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Assessment of inner-outer interactions in the urban boundary layer using a predictive model

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Urban-type rough-wall boundary layers developing over staggered cube arrays with plan 6 area packing density, λ_p , of 6.25%, 25% or 44.4% have been studied at two Reynolds 7 numbers within a wind tunnel using hot-wire anemometry (HWA). A fixed HWA probe 8 is used to capture the outer-layer flow while a second moving probe is used to capture the q inner-layer flow at 13 wall-normal positions between 1.25h and 4h where h is the height 10 of the roughness elements. The synchronized two-point HWA measurements are used to 11 extract the near-canopy large-scale signal using spectral linear stochastic estimation and 12 a predictive model is calibrated in each of the six measurement configurations. Analysis of 13 the predictive model coefficients demonstrates that the canopy geometry has a significant 14 influence on both the superposition and amplitude modulation. The universal signal, the 15 signal that exists in the absence of any large-scale influence, is also modified as a result 16 of local canopy geometry suggesting that although the non-linear interactions within 17 urban-type rough-wall boundary layers can be modelled using the predictive model as 18 proposed by Mathis et al. (2011a), the model must be however calibrated for each type of 19 canopy flow regime. The Reynolds number does not significantly affect any of the model 20 coefficients, at least over the limited range of Reynolds numbers studied here. Finally, 21 the predictive model is validated using a prediction of the near-canopy signal at a higher 22 Reynolds number and a prediction using reference signals measured in different canopy 23 geometries to run the model. Statistics up to the 4^{th} order and spectra are accurately 24 reproduced demonstrating the capability of the predictive model in an urban-type rough-25 wall boundary layer. 26

27 **1. Introduction**

As urbanization continues to advance, our cities are faced with significant challenges 28 related to air quality. These challenges are exacerbated by the complexity of the ur-29 ban geometry and the dynamic processes that take place within the urban canopy and 30 above within the atmospheric boundary layer. The urban boundary layer contains co-31 herent structures such as large-scale turbulent organized structures of either high or low 32 momentum that form above the roughness in the inertial layer from groups of hairpin 33 vortices (Adrian et al. 2000). Within the roughness sublayer, shear layers form along 34 the top of the upstream roughness elements and contain small-scale structures induced 35 by the presence of the roughness (Coceal et al. 2007). These turbulent structures and 36 the intermittent exchanges they produce govern the transport of heat, momentum and 37 pollution in the urban canopy and understanding these turbulent structures and how 38 they interact is crucial to addressing the challenges facing our cities today. 39

In smooth-wall boundary layers, in addition to the superposition mechanism of the large scales onto the near-wall flow (Townsend 1976), a non-linear mechanism of amplitude modulation has been recently shown to exist between the large-scale structures

Karin Blackman, Laurent Perret, Romain Mathis

in the inertial layer and the small scales close to the wall (Hutchins and Marusic 2007; 43 Mathis et al. 2009, 2011b,c; Marusic et al. 2011; Inoue et al. 2012). As large-scale regions 44 of high (low) momentum pass over the small scales close to the wall the small scales are 45 amplified (suppressed) (Mathis et al. 2009). This mechanism was first observed experi-46 mentally by Rao et al. (1971) who noted a strong non-linear coupling between the inner 47 and outer layer in the smooth-wall boundary layer. More recently, amplitude modulation 48 has been shown to increase with increasing Reynolds number as large-scale structures be-49 come more intense thereby contributing more to the turbulent interactions (Mathis et al. 50 2009). Furthermore, all three components of velocity have been shown to be modulated 51 by the large scales in a similar manner (Talluru et al. 2014). The near-wall evolution 52 of the amplitude modulation has been found to show strong similarities with the skew-53 ness profile of the streamwise velocity component (Mathis et al. 2009). This resemblance 54 was found to be due to one component of the scale-decomposed skewness (see §4.3 for 55 more details), which proved to be a good diagnostic quantity to study the presence of 56 amplitude modulation (Mathis et al. 2011c; Duvvuri and McKeon 2015). It should be 57 noted that strong correlation between large-scale structures and small-scale amplification 58 or suppression does not imply that the large-scales actively modulate the small scales. 59 However, some recent studies, such as Duvvuri and McKeon (2015), have found evidence 60 that support this causality. 61

Amplitude modulation has also been confirmed to exist using DNS in a d-type 2D bar-62 roughened wall with plan area packing density $\lambda_p = 12.5\%$ (the ratio between the area of 63 the surface occupied by the roughness elements and the total surface area) (Nadeem et al. 64 2015), using LES of a staggered cube array with $\lambda_p = 25\%$ and homogenous roughness 65 (Anderson 2016) and experimentally in a sand-roughened wall (Squire et al. 2016) and 66 rod-roughened wall (Talluru et al. 2014). In each of these cases the amplitude modulation 67 was modified compared to the smooth-wall flow configuration, but the nature of the 68 mechanism remained the same. The amplitude modulation was shown to be stronger in 69 rough-wall flows compared to smooth-wall boundary layers, the presence of the roughness 70 causing a wall-normal shift of the peak spectral energy of the near-wall small scales 71 resulting in a modification of the amplitude modulation behaviour in both the near-72 wall and outer-wall regions (Anderson 2016; Talluru et al. 2014). This modification was 73 shown to cause the large-scale structures of the outer layer to interact with both the 74 near-wall small scales and small scales away from the wall (Nadeem et al. 2015). When 75 investigating the influence of buoyancy effect using LES Salesky and Anderson (2018) 76 found that an increase in convection resulted in an increase in the angle of inclination 77 of near-surface large-scale structures. This in turn causes a shift in the location of the 78 outer peak of the streamwise velocity spectra until the energy is concentrated in a single 79 peak. Although the modulation is shown to decrease as the large-scale structures change 80 from streamwise to vertically dominated the modulation is still present over all cases 81 studied. Awasthi and Anderson (2018), who studied amplitude modulation in the flow 82 over roughness with spanwise heterogeneity, found that the outer peak was present in 83 upwelling zones but not present in downwelling zones where structures were steeper and 84 shorter. 85

Evidence from experiments performed in a boundary layer developing over a rough wall consisting of staggered cubes with $\lambda_p = 25\%$ confirmed the existence of a non-linear interaction between the most energetic large-scale structures present above the canopy and the small-scale structures induced by the presence of the roughness (Blackman and Perret 2016). The analysis of the spatio-temporal modulation coefficient confirmed the existence of a mechanism similar to amplitude modulation and demonstrated that the large-scale momentum regions influence the small scales within the roughness sublayer

Scale interactions in the roughness sublayer of the urban-type boundary layer 3

after a time delay, agreeing with the results of Anderson (2016). Further evidence of 93 amplitude modulation within this staggered cube roughness configuration was found 94 by Basley et al. (2018) through investigation of the characteristics of the amplitude 95 modulation coefficient of the three velocity components and the turbulent kinetic energy 96 in a wall-parallel plane located in the roughness sublayer (*i.e.* just above the top of the 97 roughness elements). Recently, using triple decomposition of the kinetic energy budget 98 in a boundary layer developing over staggered cubes with $\lambda_p = 25\%$ this non-linear relationship was linked to an instantaneous exchange of energy between the large-scale 100 momentum regions and the small scales close to the roughness (Blackman et al. 2018). 101 Finally, investigation of this non-linear relationship has been expanded to the study of 102 street canyon flows using six rough-wall boundary layer configurations consisting of three 103 upstream roughness geometries (cubes or 2D bars with different streamwise spacing) and 104 two street canyon aspect ratios (Blackman et al. 2017). Although a modification of the 105 non-linear relationship exists close to the top of the roughness elements between 3D and 106 2D roughness, the non-linear mechanism similar to amplitude modulation was confirmed 107 to exist in all of the configurations. 108

The study of amplitude modulation in the smooth-wall boundary layer has led to 109 the development of a predictive model for the near-wall fluctuations using a large-scale 110 boundary layer signal (Mathis et al. 2011a). The application of this predictive model 111 has been expanded to a rough wall consisting of sand-roughness (Squire et al. 2016) and 112 has recently been improved using Spectral Linear Stochastic Estimation (SLSE) (Baars 113 et al. 2016a). Compared to the smooth-wall boundary layer, the linear interaction or 114 superposition mechanism in the rough wall was found to be weaker while the amplitude 115 modulation was found to be stronger. This suggests that roughness elements generate 116 small scales that contribute significantly to the amplitude modulation (Squire et al. 2016) 117 agreeing with the results of Anderson (2016) and Talluru et al. (2014). 118

In the context of atmospheric flows developing over the urban canopies, the effect of 119 the roughness configuration used to generate a rough-wall boundary layer on the mean 120 flow characteristics and turbulence statistics has been studied extensively (Macdonald 121 et al. 1998; Cheng and Castro 2002; Takimoto et al. 2013; Blackman et al. 2015). Other 122 work has used two-point statistics and correlations to investigate the characteristics of 123 turbulent events such as sweeps and ejections that occur within the shear layer (Takimoto 124 et al. 2013). Recently, Perret et al. (2019) studied the influence of canopy flow regime and 125 Reynolds number on the characteristics of the scale-decomposed velocity fluctuations us-126 ing staggered cube arrays with $\lambda_p = 6.25\%$, 25% and 44.4%. The roughness configurations 127 were classified using the flow regimes identified by Grimmond and Oke (1999) as isolated 128 wake flow (6.25%), wake interference flow (25%) and skimming flow (44.4%). Through 129 spectral analysis and scale-decomposition dynamical similarities were found between the 130 canopy configurations. The Reynolds number was shown to have a negligible effect on 131 the characteristics of the large-scale fluctuations. However, the skimming flow regime 132 was shown to result in near-canopy large scales that contributed more to the variance 133 suggesting that a stronger correlation exists between the inertial layer and the roughness 134 sublayer as the canopy flow becomes less important. The above classification has recently 135 been investigated by Basley et al. (2019) who performed a PIV-based investigation of 136 the same three canopy configurations as Perret et al. (2019). Using data acquired in two 137 horizontal planes, they focused on the characteristics of the coherent structures existing 138 in the roughness sublayer and the logarithmic region. They evidenced that, closer to the 139 canopy, the features of those participating to wall-normal exchange of momentum were 140 dependent on the roughness array configuration. They appeared to be more or less free 141 to develop for the sparsest configurations while constrained in the densest case. It was 142

Karin Blackman, Laurent Perret, Romain Mathis

shown that this apparent confinement of the flow is not gradual with λ_p . Their results indeed suggest that there exists a threshold in λ_p above which the canopy-generated shear layers cannot develop freely (*i.e.* in the skimming flow regime).

The present work focuses on the interaction between the most energetic scales pop-146 ulating the outer layer and those from the roughness sublayer, just above the top of 147 the canopy. A predictive model similar to that developed by Mathis et al. (2011a) for 148 smooth-wall flows is employed to enable the quantification of both the superimposition 149 and the modulation mechanisms when the wall geometry is strongly modified. Although 150 this type of model has been applied successfully in boundary layers over smooth walls and 151 homogeneous rough walls, it has not yet been applied to an urban-type rough-wall bound-152 ary layer. Furthermore, previous work has shown a non-negligible influence of the canopy 153 configuration on the non-linear interactions (Blackman et al. 2017) and the characteris-154 tics of the near-canopy large scales (Perret et al. 2019). Here, three rough-wall boundary 155 layers developing over arrays of cubical roughness elements with $\lambda_p = 6.25\%$, 25% and 156 44.4% will be used to investigate (i) through scale decomposition of the streamwise ve-157 locity component the influence of the canopy flow regime on the interaction between the 158 most energetic scales existing in the outer layer and near the canopy, (ii) the impact of 159 varying both the Reynolds number and the canopy configuration on the predictive model 160 characteristics and (*iii*) whether the predictive model in its current form can be used in 161 an urban-type boundary layer. 162

The following sections outline the methodologies used in the present work including the predictive model (§2) and experimental details (§3). The results and discussion, including the influence of both the plan area packing density and the Reynolds number on the characteristics of the model coefficients and universal signal, which is the signal that exists in the absence of large-scale influence, are presented in §4. A validation of the predictive model is also presented using combinations of data from the six configurations. The last section (§5) is devoted to the conclusions.

170 2. The Predictive Model

The predictive model, developed by Mathis et al. (2011a) and shown in Eq 2.1, has 171 the ability to predict the statistics of the fluctuating streamwise velocity component 172 in the inner region from an outer region input. Here, u_p^+ is the predicted statistically 173 representative streamwise fluctuating velocity signal and u_{oL}^+ is the filtered outer-layer 174 large-scale streamwise fluctuating velocity signal and the only input into the model. The 175 signal u^* is the universal time series that corresponds to a small-scale signal that would 176 exist if there were no large-scale influence. The superscript + denotes normalizations of 177 the velocity fluctuations using the friction velocity u_{τ} , the distance using ν/u_{τ} , and the 178 time using ν/u_{τ}^2 . The universal signal, u^* , and coefficients β , α and θ_L are determined 179 using a calibration method involving two-point measurements of the streamwise velocity 180 fluctuations. The predicted signal, u_p^+ , the large-scale outer-layer signal, u_{oL}^+ , and the 181 universal signal, u^* , are all time series as a function of z^+ while coefficients β , α and θ_L 182 are all functions of z^+ 183

$$u_p^+(z^+) = u^*(1 + \beta u_{oL}^+(z_o^+, \theta_L)) + \alpha u_{oL}^+(z_o^+, \theta_L).$$
(2.1)

¹⁸⁴ The model consists of two parts. The first term of the right-hand side of Eq. 2.1 describes ¹⁸⁵ the amplitude modulation by the large-scale outer layer structures on the small scales ¹⁸⁶ close to the roughness, while the second term models the superposition of these large-scale ¹⁸⁷ structures. To account for the inclination angle of the large-scale structures (θ_L) a time ¹⁸⁸ lag, which corresponds to the shift in the maximum correlation between the outer- and

4

inner-layer large-scale signals, is used. For further information regarding this model the
reader is referred to the work of Mathis et al. (2009) and Mathis et al. (2011a). Recently,
an alternative approach to this model has been proposed by Baars et al. (2016a) who
rewrite the model as

$$u_p^+ = u^* (1 + \Gamma u_L^+) + u_L^+, \tag{2.2}$$

where the coefficient $\Gamma = \beta/\alpha$ and $u_L^+ = \alpha u_{oL}^+(z_o^+, \theta_L)$ represents the superposition effect of the outer large-scales felt at a wall-normal location z^+ within the near-canopy. Baars et al. (2016a) propose a refined procedure for obtaining this superposition component, u_L^+ , based on a SLSE, which is applied here. A brief explanation of the method is presented below and the reader is referred to Baars et al. (2016a) and Perret et al. (2019) for further information.

The present two-point measurements are first used to determine the linear coherent spectrum (LCS) between an outer layer signal and an inner layer signal (Eq 2.3), which represents the maximum correlation coefficient for each Fourier scale.

$$\gamma^{2}(f^{+}) = \frac{\left\| \langle U_{o}(f^{+}) \overline{\overline{U(f^{+})}} \right\|^{2}}{\langle \| U_{o}(f^{+}) \|^{2} \rangle \langle \| U(f^{+}) \|^{2} \rangle}.$$
(2.3)

²⁰² $U(f^+)$ is the Fourier transform of u at frequency f^+ , $U_o(f^+)$ is the Fourier transform of ²⁰³ the outer layer signal u_o , $\| \|$ denotes the modulus, $\langle \rangle$ denotes ensemble averaging and ²⁰⁴ $\overline{()}$ denotes the complex conjugate. Thus, the LCS represents the correlation between ²⁰⁵ streamwise velocity components at two wall-normal locations for a particular frequency. ²⁰⁶ The spectral coherence obtained for each of the six configurations studied here are shown ²⁰⁷ in Fig. 9 of Perret et al. (2019).

As in Baars et al. (2016a) the existence of a non-negligible coherence between velocities at two different wall-normal locations at certain frequencies allows for the scale decomposition of the velocity signal into u_L^+ which is the portion of the signal correlated with the outer-layer signal (large scales) and u_S^+ which is the portion uncorrelated with the outer-layer signal (small scales). A spectral linear stochastic estimation based on the cross-spectrum between the outer-layer signal, u_o^+ , and u^+ is used to derive a transfer function that is then used to extract u_L^+ from u_o^+ (Baars et al. 2016a):

$$U_L(f^+) = H_L(f^+)U_o(f^+)$$
(2.4)

where H_L is the transfer kernel which accounts for the correlation between u^+ and u_o^+ at each frequency. This transfer function kernel is computed by using the synchronized inner-layer and outer-layer data and Eq 2.5.

$$H_L(f^+) = \frac{\langle U(f^+)\overline{U_o(f^+)}\rangle}{\langle U_o(f^+)\overline{U_o(f^+)}\rangle}$$
(2.5)

The transfer kernel is therefore the ratio between the cross-spectrum of u^+ and u_o^+ and the auto-spectrum of u_o^+ . For further details see Perret et al. (2019). Beyond a certain frequency, f_{th}^+ , coherence will no longer exist between the two signals. However, due to the presence of noise a non-physical but non-negligible value of $||H_L(f^+)||$ at frequencies greater than f_{th}^+ can exist. To avoid errors in the estimated signal, u_L^+ , from these nonphysical values the transfer function is set to zero at frequencies above f_{th}^+ . As in Baars et al. (2016a) the frequency threshold f_{th}^+ is determined as the frequency at which the coherence $\gamma^2(f^+)$ falls below 0.05. The transfer kernel is also smoothed to avoid further errors from noise. The transfer kernel is then applied to u_o^+ in the spectral domain using Eq 2.4. The inverse Fourier transform of the $U_L(f^+)$ signal then gives $u_L^+(t^+)$.

Applying the SLSE method described above to each of the wall-normal locations (z), the new model becomes

$$u_p^+(z^+,t^+) = u^*(z^+,t^+) \left(1 + \Gamma(z^+)u_L^+(z^+,t^+-\tau_a)\right) + u_L^+(z^+,t^+),$$
(2.6)

where $u_L^+(z^+, t^+)$ is obtained using

$$u_L^+(z^+, t^+) = \mathcal{F}^{-1} \left[H_L(z^+, f^+) \mathcal{F}(u_o^+(z_o^+, t^+)) \right], \qquad (2.7)$$

where \mathcal{F} and \mathcal{F}^{-1} denote the direct and inverse Fourier transform operators, respectively. 231 The model input is a measurement of the streamwise velocity fluctuations from the outer 232 layer, $u_o^+(z_o^+, t^+)$, and a kernel $H_L(z^+, f^+)$. Once u_L^+ has been determined the model 233 shown in Eq 2.6 is used to obtain the predicted signal. For this, a universal signal, u^* , 234 and a coefficient, Γ , both location-dependent, are required. A phase-shift between the 235 local large scales $u_L^+(z^+, t^+)$ and the large-scale envelope of the amplitude modulated small scales $((u_S^+(z^+, t^+))^2)$ in the present case) has been evidenced both in smooth-236 237 (Guala et al. 2011; Baars et al. 2015) and rough-wall boundary layers (Basley et al. 2018; 238 Pathikonda and Christensen 2017). To account for that effect, a time shift τ_a is introduced 239 to the new model. Its inclusion results in a refined estimation of u^* and therefore a refined 240 predicted signal, u_p^+ (Baars et al. 2016a). The model parameter $\alpha(z^+)$ is chosen to be 241 equal to the maximum of from the temporal cross-correlation between the outer-layer 242 signal, u_{a}^{+} , and the large-scale signal produced from the SLSE method, $u_{L}^{+}(z^{+})$ (Mathis 243 et al. 2011a). The model calibration is conducted using the synchronized two-point hot-244 wire measurements described in §3 at each wall-normal location of measurement. To 245 derive u^* and Γ the small-scale signal of the inner layer is obtained using 246

$$u_S^+(z^+,t^+) = u^+(z^+,t^+) - u_L^+(z^+,t^+).$$
(2.8)

²⁴⁷ This signal represents the fluctuations that are uncorrelated with the large-scale struc-²⁴⁸ tures in the outer layer. For the calibration $u^+(z^+, t^+)$ is equivalent to the predicted ²⁴⁹ signal giving

$$u_S^+(z^+, t^+) = u^*(z^+, t^+) \left(1 + \Gamma(z^+) u_L^+(z^+, t^+ - \tau_a) \right)$$
(2.9)

where u^* and Γ are unknown. As discussed, the universal signal is the signal that exists in 250 the absence of any influence of the large scales in the outer layer. As described by Mathis 251 et al. (2009) and Mathis et al. (2011a) u_S^+ does not include any superposition effect, but 252 does include amplitude modulation effects. Therefore, to find u^* Eq 2.10 is used where 253 Γ is solved for iteratively such that u^* does not show any amplitude modulation. Here, 254 the absence of amplitude modulation is defined using the scale-decomposed skewness as 255 it has been previously shown by Blackman and Perret (2016) that the non-linear term 256 $\overline{u_L^+ u_S^{+2}}$ is directly related to amplitude modulation. Therefore u^* constitutes no amplitude 257 modulation when 258

$$\overline{u_L^+(z^+, t^+ - \tau_a)u^{*2}} = \overline{u_L^+(z^+, t^+ - \tau_a)\left(\frac{u_S^+(z^+, t^+)}{1 + \Gamma(z^+)u_L^+(z^+, t^+ - \tau_a)}\right)^2} = 0.$$
(2.10)

For every wall-normal measurement location, Eq 2.10 is solved iteratively to obtain $\Gamma(z^+)$ where u^* is minimally modulated by $u_L^+(z^+, t^+ - \tau_a)$. The signal u^* is then computed using the coefficient Γ , and β is determined from the relation $\Gamma = \beta/\alpha$. Finally, the predicted signal, u_p^+ , is estimated using Eq 2.6. For further details, the reader is referred to Mathis et al. (2009), Mathis et al. (2011a) and Baars et al. (2016a).

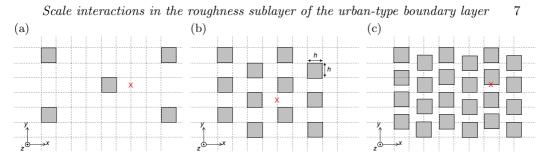


FIGURE 1. Investigated canopy configurations with a) $\lambda_p = 6.25\%$, b) $\lambda_p = 25\%$ and c) $\lambda_p = 44.4\%$ where the red cross (×) is the hot-wire measurement location.

²⁶⁴ 3. Experimental details

The experiments were conducted in a boundary layer wind tunnel with working section 265 dimensions of 2 m (width) \times 2 m (height) \times 24 m (length) and a 5:1 inlet ratio contrac-266 tion in the Laboratoire de recherche en Hydrodynamique, Energétique et Environnement 267 Atmosphérique at Ecole Centrale de Nantes. The empty wind tunnel has a freestream 268 turbulence intensity of 0.5% with spanwise uniformity to within $\pm 5\%$ (Savory et al. 269 2013). To reproduce the lower-part of the atmospheric boundary layer five 800 mm ver-270 tical tapered spires were used immediately downstream of the contraction to initiate the 271 boundary layer development and were followed by a 200 mm high solid fence located 750 272 mm downstream of the spires. These turbulence generators were then followed by a 22 273 m fetch of staggered cube roughness elements with height of h = 50 mm. For further 274 details related to the wind tunnel facility and set-up the reader is referred to Perret et al. 275 (2019). Three different staggered cube configurations were studied consisting of plan area 276 packing densities, λ_p , of 6.25%, 25% or 44.4% (Fig. 1). Finally, the experiments were per-277 formed at two nominal freestream velocities U_e of 5.7 and 8.8 m/s, resulting in a total of 278 six flow configurations. 279

Flow measurements were conducted 19.5 m downstream of the wind tunnel inlet along 280 a wall-normal profile across the boundary layer using hot-wire anemometers (HWA). Two 281 HWA probes were used simultaneously in order to investigate the relationship between 282 the lower part of the boundary layer and the logarithmic region (Fig. 2). The first was a 283 fixed HWA probe at a wall-normal location of z/h = 5 (*i.e.* within the inertial layer) while 284 the second probe was positioned at 13 different wall-normal locations in the lower part 285 of the boundary layer between z/h = 1.25 and z/h = 4. The wall-normal location of the 286 reference probe at z/h = 5 has been chosen based on previous studies (Perret and Rivet 287 2013; Blackman and Perret 2016; Basley et al. 2018), performed in the $\lambda_p = 25\%$ cube 288 array, in which the focus was to analyse scale interactions between the canopy flow and 289 the overlying boundary layer in order to highlight the existence of a non-linear amplitude 290 modulation mechanism as previously evidenced by Mathis et al. (2009) in smooth-wall 291 boundary layers. It has been shown that the amplitude modulation mechanism is effec-292 tively detected in urban surface layer with a reference point located in the range 3h - 5h. 293 This ensures that the reference point is out of the RSL (the targeted flow) and well within 294 the logarithmic layer (in the constant flux region). This mild sensitivity regarding the 295 choice of the reference wall-normal location is in agreement with the findings of Mathia 296 et al. (2009). Accuracy of the single hot-wire measurements in this region of the flow was 297 assessed by Perret and Rivet (2018) using a combination of stereoscopic PIV and the con-298 cept of convective cooling velocities. Measurements of the streamwise velocity component 299 using a single hot wire showed good accuracy with a relative error of the variance always 300 below 5%. This was further confirmed by the comparison between results obtained via 301

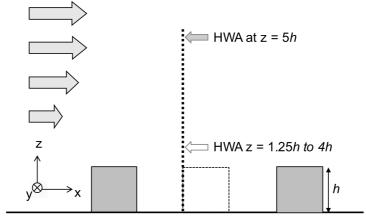


FIGURE 2. HWA measurement set-up showing the two-probe arrangement.

Laser Doppler anemometry (LDA) and HWA performed by Herpin et al. (2018). Two 302 Disa 55M01 electronics associated to Dantec 55P11 5 μ m single HWA probes with a wire 303 length of 1.25 mm were used with overheat ratio set to 1.8. The HWA measurements 304 were conducted at a frequency of 10 kHz for a period of 24 000 δ/U_e . The signals were 305 treated with an 8th order anti-aliasing linear phase elliptic low-pass filter prior to digiti-306 zation. Calibration was performed at the beginning of each measurement set by placing 307 the probes in the free-stream flow. The calibration procedure is based on King's law and 308 accounts for temperature correction using the method proposed by Hultmark and Smits 309 (2010). For further details including the relative error of the mean, variance, 3^{rd} order 310 and 4th order statistics, as well as the statistical error of convergence, refer to Perret 311 et al. (2019). A detailed comparison between the present $\lambda_p = 25\%$ flow configuration 312 and similar configurations from the literature was completed by Perret and Rivet (2018), 313 including a comparison of the standard deviation of the three velocity components and 314 Reynolds shear stress from Reynolds and Castro (2008). They also compared the wall-315 normal distribution of Q1, Q2, Q3 and Q4 events to the DNS of Coceal et al. (2007), 316 confirming that the present flow shows the correct flow structure. Further comparison 317 between the literature and measurements performed via PIV, HWA and LDA can be 318 found in Herpin et al. (2018). 319

320 4. Results

321

4.1. Boundary layer characteristics

Table 1 lists the main characteristics of the investigated boundary layers. The logarithmic-322 law parameter aerodynamic roughness length, z_0 , was determined by fitting the vertical 323 streamwise velocity profile to the logarithmic law (Perret et al. 2019). As described by 324 Perret et al. (2019) the zero-plane displacement height, d, is estimated directly from the 325 calculation of the moment of pressure forces on the roughness elements while the fric-326 tion velocity, u_{τ} , is also estimated from the measured form drag. The independence of 327 u_{τ}/U_e and z_0/h from the Reynolds number Re_{τ} indicates that the three flow configu-328 rations are in the fully rough regime. The boundary layer thickness, δ , shown in Table 329 1 defines the wall-normal location at which the mean velocity is equal to 99% of the 330 free-stream velocity U_e . In the measurement cross-section, for all the configurations, the 331 non-dimensional pressure gradient $K = (\nu / \rho U_e^3) dP/dx$ along the wind tunnel was found 332

Symbols	$\lambda_p(\%)$	$U_e \ (m/s)$	u_{τ}/U_e	δ/h	Re_{τ}	h^+	d/h	z_0/h	$K \times 10^8$	$(h-d)/\delta$	$z_{ m RSL}/h$
0	6.25	5.65	0.070	22.4	29700	1330	0.52	0.08	-2.48	0.021	3.6
•	6.25	8.80	0.072	21.5	45500	2110	0.52	0.09	-1.29	0.022	3.8
\triangle	25	5.77	0.074	22.7	32400	1430	0.59	0.11	-2.89	0.018	3.6
	25	8.93	0.076	22.1	49900	2260	0.59	0.12	-2.28	0.018	4.0
	44.4	5.62	0.063	23.2	27300	1170	0.77	0.04	-2.65	0.010	2.2
	44.4	8.74	0.063	22.1	40700	1840	0.77	0.04	-2.12	0.010	2.4
TABLE	1. Scali	ng parame	ters. Th	ie colo	oured sv	mbols	chart	will h	be used in	all the foll	owing

figures	
ngures.	

to be below -2.9×10^{-8} . The aerodynamic parameters d and z_0 can be used to classify 333 the roughness flow regime with the model derived by Macdonald et al. (1998) or the data 334 compiled by Grimmond and Oke (1999). The three canopies studied here represent the 335 three near-wall flow regimes as defined by Grimmond and Oke (1999) where the λ_p = 336 6.25% represents isolated wake flow, $\lambda_p = 25\%$ represents wake-interference flow and λ_p 337 = 44.4% represents skimming flow (see Fig. 3 of Perret et al. 2019). For further details 338 the reader is referred to Perret et al. (2019). 339

Fig. 3 shows the wall-normal profiles of the main statistical characteristics of the 340 streamwise velocity component including mean velocity, variance, skewness and kurtosis 341 for the six cases shown in Table 1. Scaling using the roughness length and displacement 342 height results in a collapse of the mean streamwise velocity component in regard to both 343 canopy geometry and Reynolds number. The remaining statistics show agreement within 344 the outer laver scaling using the displacement height and boundary laver thickness. How-345 ever, both the variance and skewness are influenced by the canopy geometry within the 346 inner layer close to the roughness. Perret et al. (2019) conducted detailed scaling analy-347 sis for these six cases, but were unable to find a scaling that collapses the variance and 348 skewness close to the wall. One salient feature of the present flow configurations put 349 forward by these authors is the variation of the wall-normal extent of the roughness sub-350 layer as a function of λ_p . While classically defined as the region where the flow statistics 351 are non-homogeneous in the horizontal plane, Squire et al. (2016) recently proposed to 352 define its upper limit z_{RSL} as the lower limit of the inertial region in which the velocity 353 variance follows a logarithmic law. Following this approach and based on the data shown 354 in Fig. 3(b), Perret et al. (2019) found that $z_{\rm RSL}$ varies with the roughness configuration 355 and Reynolds number (Table 1). This suggests that the densest canopy configuration 356 prevents the canopy-induced coherent structures from developing in the wall-normal di-357 rection. This matches well with the well-recognized picture of the skimming flow regime 358 in which a thin shear-layer develops at the canopy top with very limited penetration 359 of the flow within the canopy and is consistent with the recent results of Basley et al. 360 (2019).361

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4.2. Scale Decomposition

In the case of the atmospheric surface layer developing over large roughness elements, the 363 outer and inner peaks in the energy spectrum are rarely separated. The cubical obstacles 364 induce energetic structures with typical frequencies smaller than that of the near-smooth 365 wall turbulence in a range closer to those attributed to the large-scale structures devel-366 oping in the logarithmic and outer region. It should also be pointed out that although 367 the outer peak is not clearly visible this does not mean that large-scale influence does 368 not exist, but rather that scale separation is not clear and significant overlapping ex-369

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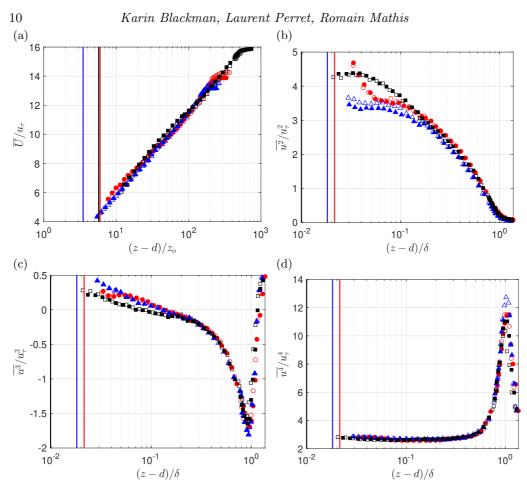


FIGURE 3. Wall-normal profiles of the a) mean b) variance, c) skewness and d) kurtosis of the streamwise velocity component. Vertical solid lines show the wall-normal location of the canopy top z = h for the three roughness configurations (being negligible when normalizing by δ , variation of $(h - d)/\delta$ with Re_{τ} is not shown).

ists between the different coherent structures interacting with each other. This has been 370 shown by Perret et al. (2019) and is the reason why the scale-separation method based 371 on a two-point measurement approach is favoured here (Baars et al. 2016b; Pathikonda 372 and Christensen 2017). Using the method described in §2 the large-scale signal, u_L^+ , is extracted from the raw near-wall velocity signal, u_{NW}^+ , at each of the moving HWA probe 373 374 wall-normal locations in each of the six cases using a transfer function. The modulus and 375 phase of the transfer function for the moving probe location of z/h = 1.25 in each of 376 the six cases are shown in Fig. 4 where it is clear that the modulus and phase of the 377 transfer function depend on the canopy geometry, but not on the Reynolds number. In 378 this section, the focus is on the main statistical characteristics of u_L and u_S and their 379 contribution to the skewness, which is an indicator of the existence of amplitude modu-380 lation (Duvvuri and McKeon 2015). A thorough analysis of the spectral content of the 381 flow and of its large- and small-scale components has been performed by Perret et al. 382 (2019) and Basley et al. (2019) in the same flow configurations as here. These authors 383 demonstrated the co-existence of VLSMs, LSMs and canopy-generated coherent struc-384

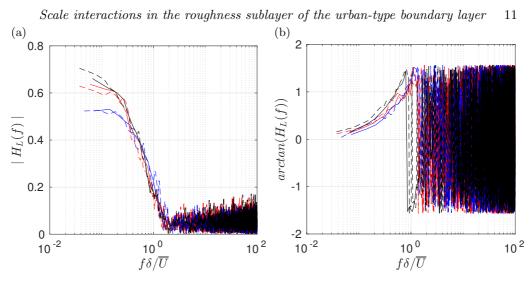


FIGURE 4. a) Modulus and b) phase of the transfer kernel $|H_L|$ at z/h = 1.25 for configurations with $\lambda_p = 6.25\%$, 25% and 44.4% at $Re_{\tau} = 32400$ and 49 900. The colour chart is as per Table 1 for canopy configurations, solid and dashed lines correspond respectively to the low and the high Reynolds numbers.

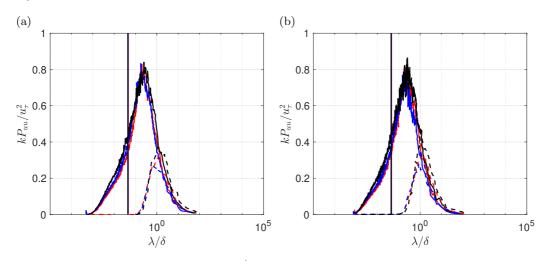


FIGURE 5. Spectra of u^* (solid line) and u_L^+ (dashed line) for configurations with $\lambda_p = 6.25\%$, 25% and 44.4% at a) $Re_{\tau} = 32400$ and b) 49 900 at z/h = 2.1. Vertical solid lines show the streamwise wavelength corresponding to the obstacle height $\lambda = h$.

tures whose characteristics obey different scaling laws. For the sake of conciseness, these results are not recalled here, the reader being referred to these studies.

Once u_L^+ is extracted using triple decomposition[†] the small-scale signal, u_S^+ , can be computed. Finally, u^* is computed using the method described in §2. The spectra of the universal and large-scale signal (Fig. 5) of the six cases show the differences in energy content of the two signals. No significant change occurs in the energy distribution between the different canopies and different Reynolds numbers. Finally, an increase in Reynolds number does not affect the magnitude of energy contained in the universal and large-

[†] Triple decomposition was first introduced by Hussain (1983) to decompose the instantaneous velocity field into mean, large-scale and small-scale components.

Karin Blackman, Laurent Perret, Romain Mathis

scale signals. This last point may be tempered by the narrow range of Reynolds number 393 used here, as it has been shown previously that the large-scale content increases as the 394 Reynolds number increases (see Mathis et al. 2009, 2011a among others). The statistics 395 of the u^* signal including variance, skewness and kurtosis are compared in Fig. 6 with the 396 statistics of the raw near-wall velocity signal u_{NW}^+ , u_L^+ and u_S^+ showing only the $\lambda_p = 25\%$ 397 case as an example. In all six cases (not shown here) u_S^+ captures the majority of the 398 variance in the inner layer while the large-scale contribution becomes important only in 399 the outer layer. The skewness is shown to be almost completely captured by u_S^+ with the 400 contribution from u_L^+ close to zero. The kurtosis of the raw signal is shown to be a result of both u_L^+ and u_S^+ with the contribution of u_S^+ increasing with wall-normal distance in 401 402 the outer layer. Mathis et al. (2011a) noted that the universal signal is the signal that 403 exists in the absence of the influence of large-scale structures while u_S^+ is the signal that 404 exists in the absence of any superposition. Therefore a comparison between the u_S^+ and 405 u^* signals provides insight into the influence of the amplitude modulation on the u_S^+ 406 structures. The presence of amplitude modulation causes no influence in the variance or 407 kurtosis as u_{S}^{+} and u^{*} have similar profiles. In the absence of amplitude modulation the 408 magnitude of skewness of u^* is significantly lower throughout the boundary layer. These 409 trends are true for each of the six configurations except in the case of the skewness of u^* . 410 The wall-normal location at which the profile of the skewness of u^* crosses the profile 411 of the skewness of u_L^+ changes depending on the roughness configuration. In roughness 412 configurations with $\lambda_p = 6.25\%$ or 25% the u^* profile crosses the u_L^+ profile at a wall-413 normal distance of approximately $(z - d)/\delta = 0.09$ while in roughness configurations 414 with $\lambda_p = 44.4\%$ this crossing occurs at $(z - d)/\delta = 0.05$. As u^* is the signal that 415 exists in the absence of influence of the large scales it should correspond to a signal 416 from a low Reynolds number flow where large-scale influence is weak. The decrease of 417 contribution of u^* to the skewness in the configuration with $\lambda_p = 44.4\%$ is a result of 418 increased large-scale activity. No significant differences are found between cases when 419 varying Reynolds number as both Reynolds numbers are sufficient to generate significant 420 large-scale activity and differ by less than a factor of two. 421

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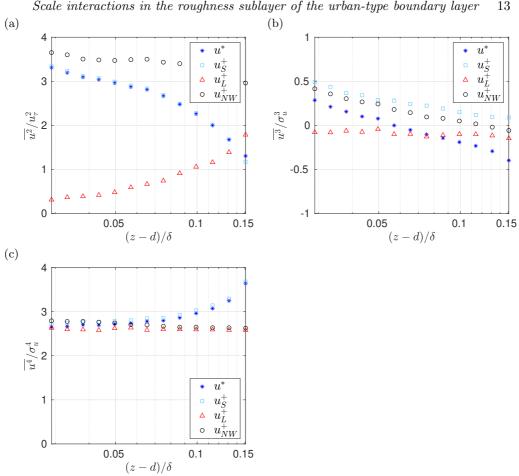
4.3. Influence of canopy geometry and Reynolds number

A23 Skewness decomposition as shown in Eq. 4.1 has been used to investigate the non-linear
interactions between large- and small-scale structures in turbulent flows (Blackman and
Perret 2016).

$$\overline{u^{+3}} = \overline{u_S^{+3}} + \overline{u_L^{+3}} + 3\overline{u_L^{+}u_S^{+2}} + 3\overline{u_L^{+2}u_S^{+}}$$
(4.1)

Here it is used to determine the influence of the canopy geometry and Reynolds num-426 ber on these non-linear interactions. Figure 7 shows the small-scale skewness, large-scale 427 skewness and two scale-interaction terms. The influence of the canopy geometry is par-428 ticularly apparent in the contribution of the small scales close to the canopy where there 429 is a clear separation between the cases (Fig. 7a). This separation is a result of the distinct 430 canopy flow regimes in each of the cases. As mentioned, within the skimming flow regime 431 $(\lambda_p = 44.4\%)$ there is a thinner shear layer (or roughness sublayer) whereas in the iso-432 lated wake ($\lambda_p = 6.25\%$) and wake-interference ($\lambda_p = 25\%$) flow regimes the shear layer 433 wall-normal extent is larger increasing the importance of the small scales. Away from 434 the canopy, in the outer-layer, the influence of the canopy geometry or flow regime is not 435 significant. Moreover, throughout the boundary layer the canopy geometry does not significantly influence the large-scale contribution or the contribution of the non-linear term 437 $u_L^{+2}u_S^+$, which represents the influence of the small scales onto the large scales. However,

12



Scale interactions in the roughness sublayer of the urban-type boundary layer

FIGURE 6. Comparison of u^* , u_L^+ , u_S^+ and u_{NW}^+ statistics a) variance, b) skewness and c) kurtosis for configuration with $\lambda_p = 25\%$ at $Re_\tau = 32400$.

an increase in Reynolds number increases the contribution of this non-linear term within 439 the outer-layer (Fig. 7d). Finally, the non-linear term $\overline{u_L^+ u_S^{+2}}$ has been shown to represent the amplitude modulation (Mathis et al. 2011c; Duvvuri and McKeon 2015). Here, it is 440 441 clear that although the canopies with $\lambda_p = 6.25\%$ and 25% display similar amplitude 442 modulation, the amplitude modulation of the canopy with $\lambda_p = 44.4\%$ is significantly 443 modified at both Reynolds numbers (Fig. 7c). Throughout the boundary layer, except 444 close to the canopy, the amplitude modulation is weaker in the $\lambda_p = 44.4\%$ canopy. As 445 mentioned in section 4.1, this flow configuration has the finest roughness sublayer. This 446 is confirmed if one considers the wall-normal location of the zero-crossing of the skew-447 ness of the streamwise velocity component as the upper limit of the roughness sublayer 448 (Fig. 7a). It is also where the small-scale component u_S is the least energetic relative to 449 the large scales (Perret et al. 2019). In this flow configuration, the small scales are less 450 energetic and more confined to near the canopy top, the amplitude modulation imprint 451 is therefore weaker than the two other cases. 452

The coefficients α and β of the predictive model computed for each of the cases listed 453 in Table 1 using the method in §2 are shown in Fig. 8 along with the coefficient Γ . The 454 roughness configuration affects the superposition coefficient, α , close to the roughness 455

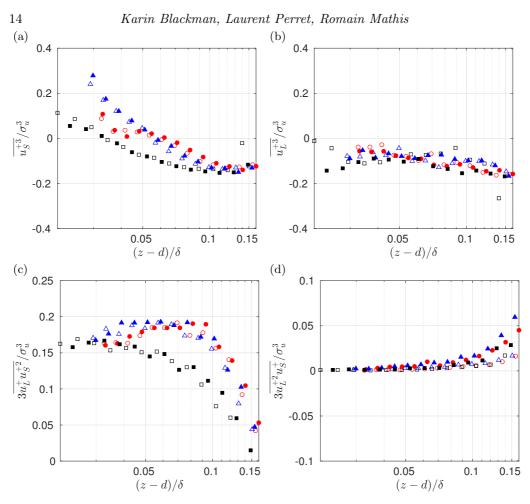


FIGURE 7. Triple decomposition of the skewness of the streamwise velocity component including a) $\overline{u_S^{+3}}$, b) $\overline{u_L^{+3}}$, c) $3\overline{u_L^{+}u_S^{+2}}$ and d) $3\overline{u_L^{+2}u_S^{+}}$.

in the inner layer where differences in the flow regimes are important. However, in the 456 outer layer the superposition is consistent in all roughness configurations. In the outer 457 layer the influence of the roughness flow regime disappears and the large-scale structures 458 become similar thereby resulting in similar superposition. The amplitude modulation 459 coefficient, β , depends on roughness configuration in the inner layer, but in the case of 460 the roughness configuration with $\lambda_p = 44.4\%$ the amplitude modulation is decreased both 461 in the inner layer and the outer layer. This is consistent with the non-linear term $u_L^+ u_S^{+2}$ 462 which shows lower magnitudes of amplitude modulation in the $\lambda_p = 44.4\%$ configuration. 463 As disussed, the characteristics of the shear layer in the skimming flow regime change 464 the characteristics of the small-scale structures and their interactions with the large-scale 465 structures in the outer layer above. The dependence of the superposition and amplitude 466 modulation on the roughness configuration close to the roughness is a result of changes 467 to the dynamics of the shear layers that develop at the top of the roughness elements 468 in the different flow regimes. Within the skimming flow regime the shear layer does not 469 penetrate the roughness elements resulting in a thin, but strong shear layer, whereas 470 the spacing between roughness elements in the isolated and wake-interference regimes 471 result in a shear layer that penetrates the canopy layer increasing the vertical transfer 472

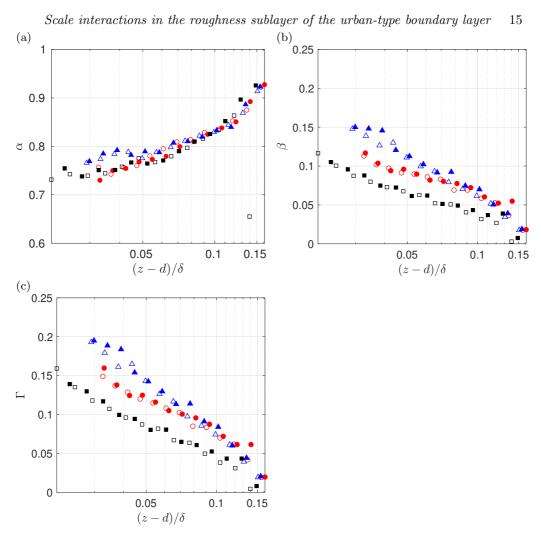


FIGURE 8. Predictive model coefficients a) α , b) β and c) Γ for configurations with $\lambda_p = 6.25\%$, 25% and 44.4% at $Re_{\tau} = 32400$ and 49 900.

of momentum of small-scale structures in this region (Basley et al. 2019). The shear 473 layer in the wake-interference flow regime also experiences a strong flapping phenomenon 474 that promotes the transfer of momentum between the canopy layer (small scales) and 475 outer layer (large scales). The results show that an increase in Reynolds number does not 476 increase the superposition or the amplitude modulation in contradiction to Mathis et al. 477 (2011a) who found that increased Reynolds number increases the large-scale activity in 478 the outer layer thereby increasing the amplitude modulation. These results should be 479 tempered by the fact that the Reynolds numbers used here are not sufficiently separated 480 to significantly affect the large scales and therefore the scale interactions. 481

The variance, skewness and kurtosis of the universal signal, u^* , and u_L^+ in each of the six cases are presented in Fig. 9. The influence of the roughness configuration can be seen in the profiles of variance and skewness in the inner-layer close to the roughness, whereas this influence becomes negligible in the profile of kurtosis. The changes in variance and skewness are a result of changes to the small-scale structures produced by the roughness. Small scales in the wake-interference flow regime have larger magnitudes of skewness

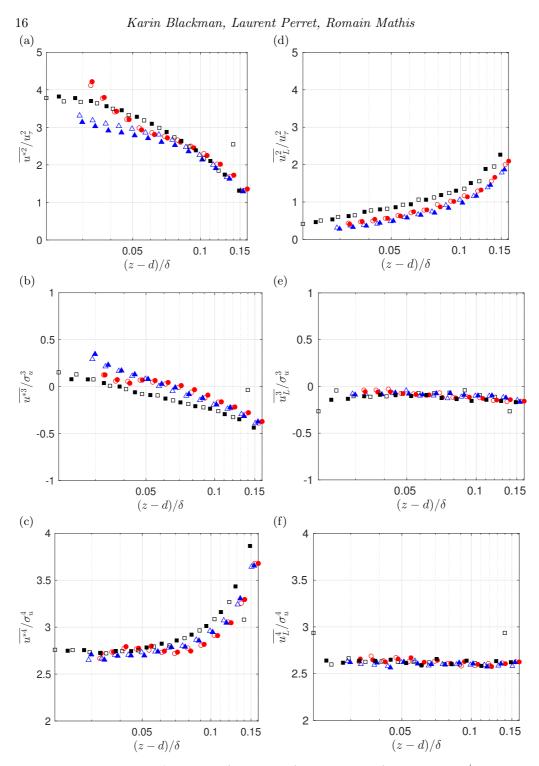


FIGURE 9. Comparison of u^* statistics a) variance, b) skewness and c) kurtosis and u_L^+ statistics d) variance, e) skewness and f) kurtosis for configurations with $\lambda_p = 6.25\%$, 25% and 44.4% at $Re_{\tau} = 32400$ and 49 900.

	Test 1		Test 2	2	Test 3		
	λ_p (%)	Re_{τ}	$\lambda_p \ (\%)$	Re_{τ}	$\lambda_p \ (\%)$	Re_{τ}	
Calibration	25	32400	25	32400	44.4	32400	
Large-scale	25	49900	6.25 or 44.4	32400	25	49900	
Prediction	25	49900	25	32400	44.4	49900	

TABLE 2. Characteristics of the input (calibration parameters and large-scale signal) and output of the predictive model used for testing and validating the prediction capabilities of the model.

and smaller magnitudes of turbulence intensity compared to the skimming flow regime. 488 Although there is an increase in magnitude of variance of the large-scale structures in the 489 44.4% configuration these changes are not limited to the region close to the roughness 490 as in the u^* profile (Fig. 9d). Excluding this slight increase in the variance the similarity 491 of the other u_L^+ profiles suggests that the very-large-scale structures in each of the cases 492 have similar characteristics. Using the outer-layer scaling a change in Reynolds number 493 does not affect the statistics of the universal or large-scale signals. These results have 494 shown that the model coefficients and universal signal are significantly influenced by the 495 canopy geometry or canopy flow regime while the large-scale structures have been shown 496 to be similar in each of the cases. Therefore, the universal signal is not universal for all 497 rough-wall boundary layers and the predictive model must be calibrated for each of the 498 roughness flow regimes. 499

4.4. Prediction and Validation

500

Model coefficients provided by the calibration allow for the prediction of a statistically 501 representative signal, u_p^+ , that hypothetically can be reconstructed at any Reynolds num-502 ber, where the only required input is the large-scale reference signal, u_L^+ . In this section, 503 a series of tests are performed in order to assess whether the above assumption, which 504 works well in smooth-wall boundary layer, still holds in an atmospheric boundary layer 505 over an urban canopy. To do so, a series of tests is performed to validate and assess 506 the capabilities of the model, in which canopy configuration and Reynolds numbers are 507 mixed, as seen in Table 2. 508

The capabilities of the predictive model, which has been calibrated for $\lambda_p = 25\%$ 500 and $Re_{\tau} = 32400$, is first tested by predicting the near-canopy signal for the same 510 plan density at the higher Reynolds number $Re_{\tau} = 49\,900$ (Test 1). To do this a large-511 scale reference signal measured at $Re_{\tau} = 49\,900$ is used to run the predictive model 512 where the universal signal and model coefficients were determined from a calibration at 513 $Re_{\tau} = 32\,400$. Additionally, the large-scale reference signal must be interpolated onto 514 the non-dimensional time-scale t^+ of the universal signal so that the time sampling of 515 both signals is consistent. In addition, the two signals must have the same length, by 516 clipping the longest of the two. Figure 10 shows the characteristics of the predicted 517 signal (blue stars) compared with the characteristics of the measured near-canopy signal 518 (black circles) up to the 4^{th} order. Although there is some slight discrepancy between 519 the prediction and the near-canopy signal, it is clear that the predictive model calibrated 520 at a lower Reynolds number is able to reproduce the characteristics of the near-canopy 521 signal at a higher Reynolds number. Finally, the spectra of the predicted signal are 522 similar to the spectra of the measured signal as shown in Fig. 11. There is a slight shift 523 in the wavelength of the spectra of the predicted signal that becomes more significant 524 closer to the roughness. This might be due to the application of Taylor's hypothesis 525 which has questionable suitability close to the roughness. However, the similarity of the 526

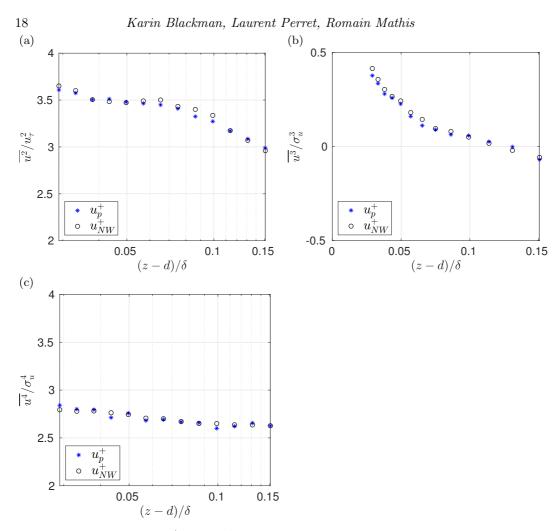
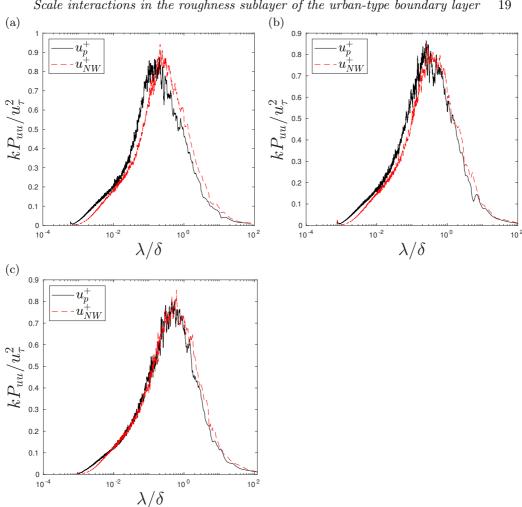


FIGURE 10. Comparison of u_{NW}^+ and u_p^+ statistics a) variance, b) skewness and c) kurtosis for $\lambda_p = 25\%$ and $Re_{\tau} = 49\ 900$ where u_p^+ is determined using model coefficients calibrated at $Re_{\tau} = 32\ 400$ and u_L^+ at $Re_{\tau} = 49\ 900$ (Test 1).

spectra further validates the model and suggests that the model can be calibrated at any
 arbitrary Reynolds number.

Another crucial question in making a predictive model for urban canopy flow, is to 529 what extent the calibration is dependent on the plan area packing density at which the 530 calibration is performed. Indeed, the previous section clearly evidenced that the universal 531 signal and model coefficients are canopy dependent. In an attempt to shed light on this, 532 the near-canopy signal is predicted for the $\lambda_p = 25\%$ at $Re_\tau = 32\,400$ configuration using 533 large-scale reference signals from the datasets of the $\lambda_p = 6.25\%$ and 44.4% configurations 534 at the same Reynolds number (Test 2). To perform these predictions the calibrated model 535 for the $\lambda_p = 25\%$ configuration is used along with a large-scale reference signal from a 536 configuration with a different λ_p . As above, the large-scale reference signal from either 537 the $\lambda_p = 6.25\%$ or 44.4% configuration is interpolated onto the non-dimensional time-538 scale of the universal signal calibrated for the $\lambda_p = 25\%$ configuration. Fig. 12 shows 539 the characteristics of the predicted signal using a large-scale reference from the λ_p = 540 6.25% configuration (blue triangles), $\lambda_p = 44.4\%$ configuration (red squares) and the 541



Scale interactions in the roughness sublayer of the urban-type boundary layer 19

FIGURE 11. Spectra of u_{NW}^+ and u_p^+ at a) z/h = 1.25, b) z/h = 2.1 and c) z/h = 3.2 for $\lambda_p =$ 25% and $Re_{\tau} = 49\ 900$ where u_p^+ is determined using model coefficients calibrated at $Re_{\tau} = 32$ 400 and u_L^+ at $Re_{\tau} = 49\ 900$ (Test 1).

measured near-canopy signal of the $\lambda_p = 25\%$ configuration (black circles). The spectra 542 of the predicted signals and measured near-canopy signal are shown at several wall-543 normal locations in Fig. 13. There is excellent agreement between the predicted signals 544 and the near-canopy signal for the statistics up to the 4^{th} order and the spectra in both 545 prediction cases. 546

To determine the error associated with these predictions the near-canopy signal was 547 predicted within each canopy using a large-scale reference signal from each of the other 548 canopy configurations for the lowest wall-normal location of z/h = 1.25 as a test. The 549 error for the statistics up to the 4^{th} order was computed for each prediction using Eq. 4.2 550 where ϕ_m and ϕ_p are any statistics of the original measured and predicted signals, re-551 spectively. 552

$$error = (\phi_m - \phi_p)/\phi_m \tag{4.2}$$

Fig. 14 shows the error averaged over the two predictions for each canopy configura-553

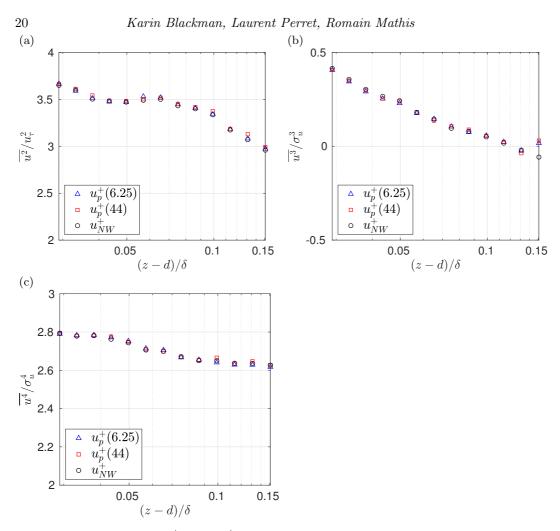
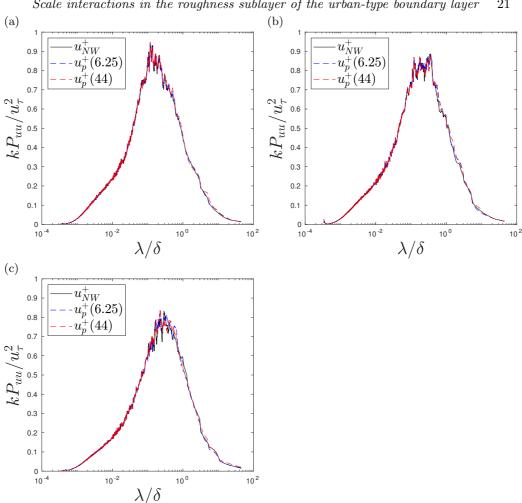


FIGURE 12. Comparison of u_{NW}^+ and u_p^+ statistics a) variance, b) skewness and c) kurtosis for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and u_L^+ from $\lambda_p = 6.25\%$ or 44.4% (Test 2).

tion. The error is less than 3% for all statistics and in all canopies with the largest error of 3% for the kurtosis of the $\lambda_p = 25\%$ configuration. This confirms that a calibrated predictive model can be used to predict the near-canopy signal using a large-scale reference measured in any other canopy configuration.

The final validation of the model combines both the Reynolds number and λ_p validation 558 by predicting a near-canopy signal within the $\lambda_p=44.4\%$ configuration at $Re_\tau=49~900$ 559 using the calibrated model at $Re_{\tau} = 32400$ and a large-scale reference signal from the 560 $\lambda_p = 25\%$ configuration at $Re_\tau = 49~900$ (Test 3). As in the previous validation the 561 model is able to accurately reproduce the spectra of the near-canopy signal as well as 562 the statistics up to the 4^{th} order (Fig. 15). The model is able to accurately reproduce 563 these statistics because, as has been shown here, the characteristics of the large scales 564 in each of the canopies are similar. However, the differences in the characteristics of 565 the universal signal and the predictive model coefficients prevent the application of a 566 calibrated model at one λ_p to a prediction at another λ_p . The model must be calibrated 567 using measurements from a canopy with the same configuration as the targeted one. 568



Scale interactions in the roughness sublayer of the urban-type boundary layer 21

FIGURE 13. Spectra of u_{NW}^+ and u_p^+ at a) z/h = 1.25, b) z/h = 2.1 and c) z/h = 3.2 for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 25\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 325\%$ and $Re_{\tau} = 32400$ where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 325\%$ and $Re_{\tau} = 32400$ where u_p^+ and $u_$ 25% and u_L^+ from $\lambda_p = 6.25\%$ or 44.4% (Test 2).

In the smooth wall special attention has been paid to conserving the phase between 569 the universal signal and large-scale signal used to run the predictive model (Mathis et al. 570 2011a). In these cases the large-scale reference signal used to run the predictive model 571 was adjusted to retain the Fourier phase information of the large-scale signal used to 572 build the universal signal. The phase information of the original large-scale signal is 573 extracted using a Fourier transform and applied to the new large-scale reference signal. 574 This process essentially re-synchronizes the new large-scale reference with the universal 575 signal, u^* (Mathis et al. 2011c). Here, this process was applied before performing the 576 predictions detailed above. To determine influence of the phase shift on a prediction 577 a test is performed using the large-scale reference signal used to build the predictive 578 model. This signal is shifted out of phase with the universal signal and a prediction of 579 the statistics made at each time-shift (Fig 16). As the phase shift increases the estimation 580 of the variance, skewness and kurtosis worsen until they reach a plateau. The effect of the 581 phase shift increases with increasing order of the statistic with the kurtosis showing the 582

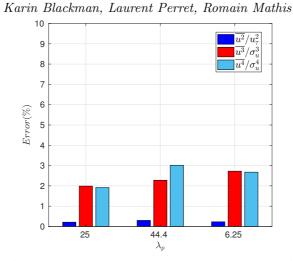


FIGURE 14. Error of u_p^+ statistics variance, skewness and kurtosis where u_p^+ is determined using model coefficients calibrated at a certain λ_p and u_L^+ at a different λ_p both at $Re_{\tau} = 32$ 400.

- ⁵⁸³ largest discrepancy. This suggests that conserving the phase information of the large-scale
- $_{\tt 584}$ $\,$ signal used to calibrate the model is important to the prediction.

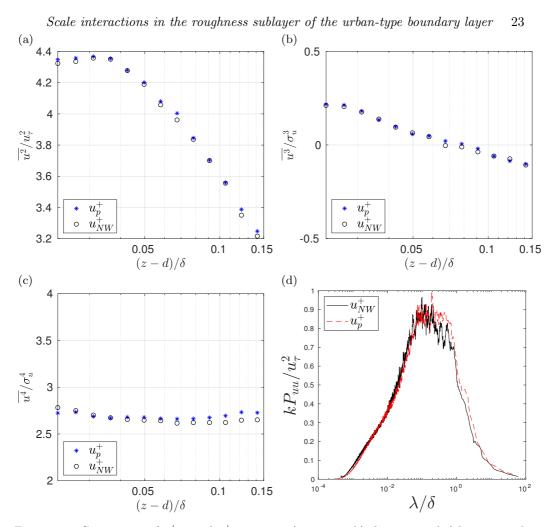


FIGURE 15. Comparison of u_{NW}^+ and u_p^+ statistics a) variance, b) skewness and c) kurtosis and d) spectra at z/h = 1.5 for $\lambda_p = 44.4\%$ and $Re_{\tau} = 49$ 900 where u_p^+ is determined using model coefficients calibrated for $\lambda_p = 44.4\%$ and $Re_{\tau} = 32$ 400 and u_L^+ from $\lambda_p = 25\%$ and $Re_{\tau} = 49$ 900 (Test 3).

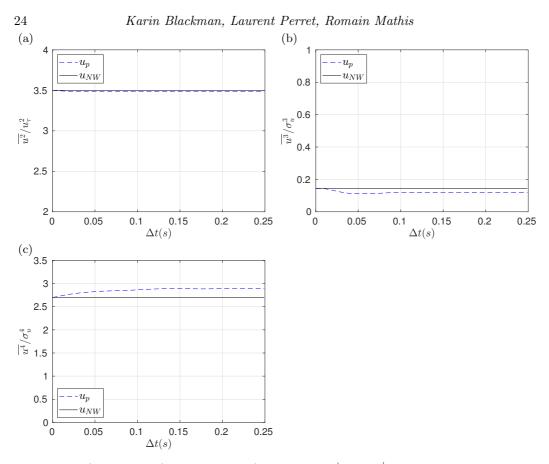


FIGURE 16. a) Variance, b) skewness and c) kurtosis of u_p^+ and u_{NW}^+ for configuration with $\lambda_p = 25\%$ at $Re_\tau = 32400$ using phase shifted large-scale reference signal at z/h = 2.1 $((z-d)/\delta = 0.066)$.

Scale interactions in the roughness sublayer of the urban-type boundary layer 25

585 5. Conclusion

A predictive model of the same form as that originally introduced by Mathis et al. 586 (2011a) for the smooth-wall boundary layer has been derived to investigate the scale-587 interaction mechanisms known to exist in the near-canopy region of boundary-layer flows 588 developing over large roughness elements. This modeling approach allows for the iden-589 tification and quantification of both the superimposition of the most energetic (large) 590 scales from the outer layer onto the near-canopy (smaller-scale) turbulence and the am-591 plitude modulation of the near-canopy flow by the outer-layer flow. It also enables the 592 extraction of the portion of the near-canopy velocity that is free from any influence of 593 the large scales. Three roughness arrays consisting of cubical roughness elements with 594 plan area packing densities of 6.25%, 25% and 44.4% (corresponding to the three flow 595 regimes identified in such flows, Grimmond and Oke 1999; Perret et al. 2019) were stud-596 ied at two freestream velocities and used to determine the influence of both the canopy 597 geometry and Reynolds number on the interaction between the most energetic scales from the outer layer and those in the roughness sublayer. Through analysis of the pre-599 dictive model coefficients it was shown that the canopy geometry has a non-negligible 600 influence on the scale interactions. The superposition, represented by the coefficient α , 601 was modified in the inner layer close to the canopy top as a result of a change in the local 602 flow regime. Furthermore, the skimming flow regime, $\lambda_p = 44.4\%$, showed lower levels of 603 amplitude modulation (given by the model parameter β), both in the inner and outer 604 layers when compared to configurations of isolated and wake interference flow regime. 605 These patterns were also visible in the statistics of the universal signal, u^* , where the variance was modified close to the roughness as a result of local canopy geometry. For 607 the densest canopy, both the variance and skewness had lower magnitudes throughout 608 the roughness sublayer. Investigation of the model coefficients α and β and statistics 609 of u^* demonstrated that the Reynolds number does not significantly influence the su-610 perposition or amplitude modulation contradicting previous results in the smooth-wall 611 boundary layer (Mathis et al. 2011a). However, this is likely a result of the limited range 612 of Reynolds numbers used here and therefore requires further investigation. 613

The capacity of the derived models to serve as predictive tools to model near-canopy 614 turbulence and to generate synthetic signals which have the same statistical character-615 istics of the targeted flows has also been investigated. Model validation was performed 616 in three steps. The first, consisted of a prediction of the streamwise velocity component 617 within the roughness sublayer of the $\lambda_p = 25\%$ configuration at the highest Reynolds 618 number, $Re_{\tau} = 49$ 900, using the model parameters calibrated at $Re_{\tau} = 32$ 400 (Test 619 1). The second validation consisted of a prediction of the streamwise velocity component 620 within the roughness sublayer of the $\lambda_p = 25\%$ configuration using its model parameters 621 combined with a large-scale signal from the $\lambda_p = 6.25\%$ or 44.4% configurations (Test 622 2). Finally, the third validation consisted of a prediction of the streamwise velocity com-623 ponent within the roughness sublayer of the $\lambda_p = 44.4\%$ configuration at the highest 624 Reynolds number, $Re_{\tau} = 49$ 900, using the model parameters calibrated at $Re_{\tau} = 32$ 625 400 and a large-scale signal from the $\lambda_p = 25\%$ configuration (Test 3). Each of the model 626 validations demonstrated the suitability of the predictive model within the urban-type 627 rough-wall boundary layer. The statistics up to the 4^{th} order were accurately reproduced 628 as well as the spectra. Finally, analysis of the phase between u^* and u_L^+ suggests that it is 629 important to preserve the phase between the two signals particularly in the case of higher 630 order statistics. It should be however emphasised that the model must be calibrated for 631 each type of canopy flow regime. 632

⁶³³ Through this work it has been demonstrated that the non-linear interactions within the

Karin Blackman, Laurent Perret, Romain Mathis

roughness sublayer of urban-type rough-wall boundary layers can be modelled using the 634 predictive model as proposed by Mathis et al. (2011a). Although the Reynolds number 635 was shown to have a negligible influence on the model parameters data should be obtained 636 from higher Reynolds number rough-wall flows to expand the range studied. Another 637 point of importance, not addressed in the present study, is the strong spatial heterogeneity 638 of the flow within the roughness sublayer and inside the canopy. The recent experimental 639 study by Herpin et al. (2018) on the scale superimposition in these regions has shown 640 the spatial heterogeneity, both in the wall-normal direction and in the horizontal plane, 641 of this mechanism. These results combined with those obtained here call for a more 642 sophisticated model capable of accounting for the spatial heterogeneity of the flow over 643 large roughness elements. In its present form, the statistical predictive model is a powerful 644 tool, but the dynamic nature of the urban boundary layer and the complexity of the 645 transport processes in the urban canopy limit the capabilities of a statistical model. 646 Future efforts should concentrate on developing a dynamic predictive model, which would 647 have significant potential for the urban boundary layer. Finally, urban canopies with uniform height, such as those studied here, have been shown to have characteristics that 649 are common to other obstructed shear flow canopies (Ghisalberti 2009). These canopies 650 range from terrestrial vegetative canopies to submerged aquatic canopies such as coral 651 and all have an inflection point in the profile of the shear stress. This commonality points 652 to the need for more general approaches to the investigation of amplitude modulation in 653 canopies. 654

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