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Piezomagnetic behavior: experimental approach and multiscale modeling

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Abstract:

This work deals with the study of magnetoelastic coupling in the framework of non-destructive testing. Experimental hysteretic and cyclic piezomagnetic measurements carried out on a dual-phase steel submitted to different magnetic field and stress conditions are reported. The effect of concomitant magnetic field and stress, considering static or variable amplitudes, is discussed. A new multiscale modeling of piezomagnetic hysteresis is finally proposed.

Keywords: Magnetic and Piezomagnetic hysteresis, magnetoelastic coupling, multiscale modeling

1 Introduction

The submission of a ferromagnetic material to a magnetic field leads to a geometric distortion of the sample. This deformation is called the magnetostriction strain. Conversely, the application of an external mechanical stress to a ferromagnetic material, initially magnetized even faintly, leads to a significant change of magnetization. These behaviors are symptomatic of the same coupling called the *piezomagnetic* or Villari effect [1]. Indeed mechanical stress is one of the three major factors that can affect the magnetization in addition to magnetic field and temperature. The magnetic behavior is thus sensitive to any mechanical loading and its evolution will be different depending on the loading level, direction and nature [2]. Since then, numerous works have been initiated to understand, model and use this coupling effect in industrial applications such as on Non-Destructive Testing (NDT). We can cite for example: magnetic particle inspection (MPI), Eddy currents, Barkhausen noise... etc. The purpose of all these magnetic methods is to extract information about the metallurgical and mechanical states of a material by analyzing the electromagnetic signal [3].

Piezomagnetic control methods have undergone recent developments [4] [5] but still face modeling issues, especially when no controlled magnetic field is applied [6]. The development, the implementation and the generalization of such techniques involve, in one hand, the establishment of experiments to highlight the magnetoelastic coupling in a controlled framework, and on the other hand, the development of innovative modeling methods. Both aspects are addressed in this paper. The measurements presented are related to the hysteretic and cyclic piezomagnetic behavior [7] of a dual-phase steel submitted to

various magnetic field and stress conditions. After describing a multiscale approach of magneto-elastic couplings in a reversible framework and of associated magnetic hysteresis model, we then propose a new modeling of piezomagnetic hysteresis behavior.

2 Material and procedure

2.1 Material

The material used for the experiments is a dual-phase low carbon steel (DPS780 from ArcelorMittal). Its microstructure consists of about 30%vol. of hard (mechanically) martensite islands dispersed in a soft (ductile) ferritic matrix. From a magnetic consideration the material can be considered as 70%-pure iron as a first approximation since martensite exhibits a susceptibility much lower than the susceptibility of ferrite. Its contribution is neglected for the modeling. This material has been the subject of several studies in particular in the context of the link between mechanical state and magnetic behavior [8, 9].

2.2 Set up and experiments

Samples consist in 200 mm long, 12.5 mm wide and 1.6 mm thick strips (figure 1) suitable for the experimental set-up used for experiments.

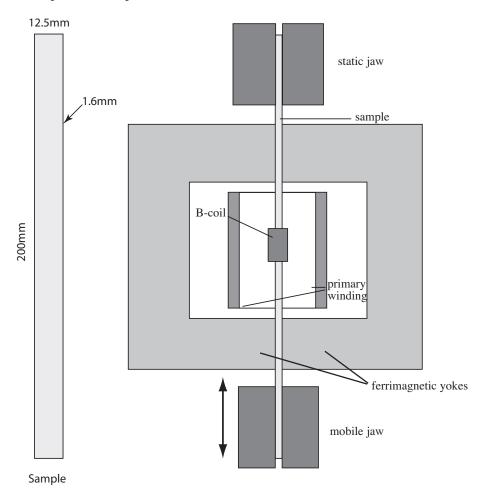


FIGURE 1 – Sample geometry and experimental set up.

Two different experiments have been carried out in this study: hysteretic measurements under static

mechanical stress and piezomagnetic measurements under cyclic mechanical stress. For both tests, the same experimental apparatus has been used as sketched in figure 1 (details concerning the experimental apparatus can be found in [4] and [5]). The sample is placed between two "U" ferrite yokes allowing the re-close of the magnetic flux. The excitation field is applied by the primary winding formed of N=81 turns and fed by an electrical current of intensity i(t). The magnetic flux in the sample is estimated by integrating the induced voltage at the terminals of a B-coil, formed of n=700 turns. The measurement of the magnetic flux in the sample allows the induction B, then the magnetization M to be calculated. The set-up is mounted inside an electro-hydraulic MTS machine, applying from compressive to tensile stresses. The set-up allows the study of magnetic behavior of the material under stress. A LabView system allows the simultaneous acquisition and recording of the different quantities of interest (force, displacement, applied current and induced voltage).

The first part of the work consists in measuring the magnetic hysteresis behavior of the material under static uniaxial stress. The magnetic cycles are produced by applying a triangular current intensity (allowing a constant magnetic field rate). Test parameters are the mean magnetic field (H_m =0A/m), the frequency f_{mag} (0.1Hz), the magnetic amplitude ΔH (850A/m, 1700A/m, 3400A/m, 8500A/m, 15000A/m) and the static stress value σ_{stat} (from -100MPa to 300MPa). The procedure is composed of the following steps: 1- Application of the mechanical loading σ_{stat} ; 2- Demagnetizating by applying a decreasing amplitude sinusoidal current; 3- Application of magnetic field H(t) and measurement of induced voltage; 4- Recording of measurements.

The second part of this work consists to measure the piezomagnetic behavior of the material under different levels of the static magnetic field H_{stat} (850A/m, 1700A/m, 3400A/m, 8500A/m, 15000A/m). A sinusoidal stress waveform has been used for mechanical loading. Test parameters are the mean stress σ_m (from -50MPa to 300MPa), the stress amplitude $\Delta\sigma$ (from 50MPa to 200MPa) and the frequency of loading f_{mec} (0.5Hz). The mechanical loading is chosen in the range [-100MPa 300MPa] in order to avoid the sample yielding and buckling. The procedure is composed of the following steps: 1- Cyclic mechanical loading of amplitude $\Delta\sigma$; 2- Application of the static magnetic field after demagnetizing; 3- Measurement and averaging over 50 cycles after stabilization of induced voltage; 4- Recording of the measurements.

3 Experimental results

3.1 Magnetic hysteresis

When the material is submitted to an alternative magnetic field, the magnetization forms an hysteresis loop illustrating the irreversibility of the magnetic behavior and the presence of dissipative phenomena. Figure 2 depicts the evolution of the magnetic hysteresis loop at different magnetic field levels for σ_{stat} = 0MPa. The cycles are nested inside each other. It can be noticed that the evolution of the shape of the hysteresis cycles is highly dependent on the magnetic field level. Indeed, we can see that the maximal dM/dH slope and the cycle area increase with increasing amplitude of the magnetic field. It can be noticed also that magnetization saturation is not far to be reached for loop obtained at the highest magnetic field strength. Its level remains however lower than the theoretical saturation of pure iron $(1.71 \times 10^6 \text{ A/m})$ due to the martensite ratio and various demagnetizing effects.

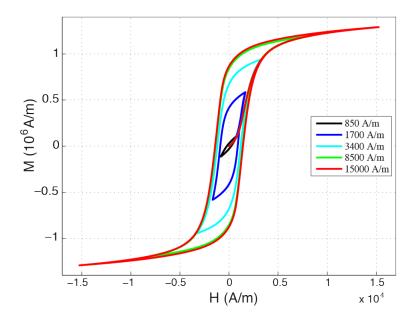


FIGURE 2 – Experimental results : Magnetic hysteresis at increasing magnetic field levels without applied stress - $M = f(H, \sigma = 0 \text{MPa})$.

Magnetic measurements reported in figure 3 represent the hysteretic cycles under uniaxial stress. Measurements lead to conventional results for low carbon steel: global degradation of magnetization due to compressive stress at a given magnetic field (decrease of magnetic susceptibility), improvement due to tensile stress and Villari reversal effect [9]. The Villari reversal is associated with the change of $dM/d\sigma|_H$ sign: at weak and intermediate magnetic field, the ratio $dM/d\sigma|_H$ is positive. It becomes negative at higher magnetic field leading to a change of sign of $dM/d\sigma|_H$ (becoming negative and corresponding to the *reversal* point). A higher stress level progressively shifts the Villari reversal point to the lower magnetic field values. It can be noticed that the Villari reversal can be related to the change of sign of the magnetostriction vs. magnetic field behavior [13].

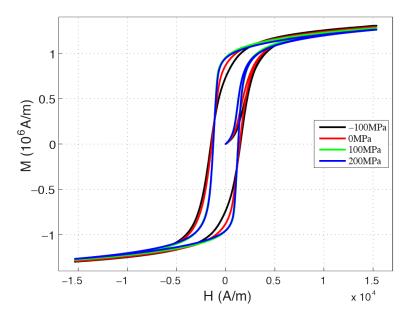


FIGURE 3 – Experimental results : hysteretic cycles under different mechanical loading conditions – $M = f(H, \sigma = \text{cte})$.

3.2 Piezomagnetic hysteresis

Figure 4 shows the magnetic response associated with the variation of stress (σ_m =100MPa, $\Delta\sigma$ =200MPa, f $_{mec}$ =0.5Hz) for H_{stat} =(850A/m, 1700A/m,3400A/m, 8500A/m, 15000A/m). In order to facilitate the comparison of the experimental and numerical results, we considered the magnetic state at 300MPa as a reference state for magnetization. As shown in figure 4, the piezomagnetic cycles are not symmetric and non-monotonous: positive stress leads to quasi-reversible situation and negative stress increases the cycle area. Again, for a weak to intermediate magnetic field, instantaneous slope $dM/d\sigma|_H$ is practically positive for compressive to weak tensile stress. The sign reversal of $dM/d\sigma|_H$ occurs for stress levels varying from 70MPa to 230MPa depending on position on the cycle. At higher magnetic field strength, reversal clearly occurs at lower stress. High magnetic fields (H \geq 4kA/m) lead to a negative and quasi constant slope. Moreover the piezomagnetic behavior becomes quasi-reversible. This result is interesting if a sensor application is looked for. Indeed, the applied mechanical stress could be estimated by only measuring the magnetization of material (and knowing a reference point).

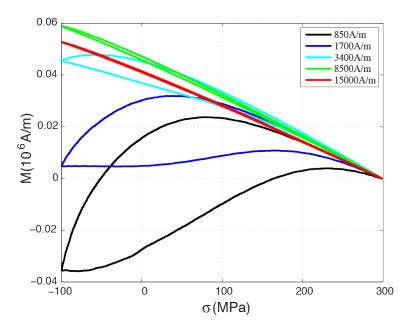


FIGURE 4 – Experimental results : piezomagnetic behavior obtained under cyclic stress conditions and at different magnetic field levels - $M = f(H = \text{cte}, \sigma)$.

4 Multiscale modeling

The model is derived from a description of reversible magneto-elastic behavior [11][13] extended recently to magnetic hysteresis [12]. This description relies on the definition of the material Gibbs free energy at the magnetic domain scale and the estimation of the domains volume fractions using a *at equilibrium* stochastic approach at the grain scale. Some scale transition rules are used to define the behavior at the polycrystalline scale considered as the representative volume element (*RVE*).

4.1 Gibbs free energy and reversible modeling

The Gibbs free energy density is written at the magnetic domain scale α . The reader can find in [13] complete and comprehensive explanation and hypotheses about the construct of this energy functional. Indeed at the domain scale, both magnetization \vec{M}_{α} and magnetostriction strain ϵ^{μ}_{α} (seen as a free deformation tensor) can be considered as homogeneous. The norm of \vec{M}_{α} is the saturation magnetization M_s as a first constant of the model (see equation (1), where γ_k are the direction cosines of magnetization vector and \vec{e}_k are the unit vectors of the crystallographic frame). In the framework of linear magnetoelastic coupling, ϵ^{μ}_{α} is stress independent and isochorus, given by equation (2), where λ_{100} and λ_{111} are two other constants measuring the saturation deformation along < 100 > and < 111 > crystallographic directions respectively. Moreover in the framework of this paper and for the seek of simplicity, stress σ and magnetic field \vec{H} are considered homogeneous over the RVE (avoiding any complex rules for localization or homogenization).

$$\vec{M}_{\alpha} = M_s \, \gamma_k . \vec{e_k} \tag{1}$$

$$\epsilon_{\alpha}^{\mu} = \frac{3}{2} \begin{pmatrix} \lambda_{100} (\gamma_1^2 - \frac{1}{3}) & \lambda_{111} \gamma_1 \gamma_2 & \lambda_{111} \gamma_1 \gamma_3 \\ \lambda_{111} \gamma_1 \gamma_2 & \lambda_{100} (\gamma_2^2 - \frac{1}{3}) & \lambda_{111} \gamma_2 \gamma_3 \\ \lambda_{111} \gamma_1 \gamma_3 & \lambda_{111} \gamma_2 \gamma_3 & \lambda_{100} (\gamma_3^2 - \frac{1}{3}) \end{pmatrix}$$
 (2)

Following these simplifications, the Gibbs free energy density at the magnetic domain scale is simply expressed as:

$$q_{\alpha}(\vec{H}, \boldsymbol{\sigma}) = K_1(\gamma_1^2 \gamma_2^2 + \gamma_2^2 \gamma_3^2 + \gamma_3^2 \gamma_1^2) - \mu_0 \vec{H} \cdot \vec{M}_{\alpha} - \boldsymbol{\sigma} : \boldsymbol{\epsilon}_{\alpha}^{\mu}$$
(3)

 μ_0 is the vacuum magnetic permeability. Term $K_1(\gamma_1^2\gamma_2^2+\gamma_2^2\gamma_3^2+\gamma_1^2\gamma_3^2)$ is the magnetocrystalline energy density with K_1 a magnetocrystalline constant. This non-convex term allows the so-called *easy* magnetization directions (six < 100 > directions for iron and iron alloys) to be defined. These directions define the number of domains (or *domain families i*) that can be seen as crystallographic variants. Calculation of magnetic domains volume fraction is made possible by using a *at equilibrium* stochastic approach, which neglects the transition zones (domain walls) between domains. This calculation is complemented by a minimization process of g_i regarding the direction cosines of domain families i to take the so-called magnetization rotation mechanism into account. Following this strategy, a Boltzmann function gives the solution of the stochastic approach [14] (with V_0 a reference microscopic volume, k the Boltzmann constant $(1.38 \times 10^{-23} \text{J.K}^{-1})$ and T the temperature (293K)).

$$f_i = \frac{\exp\left(-\frac{V_0}{kT}g_i\right)}{\sum_{i=1}^6 \exp\left(-\frac{V_0}{kT}g_i\right)} \tag{4}$$

$$\vec{\gamma}_i = \min(g_i(\vec{\gamma}, \vec{H}, \boldsymbol{\sigma})) \tag{5}$$

Averaging operations end the process as expressed in equation (6) and (7), with N_g the number of grains g involved in the process (a discrete orientation distribution function - ODF- extracted from Electron Back-Scattered Diffraction - EBSD- measurement is used).

$$\vec{M} = \frac{1}{N_g} \sum_{g} (\sum_{i=1}^{6} f_i \vec{M}_i) \tag{6}$$

$$\epsilon^{\mu} = \frac{1}{N_g} \sum_{g} \left(\sum_{i=1}^{6} f_i \epsilon_i^{\mu} \right) \tag{7}$$

Both stress and magnetic field variations are the possible loadings of the problem. A cyclic magnetic field at constant stress leads to magnetic and field-induced magnetostriction behaviors at constant stress. A cyclic stress at constant magnetic field leads to the piezomagnetic and stress-induced magnetostriction behaviors at constant magnetic field.

4.2 Irreversible modeling - application of Hauser's modeling to Piezomagnetic cycle

The multiscale approach is by definition anhysteretic, meaning that it is restricted to the reversible part of magneto-elastic behavior. It has been proposed in [12] to introduce hysteresis effects in the multiscale

model in terms of irreversible magnetic field. The dissipation is introduced (initially in the single crystal model) by adding an irreversible contribution H_{irr} to the anhysteretic magnetic field H (considered as the *reversible* magnetic field H_{rev}). The definition of H_{irr} is based on the works by Hauser [10], extended to magneto-mechanical loadings.

The Hauser's model predicts the magnetic state of the ferromagnetic material by minimizing the overall energy state of the system. This approach is based on a physical and probabilistic description of the volume distribution of the magnetic domain families. The dissipative behavior results from the probability of encountering a defect during the displacement of magnetic walls separating the magnetic domains. The expression of the irreversible energy is a decreasing exponential function which depends on the variations of the anhysteretic volume fraction. It reflects the fact that a wall has a lower probability of being pinned to a defect, when it is away from it. Hauser has often simplified this development by studying a load applied along an easy magnetization axis of the material and considering quantities as isotropic and at the macroscopic scale. Following these simplifications, equation (8) gives the expression of H_{irr} retained for this work.

$$H_{irr} = \delta(H_c + a|H_{rev}|) \left[1 - \kappa \exp(-\frac{k_a}{\kappa}|M - M_{prev}|)\right]$$
(8)

where

$$\kappa = 2 - \kappa_0 \exp\left(-\frac{k_a}{\kappa_0}|M - M_{prev}|\right) \tag{9}$$

 H_{irr} is assumed to be parallel to H and H_{rev} , since $H=H_{rev}+H_{irr}$. Hysteresis is restricted to magnetic field amplitude effects, rotational effects cannot be modeled. δ is equal to ± 1 , depending on the loading direction. The sign of δ starts as positive and is then changed at each inversion in loading direction. H_c denotes the coercive field of the material (magnetic field required to annul the remnant magnetization for a major cycle). a, k_a and κ are material parameters. a controls the first magnetization behavior, and k_a and κ the width and inclination of the hysteresis cycle. The value of κ changes each time there is an inversion in the loading direction. The new κ value is calculated from the previous value κ_0 according to equation (9). The initial κ value is a material constant. M_{prev} is the value of magnetization M at the previous inversion of the loading direction. In the case of a purely magnetic loading, an inversion of loading direction is defined as a change of sign for the time derivative of the applied magnetic field.

Extension of this model to stress loading is key once a piezomagnetic cycle is expected to be modeled. It must be recalled that the expression from Hauser comes from an observation and calculation of the energy dissipated by the pinning mechanisms and by the wall jumps. It depends only on the path made by the walls and does not depend on the whether the walls movement is generated by the application of a magnetic field or a mechanical stress. Indeed the intrinsic dissipation part of Clausius-Duhem inequality can be built at the macroscale using irreversible magnetic field or irreversible stress following:

$$\mu_0 \, \dot{\vec{M}}. \vec{H}_{irr} + \dot{\boldsymbol{\epsilon}}_{\mu}. \boldsymbol{\sigma}_{irr} \ge 0 \tag{10}$$

It is possible to propose a dissipation pseudo-potential Φ (convex and positive) so that, for a step-time

dt and considering a monotonous evolution of magnetization (by part) in uniaxial condition, one gets:

$$H_{irr} = \frac{d\Phi}{\mu_0 dM} dt \tag{11}$$

The definition of H_{irr} given by Hauser allows an appropriate definition of dissipation pseudo-potential Φ . The same comment can be made for irreversible stress. Considering a monotonous evolution of magnetostriction deformation in uniaxial condition, one gets:

$$\sigma_{irr} = \frac{d\Phi}{d\epsilon_{\mu}} dt \tag{12}$$

The definition of an *irreversible stress* directly inspired form the irreversible magnetic field definition can be proposed, restricted to 1D loading;

$$\sigma = \sigma_{rev} + \sigma_{irr} \tag{13}$$

with σ_{rev} the *reversible* stress leading to the at equilibrium magnetization using the multiscale model. σ_{irr} is given by :

$$\sigma_{irr} = \delta(\sigma_C + a'|\sigma_{rev}|) \left[1 - \kappa' exp(-\frac{k'_a}{\kappa'}|\epsilon^{\mu} - \epsilon^{\mu}_{prev}|) \right]$$
 (14)

and

$$\kappa' = 2 - \kappa_0' \exp\left(-\frac{k_a'}{\kappa_0'} |\epsilon^{\mu} - \epsilon_{prev}^{\mu}|\right)$$
 (15)

These equations define four more material coefficients: a coercive stress σ_c , and parameters a', k'_a and κ'_0 . a' controls the first stress-induced magnetostriction behavior, and k'_a and κ' the width and inclination of the stress-induced magnetostriction hysteresis cycle. An inversion of loading direction (leading to a change of the sign of parameter δ) is defined as a change of sign for the time derivative of the applied stress. Figure 5 illustrates the dissipation pseudo-potential for magnetization Φ_M at constant stress and for stress Φ_σ at constant magnetic field during the transient first loading (first magnetization and first stress) and cycles (one curve per branch) for the parameters reported in tables 1 and 2 (but considering parameters a and a' at zero). It exhibits the appropriate properties (positive and convex).

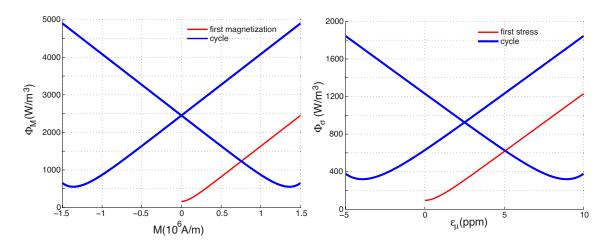


FIGURE 5 – Illustration of dissipation pseudo-potential for magnetization Φ_M at constant stress and for stress Φ_{σ} at constant magnetic field during the transient first loading and the cycle.

However, it must be underlined that the stress-induced magnetostriction cycle (stress vs magnetostriction) can hardly be obtained experimentally. The more relevant indicator of the effect of a variable stress is of course the piezomagnetic cycle. Comparisons of experimental and modeled piezomagnetic cycles are possible thanks to the definition of irreversible stress. They can help to adjust the modeling parameters. It must be underlined on the other hand that following the previous remarks and discussion, a piezomagnetic cycle is not representative of an energy dissipation, unlike a magnetostriction vs. stress cycle.

5 Modeling results and discussion

5.1 Numerical parameters used for modeling

Physical constants of pure iron have been used for the anhysteretic parameters. They are reported in table 1. An orientation data file made of 440 orientations has been used to model the RVE. Related pole figures are plotted in figure 6. Table 2 gathers parameters used to model the irreversible magnetic field and stress, that fit properly the experimental results, but without numerical optimization (improvements are possible).

Table 1 – Parameters used in the multiscale modeling - anhysteretic behavior

Parameter	M_s	K_1	λ_{100} ; λ_{111}	V_0
Value	1.71×10^6	48	21.5; -21.5	81
Unit	A/m	kJ/m ³	ppm	$\mu\mathrm{m}^3$

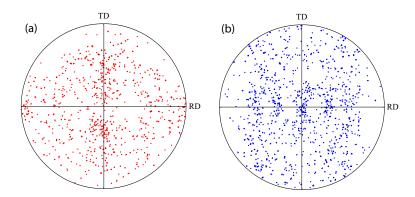


FIGURE 6 – Poles figures of the material : a) < 100 > poles ; b) < 111 > poles. RD : rolling direction ; TD : transverse direction.

Table 2 – Parameters used in the multiscale modeling - cyclic magnetic and cyclic piezomagnetic behaviors

Parameter	H_c	a	k_a	κ_0	σ_c	a'	k_a'	κ_0'
Value	1300	0.1	1×10^{-5}	1	123	0.0	1.3×10^{6}	1
Unit	A/m	-	$m.A^{-1}$	-	MPa	-	-	-

It must be noticed that an energy equivalence allows the coercive stress to be theoretically related to the coercive field, using an equivalence in energy, following:

$$\sigma_c \approx H_c \frac{5\mu_0 M_s}{2\lambda_{100}} \tag{16}$$

In order to adjust the numerical results to fit the experimental measurements, we chose σ_c =123 MPa instead of 332 MPa given by this equation.

5.2 Magnetic hysteresis

In this section the multiscale model is applied to describe the magnetic hysteresis behavior of the dual-phase steel. As a first step, the material is supposed to have the same magnetic behavior as pure iron. Figure 7 reports the hysteretic cycles at the unloaded state for different magnetic field levels used for experiments (Figure 2). In the other hand, the major hysteresis loops at the unloaded state and under -100 MPa, 100 MPa and 200 MPa are plotted in figure 8 (to be compared with results plotted in figure 3). The general trends are correctly met. The effect of tensile and compressive uniaxial stress on the material magnetization are properly rendered. Both experimental and numerical results show that for low levels of magnetic field, a tensile stress increases the magnetic susceptibility represented by $dM/dH|_{\sigma}$ slope, whereas a compression decreases it. This effect is inverse at high magnetic field levels by Villari effect, and the modeling reproduces it fairly. A cycle-to-cycle comparison is however not possible without taking into account the effective quantity of magnetic material.

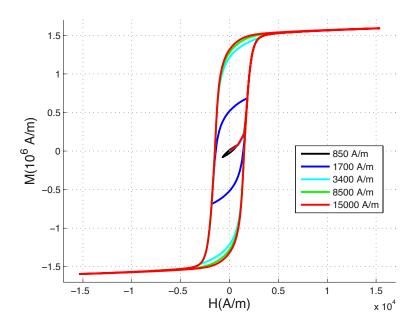


Figure 7 – Modeling results : evolution of the hysteretic cycles with the applied magnetic field $M=f(H,\sigma=0MPa)$.

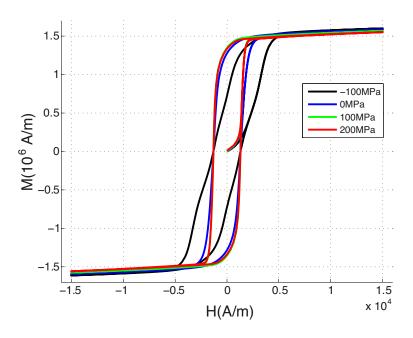


Figure 8 – Modeling results : hysteretic cycles under different mechanical loading conditions $M=f(H,\sigma^{cte})$.

5.3 Piezomagnetic hysteresis

As explained in section 4.2, the modeling of the piezomagnetic behavior proposed in this work is inspired from the description of the hysteretic irreversibility given by the Hauser's model. The definition of the irreversible stress allows the modeling of the stress-induced magnetostriction. Figure 9 represents this

cycle, representative of a mechanical dissipation ¹. This cycle, drawn for pure iron, can be hardly obtained experimentally because magnetostrictive deformations are very low compared to elastic deformation.

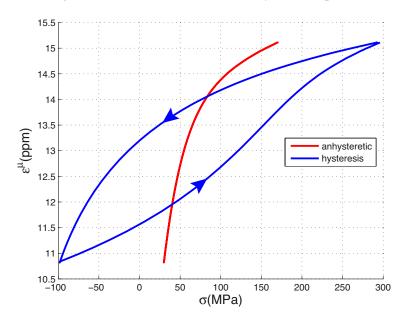


Figure 9 – Modeling results: stress-induced magnetostriction vs. stress cycle.

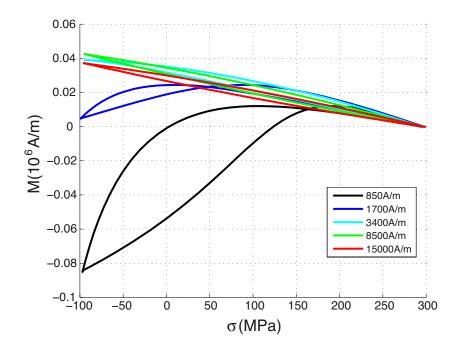


FIGURE 10 – Modeling results : evolution of the piezomagnetic cycles with the magnetic field level $M = f(H = \text{cte}, \sigma)$.

Thanks to this modeling strategy we succeed to reproduce piezomagnetic irreversibility. The piezomagnetic cycles are calculated for different magnetic field levels H_{stat} (850 A/m, 1700 A/m, 3400 A/m, 8500 A/m, 15000 A/m) by plotting the magnetization as function of *total* stress ($\sigma = \sigma_{rev} + \sigma_{irr}$) as

^{1.} The dissipation can be estimated at 320 J/m^3 per cycle. This value is much lower than the dissipation measured during a magnetic cycle that is about 9300 J/m^3 for a major cycle.

shown in figure 10. This result is given for pure iron. The mechanical loading used for modeling is a triangular stress waveform with a frequency of f_{mec} =0.5 Hz. The mechanical loading amplitude is not perfectly mastered since the component σ_{irr} changes its value at each step of calculation. The cycles reproduced by the model show less variations and new phenomena such as the presence of cross points close to the Villari reversal points (figure 10), which has been observed for other steels [5]. Nevertheless, a good general agreement with the experimental observations is obtained. For comparison of magnetization levels, the volume fraction of effective ferromagnetic material must be taken into account.

5.4 Comparison between experimental measurements and modeling results

The material is supposed to be composed of about 70%-pure ferrite and that martensite brings non magnetic contribution to the magnetization. Figure 11 shows a comparison between the experimental and modeled magnetic behavior of the material under uniaxial stress (0 MPa, +100 MPa and -100MPa). A good general agreement is observed. The model tends to underestimate the magnetization of the material for a given magnetic field, especially at the magnetic saturation. Contribution of martensite is probably missing.

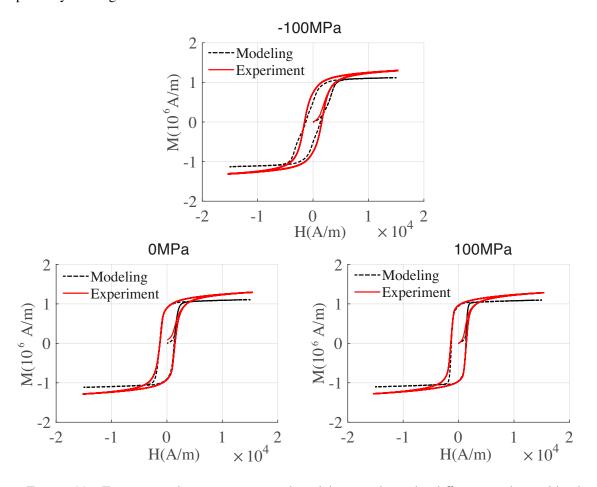


Figure 11 – Experimental measurements and modeling results under different mechanical loading.

Figure 12 presents the measured and predicted piezomagnetic loops under static magnetic field. The model succeeds to reproduce the effect of the external magnetic field on the piezomagnetic behavior. Some peculiar experimental behaviors such as the change of the sign of the $dM/d\sigma|_H$ slope and the

decreasing of the dissipation are well rendered by the model. The contribution of martensite does not seem to be missing here. The amplitude of the modeled low-field cycle is even greater than the amplitude observed during the experiment.

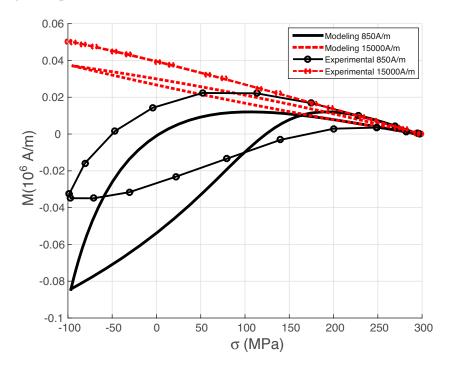


Figure 12 – piezomagnetic behavior measured and calculated by the model.

6 Conclusion

The subject of this work was the study of the hysteretic and piezomagnetic behavior of a dual-phase steel. An experimental protocol was first presented. Hysteretic and piezomagnetic measurements were then performed under different loading (mechanical and magnetic) conditions. Experimental results are consistent with former results performed with low carbon steels. They highlight the effect of uniaxial stress and the magnetic field level on the magnetization of the material. A multiscale modeling has been used to calculate both the hysteretic and piezomagnetic behavior. Comparisons have been made between the prediction of modeled and measured results. The multiscale model seems able to describe correctly the effect of an applied stress and of an external magnetic field on the magnetization. Improvements are expected by taking the magnetic behavior of martensite phase into account. However, some short-comings of the model are noticed: the magnetic and mechanical stress are considered homogeneous at the RVE scale and the behavior is only seen through the configuration of magnetic domains, neglecting some boundary and interface effects. Applications to the development of novel non destructive testing procedures is foreseen.

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