquire mobile genetic elements 324 carrying multiple resistance genes, with limited fitness costs.<sup>37</sup> Following prior linear time- $325$  series analyses from the region,<sup>14</sup> we hypothesised use of fluoroquinolones, 3GC, co-326 amoxiclav, and macrolides could be important predictors of MRSA epidemiology.

327

328 In the best-fit model ( $R^2$ =0.53), MRSA incidence density was positively associated with rates 329 of MRSA in the previous month and use of fluoroquinolones, 3GC, and co-amoxiclav 330 exceeding minimum thresholds (Supplementary Table 1). An inverse relationship was seen 331 with increased hospital use of alcohol-based hand rub (ABHR) up to 6.9 Litres per 1000 332 OBDs, above which further increases in ABHR use was not associated with further declines 333 in MRSA.

334

335 Declining MRSA incidence density was partly explained by deliberate restriction of 336 fluoroquinolone use, and concurrent declines in co-amoxiclav and 3GC. Strong 337 autoregression, and inverse association with ABHR use, were consistent with importance of 338 infection control measures in interrupting horizontal transmission. Reversal of previous 339 declines in fluoroquinolone use were seen by the last year of study. Findings suggested 340 maintaining use of co-amoxiclav and 3GC under thresholds, use of ABHR at threshold levels, 341 and further restriction of fluoroquinolones (table 1).

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### 346 **Discussion**

347 Using a non-linear time-series analysis (NL-TSA) approach, we found empirical evidence of 348 non-linear relationships between population antibiotic use and resistance rates in five 349 European settings. The method was generalisable to different clinical populations, resistant 350 pathogens, definitions of resistance burdens, and epidemiological phases. We demonstrated 351 that identification of minimum thresholds, and associated confidence intervals, could provide 352 population-specific quantitative targets for antibiotic stewardship.

353

354 Our approach builds upon earlier work using linear time-series analysis to explain temporal 355 relationships between antibiotic use and resistance.<sup>12-16</sup> NL-TSA shares a number of 356 strengths, including: low-informational demands; ease of reiteration as new data becomes 357 available; adjustment for the non-independence of serial observations and stochasticity 358 inherent to time-series of communicable diseases; identification of temporality in associations 359 and 'lagged' effects; and integration of impacts of multiple exposures.<sup>12</sup> Additionally, NL-360 TSA reveals non-linear relationships, providing more accurate understanding of how 361 modifying antibiotic use, infection control or other exposures is likely to affect resistance. 362 Limitations of NL-TSA include: the need for longer time-series than linear TSA; the potential 363 for spurious thresholds in areas of limited data or extremes of the exposure variable range; 364 and difficulty in identifying thresholds in situations of stable resistance and prescribing. We 365 note the poorer predictive performance of some models (e.g. example 3), may be explained 366 by absence of data on infection prevention and control activities, and resistance levels in 367 interacting populations.

368

369 Our findings may have important implications for antibiotic stewardship. In general, impacts 370 of changes in antibiotic use on resistance vary dependent upon the antibiotic use level. More 371 specifically, minimum thresholds may be interpreted as an upper limit for 'safe' population 372 antibiotic use which does not appear to substantially increase resistance rates at the 373 population level. Alternative theories may suggest the threshold indicates: a maximum level 374 of selection pressure not conferring a survival advantage to resistant pathogens to spread 375 within populations or ecological niches,  $8,12$  or strong enough to induce resistance;<sup>18</sup> or a 376 minimum level of use, below which antibiotic substitution creates equivalent or greater 377 selection pressure.<sup>8</sup> Crucially, they may provide quantitative targets for balancing the need to 378 access therapies with control of resistance, analogous to 'quotas' applied to other natural 379 resources which seek to maximize extracted value while maintain a non-declining stock.<sup>1,2,38</sup> 380 Moving from qualitative targets of reducing use, to quantitative targets may also aid 381 operational effectiveness. Targets appear to work best if pragmatic, collaborative and 382 iterative.<sup>39</sup> Complete restriction of use of agents is rarely feasible: in balancing access to 383 effective therapies with control of resistance, quantitative targets could align interests of 384 clinicians and antimicrobial management team.<sup>40</sup>

385

386 We emphasise the need for caution with interpretations of thresholds. Firstly, thresholds 387 should offer guidance rather than strict limits. Uncertainty around thresholds is variable, as 388 reflected in width of associated confidence intervals. Narrower confidence intervals around 389 threshold locate with reasonable precision the level of antibiotic use at which effects on 390 resistance are substantially altered. Wider intervals may indicate insufficient data, or the 391 influence of additional explanatory variables. In rare instances of multiple closely occurring 392 thresholds in a single functional relationship, the width of confidence intervals may be under-393 estimated and should be interpreted with particular caution. We suggest a pragmatic 394 approach, of interpreting thresholds depending upon the policy scenario. Where the priority is 395 strict control of resistance a conservative approach of limiting use to the lower limit of the

396 threshold confidence interval is advisable. Where excessive restriction is a concern, the 397 standard approach of limiting use to the point estimate of the threshold is likely to offer the 398 best balance between restriction and control of resistance. Secondly, changes in molecular 399 epidemiology under sustained antibiotic selection pressures, such as compensatory mutations 400 minimising fitness costs,  $26,27$  or strain replacement,  $24,25$  may mean thresholds vary by 401 epidemiological phase and time. Variation in thresholds across populations can be 402 anticipated, reflecting host, environment, and organism factors.<sup>23-25</sup> Therefore, models based 403 on local data and iterative analysis is necessary to ensure time and context-specific guidance. 404 Thirdly, it is important not to assume that all antibiotic use below thresholds is safe, since 405 antibiotic exposures may be important for individual patients, or cause unseen change in 406 reservoirs of resistant pathogens in environment or hosts.

407

408 Potential foci for further research include: evaluating the consistency of thresholds for 409 specific antibiotic use-resistance combinations across different settings and identifying 410 factors affecting thresholds; applying NL-TSA to composite indices of resistance;  $41,42$  use of 411 Bayesian approaches in selection of explanatory variables and analysis with short time-series 412 or rare resistance outcomes;<sup>43</sup> and prospective studies to validate the effectiveness of 413 quantitative targets in antibiotic stewardship.

414

415 We have illustrated how non-parametric time-series models based on empirical data can 416 identify non-linear relationships between population antibiotic use and resistance burdens. 417 Further we have shown how identification of population-specific minimum thresholds may 418 guide rational compromises between control of resistance and access to therapeutics. With 419 the increasing availability of electronic surveillance and healthcare systems, this approach 420 offers a useful tool for sustaining the effectiveness of current antimicrobials in many areas of 421 the world.

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### 446 **Methods**

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### 448 **Design and study populations**

449 This was a multi-centre time-series study. We used multivariable non-linear time-series 450 analysis to quantify associations between ecological exposures, including population use of 451 antibiotic groups, and rates of antibiotic-resistant infections in five populations from France, 452 Hungary, Northern Ireland (UK), and Spain (Supplementary Table 5).

453

454 The populations and resistance outcomes were a purposive sample, chosen to reflect varying 455 epidemiological scenarios, clinical settings, and resistant infections in European centres 456 participating in the THRESHOLDS (THReshold EStimation to Help Optimise Local 457 Decisions on antibiotic Stewardship) study group. This collaborative aims to further the 458 development of time-series analysis for understanding antibiotic resistance and planning 459 antibiotic stewardship. Members included centres with prior experience in applying linear 460 time-series approaches. Investigators were asked to identify an important resistance problem 461 in a defined clinical population from their region. Minimum data requirements were 462 consistent microbiological and prescribing data across a minimum of 60 monthly 463 observations (5 years). Duration of time-series was defined by the longest period of 464 consistent data for a minimum data set of the outcome and candidate explanatory variables.

465

466 For each population we described the regional scenario for the chosen outcomes, the 467 theoretical basis for inclusion of candidate explanatory variables, findings from the non-linear 468 time-series analysis, and how these could inform local antibiotic stewardship policy.

469

### 470 **Outcome and explanatory time series**

471 The outcome time-series for each population were: carbapenem-resistant *Acinetobacter*  472 *baumannii* (Debrecen, Hungary); extended spectrum β-lactamase producing *Escherichia coli* 473 in hospital and community (Orihuela, Spain); cefepime-resistant *Escherichia coli* (Seville, 474 Spain); gentamicin-resistant *Pseudomonas aeruginosa* (Besançon, France); and methicillin-475 resistant *Staphylococcus aureus* – MRSA (Antrim, Northern Ireland). Cases were defined 476 microbiologically as isolates from all relevant body sites not identified as infection control 477 specimens and meeting consistent criteria for resistance or resistance mechanism (see 478 supplemental file for details). Isolates from the same patient identified within 30 days of a 479 prior isolate with the same organism were considered part of the same infectious episode and 480 de-duplicated. Outcomes were expressed, where possible, as monthly incidence density of 481 resistant infections (cases per 1000 or 10,000 occupied bed days, OBDs). Where there were 482 large changes in testing frequency or organism identification over time, we defined resistance 483 as a percentage of clinical isolates from the same organism with any susceptibility pattern.

484<br>485 The primary explanatory variables were monthly population use of antibiotic agents 486 classified by pharmacological sub-group of antibacterials for systemic use (J01) in the 2016 487 WHO/ATC index, and expressed as defined daily doses (DDDs) per 1000 OBDs (hospital) or 488 1000 inhabitant-days (community). Candidate antibiotic sub-groups were identified *a priori*, 489 on the basis of regional co-resistance profiles, molecular epidemiology in the region, reviews 490 and prior evidence on individual or population level risk factors for acquisition of the 491 resistant infection. We included separate time-series for individual antibiotic agents or 492 chemical sub-groups only where there were strong theoretical grounds for investigating 493 independent associations, such as prior evidence of variable within-class actions or targeting 494 within antibiotic stewardship interventions.

496 In addition, we incorporated autoregressive terms capturing association between current 497 incidence density and incidence density in recent months. Where available, we incorporated 498 infection prevention and control (IPC) variables such as use of alcohol-based hand-rub. 499 Dummy variables were added to capture immediate and gradual impacts of changes in 500 laboratory methods or other planned interventions. We considered lags in association of up to 501 6 months and seasonal autoregressive terms (lag 12).

502

### 503 **Data collection and laboratory procedures**

504 In all centres, microbiological and prescribing and IPC data were extracted from electronic 505 databases maintained for routine healthcare activities. Data were anonymised and aggregated 506 before electronic submission to the THRESHOLDS study group. Meta-data on population 507 characteristics, IPC activities, antibiotic stewardship interventions and resources for control 508 of antibiotic resistance were captured using a standardised questionnaire.

509

510 Pathogens were identified using standard laboratory methods. Susceptibility testing was by 511 disc-diffusion (Besançon, Debrecen, Antrim) or broth microdilution (Seville, Orihuela). 512 Isolates were defined as resistant if not susceptible to an antibiotic agent according to zone 513 diameter (for disc-diffusion) or minimum inhibitory concentration (MIC, for broth 514 microdilution) breakpoints as recommended by the European Committee on Antimicrobial 515 Susceptibility Testing (EUCAST) or Clinical & Laboratory Standards Institute (CLSI). 516 Details of standards used, and deviations from EUCAST or CLSI criteria are detailed in table 517 i. Known changes in breakpoints and laboratory methods were adjusted for in time-series 518 analysis.

519

### 520 **Statistical methods**

521 In the following sections we provide a technical exposition of the statistical methods used. 522 We offer here, a brief description for the general reader.

523

524 Before applying non-linear time-series analysis (NL-TSA) to real-world datasets from study 525 populations, we performed a statistical, Monte-Carlo, experiment to illustrate its advantages 526 over, more familiar, linear TSA. We applied both linear and non-linear TSA to computer-527 simulated time-series, where the relationship between the outcome and explanatory time-528 series was known. Three types of relationship were explored: a linear relationship; a non-529 linear relationship without correlations between successive data points in time-series 530 (autoregression), and a non-linear relationship with autoregression; By running this 531 experiment over 10,000 simulated datasets for each type of relationship we evaluated the 532 typical ability of linear and non-linear TSA to describe the relationships accurately.

533

534 We next applied a seven-step non-linear time-series analysis approach to resistance problems 535 in study populations (figure 6).

536

537 Mirroring more familiar regression techniques, we started by defining a set of explanatory 538 variables including antibiotic use, infection control, population interactions, alongside terms 539 for autoregression. This set was defined by (a) expert opinion informed by prior risk-factor 540 studies, molecular epidemiology in the region; and (b) inspection of resistance profiles of the 541 pathogen of interest. We consider delays between changes in explanatory time-series and 542 associated change in outcome time-series (lags) of up to 6 months. Before analysis we 543 checked time-series and make adjustments for extreme values (outliers) or unexpected shifts 544 in mean (structural changes). We also used vector autoregression (VAR) models to help 545 distinguish any reverse causality in relationships between explanatory and outcome series:

546 this might occur, for example, if prescribing behaviour was altered by resistance rates in the 547 population in previous months. Next we restrict the set of explanatory variables, and lags, to 548 be put into final multivariable models. We use a procedure that fits smooth functions to 549 relationships between explanatory and outcome time-series, and allows visual inspection of 550 likely significant associations. After identifying the most promising explanatory variables 551 (and lags) we enter these into a Multivariate Adaptive Regression Splines (MARS) model 552 which both identifies significant predictors, and defines any non-linear relations as a series of 553 linear relationships connected by 'knots' or thresholds. Model fit for MARS is checked by 554 ensuring residuals were normally distributed without unexplained non-linearities. Confidence 555 intervals around each threshold were fit by a conditional conservative inverted likelihood 556 ratio (CCILR) method, using partial residuals. Finally, we converted thresholds from models 557 into suggested maximum total treatment courses per month in the population by multiplying 558 model thresholds by the size of the population and dividing by an average treatment course.

559

#### 560 **Figure 6: Summary of the 7-step non-linear time-series methodology and potential**  561 **pitfalls**

#### **Step 1: Theoretical foundation**

Identification of antibiotic sub-groups or agents, infection control interventions, and other ecological variables hypothesised to predict the outcome:

- Prior evidence on risk-factors
- Regional molecular epidemiology
- Most frequent co-resistances in antibiograms of resistant pathogen

#### **Step 2: Data validation**

Review of time-series to identifiy unanticipated step-wise changes in time-series(Chow's test), or outliers (Cooks distances) and to make appropriate adjustment or replacements

#### **Step 3: Identifying the most likely predictors and their lags**

- Direction of temporal association explored by vector autoregression (VAR) analyses
- Significant associations (and lags) identified by inspection of plots from multivariable General Additive Model (GAM) plots.

#### **Step 4. Multivariable model estimation**

• Multivariate Adaptive Regression Splines(MARS) procedure to select and estimated final multivariable models, and describe associations in terms of one or more stable linear functions linked by thresholds or 'knots'.

#### **Step 5: Diagnostic checks of model fit**

- Normal distribution of residuals with mean zero, and homogenous variance
- Absence of residual autocorrelation, evaluated by autocorrelation function (ACF) plots
- Absence of residual non-linearities in Hinich Test

#### **Step 6. Confidence intervals for thresholds**

• Conditional conservative inverted Likelihood Ratio (CCILR) confidence intervals for each threshold generated using partial residuals after adjustment for other covariates and thresholds.

#### **Step 7. Interpretation**

- Suggested maximum total treatment courses per month calculated as:
- Threshold values (DDDs per 1000 OBDs or IDs) x population size (OBDs or IDs per month) Average treatment course in DDDs (e.g. 7).
- Comparison to current total treatment courses per month in population



564 To provide an example of how model findings can inform policy, for the Orihuela population, 565 we predicted the effects of restricting antibiotic use to threshold levels compared to a 566 'business as usual' scenario of prescribing based on the last months of study. We quantify 567 impacts of immediate restriction sustained over two years.

568

570

569 A technical explanation follows:

### 571 **a) Comparing linear and non-linear time-series model performance**

572 We used a Monte-Carlo experiment to compare the ability of linear (Ordinary Least Squares, 573 OLS) and non-linear (Multivariate Adaptive Regression Splines, MARS) time-series models 574 in identifying various pre-defined functional relationships between simulated explanatory and 575 outcome time-series. We hypothesised that for time-series related by simple linear processes 576 MARS and OLS regression methods would perform equally well, but that only MARS would 577 accurately identify non-linear associations. We generated 10,000 simulated datasets using 578 simple stochastic processes incorporating the following pre-defined functional relationships:

579

580 (i) Non-autoregressive without threshold

$$
\frac{581}{582}
$$

$$
y_t = -4 + 2x_t + u_t \quad u_t \sim N(0, \sigma^2 = 0.02) \quad \forall t = 1, \cdots, 200
$$

584

583 (ii) Non-autoregressive with threshold

$$
\begin{cases}\n\text{if } x_t \le 2; & y_t = u_t \\
\text{if } x_t > 2; & y_t = -4 + 2x_t + u_t \\
\end{cases} \quad u_t \sim N(0, \sigma^2 = 0.5) \quad \forall t = 1, \cdots, 200
$$

585 586

587 (iii) Autoregressive with threshold

588

589

$$
\begin{cases} if x_t \le 0; \quad y_t = 0 + \rho y_{t-1} + u_t & u_t \sim N(0, \sigma^2 = 0.05) \\ if x_t > 0; \quad y_t = 0 + \rho y_{t-1} + 1 x_t + u_t & u_t \sim N(0, \sigma^2 = 0.05) \end{cases} \forall t = 1, \cdots, 200
$$

590 Where:

 $x_t$  is the explanatory (independent) time-series variable at time *t*  $y_t$  is the outcome (dependent) time-series variable at time *t*  $u_t$  is the error term at time *t*, with Normal distribution, zero mean and variance  $\sigma^2$  $\rho y_{t-1}$  is an autoregressive term or order 1 (i.e. dated at *t*-*1*) with  $\rho = 0.25$ 

595

596 For each dataset we fitted both linear and non-linear time-series analyses, and recorded sample parameter estimates (*a* constant, *b* slope, and  $s^2$  as the estimate of population 598 variance) and a measure of goodness of fit  $(R^2)$ . Histograms were created illustrating the 599 distributions of  $R^2$  values and parameter estimates from both linear and non-linear models. 600 Visual comparison was made to pre-defined parameter values to identify bias in parameter 601 estimates. We used a t-test of mean difference for independent samples to compare model 602 performance based on  $R^2$  values.

603

### 604 **b) Applications of non-linear time-series analysis to real-world datasets**

605 We applied a seven-step approach to generate non-linear time-series models describing how 606 contemporaneous and prior population antibiotic use, and other ecological variables, explain 607 monthly variation in clinical burdens from antibiotic-resistant infections in five European 608 centres.

- 610
- 611
- 612

### 613 *Step 1: Theoretical foundation*

614 Participating centres identified *a priori* a minimum dataset of antibiotic sub-groups or agents 615 they considered most likely to affect the epidemiology of the resistant organism under 616 investigation (target organism). Decisions were based upon: previous empirical evidence of 617 risk factors and molecular epidemiology in the study region or related contexts. Additionally, 618 using antibiogram data from the study period and population, we reviewed co-resistances to 619 other antibiotics among isolates of the target organism with and without the resistance under 620 investigation. We considered antibiotics with the largest absolute rates of co-resistance in the 621 resistant isolates to be most likely to exert significant selection pressures.<sup>44,45</sup> Consensus on 622 the list of potential predictive variables was found through discussion among all 623 THRESHOLDS study group members.

624 Where data was available we integrated additional explanatory variables on hospital activity 625 or infection control activities, associated with the outcome variable in previous studies.

626

### 627 *Step 2: Data validation*

628 To ensure consistent time-series we first accounted for known changes in exogenous 629 conditions, such as changes in laboratory method. We captured immediate and gradual effects 630 by entering a dummy variable (0 in months before the change, 1 in months after change) and 631 its interaction with an autoregressive term, as explanatory variables. We then reviewed time-632 series to detect possible unknown measurement errors as follows. Visual inspection identified 633 potential structural changes (seen as large step-wise change in mean for instance) or outliers 634 (seen as values deviating substantially from surrounding values). Successive Chow tests were 635 applied to automatically detect the most probable dates of structural changes in the time-636 series and, where necessary, to disaggregate the sample into two or more segments, each with 637 a stable mean. For each segment we applied an outlier detection technique using the 638 following criterion: an observation was considered as an outlier if Cook's distance at this 639 point was greater than five times the mean of Cook's distances of all the observations of the 640 segment. Finally, we replaced outlier values with the mean of the three preceding and three 641 following observations.

642

643 *Step 3 Identifying the most likely predictors and their lags* 

644 Given the potentially complex relationships between ecological variables under investigation 645 we sought to refine our understanding of potential associations before applying final 646 multivariable non-linear models.

647

648 Firstly, situations of reverse causality could exist when ecological exposures - such as rates of 649 infections with resistant pathogens connected populations, or use of some antibiotic groups in 650 a given population - respond to, rather than predict, rates of resistance. In order to minimise 651 this risk, we tested direction of temporal relationships between explanatory and outcome 652 time-series by applying Granger-causality analysis and Vector Autoregression (VAR) 653 models. Secondly, non-linear models of the type used in this study are potentially complex 654 and difficult to extract form the data if too many predictors are used at the same time. 655 Therefore, we carried out an additional *a priori* data-based selection of candidate explanatory 656 variables and lags (the lag refers to the delay in months between change in exposure and 657 associated change in outcome). This was done through inspection of outputs from fitting a 658 General Additive Model (GAM) to the data. GAM is a very general procedure that can be

659 used for the identification of the most likely predictors, since it runs a non-parametric 660 estimation of the functional relationships between explanatory (*x*) and outcome (*y*) time-661 series, based upon iterative data fitting, rather than prior assumptions. It also allows for 662 variability in the functional relationships across different values of the explanatory variables 663 and can therefore capture non-linear associations between ecological variables and resistance outcomes.49 664 In particular, we used the GAM procedure in the SCAB34S Splines module 665 (available in SCA Workbench, Scientific Computing Associates Corp, Illinois, USA) to 666 define the relationship between  $p$  explanatory  $(x)$  and the outcome  $(y)$  time-series as a sum of 667 smooth, or spline, functions:

$$
E(y|x_1, x_2, ..., x_p) = s_0 + \sum_{j=1}^r s_j(x_j)
$$

668

where  $(s_i(x_i))$  are the spline functions; they were standardised such that, after removal of free 670 constants  $(s_o)$  their expected contribution to the outcome (*y*) is zero (i.e. Es<sub>i</sub>(*x<sub>i</sub>*)=0 for each *j*).

671

672 The splines were derived by a process of splitting the time-series into sections, joined at knot 673 points, and fitting simple curves described by cubic functions to the data in each section. The 674 GAM methodology identified the optimal combination of spline functions  $s_i(x_i)$ , following 675 the iterative procedure suggested by Hastie and Tibshirani(1986).<sup>46</sup> Combining a local 676 scoring algorithm and a backfitting procedure, this method converges on a solution balancing 677 data fit with smoothness.

678

679 To identify the most relevant explanatory time-series, for each centre we started with a 680 multivariable GAM model including all theoretically relevant variables at lags of 1 to 6 681 months and autoregressive terms at lags 1 and 2. We limited lags to 6-months based on 682 widespread evidence of declining relevance of antibiotic exposures by time-since exposure, 683 and prior experience that considerations of longer lags lead to problems of concurvity. On 684 the basis of the GAM outputs, an explanatory variable with a specific lag was retained in the 685 model only if its contribution was significant at a 5% level of probability (identified on 686 contribution charts by the zero line of non-association falling outside of 95% confidence 687 intervals around the estimate). The process was run iteratively by removing first those 688 variables and lag combinations whose contributions were non-significant before re-running 689 the GAM model on a reduced subset of variables and lags. The process stopped when the 690 model contained only significant contributions of variables and lags. These constituted the 691 restricted set of explanatory variables for entry into MARS analysis.

692

693 A further objective of applying the GAM procedure was to determine whether consideration 694 of non-linear associations is justified in terms of improvement in predictive performance. For 695 each explanatory variable (and lag), GAM provides a comparison of the data fit of a non-696 linear spline function (*nl*) with an analysis in which this relationship is restricted to a linear 697 function (*l*). Significant improvement in goodness of fit over a linear fit is defined by an *F*-698 test, as follows:

699

$$
F_0 = \frac{(SSR_l \cdot SSR_{nl})/(p_{nl} \cdot p_l)}{SSR_{nl}/(n \cdot p_{nl})} \sim F_{(df_{nl} \cdot df_l),(n \cdot p_{nl})}
$$

701

702 where;  $SSR = Sum$  of squares of residuals,  $n = number$  of observations,  $p = number$  of 703 parameters, *l* = linear function*,* and *nl* = non-linear spline function.

704 The null hypothesis that estimates from an enhanced (non-linear) model do not provide a 705 significantly better fit than those from a linear model can be rejected where *F* exceeds a 706 critical value ( $a = 0.05$ ) from an F-distribution with ( $p_{nl}$ - $p_l$ ,  $n-p_{nl}$ ) degrees of freedom.

707

### 708 *Step 4. Multivariable model estimation*

709 After identifying the most likely explanatory variables (and lags), and whether associations 710 with the outcome series were linear or non-linear, we used the MARS procedure (in the 711 SCAB34S Splines module) to obtain an easily interpretable characterization of these 712 associations.<sup>47</sup> MARS is a non-parametric regression approach suitable for situations of non-713 linear associations that can provide more interpretable and interesting empirical results than 714 GAM. Given our research aims, its particular advantages were: (i) the ability to identify 715 distinct threshold values ('knots') of the explanatory variables delimiting regions (ranges of 716 values) of individual or interacting explanatory variables within which associations with the 717 outcome differs substantially from those in other regions; and (ii) a systematic approach for 718 model identification and estimation, which automatically selects the combination of 719 explanatory variables and threshold values which most efficiently explain variation in 720 outcomes. MARS is related to, but more general than, regression tree algorithms, and has 721 several important, interrelated advantages: (a) when thresholds may affect several 722 explanatory variables, the final MARS model is far more synthetic, and therefore more 723 interpretable, in terms of quantifying how each explanatory variable (e.g. antibiotic use) 724 affects the response variable (e.g. resistance) and interacts with other explanatory variables; 725 (b) the MARS algorithm in general deals much better with numerical data and continuous 726 data; (c) it allows for dynamic relationships and thresholds in the dynamic dependences - 727 especially important when analysing effects with time series data; and (d) MARS does better 728 in extrapolating the results outside the sample data ranges of explanatory and outcome 729 variables. These advantages are important when considering policy implications of findings 730 for control of AMR.

731

732 MARS approximates the functional relationship between an outcome time-series (*yt*) and a

733 vector of *p* explanatory variables  $x_t = (x_t^1 \dots x_t^p)$  as: 734

$$
y_t = \beta_0 + \sum_{m=1}^{M} \beta_m b_m(x_t) + \varepsilon_t
$$

735 where;

 $\beta_0$  is a constant  $β_m$  is the coefficient for the *m<sup>th</sup>* basis function, m=1,...,M  $b_m(x_t)$  is the  $m^{th}$  basis function, m=1,...,M  $\varepsilon_t$  is an independently distributed error term.

740 The basis functions are products of up to two truncated linear or hinge functions, describing 741 the relationship between one or more explanatory variables and the outcome in terms of 742 segments of stable association separated by knots or thresholds values. These interacting 743 hinge functions allow us to identify possible interactions between variables as in Figure 744  $IC(ii)$ . Namely, the  $m<sup>th</sup>$  basis function takes one of the following two forms:

745 No interaction: 
$$
b_m(x_t) = h(x_t^k, t_{k,m})
$$
 for some  $k = 1, ..., p$ 

 $\mathbb{R}^2$ 

746 With interaction: 
$$
b_m(x_t) = h_m(x_t^k, t_{k,m}) \cdot h_m(x_t^j, t_{j,m})
$$
 for some  $k, j = 1, ..., p, k \neq j$ 

747 where  $t_{k,m}$  is the threshold value of  $x_t^k$  in the  $m^{th}$  basis function and where  $h(x_t^k, t_{k,m})$  is a

748 hinge function that takes the following form depending on whether the basis function takes 749 effect above or below the threshold  $t_{k,m}$ 



753 If no knot (threshold) is detected, then a simple linear (and therefore constant) association 754 between explanatory and outcome variable can be specified as a single function applied 755 across the total range of values of the explanatory variable.

756

752

757 All potentially significant explanatory variables, and associated lags, identified in previous 758 steps, were incorporated into models. Model identification and estimation proceed by an 759 automated, iterative, process:

760

761 *Forward pass:* starting with the simplest model containing only a constant basis function, 762 MARS generates a matrix of basis functions in a forward stepwise manner. Candidate base 763 functions are added in order of ability to improve model fit, until the model reaches a 764 predefined limit of complexity. The candidate basis functions are identified by a nested 765 exhaustive search looping over the existing set of basis functions, and all other possible 766 explanatory variables (or interactions) and knot positions.

767

768 *Backwards (pruning) pass:* During the subsequent pruning pass MARS removes basis 769 functions contributing least to model fit, until no significant improvement is seen in a 770 modified form of the generalized cross validation (MGCV) criterion:

$$
MGCV = \frac{\frac{1}{N} \sum_{i=0}^{n} (y \cdot f(x))^{2}}{1 - ((C(M) + dM)/n)^{2}}
$$

771 772

773 Where;  $N$  is the number of observations,

774  $\sum_{i=0}^{n} (y - f(x))^2$  is the sum of square of residuals (observed - estimated y). 775 *C(M)* is the number of parameters being fitted, *M* the number of non-constant basis 776 functions and *d=3* (conventional value).

777

778 The MGCV incorporates a complexity penalty accounting for the inherent improvement in 779 explained variance associated with increasing numbers of basis-functions, and its calculation 780 allows estimates of the relative importance of each basis function. Model selection therefore 781 converges on a set of basis functions that most efficiently explain variation in antibiotic 782 resistance before a final model fit by OLS estimation.

783

784 From the output of each MARS model we generated contribution charts illustrating the 785 change in the outcome time-series across the observed ranges of explanatory variables. 786

787 *Step 5. Diagnostic checks* 

788 Adequacy of model fit was defined by three criteria: (i) *Normally distributed residuals* – with 789 homogenous variance and mean equal to zero, as evaluated by a Normality test; (ii) *absence*  790 *of significant residual autoregression* – identified in lags 0 to 6 on an autocorrelation function 791 (ACF) plot; and (iii) *absence of residual non-linearities* – as evaluated by a Hinich test. In addition to the MGCV we reported more familiar measures of model performance such as  $R^2$ 793 and the mean absolute percentage error (MAPE).

794

795 *Step 6: Confidence intervals (CIs) for thresholds values* 

796 In the absence of an existing method for deriving measures of uncertainty around thresholds 797 derived from non-parametric MARS models, we develop a procedure inspired by Hansen (2000).48 798 His procedure considers a simple threshold model with only one variable affected 799 by a threshold effect, and obtains a distribution theory for the threshold parameter  $(\tau)$  from 800 which asymptotic confidence intervals can be built. He first derives the limiting distribution 801 of a Likelihood Ratio test (LR) for the null hypothesis that the threshold parameter  $\tau = \tau_0$ . He 802 then builds confidence intervals through the inversion of LR: the  $(1-\alpha)$  Inverted Likelihood 803 Ratio (ILR) confidence interval consisting of all the possible values of  $\tau$  for which the null 804 hypothesis would not be rejected at the  $\alpha$  level. Donayre et al. (2018) examine improvements 805 of Hansen's ILR confidence interval, increasing its quality in finite samples with large 806 threshold effects (i.e. when the change in slope from one side of the threshold to the other is 807 large).<sup>49</sup> They show that a 'conservative modification' enlarging Hansen's ILR confidence 808 interval is optimal. In this "conservative ILR confidence interval" the lower end of the 809 interval is enlarged from the first value lower than  $\tau_1$  for which the null hypothesis is 810 rejected, up to  $\tau_i$ ; at the upper end, it is enlarged from  $\tau_u$  up to the first value greater than  $\tau_u$ 811 for which the null hypothesis is rejected. This modification provides intervals at a confidence 812 level at least as high as the nominal one that are still informative.

813

814 We adapted this procedure for MARS estimations with more than one explanatory variable 815 containing thresholds, and one or more thresholds per variable, by using the partial residuals 816 –i.e. the variation in the outcome not explained by other explanatory variables and their 817 thresholds. This allowed us to identify conservative ILR confidence intervals for each 818 explanatory variable, conditional on all the estimated coefficients and thresholds other than 819 the one for which the confidence interval is computed. Since in MARS all thresholds and 820 slope coefficients are anyway selected and estimated to optimise overall model fit using 821 conditional inference, identifying these 'conditional conservative ILR (CCILR) confidence 822 intervals' does not impose costs to reliability. Computing confidence intervals conditional 823 only on other thresholds, but with re-estimation of coefficients describing piece-wise 824 associations (slopes), offers a valid alternative. In Monte Carlo simulations (results available 825 on request) we found both approaches resulted in adequate coverage (>95% of intervals 826 including the actual value of the threshold) but CIs were wider with a procedure with slope 827 re-estimation and less informative for a given coverage rate. Our simulations show that the 828 superiority of the partial residual approach is independent of the degree of correlation 829 between antibiotic segments (values of antibiotic use over which association with the 830 outcome is constant) where correlation is between 0% and 75%. There is some risk of very 831 slight under coverage with the partial residual approach where correlations are  $\geq$ 85%, but 832 such high levels of correlation are unlikely unless several the functional relationship involves 833 multiple, closely occurring, thresholds. In such situations, re-estimation of slope co-efficients 834 is anyway not feasible. As a result, we recommend the partial residual approach, with a 835 caution that the CI could be somewhat wider in specific and infrequent situations where 836 multiple close thresholds for the same independent variable are detected (e.g. fluoroquinolone 837 association with %Ec-ESBL in Orihuela hospital population).

838 *Step 7. Interpretation* 

839 The minimum thresholds identified for each significantly associated antibiotic group were 840 translated into suggested maximum numbers of patient treatment courses per month not 841 expected to adversely affect resistance at population levels. We multiplied the threshold, 842 expressed in DDDs per 1000 OBDs (or IDs), by the size of the monthly patient population (in 843 thousands of OBDs or IDs), and then divided by an average patient treatment course of 7 844 DDDs (except for aminoglycosides which were considered as 3 DDDs). These maximums 845 were further compared to contemporary levels of antibiotic use in the last year of study, to 846 provide indications of how current use of antibiotics should be modified to avoid resistance 847 spread.

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- 

### **Projections for alternative antibiotic stewardship policy options**

851 To illustrate the potential effects of restricting antibiotics associated with %Ec-ESBL+ to 852 threshold levels in populations of Orihuela, we compared the expected evolution of %Ec-<br>853 ESBL+ under a 'business as usual' scenario in which antibiotic use continued as in last year ESBL+ under a 'business as usual' scenario in which antibiotic use continued as in last year 854 of study, to projected time-series with antibiotics restricted to threshold levels. We used a 855 breakpoint analysis to identify the last stationary segment in %Ec-ESBL+ time-series from 856 the study period. We recursively estimated MARS models using means from these stationary 857 segments as starting points to derive steady states for %Ec-ESBL+ in community and 858 hospital populations. Based on steady state values and MARS models for the study period 859 (baseline) we simulated 1000 samples of 24-month projections, incorporating random error 860 term with variance as derived in the baseline MARS model. For each sample projection we 861 entered mean antibiotic levels in the last year of the study period ('business as usual') and 862 alternative levels set at identified thresholds. We calculated the mean difference between 863 business as usual and each policy option for every month along with 95% confidence 864 intervals. Finally, we illustrated alternative projections and differences using medians of 865 distributions from the 1,000 sample projections.

 

### **Data availability**

869 The data that support the findings of this study are available from the corresponding 870 author upon reasonable request.

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### 1101 **Supplementary information**

- 1102 Is available in the online version of the article
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### 1122 **Author contributions**

1123 J-M.L-L., T.L., C.N., A.B., and I.M.G., proposed the original idea and designed the study. 1124 X.B., D.H., M.A., G.C-B., M.S., D.F., G.K., J.R-B., P.R., and N.G., collated centre-specific 1125 data, situational analysis, and hypotheses. J-M.L-L., T.L., C.N., A.B., contributed to 1126 statistical analysis, with C.N. and A.B, the principal analysts. All authors discussed the 1127 results and commented on the manuscript.

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### 1129 **Competing interests**

1130 IMG is in receipt of payments for consultancies and lectures from numerous Pharmaceutical 1131 firms developing new antimicrobials. Otherwise, the authors declare no competing interests.

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### 1140 **Figure legends**

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### 1142 **Figure 1 | Carbapenem-resistant** *A. baumannii* **and antibiotic use**

1143 **(a)** Time series for observed and predicted incidence density of CRAb, with observed

1144 incidence density of CSAb. **(b)** Time series for use of potential explanatory antibiotic groups

- 1145 (5-month moving averages). **(c)** Contribution charts illustrating the relationship between
- 1146 explanatory variables and CRAb incidence density (sample size, n=143 months of 1147 observation).
- 1148 <sup>a</sup> Change relative to median monthly CRAb incidence density for study period.
- 1149 CRAb, carbapenem-resistant *A. baumannii.* CSAb, carbapenem-susceptible *A. baumannii*.
- 1150 DDDs, defined daily doses. IQR, Interquartile range. MARS, Multivariate Adaptive
- 1151 Regression Splines. NL-TSA, non-linear time series analysis. OBDs, occupied bed days.
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### 1153 **Figure 2 | Extended-spectrum β-lactamase (ESBL)-producing** *Escherichia coli* **and**  1154 **antibiotic use in hospital and community.**

- 1155 **(a)** Time series for observed and predicted %Ec-ESBL+ in hospital population. **(b)** Time
- 1156 series of potential explanatory antibiotic groups in hospital population (5-month moving
- 1157 averages). **(c)** Time series for observed and predicted %Ec-ESBL+ in community population.
- 1158 **(d)** Time series of potential explanatory antibiotic groups in community population (5-month
- 1159 moving averages). **(e)** Contribution charts illustrating the relationship between explanatory
- 1160 variables and hospital or community %Ec-ESBL+. (sample size, n=304 months of
- 1161 observation).
- 1162  $\alpha$  compared to median monthly %Ec-ESBL+ for study period.
- 1163 \* confidence interval around lower threshold in association between fluoroquinolones and
- 1164 %Ec-ESBL+ in hospital may be wider due to risk of slight under-coverage of confidence
- 1165 interval estimation arising from a problem of multiple closely occurring thresholds.
- 1166 %Ec-ESBL+, percentage of *E. coli* isolates producing extended-spectrum beta-lactamases.
- 1167 DDDs, defined daily doses. IQR, Interquartile range. MARS, Multivariate Adaptive
- 1168 Regression Splines. NL-TSA, non-linear time series analysis. OBDs, occupied bed days.
- 1169

### 1170 **Figure 3 | Cefepime-resistant** *Escherichia coli* **and antibiotic use**

- 1171 **(a)** Time series for observed and predicted incidence density of %Ec-FepR. **(b)** Time series
- 1172 of potential explanatory antibiotic groups (5-month moving averages). **(c)** Contribution charts
- 1173 illustrating the relationship between explanatory variables and %Ec-FepR (sample size,
- 1174 n=105 months of observation).
- 1175 <sup>a</sup> compared to median monthly %Ec-FepR for study period.
- 1176 DDDs, Defined Daily Doses. IQR, interquartile range. %Ec-FepR, percentage of *E. coli*
- 1177 isolates resistant to cefepime. OBDs, Occupied Bed Days.
- 1178<br>1179

### 1179 **Figure 4: Gentamicin-resistant** *Pseudomonas aeruginosa* **and antibiotic use**

- 1180 **(a)** Time series for observed and model predicted incidence density of GRPa. **(b)** Time series
- 1181 of potential explanatory antibiotic groups (5-month moving averages) **(c)** Contribution charts
- 1182 illustrating the relationship between explanatory variables and GRPa incidence density
- 1183  $\alpha$  compared to median monthly GRPa incidence density for study period (sample size, n=192) 1184 months of observation).
- 1185 DDDs, Defined Daily Doses. GRPa, gentamicin-resistant *P. aeruginosa*; GSPa, gentamicin-
- 1186 susceptible *P. aeruginosa* isolates. IQR, Interquartile range. MARS, multivariate adaptive
- 1187 regression splines OBDs, Occupied Bed Days.
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# 1240 **Tables**  1240<br>1241<br>1242

# 1242 **Table 1: Translation of thresholds identified in non-linear models into population-**

specific antibiotic stewardship policy recommendations



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— **III** —

**c**

- - Estimated change in outcome by level of explanatory variable

Current use level (circle) and suggested change in  $- - - - - \spadesuit$ use for standard (solid arrow) or conservative (dashed arrow) policy options





- Median (IQR) and range of monthly antibiotic use
	- Estimated change in outcome by level of explanatory variable

Threshold and 95% confidence interval

Current use level (circle) and suggested change in use for standard (solid arrow) or conservative (dashed arrow) policy options



**c**







**d**



**c**

Estimated change in outcome by level of explanatory variable



Current use level (circle) and suggested change in use for standard  $\bullet$ (solid arrow) or conservative (dashed arrow) policy options