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Kinetic study of the dissolution of vanadyl sulfate and vanadium pentoxide in sulfuric acid aqueous solution

R. El Hage a, F. Chauvet B, B. Biscans b, L. Cassayre b, L. Maurice c, T. Tzedakis a,*

HIGHLIGHTS

- Vanadium (IV) sulfate VOSO₄ and vanadium (V) pentoxide V₂O₅ dissolution.
- Temporal evolution of the concentrations of VO2+ and VO2+ at various temperatures.
- Understanding the dissolution limitations: V^{IV} → mass transfer; V^V → reaction with H⁺.
- Simple kinetic models to predict the evolution of VO²⁺ and VO₂+ concentrations.

ARTICLE INFO

ABSTRACT

Keywords: Vanadyl sulfate Vanadium pentoxide Dissolution kinetics Vanadium redox battery Solubility The study deals with the 'vanadium (IV) sulfate' and 'vanadium (V) pentoxide' dissolution processes in 3 M $\rm H_2SO_4$ aqueous media. Several measurements of the concentration of dissolved $\rm VO_2^{2*}$ and $\rm VO_2^{2*}$ were achieved in the range of 0 40 °C, and allowed to understand the limitations of the dissolution process ('endothermic' mass transport for $\rm VOSO_4$ and 'exothermic' reaction with the proton for $\rm V_2O_5$). In addition, simple models were proposed (diffusion/accumulation for $\rm VOSO_4$ and kinetic rate for $\rm V_2O_5$) and their resolution leads to theoretical kinetic equations describing the temporal evolution of these concentrations with satisfactory agreement with the experimental curves. Solubility's data and their temperature dependence were determined for both vanadium compounds involved.

1. Introduction

Renewable energy storage studies have expanded in the past decades due to the rapid increase in energy consumption, limited fossil fuels reserves and growing ecological concems of their impact on health and environment.

Only a very limited number of systems enable energy storage such as thermal storage, pumped hydropower and compressed air energy storage (Amirante et al., 2017; Ding et al., 2009). Electro chemical storage constitutes an interesting alternative and recently the Redox Flow Battery (RFB) acquired a great importance as they have the particularity of converting and storing energy by using electroactive species dissolved in electrolyte solutions (Wang et al., 2013; Leung et al., 2012). The most spread RFB is the "all

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vanadium" redox flow battery (VRFB) developed in the 1980's by Rychcik and Skyllas Kazacos (1988), Skyllas Kazacos et al. (1988) and has been widely explored since (Cunha et al., 2015; Skyllas Kazacos et al., 2016, 2015, 2013).

The battery was introduced to overcome the problem of cross contamination of electrolytes, inducing capacity losses reported primarily by NASA researches in the 1970s for the Fe Cr system (Thaller, 1977, 1974). Given that the same element in different oxi dation states is used in both compartments of the VRFB, no con tamination of the active material will occur in case ions cross the ionic separator. The redox couples employed are $V^{(III)}/V^{(II)}$ and $V^{(V)}/V^{(IV)}$ for the negative and the positive half cells respectively (Sum et al., 1985; Sum and Skyllas Kazacos, 1985), and the only redox reactions involved are thus the valence changes of the vana dium ions. The electrolyte solutions are usually prepared in 2 3 M sulfuric acid, even if other electrolytes have been investigated (generation 2 and 3 of the VRB) (Skyllas Kazacos et al., 2007. The VRB is characterized by a long life span (>10,000 cycles) (Ashby and Polyblank, 2012), low maintenance cost and deep discharge

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Nomenclature $A_{(765 \text{ nm})}$ absorbance at the wave length of 765 nm PES polyether sulfone Arrhenius pre exponential factor R° initial radius of the particle (m) a_{VOSO4 solid} activity of the solid compound radius of the particle at the dissolution time t (m) $R_{(t)}$ initial reaction rate (mol L ¹ s ¹) constant (Leveque correlation) r° A_1 , A_2 , A_3 and A_4 constants (defined in Appendix A) total rate of the reaction of the dissolution of V₂O₅ (mol r_{global} concentration of VO²⁺ in the bulk (M) $L^{1} s^{1}$ C_{bulk} $C_{saturation}$ superficial concentration of VO²⁺, assumed at Redox Flow Battery Reynolds number $\frac{d_p \times u}{v} = d_p \times \bar{u} \times \frac{\rho}{\mu}$ scanning electron microscope **RFB** $C_{surface}$ saturation (M) Re $d_{p} \\$ particle diameter at time t (µm) SEM Ď diffusion coefficient (m²/s) S surface of particles involved in the dissolution process E_a activation energy (J/mol) (m^2) thickness of the spherical crown film, function of the Schmidt number = v/DSc $e_{(t)}$ Sherwood number (Solution $2 + a \times Re^{1/2} \times Sc^{1/3} \rightarrow Leveque \ correlation)$ time (m) Sh absorptivity (cm 1 M 1) 3 dissolution time (expressed in 's' for VOSO4 and in 'h' for reaction enthalpy (I/mol) $\Delta_R H$ t number of iterations taken as 100 k kinetic constant following the Arrhenius law (unit func average rate of the liquid around the solid particle cal tion of the reaction order) culated from the stirring rate (m/s), assumed constant $\frac{D}{e_{(t)}}$ mass transfer coefficient of the VO²⁺ around the solid $k_{(t)}$ during the experiment time particle of VOSO₄ (m⁻¹ s) kinematic viscosity (m²/s) μ/ρ ν moles number of dissolved VOSO₄ (to VO²⁺) into the internal energy (J/mol) ΔU m VRFB Vanadium Redox Flow Battery molar mass of the solid VOSO₄ 5H₂O (kg/mol) solid volume present in the solution at time t (m³) M Ν number of VOSO₄ particles having a certain initial ra V_{I} total volume of the solution (including both the liquid dius R° and the powder) initial moles number of V₂O₅ (mol) stirring rate (rpm) $n^{\circ}_{(V)}$ ω initial moles number of H⁺ (mol) moles number of V₂O₅ dissolved at time t Χ $n^{\circ}_{\,(H)}$ specific gravity of the powder (kg/m³) . PTFE polytetrafluoroethylene

capability (Vijayakumar et al., 2013). The energy density of the bat tery is largely depending on the volume and concentration of the vanadium electrolytic solutions and numerous authors studied the effect of the composition of electrolyte solutions (Choi et al., 2017; Skyllas Kazacos et al., 2016) on the performance of the battery.

Despite that, stable solutions with vanadium concentrations higher than 2 M could not be achieved in the working conditions of the VRB, limiting the quantity of stored energy to around 40 kWh/m^3 .

The electrolyte in the negative electrode compartment does not seem to exhibit major limitations related to the solubility of $V^{(III)}$ and $V^{(II)}$, but one point to mention is that $V^{(II)}$ is easily oxidized by air (choi et al., 2013). One important limitation encountered by the vanadium battery appears to be related to the precipitation of compounds in the positive electrode: precipitation of the $V^{(IV)}$ at low temperature and precipitation of the $V^{(V)}$ compounds at high temperature.

This fact limits the working temperature range of the VRB between 10 and 40 °C (Li et al., 2011). Precipitation of various vanadium salts and oxides was studied by several research groups and it was found that higher sulfuric acid concentrations stabilizes the $V^{(V)}$ solutions (Rahman, 1998) but decreases the solubility of $V^{(II)}$, $V^{(III)}$ and $V^{(IV)}$. This is attributed to the common sulfate ion effect (Skyllas Kazacos et al., 2016): increasing the total sulfate concentration shifts the equilibria (1) (4) towards the left, leading to a lesser dissociation of the vanadium sulfate salts (Rahman and Skyllas Kazacos, 1998; Cheng, 1991) and to the precipitation of the salts in solution.

$$VSO_{4(s)} \leftrightarrows V^{2+} + SO_4^2 \tag{1}$$

$$V_2(SO_4)_{3(s)} \leq 2 V^{3+} + 3SO_4^2$$
 (2)

$$VOSO_{4(s)} \leftrightharpoons VO^{2+} + SO_4^2 \tag{3}$$

$$(VO_2)_2SO_{4(s)} \leq 2VO_2^+ + SO_4^2$$
 (4)

As mentioned by Rahman and Skyllas Kazacos (2009), vana dium (V) can precipitate after 1000 h at 50 °C and the redissolution of the oxide V_2O_5 (Rahman, 1998) appears to be difficult. Numer ous authors (Ivakin and Voronova, 1973; Vijayakumar et al., 2011; Kausar, 2002) conducted studies to understand the poor thermal stability of $V^{(V)}$ at high temperatures. They showed that the precipitation process of V_2O_5 is endothermic and thus enhanced when temperature increases.

Moreover, the aqueous chemistry of vanadium (V), studied by several authors (Crans et al., 2004; Elvingson et al., 1998), inferred the presence of many species as a function of the solution's pH. It was suggested that pervanadyl or dioxovanadium cation (VO₂) is the main species formed in the lower pH range (0.5 1.3) (Baes and Mesmer, 1976). However, the presence of VO₃ species was also reported in the concentration range of 1 M of V^(V) in 5 M total sul fate (Kausar, 2002). Based on Raman spectroscopy analysis, the authors propose that VO₃ species are surrounded by a densely packed ionic environment of other V^(V) and sulfate ions and these ions could be involved in weak or unstable complex formation with other ions. In the case of H⁺ ions depletion, VO₃ tends to pre cipitate as a disordered V₂O₅ aggregate (Kausar, 2002). Increasing the acid concentration enables to prevent this precipitation and favor the stabilization of V(V) in the form of VO₂⁺. However, this induces a negative effect on the overall performance of the battery because of the increasing viscosity and an enhancement of the ohmic drops resulting in the lowering of the energy efficiency (Choi et al., 2017).

Numerous works exist on the field of the vanadium battery, and one important objective is to avoid the vanadium pentoxide precipitation. Indeed according to Rahman (1998) and Rahman and Skyllas Kazacos (2009) vanadium (V) oxide dissolution is dif ficult, in addition to being an endothermic dissolution (Ivakin and Voronova, 1973; Vijayakumar et al., 2011; Kausar, 2002). Neither the understanding of the dissolution phenomena of the vanadium compounds, nor elucidation of the corresponding mechanisms was significantly explored; the published studies do not exhibit the determination of the physical limitations in order to act upstream. Hence, the present work deals with the study of the dissolution mechanisms of two common vanadium compounds in 3 M sulfuric acid, at various temperatures (0 40 °C), stirring rates and initial particles size. Apart from being the most com mon concentration used for an operating battery with 2 M VOSO₄, the sulfuric acid concentration (3 M) is chosen here, as a compro mise between its positive effect on the dissolution of the vana dium pentoxide and its negative effect on the dissolution of vanadium sulfate (Rahman, 1998). Note also that, by increasing the sulfuric acid concentration, the solubility of the oxide increases, but this increases the viscosity of the solution leading to a pressure drop. Moreover, during the cycling of the battery and more specifically during recharge (oxidation of $V^{(IV)}$ to $V^{(V)}$), H⁺ ions are generated in the positive compartment leading to an increase in acidity, therefore, it is not necessary to study higher H₂SO₄ concentrations.

To sum up, the general purpose of this study is to understand the phenomena governing the dissolution of vanadyl sulfate VOSO $_4$ and vanadium pentoxide V $_2$ O $_5$ and to establish the corresponding kinetic laws, in order to have a better control on the accidental pre cipitation during VRB operations.

2. Material and methods

2.1. Dissolution protocol

The chemicals used are vanadium (IV) sulfate oxide hydrate VOSO $_4$ xH $_2$ O (99.9%), vanadium (V) pentoxide V $_2$ O $_5$ (99.6%) from Alfa Aesar, NormaPur H $_2$ SO $_4$ from Sigma Aldrich, and deionized water.

Dissolution experiments were achieved in a thermo regulated reactor (cylinder of an internal diameter = 2 cm) at constant tem perature. An adequate volume of aqueous solution 3 M sulfuric acid is poured in the reactor and stirred with a 1.5 cm magnetic bar until reaching the selected temperature. Then, an excess of vanadium compound is added ($m_{(vanadyl\ sulfate)}$ = 4.559 g and $m_{(vanadium\ pentoxide)}$ = 1.461 g), marking the initial time of the experiment. Stirring rate is kept constant during the experiment. At regular time intervals, aliquots are withdrawn from the solution with plastic syringes and are directly filtered twice with filters resisting to the acid media. The first filtration is performed using a polyether sulfone (PES) filter with a pore diameter of 0.23 μ m, and the second one a polytetrafluoroethylene (PTFE) membrane filter (Millipore ready to use filters in plastic assembly) with a pore diameter of 0.1 μ m.

The recovered filtrate is diluted and analyzed with the appropriate method.

The vanadium compounds dissolution occurs according to reactions (3) and (5) for $VOSO_4$ and V_2O_5 respectively.

$$V_2O_{5(s)} + 2H^+ \Leftrightarrow 2VO_2^+ + H_2O$$
 (5)

These reactions were taken into account because the species involved at the chosen concentration of H_2SO_4 (3 M) are in agree ment with the E pH diagram indicated by Post and Robins (1976), and with the $V^{(V)}$ species distribution calculated from constants given by Baes and Mesmer (1976), Guzman et al. (2002).

2.2. Characterization methods

2.2.1. UV visible spectrophotometry for vanadium (IV) analysis

The UV VIS spectrophotometer device is a Hewlett Packard Model 8453.

According to their oxidation state, the vanadium compounds exhibit various absorption bands at the UV visible wavelengths range. However, no absorption band could be determined for the VO_2^+ species; this is why potentiometric titration was used (see next section).

For the $V^{(IV)}$ quantification, the absorbance was measured at a wavelength of 765 nm (Choi et al., 2017) exclusively due to VO^{2^+} . A preliminary calibration enables to obtain the $A_{(765nm)}$ = f ([VO^{2^+}]) correlation and leads to an absorptivity ϵ value of 21.4 cm 1 M 1 , with deviations $\frac{\Delta \epsilon}{\epsilon}$ of 0.6 and 0.25 from the values proposed by Choi et al., 2013 and Brooker et al.(2015) respectively.

2.2.2. Potentiometric titration of vanadium (V)

A potentiometric titration method is used to determine the concentration of the VO_2^+ released from the dissolved V_2O_5 powder. The titration agent is Mohr salt, supplied by Sigma Aldrich and prepared in sulfuric acid media (Le Flem, 1964). The redox systems involved in this titration are thus VO_2^+/VO^{2+} and $Fe^{(III)}/Fe^{(II)}$ and the titration reaction is:

The titrations are carried out using a combined Pt Ag/AgCl/Cl electrode.

2.2.3. ICP analysis

ICP analysis (Inductively Coupled Plasma; ULTIMA 2 ICP OES) was used for total vanadium aqueous concentration determination, in order to characterize the amount of water in the commercial vanadyl sulfate powder VOSO₄ xH₂O.

2.2.4. Morphology and particle size distribution of the powders

The scanning electron microscope (SEM) used to observe the grains morphology is a PhenomWorld XL SEM. The solid powders $(V_2O_5$ and $VOSO_4$ xH $_2O)$ were coated with a thin gold layer (using an Emiteck K550X device) prior SEM observation.

A laser diffraction particle sizing technique, using a Malvern Mastersizer 3000, was used to get the size distribution of the grains. The Malvern Mastersizer is usually used for materials rang ing from hundreds of nanometers to several millimeters in size (Fu and Sun, 2001). The particle size is reported as a volume equivalent sphere diameter.

3. Results and discussion

3.1. Dissolution of vanadium (IV) sulfate

3.1.1. Characterization of the initial powder

The commercial vanadyl sulfate powder VOSO₄ xH₂O used for the dissolution experiments is partially hydrated. Its water content x was determined by ICP at different concentrations, according to the method of determination of the vanadium concentration in an aqueous solution. The results of three analyses are found to be in the range from 5.4 to 5.6; thus taking into account the uncer tainties of the analyses, the retained value of x is 5. Note that this result is in agreement with an octahedral geometry, and also with the fact claimed by Selbin (1965), the hydrated vanadyl sulfate exists as $[VO(H_2O)_5]^{2+}$, 'the vanadyl ion' in acidic solutions. In the following, $VOSO_4$ xH₂O is thus indicated as $VOSO_4$ 5H₂O Fig. 1.

Fig. 1 presents SEM micrographs of the commercial powder. These images display aggregated and multi shaped particles of

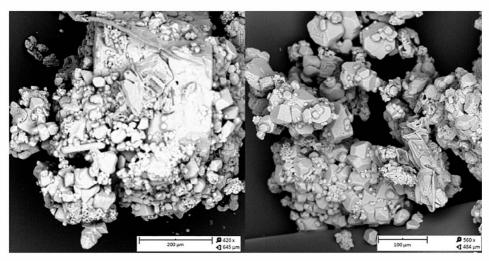


Fig. 1. SEM images of the vanadyl sulfate VOSO₄·5H₂O commercial powder; 15 kV-Point; BSD full.

all sizes. Their dispersion during the dissolution in a stirred solution is expected to be easy, because of the dislocation occurring after the dissolution of the smallest particles.

The VOSO₄ 5H₂O particle size distribution is presented in Fig. 2. The first graph (Fig. 2 1) provides the particle size distribution of the commercial powder and clearly shows two distinct ranges: from 5 to 350 μm and from 350 μm to 4 mm. The commercial powderwas sieved at 315 μm and separated into two fractions, for which particle sizes are presented in Fig. 2 2 and 2 3. They confirm two distinct populations of particle diameter: $d_p < 315~\mu m$ and $d_o > 315~\mu m$.

3.1.2. Temperature dependence of the dissolution kinetics

Fig. 3 gathers experimental measurements of VO²⁺ concentration in the electrolyte during the dissolution, for temperatures in the range from 5 to 30 °C. For all the examined temperatures, a similar temporal evolution of the concentration of VO²⁺ was observed: the concentration increases rapidly at short reaction times (t < 3 min) and then the dissolution slows down until equi librium is reached, after around 10 min. When the temperature increases from 5 to 30 °C the initial dissolution rate increases as well.

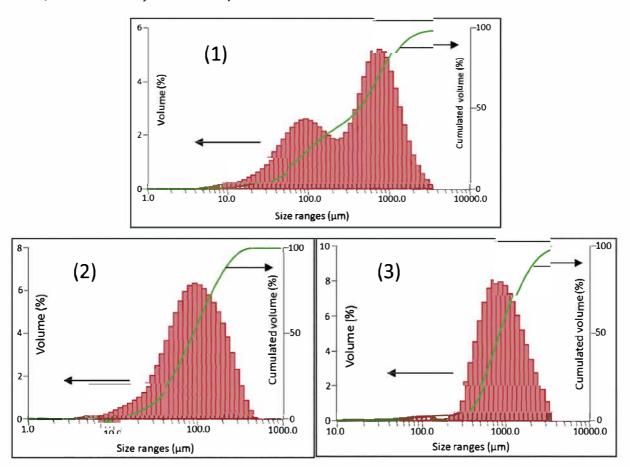


Fig. 2. Laser diffraction analysis (P = 3 bar; dry mode) showing the VOSO₄·5H₂O size distribution: (1) commercial powder; (2) sieved powder $d_p < 315 \mu m$; (3) sieved powder $d_p > 315 \mu m$.

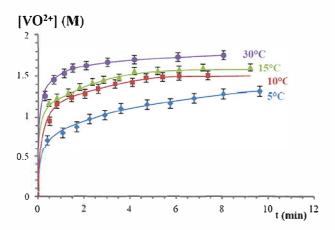


Fig. 3. Temporal evolution of the concentration of VO $^{2+}$ released by the dissolution of a VOSO₄·5H₂O commercial powder, for various temperatures; [H₂SO₄] = 3 M; stirring 500 rpm; aliquots filtered by 0.23 and 0.1 μ m filters.

The first concentration reported on the graph corresponds to 20 s after the introduction of the solid into the stirred solution. For this first measurement, at 5 °C the vanadium concentration reaches 0.7 M and this value doubles (1.3 M) at 30 °C.

The concentration of the VO²⁺ measured at 20 s, will be used to determine the initial dissolution rate r° (defined as the ratio $\frac{\lfloor VO^{2+} \rfloor_{20s}}{20s}$). Assuming that the kinetic constant of the initial dissolution rate follows the Arrhenius law, Eq. (1) gives the initial dissolution rate r° .

$$\mathbf{r}^{\circ} \quad \mathbf{k} \times \mathbf{f} \quad \mathbf{A} \times \mathbf{e}^{\mathbf{E}_{\mathbf{d}}/\mathbf{R}\mathbf{T}} \times \mathbf{f}$$
 (1)

where f is a function of the various operating parameters (activity of the solid vanadyl sulfate, diffusion coefficient of VO^{2+} , size of solid particles...). Some of these parameters depend on the temper ature and this dependence is expected to be studied in a future work. Here, in order to get a rough order of the magnitude of the activation energy, the experimental data were analyzed (assuming the function f independent of T) and leads to the following linear regression:

$$\ln r^{\circ}_{(\frac{mad}{2})} = \frac{2266.7}{T_{(K)}} + 4.8579 \tag{2}$$

This relation leads to an approximation of the activation energy of 18.8 kJ/mol for the dissolution of $VOSO_4 5H_2O$ in 3 M sulfuric acid, a value relatively low compared to the activation energy of a classical chemical reaction.

3.1.3. Effect of stirring rate and particle size on dissolution kinetics

Several dissolution experiments were achieved by applying three stirring rates (500, 100 and 15 rpm), corresponding respectively to (i) a well stirred homogeneous suspension, (ii) a mini mum stirring rate enabling to uplift the particle and (iii) partially decanted solid. Besides, these experiments were carried out for two different particles size d_p (<315 μ m and >315 μ m). The corresponding time evolution of VO²⁺ concentration is presented in Fig. 4.

For a defined range of particles size (d_p < 315 μm curves 1 2 3 or d_p > 315 μm curves 4 5 6, Fig. 4), it appears that a higher stir ring rate increases the dissolution kinetics, since higher concentrations are achieved in a shorter time. For instance, $[VO^{2+}]_{(dp < 315 \ \mu m; \ \omega = 100 \ rpm; \ t = 1')} = 1.5 \ M$ and $[VO^{2+}]_{(dp < 315 \ \mu m; \ \omega = 100 \ rpm; \ t = 1')} = 1.0 \ M$.

Under constant stirring, the dissolution rate increases by decreasing the particles size. Thus, for a given dissolution time, and before reaching equilibrium, higher salt concentrations were measured with smaller particles. Indeed comparison of curves (1) and (4) obtained in two "well stirred" suspensions show that the concentration of VO^{2+} after 1 min reaction time increases from ~ 1.2 to ~ 1.5 M when the size decreases from $d_p > 315$ μm to $d_p < 315$ μm .

A different shape is obtained for curves (3) and (6), which cor responds to the lowest stirring rate; they exhibit the slowest disso lution rate for both particle sizes. The slow agitation does not enable the motion of the particles which sediment at the bottom of the vessel, forming a 'coagulated' powder paste. Around each grain of this paste, the VO²⁺ concentration reaches rapidly the sat uration concentration. These facts are in agreement with a dissolution rate limited by mass transfer. For long reaction time, all the curves tend to converge to the same saturation concentration (~1.7 to 1.8 M).

3.1.4. Equilibrium data

After a certain time of stirring (between 5 and 10 min), the solution is saturated and the concentration of VO²⁺ is constant. The equilibrium values are reported in Fig. 5, along with data from Skyllas Kazacos et al. (2016) and Rahman and Skyllas Kazacos (1998)

A satisfactory agreement is observed between our results and those of previous works, which confirms that the solubility of VO²⁺ increases with temperature. For the highest comparable tem perature (30 °C), a significant difference of around 20% is observed.

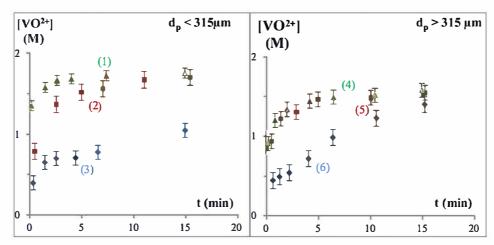


Fig. 4. Temporal evolution of the concentration of VO²⁺ released by the dissolution of a VOSO₄·5H₂O commercial powder, for suspensions containing two different particle sizes and subjected to various stirring rates ω , T = 25 °C, [H₂SO₄] = 3 M, VOSO₄·5H₂O powder; Left: $d_p < 315 \mu m$: ω (in rpm) for (1), (2) and (3) are 500/triangles, 100/squares and 15/diamonds respectively; Right: $d_p > 315 \mu m$: ω (in rpm) for (4), (5) and (6) are 500/triangles, 100/squares and 15/diamonds respectively.

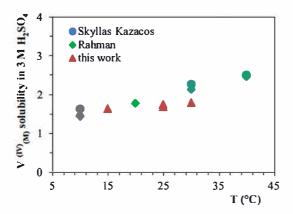


Fig. 5. Influence of temperature on the solubility of $V^{(IV)}$. Triangles: this work; circles: M. Skyllas-Kazacos et al.; diamonds: F. Rahman et al.

This could be attributed to the difficulties encountered in the mea surement of a precise volume at this temperature.

The results show that the solubility of VO²⁺ increases with tem perature. The equilibrium constant of the VOSO₄ 5H₂O dissolution (reaction (3)) can be written as following:

$$\mathbf{K}_{(3)} = \left(\frac{a_{VO^{2+}} \times a_{SO_4^2}}{a_{VOSO_4} \text{solid}}\right)_{at \text{ the equilibrium}} \tag{3}$$

Even if the first dissociation of H_2SO_4 to HSO_4 is total (high $K_{H_2SO_4/HSO_4}$), the second dissociation to SO_4^2 remains partial with an equilibrium constant K_{HSO_4/SO_4^2} 0.013 at 25 °C(the concentrations are in mol/kg) (Wallace, 1966). However, the released quantity of sulfate ions from HSO_4 dissociation is not significant compared to the quantity released from the dissolution of $VOSO_4$; this imply that $[VO^{2+}]$ can be assumed equal to $[SO_4^2]$.

Concerning the activity of the solid powder of VOSO₄, we will assume it equal to 1. Thereby, the above equation can be written as follows:

$$K_{(3)} = \frac{\gamma_{VO^{2+}} \times \gamma_{SO_4^2}}{a_{VOSO_4Solid}} \times \left[VO^{2+}\right] \times \left[SO_4^2\right] \Rightarrow K_{(3)}$$

$$\lambda \times \left(\left[VO^{2+}\right]_{at \ equilibrium}\right)^2$$
where $\lambda = \frac{\gamma_{VO^{2+}} \times \gamma_{SO_4^2}}{q_{SOS_0.80M}}$. (4)

Because the concentrations of VO^{2+} at saturation are relatively high (1.2–1.7 M), the activity coefficients depend on the concentration, while the activity of the vanadyl sulfate solid is equal to 1; in a future work, the Pitzer model will be used in order to express these activity coefficients. Here, in order to get a rough estimation of the sensitivity of vanadyl sulfate solubility against temperature, the logarithm of the VO^{2+} saturation concentration was plotted versus $1/\Gamma$, assuming λ independent from the concentration of the various

The linear regression analysis leads to the following relation:

$$ln[VO^{2+}]_{(ext\ inM)}$$
 $\frac{982.2}{T_{(inK)}} + 3.8$

species.

with a relatively low correlation coefficient (R^2 = 0.91) with the experimental results, explaining the uncertainties due to the dependence of the activity coefficients on the concentration.

From the slope of the above equation (982.2 k/(2R)), we deduce the value of k = 16.3 kJ/mol.

The obtained value is (i) positive showing the endothermic character of the vanadyl sulfate dissolution, and (ii) a relatively low value, compatible with the dissociation of an ionic salt weakly bonded.

3.1.5. Elucidation of the mechanism of the vanadyl sulfate dissolution

The results of this study show that, at constant temperature, the dissolution of vanadyl sulfate in 3 M sulfuric acid is limited by mass transport and that two main parameters (stirring rate and particle size) affect the dissolution rate.

Let us consider the following mechanism for the dissolution of the solid salt VOSO₄ 5H₂O:

$$VOSO_{4(solid)} \leftrightharpoons VOSO_{4(solvated/dissolvedonthesurface)}$$
 (7)

VOSO₄(solvated/dissolvedonthesurface) \Rightarrow (VO²⁺ + SO₄²) boths pecies dissociated on the surface (8

$$VO^{2+}_{(dissociatedonthesurface)} \leftrightharpoons VO^{2+}_{(bulk)}$$
 (9)

Taking into account the results related to the effect of stirring (§3.1.3), the limiting step in the vanadyl sulfate dissolution will be assumed to be the transport of the VO²⁺ from the surface of the particles to the bulk i.e. reaction (9). Besides, in the absence of an electric field, the transport of ions produced in reaction (8) is assumed to occur both by diffusion and by convection.

The mass balance for VO^{2+} in the area between the surface of the particle and the bulk could be written, (using m as the $V^{(IV)}$ molar concentration), as following:

Dissolution flux $_{(7)} \approx$ dissociation flux $_{(8)} \approx$ diffusion flux $_{(9)} =$ accumulation of VO²⁺ flux into the bulk

$$\frac{\left(\frac{\partial \vec{m}}{\partial t}\right)_{bulk}}{\left(\text{Fick's 1st law}\right)}$$
 $S \times D \times (grad \vec{C})_{surface of particle}$ (5)

To simplify, the VOSO₄ 5H₂O solid particles are considered spherical and a simple film model around the particle is creating the limitation to mass transfer (i.e. one direction transfer), the pre vious equation can be simplified as following:

$$\left(\frac{\partial \vec{m}}{\partial t}\right)_{\text{bull.}}$$
 $S \times D \times \left(\frac{\partial \vec{C}}{\partial R}\right)_{\text{surface of particle}} \Rightarrow$

$$\frac{\left(\frac{\partial \mathbf{m}}{\partial t}\right)_{\text{bulk}}}{S \times D \times \frac{C_{\text{bulk}}}{\left(\mathbf{R}_{(t)} + e_{(t)}\right)} \frac{C_{\text{surface}}}{\mathbf{R}_{(t)}}}{S \times \mathbf{k}_{(t)} \times (C_{\text{sat}} \quad C_{\text{bulk}})}$$
(6)

The effect of the convection was examined on the mass transfer coefficient $k_{(t)}$, using the expression of Ranz and Marshall relative to a forced convection around a solid sphere (Cussler, 1984) (also known as the Leveque correlation providing the Sherwood number).

Sh Sherwood number
$$\frac{\mathbf{k}_{(t)} \times \mathbf{d}_{p}}{\mathbf{n}} = 2 + \mathbf{a} \times \mathbf{R} \mathbf{e}^{1/2} \times \mathbf{S} \mathbf{c}^{1/3}$$
 (7)

This correlation is appropriated for spherical particles having the same size. In order to improve its applicability on the present case, some assumptions will be considered:

The calculations will be achieved assuming the presence of four separated size ranges of the solid particles having an initial radius R° = 20, 40, 500 and 1000 μ m representing respectively 20%, 35%, 35% and 10% of the total solid volume (see curve of Fig. 2 1, cumulated volume);

All the particles of the powder will be assumed spherical, despite the various shapes observed (Fig. 1). Considering Eq. (7), the constant "a" is generally assumed equal to 0.6. However, in the present study and because of the large size distribution, "a" will be taken as an adjusting factor, which effect will be examined.

The molar quantity of the dissolved VO²⁺ "m" for N particles of initial radius R° can be expressed as:

$$m = \frac{\rho \times V}{M} = N \times V_{one particle} \times \frac{\rho}{M}$$

$$N \times \frac{4}{3} \pi \times (R^{\circ 3} - R_{(t)}^{3}) \times \frac{\rho}{M}$$

$$(8)$$

(Refer to notation and symbols)

The concentration of VO²⁺ in solution can be written as $C_{bulk} = \frac{m}{V_l}$, being the total volume of the suspension (including both the liquid and the solid).

Combining Eqs. (6) (8) leads to Eq. (9) describing the variation of the radius R of the solid particles as a function of time, and representing the dissolution rate \imath of the vanadyl sulfate:

$$i \Rightarrow \frac{dR}{dt} = \frac{A_{1} - A_{2} \left(R^{\circ 3} - R_{(t)}^{3}\right) + A_{3} \sqrt{R_{(t)}} - A_{4} \left(R^{\circ 3} - R_{(t)}^{3}\right) \sqrt{R_{(t)}}}{R_{(t)}}$$
(9)

where A_1 to A_4 are constants (refer to Appendix A for their developed expressions).

Eq. (9), written as $\imath \Rightarrow \frac{dR}{dt} \quad f(R)$, is solved numerically using the Euler method $(R_{j+1} \quad R_j + step \times f(R,t))$ and enables to calculate a theoretical radius at time t, given that at t° = 0, R = R°.

Note that the step used is: $\frac{reaction time}{number of iterations j}$ $\frac{10}{100}$ 0.1 min

The value of the radius R of a certain particle of $VOSO_4 5H_2O$, obtained at a certain time t, from the resolution of Eq. (9) enables to obtain the theoretical values of the dissolved quantity of VO^{2+} i.e. the moles number, using Eq. (8).

Note that Eq. (9) is resolved 4 times, each for one of the chosen initial R° (20, 40, 500 and 1000 μ m) of the solid particles and the total concentration of the dissolved vanadium sulfate (VO²⁺) in solution is deduced (sum of the four obtained values of molar quantity divided by V_1). Also, for each R°, a different value of the adjusting factor "a" (Eq. (7)) was determined.

Fig. 6 shows two examples of the iterative determination, at $30\,^{\circ}$ C, of the optimal value of two parameters (the constant "a" in the Leveque equation and the percentage of each particle size range which directly affects the number of total particles N of each R°). The optimized value of "a" or "N", is the one leading to a curve of the concentration of the dissolved vanadium sulfate which fits best with the experimental data curve.

Following this iterative mode enables to evaluate the calculated curves at each temperature and the results are presented in Fig. 7 comparatively to the experimental data. Note that the viscosity was calculated for each temperature (Fassulo, 1965), while the value of the diffusivity at 25 °C (Jiang et al., 2016) was used for all the examined temperatures.

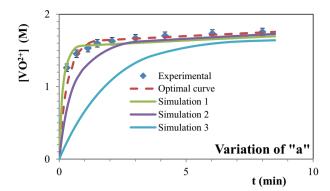
A relatively good agreement ($\frac{\Delta C}{C}$ ± 0.1 M/ ~ 1.5 M) is observed between the results of the model and the experimental ones. Discrepancies are observed for short durations of the dissolution (t < 1 min) because of the difficulty to standardize rapidly the suspension and to achieve precise measurement at the first few seconds after the stirring begins

Another difficulty comes from the dissolution of the smallest particles, which exhibit fast kinetics. In fact, compared to the bigger particles, this introduces additional uncertainties because the num ber of small particles of powder was not exactly taken into account.

To sum up, the obtained results lead to the following conclusions:

Regarding the effect of temperature:

The initial dissolution rate increases with temperature.
 The solubility of the vanadyl sulfate at saturation (when the equilibrium of dissolution is reached) increases slightly with the temperature in the examined range of 5 30 °C, and this is compatible with the dissociation of an ionic salt weakly bonded.



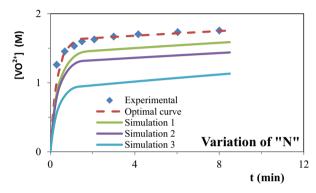


Fig. 6. Temporal evolution of the concentration of VO^{2+} released by the dissolution of the $VOSO_4 \cdot SH_2O$ commercial powder: dots = experimental curves; Continuous lines = simulated curves obtained with the non optimized parameter value, i.e. the constant "a" in the Leveque equation (figure on the top), and the percentage of each particle size range which directly affects the number of total particles "N" of each R° (figure on the bottom); Broken lines = simulated curves obtained with the optimized parameters of "a" (figure on the top), and "N" (figure on the bottom).

Both the stirring of the suspension and the size of the particles strongly affect the dissolution rate (mainly for dissolution times lower than 5 min), proving that the dissolution kinetics of the vanadyl sulfate (to VO²⁺), is limited by the mass transfer of VO²⁺ from the solid powder surface to the bulk, while the chem ical reaction with the proton is not limiting.

3.2. Dissolution of vanadium pentoxide

3.2.1. Characterization of the initial powder

The commercial powder of V_2O_5 was characterized by SEM and laser diffraction particle sizing technique. The SEM micrograph in Fig. 8 1 shows that the V_2O_5 particles form agglomerated sticks of various sizes. The size distribution (Fig. 8 2) shows a large dispersion of particle size from 120 nm to 4 mm.

The graph exhibits three peaks located respectively at 2, 80 and 900 μm ; therefore, in order to study the effect of particles size on the dissolution kinetic, the initial powder was sieved using four different cut off threshold sieves: 315 μm ; 200 μm ; 120 μm and 80 μm . Thus, five different diameter ranges of powder were obtained: $d_p > 315 \ \mu m$; 315 > $d_p \ (\mu m) > 200$; 200 > $d_p \ (\mu m) > 120$; 120 > $d_p \ (\mu m) > 80$ and $d_p \ (\mu m) < 80$, three of which were used to carry out dissolution experiments.

3.2.2. Effect of temperature on dissolution kinetics

The effect of temperature on the dissolution of vanadium pen toxide was studied in the range 0 40 $^{\circ}$ C and the temporal evolution of the dissolved VO₂ concentration is presented in Fig. 9.

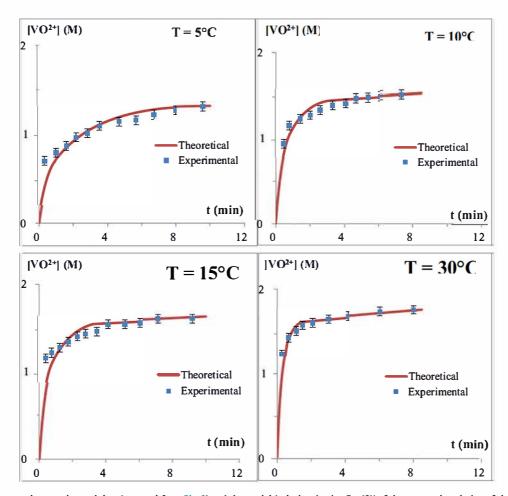


Fig. 7. Comparison between the experimental data (reported from Fig. 3) and the model (calculated using Eq. (9)) of the temporal evolution of the concentration of VO²⁺ released by the dissolution of a VOSO₄-5H₂O commercial powder, at various temperatures.

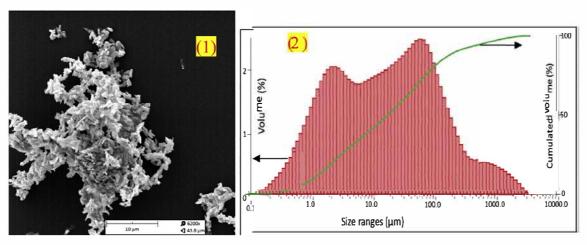


Fig. 8. (1) SEM pictures (10 kV-Point; SED) and (2) size distribution obtained (by laser diffraction sizing technique; P = 3 bar, dry mode) of the vanadium pentoxide V_2O_5 commercial powder.

The behavior is rather similar for each temperature: a rapid dis solution occurs at "short" reaction times (less than 1 h) and then the concentration tends to reach a constant value. Note that, for all the examined temperatures (except 0 °C), the dissolution equi libria of the vanadium pentoxide to VO₂ is achieved after 5 h of

stirring; for the dissolution at 0°C a higher reaction time is required to reach the saturation.

Several differences can be observed compared to the dissolution features of VOSO₄:

The saturation concentrations ($C_{sat.}$) of VO₂ are about three times lower than those of the VO²⁺; in addition, the $C_{sat.}$ decreases when the temperature increases (contrary to the case of the V^(IV), where $C_{sat.}$ increases with T). This point will be analyzed in the next section.

For the stronger stirring (500 rpm), the time required to dissolve the oxide and to reach the saturation concentration of VO_2^+ is more than fifty times higher than that required for the VO^{2+} . Typical comparative values are 5 min to reach a concentration of VO^{2+} of 1.5 M, while 3 h were required to reach a concentration of VO_2^+ of 0.5 M. Moreover, at 40 °C, the saturation concentration of VO_2^+ is reached for t < 20 min, while at 0 °C the solution is not saturated, even after 5 h. Another experiment was carried out at 0 °C where the suspension of vanadium pentoxide was left under stirring for one day. The concentration of the dissolved VO_2^+ was determined and the following values were obtained: $[VO_2^+]_{23h} = 0.788$ M and $[VO_2^+]_{25h} = 0.783$ M. This last result tends to show that the mass transport is not the limiting step.

The concentration of the VO $_2^+$ measured for reaction times lower than five minutes (named $t_{initial}$), will be used to estimate approx imatively the initial rate of the V_2O_5 dissolution r^o (defined as the ratio $\frac{|VO_2^+|_{t_{initial}}}{t_{oitial}}$).

Assuming, as for the vanadyl sulfate, that (i) the kinetic constant

Assuming, as for the vanadyl sulfate, that (i) the kinetic constant of the initial dissolution rate follows the Arrhenius law, and (ii) the others terms of the expression of the dissolution rate are independent of the temperature, then, the logarithmic analysis of the evolution of the initial rate with the temperature leads to the following correlation:

$$\ln \mathbf{r}_{(\mathbf{r} \circ in \frac{md}{2})}^{\circ} = 22.7 - \frac{8727.3}{T_{(in. K)}}$$
 (10)

The slope of this linear relation enables the determination of a roughly estimated value of the activation energy of the dissolution process: E_a 73 kJ/mol.

This energy is more than four times higher than the value obtained for the dissolution of VOSO₄ (18.8 kJ/mol). This could be explained by the fact that the hydration of the vanadium pentoxide (V₂O₅ which exhibits covalent bonds) followed by its reaction with H⁺ ions is energetically more difficult to achieve, comparatively to the simple dissociation of the ionic salt VOSO₄.

3.2.3. Effect of available surface area on dissolution kinetics

The effect of the particle size on the dissolution rate of V_2O_5 was examined at 40 °C and 500 rpm stirring rate and the results are shown in Fig. 10.

Practically the same concentrations were measured for the three different size ranges of the solid particles ($80 < d_p < 120 \mu m$, $120 < d_p < 200 \mu m$ and $200 < d_p < 315 \mu m$). These results tend to show that the dissolution rate does not depend on the solid/liquid exchange surface. Theoretically, the particle size affects the initial rate of the dissolution that should increase. However, in our case, owing to the low values of these dissolution rates, the curves do not have enough resolution to show any difference. Moreover, these results support our previous conclusion: the mass transfer does not represent a limitation to the dissolution of V_2O_5 but it is rather the chemistry of the system.

Consequently, the effect of stirring on the dissolution was not studied.

Since the dissolution is not significantly affected by the particles size, the possibility of kinetic control by surface passivation was evaluated.

A simplified reaction scheme is proposed below for the vana dium pentoxide dissolution (R5):

Hydrogen ion attacks the oxide and the product obtained from reaction (5_b) decomposes according to reaction (5_c); then by reaction with H⁺, it forms an intermediate (In) which dehydrates to lead to VO₂⁺.

However, another reaction pursue of the intermediate (In) could be its polymerization according to various reactions and in the last case, the external surface of each solid particle could be entirely covered by a passive layer that prevents the dissolution and could be the reason for which the observed saturation concentration of VO₂⁺ remains low.

To clarify this point, the following dissolution experiment was carried out: a solid liquid suspension of the commercial V_2O_5 sieved powder $(200 \le d_p \le 315~\mu m)$ was introduced into a H_2SO_4 3 M solution at 25 °C and stirred during 5 h. The results are illus trated in Fig. 11: the $\{VO_2^*\}$ increases to reach the saturation concentration ($\sim\!0.55~M$ after $t\sim\!1~h)$ then remains constant. Then the suspension was filtered to remove the residual solid and a fresh sample of the powder was added into the filtrate. The dissolution experiment was pursued for 6 h, and the temporal evolution of the concentration of the vanadium is indicated into Fig. 11 (for t>22~h until t=28~h). The renewal of the solid does not change the dissolved amount of vanadium, implying that the equilibrium was reached and no further dissolution can be achieved. This test confirms that there is no passivating or inhibiting layer formed on the surface of the particles.

3.2.4. Equilibrium data

The saturation concentration of VO_2^{\star} , obtained for t > 5 h (extracted from Fig. 9), are reported in Fig. 12, simultaneously with the values from Rahman (1998), Skyllas Kazacos et al. (2016). Note that the values extracted from the bibliography were multiplied by 2 in order to obtain the concentration of VO_2^{\star} , instead of the solu bility of V_2O_5 used in the cited references. The saturation concentration of VO_2^{\star} decreases when the applied temperature increases, even if a shorter time is required to reach the equilibrium.

The equilibrium constant of reaction (5) can be written as a function of the activities of the species in solution:

$$K_{(5)} = \frac{\left(a_{VO_2^+}\right)^2 \times a_{H_2O}}{a_{V_2O_5 \text{ solid}} \times \left(a_{H^+}\right)^2}$$

$$= \frac{a_{H_2O} \times \left(\gamma_{VO_2^+}\right)^2}{a_{V_2O_5 \text{ solid}} \times \left(\gamma_{H^+}\right)^2} \times \left(\frac{\left[VO_2^+\right]}{\left[H^+\right]^\circ \quad \left[VO_2^+\right]}\right)^2$$

$$(11)$$

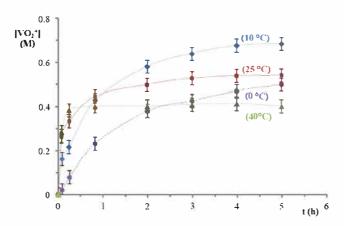


Fig. 9. Temporal evolutions of the concentration of the VO_2^* (released by the dissolution of a V_2O_5 commercial powder), at various temperatures; $[H_2SO_4] = 3$ M; stirring 500 rpm.

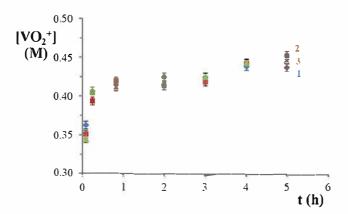


Fig. 10. Temporal evolutions of the dissolved VO₂ concentration (released by the dissolution of a V_2O_5 commercial powder) for various initial sizes of the solid particles of V_2O_5 obtained by sieving; $[H_2SO_4]$ = 3 M, stirring 500 rpm, sieved V_2O_5 powder, T = 40 °C. (1) $80 < d_p < 120 \ \mu m$; (2) $120 < d_p < 200 \ \mu m$; (3) $200 < d_p < 315 \ \mu m$.

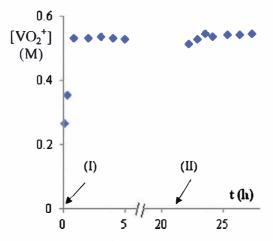


Fig. 11. Temporal evolution of the VO $_2^*$ concentration (released by the dissolution of a V $_2O_5$ commercial powder) for two different additions of solid samples of V $_2O_5$ into the liquid; 15 cm 3 of [H $_2$ SO $_4$] = 3 M, stirring 500 rpm, T = 25 °C, sieved V $_2O_5$ powder (200 < d $_p$ < 315 μ m). (I) first introduction of 2.2 g of V $_2O_5$; (II) filtration and second introduction of 2.2 g of V $_2O_5$.

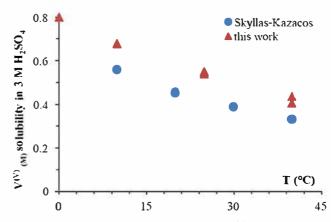


Fig. 12. Influence of temperature on the solubility of $V^{(V)}$. Triangles: this work; circles: Rahman (1998), Skyllas-Kazacos et al. (2016).

In the present case, the concentrations of the VO_2^* at saturation are lower than the values obtained for VO^{2*} at saturation (Fig. 9: 0.4 0.7 M for stirring duration of 5 h). The effect of the concentration on the activity coefficient will also be examined in a future work via the Pitzer model.

For the time being, in order to get a preliminary rough estimation of the sensitivity of the vanadium pentoxide solubility against

the temperature, the term $\frac{a_{H_2O} \times \left(\gamma_{VO_2^*}\right)^2}{a_{V_2O_2^*sold} \times (\gamma_{H^*})^2}$ will be considered con stant and named ξ . Then a logarithmic analysis of the data at the equilibrium (Fig. 9) versus the reverse temperature was performed according to the following equation:

$$\ln\left(\frac{[VO_2^+]_{sat}}{[H^+]^{\circ} [VO_2^+]_{sat}}\right) \quad 0.5 \times (constant \quad ln\xi) \quad \frac{k'}{2R} \times \frac{1}{T}$$
 (12)

The linear regression analysis of the experimental results leads to the following equation $\ln\left(\frac{|VO_2^t|_{loc}}{[H^*]^3-|VO_2^t|_{soc}}\right) = 9.15 + \frac{2272}{T}$ with a correlation coefficient with the experimental results of $R^2 = 0.9997$, a satisfactory value taking into account the uncertain ties on the dependence of the activity coefficient to the concentration.

The slope of the above equation (+2272 k'/(2R)), enables to deduce k'=37.8 kJ/mol, a negative value; it could be attributed, very approximately, to the changes in the enthalpy of the reaction between H* and V_2O_5 which appears to be an exothermic process. This is also confirmed by the bibliography and particularly the studies of (Rahman and Skyllas Kazacos, 2009) which claims that the reaction (5) is an endothermic reaction. Note that, the obtained negative value is in agreement with the effect of temper ature on the saturation concentration: the saturation concentration of VO_2^+ decreases when the temperature of the stirred suspension increases.

Besides comparison of k for the vanadyl sulfate (+16.3 kJ/mol) and k' for the vanadium pentoxide (37.8 kJ/mol) enables to con clude that the dissolution of both vanadium compounds follows different schemes: the process is endothermic for the dissolution of VOSO₄ and exothermic and more 'difficult' for the breaking of the oxide bonds (V-O bond have a more covalent character than bond VO-SO₄ bond).

3.2.5. Kinetic model of the dissolution

The comparison of the dissolution of both $VOSO_4$ and V_2O_5 lead to the following conclusions:

The time required to saturate the solution with VO_2^* is in the order of "some hours" compared to a time in the order of some minutes for VO^{2*} , especially for 'low' temperature (0 °C). More over, the saturation concentration of the VO_2^* is, as function of T, much lower than the saturation concentration of VO^{2*} ;

Taking into account the fact that 5 h were required to saturate the $V^{(V)}$ solution, it can be concluded that the mass transfer is not a limiting factor of the oxide dissolution. Besides, it was shown that the observed limitation in the V_2O_5 dissolution does not come from the physical properties of the powder, nor from an eventual secondary reaction taking place on the particles' surface and blocking the main dissolution (§ 3.2.3).

Therefore, the dissolution of the $V^{(V)}$ will be assumed to be lim ited by the chemistry of the reaction (5), assumed to be a slow equi librium, of which the global rate can be expressed by the Eq. (13).

$$V_2O_{5(s)} + 2H^+ \stackrel{k_{(5)}}{\rightleftharpoons} 2VO_2^+ + H_2O$$
 (5)

$$r_{(5)} = +\frac{1}{2} \frac{d[VO_2^+]}{dt} = k_{(5)} \times \frac{N_{\sigma}^{\alpha}}{N_{\sigma}^{\beta}} \times \frac{\text{(moles of } H^+)}{V_{suspension}}^{\beta} = k_{(5)}$$

$$\times \frac{\text{(moles of } VO_2^+)}{V_{suspension}}^{\gamma}$$
(13)

(Refer to Appendix B for the detailed development of Eq. (13)) Thus, for particles 'i' having, at the time t:

 S_i as surface $N_{\sigma i}$ sites on their surface, and releasing by dissolution $2(X)_s$ moles of VO_2^*

The dissolution rate Eq. (13) can be expressed as following:

$$\mathbf{r}_{(5)S_{i}} = +\frac{1}{2} \frac{d[\mathbf{VO}_{2}^{+}]_{S_{i}}}{dt} = \frac{1}{2} \frac{d(2X)_{S_{i}}}{\mathbf{V}_{suspension} dt} \frac{d(X)_{S_{i}}}{\mathbf{V}_{suspension} dt}$$

$$\mathbf{k}_{(5)} \times \left(\frac{N_{\sigma i}}{N_{a}}\right)^{\alpha} \times \frac{\left\{\mathbf{n}^{\circ}_{H} - 2 \times (X)_{S_{i}}\right\}^{\beta}}{\mathbf{V}_{suspension}^{\beta}} = \mathbf{k}_{(-5)} \frac{\left\{2 \times (X)_{S_{i}}\right\}^{\gamma}}{\mathbf{V}_{suspension}^{\gamma}}$$
(14)

The same equation will be written three times, because for the calculation, three particle surfaces S_1 , S_2 and S_3 are considered rel atively to three particle diameters: 10, 60 and 1000 μ m according to the Fig. 8 2.

Then the resolution of each equation will provide the released moles number $(2X)_{S_1}$ of VO_2^+ , and in order to determine the global released moles number of VO_2^+ , it is necessary to sum the four individual moles numbers, i.e. $(2X)_{global} = (2X)_{S_1} + (2X)_{S_2} + (2X)_{S_3}$

On the other hand, the expression of N_{σ} , considered to be the number of available V_2O_5 sites, as a function of the particle radius R_i and the vanadium initial concentration can be written as:

$$N_{\sigma i} = \frac{N_i}{\sigma^{\circ}} \times \left(\frac{3(4\pi)^{0.5} M}{\rho}\right)^{2/3} \times \left(n^{\circ}_{V} - X_{R_i}\right)^{2/3}$$

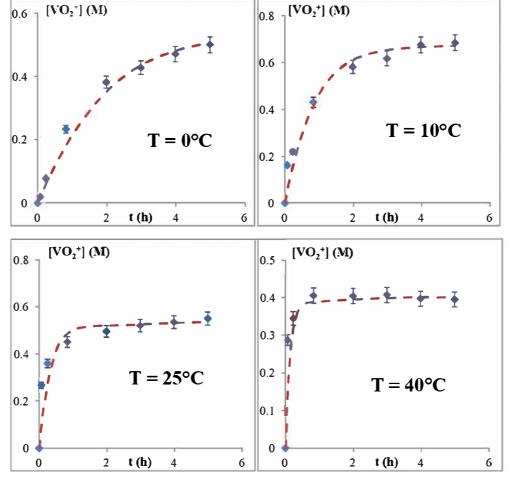


Fig. 13. Comparison between the experimental data (diamonds, imported from Fig. 9) and the model (broken lines, calculated using Eq. (15)) for the temporal evolution of the concentration of VO_2^* released by the dissolution of a V_2O_5 commercial powder, at various temperatures.

Table 1 Iteratively estimated values of the kinetic constants $k_{(5)}$ and $k_{(5)}$ for the studied temperatures, and their corresponding activation energies (estimations).

Temperature (°C)	k ₍₅₎ (mol ² s ¹ L g)	k ₍₅₎ (mol 1 s 1 L)
0	0.9×10^{-4}	2.3×10^{-4}
10	2.6×10^{-4}	3.4×10^{-4}
25	4.8×10^{-4}	13×10^{-4}
40	7×10^{-4}	41×10^{-4}
Activation energy (estimated by	Ea	Ea
$k = Ae^{Ea/RT}$	₍₅₎ = 34.5 kJ/mol	$_{(5)}$ = 52.9 kJ/mol

Substituting it in Eq. (14) and considering the reaction orders with respect to V_2O_5 , $H^{\scriptscriptstyle +}$ and $VO_2^{\scriptscriptstyle +}$, to be equal to their stoichiomet ric coefficients, the expression of global rate of the reaction is:

$$\begin{split} \boldsymbol{r}_{(5)\boldsymbol{S_{i}}} & \quad \boldsymbol{d}(\boldsymbol{X})_{\boldsymbol{S_{i}}} \\ & \quad \boldsymbol{k}_{(5)} \times \frac{\boldsymbol{N_{i}}}{\boldsymbol{N_{a}} \times \boldsymbol{\sigma}^{\circ}} \times & \quad \frac{3(4\pi)^{0.5}\boldsymbol{M}}{\boldsymbol{\rho}} \bigg)^{2/3} \\ & \quad \times \left(\boldsymbol{n}^{\circ}_{\boldsymbol{V}} \quad \boldsymbol{X_{R_{i}}}\right)^{2/3} \times \frac{\left\{\boldsymbol{n}^{\circ}_{\boldsymbol{H}} \quad 2 \times (\boldsymbol{X})_{\boldsymbol{S_{i}}}\right\}^{2}}{\boldsymbol{V}_{\boldsymbol{suspension}}} \quad \boldsymbol{k}_{(-5)} \frac{\left\{2 \times (\boldsymbol{X})_{\boldsymbol{S_{i}}}\right\}^{2}}{\boldsymbol{V}_{\boldsymbol{suspension}}} \end{split}$$

Eq. (15), solved numerically using the Euler method, provides the variation of the quantity of VO_2^+ as a function of time. The only unknown parameters are $k_{(5)}$ and $k_{(-5)}$, the kinetic constants of the forward and backward reaction. They will be adjusted in order to determine the theoretical evolution of the VO_2^+ concentration which correctly correlates with the experimental one.

Fig. 13 shows the correlation between the calculated values of dissolved VO_2^+ (broken lines) and the experimental data (dia monds). The values of the kinetic constants, enabling to get a sat isfactory agreement between theory and experiment, are indicated in Table 1.

The results show that the backward kinetic constant $k_{(5)}$ is more sensitive to the temperature than the forward $k_{(5)}$. Besides, for all the examined temperatures, $k_{(5)}$ is higher than the $k_{(5)}$. This means that the dissolution of the oxide is allowed only for 'rela tively' low concentrations of VO_2^+ , enabling to keep the term of the backward rate lower than this of the forward rate.

Note also that, because the order against the H⁺ concentration (in the forward term of the rate) is equal to 2, the acidic media is beneficial to the dissolution of the oxide and this is also in agree ment with the results of Rahman and Skyllas Kazacos (2009).

4. Conclusion

Numerous works exist in the field of the vanadium battery and one important objective is to avoid the vanadium pentoxide pre cipitation, because its dissolution seems difficult. In addition, the published studies do not exhibit the determination of the physical limitations and phenomena to be overcomed, in order to act upstream. The aim of present work was the study of the dissolution mechanisms of the vanadyl sulfate VOSO₄ and vanadium pentox ide V_2O_5 in 3 M sulfuric acid, under various operative conditions, and also to bring knowledge on the understanding of the phenom ena governing these dissolutions.

Several experimental data giving the temporal evolution of the dissolved vanadium concentrations versus various operating parameters were acquired and supplied. Moreover, kinetic laws describing both dissolution limitations phenomena were deter mined and explained. As expected these compounds exhibit differ ent behaviors towards dissolution. The general results show that the dissolution of VOSO₄ 5H₂O, an 'ionic salt', appears to be easier

and more rapid, comparatively to that of the V_2O_5 oxide (which is covalently bonded).

Their initial dissolution rate increases with temperature, for both compounds $VOSO_4$ and V_2O_5 , and the rough estimations of the activation energies at the beginning of the dissolution (18.8 kJ/mol for $VOSO_4$ and 73 kJ/mol for V_2O_5) clearly show that the tem perature influence two different phenomena: the mass transport for the vanadyl sulfate, and the reaction with the proton for the vanadium pentoxide.

The saturation concentration of the VO_2^{2+} is reached after few minutes of stirring (<10 min), while several hours (>5h) were required for the VO_2^{+} released by the oxide V_2O_5 to reach saturation (and more than 1 day at 0 °C). In addition the solubility of the $V^{(IV)}$ salt is higher than the solubility of the oxide (at least two times, even three for certain temperatures): VO^{2+} concentrations of 2 M can be achieved from the dissolution of $VOSO_4$ at $T \geq 30$ °C, while for the oxide dissolution the VO_2^{+} saturation concentration reaches \sim 0.45 M at 40 °C.

Moreover, conversely to the $V^{(IV)}$, in the case of vanadium pen toxide decreasing the temperature causes the saturation concentration of VO_2^{\star} to increase: from 0.42 to 0.78 M respectively at 40 and 0 °C, and the whole dissolution process appears to be exother mic (k' = 37.8 kJ/mol).

Concerning the kinetic models, the dissolution of VOSO₄ con sists of the dissociation in the acid media, followed by its disper sion in the bulk. The whole process is limited by mass transport (more specifically diffusion and convection). The accumulation flux of VO²⁺ was expressed using Fick's Ist law and the Sherwood corre lation and the simulated results enable to reproduce experimental measurements and to validate the mass transport limitation. For V_2O_5 , the dissolution rate appears to be limited by a chemical reaction (acidic attack followed by the breaking bonds). A simple reaction scheme was proposed for the dissolution and its rate was expressed assuming the chemical reaction as an elementary reaction. The model agrees with the experimental data and the resulting kinetic constants show a backward reaction (5) more sensitive to temperature and having a rate in certain conditions higher than the rate of the forward reaction (5).

Note that the obtained results were very sensitive to the sulfuric acid concentration which changes during the battery operation (increases during the charge and decreases during the discharge). The 3 M of sulfuric acid was chosen as a compromise between its positive effect on the dissolution of the vanadium pentoxide and its negative effect on the dissolution of vanadium sulfate.

To sum up, in the absence of chemical additives enabling to keep the $V^{(V)}$ under dissolved form and avoid precipitation of the vanadium pentoxide, it is required to operate in strong acidic con ditions, with a "discharged battery" instead of a "battery com pletely charged". Moreover, a charged vanadium battery will exhibit a more stable behavior if stored in low (T < 20 °C) temper ature conditions, rather than in high temperature conditions (T > 40 °C). Also, taking into account the results of the bibliography, it is better to avoid maintaining the battery in recharged state for a long time.

Declaration of interests

The authors declare that there is no conflict of interest.

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Appendix A

The combination of Eqs. (6) (8) enables to obtain the expres sion of $\frac{dR}{dt}$ (Eq. (9)) also noted z expressing the variation of the particles radius over time and representing the dissolution rate of the VOSO₄ 5H₂O. To reach this expression, the following calculation steps were followed:

$$Sh \quad \frac{k_{(t)} \times d_e}{D} \quad 2 + a \times Re^{\frac{1}{2}} \times Sc^{\frac{1}{3}} \rightarrow k_{(t)} \quad \frac{D}{2R} (2 + a \times Re^{\frac{1}{2}} \times Sc^{\frac{1}{3}})$$

$$\left(\frac{dm}{dt}\right)_{R\to\infty} + S \times k_{(t)} \times (C_{sat} \quad C_{bulk})$$

$$\frac{d\left(\frac{4}{3}\pi\times\frac{\rho\times N}{M}\times\left(R^{\circ^3}-R^3\right)\right)}{dt}-4\pi R^2\times\left(\frac{D}{2R}\left(2+a\times Re^{\frac{1}{2}}\times Sc^{\frac{1}{3}}\right)\right)\times$$

$$(C_{sat} \quad \frac{4}{3}\pi \times \frac{\rho \times N}{M \times V_{I}} \times (R^{\circ 3} \quad R^{3}))$$

Developing the above equation leads to:

$$\frac{-R\times dR}{dt} \quad \frac{MDC_{sat}}{\rho} \quad \frac{4}{3}\pi \frac{ND}{\rho V_I} \left(R^{\circ 3} \quad R^3\right) + \frac{aMC_{sat}}{2\rho} (2\,\varkappa)^{\frac{1}{2}} D^{\frac{2}{3}} \nu^{\left(-\frac{1}{6}\right)} R^{\frac{1}{2}}$$

$$\frac{4}{6}\pi \frac{aN}{V_{I}}(2\,\omega)^{\frac{1}{2}}D^{\frac{2}{3}}v^{\left(-\frac{1}{6}\right)}(R^{\circ 3}-R^{3})R^{\frac{1}{2}}$$

$$i \Rightarrow \frac{dR}{dt} \quad \frac{A_1 \quad A_2 \left(R^{\circ^3} \quad R^3\right) + A_3 \sqrt{R} \quad A_4 \left(R^{\circ^3} \quad R^3\right) \sqrt{R}}{R} \tag{9}$$

A ₁	A ₂	A ₃	A ₄
$\frac{M \times D \times C^{sat}}{\rho}$	$\frac{4}{3}\pi \frac{D\times N}{V_l}$	$\frac{aMC_{sat}}{2\rho} (2 \overline{u})^{\frac{1}{2}} D^{\frac{2}{3}} v^{(-\frac{1}{6})}$	$\frac{4}{6}\pi \frac{aN}{V_{i}}(2\bar{u})^{\frac{1}{2}}D^{\frac{2}{3}}v^{\left(-\frac{1}{6}\right)}$

Appendix B

$$r_{(5)} = +\frac{1}{2} \frac{d[VO_2^+]}{dt} = k_{(5)} \times (\frac{N_\sigma}{N_a})^{\alpha} \times \left(\frac{\text{moles of } H^+}{V_{suspension}}\right)^{\beta} = k_{(-5)}$$

$$\times \left(\frac{\text{moles of } VO_2^+}{V_{suspension}}\right)^{\gamma}$$

$$(13)$$

The following nomenclature will be used to treat this equation and to determine the theoretical concentration of VO₂⁺:

For the considered weight of the V_2O_5 particles having as initial diameter: 10, 60 and 1000 μm (from Fig. 8), it will be noted:

 S_1° , S_2° , and S_3° : their average initial surface.

 S_1 , S_2 and S_3 : their average surface at the time t.

 R_1° , R_2° and R_3° : their average initial radii.

 R_1 , R_2 and R_3 : their average radii at the time t.

also:

 N_1, N_2 and N_3 : are the number of particles having as initial diameter: 10, 60 and 1000 μm

 $N_{\sigma1},N_{\sigma2}$ and $N_{\sigma3}$: are the number of sites (i.e. the number of the V_2O_5 molecules) accessible to the proton H^+ , at time t for the particles having as initial diameter: 10, 60 and 1000 μ m

 σ° : is the surface occupied by one molecule of V_2O_5

N_a: Avogadro number

the exponents α , β and γ are the reaction orders, respectively for: a site constituted by V_2O_5 , H^* and VO_2^* ;

 $k_{(5)}$ and $k_{(\ 5)}$ the forward and backward kinetic constants respectively.

 N_{σ} = the number of sites accessible to H^+ , at time t = $N_{\sigma 1} + N_{\sigma 2} + N_{\sigma 3}$ surface of the particles atthetimet $\frac{\Sigma(N_j \times S_j)}{\sigma^\circ}$

in addition: " ${\pmb n}_V^\circ$ ", and " ${\pmb n}_H^\circ$ " represents respectively the initial moles number of V_2O_5 and H^+ ,

"X" the moles number of V_2O_5 dissolved at time t, by con sumption of 2X moles of

H⁺, and releasing 2X moles of VO₂⁺;

$$\mathbf{r}_{(5)\mathbf{S}_{i}} = +\frac{1}{2} \frac{d[\mathbf{VO}_{2}^{+}]_{\mathbf{S}_{i}}}{dt} = \frac{1}{2} \frac{d(2X)_{\mathbf{S}_{i}}}{\mathbf{V}_{\text{suspension}} dt} = \frac{d(X)_{\mathbf{S}_{i}}}{\mathbf{V}_{\text{suspension}}}$$

$$\mathbf{k}_{(5)} \times (\frac{N_{\sigma i}}{N_{a}})^{\alpha} \times \frac{\left\{\mathbf{n}^{\circ}_{H} - 2 \times (\mathbf{X})_{\mathbf{S}_{i}}\right\}^{\beta}}{\mathbf{V}_{\text{suspension}}^{\beta}} = \mathbf{k}_{(-5)} \frac{\left\{2 \times (\mathbf{X})_{\mathbf{S}_{i}}\right\}^{\gamma}}{\mathbf{V}_{\text{suspension}}^{\gamma}}$$

$$(14)$$

Moreover, the following changes are required in order to trans form Eq. (14) into a resolvable form:

$$N_{\sigma i} = \frac{S_i}{\sigma^{\circ}} = \frac{4\pi \times N_i}{\sigma^{\circ}} R_i^2$$
 (A)

Besides the mass of the V_2O_5 introduced into the suspension is: $m_{V_2O_5} \quad m_{R_1}+m_{R_2}+m_{R_3}$

The mass of V_2O_5 particles having R_i as diameter can be expressed by the two following equations:

 m_{R_i} Molecular weight of $V_2O_5 \times mol$ number of particles having R_i $M \times n_{VR_i}$

and
$$m_{R_i}$$
 $\rho V_{solideR_i}$ $\rho \frac{4\pi R_i^3}{3}$

Combining both equations leads to: $M \times \mathbf{n}_{VR_i} \quad \rho \frac{4\pi R_i^3}{3} \Rightarrow$

$$\mathbf{R}_{i} = \left\{ \frac{3M\mathbf{n}_{VR_{i}}}{4\pi\rho} \right\}^{\frac{1}{3}} \quad (\mathbf{B})$$

Substituting (B) into (A) gives the number of sites having, at time t, R_i as initial diameter:

$$N_{\sigma i} = \frac{4\pi \times N_i}{\sigma^{\circ}} \left(\left\{ \frac{3M \mathbf{n}_{VR_i}}{4\pi \rho} \right\}^{1/3} \right)^2 \Rightarrow N_{\sigma i} = \frac{N_i}{\sigma^{\circ}} \times \left(\frac{3(4\pi)^{0.5} M \mathbf{n}_{VR_i}}{\rho} \right)^{2/3}$$

And substituting $n_{VR_i}by(n^{\circ}_V X_{R_i})gives :\Rightarrow$

$$N_{\sigma i} \quad \frac{N_i}{\sigma^{\circ}} \times \quad \frac{3(4\pi)^{0.5}M}{\rho} \Biggr)^{2/3} \times (n^{\circ}_{V} \quad X_{R_i})^{\frac{2}{3}} \quad (C)$$

Substituting **(C)** into the expression of the rate (Eq. (14)) leads to:

$$\begin{split} \pmb{r}_{(5)S_i} & \quad \frac{d(\pmb{X})_{S_i}}{\pmb{V}_{suspension}dt} \\ & \qquad \pmb{k}_{(5)} \times \left(\frac{\pmb{N}_i}{\pmb{N}_a \times \sigma^\circ} \times \quad \frac{3(4\pi)^{0.5}\pmb{M}}{\pmb{\rho}}\right)^{2/3} \times \left(\pmb{n}^\circ_{\pmb{V}} \quad \pmb{X}_{\pmb{R}_i}\right)^{2/3} \right)^\alpha \\ & \qquad \times \frac{\left\{\pmb{n}^\circ_{\pmb{H}} \quad 2(\pmb{X})_{S_i}\right\}^\beta}{\pmb{V}^\beta_{suspension}} \quad \pmb{k}_{(-5)} \frac{\left\{2(\pmb{X})_{S_i}\right\}^\gamma}{\pmb{V}^\gamma_{suspension}} \end{split}$$

$$\begin{split} \boldsymbol{r}_{(5)\boldsymbol{S_{i}}} & \quad \boldsymbol{\frac{d(\boldsymbol{X})_{\boldsymbol{S_{i}}}}{dt}} & \quad k_{(5)} \left(\frac{N_{i}}{N_{a} \times \sigma^{\circ}} \times \frac{3(4\pi)^{0.5} M}{\rho} \right)^{2/3} \right)^{\alpha} \\ & \quad \times \left(\left(n^{\circ}_{V} - \boldsymbol{X}_{R_{i}} \right)^{2/3} \right)^{\alpha} \frac{\left\{ \boldsymbol{n}^{\circ}_{H} - 2 \times (\boldsymbol{X})_{\boldsymbol{S_{i}}} \right\}^{\beta}}{\boldsymbol{V}_{\text{suspension}}^{\beta - 1}} & \boldsymbol{k}_{(-5)} \frac{\left\{ 2 \times (\boldsymbol{X})_{\boldsymbol{S_{i}}} \right\}^{\gamma}}{\boldsymbol{V}_{\text{suspension}}^{\gamma - 1}} \end{split}$$

The size of all these equations appears to be so high!! why??? To solve this equation, the reaction orders are required and they will be assumed to be equal to the stoichiometric coefficients of each reactant, i.e. $\alpha = 1$ and $\beta = \gamma = 2$.

$$\begin{split} \mathbf{r}_{(5)S_{i}} &= \frac{d(\mathbf{X})_{S_{i}}}{dt} \\ &= \mathbf{k}_{(5)} \times \frac{\mathbf{N}_{i}}{\mathbf{N}_{a} \times \sigma^{\circ}} \times \left[\frac{3(4\pi)^{0.5}\mathbf{M}}{\rho} \right]^{2/3} \times \left(\mathbf{n}^{\circ}_{\mathbf{V}} - \mathbf{X}_{R_{i}} \right)^{2/3} \\ &\times \frac{\left\{ \mathbf{n}^{\circ}_{\mathbf{H}} - 2 \times (\mathbf{X})_{S_{i}} \right\}^{2}}{\mathbf{V}_{\text{suspension}}} - \mathbf{k}_{(-5)} \frac{\left\{ 2 \times (\mathbf{X})_{S_{i}} \right\}^{2}}{\mathbf{V}_{\text{suspension}}} \end{split} \tag{15}$$

Note that three equations must solved for the three particle sizes chosen, each one providing the mole number of VO_2^{\star} produced by the dissolution of the corresponding family of these particles as indicated in the following table.

Dissolution rate relative to the particles $r_{(5)S_1}$ $r_{(5)S_2}$ $r_{(5)S_3}$ having, at time t, an average Radii Ri (i going from 1 to 3, as defined above) the number of the particles having, at N_1 N_2 N_3 time t, an average Radii Ri The mole number of VO₂ produced by $2X_{R_1}$ $2X_{R_2}$ $2X_{R_3}$ the dissolution of the particles having, at time t, an average Radii Ri Total mole number of VO₂ produced by the dissolution of all the particles at the time t $2X \quad 2X_{R_1} + 2X_{R_2} + 2X_{R_3}$

References

- Amirante, R., Cassone, E., Distaso, E., Tamburrano, P., 2017. Overview on recent developments in energy storage: mechanical, electrochemical and hydrogen technologies. Energy Convers. Manage. 132, 372–387. doi.org/10.1016/j. enconman.2016.11.046.
- Ashby, M.F., Polyblank, J., first published January 2012. Materials for Energy Storage Systems – A White Paper. University of Cambridge. Materials for Energy Storage Systems, Granta Teaching Ressources, Version 2.0.
- Baes, C.F., Mesmer, R.S., 1976. The Hydrolysis of Cations. Wiley, New York.
- Brooker, R.P., Bell, C.J., Bonville, L.J., Kunz, H.R., Fenton, J.M., 2015. Determining vanadium concentrations using the UV-Vis response method. J. Electrochem. Soc. 162 (4), A608–A613. https://doi.org/10.1149/2.0371504jes.
- Cheng, M., 1991. Electrolyte Optimization and Studies for the Vanadium Redox Flow Battery. Master Thesis. University of New South Wales, Australia.
- Choi, Nak Heon, Kwon, Soon-kwan, Kim, Hansung, 2013. Analysis of the oxidation of the V(II) by dissolved oxygen using UV-Visible spectrophotometry in a Vanadium Redox Flow Battery. J. Electrochem. Soc. 160, A973–A979. https:// doi.org/10.1149/2.145306jes.
- Choi, Chanyong, Kim, Soohyun, Kim, Riyul, Choi, Yunsuk, Kim, Soowhan, Jung, Hoyoung, Hoon Yang, Jung, Kim, Hee-Tak, 2017. A review of vanadium electrolytes for vanadium redox flow batteries. Renew. Sustain. Energy Rev. 69, 263–274. https://doi.org/10.1016/j.rser.2016.11.188.
- Crans, D.C., Smee, J.J., Gaidamauskas, E., Yang, L., 2004. The chemistry and biochemistry of vanadium and the biological activities exerted by vanadium compounds. Chem. Rev. 104, 849–902. https://doi.org/10.1021/cr020607t.
- Cunha, Á., Martins, J., Rodrigues, N., Brito, F.P., 2015. Vanadium redox flow batteries: a technology review. Int. J. Energy Res. 39, 889–918. https://doi.org/10.1002/er.3260.
- Cussler, E.L., 1984. Diffusion Mass Transfer in Fluid Systems, third ed., Cambridge. Ding, Y., Chen, H., Cong, T.N., Yang, W., Tan, C., Li, Y., 2009. Progress in electrical energy storage system: a critical review. Prog. Nat. Sci. 19, 291–312. https://doi.org/10.1016/j.pnsc.2008.07.014.
- Elvingson, K., Keramidas, A.D., Crans, D.C., Pettersson, L., 1998. Speciation in vanadium bioinorganic systems. 5. Interactions between vanadate, uridine, and imidazoles an aqueous potentiometric, 51V, 17O, and 13C NMR study. Inorg. Chem. 37 (24), 6153–6160. https://doi.org/10.1021/ic9712333.
- Fassulo, O.T., 1965. Sulfuric Acid; Use and Handling. McGraw-Hill, University of Minnesota - New York.

- Fu, Q., Sun, W., 2001. Mie theory for light scattering by a spherical particle in an absorbing medium. Appl. Opt. 40 (9), 1354–1361. doi.org/10.1364/ AO.40.001354.
- Guzman, J., Saucedo, I., Navarro, R., Revilla, J., Guibal, E., 2002. Vanadium interactions with chitosan: influence of polymer protonation and metal speciation. Langmuir 18 (5), 1567–1573. https://doi.org/10.1021/la010802n.
- Ivakin, A.A., Voronova, E.M., 1973. A spectrophotometric study of vanadium (IV) sulfate complexes. Russ. J. Inorg. Chem. 18 (7), 956.
- Jiang, Z., Klyukin, K., Alexandrov, V., 2016. Structure, hydrolysis, and diffusion of aqueous vanadium ions from Car-Parrinello molecular dynamics. J. Chem. Phys. 145, 114303. doi.org/10.1063/1.4962748.
- Kausar, N., 2002. Studies of V(IV) and V(V) species in vanadium cell electrolyte. April 2002, A thesis submitted as part of the requirements for the degree of Doctor of Philosophy (Ph.D) M.Sc (Chemistry), University of New South Wales, Sydney 2052, Australia.
- Le Flem, G., 1964. Le système V205 ThO2. Faculté des Sciences de l'Université de Bordeaux.
- Leung, P., Li, X., Ponce-de-León, C., Berlouis, L., John-Low, C.T., Walsh, F.C., 2012. Progress in redox flow batteries, remaining challenges and their applications in energy storage. RSC 2, 10125–10156. https://doi.org/10.1039/c2ra21342g.
- Li, L., Kim, S., Wang, W., Vijayakumar, M., Nie, Z., Cheng, B., Zhang, J., Xia, G., Hu, J., Graff, G., Liu, J., Yang, Z., 2011. A Stable Vanadium Redox Flow Battery with High Energy Density for Large Scale Energy Storage. Adv. Energy Mater. 1, 394–400. https://doi.org/10.1002/aenm.201100008.
- Post, K., Robins, R.G., 1976. Thermodynamic diagrams for the vanadium-water system at 298.15K. Electrochim. Acta 21 (6), 401–405. https://doi.org/10.1016/ 0013-4686(76)85115-8.
- Rahman, F., 1998. Stability and Properties of Supersaturated Vanadium Electrolytes
 For High Energy Density Vanadium Redox Battery PhD Thesis. University of
 New South Wales, Australia.
- Rahman, F., Skyllas-Kazacos, M., 1998. Solubility of vanadyl sulfate in concentrated sulfuric acid solutions. J. Power Sources 72 (2), 105–110. doi.org/10.1016/S0378-7753(97)02692-X.
- Rahman, F., Skyllas-Kazacos, M., 2009. Vanadium redox battery: positive half-cell electrolyte studies. J. Power Sources 189 (2), 1212–1219. https://doi.org/10.1016/j.jpowsour.2008.12.113.
- Rychcik, M., Skyllas-Kazacos, M., 1988. Characteristics of a new all-vanadium redox flow battery. J. Power Sources 22 (1), 59–67. 10.1016/0378-7753(88)80005-3.
- Selbin, J., 1965. The chemistry of oxovanadium (IV). Chem. Rev. 65 (2), 153–175. https://doi.org/10.1021/cr60234a001.
- Skyllas-Kazacos, M., Rychick, M., Robins, R., 1988. All-vanadium redox battery. US4786567.
- Skyllas-Kazacos, M., Cao, L., Kazacos, M., Kausar, N., Mousa, A., 2016. Vanadium electrolyte studies for the vanadium redox battery—a review 9(13), 1521–1543. doi.org/10.1002/cssc.201600102.
- Skyllas-Kazacos, M., Kim, K.J., Park, M.S., Kim, Y.J., Kim, J.H., Dou, S.X., 2015. A technology review of electrodes and reaction mechanisms in vanadium redox flow batteries. J. Mater. Chem. A 3, 16913–16933. https://doi.org/10.1039/ C5TA026131.
- Skyllas-Kazacos, M., Milne, N.A., Kazacos, G.C., 2007. Membrane properties and behaviour in the Generation 2 Vanadium Bromide Redox Flow batteries. Mater. Forum 32, 72–77.
- Skyllas-Kazacos, M., Parasuraman, A., Lim, T.M., Menictas, C., 2013. Review of material research and development for vanadium redox flow battery applications. Electrochim. Acta 101, 27–40. doi.org/10.1016/ j.electacta.2012.09.067.
- Sum, E., Rychick, M., Skyllas-Kazacos, M., 1985. Investigation of the V(V)/V(IV) system for use in the positive half-cell of a redox battery. J. Power Sources 16 (2), 85–95. https://doi.org/10.1016/0378-7753(85)80082-3.
- Sum, E., Skyllas-Kazacos, M., 1985. A study of the V(II)/V(III) redox couple for redox flow cell applications. J. Power Sources 15 (2), 179–190. https://doi.org/10.1016/0378-7753(85)80071-9.
- Thaller, L.H., 1974. Electrically rechargeable redox flow cells. Bibliographic Code: 1974iece.conf.924T. Published. In: Intersociety Energy Conversion Engineering Conference, 9th, San Francisco, Calif., August 26–30, 1974, Proceedings. (A75–10476 01–44) New York, American Society of Mechanical Engineers, p. 924–928
- Thaller, L.H., Jan. 01, 1977. Redox flow cell development and demonstration project. NASA Tech. Memo.-79067; Document ID: 19790016274; Accession Number: 79N24445.
- Vijayakumar, M., Li, Liyu, Graff, Gordon, Liu, Jun, Zhang, Huamin, Yang, Zhenguo, Hu, Jian Zhi, 2011. Towards understanding the poor thermal stability of V5+ electrolyte solution in Vanadium Redox Flow Batteries. J. Power Sources 196 (7), 3669–3672. https://doi.org/10.1016/j.jpowsour.2010.11.126.
- Vijayakumar, M., Wang, W., Nie, Z., Sprenkle, V., Hu, J., 2013. Elucidating the higher stability of vanadium(V) cations in mixed acid based redox flow battery electrolytes. J. Power Sources 241, 173–177. https://doi.org/10.1016/j.ipowsour.2013.04.072.
- Wallace, R.M., 1966. Determination of the second dissociation constant in sulfuric acid by Donnan Membrane Equilibrium. J. Phys. Chem. 70 (12), 3922–3927. https://doi.org/10.1021/j100884a029.
- Wang, W., Luo, Q., Li, B., Wei, X., Li, L., Yang, Z., 2013. Recent progress in redox flow battery research and development. Adv. Funct. Mater. 23 (8), 970–986. https:// doi.org/10.1002/adfm.201200694.