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Energy release rate of the fiber/matrix interface crack in UD composites under transverse loading: effect of the fiber volume fraction and of the distance to the free surface and to non-adjacent debonds

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Abstract

The effects of crack shielding, finite thickness of the composite and fiber content on fiber/matrix debond growth in thin unidirectional composites are investigated analyzing Representative Volume Elements (RVEs) of different ordered microstructures. Debond growth is characterized by estimation of the Energy Release Rates (ERRs) in Mode I and Mode II using the Virtual Crack Closure Technique (VCCT) and the J-integral. It is found that increasing fiber content, a larger distance between debonds in the loading direction and the presence of a free surface close to the debond have all a strong enhancing effect on the ERR. The presence of fully bonded fibers in the composite thickness direction has instead a constraining effect, and it is shown to be very localized. An explanation of these observations is proposed based on mechanical considerations.

Keywords: Polymer-matrix Composites (PMCs), Thin-ply, Energy Release Rate, Debonding, Finite Element Analysis (FEA)

1. Introduction

Stimulated by the ever more stringent requirements in terms of weight and mechanical performances of the aerospace industry, in recent years the com-

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posite community has returned its attention to the mechanisms of intralam-
5 inar crack initiation with a focus on thin-ply laminates. Alternative design
approaches are now considered based on this non-conventional laminate in ap-
plications ranging from cryogenic pressure vessels [1], to airplanes' wings [2],
and even reusable space launchers [3].

Thin-ply laminates are the result of a technological innovation, the *spread tow*
10 *technology*, which consists in opening or spreading the tows, in which fibers
(carbon, glass, aramid, basalt among others) are usually shipped in, into very
thin tapes used for laminate production. Ply thicknesses of less than 50 μm
can nowadays be mass-produced, and record thicknesses of around 20 – 25 μm ,
or $\sim 4 - 5$ times the average fiber's diameter, have been achieved. In its cur-
15 rent form the technique, sometimes referred to as "FUKUI method", was firstly
proposed towards the end of the 1990s [4] and perfected in the subsequent
decade [5, 6].

Several experimental investigations on *thin ply* laminates have highlighted their
main properties [7, 8, 9, 10, 11, 12, 13]: increased fiber content; more uniform
20 packing of fibers; delay and even suppression of intralaminar cracking (called
also transverse-, matrix- or micro-cracking) and delamination. A very insight-
ful work documenting how these phenomena are affected by the morphology of
thin-ply laminates is the microscopic study of Saito & al. [14], which focuses on
the effect of ply thickness on the onset and propagation of intralaminar crack-
25 ing. In their investigation, tensile tests were performed on carbon fiber/epoxy
[0₂, 90_n, 0₂] *thin-ply* laminates for $n = 1, 2, 4$ and the crack density was mea-
sured with a digital microscope at several levels of applied tensile strain in the
range between 0% and 1.5%. Furthermore, they performed microscopic obser-
vations on the specimen's edge at each level of strain. They observed the onset
30 of fiber/matrix interface cracks (referred to as debonds in the following) at lower
levels of strain in thinner plies, while at the same time coalescence of debonds
and through-the-thickness propagation of transverse cracks in thin plies were
delayed and even suppressed as ply thickness decreased. In particular, they
reported the first onset of debonds at 0.4% for $n = 1, 2$ and 0.7% for $n = 4$. For

35 $n = 1$, however, at $\varepsilon = 1.5\%$ coalescence of debonds had started to take place but the crack had not completely propagated through the thickness, while for $n = 2$ and $n = 4$ the latter already happened at a value of strain respectively of 1.3% and 1%. Our inability to explain these observations with the currently accumulated knowledge demonstrates the necessity of further investigation of
40 interactions between debonds and studies of the constraining (or accelerating) effect of presence of bonded fibers, free and constrained boundaries in the vicinity of a partially debonded fiber.

Early studies on the effect of ply thickness on the onset and propagation of transverse cracks were conducted on glass fiber/epoxy cross-ply laminates by
45 Bailey, Parvizi and collaborators [15, 16, 17], who firstly observed the beneficial effect of thickness reduction on the delay of transverse cracking. They furthermore pointed the attention to the appearance of debonds at the fiber/matrix interface and their subsequent coalescence as the mechanism at the origin of transverse cracks [18]. Moreover, they identified the main mechanical driver of
50 the damage process in the mismatch of elastic properties, and particularly of Poisson's ratios, between fibers and matrix [19]. A full understanding of damage onset and propagation in *thin-ply* laminates thus requires comprehension of the mechanisms governing its very first stage, i.e. the fiber/matrix interface crack. First results were obtained through analytical models in the case of a
55 single fiber with an arc crack (debond) in an infinite matrix under transverse tension by England [20] and Perlman & Sih [21], who obtained the stresses at the interface and calculated the stress intensity factors at the crack tip, and by Toya [22], who evaluated the Energy Release Rate (ERR). Drawing upon the results for the straight bi-material interface crack by Comninou [23], the ef-
60 fect of crack face contact in fiber-matrix debonding was investigated in [24, 25]. In [26], it was showed in terms of ERR why the case of a single asymmetric debond is more likely to be observed under remote transverse tension than two symmetric debonds on the same fiber. The effect of different types and combinations of loads on debonding have been studied for the single fiber model:
65 compression [27], residual thermal stresses [28], and biaxial configurations with

different combinations of tension and compression [29, 30]. The effect of the presence of nearby bonded fibers on the debonding of a fiber embedded in an infinite matrix has been studied under uniaxial transverse tension [31], biaxial tension [32] and uniaxial transverse compression [33]. The effect of inter-fiber distance on debond growth has been studied for a partially debonded fiber at the center of a hexagonal cluster inside a homogenized UD composite in the case of fully bonded neighbouring fibers [34] and of two partially debonded fibers out of the surrounding six [35]. An understanding of crack shielding and finite ply thickness effects on debond growth in non-homogenized microstructural models of UD composites seems thus to be lacking: this is the problem that we want to address in the present work. Mode I and Mode II energy release rates will be analyzed using stress fields calculated with the FEM for a variety of Repeating Unit Cell (RUC) of the composite with square packing of fibers under transverse tensile loading. The choice of a square packing configuration for the fibers is motivated by its simplicity, as it allows to easily separate the effect of fibers (fully bonded and/or partially debonded) placed along the loading direction from that of fibers placed in the through-the-ply-thickness direction. These RUCs represent composites with different distances between partially debonded fibers and a varying number of bonded fibers between them, which allows to study the effect of crack shielding on the ERR. In the ply thickness direction, the varying number of perfectly bonded fiber rows exposes the effect of the proximity of the free boundary of the composite on debond growth. Finally, using coupling of thickness direction displacements on horizontal boundaries of the RUC, the accelerating effect of the interaction between debonds of fibers located on the same vertical line is studied.

2. RVE models & FE discretization

2.1. Introduction & Nomenclature

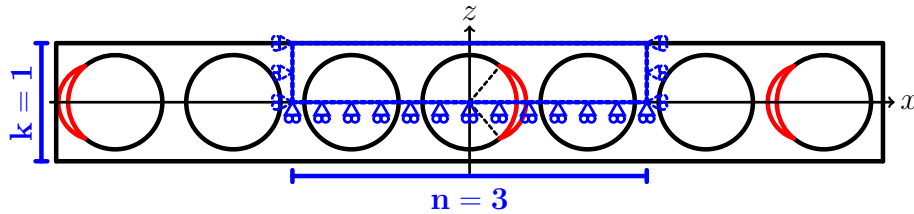
In this paper, we analyze debond development in unidirectional (UD) composites subjected to in-plane transverse tensile loading. The interaction between

95 debonds in UD composites is studied developing models of different Repeating
 Unit Cells (RUC) of laminates (see Fig. 1 to Fig. 3) where only the central
 fiber in the cell has a damage in the form of a fiber/matrix interface crack
 (debond). The composite RUC may be repeating in the in-plane transverse
 direction only (representing an ultra-thin composite) or repeating also in the
 100 composite thickness direction, representing an infinite composite in a limiting
 case. Thus, the conditions at the UD composite's upper and lower bound-
 aries are one of the parameters for the investigation. The used RUCs allow
 for considering the composite with debonds as a sequence of stacked damaged
 and undamaged fiber rows, each row with only one fiber in the thickness direc-
 105 tion. Since all of these RUCs feature regular microstructures with fibers placed
 according to a square-packing configuration, they are Representative Volume
 Elements (RVE) of composites with a certain distribution of debonds. Intro-
 ducing in-plane coordinates x and y , where x is in the transverse direction of
 the UD composite under consideration, the strain in the y -direction due to a
 110 load in the x -direction is small, caused in turn by the very small minor Pois-
 son's ratio of the UD composite. Additionally, debonds are considered to be
 significantly longer in the fiber direction than in the arc direction. Therefore,
 we use 2D models under the assumption of plane strain, defined in the $x - z$
 section of the composite. Thus, the analysis presented applies to long debonds,
 115 with a focus on understanding the mechanisms of growth along their arc di-
 rection. The composites are subjected to transverse tensile strain, applied as
 a constant displacement in the x -direction along the vertical boundary of the
 RUC as shown in Figures 1 to 4. As the models are differentiated by the num-
 ber of rows of fibers and by the spacing between debonds along the vertical and
 120 horizontal directions, the corresponding RUCs can be distinguished from each
 other based on the number n of fibers in the horizontal direction and k in the
 vertical direction. Furthermore, the horizontal surfaces can be either free or
 vertical displacement coupling can be applied. We thus introduce a common
 notation $n \times k - free$ and $n \times k - coupling$ to denote a RUC with $n \times k$ fibers
 125 and, respectively, a free upper surface or with kinematic coupling applied to it.

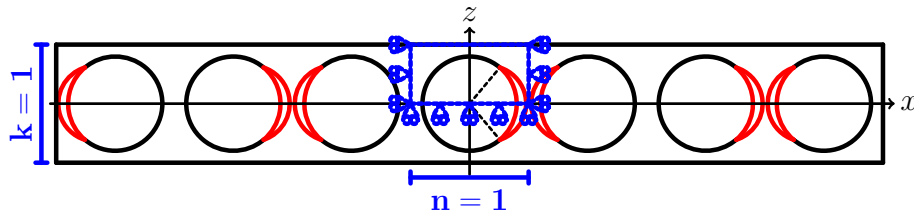
The specific combinations of particular choices of n , k , and boundary conditions are detailed in Section 2.2, together with the description of the corresponding models of damaged composite they are representing.

2.2. Models of Representative Volume Element (RVE)

130 The first two models feature, as shown in Fig. 1, an ultra-thin UD lamina
 with only one row of fibers across its thickness, $k = 1$. This is quite an
 extreme model from the microstructural point of view; however, it allows to
 focus the analysis on the interaction between debonded fibers placed along the
 x-direction. Furthermore, as the horizontal surfaces are considered free, the in-
 135 teraction is stronger in this case than in any other, making the trends very clear
 and the predictions of this model rather conservative. In retrospective, if only
 20 years ago such a model would have been considered too abstracted from the
 physical reality, the recent advancements in the spread tow technology make
 this approach appealing also as a limiting case for practical considerations.



(a) Single row of fibers with a debond appearing every n fibers: model $n \times 1 - free$ ($n = 3$ in the figure).



(b) Single row of fibers with debonds appearing on each fiber: model $1 \times 1 - free$.

Figure 1: Models of ultra-thin UD composites with a single “row” of fibers and debonds repeating at different distances.

140 In the sub-model of Fig. 1a, every n^{th} fiber in the composite is partially debonded on alternating sides of the fiber. The symmetries of the model allow the use of the upper part of the RUC, as highlighted in Fig. 1 to 3. Following the notation introduced in Section 2.1, we will refer to this model as $n \times 1 - free$. In the sub-model $n = 1$, Fig. 1b, a debond appears on each fiber on alternating
 145 sides and the corresponding RUC contains only one fiber. We will refer to this model as $1 \times 1 - free$.

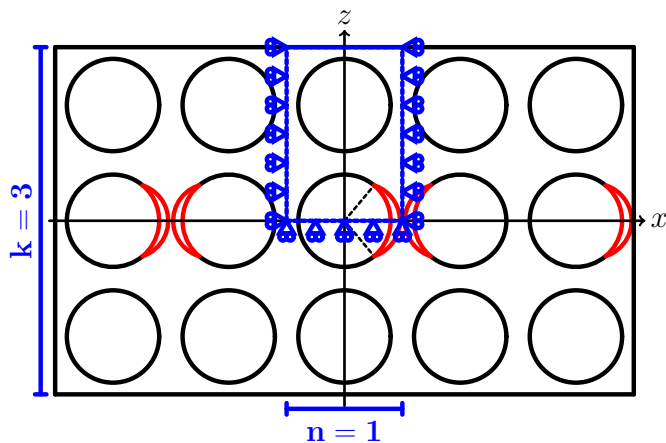
The second set of models in Fig. 2 and Fig. 3 considers laminates with multiple rows of fibers across the thickness: a finite number of rows in the first two sub-models in Fig. 2; an infinite number in the model of Fig. 3. In Fig. 2a,
 150 the RUC contains $n = 1$ fiber in the x-direction, k fibers across the thickness and the central fiber is debonded. This model will be referred to in the following as $1 \times k - free$. Thinking in terms of rows, in this model we have a central row where each fiber is debonded. This row is surrounded from each side by $(k-1)/2$ rows with perfectly bonded fibers. In the sub-model in Fig. 2b, each n^{th} fiber
 155 in the central row is debonded and this row is surrounded by $(k-1)/2$ rows of undamaged fibers from each side. We will refer to this model as $n \times k - free$ (because the horizontal boundary of the RUC is free of any constraint).

Finally, the model in Fig. 3 represents an UD composite with an infinite number of rows; all of them with partially debonded fibers. As all fibers have
 160 debonds, the corresponding RUC is made of a single partially debonded fiber with kinematic coupling conditions applied to the upper boundary to assure periodicity. This model is referred to as $1 \times 1 - coupling$.

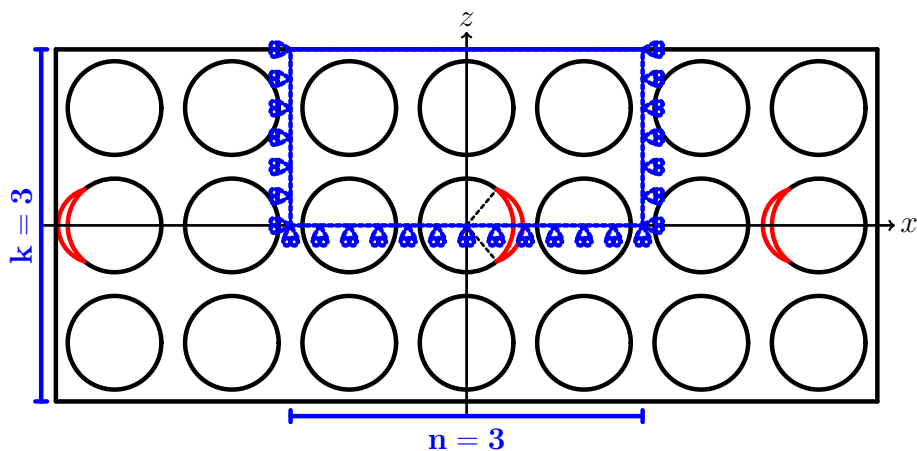
2.3. Finite Element (FE) discretization

Each RUC is discretized using the Finite Element Method (FEM) within
 165 the Abaqus environment, a commercial FEM package [36]. The length l and height h of the model are determined by the number of fibers n in the horizontal direction and k across the thickness (see 2.2) according to Eq. 1:

$$l = 2nL \quad h = kL; \quad (1)$$



(a) Multiple rows of fibers with debonds appearing on each fiber belonging to the central row: model $1 \times k - free$ ($k = 3$ in the figure).



(b) Multiple rows of fibers with a debond appearing every n fibers within the central row: model $n \times k - free$ ($n = 3$ and $k = 3$ in the figure).

Figure 2: Models of UD composites with different “rows” of fibers and debonds repeating at different distances.

where $2L$ is the length of a one-fiber unit, see Fig. 4, defined as a function of the fiber volume fraction V_f and the fiber radius according to

$$L = \frac{R_f}{2} \sqrt{\frac{\pi}{V_f}}. \quad (2)$$

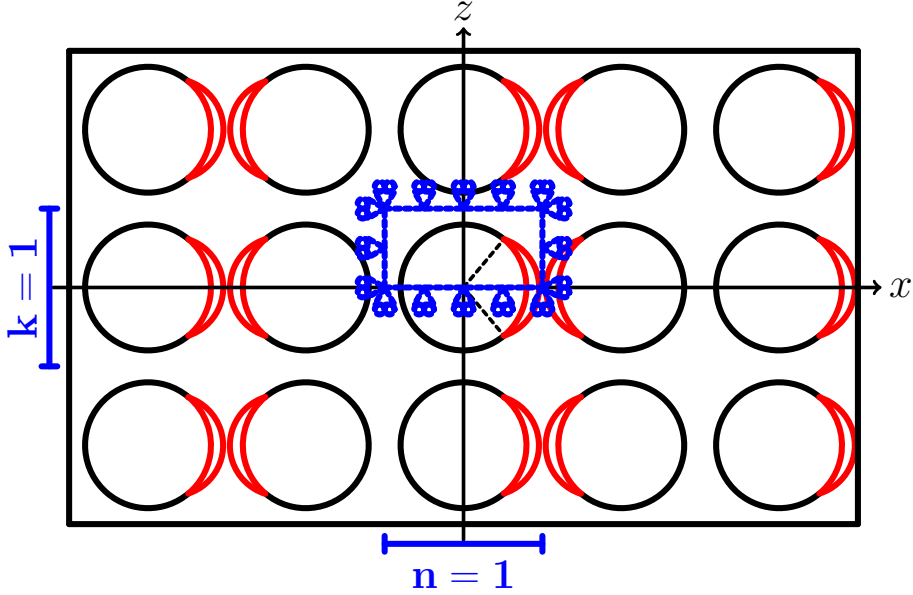


Figure 3: Model of UD composites with an infinite number of “rows” of fibers and debonds appearing on each fiber: model 1×1 – coupling .

170 The fiber radius R_f is assumed to be the same for each fiber in the model and equal to $1 \mu m$. The latter value is not physical and it has been chosen for simplicity. It is worth to note at this point that, in a linear elastic solution as the one presented here, the ERR is proportional to the geometrical dimensions and recalculation of the ERR for fibers of any size, thus, requires a simple
 175 multiplication. Furthermore, notice that the relationships in Eqs. 1 and 2 ensure that the local and global V_f are everywhere equal.

The debond is placed symmetrically with respect to the x axis (see Fig. 4) and we characterize it with an angular size of $\Delta\theta$ (the full debond size is thus $2\Delta\theta$). For large debond sizes ($\geq 60^\circ - 80^\circ$), a region of variable size $\Delta\Phi$ appears
 180 at the crack tip in which the crack faces are in contact and slide on each other. Due to its appearance, frictionless contact is considered between the two crack faces to allow free sliding and avoid interpenetration. The presence of friction at the interface is considered in [37], where the authors model the contact interaction between crack faces using Coulomb’s friction with a coefficient $\mu = 0.25$

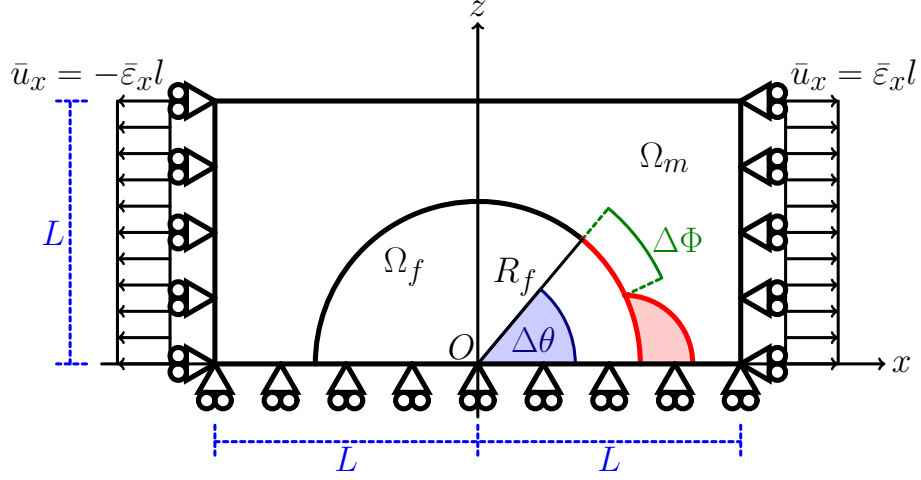


Figure 4: Schematic of the model with its main parameters.

185 and show that, for a debond with $\Delta\theta = 80^\circ$, the crack sliding displacement is
 always different from zero in every point of the crack and only slightly lower
 than that of the frictionless case. This in turn means that the estimation of G_{II}
 in the case of frictionless contact provide an upper bound and thus the results
 presented here represent a conservative estimation (a higher ERR corresponds
 190 to higher likelihood of crack propagation). Symmetry with respect to the x
 axis is applied on the lower boundary. The upper boundary is in general free,
 except for the model 1×1 – *coupling* (Fig. 3) which requires kinematic coupling
 of vertical displacements also on the upper side. Kinematic coupling on the
 x -displacement is applied along the left and right sides of the model in the form
 195 of a constant x -displacement $\pm\bar{\varepsilon}_x l$, corresponding to transverse strain $\bar{\varepsilon}_x$ equal
 to 1%.

Table 1: Summary of the mechanical properties of fiber and matrix. E stands for Young's modulus, μ for shear modulus and ν for Poisson's ratio.

Material	E [GPa]	μ [GPa]	ν [-]
Glass fiber	70.0	29.2	0.2
Epoxy	3.5	1.25	0.4

The model is meshed using second order, 2D, plane strain triangular (CPE6) and rectangular (CPE8) elements, which have respectively 6 and 8 nodes per element. Each node has 2 degrees of freedom, i.e. the horizontal displacement u_x and the vertical displacement u_z . A regular mesh of quadrilateral elements with an almost unitary aspect ratio is required at the crack tip. The angular size δ of an element in the crack tip region is always equal to 0.05° . The overall number of elements needed to discretize the model depends on the debond size $\Delta\theta$ (larger debonds have larger contact zones which require more elements for their correct resolution), the fiber volume fraction (which determines the size of the RVE) and the number of fully bonded fibers present in the model. As an example, the discretization of the 1×1 - *free* model at $V_f = 60\%$ requires a total of 132507 elements for $\Delta\theta = 10^\circ$ and of 296606 elements for $\Delta\theta = 140^\circ$, which corresponds to a minimum required RAM respectively of 445 MB and 1014 MB and to a minimum RAM needed to minimize I/O operations respectively of 1.63 GB and 3.87 GB. To put it into perspective, the wallclock time required for their solution is respectively 1.3 [min] and 14.95 [min] on a laptop with a 2.5 GHz Intel Core i5 processor and 6 GB of installed RAM. The crack faces are modeled as element-based surfaces and a small-sliding contact pair interaction with no friction is established between them. The Mode I, Mode II and total Energy Release Rates (ERRs) (respectively referred to as G_I , G_{II} and G_{TOT}) represent the main output of the FEM analysis; they are evaluated using the VCCT [38] implemented in a custom Python routine and, for the total ERR, the J-integral [39] is obtained by application of the Abaqus built-in functionality. A glass fiber-epoxy system is considered throughout this paper, and it is assumed that their response lies always in the linear elastic domain. The latter assumption lies on the work of Asp and co-workers, who show that epoxy subjected to a tri-axial stress state as the one observable in the inter-fibers region fails at very low strains ($\sim 0.5\% - 0.8\%$) [40] and in a brittle manner [41], and that the magnitude of deviatoric stresses (evaluated in terms of equivalent Von Mises stress) in the fiber/matrix interface neighborhood does not justify the occurrence of plastic deformations in the case of debond propagation [41].

The properties used are listed in Table 1.

2.4. Validation of the model

230 The model is validated in Fig. 5 against the results reported in [42, 31], obtained with the Boundary Element Method (BEM) for a single fiber with a symmetric debond placed in an infinite matrix. This situation is modeled using the 1×1 - *free* RVE with $V_f = 0.0079\%$, which corresponds to a RUC's length and height of respectively $\sim 200R_f$ and $\sim 100R_f$.

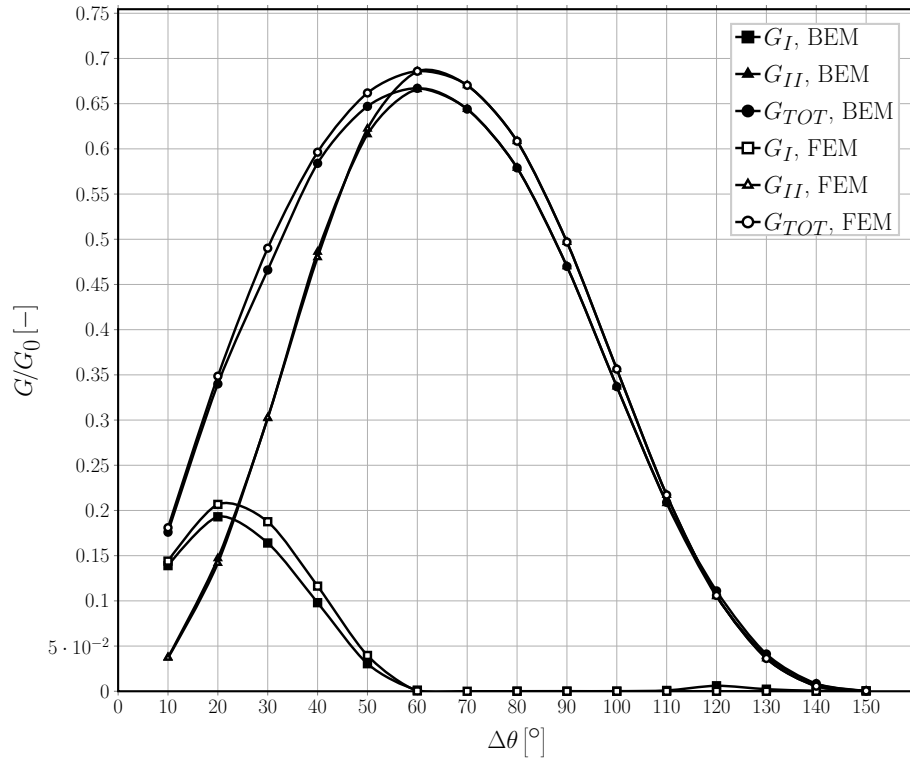


Figure 5: Validation of the single fiber model for the infinite matrix case with respect to the BEM solution in [31].

235 To allow for a comparison, the results are normalized following [31] with respect to a reference Energy Release Rate G_0 defined as

$$G_0 = \frac{1 + k_m}{8\mu_m} \sigma_0^2 \pi R_f \quad (3)$$

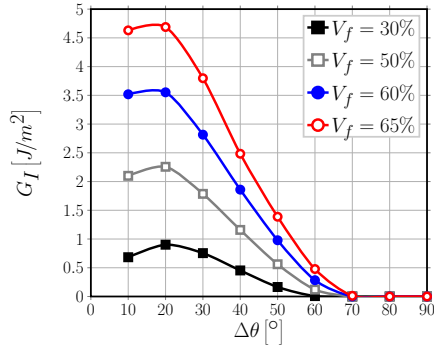
where μ is the shear modulus, k is the Kolosov's constant defined as $3 - 4\nu$ for plane strain conditions, R_f is the fiber radius and the index m refers to the properties of the matrix. σ_0 is the stress at the boundary, computed as the average of the stress extracted at each boundary node along the right side (arithmetic average as nodes are equispaced by design along both the left and right sides). The agreement is good: the difference between the BEM solution, which is considered more accurate, and the FEM solution does not exceed 5%. The ERRs' maxima are in the same positions and the size of the contact zone is the same. Nevertheless, an analysis of phenomena leading to less than 5% differences in ERR would not be reliable and, therefore, it is not recommended.

3. Results & Discussion

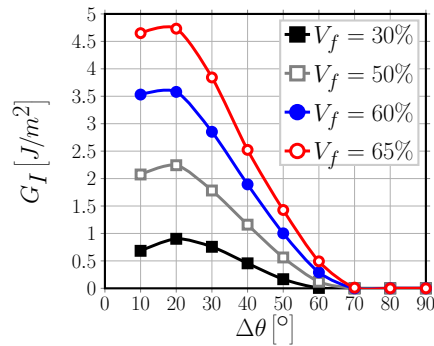
3.1. Effect of Fiber Volume Fraction

As shown in Figs. 6 and 7, respectively for Mode I and Mode II, the fiber content has a drastic effect on the Energy Release Rate at the tip of the fiber/matrix interface crack. The effect of four levels of fiber volume fraction are compared, 30%, 50%, 60% and 65%, on two microstructural models: a 11×11 - *free* (every 11th fiber in the central fiber row is partially debonded and, on the top of this row, we have 5 undamaged fiber rows), Figs. 6a and 7a, and a 21×21 - *free* (every 21th fiber in the central fiber row is partially debonded and, on the top of this row, we have 10 undamaged fiber rows), Figs. 6b and 7b.

Comparing Fig. 6a with 6b, and Fig. 7a with 7b, we can observe that the ERRs' values are very similar for RUCs with 11×11 and 21×21 fibers, though they are slightly higher for the larger RUC where the next debonded fiber and the free surface are further away from the debonded fiber. From these results we conclude that both RUCs are large enough to represent a single debonded fiber in an infinite array of bonded fibers. Obviously, there exists a specific effect of the fiber content. For Mode I, Fig. 6, the maximum value of the ERR increases by ~ 5.2 times when V_f changes from 30% to 65%. The debond's angular size for which the peak value occurs remains unchanged at 20° , but for $V_f = 60\%$



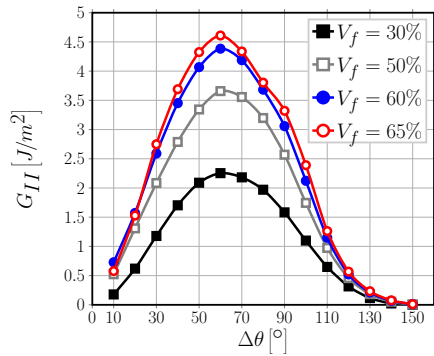
(a) Model 11×11 – *free*.



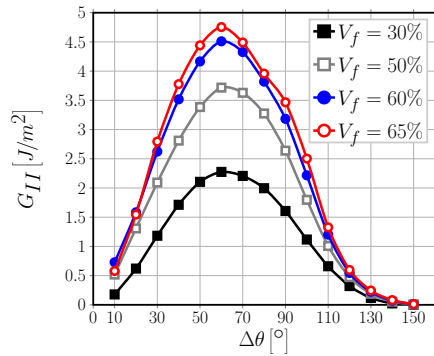
(b) Model 21×21 – *free*.

Figure 6: A view of the effect of fiber volume fraction on Mode I ERR in two exemplificative models, subject to an applied transverse strain ε_x of 1%.

and 65% the values of Mode I ERR are rather similar when measured at 10° and at 20° , approximately creating a plateau. Furthermore, increasing the fiber volume fraction delays the onset of the contact zone, which corresponds in Fig. 6 to the first value of $\Delta\theta$ for which G_I is equal to zero. For $V_f = 30\%$, the contact zone first appears for a debond of 60° , similarly to what happens in the single fiber in infinite matrix model (Fig. 5). For higher fiber contents, the contact zone's onset is delayed to a debond's size approximately equal to 70° .



(a) Model 11×11 – *free*.



(b) Model 21×21 – *free*.

Figure 7: A view of the effect of fiber volume fraction on Mode II ERR in two exemplificative models, subject to an applied transverse strain ε_x of 1%.

For Mode II, Fig. 7, there is a distinct maximum in the curve and its shape does not depend on the fiber content. The maximum value of the ERR increases
275 by ~ 2.1 times when V_f changes from 30% to 65%. The effect is thus similar to Mode I, but with a significantly lower magnitude. Similar to Mode I, the debond's size for which the peak value of Mode II occurs remains unchanged, at 60° . It is worthwhile to notice that the ratio of Mode II to Mode I peak values is $\frac{\max(G_{II})}{\max(G_I)} \sim \frac{2.2}{0.9} \sim 2.4$ for $V_f = 30\%$, while it is $\sim \frac{4.7}{4.7} \sim 1$ for $V_f = 65\%$.

280 The general increasing trends observed in Figs. 6 and 7 are related to the fact that, given that the global and local V_f are everywhere identical in the models presented, an increase in fiber content corresponds to a decrease in the average distance between fibers. Thus, the distances for the decay of the local stress and strain fields in the matrix domain become shorter, leading to higher stresses in
285 general and causing higher values at the crack tip. The difference in relative magnitude between Mode I and Mode II and the delay in the contact zone's onset are instead due to the interplay between two different mechanisms, both caused by the ordered microstructural arrangement of the model. In the models considered, a fully bonded fiber is always placed along the horizontal direction,
290 aligned with the partially debonded fiber and exactly in front of the debond. By increasing V_f , the former moves closer to the latter and for small debonds this causes a magnification of the x -strain at the crack tip. For small debonds ($\leq 20^\circ - 30^\circ$) in fact, the crack tip is approximately normal to the x -direction and thus an increase in ε_x causes an increase in G_I . On the other hand, for large
295 debonds ($\geq 70^\circ - 80^\circ$) the crack growth direction is almost aligned with the x -axis, thus a magnification in the x -strain translates into an increase of Mode II ERR. However, this increasing effect on G_{II} is partially counteracted by the presence of a fully bonded fiber on top of the debonded fiber and aligned with it. As fibers are more rigid than the surrounding matrix, the presence of the former
300 will restrain horizontal displacements, thus hampering strong increases in G_{II} for large debonds. Furthermore, due to the mismatch in the Poisson's ratios, the fully bonded fiber placed above generates an upward-directed component of the vertical displacement field in the matrix, which tends to open the debond

and causes the delay in the contact zone’s onset. The interplay between these
305 mechanisms is governed by the average inter-fiber distance and, in turn, by the
fiber volume fraction.

These observations are in agreement with the results reported in [31], where
the effect on the ERR of a partially debonded fiber of two fully bonded nearby
fibers, placed symmetrically with respect to the loading direction, is studied for
310 different angular positions (denoted as θ_2) and radial distances in a model with
an effectively infinite matrix ($V_f \sim 0.09\%$). The effect of the former is studied
for a constant value of the radial distance between the debonded and bonded
fibers, which corresponds to a local V_f^{local} of $\sim 62\%$ assuming hexagonal pack-
ing. They report an increase in both Mode I and Mode II ERR with respect to
315 the single fiber case when the two fibers are placed at an angle of respectively
 $\pm 25^\circ, \pm 30^\circ, \pm 140^\circ, \pm 150^\circ, \pm 155^\circ$, i.e. closest to the loading direction. Notice
that for $\pm 25^\circ$ and $\pm 155^\circ$ the two fully bonded fibers are almost in contact, with
an inter-fiber distance of ~ 0.04 times their radius. This result confirms the
considerations made in the previous paragraph about the x -strain magnifica-
320 tion caused by the presence of fully bonded fibers along the loading direction.
The effect is further analyzed and discussed in Sec. 3.2 and Sec. 3.4. In the
range $\pm 40^\circ - \pm 130^\circ$ instead, the presence of the other fibers causes a reduction
of the ERR and, particularly in the range $80^\circ - 120^\circ$, results are very close and
almost insensitive to variations in θ_2 , which supports the previous conclusion
325 about the effect of a fully bonded fiber on top the partially debonded one. This
effect is treated in more detail in Sec. 3.3.

Comparing the results from [31] with those presented in this paper, an hypoth-
esis can be furthermore formulated about the robustness of the results of the
present article with respect to deviations in fiber position: it seems reasonable
330 to assume a tolerance to deviations of max. $\pm 30^\circ$ with respect to the loading
direction and of max. $\pm 20^\circ$ with respect to the through-the-thickness direction.
The effect of the local fiber content is also investigated in [31], by changing
the radial distance between the partially debonded fiber and the fully bonded
ones. They observe that the further the fully bonded fibers are placed from the

335 central one, i.e. the lower the local V_f , the lower is their effect on the ERR.
 The magnitude of the effect is however small: the maximum increase of the
 total ERR is of ~ 1.15 times for $\theta_2 = 30^\circ$ and 150° when increasing V_f^{local}
 from 28% to 62%; the total ERR decreases by a factor of ~ 0.62 for $\theta_2 = 60^\circ$,
 ~ 0.74 for $\theta_2 = 90^\circ$ and ~ 0.5 for $\theta_2 = 120^\circ$ when increasing V_f^{local} from 28%
 340 to 62%. Analogous results can be found in [34], where the authors consider
 a centrally-placed partially debonded fiber surrounded by an hexagonal cluster
 inside an homogenized UD composite. They observe a reduction in the ERR
 when the local fiber volume fraction is increased, i.e. when the spacing between
 fibers is reduced. The strongest change is reported for Mode II, which decreases
 345 by a factor of ~ 0.73 when the local fiber volume fraction is decreased from
 66% to 78%. Thus, the trends presented in [31, 34] are in agreement with our
 results on the effect of V_f and support the considerations made so far. The
 stark difference in magnitude however highlights the contrast between the ef-
 fect of the local fiber volume fraction of a cluster of fibers inside an infinite
 350 medium and of the global V_f of long-range microstructural arrangements, such
 the ones considered in this article. The similarity in trends with the concurrent
 difference in magnitudes can be explained in relation to the characteristics of
 the elastic solution computed. In the first case the local fiber volume fraction
 controls the distance, with respect to the central partially debonded fiber, at
 355 which a localized perturbation zone appears in the far-field elastic solution; in
 the second case the global V_f determines the characteristic lengths of a global
 periodic solution.

3.2. Interaction between debonds in UD composites with a single row of fibers

The interaction of debonds appearing at regular intervals in an ultra-thin
 360 UD composite with a single row of fibers is studied for Mode I (Fig. 8) and Mode
 II (Fig. 9) and fiber content equal to 30% (Figs. 8a and 9a) and 60% (Figs. 8b
 and 9b). The models treated are $3 \times 1 - free$, $5 \times 1 - free$, $7 \times 1 - free$,
 $11 \times 1 - free$, $21 \times 1 - free$, $101 \times 1 - free$ and $201 \times 1 - free$, corresponding
 respectively to a debond every 3^{rd} , 5^{th} , 7^{th} , 11^{th} , 21^{st} , 101^{st} and 201^{st} fiber

365 (Fig. 1a). Given that the upper surface of the UD row is left free, the interaction
with the debonded fiber in the next RUC is stronger than in any other case and
the results of this section are thus the most conservative in terms of debond's
growth: the ERRs should be the largest. The effect is enhanced in composites
with high V_f and especially for G_{II} : at $V_f = 60\%$ the highest G_{II} value for the
370 $201 \times 1 - free$ composite in Fig. 9b is more than 3 times higher than the G_{II}
value value for the $21 \times 21 - free$ composite in Fig. 7b. Even the maximum is
shifted to larger angles. The G_I value is for some cases only 30% higher.
From both Fig. 8 and Fig. 9, it can be seen that the presence of a debond close
to the analyzed debond decreases the strain magnification effect discussed in
375 Sec. 3.1 and thus reduces the value of the ERR. This phenomenon is called
“crack shielding” [26].

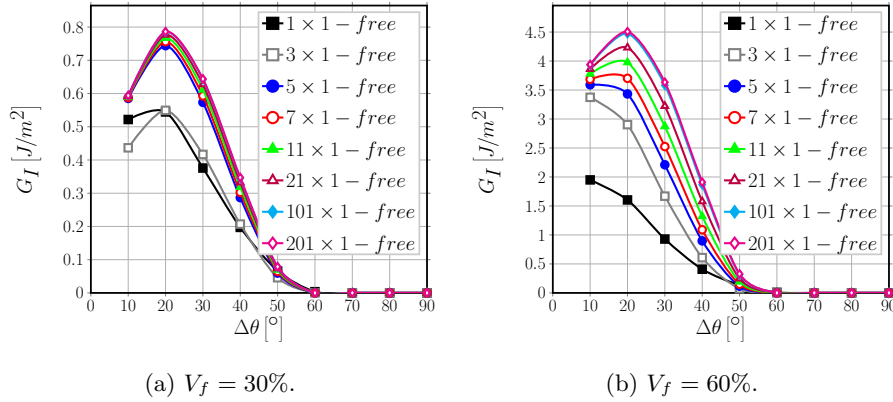


Figure 8: Effect of the interaction between debonds appearing at regular intervals on Mode I ERR in an UD with a single row of fibers at different levels of fiber volume fraction V_f , subject to an applied transverse strain ε_x of 1%.

For Mode I, the presence of a free surface, and inversely the absence of
a fully bonded fiber along the vertical direction, implies the absence of the
counteracting upward-oriented vertical component of the displacement field due
to the mismatch in Poisson's ratios. This in turn translates into the constancy
380 of the value of $\Delta\theta$ corresponding to contact zone's onset, always equal to 60° .
For $V_f = 30\%$, Mode I is reduced when the spacing between debonds (in terms

of number of fully bonded fibers between them in our models) decreases, but the magnitude of change is significant only in the range when the spacing is
 385 reduced from a debond every 5th fiber to one every 3rd. For comparison, the difference of peak G_I values for $V_f = 30\%$ between $5 \times 1 - free$ and $3 \times 1 - free$ is $\sim 0.2 \frac{J}{m^2}$ (around 30% of the lower value), while between $201 \times 1 - free$ and $5 \times 1 - free$ is $\sim 0.05 \frac{J}{m^2}$ (around 7% of the lower value). A similar observation can be made for $V_f = 60\%$, but for larger spacings: no difference can be seen
 390 between the case of a debond placed every 101st and every 201st fiber. These observations suggest the existence of characteristic distance dependent on the fiber volume fraction which governs the interaction between debonds: in low V_f composites ($V_f = 30\%$) the convergence to a non-interactive solution is faster (less interaction between debonded fibers in neighboring RUCs).

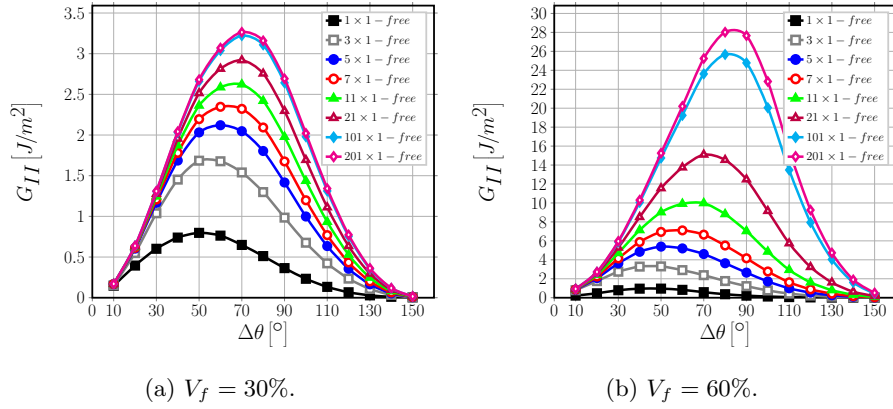


Figure 9: Effect of the interaction between debonds appearing at regular intervals on Mode II ERR in an UD with a single row of fibers at different levels of fiber volume fraction V_f , subject to an applied transverse strain ε_x of 1%.

395 Without constraint on the upper surface, the strain magnification effect creates a larger displacement gap in the x -direction, which increases Mode II for larger debonds. When debonds are far apart, the series of rigid elements in the ultra-thin composite row (constituted by fully bonded fibers and their surrounding matrix) creates higher x -strains than in average in the element with the
 400 debonded fiber, which in turn generates higher tangential displacements at the

crack tip for larger debonds. Conversely, when debonds are closer (smaller number of rigid elements between them), the strain concentration in the debonded element is more similar to the applied strain (the magnification is reduced) and the tangential displacement component at the crack tip decreases for large $\Delta\theta$.

405 This is the mechanism behind the change in the value of $\Delta\theta$ for which the peak of G_{II} occurs: from 70° to 50° at 30%, and from 80° to 40° at 60% going from the higher to the smaller spacing of debonds. Differently from Mode I, the presence of a characteristic distance is harder to establish. For $V_f = 30\%$ (Fig. 9a), it seems reasonable to establish it at around 100 fully bonded fibers

410 between each debond. For $V_f = 60\%$ (Fig. 9b), the difference between models $101 \times 1 - free$ and $201 \times 1 - free$ is still sizable, thus preventing the establishment of such characteristic distance. It is possible to observe, however, that the change between $101 \times 1 - free$ and $201 \times 1 - free$ is significantly smaller than between $21 \times 1 - free$ and $101 \times 1 - free$ ($2 \left[\frac{J}{m^2}\right]$ vs $11 \left[\frac{J}{m^2}\right]$), thus suggesting the existence of the characteristic distance outside the range studied.

415 Nevertheless, one should question whether the single row composite with free surface is an appropriate RUC for defining the upper bound for G_{II} : G_{II} may be more affected by the free surface than by the effect of the interaction between debonds in the row.

420 3.3. Influence of rows of fully bonded fibers on debond's ERR in the middle row

The effect of the presence of rows of fully bonded fibers on debond's growth in the central row with all fibers partially debonded is studied for Mode I (Fig. 10) and Mode II (Fig. 11) and fiber content equal to 30% (Figs. 10a and 11a) and 60% (Figs. 10b and 11b). The models treated are $1 \times 3 - free$, $1 \times 5 - free$,

425 $1 \times 7 - free$, $1 \times 11 - free$, $1 \times 21 - free$, $1 \times 101 - free$ and $1 \times 201 - free$, corresponding to a UD composite with respectively 3, 5, 7, 11, 21, 101 and 201 rows of fibers (Fig. 2a).

The results shown strengthen the arguments made in Sec. 3.1 and Sec. 3.2. It can, in fact, be seen in Fig. 10 that an increasing number of bonded fiber rows

430 across the thickness delays the onset of the contact zone to a debond of 70° in

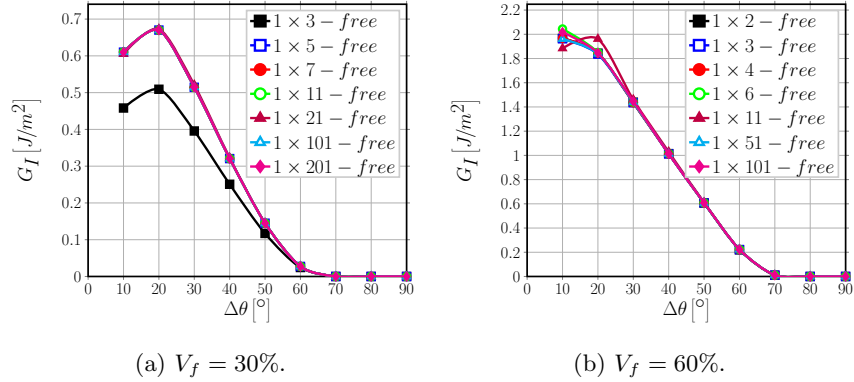


Figure 10: Influence of rows of fully bonded fibers on debond's growth in Mode I ERR in a centrally located row of debonded fibers at different levels of fiber volume fraction V_f , subject to an applied transverse strain ε_x of 1%.

size, due to the introduction of an additional positive component of the vertical displacement which translates into an opening displacement at the debond's tip. Comparing Fig. 9b with Fig. 11b, we observe that the presence of bonded fiber rows significantly reduce the G_{II} and its maximum is shifted back to 60° , thus
435 confirming the hypothesis in Section 3.2 that the absence of G_{II} convergence with the increasing distance in a single-row composite is caused more by the free surface than by the interaction between debonds.

The results of both Mode I and Mode II show that the introduction of an increasing number of fully bonded fiber rows doesn't change the ERR calculated
440 at the crack tip after adding more than one row (the convergence is very fast). A small effect, mostly on Mode I, of the number of bonded fiber rows can be observed at low fiber content (Figs. 10a and 11a), while for high fiber content the smaller model with only one fiber row above the partially debonded one is already representative.

445 3.4. Effect of multiple rows of bonded fibers on debonding in the central row of a UD composite with different distances between debonded fibers

The ERR of debonds appearing at regular intervals in the central row of fibers in UD composites is affected by the number of rows with bonded fibers.

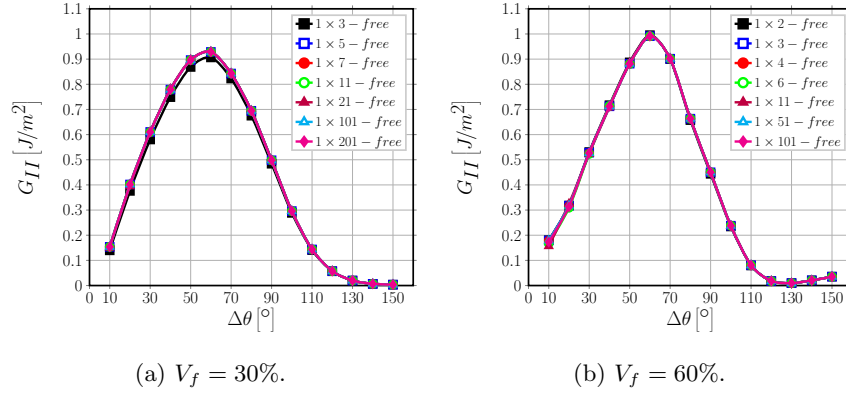
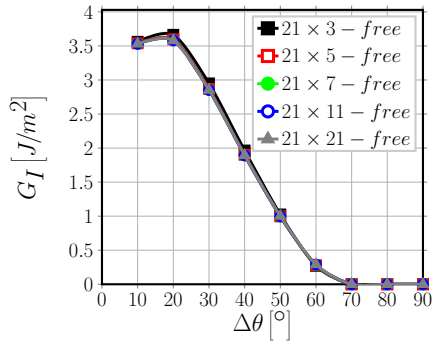


Figure 11: Influence of rows of fully bonded fibers on debond's growth in Mode II ERR in a centrally located row of debonded fibers at different levels of fiber volume fraction V_f , subject to an applied transverse strain ε_x of 1%.

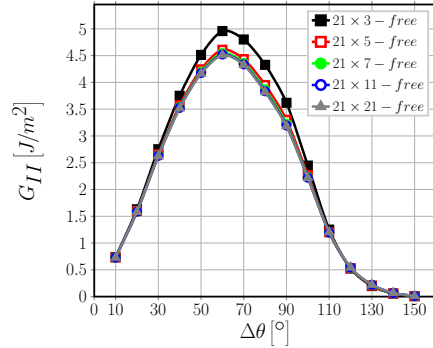
The effect is investigated using different combinations of horizontal debond spacing, controlled by the number of bonded fibers in the central row of the RUC, and the number of rows of bonded fibers on top of it. The following models have been studied: $3 \times 3 - free$, $5 \times 3 - free$, $5 \times 5 - free$, $7 \times 3 - free$, $7 \times 5 - free$, $7 \times 7 - free$, $11 \times 3 - free$, $11 \times 5 - free$, $11 \times 7 - free$, $11 \times 11 - free$, $21 \times 3 - free$, $21 \times 5 - free$, $21 \times 7 - free$, $21 \times 11 - free$, $21 \times 21 - free$, $101 \times 3 - free$, $101 \times 5 - free$, $101 \times 7 - free$, $101 \times 11 - free$, $201 \times 3 - free$, $201 \times 5 - free$, $201 \times 7 - free$, $201 \times 11 - free$ (Fig. 2b).

The results shown in Fig. 12 confirm the observations discussed in Sec. 3.2 and Sec. 3.3: the presence of fully bonded fiber rows on top of the central row with debonded fibers reduces the interaction with the free surface and thus has a restraining effect on the ERR, that counteracts the magnification due to an increasing number of fully bonded fibers in the horizontal direction. The interplay is further modulated by the fiber content. Observing Fig. 12, it is possible to note how the free surface interaction decays fast: the presence of 5 fiber rows across the thickness is already sufficient to prevent any significant effect of additional fiber rows on the ERR of a debond in the central row.

The results in Fig. 13 show instead the effect of increasing the distance

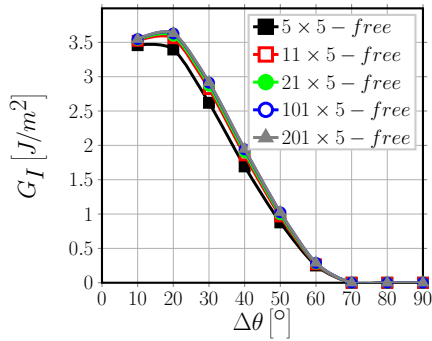


(a) G_I .

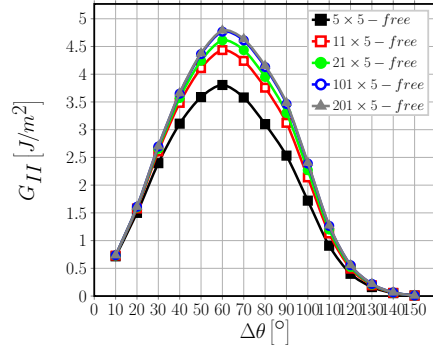


(b) G_{II} .

Figure 12: Effect on Mode I and Mode II ERR of the presence of an increasing number of rows of fully bonded fibers in UD composites with debonds appearing every 10^{th} fiber (model $21 \times k - free$). $V_f = 60\%$ and $\varepsilon_x = 1\%$.



(a) G_I .



(b) G_{II} .

Figure 13: Effect on Mode I and Mode II ERR of increasing the spacing between debonds appearing in the central row of fibers in a UD composite with a fixed number of rows across the thickness. $V_f = 60\%$, $k = 5$ and $\varepsilon_x = 1\%$.

between two consecutive debonds in the central row of a UD composite of given thickness. In agreement with the observations of Section 3.2, increasing the distance between debonds (measured in terms of fully bonded fibers between them) causes an increase in the ERR in both Mode I and Mode II. For both Mode I and Mode II, it is possible to observe the existence of a characteristic distance which defines the limit between the interactive and the non-interactive

solution. Furthermore, comparing Figure 13a and 13b, it is possible to notice that Mode I is less sensitive than Mode II to the horizontal spacing of debonds.

475 *3.5. Comparison with the single fiber model with equivalent boundary conditions*

The single fiber RUC (1×1 -free or 1×1 -coupling) corresponds to the most damaged state of the composite, i.e. the state in which all fibers have debonds. The 1×1 -free model represents an ultra-thin UD composite with a single row of partially debonded fibers. The 1×1 -coupling model, where the displacement
480 coupling is used to enforce periodic boundary conditions, represents an infinite composite.

The comparison of the 1×1 -free model with one row multi-fiber models $n \times 1$ -free in Figure 8 and Figure 9 show that the former provides in general the lowest value of the ERR (the highest crack shielding case).

485 The 1×1 -coupling model is compared with 1×3 -free and 1×201 -free models in Fig. 14. In all three models the distance between debonds in the x -direction is the same and the difference is in the vertical direction. The 1×1 -coupling model describes the interaction between debonds in different rows of debonded fibers whereas the $1 \times k$ -free models describe the effect of the
490 proximity of the composite's free surface. The Mode I ERR in the 1×3 -free and 1×201 -free model is very similar to the 1×1 -coupling model, which leads to a rather surprising conclusion. In both models we have, on the top of the central one, a large amount of fibers (bonded in two cases and debonded in the third case). It appears that the effect of bonded and debonded fibers on the
495 central debond is the same. This implies that, for Mode I ERR, the interaction between debonds in elements placed on top of each other is small.

The same comparison for Mode II shows a sizeable difference in the range $50^\circ - 90^\circ$, while the results almost coincide for smaller values of $\Delta\theta$. The lower values of G_{II} of the 1×1 -coupling model in the range $50^\circ - 90^\circ$ are due to the
500 shielding effect of a debond of the same size in the fiber just above the central one (modeled by the coupling boundary condition), which leaves the strip of matrix between the two fibers free to deform away from both of them due to

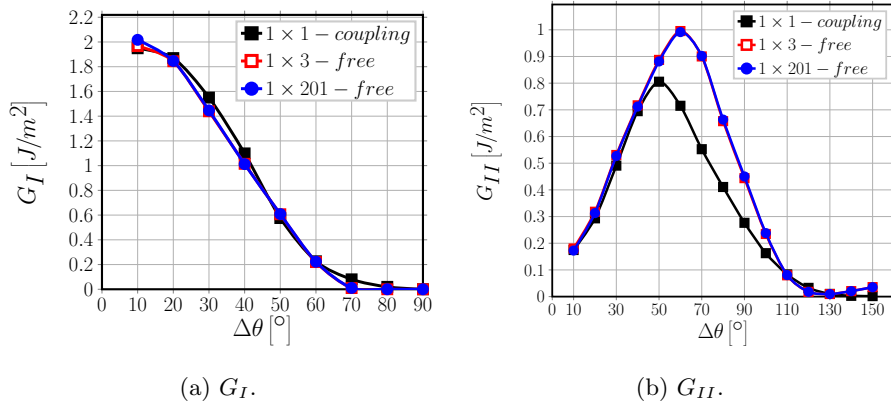


Figure 14: Comparison of the ERR between the single fiber model with coupling conditions along the upper boundary and the $1 \times k$ - free model. $V_f = 60\%$ and $\varepsilon_x = 1\%$.

the Poissons effect and thus favors Mode I and reduces Mode II. This translates into the delay in the appearance of the contact zone, particularly evident in
 505 Fig. 14a.

4. Conclusions & Outlook

Several models of Repeating Unit Cell, representative of different microstructural arrangements of a unidirectional (UD) composite, have been studied in order to investigate the effect on fiber/matrix interface crack growth of the presence of partially debonded and/or fully bonded fibers. Regular microstructures
 510 based on square-packing arrangements of fibers have been loaded in transverse tension, with debonds appearing in the central row of fibers at regular intervals measured in terms of number of fully bonded fibers between them. This central row is embedded in-between a varying number of rows with perfectly bonded
 515 fibers. The surface of the composite is either traction-free or with imposed vertical displacement constraint imitating a periodic structure in the composite thickness direction.

In each RUC, the fiber volume fraction is spatially homogeneous (no fiber clustering is considered) and the fiber distribution is uniform by design, which

520 establishes a direct relationship between fiber content and inter-fiber distance.
The main conclusions of this work are summarized here.

1. With a decreasing number of fully bonded fibers between two partially debonded fibers in the central row, the ERR decreases. It seems to exist a characteristic distance between debonds which defines the transition to a non-interactive solution. However, this distance depends on the number of perfectly bonded fiber rows surrounding the central row and on the fiber volume fraction. This distance can be estimated to be around 100 fully bonded fibers for a 1-fiber-row thick UD with $V_f = 30\%$ and 200 for a 1-fiber-row thick UD with $V_f = 60\%$, while it is expected to be around 100 fibers for a 5-fibers-row thick UD with $V_f = 60\%$.
525
2. The presence of a free surface close to the debond leads to higher Mode I and Mode II ERRs and a shift of the peak G values to larger debonds.
3. The presence of fibers (fully or partially bonded) in the composite thickness direction, along the same vertical line as the analyzed central fiber, appears to have a restraining effect on both G_I and G_{II} . The free composite surface effect on the ERR decays very fast: adding more than 2 fully bonded fibers below and above the central row leads to stable constant values of ERR.
535
4. The presence of a debond in the fiber above the central partially debonded one only delays the appearance of the contact zone, while no significant effect on the ERR has been observed.
540
5. Increasing the fiber content (decreasing the inter-fiber distance), magnifies in general the effects described in the previous points.
6. The results and conclusions presented agree well with previous observations reported in the literature [31, 34]. A mechanical explanation of the observed trends has been presented based on the mismatch in elastic properties, particularly Poisson's ratios, and the positions of fibers and debonds with respect to the loading direction.
545

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